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1	Normal fault growth in continental rifting: insights from changes in displacement and
2	length fault populations due to increasing extension in the central Kenya Rift
3	
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10	Keywords: Scaling properties, Strain accommodation, Fault growth, Rift evolution

11 Highlights

12 • Examination of upper crust brittle deformation during continental rifting from DEM data.

13 • Examination of fractal dimension of power law fit of fault populations with increasing strain.

• Determination of fault growth models from fault population scaling properties.

15 Abstract

This study examines the scaling relationship between fault length and displacement for the purpose of gaining 16 17 a better understanding of the evolution of normal faults within the central Kenya Rift. 620 normal faults were 18 manually mapped from a digital elevation model (DEM), with 30 m² resolution and an estimated maximum displacement of $\sim 40 - \sim 6030$ m and fault lengths of 1270 - 60600 m. To assess the contribution of fault 19 20 populations to the strain accommodation from south to north, the study area has been divided into three zones 21 of fault populations based upon their average fault orientations; zone 1 in the north is dominated by NNE 22 striking faults, zone 2 in the centre of the rift is characterised by NNW to NNE fault trends, whereas zone 3 23 in the south is characterised by NNW striking fault systems. Extensional strain was estimated by summing 24 fault heaves across six transects along the rift, which showed a progressive increase of strain from south to 25 north. The fault length and displacement data in the three zones fit to a power law distribution. The cumulative 26 distributions of fault length populations showed similar fractal dimension (D) in the three zones. The 27 cumulative displacement distributions for the three zones showed a decrease in the Power-law fractal 28 dimension with increasing strain, which implies that the strain is increasingly localised onto larger faults as 29 the fault system becomes more evolved from south to north. Increasing displacement with increasing strain 30 while the fault length remains almost constant may indicate that the fault system could be evolving in 31 accordance with a constant length fault growth model, where faults lengthen quickly and then accrue 32 displacement. Results of this study suggest that the process of progressively increasing fault system maturity

and strain localization onto large faults can be observed even over a relatively small area (240 x 150 km)
within the rift system. It is also suggested that patterns of fault growth can be deduced from the fractal
dimension of cumulative distribution of fault size populations.

36 1 Introduction

Observations of fault size, specifically displacement versus length distributions can be used to help understand
rift development (e.g.Gupta and Scholz, 2000). Moreover, in order to understand the surface deformation of
tectonically active regions, it is critical to understand the evolution of normal faulting associated with rifting
and extensional processes.

41 Quantitative analyses of fault population parameters, such as trace-length, and displacement as well as 42 displacement distributions have been studied in recent decades in many studies (e.g. Cowie and Scholz, 1992a, 43 Dawers et al., 1993, Schultz and Fossen, 2002, Walsh et al., 2002b, Soliva and Schultz, 2008, Torabi and 44 Berg, 2011, Torabi et al., 2019) in order to understand the growth history of fault populations. Such analyses have also been used to suggest a number of fault growth models including fault growth by radial propagation 45 46 (Walsh and Watterson, 1988), a coherent fault model of segment linkage of fault arrays by Cartwright et al. 47 (1995) and an alternative fault growth model suggested by e.g. Walsh et al. (2002a) and Rotevatn et al. (2019), 48 where fault lengths are near constant from an early stage and growth is largely achieved by an increase in 49 fault displacement.

50 Cumulative frequency distribution functions (CDF) are the most common way to describe attributes of fault 51 populations (e.g. length, displacement) and have been used in many studies (e.g. Walsh et al., 1991, Jackson 52 and Sanderson, 1992, Cladouhos and Marrett, 1996, Bonnet et al., 2001). Most populations of fault lengths 53 and displacements have been found to plot along a more or less straight line in log-log space (e.g. fault length 54 vs. cumulative number) which implies a power-law distribution (e.g. Watterson et al., 1996, Ackermann and 55 Schlische, 1997, Poulimenos, 2000, Gillespie et al., 2001, Peacock, 2002, Bailey et al., 2005, Soliva and 56 Schultz, 2008, Torabi et al., 2019). This power-law distribution is described mathematically as:

57

$$N=aS^{-D}$$

58 where S is fault offset (i.e. length, displacement, throw or heave), N is the cumulative number of fault offset,

and a is a constant. D is an exponent, and it describes the fractal dimension of slope of the straight segment

60 (Walsh et al., 1991, Yielding et al., 1996)

It has been demonstrated in several studies that differences in the value of the exponent D (the fractal dimension) are attributed to variations in the amount of strain accommodated by fault systems, and it may also change for different stages of fault evolution (i.e. fault nucleation, propagation and amalgamation) (e.g. (e.g. Cowie et al., 1995, Cowie, 1998a, Ackermann et al., 2001, Bailey et al., 2005). It has also been found

that the fractal dimension is inversely related to the strain, where the former decreases systematically as the latter increases and vice versa (e.g. Cartwright et al., 1995, Poulimenos, 2000, Moriya et al., 2005). Therefore, analysis of the fractal dimension of power law distributions can be used to characterize the spatial distribution of faults (Cowie, 1998a, Sornette et al., 1993). It was also found that high fractal dimensions reflect a greater proportion of small faults relative to larger faults than lower fractal dimensions (Marrett and Allmendinger,

70 1991, Yielding et al., 1996)

71 The aims of this paper are to quantitatively investigate fault scaling relations (fault length and displacement) 72 of three different fault populations for the purpose of providing insights into the evolution of normal fault 73 systems in the central Kenya Rift. To achieve this aim, a Digital Elevation Model (DEM) with 30 m horizontal 74 resolution is used to produce a detailed fault geometry dataset for surface faults of the central Kenya Rift. 620 75 faults have been manually mapped from this DEM over an area measuring 240 x 150 km. In this study, we 76 measured the throw and length of surface faults derived from ASTER DEM data. Second, we estimated the 77 part of fault throws obscured due to burial by volcanics and sediments in the hanging wall. Fault throw was 78 then used to calculate the maximum displacement using an average fault dip for the central Kenya rift. The 79 effect of data resolution on the fault trace length was also corrected by adding an estimated tip length. Next, 80 three domains of differing fault populations have been identified, which offer an opportunity to investigate 81 fault scaling relations of the fault populations along the central Kenya Rift during progressive deformation. 82 Finally, we discuss the results addressing implications for the evolution of the rift and the growth of normal 83 faults in the study area.

84

85 2 Tectonic and geological background

86 The spatial extent of this study covers a portion of the central Kenya Rift located between Lat 1.05° N to -1° 87 S and Long 35.5° to 36.7° E that covers an area of 240 x 150 km (Figure 1). The central Kenya Rift is thought 88 to represent a phase of relatively early continental rifting (Baker and Wohlenberg, 1971) where most 89 deformation is accommodated on small boundary faults with an absence of internal faults (e.g. Corti, 2009, 90 Agostini et al., 2011b). The northern part of the central Kenya Rift comprises two parallel Rift valleys (Figure 91 2). The eastern rift is known as the Kenya Rift and the western one is called the Kerio Rift, separated by the 92 Kamasia horst, and these structures are oriented N10ºE (Figure 2). Both Rift basins are west-dipping half-93 grabens, with major border faults on the western rift shoulders, the Kerio Rift terminating west of Lake 94 Bogoria, while the Kenya Rift continues farther to the south and bends sharply at the Gregory Rift (Figure 2). 95 This bend has been interpreted as the intersection with a large NW trending basement structure known as the 96 Aswa lineament (Smith and Mosley, 1993, Chorowicz, 2005, Omenda, 2010).

97 The central segment of the Kenya rift system is known as the Gregory Rift (Figure 2) and is a complex graben 98 that trends N-S. It is 60 -70 km in width and is bounded by en echelon arrangements of major normal faults 99 forming the Nguruman, Mau, and Elgeyo escarpments on the western boundary and the Aberdare escarpment 100 on the eastern boundary (Jones and Lippard, 1979, Baker et al., 1988) (Figure 2). Fault escarpments are well 101 defined and reach up to 2000 m in height (Baker and Wohlenberg, 1971). The central Kenya rift encompasses 102 a number of half graben basins that have varying orientations ranging from NNE-SSW to NNW-SSE (Smith 103 and Mosley, 1993). The major faults in the central Kenya Rift are antithetic and dominantly dip eastwards 104 (Baker and Wohlenberg, 1971, Baker et al., 1972). Overall, the tectonostratigraphic evolution of these Rift 105 sectors shows a successive migration of normal faulting from the boundary faults inwards toward the Rift 106 valley, where the structural development has been characterized by a concentration of faulting associated 107 with volcanism since late Pliocene era (Baker and Wohlenberg, 1971).

108 Volcanism and rifting started in the Kenya Rift around the early Miocene in the north, in the Lake Turkana 109 area and migrated southwards. Rifting was active from around the middle to late Miocene in the central segment (Baker et al., 1972, Smith and Mosley, 1993). The Kerio basin in the centre and the Baringo basin 110 111 in the north of the central Kenya Rift witnessed a long period of extensive basaltic lava extrusion during the 112 initial phase of rifting (Paleogene to lower Miocene) (Ebinger, 1989). Therefore, infill in the central Kenya 113 Rift is predominantly volcanogenic (Smith, 1994). Furthermore, a geological map of Kenya (Ministry of 114 energy of Kenya 1987, Figure 1) shows that the study area is covered by Quaternary and Tertiary volcanic sediments. The thickness of sediments and volcanic deposits in this region is ~4.5-5km (Hautot et al., 2000) 115 116 as determined from magnetotelluric (MT) data, which is a geophysical method used to model the Earth's 117 subsurface from measurements of natural geomagnetic and geoelectric field variation at the Earth's surface.

118 It has been proposed that faults in the East African Rift System (EARS) are not randomly distributed but tend 119 to follow the trend of pre-existing weakness zones within the lithosphere i.e. Proterozoic mobile belts, and 120 avoid the Archaean stable cratonic areas (McConnell, 1972, Daly et al., 1989, Petit and Ebinger, 2000, Ziegler 121 and Cloetingh, 2004). The central Kenya Rift segments formed along old zones of weakness at the contact 122 between two contrasting types of lithosphere; the Archean Tanzanian craton and the Proterozoic Mozambique 123 belt (e.g. Smith and Mosley, 1993, Mariita and Keller, 2007). Therefore, the extensional deformation may be 124 localized along mobile belts and suture zones as they tend to be weaker than the surrounding areas (Petit and 125 Ebinger, 2000).



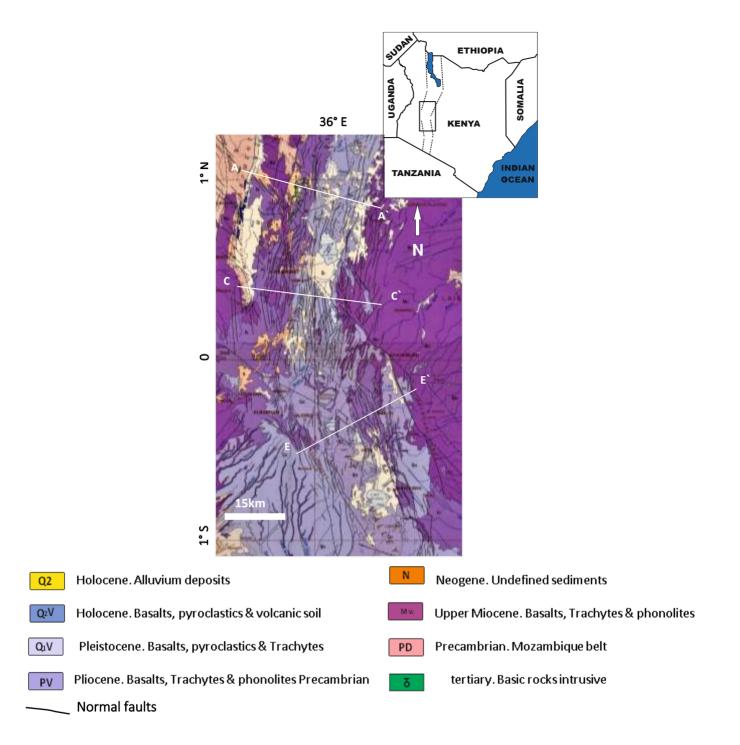


Figure 1. a geological map of the study area, from geological map of Kenya (Ministry of Energy of Kenya 1987). The small inset image displays the location of the study area, the central Kenya rift. The white lines are locations of the topographic profile shown in figure 8.

128 **3** Methodology

129 **3.1 Data and interpretation of fault traces**

130 In this study, 620 discrete faults were identified, from which fault measurements were made such as fault 131 trace length, maximum apparent throw, orientation, and throw\length ratio. Maximum apparent displacement 132 was derived from each maximum fault throw value using an average fault dip of 65°. There are several reasons 133 for using an average fault dip in this regional study: firstly, fault dips cannot be directly measured from 134 ASTER DEM data. Secondly, lack of fault dip data in previous studies for the study area and thirdly, the large 135 number of faults involved in this study that required a generalized assumption. This fault dip value of 65° is 136 the average of a fault dip range of 55° to 75° for the central Kenya Rift as reported in Zielke and Strecker (2009).137

138 Digital elevation models (DEM) are the main data used to investigate the upper crust brittle deformation in 139 the study area. The DEM data were obtained from the USGS (https://lpdaac.usgs.gov/) through Advanced 140 Space-borne Thermal Emission and Reflection Radiometer (ASTER) data with ground resolution of 30 m x 141 30 m and vertical resolution of 20 m to provide information on the morphology of surface faults. Google 142 Earth optical spectrum imagery with a resolution of about 15 m was used along with the ASTER DEM to 143 assist in viewing the topography and determine the dip direction of the mapped faults. The data resolution 144 refers to the minimum distance by which data can be recorded from the scanned scene. The main effect of 145 resolution is a truncation, which means fault trace lengths below 30 m (found in fault tips) and fault heights 146 (throws) below 20 m cut-offs are not resolvable, which lead to underestimation of these parameters. However, 147 the effect of truncation is more significant on small size fault populations (Walsh et al., 1996, Watterson et 148 al., 1996, Yielding et al., 1996)

149 The DEM data were converted into a shaded relief surface (Figure 2). Fault traces were identified on the DEM surface by using several techniques available in Petrel software, including edge detection, which is 150 151 particularly useful in identifying where subtle changes in the surface topography occur, thereby enhancing 152 confidence in mapping fault escarpments. Vertical exaggeration of x5 was also used to facilitate tracing fault 153 scarps. Given the resolution of the DEM used, some topographic features (i.e. <20 m height) that do not show 154 clear topographic scarps were not considered to be faults. Nevertheless, hundreds of fault scarps were readily 155 distinguishable on the DEM surface across the study area. Fault scarps were interpreted and recorded based 156 on their length, and when fault segments were linked, the entire length of the fault segment array was mapped 157 as a single larger fault.

In this study, the height of fault scarp measured from the DEM has been used as a proxy for fault throw.However, accumulation of sediment, volcanic and erosional deposits reduce the apparent height of the fault

much erosion of the block has occurred. All these uncertainties may introduce systematic error into throw 161 162 measurements and strain estimations. For each fault, footwall cut-offs were manually digitized by tracing the 163 crest of each topographic scarp along strike (blue dots on blue lines in Figure 3A –C), whilst apparent hanging wall cut-offs were picked by tracing the lower-most position of the fault along its trace (pink dots on pink 164 165 lines in Figure 3A – C). Therefore, the measured throw was the maximum value of the apparent fault height/ 166 throw between the corresponding points picked in the footwall cut-off and the hanging wall cut-off along each 167 fault trace measured in two dimensions (2D). Fault length defined in this study is the horizontal exposed fault 168 trace length along strike. 169 The chronology of fault formation in the central Kenya rift is that major faults were first formed between 16

scarp. Moreover, fault blocks are normally eroded, and in DEM surfaces, it is not possible to determine how

and 8 Ma (Smith, 1994), and the volcano-sedimentary infill in the rift is between 4.5-5km thick (Hautot et al.

171 (2000). Consequently, fault throws, and lengths measured at this stage are just the apparent or exposed values

172 of fault throw, and length due to possibility of hanging walls being partially filled with sediment, volcanic

and erosional deposits, and subsequent burial of fault tips.

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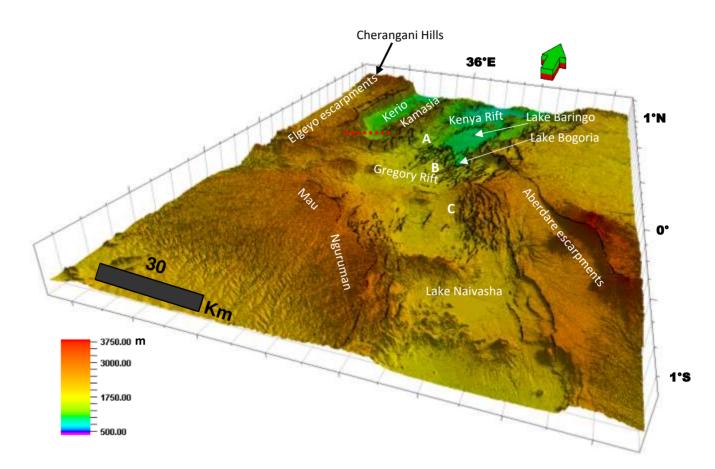


Figure 2. A shaded relief surface image generated from ASTER DEM. The small inset image displays location of study area within the East Africa Rift System; dashed red line is a location of seismic line shown in (Figure 4); A, B and C are locations of close-up images (Figure 3)

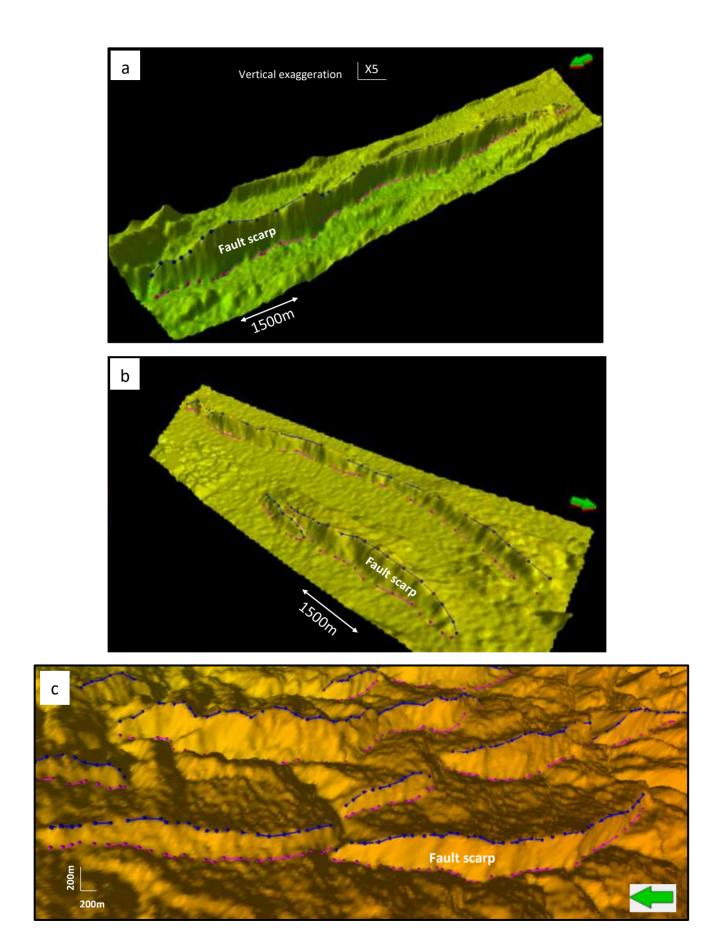


Figure 3. Examples to show how the faults were picked using the DEM surface. The footwall cut-off is picked (shown as blue circles on blue polyline) followed by picking the corresponding apparent hanging wall cut-off (pink circles on pink polyline), resulting in the same number of picks top and bottom, which were used to calculate throw. a) Fault scarp structure shows the final picks for the footwall and hanging wall cut-offs. b) Fault structure on the left-hand side of the image is an example of fault picking along two faults separated by a relay ramp. c) Picks along several en echelon fault scarps in the central part of the study area. (See Figure 2 for image locations).

177

178 **3.2 Under** sampling of faults lengths due to truncation bias.

Data resolution and burial of fault tips may mask the true positions of fault tips at the surface and therefore 179 180 cause fault lengths to be underestimated. Truncation bias refers to effects caused by systematic under-181 representation of smaller faults in a sample due to limitations in data resolution, below which the fault length 182 and throw cannot be detected (Pickering et al., 1995, Watterson et al., 1996, Zhang and Einstein, 2000, Bonnet 183 et al., 2001). This truncation bias needs to be corrected for, to provide a more reliable estimate of the fault trace length. However the effects of truncation are relatively more significant on small scale fault populations 184 185 (Walsh et al., 1996, Watterson et al., 1996, Yielding et al., 1996). Censoring bias refers to partial sampling of 186 large faults that extend beyond the sample area and therefore are incompletely characterized (Pickering et al., 187 1995, Zhang and Einstein, 2000, Bonnet et al., 2001). Censoring is thought to not be of great significance 188 unless the sample area is small relative to the full lengths of the majority of fault traces (Heffer and Bevan, 189 1990).

190 It has been shown in some studies such as Pickering et al. (1997) and Soliva and Schultz (2008) that the 191 truncation bias can be estimated by dividing the lowest throw value that can be resolved by the average value 192 of throw/length ratio in a given region. The average throw/length ratio calculated for this study area was 0.04, 193 which is similar to that estimated by Le Gall et al. (2008), in southern Kenya close to the Tanzania border. 194 Given the vertical resolution of 20m ASTER DEM (https://lpdaac.usgs.gov/), we estimate that a truncation 195 bias occurs for fault lengths less than 500 m. To account for the truncation bias, we added a 500 m to the end of each fault to enable us to estimate the true distribution of fault lengths. By adding the 500 m to fault tips 196 of the 620 mapped faults, the length populations range from 1270 m to 60600 m, with an average length of 197 198 6150 m.

200 **3.3 Under sampling of fault throws and derivation of displacements**

201 In this study we quantified throw as the height of the fault scarp measured from the DEM. The extent of total 202 fault throws into the subsurface is hard to be constrained due to the scarcity of seismic data over this region 203 of the EARS. However, a seismic line (Figure 4b) shown in Morley and Ngenoh (1999c) was used in an 204 attempt to account for the missing throw. This seismic line was shot by the National Oil Corporation of Kenya 205 (NOCK) in 1990 over at the southern end of the Kerio Rift between the Elgevo escarpment and the Kamasia 206 horst (see Figure 2 for location). According to the interpretation by Pope (1992) and Ngenoh (1993), this 207 seismic line shows a large boundary fault, namely the Elgayo Fault in the subsurface, which marks the western 208 boundary of the Rift (Figure 4b). The DEM image resolves the continuation of the Elgayo escarpment at the

surface (Figure 4a).

210 From the seismic line (Figure 4 b) we interpret the Elgavo Fault hanging wall cut-off to be at a depth of ~ 2 211 sec (TWT) (Figure 4c). Given that the average seismic velocity for the rift infill between Lake Baringo and Lake Naivasha is about 4000 m/s as determined by Henry et al. (1990b), the subsurface fault throw is therefore 212 213 about 4 km. This value is in general agreement with the thickness of volcanic-sedimentary infill of \sim 4.5 km 214 estimated in Hautot et al. (2000) using Magnetotellurics (MT), and an estimate of 4km in Henry et al. (1990b) 215 that derived the thickness of the sediment/volcanics layer from two seismic refraction lines in the central 216 Kenya Rift. Consequently, the buried throw is about 2.5 times the apparent throw of ~1560 m estimated from 217 the surface scarp of the Elgevo escarpment. Since there have been no detailed regional studies that recorded the 218 volcano-sedimentary infill in different parts of the central Kenya rift, and also due to the lack of adequate 219 subsurface data in this rift, the buried throw of different size faults across the rift cannot be established. Therefore, 220 for simplicity, we assumed that all mapped faults extend under the surface by the same factor of 2.5 time as 221 that calculated for the Egleyo escarpment. So, the correction consists of simply multiplying each surface 222 apparent fault throw measurement by 2.5 and adding the apparent surface throw for each mapped fault. 223 Consequently, the estimated maximum throw range is ~ 37 to ~ 5460 m with an average of ~ 450 m. Fault 224 displacements were then derived from fault throws through a simple geometric calculation using a 225 representative fault dip of 65°.

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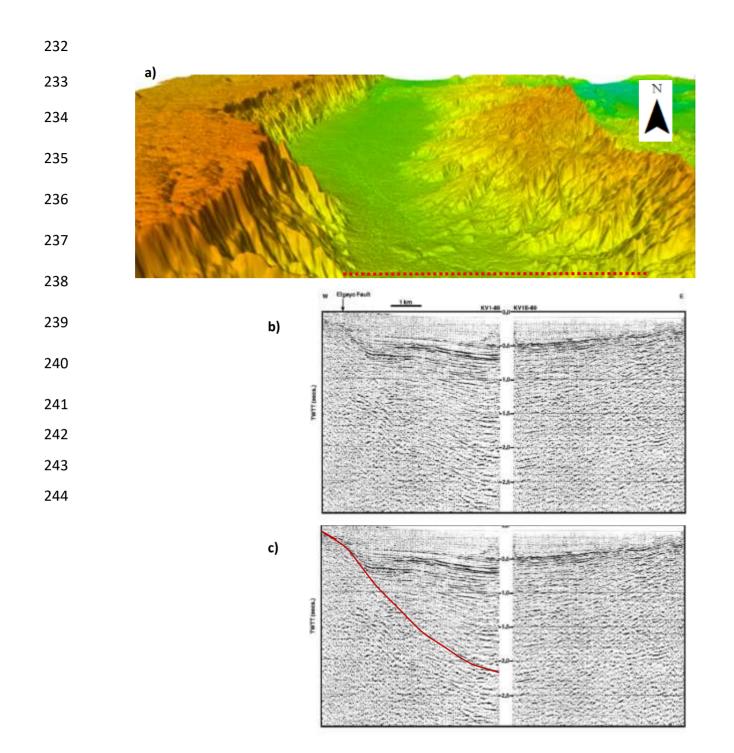


Figure 4. a) DEM surface showing the Elgayo Fault escarpment, dashed red line shows the location of seismic line, which is about 12 km in length (see Figure 1). b) seismic line in the Kerio Rift from Morley and Ngenoh (1999c). c) interpretation of the Elgayo Fault.

245 3.4 Fault analysis methods

As part of examining the 620 faults mapped from the DEM surface, the relationship between fault displacement and fault length is plotted and compared with a global data set of normal faults. It has been largely accepted that the relationship between displacement and fault length provides crucial information on the growth of faults through time (e.g. Walsh and Watterson, 1988, Cowie and Scholz, 1992b). The relationship between the maximum displacement (D) and the fault length (L) has been defined as follows (e.g. Walsh and Watterson, 1988, Dawers et al., 1993):

252 $dmax = cL^n$

where c is a constant relating to material properties, *n* is the exponent value, which ranges from 0.5 to 2.0 for tectonic fault systems. published values of n are; n = 0.5 (Fossen and Hesthammer, 1997), n = 1.0 (Cowie and Scholz, 1992a, Dawers et al., 1993, Schlische et al., 1996, Davis et al., 2005, Stanton-Yonge et al., 2020), *n* =1.5 (Marrett and Allmendinger, 1991, Gillespie et al., 1992) and n = 2.0 (Watterson, 1986, Walsh and Watterson, 1988), The n value of fault Displacement/Length data has implications for what fault model best describes the growth of faults.

259 In this paper, the trend of extensional strain from south to north of the study area was estimated by measuring 260 total fault heave across faults along six transects along the rifts (Figure 3), in order to determine the 261 contribution of different fault populations to the strain. The horizontal fault separation (heave) was estimated 262 by measuring the horizontal distance between the hanging-wall and footwall cut-offs, measured perpendicular 263 to the trace of the fault in map view (2D) for all faults that intersect the cross-sections. However, volcanic and 264 sediment infill as well as eroded faults scarps prevent identifying the original positions of faults hanging wall 265 and footwall cut-offs, which in turn would introduce some uncertainties on heave measurements. Moreover, 266 the extensional strain may also be underestimated due to underrepresentation of small faults that fall below 267 the resolution of observation.

268 Fault displacements and fault lengths were analysed through fault cumulative frequency plots. This can be 269 done through ranking the displacement/length data in a descending order and then plotting fault 270 displacement/length data against the cumulative frequency in a log-log scale. Different statistical functions 271 (i.e. power law, lognormal and exponential laws) have been used to examine the best fit for the fault 272 displacement/length data. These statistical functions deploy a transformed regression model, which is a type 273 of least squares estimation method to fit statistical distributions that has been widely used in geological studies 274 (Pickering et al., 1995, Poulimenos, 2000, Peacock, 2002, Bailey et al., 2005, Soliva et al., 2006, Soliva and 275 Schultz, 2008).

277 **4** Fault Population analysis and results

278 4.1 Relationship between fault length and displacement

Fault displacement and length data obtained in this study were compared with previously published
displacement-length data (Figure 5) for normal faults from different sources compiled by Gillespie et al.
(1992) and Bailey et al. (2005). The mapped faults lie well within the published global dataset.

282 Fault maximum displacement and length data from the three zones were plotted in different colors in a log-283 log space (Figure 6a). The data from the three zones combined showed a large scatter that spans about two 284 orders of magnitude in both variables. A linear regression line passing through the data points is expressed as $v = 0.0691x^{+129.5}$ with coefficient of determination $R^2 = 0.479$ and a power law fit, with a slope of n = 1.09285 and $R^2 = 0.382$. The low coefficient of determination together with the large extent of scatter cannot justify 286 287 the regression lines. The maximum displacement-length data for each individual zone also exhibited a low 288 coefficient of determination for both linear and power law trendlines due to the high scatter. Such scatter is 289 common to other fault population studies and has been attributed to: combining data sets from areas of 290 different lithology and material properties (e.g. Cartwright et al., 1995, Peacock and Sanderson, 1991, 291 Peacock, 2002, Cowie and Scholz, 1992a), fault growth and segment linkage (Cartwright et al., 1995, 292 Schlische et al., 1996, Cartwright et al., 1996, Mansfield and Cartwright, 2001), sampling effects and 293 inaccurate measurement (Gillespie et al., 1992). However, despite this high scatter, it can be observed from 294 displacement-length data for each individual zone (Figure 6b, c, d), where several faults have a comparable 295 length but varying displacement, that this will lead to increasing displacement-length ratios for larger faults, 296 and create a general vertical trend of increasing displacement for those faults which have fixed length but 297 accumulate throw.

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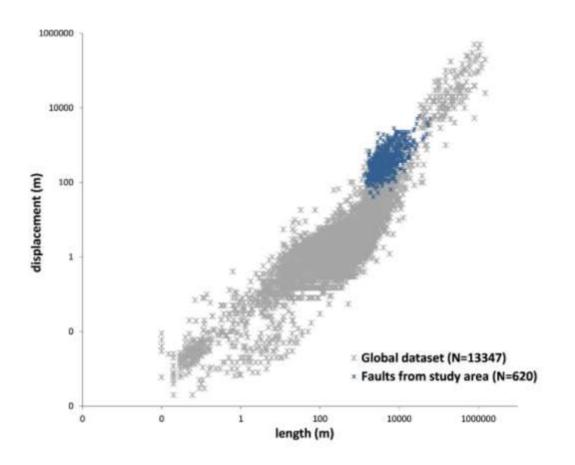


Figure 5. Log-log plot of fault displacement vs. length for faults from the study area along with previously published data from (Gillespie et al., 1992, Bailey et al., 2005).



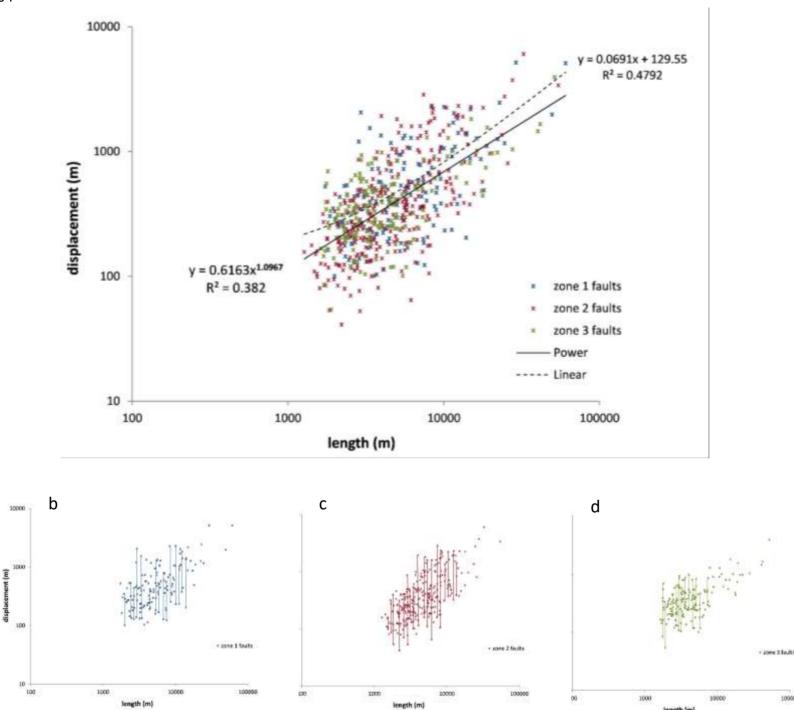


Figure 6. (a) Log-log plot for displacement vs length for all faults mapped in the study area showing a large scatter. (b, c & d) Displacement vs. length plots of individual fault zones, faults showing comparable length, but varying displacement are joined by lines to illustrate the observed vertical trend of increasing displacement population..

305 4.2 Relationships between strain and fault populations

There are different fault orientations throughout the study area (Figure 7). Therefore, to assess the contributions of different fault sets to the strain accommodation of the entire area, the region was divided into three subzones (zone 1, zone 2 & zone 3) based upon average fault orientations (Figure 7). Zone 1, in the north is dominated by N-NNE striking faults, zone 2 in the central section of the rift is characterised by a NNW to NNE fault strike, whereas zone 3 in the south is characterised by a N-NNW striking fault system (Figure 7). The number of resolved faults is 149, 295 and 177 for zone1, zone 2 and zone 3 respectively.

312 Normal faults typically form perpendicular to the stress direction. The average fault orientation for zone 3 313 (shown as a red line in the rose diagrams in Figure 7) is $\sim 10^{\circ}$ oblique from being perpendicular to the regional 314 EW-trending extension orientation, and more oblique compared to zone 2 and zone 1. In theory, such obliquity 315 would cause the displacement vector to deviate from true dip-slip and produce what is called an oblique-slip 316 fault. However, the true displacement vector cannot be estimated from a DEM in such a regional study, 317 because defining a fault as oblique requires both dip and strike components to be measurable and significant. 318 Therefore, for the purpose of this study, we assumed the effect of $\sim 10^{\circ}$ obliquity between the average fault 319 orientation and the EW-trending regional extension in zone 3 to be insignificant, and consequently error 320 associated with calculating displacement from the apparent throw measurements to be also negligible.

321 4.3 Strain accommodation

322 Fault heaves are an expression of strain in extensional tectonic settings. Fault displacement (i.e. heave and 323 throw) increases as strain accumulates (e.g. Poulimenos, 2000, Walsh et al., 2002a, Schlagenhauf et al., 2008). 324 Therefore, in this study, we consider that total (cumulative) heave and associated heave percentage (Table 1) 325 are illustrative of strain. The strain along the rift from south to north was then assessed using six cross-sections 326 (Figure 7). The cross-sections were defined perpendicular to the trend of fault populations in each zone. We present two cross-sections for each zone, AA` & BB` in zone 1, CC` & DD` in zone 2 trend ESE-WNW and 327 328 EE`& FF` in zone 3 trend ENE-WSW (Figure 7). Total fault heave that has been taken as representative of 329 strain was then estimated by summing fault heaves across each cross-section. This analysis shows that average 330 strain in each zone increases from \sim 5560 m in zone 3 (south) to \sim 7470 m in the central (zone 2), whereas 331 zone 1 in the north exhibited the largest average extension of ~ 9800 m (Table 1). The percentage of strain 332 accommodated at each cross-section in relation to the overall strain of the study area was defined by dividing 333 the amount of strain of each transect by the total amount of strain estimated for the entire study area (Table 1). Figure 9 shows a progressive increase of strain from zone 3 in the south to zone 1 in the north. Estimations 334 335 of uncertainty in measurements of each total heave (Error! Reference source not found.) did not show a 336 significant error contribution (Figure 9).

- 337 (Figure 8) shows topographic profiles of cross-sections AA[`], CC[`] and EE respectively. These profiles show
- that the width of the rift valley widens from 19 km in the south (cross-section EE`) to 40 km in the north
- $(cross-section AA^{)}$. Elevation of the rift valley also decreases from ~2000 m in the south (cross-section EE⁾)
- 1000 m in the north (cross-section AA⁽⁾), where rift valleys of the Kero Rift and the Kenya Rift appear to
- be in the lowest part of the study area. This systematic decrease in rift floor elevation is interpreted to reflect
- 342 increased lithospheric thinning and subsidence, as indicated by Cowie et al. (2005). The geological formations
- 343 shown in the cross-sections depict extensive volcanic deposits along the rift as reported by Ebinger (1989).

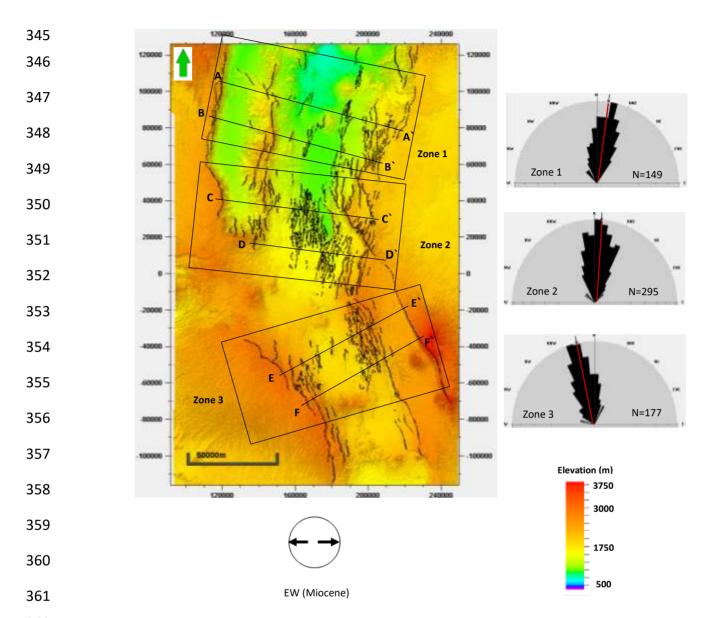
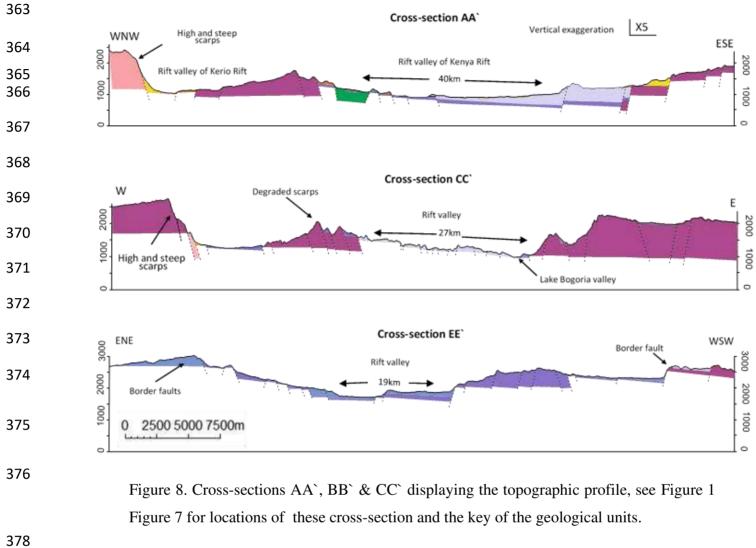


Figure 7 . Rectangles represent the three structural zones defined within the study area, and location of cross-sections (see Figure 2 for location of the 3D surface). The two opposite arrows indicate extension direction, and the red line within the rose diagrams shows the average orientation of fault population.





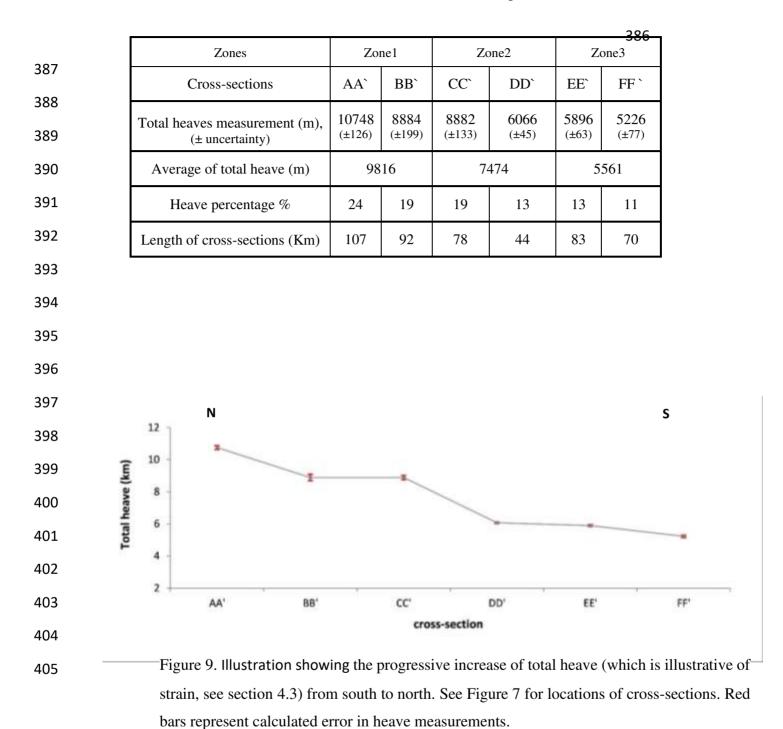


Table 1 Total fault heaves obtained from each cross-section (Figure 7)

408 **4.4 Fault displacement populations**

410	Rift zone	R ² for Function fits			
411	KIIT ZOIIE	Power-law	Log-normal	Exponential	
412	zone 1	0.96	0.90	0.81	
412	zone 2	0.93	0.91	0.82	
413	zone 3	0.90	0.92	0.85	
414	All zones	0.92	0.90	0.83	

409 Table 2. Results of functions fit to displacement data

Fault displacement data for the three zones combined (Figure 10) and individually (Figure 11) were analysed using fault cumulative frequency log-log plots, and three statistical models including power law, log-normal and exponential laws were used to assess the best fit for the fault displacement populations. Generally power law scaling was found to be the best statistical model to fit the displacement data based upon the values of coefficient of determination R² (Table 2).

420 It has been shown in the literature that power law is preferred over other statistical distributions because it 421 provides a better description of fault size distributions (e.g. Bonnet et al., 2001). For this reason, the power-422 law distribution is used in this study to assess the amount of deformation and to highlight the contribution 423 of different fault sizes to the strain accommodation.

The exponents of the power-law distributions of fault displacement data from zone 1, zone 2 and zone 3 were found to be 1.0, 1.1 &1.4 respectively (Figure 11), and 1.2 for the three zones combined (Figure 10). These exponents are comparable to those obtained from a number of studies on tectonic fault systems that range from 1.0 to 1.5 (e.g. Scholz and Cowie, 1990, Marrett and Allmendinger, 1992, Gauthier and Lake,

428 1993, Watterson et al., 1996, Yielding et al., 1996).

429 It is worth mentioning that large faults do not really follow the same trend as the mid-size faults (Figure 10 430 & Figure 11), which might be because large faults accommodate disproportionately higher strain, leading to 431 the steepening of population curves, as suggested by Bailey et al. (2005). Moreover, it can also be observed 432 that there is an inverse correlation, where the lowest fractal dimension of D = 1.0 in zone 1 (Figure 10) 433 corresponds to the largest average fault length and fault displacement of 7155 m and 660 m respectively 434 (Table 3). On the other hand, the smallest average length and fault displacement of 5610 m and 450 m 435 respectively corresponds to the highest fractal dimension of $D = \sim 1.4$ in zone 3; this issue is returned to 436 later.

437 Table 3. Statistics of fault lengths and fault displacements in the three zones

	Length (m)			Displacement (m)		
	Min	Max	Average	Min	Max	Average
Zone 1 (n = 149)	1740	60600	7155	100	5160	660
Zone 2 (n = 295)	1270	54515	5775	40	6030	550
Zone 3 (n = 177)	1630	51477	5610	54	3939	450

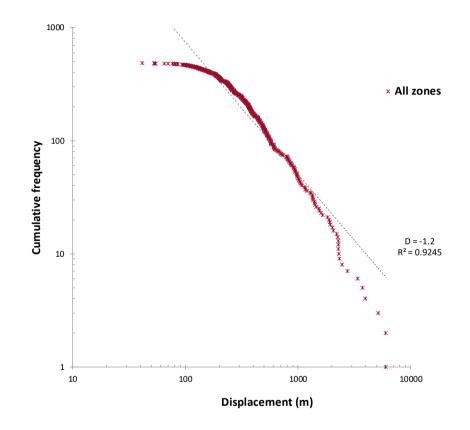
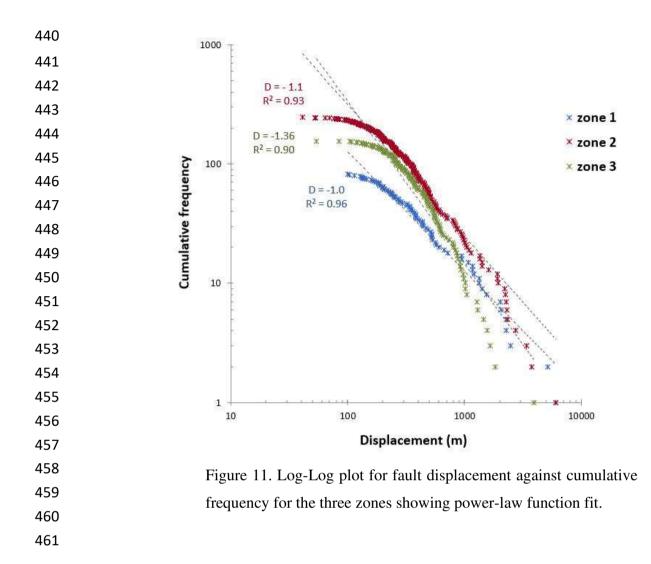
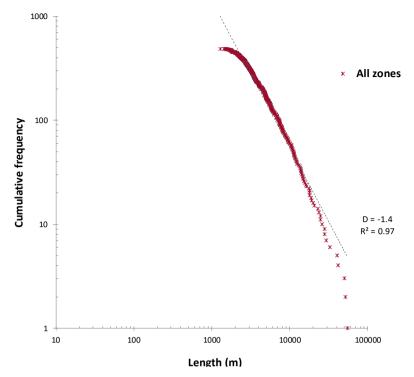


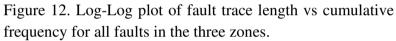
Figure 10. Displacement population showing a straight-line of power-law fitting with a slope of D = -1.2 in Log-Log plot for fault displacement against cumulative frequency for the three zones combined.



462 **4.5 Fault length populations**

Several studies have suggested that there is a strong correlation between fault displacement and fault length 463 464 (e.g. Walsh and Watterson, 1988, Peacock and Sanderson, 1991, Cowie and Scholz, 1992a, Gillespie et al., 465 1993, Cartwright et al., 1995, Cowie, 1998b, Kim and Sanderson, 2005). Moreover, distribution of fault 466 lengths should follow similar scaling relationships to fault displacement (Cladouhos and Marrett, 1996). 467 Therefore, analysing attributes of fault length populations for the three zones using cumulative frequency 468 function log-log plots would be expected to also show a power-law distribution. The power law exponent 469 (D) for the length population for the three zones combined (Figure 12), and for each individual zone (Figure 470 13) was found to be ~1.4, which is in agreement with the range of 1.0 to 1.7 from previously published fault length populations observed in natural fault systems (e.g. Gauthier and Lake, 1993, Scholz et al., 1993, 471 Watterson et al., 1996). We notice here that the D values for the fault traces remain almost unchanged in the 472 three zones; the implications of this will be discussed in the next section. 473





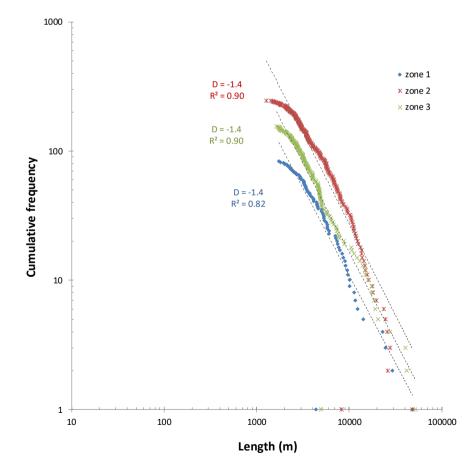


Figure 13. Log-Log plot of fault trace length vs cumulative frequency for the three zones showing power law fit.

478 5 Discussion

479 **5.1 Displacement-length scatter**

480 The datasets of 620 faults presented here is large enough to make reliable assessments and observations of 481 changes in geometry and behaviour of fault size attributes, which may shed light on the underlying physical 482 mechanism of fault growth and rift evolution. One possible limitation with the mapped faults in this study 483 is that the measured fault scarp height/ throw was not fully constrained. Accumulation of sedimentary and 484 volcanic deposits lower the apparent scarp height and would lead to underestimation of the displacement values and, in turn, extension estimates and the D\L ratios. However, this has been overcome by the 485 486 application of a correction for the "hidden" throw. The displacement-length data for the mapped faults plot 487 generally within the field of displacement-length values compiled by Gillespie et al. (1992) and Bailey et al. 488 (2005) as shown in Figure 5. Therefore, we consider discussing results of this study in the light of published 489 literature of normal faults to be valid.

490 It has been observed from displacement-length data of each individual zone (Figure 6b, c, d) that several 491 faults have a comparable length but varying displacement. Such a vertical trend of increasing displacement 492 for given fault length will result in an increase of displacement-length ratio for larger faults (Walsh et al., 493 2002a). Dawers et al. (1993) argued that the displacement-length relationship becomes non-linear in an 494 upward increasing manner when length is considered fixed relative to the cumulative slip from many slip 495 events. Therefore, the observed upward trend of increasing displacement population in each zone of the 496 study area (Figure 6 b, c, d) could be explained as follows: smaller faults that have experienced fewer slip 497 events should have lower displacement-length ratios than larger faults that have experienced more slip 498 events. This interpretation may be valid for the mapped faults in this study that occur in a single geological 499 setting, whilst recognising that previous research by Cowie and Scholz (1992a) suggests that the fault 500 displacement-length ratio may also be modified by material properties of the rock or if data are combined 501 from diverse geologic settings.

502 It has been mentioned in section 4 above that the scatter in any the maximum displacement-length data could 503 be caused by several sources; errors associated with the fault picks from the DEM surface could contribute 504 to the large scatter observed in this dataset (Figure 6). It also has been noted from the geological map of 505 Kenya (Figure 1) that the study area is covered by Quaternary and Tertiary volcanic sediments that could be relatively uniform in lithology. Moreover, Smith (1994) indicated in his study that therefore, the lower 506 507 Miocene sediments deposited in central Kenya are predominantly volcanogenic. Therefore, it could be 508 argued that scattering shown by this dataset may be caused by other sources other than the rock lithology. 509 Another likely source that introduces scatter to plots of maximum displacement versus length of this dataset 510 is the process of fault growth through segment linkage, which is discussed further below.

512

513 **5.2 Strain distribution**

514 Extension regime in the central Kenya Rift is believed to occur in an approximately E-W direction, as 515 supported by geological data (Daly et al., 1989, Morley, 1988), current seismicity (Fairhead and Stuart, 516 1982, Foster and Jackson, 1998) and GPS analysis (Calais et al., 2006). The central Kenya Rift is thought 517 to be developed on a strongly heterogeneous basement, exhibiting a series of late Proterozoic, regional scale 518 NW-SE and NS trending ductile/brittle shear zones, which exist in the lithosphere beneath the rift (Daly et 519 al., 1989, Maurin and Guiraud, 1993, Mosley, 1993). Moreover, underlying basement fabric structures may 520 occur such as faults (Giba et al., 2012, Bellahsen and Daniel, 2005), shear zones (Corti, 2008, Agostini et 521 al., 2011, Corti, 2012) or foliations (Hetzel and Strecker, 1994) which could interfere with the regional stress 522 leading to localized variations in stress orientations (Aleksandrowski et al., 1992, Teyssier and Tikoff, 523 1999), and influence the orientation of normal faults during their initiation and evolution (Giba et al., 2012, 524 Bellahsen and Daniel, 2005, Agostini et al., 2009). Consequently, different orientations of fault populations 525 observed in the three zones (zone 1, 2 &3) in the central Kenya rift under the same regional extension 526 direction could be due to existence and influence of pre-existing structures with different orientations.

527 Estimation of strain through heave measurements along the study area (Figure 3.10a) exhibits that cross-528 sections EE` and FF` in zone 3 in the south part of the rift also cross through a relatively large number of 529 faults but still have the least average heave percentage of $\sim 12\%$, and that is because faults in zone 3 are 530 relatively smaller in size as indicated by the smallest average fault length and displacement (see Table 3). 531 Cross-sections CC` and DD` in zone 2 pass across a relatively larger number of faults and accommodate an 532 average heave percentage of $\sim 16\%$. On the other hand, cross-sections AA` and BB in zone 1 in the north 533 accommodate the largest average heave percentage of ~22% along this part of the Rift. Table 3 displays that 534 zone 1 encompasses the fewest number of resolved faults (n = 149) and has the largest average of fault trace-535 length and fault displacement. Therefore, differences in extensional strain accommodated between the 536 southern and northern zones of the study area are attributable to the extensional strain localization along a 537 few faults in the northern part (zone 1). These faults are deeper, with larger throws, and therefore take up 538 more extensional strain than those in the southern part (zone 3). These strain estimations suggest that zone 539 1 accommodates the largest amount of strain, followed by zone 2 then zone 3.

540

541 **5.3** Fault population analysis and implications for fault growth and rift evolution

542 It has been demonstrated earlier that fault populations in the three defined zones (zone 1, zone 2 and zone 543 3), either individually or combined have exhibited a power-law distribution for both fault length and displacement data. Fitting to a power law distribution for fault length populations in the three zones is
compatible with the low-strain settings of early continental Rifting (Gupta and Scholz, 2000, Vétel et al.,
2005). That contrasts with a high strain setting where rifts are more evolved and, therefore, an exponential
scaling function appears in the cumulative distribution for fault lengths as observed in the North Ethiopian
Rift–Afar transition area by Soliva and Schultz (2008), and in the Main Ethiopian Rift by Agostini et al.
(2011).

550 Differences in the exponent of power law scaling of fault size population distributions are used to assess the 551 contribution of different fault sizes to total strain accommodation (Yielding et al., 1996). The higher the 552 exponent of population slopes, D (fractal dimension), the higher the contribution of small faults to strain accommodation (Marrett and Allmendinger, 1991, Yielding et al., 1996). This has been confirmed in the 553 554 current study for the examined fault displacement distributions (Figure 11), where zone 3 in the south 555 accommodates the least strain (Figure 9 & Table 1) and has the highest fractal dimension of $D = \sim 1.4$ 556 (Figure 11). This implies that zone 3 encompasses a larger number of small faults contributing to the strain 557 accommodation compared to zone 2 and zone1, and that is supported by the smallest averages of fault length 558 and fault displacement of 5610 m and 450 m respectively calculated for zone 3 (Table 3).

559 In the centre of the study area, the cumulative extension in zone 2 has increased to 7474m as opposed to 560 5561m in zone 3 (Figure 9 & Table 1). Consequently, the power law exponent of fault displacement 561 population decreases to D = 1.1 (Figure 11). Previous studies such as Cartwright et al. (1995) and Cladouhos 562 and Marrett (1996)) and experimental models e.g. Sornette et al. (1993) suggest that in all fault linkage 563 models, the fractal dimension (D value) of power-law distribution decreases systematically with increasing 564 fault strain as faults link. Thus, our observations suggest that zone 2 (where the averages of fault length and 565 displacement are greater than that of zone 3 as shown in Table 3) is a more mature fault zone with more 566 fault-linkage than zone 3.

Moreover, the fractal dimension for fault displacement decreases further to 1.0 in zone 1 (Figure 11) in the north where the highest strain was estimated (Figure 9 & Table 1). It has been reported in some previous studies (e.g. Cartwright et al., 1995, Cowie et al., 1995, Cladouhos and Marrett, 1996, Ackermann et al., 2001, Walsh et al., 2003b, Moriya et al., 2005) that such a decrease of fractal dimension indicates that the deformation is increasingly localised onto fewer large faults as the fault system. This has been supported in this study by the greatest statistics of fault length and fault displacement calculated for zone 1 (Table 3) where the fewest number of faults were mapped.

However, in many cases a simple power-law may not account for the full-range of the observed scaling
behaviour (Davy, 1993, Soliva and Schultz, 2008, Vétel et al., 2005). Among other factors that contribute

576 to the complexity of the fault network evolution, the boundary condition of the brittle layer may also affect 577 how the fault system evolves (Cowie et al., 2005, Hardacre and Cowie, 2003). Kudo and Furumoto (1998) 578 applied the fractal dimension analysis to characterize the crustal structures in three Japanese Islands, and 579 they observed changes in fractal dimension in the three areas, which were attributed to the lateral variation 580 of the crustal thickness in those areas. Therefore, it is worth mentioning that seismic refraction and regional 581 reflection studies of Henry et al. (1990a) and KRISP (1991) indicate significant variations in crustal 582 thickness between the craton and the mobile belt along the length of the Kenya Rift. Major crustal thinning 583 occurs along the axis of the Kenya Rift where the crustal thickness varies from 35 to 40 km in the south 584 beneath the central part of Kenya, within the vicinity of Lake Naivasha, to 18 -20 km in the north beneath 585 Lake Turkana. Therefore, the observed changes in fractal dimension of displacement distributions for the 586 three zones could also be due to variations in the crustal thickness of this region. However, the 587 abovementioned results may suggest more simply that rift zone 3 in the south is in a less mature stage than 588 rift zone 2 in the centre, and zone 2 is less developed than rift zone1 in the northern part of the study area. 589 This phenomenon of northward increase in continental Rift evolution was also observed in the North 590 Ethiopian Rift-Afar transition area (Soliva and Schultz, 2008) and the Main Ethiopian Rifts (Agostini et al., 591 2011). These inferences suggest that the processes of progressively increasing fault system maturity and 592 strain localization onto large faults could happen even over relatively small spatial scales (as small as this 593 study area, 240 x 150 km) within the same rift system.

594 In contrast to fractal dimensions of fault displacement populations (Figure 11) that decrease with increasing 595 strain, the power law distribution of fault length populations exhibit fractal dimensions of 1.4 (Figure 13), a 596 value which stays almost constant in the three zones despite increasing strain along the rift (Figure 9 & 597 Table 1). Previous studies of fault linkage suggest that fractal dimension decreases systematically with 598 increasing fault strain (e.g. Sornette et al., 1993, Cartwright et al., 1995, Cladouhos and Marrett, 1996). Such 599 stabilization of the fractal dimension of trace-length populations was interpreted by Poulimenos (2000) to 600 imply that linkage cessation is an important process for the evolution of the fault population over the 601 observed range of strains.

The observed relationship between the fractal dimension and strain for fault scaling properties is illustrated in Figure 14, which may suggest that the fractal dimensions of fault population length is independent of strain. In other words, the trace-length distribution is independent of strain and the increasing strain has no effect on the fractal dimension of the fault length population.

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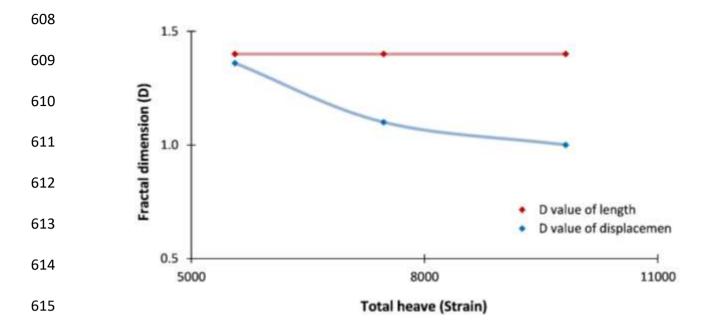


Figure 14. Illustration showing the observed relationship between the fractal dimension (D) and total heaves that represent strain for fault size attributes. Here, the D value of displacement
 population decreases with increasing strain, whereas the D value of length population remains almost constant as strain increases.

619 This would mean that with increasing strain, fault displacement increases, but fault lengths remain near 620 constant. Moreover, these inferences support the observation of the vertical spread in the displacement 621 population noticed in each zone of the study area (Figure 6 b, c, d). In this regard, this is consistent with the 622 view that faults typically grow by steep or vertical growth trends rather than progressive increases both in 623 displacement and in length (Walsh et al., 2002a, Nicol et al., 2010, Rotevatn et al., 2019). Similarly, vertical 624 growth trends have also been observed in a natural normal fault system in the Timor Sea (Walsh et al., 2002a) and in analogue modelling (Schlagenhauf et al., 2008). Vertical growth trends like these require that, 625 626 after initial rapid propagation, faults do not grow significantly in length (Walsh et al., 2002a, Nicol et al., 627 2010, Rotevatn et al., 2019). Therefore, these inferences are in line with the alternative/ coherent/ constant-628 length fault growth model suggested in previous studies (Walsh et al., 2002a, Walsh et al., 2003a, Childs et 629 al., 2009, Giba et al., 2012, Jackson and Rotevatn, 2013, Rotevatn et al., 2019, Jackson et al., 2017, Nicol et 630 al., 2016). This model has recently been referred to as the coherent constant-length model (Nicol et al., 631 2020). In that model, faults grow by rapidly establishing their near-maximum fault length in an early phase 632 of deformation followed by accumulation of displacement with limited fault tip propagation. In this model, when strain fields of nearby isolated faults start to overlap and interact, as fault interactions are an essential 633 634 feature of all fault systems (Walsh and Watterson, 1991), we see the instantaneous increase in fault length 635 achieved by the coalescence and linkage of previously isolated faults (Walsh et al., 2002a, Rotevatn et al., 636 2019). The linked faults then begin to accrue displacement with no or little fault lengthening (Cartwright et al., 1995). This process will result in the creation of large localized faults. It has been mentioned above that
the process of fault growth through segment linkage is an important factor to cause scatter in maximum
displacement-length data (e.g. Cartwright et al., 1995, Mansfield and Cartwright, 2001). Therefore,
segmented fault geometries could be responsible for the scatter in this dataset, which complicates the
establishment of any scaling law.

The rapid growth of fault length to near-maximum in the early stages of rifting has also been observed further north in the Turkana Rift, north Kenya by Vétel et al. (2005) using fault displacement and length data derived from outcrop studies, and digital elevation models. Moreover, the fault growth model is found to be a dominant behaviour of normal fault growth in many extensional settings (e.g. Walsh et al., 2002a, Walsh et al., 2003a, Giba et al., 2012). Therefore, the coherent constant-length model appears to be the most plausible scenario for the mode of normal fault growth in the study area.

648 A study by Poulimenos (2000) in the active basin of the western Corinth Graben of central Greece, and 649 another study by Meyer et al. (2002) in the Vulcan Sub-basin of the Timor Sea, northwest Australia 650 examined fault growth of normal faults using fractal dimension analysis of fault size populations. Both 651 studies reached a similar conclusion to the current one, where fault lengths were established early during 652 extension of the basin and a later extension was largely accommodated by accumulation of displacements 653 with minimal fault propagation. However, those studies could not establish the generality of their findings 654 due to lack of detailed studies of the growth of fault populations with which their conclusions can be 655 compared. Thus, having compared the current study with those studies, it can be concluded that, in active extensional setting, fractal dimension analysis appears to be a useful factor to describe the displacement-656 657 length relationship in case the high scatter in displacement-length does not help in understanding the growth 658 of normal faults.

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666 6 Conclusion

620 normal faults have been mapped from ASTER DEM surface data within the central Kenya Rift. Fault 667 trace lengths were corrected for resolution bias, and the extent of total fault throw into the subsurface was 668 669 estimated. The maximum displacement was therefore calculated using an average dip value for the study 670 area. Three fault populations have been identified within the study area according to their average fault strike 671 as zone 1 in the north, zone 2 in the centre & zone 3 in the south. The wide scale range of fault size populations (maximum displacement of $\sim 40 - \sim 6030$ m; lengths of 1270 m to 60600 m) contained within 672 673 the data, allowed quantitative assessment of the scaling properties of the three fault populations, in order to 674 inform our understanding of the growth of normal faults. Estimations of extensional strain obtained from 675 six transects along the rift revealed a general increase of strain northward. Fault displacement data, analysed 676 by the cumulative frequency, obey a power-law distribution for the three zones of fault populations with 677 fractal dimension D of 1.0, 1.1 &1.4 for zone 1, zone 2 and zone 3 respectively. Fault trace-length data also 678 conform to the same power-law relationships, but with D Values of ~1.4 for all three zones. Values of fractal 679 dimension of displacement distribution for the three zones showed a decrease with increasing strain as we 680 move from the south (zone3) through the centre (zone2) to the north (zone1) along the rift, which implies 681 that the strain is increasingly localised onto larger faults as the fault system evolves. In addition, values of 682 fractal dimension of fault length distributions remained almost unchanged in the three zones even with 683 increasing strain. Increasing fault displacement whilst the length remains almost fixed with increasing strain 684 along the study area may suggest that the fault system could be evolving in accordance to the coherent constant-length fault growth model. Therefore, findings of this study suggest that the evolution of rift 685 686 deformation, can be observed even over relatively short spatial scales. It has also been concluded that 687 patterns of fault growth can be deduced from fractal dimension of cumulative distribution of fault size 688 populations.

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