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Article

Application of Density Plots and Time Series Modelling to the Analysis of Nitrogen Dioxides Measured by Low-Cost and Reference Sensors in Urban Areas

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Abstract: Temporal variability of NO₂ concentrations measured by 28 Envirowatch E-MOTEs, 13 AQMesh pods, and eight reference sensors (five run by Sheffield City Council and three run by the Department for Environment, Food and Rural Affairs (DEFRA)) was analysed at different time scales (e.g., annual, weekly and diurnal cycles). Density plots and time variation plots were used to compare the distributions and temporal variability of NO₂ concentrations. Long-term trends, both adjusted and non-adjusted, showed significant reductions in NO₂ concentrations. At the Tinsley site, the non-adjusted trend was -0.94 (-1.12 , -0.78) $\mu\text{gm}^{-3}/\text{year}$, whereas the adjusted trend was -0.95 (-1.04 , -0.86) $\mu\text{gm}^{-3}/\text{year}$. At Devonshire Green, the non-adjusted trend was -1.21 (-1.91 , -0.41) $\mu\text{gm}^{-3}/\text{year}$ and the adjusted trend was -1.26 (-1.57 , -0.83) $\mu\text{gm}^{-3}/\text{year}$. Furthermore, NO₂ concentrations were analysed employing univariate linear and nonlinear time series models and their performance was compared with a more advanced time series model using two exogenous variables (NO and O₃). For this purpose, time series data of NO, O₃ and NO₂ were obtained from a reference site in Sheffield, which were more accurate than the measurements from low-cost sensors and, therefore, more suitable for training and testing the model. In this article, the three main steps used for model development are discussed: (i) model specification for choosing appropriate values for p , d and q , (ii) model fitting (parameters estimation), and (iii) model diagnostic (testing the goodness of fit). The linear auto-regressive integrated moving average (ARIMA) performed better than the nonlinear counterpart; however, its performance in predicting NO₂ concentration was inferior to ARIMA with exogenous variables (ARIMAX). Using cross-validation ARIMAX demonstrated strong association with the measured concentrations, with a correlation coefficient of 0.84 and RMSE of 9.90. ARIMAX can be used as an early warning tool for predicting potential pollution episodes in order to be proactive in adopting precautionary measures.



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Keywords: ARIMA; ARIMAX; air quality modelling; low-cost sensors; air pollution; nonlinear modelling; time series analysis; autoregressive; moving average; Sheffield

1. Introduction

Air pollution is one of the most serious environmental threats to health, killing 6.4 million people in 2015 worldwide both in developed and less-wealthy nations [1]. Out of these, 2.8 million deaths were caused by indoor air pollution and 4.2 million deaths by outdoor air pollution. Air pollution is causing various health problems including respiratory problems, cardiovascular diseases, lung cancer and asthma [2]. Walters and Ayres [3] have also reported that air pollution, especially particulate matter and nitrogen dioxide (NO₂) pollution, may cause premature deaths and hospital admissions for conditions such as cardiovascular problems, allergic reactions and lung cancer. It is reported that exposure to air pollution is particularly harmful for children, people with existing health problems and the elderly [4–6]. Evidence suggests that the negative impacts of air pollution are dependent on the levels of air pollutants and length of exposure, higher levels and longer

exposure resulting in more severe adverse effects [3,6]. Furthermore, air pollution may reduce visibility, damage historical buildings and monuments, affect vegetation and reduce crop yield and quality [4–7].

Air quality modelling is carried out for several purposes, including air quality prediction, quantifying the impacts of air pollution, modelling the impacts of various factors on air pollution, modelling pollution processes and transport, running and testing emission scenarios, modelling the dispersion of air pollutants in the atmosphere, quantifying the emissions of air pollutants from various emission sources, determining long-term trends in air pollutant concentrations and producing high-resolution spatiotemporal maps of air pollution [6–15]. In this study, the main purposes were to compare the performance of different time series models and to develop a time series model for predicting future NO₂ concentrations in Sheffield, UK. Time series models are one of the popular tools for predicting the future by understanding the past changes in air pollution concentrations [16].

Time series modelling is a useful tool for data analysis and has several benefits, which include data cleaning, data understanding and forecasting [17]. Time series modelling can help us filter out the noise and reveal the true signal in a dataset. Once a dataset is cleaned and the time series is divided into its different components, it helps us understand the true nature of the dataset. Finally, like other modelling approaches, time series modelling helps us predict future levels with the help of present and past levels of the time series (here NO₂ concentrations) [17]. To build a time series model the time series data must be stationary. For a time series to be stationary, the mean, variance and covariance of the time series should not be a function of time [18]. If the time series is not stationary, it should be stationarised first before fitting a model to it [18]. To stationarise a time series, it should be detrended and deseasonalised using differencing and power transformations [16]. A time series model can be linear or nonlinear depending on the relationship between current and past observations [16]. The Autoregressive (AR) and moving average (MA) models are the two widely used linear time-series models [19]. The AR and MA models can be combined to form the autoregressive moving average (ARMA) and autoregressive integrated moving average (ARIMA) models [20]. To model and predict a seasonal time series, the seasonal autoregressive integrated moving average (SARIMA) model is used, which is a variation of ARIMA [19]. ARIMA along with its various variations are also known as the Box–Jenkins models because they are based on the Box–Jenkins principle [19]. Classification of time series models is shown in Figure 1 [21–23].

Although air pollutant levels have decreased in the UK and Europe during the last decade or so, some air pollutant levels still exceed air quality standards in many urban areas [24] and 620 air quality management areas (AQMAs) have been declared across the UK [25]. Out of these areas, five cities (Birmingham, Leeds, Southampton, Derby and Nottingham) will not achieve the targets until 2025 and London will not comply until 2030 if additional control measures are not taken [24]. Most of the exceedances are due to the high levels of NO₂ and PM₁₀ [26], emphasising that these air pollutants are a serious problem in urban areas. Further actions are required to cut emissions and understand the main drivers of high levels of NO₂ and PM₁₀ in urban areas. Air pollution modelling is a part of these actions.

In first part of this article, NO₂ concentrations measured by different grades of sensors are compared graphically, whereas, in the second part, a comparison of time series modelling approaches is made using measured time series data of NO₂ collected at an urban monitoring site in Sheffield. A comparison is made between linear and nonlinear time series models and the better performing model is then compared with the ARIMAX model, which, in addition to persistence, uses exogenous variables. The aim is to assess the suitability of time series models for NO₂ prediction and choose the best time series model for air quality modelling in the urban environment.

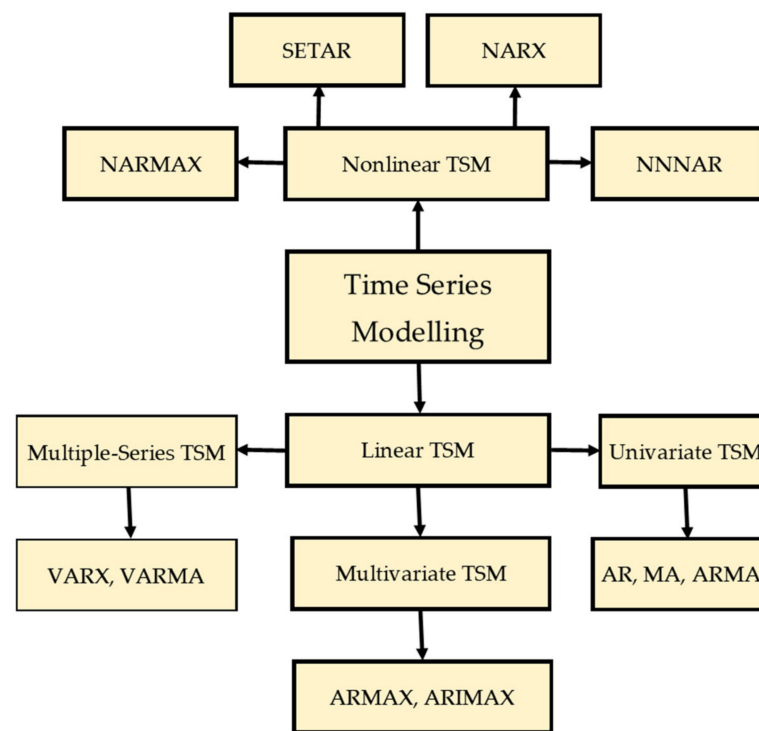
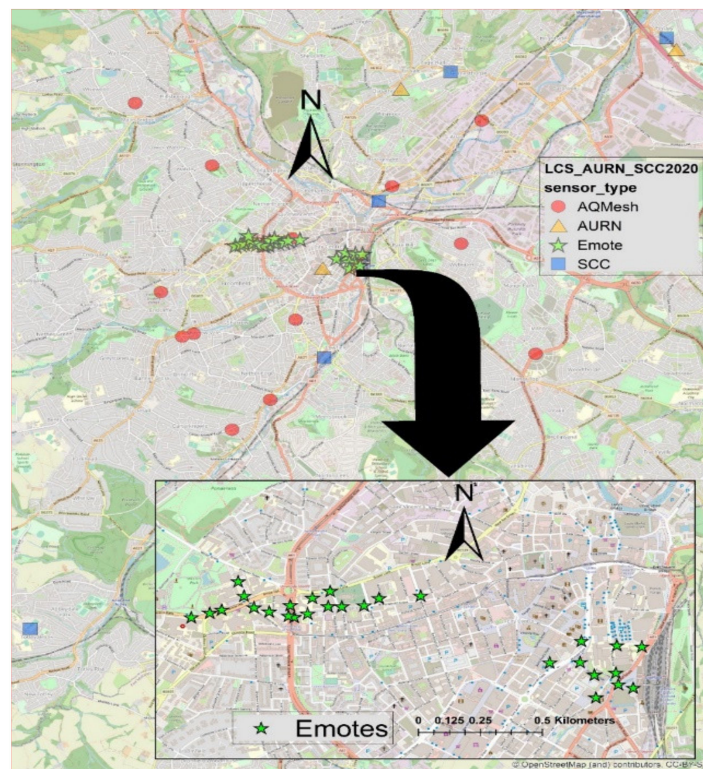


Figure 1. Classification of time series models. TSM, time series model; AR, autoregressive; MA, moving average; ARMA, autoregressive moving average; ARMAX, autoregressive moving average with exogenous variables; ARIMAX, autoregressive integrated moving average with exogenous variables; VARX, vector autoregressive with exogenous variables; VARMA, vector autoregressive moving average; NARX, nonlinear autoregressive with exogenous variables; NARMAX, nonlinear autoregressive moving average with exogenous variables; SETAR, self-exciting threshold autoregressive; NNNAR, neural network nonlinear autoregressive.

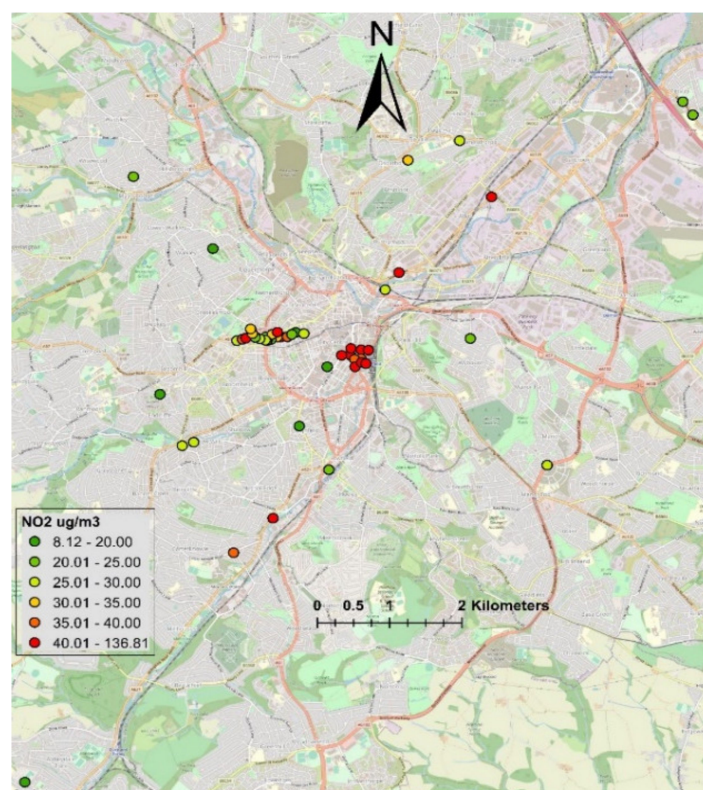
2. Methodology

2.1. A Brief Description of the Monitoring Network

In this study, NO_2 concentrations ($\mu\text{g}/\text{m}^3$) from a network of low-cost sensors (LCSs) and reference sensors were analysed in Sheffield, United Kingdom. A network of LCSs was made by the Urban Flows Observatory, University of Sheffield, UK, consisting of 28 Envirowatch E-MOTEs and 13 AQMesh pods. These are all urban traffic sites. In addition, five reference air quality monitoring stations are operated by Sheffield City Council (SCC) and three are operated by the UK Department for Environment, Food and Rural Affairs (DEFRA), which are part of the Automatic Urban and Rural Network (AURN), the largest air quality monitoring network in the UK. The locations of the air quality monitoring stations (AQMSs) are shown in Figure 2 and their names, coordinates and annual mean NO_2 concentrations are given in Table 1. Data from these sensors were analysed from August 2019 to September 2020.



(a)



(b)

Figure 2. (a) The locations of air quality monitoring stations (AQMSs) in Sheffield; (b) annual mean NO₂ levels ($\mu\text{g}/\text{m}^3$) measured by low-cost sensors (LCSs) and Automatic Urban and Rural Network (AURN) and Sheffield City Council (SCC) AQMSs in Sheffield from August 2019 to September 2020.

Table 1. Names, IDs and annual mean NO₂ concentrations (µg/m³) measured by low-cost sensors (AQMesh and Envirowatch E-MOTEs) and AURN and Sheffield City Council sites from August 2019 to September 2020.

Site Name	Sensor Type	Sensor ID	NO ₂ (µg/m ³)
Brightside Lane	AQMesh	2003150	41.3
Saville Street	AQMesh	2005150	46.9
Cundy Street	AQMesh	2007150	19.8
off Endcliffe Crescent	AQMesh	2008150	12.7
Sharrow Vale Rd	AQMesh	2009150	25.1
Abbeydale Rd	AQMesh	2450206	43.7
London Rd	AQMesh	2001150	14.6
Prince of Wales Rd	AQMesh	2006150	28.2
Maltravers Rd	AQMesh	2004150	20.8
Hunter's Bar School	AQMesh	2450204	29.0
Malin Bridge PS	AQMesh	1999150	22.6
Broad Lane	AQMesh	1998150	19.2
Carter Knowle Bridge	AQMesh	2450205	37.6
Tinsley	AURN	SHE	22.9
Devonshire Green	AURN	SHDG	19.1
Barnsley Road	AURN	SHBR	32.1
Regent Court, E-camp	E_MOTE	711	41.7
Leavygreave Road, E-camp	E_MOTE	712	34.2
Gell Street, E-camp	E_MOTE	701	21.1
Upper Hanover/Henderson's building	E_MOTE	702	28.7
Behind Jessop West	E_MOTE	703	23.7
Diamond/Bio-incubator	E_MOTE	704	34.2
Broad Lane/St George's Terrace	E_MOTE	713	44.9
Portobello Street, Mappin Street	E_MOTE	714	37.6
28 Portobello Street, EC	E_MOTE	705	20.8
Howard Street, CC	E_MOTE	731	41.2
Arundel Gate/Genting Club	E_MOTE	732	115.6
Arundel Gate/Surrey Street	E_MOTE	733	43.5
Harmer Lane/Pond Street	E_MOTE	901	44.2
Harmer Lane/Sheaf Street	E_MOTE	902	49.9
Pond Street/Sheaf Building	E_MOTE	736	38.3
Howard Street/Science Park	E_MOTE	734	39.0
Paternoster Rows	E_MOTE	735	42.4
Sheaf Street/Sheaf Square	E_MOTE	903	107.2
Railway Station Taxi rank	E_MOTE	904	136.8
Upper Hanover St/Info. Commons	E_MOTE	707	26.6
Leavygreave Road/Favell Road	E_MOTE	708	25.7
Hounsfield Rd/Hicks Building	E_MOTE	709	24.9
Sheffield Children's Hospital	E_MOTE	710	28.2
Robert Hadfield Building	E_MOTE	706	25.2
Brook Hill/Firth Court1	E_MOTE	737	39.3
Brook Hill/Firth Court2	E_MOTE	738	42.9
Arts Tower Concourse	E_MOTE	739	34.3
Arts Tower Concourse/Library	E_MOTE	740	33.2
Firvale	SSC	GH1	25.0
Tinsley	SSC	GH2	24.1
Lowfield	SSC	GH3	24.6
Wicker	SSC	GH4	25.9
King Egbert	SSC	GH5	8.1

LCSs are compact, portable and use less power when compared to reference instruments. LCSs range in price from a couple of thousand to several thousand pounds (for a relatively sophisticated multi-pollutant and meteorological sensor with communication capabilities). Reference sensors are expensive, both to purchase and maintain, and bulky, but are the most accurate units, recommended for use by EU and UK government bodies

for air quality (AQ) monitoring and complying with standards such as MCERTS in the UK. A single reference unit costs in the region of 20,000 pounds to monitor a single gaseous or particle pollutant. LCSs and reference sensors employ different techniques for air pollutant measurement, which include optical particle counters, light scattering, metal oxide semiconductor sensors, electrochemical sensors, nondispersive infrared sensors, ultraviolet fluorescence, chemiluminescence, infrared photometry and photo-ionisation detection sensors. For more detail, see [27,28]. The LCSs used in this project were either Envirowatch E-MOTEs [29] or AQMesh pods [30]. The Envirowatch E-MOTEs are deployed in a local mesh in a cluster, providing data via ZigBee, within a certain area for high-resolution monitoring, no more than 100 m from each other, with a gateway providing an uplink capability. AQMesh sensors are independent and can be deployed at both high and low spatial resolutions. Both Envirowatch E-MOTEs and AQMesh pods are electrochemical sensors, whereas the sensors used by DEFRA and SCC are reference sensors which use chemiluminescent analysers for NO₂ and an ultraviolet (UV) absorption analyser for O₃ measurements. The reference sensors are more reliable and accurate than the electrochemical sensors. The lowest detection limit for reference sensors and electrochemical sensor is <2 µg/m³. Electrochemical sensors are smaller and cheaper to purchase and maintain. Envirowatch E-MOTEs in a cluster communicate with a gateway by means of the Zigbee protocol within a specific area for high-resolution monitoring. The use of this protocol allows the individual units to communicate with each other and pass data from sensors that are not in range or without line-of-sight of the gateway. Using GPRS, the gateway device communicates the collected data over an internet connection to a cloud server operated by Envirowatch. Each AQMesh pod independently sends data to a cloud server using GPRS. For the reference sensors, the data logger is connected to the central management and coordination unit (CMCU) central computer, which collects the data using a GPRS mobile phone connection or wireless broadband.

2.2. Comparing NO₂ Measured at Different Sites

In this study, we compared NO₂ concentrations measured at different AQMSs using LCSs and reference sensors from August 2019 to September 2020. For inter-site comparison, density plots and time variation plots were used, which were developed in R programming language [31] using the “openair” package [32]. Density plots, also known as kernel density estimation (KDE) plots, showed the distribution of NO₂ concentrations and are smoothed versions of histograms. The peaks of density plots show where values of the variables are concentrated. Furthermore, time variation plots were developed to show the temporal variability in NO₂ concentrations over different temporal scales; especially, they depict the diurnal, weekly and annual cycles of NO₂ concentrations.

2.3. Long-Term Temporal Trend Analysis

Quantification of temporal trends in air pollutant concentrations serves to assess the effects of emission control strategies over a given period of time. In this study, the temporal trend of NO₂ concentrations was determined over the last 20 years (2000–2019) at the Tinsley AQMS, which is part of the UK AURN. This is an urban background site located at the Sheffield Tinsley Community Centre, approximately 200 metres east of the M1 motorway. The temporal trend was also determined at the Devonshire Green AQMS from 2014 to 2019, an urban background site, installed in Devonshire Green Park in Sheffield within a self-contained air-conditioned unit, surrounded mainly by open land and vegetation. To calculate long-term trend in NO₂ concentrations, here we employed the TheilSen function of the “openair” package [32]. The TheilSen function is a non-parametric approach and uses bootstrap simulations. This technique estimates all the regression parameters through bootstrap resampling. The technique is not affected by outliers as it is based on the median (not mean) and can be applied to a non-normal distribution.

2.4. Time Series Model

To carry out time series modelling in this study, NO₂, NO and O₃ data were used from the Devonshire Green AQMS in Sheffield. The site is part of the AURN network and has been monitoring various air pollutants, including NO₂, NO, NO_x and O₃, since 2013. Figure 3 shows the monthly average of pollutants, which exhibits a general trend of higher NO, NO₂ and NO_x concentrations in winter and lower concentrations in summer. In contrast, O₃ concentrations were higher in spring and summer and lower in winter. In winter the atmosphere is relatively static and the atmospheric boundary layer is shallower, which is a hindrance in pollutant dispersions; whereas, in summer, the atmosphere is more turbulent and both horizontal and vertical dispersion processes are active in dispersing locally emitted pollutants. This is probably the main reason that the concentrations of NO, NO₂ and NO_x were lower in summer and higher in winter. On the other hand, ground level O₃ is a secondary pollutant and is produced by the photochemical reactions of NO_x and volatile organic compounds (VOCs) in the presence of solar radiation. In summer, high temperature and solar radiation lead to higher levels of O₃ production than in winter, when the weather in the UK is cold, not conducive to O₃ formation. O₃ concentration was highest in May, when in addition to the weather conditions, O₃ precursors were abundant, in contrast to June and July when the precursors were relatively lower [33].

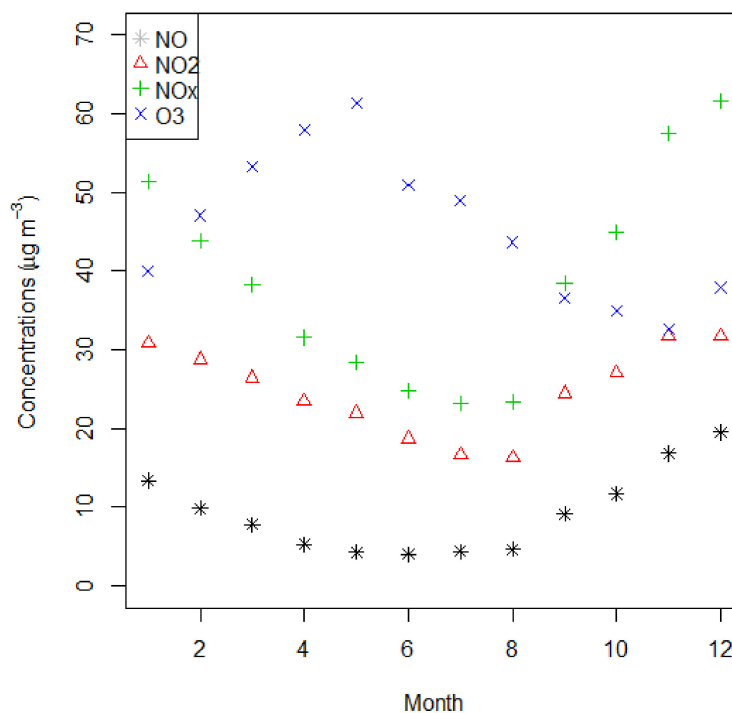


Figure 3. Monthly average concentrations ($\mu\text{g}/\text{m}^3$) of NO, NO₂, NO_x and O₃ in different months of the year from the Devonshire Green AQMS in Sheffield, 2014–2019.

Time series data mainly have three building blocks: seasonality, trend and residuals [34]. Deconstruction (decomposition) of a time series is helpful in understanding the behaviour of a time series. The seasonality (seasonal component) of the time series refers to the fluctuations in the levels of pollutants related to seasonal factors. Seasonality is always of a fixed and known period, normally twelve months. The trend component is the overall long-term pattern of the time series and indicates if a pollutant concentration is increasing or decreasing over time. The residual or error component of the time series is the remainder part that cannot be attributed to seasonality and trend components. The three components of the time series are shown below in Equation (1):

$$Y = T_c + S_c + R_c \quad (1)$$

In Equation (1), a time series (Y) is divided into three components, which are the trend component (T_c), seasonal component (S_c) and residual or remainder component (R_c). For dividing the time series into three components, seasonal-trend decomposition based on loess (STL) was used, which was initially proposed by Cleveland et al. [35]. The process of extracting these components from the time series is referred to as decomposition. The three components of the NO_2 time series are shown in Figure 4.

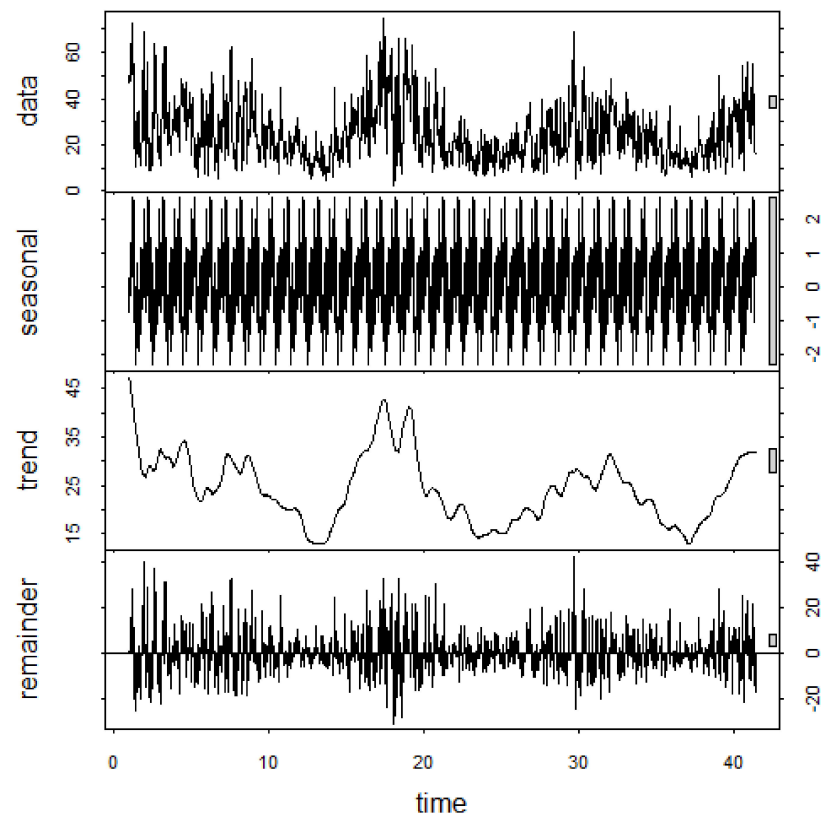


Figure 4. Three additive components obtained from seasonal-trend decomposition based on loess (STL), decomposition of NO_2 concentration ($\mu\text{g}/\text{m}^3$) collected at the Devonshire Green AQMS, Sheffield.

In this study, air pollution data were analysed using four time series models: ARIMA, ARIMAX, the self-exciting threshold autoregressive (SETAR) and neural network nonlinear autoregressive (NNNAR). For more details on these models, see [36–38]. Time series model development and application consist of three main steps [39]:

- model specification;
- model fitting (parameters estimation); and
- model diagnostic (testing the goodness of fit of the fitted model).

2.4.1. Model Specification

Model specification means choosing appropriate values for p , d and q for a given time series, where p is the lag orders (i.e., the number of lagged values that NO_2 is regressed on), referred to as the autoregressive component, d is the degree of differencing (integration) and q is the order of moving average. Differencing a series involves simply subtracting its current and previous values' d times. Often, differencing is used to stabilize a series when the stationarity assumption is not met. For model specification (to specify the values of p , d and q), firstly, the auto-correlation function (ACF) and partial auto-correlation function (PACF) plots of the NO_2 time series were used. The ACF plot (Figure 5a) displays correlation between a series and its lags (previous values) and helps determine the order of differencing (d). Furthermore, the ACF plot can help in determining the order of the MA component. An MA component represents the error of the model as a combination of

previous error terms [39]. The order q determines the number of terms to be included in the model. The ACF plot of the NO₂ series (Figure 5a) shows the properties of a nonstationary series, as the ACF fails to die out rapidly with increasing lags. All ACF values are significant (significantly greater than zero) and the only pattern is perhaps a linear decrease with increasing time lag. This shows that NO₂ series is nonstationary. Before a time-series model (e.g., the ARIMA model) is applied, the time-series must be stationarised, which means the variance, mean and auto-covariance of the time series need to be time invariant. The ACF plots of the NO₂ series differenced once and twice are presented in Figure 5b,c, respectively. After differencing once, the pattern emerged much more clearly, suggesting that the ARIMA model with difference 1 ($d = 1$) was probably a suitable model.

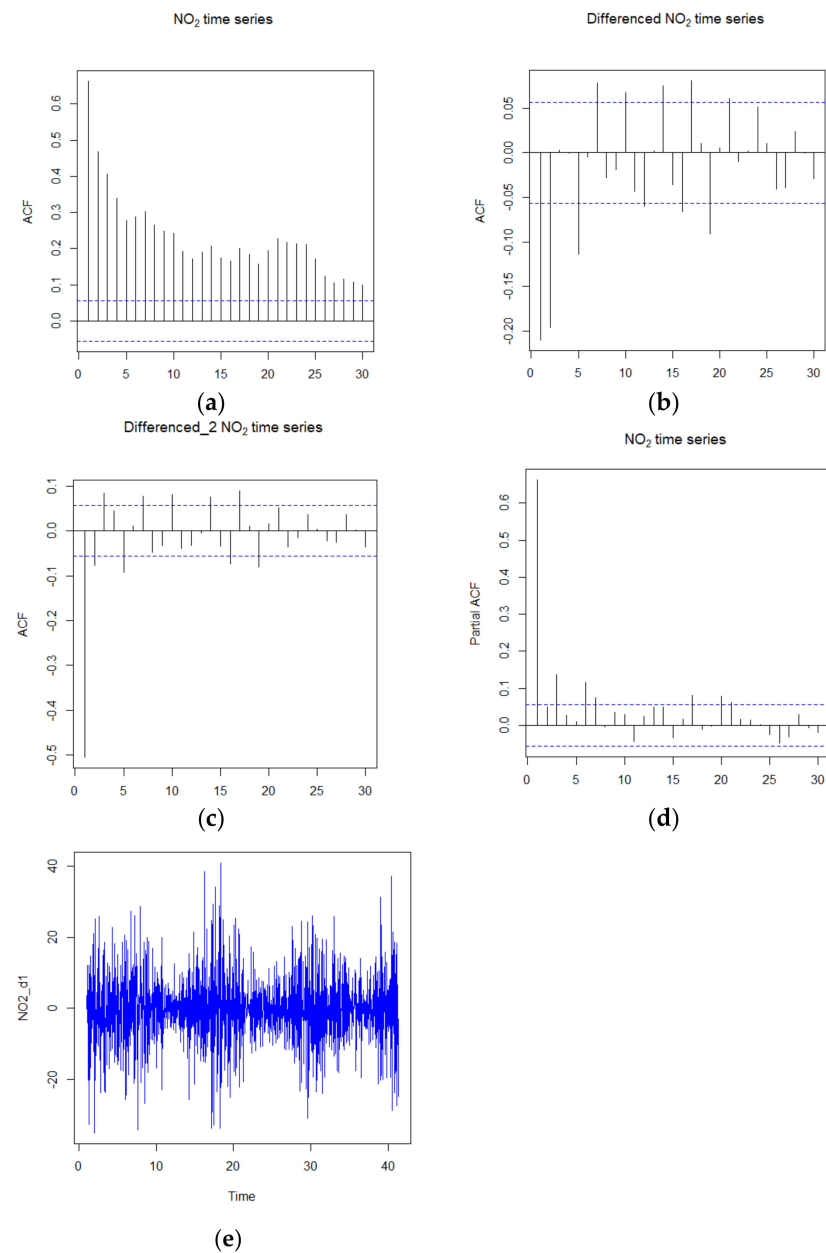


Figure 5. Auto-correlation function (ACF) plot of the NO₂ ($\mu\text{g}/\text{m}^3$) time series (not differenced) (a), differenced once (b) and differenced twice (c); partial ACF plot (d) and once-differenced NO₂ plot of oscillating pattern around zero with no visible strong trend (e) showing that the series is stationary. NO₂ concentrations used here were collected at the Devonshire Green AQMS, Sheffield.

The PACF plot (Figure 5d) displays the correlation between a variable and its lags that is not explained by previous lags. PACF plots are useful when determining the order p of the AR component, which specifies the number of lags used in the model; for example, AR (2) or ARIMA (2,0,0) showed that the order of AR was 2. The PACF plot showed that an AR (1) model should be considered (Figure 5d). The plot of differenced NO_2 is shown in Figure 5e, wherein the oscillating pattern around the zero shows that the series was stationary after the series was differenced once. This suggested that differencing of order 1 terms is sufficient and should be included in the model. Sometimes, if the series is not stationarised after differencing once, we need to difference it again. In addition to the ACF and PACF plots, we also considered model selection criteria based on the value of the Akaike's information criterion (AIC). The time series model with a lower value for the AIC showed a better fit. Based on the AIC values (Table 2), ARIMA (1,1,1) was selected. Differencing, autoregressive and moving average components make up an ARIMA model. ARIMA (1,1,1) showed that the model incorporated differencing of degree 1 and used an AR term of first lag and an MA of order 1. Although some of the other models (Table 2) had slightly lower AIC values, the difference was not significant and the model was more complicated, which is against the principle of parsimony, meaning that the selected model should use the lowest number of parameters providing adequate representation of the time series. When the ARIMA (1,1,1) model was applied to the square root and log of the NO_2 time series in contrast to observed NO_2 concentrations, the AIC values dropped to 3230.6 and 1117.5, respectively, which are much lower than the values presented in Table 2. Therefore, log- NO_2 was adopted in this study instead.

Table 2. Autoregressive integrated moving average (ARIMA) model specification and corresponding Akaike's information criterion (AIC) values of NO_2 time series ($\mu\text{g}/\text{m}^3$), where p represents the order of the autoregressive, d represents the difference and q represents the MA.

AIC	p	d	q
8910.88	1	1	1
9104.28	1	2	1
8910.53	2	1	1
8912.42	2	1	2
8944.8	1	0	0
8941.53	1	0	1
8904.29	3	1	1
8905.83	4	1	1

2.4.2. Model Fitting

Model fitting is basically parameter estimation. This study used the maximum likelihood estimation approach, which produces more accurate estimation of parameters in comparison to least square estimation [39]. The main advantage of the maximum likelihood estimation is that it uses all of the information in the data rather than just using the mean and variance of the data, as is the case with least square estimation [39]. Using daily NO_2 concentrations (2015 to 2019), the dataset was divided into training (70%) and testing (30%) datasets, which were selected randomly. Time series linear models were fitted (trained) with the TSA-package [40] and forecast-package [41] in R programming language [31]. The neural network nonlinear autoregressive and self-exciting threshold autoregressive (SETAR) nonlinear models were implemented in R-package "tsDyn" [38]. The model performance was assessed using both training and testing datasets. The specified models were run to estimate the model parameters.

2.4.3. Model Diagnostic and Forecasting

Residuals of a model are defined as the difference between the actual (observed) and predicted (modelled) values, as shown in Equation (2):

$$\text{Residual} = \text{Actual values} - \text{Predicted values} \quad (2)$$

Residual analysis of the model was performed by graphical presentation using a plot of standardised residuals, a quantile–quantile (Q–Q) plot and a histogram of the residuals. For an adequate model, a plot of standardised residuals shows a rectangular scatter around a zero horizontal level with no trends, whereas a Q–Q plot and histogram of the residuals show the normality of the error terms.

The model performance was assessed by comparing predicted with observed NO₂ concentrations both graphically, using time plots and scatter plots, and using several statistical metrics, including correlation coefficients (r), root mean square error (RMSE), factor of two (FAC2), mean biased error (MBE) and mean absolute error (MAE) [42,43]. The Pearson correlation coefficient measures the strength of the linear relationship between the measured and modelled concentrations. FAC2 is the fraction of predicted concentrations within a factor of two of the measured concentrations. RMSE, MAE and MBE provide an estimation of the error of the model prediction. However, RMSE and MAE do not define the direction of the error, as they provide absolute error, whereas MBE, in addition to the size, defines the direction of the error; i.e., negative MBE indicates under-prediction whereas positive MBE indicates over-prediction of a model.

The fitted model was used to predicted NO₂ concentrations, which were cross-validated with the testing dataset. If the predicted value (forecast) is denoted by $\hat{Y}_t(l)$, where l is the lead time for forecast and time t is the forecast origin, then forecasting one time-unit into the future (one step ahead) ($\hat{Y}_t(1)$) can be achieved as in Equation (3) (Cryer and Chan, 2008):

$$\hat{Y}_t(1) = \mu + \phi (Y_t - \mu) \quad (3)$$

where μ is the intercept and ϕ is the estimated parameter of the AR component. Equation (3) shows that, to forecast the next step, a proportion ϕ of the current deviation from the process mean is added to the process mean. To consider a general lead time l , we replace time t by $t + l$ in Equation (3) and take the conditional expectation of both sides, which produces Equation (4) [39]:

$$\hat{Y}_t(l) = \mu + \phi [\hat{Y}_t(l-1) - \mu] \text{ for } l > 1 \quad (4)$$

Equation (4) is recursive in the lead time l and shows how the forecast for any lead time l can be built up from the forecast for a shorter lead time l by starting with the initial forecast as given by Equation (3). The forecast $\hat{Y}_t(2)$ is then obtained from $\hat{Y}_t(2) = \mu + \phi [\hat{Y}_t(1) - \mu]$, then $\hat{Y}_t(3)$ from $\hat{Y}_t(2)$ and so on. Equation (4) is also known as the "difference equation form" of the forecast [39]. An explicit expression for the forecast in terms of the observed history of the time series for Equation (4) can also be given in the form of Equation (5) [39].

$$\hat{Y}_t = \mu + \phi^l (Y_t - \mu) \quad (5)$$

Equation (5) shows that the current deviation from the mean is discounted by a factor ϕ^l , whose magnitude decreases with increasing lead time l . The discounted deviation is then added to the process mean to produce the lead l forecast.

It should be noted that, in forecast, if an exogenous variable is used, then the number of steps ahead are ignored and the number of forecast periods is set to the number of rows of exogenous variables in the new data, which here is equal to the number of rows of the testing dataset.

3. Results and Discussion

3.1. Comparing NO₂ Measured at Different AQMSs

3.1.1. Density Plots

NO₂ concentrations ($\mu\text{g}/\text{m}^3$) measured by different grades of sensors at different monitoring stations in Sheffield were compared employing density plots. Density plots offer an easy way to compare the distribution of NO₂ concentrations measured at different monitoring stations. Figure 6 shows NO₂ concentrations measured by Envirowatch E-MOTEs. The performance of Envirowatch E-MOTEs was assessed by Munir et al. [44] by comparing their concentrations with a nearby reference sensor in Sheffield. The sensors were divided into four sub-groups based on the mean NO₂ concentrations. In first group of sensors (Figure 6a), the range of NO₂ concentrations was 0 to 50 $\mu\text{g}/\text{m}^3$ and the highest density (mode) occurred at 10–15 $\mu\text{g}/\text{m}^3$. This represents the group of sensors with the lowest concentrations, which are deployed outside the city centre at the University of Sheffield campus. The second group (Figure 6b) had mean values of 31–40 $\mu\text{g}/\text{m}^3$ and the highest density was recorded at 20–25 $\mu\text{g}/\text{m}^3$. Most of the sensors in this group had a range of 0 to 60 $\mu\text{g}/\text{m}^3$, however some sensors recorded NO₂ concentrations as high as 120 $\mu\text{g}/\text{m}^3$. The third group (Figure 6c) had mean concentrations of 41 to 50 $\mu\text{g}/\text{m}^3$ and the concentrations ranged from 0 to 140 $\mu\text{g}/\text{m}^3$. These sensors recorded mean values over 40 $\mu\text{g}/\text{m}^3$, exceeding annual air quality standard. The fourth group (Figure 6d) recorded the highest NO₂ concentrations, where mean concentration was greater than 100 ($\text{NO}_2 > 100 \mu\text{g}/\text{m}^3$). The highest density was shown at 70 to 80 $\mu\text{g}/\text{m}^3$. In total, 11 sensors violated AQ standards ($\text{NO}_2 > 40 \mu\text{g}/\text{m}^3$). Three sites with mean NO₂ levels higher than 100 ($\mu\text{g}/\text{m}^3$) were: (i) the Taxi Rank at the Sheffield Railway Station (NO_2_{904} , 136.81 $\mu\text{g}/\text{m}^3$), (ii) Arundel Gate opposite to the Genting Club (NO_2_{732} , 115.56 $\mu\text{g}/\text{m}^3$) and (iii) the pedestrian crossing at Sheaf Street/Sheaf Square (NO_2_{903} , 107.17 $\mu\text{g}/\text{m}^3$). The reason for recording higher NO₂ concentrations is that these sensors are installed next to busy locations in terms of road traffic flows and engine idling while stationary. The taxi stand (E-MOTE 904) is a good example of how engine idling can result in worse air pollution in urban areas. E-MOTE 903 is installed next to a pedestrian crossing on a busy road. People coming out of the train station use the pedestrian crossing going towards the high street, Sheffield Hallam University, and other parts of the city. The traffic light turns red and green regularly, which cause congestions. When the lights are red, road traffics stop but vehicle engines keep running. When traffic lights turn green, all vehicles try to accelerate quickly. Therefore, idling of engine and sudden acceleration emit extra pollution. E-MOTE 732 is installed in a typical street canyon, where the road has tall buildings on both sides, hindering the dispersion of the pollutants emitted by the road traffics, causing the pollution levels to go up. The other sites in the city centre where air quality standards were violated were Paternoster Rows, Harmer Lane near Sheaf Street, Harmer Lane near the bus station, Arundel Gate near Surrey Street, and Howard Street. Two E-MOTEs at the University campus that exceeded air quality limits were Regent Court and Broad Lane (near St. George's Terrace).

The distributions of NO₂ concentrations measured by different AQMesh pods are compared using density plots in Figure 7. Most of the AQMesh pods were deployed in the outskirts of the city (Figure 2). The distribution is mostly skewed right with heavy right tails. Only three AQMesh pods exceeded AQ standards, which were NO_2_{206} (Abbeydale Rd, 43.67 $\mu\text{g}/\text{m}^3$), NO_2_{2003} (Brightside Lane, 41.34 $\mu\text{g}/\text{m}^3$) and NO_2_{2005} (Savile Street, 46.91 $\mu\text{g}/\text{m}^3$). The measurements seem realistic as these sensors are deployed on very busy roadsides.

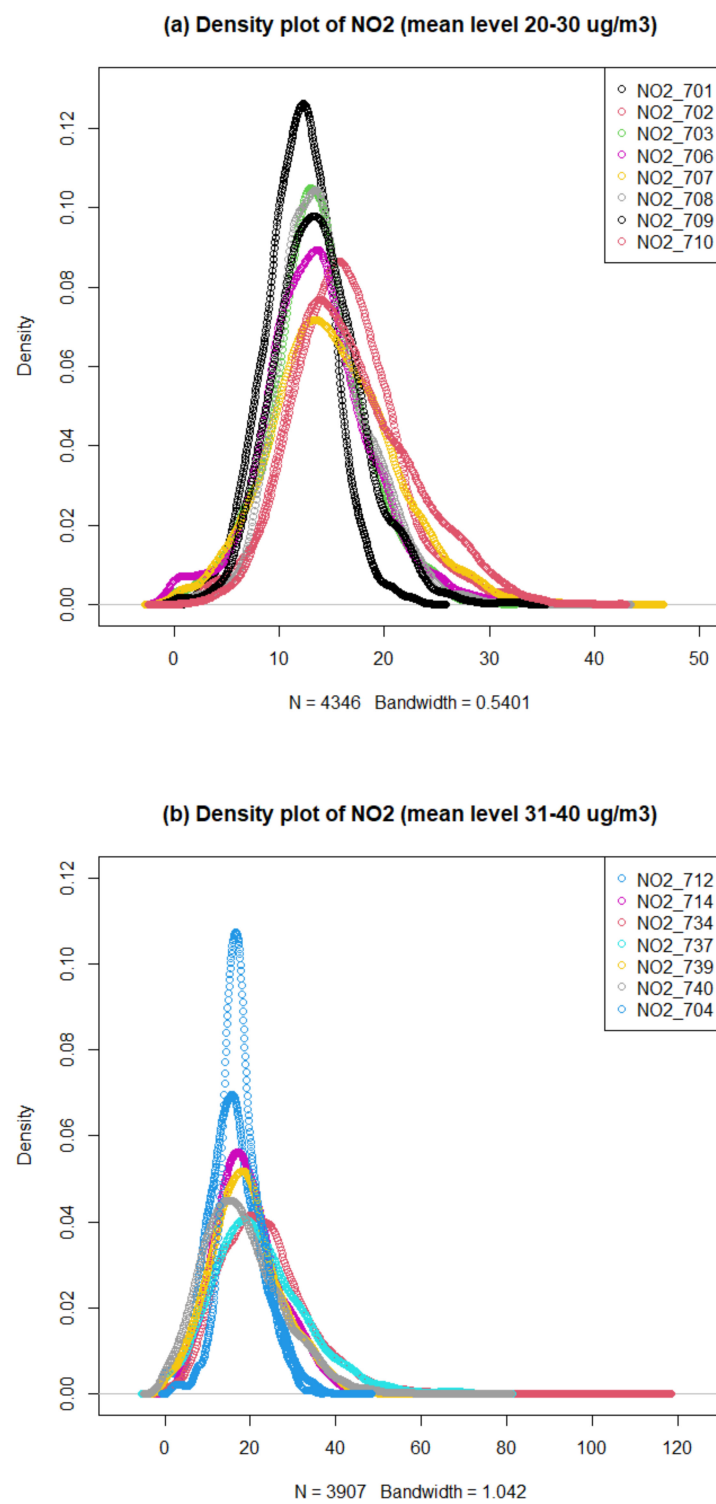


Figure 6. Cont.

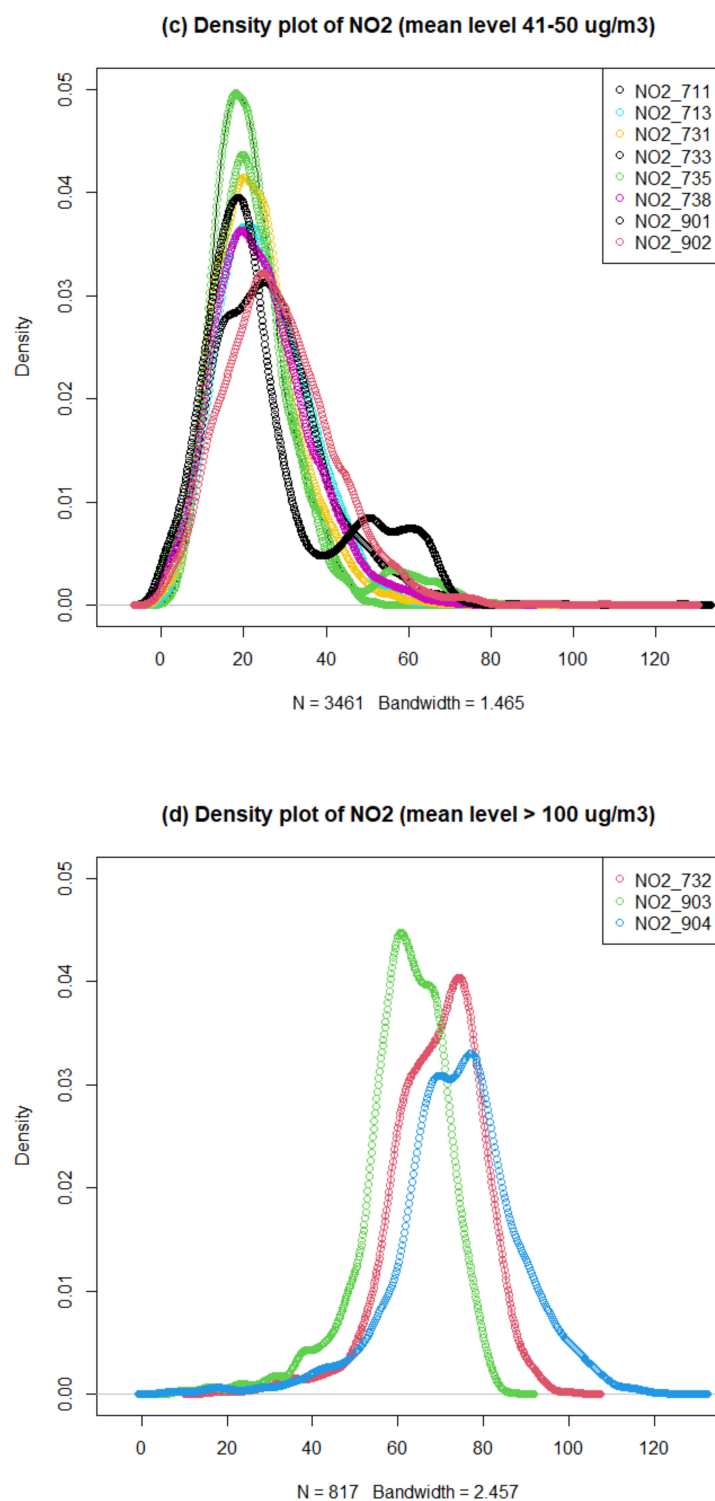


Figure 6. Different density plots of hourly NO₂ concentrations ($\mu\text{g}/\text{m}^3$) measured by Envirowatch E-MOTEs, August 2019–September 2020 in Sheffield.

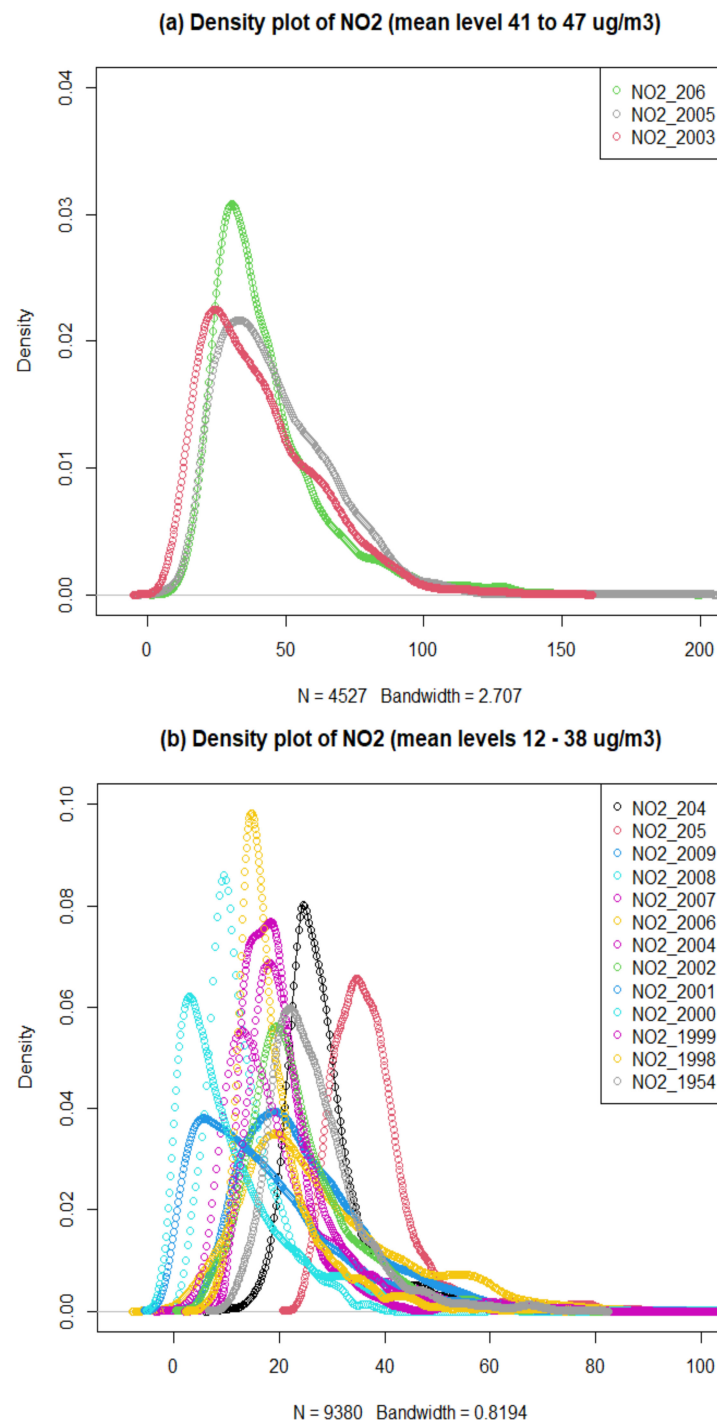
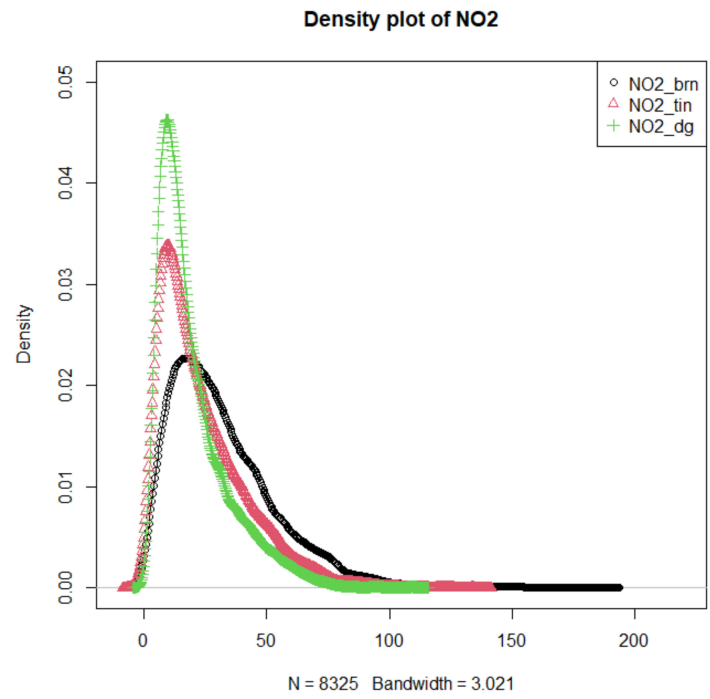


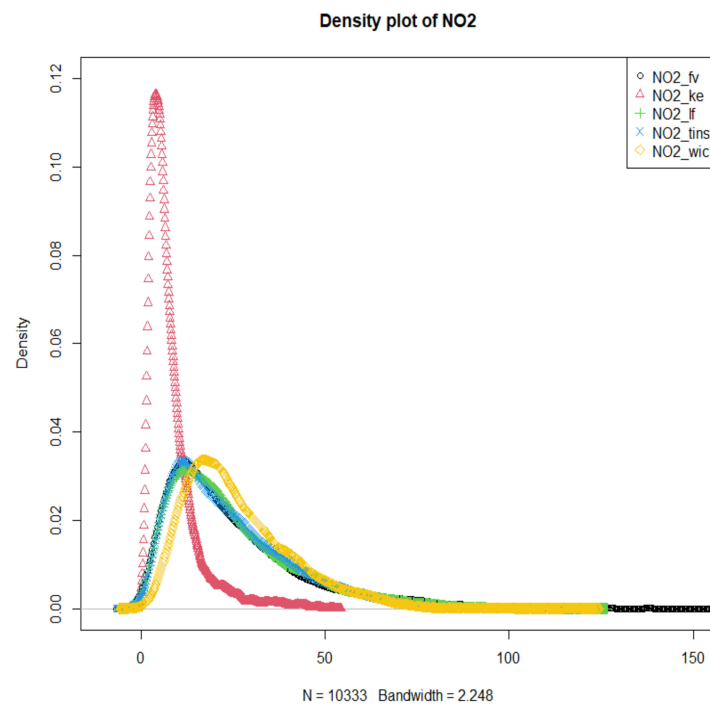
Figure 7. Density plots of hourly NO₂ concentrations ($\mu\text{g}/\text{m}^3$) measured by AQMesh pods from August 2019 to September 2020 in Sheffield.

Density plots of NO₂ concentrations measured by AURN sites and SSC sites are shown in Figure 8a,b, respectively. The distributions are skewed right. AURN sites had mean NO₂ concentrations of 23, 19 and 32 $\mu\text{g}/\text{m}^3$ at the Sheffield Tinsley, Devonshire Green and Barnsley road AQMSs, respectively. The SSC sites Firvale, Tinsley, Lowfield, Wicker and King Ecgbert had mean concentrations of 25, 24, 25, 26 and 8 $\mu\text{g}/\text{m}^3$, respectively. The concentrations measured at both AURN and SSC sites were well below the AQ standards. The lowest concentrations were recorded at the King Ecgbert site, which is located in a background location well outside the city centre. In this section, we consider the distribution and annual mean of NO₂ concentrations measured at different AQMSs of

different grades. Density plots are a useful tool for understanding the distribution of NO₂ concentrations and comparing the distributions of different monitoring sites. However, density plots provide no information on the temporal variability of NO₂ concentrations, which are analysed in the coming section.



(a)



(b)

Figure 8. Density plots of NO₂ concentrations ($\mu\text{g}/\text{m}^3$) measured by: (a) AURN sites-Barnsley road (brn), Tinsley (tin) and Devonshire Green (dg); and (b) SCC sites-Firvale (fv), King Egbert (ke), Lowfield (lf), Tinsley (tins) and Wicker (wic), from August 2019–September 2020.

3.1.2. Time Variation Plots

It is important to know how NO₂ concentrations vary at different time scales. Time variation plots show variations in NO₂ concentrations on diurnal, weekly and annual cycles. Such information is useful in understanding the emission sources of air pollutants. In this section, temporal variabilities of NO₂ concentrations are analysed by employing time variation plots, using data from AURN, SSC, Envirowatch E-MOTEs and AQMesh pods. NO₂ concentrations measured by AURN and SCC sites are analysed first to set a benchmark of temporal variation for the LCS.

Barnsley is a roadside (urban traffic) AQMS, whereas Tinsley and Devonshire Green are urban background sites. Therefore, NO₂ concentrations measured at Barnsley site (NO₂_brn) were higher than at the other two sites (Figure 9). Figure 9 shows that, on diurnal cycles, NO₂ concentrations were higher in the busy morning hours (07:00–09:00 h) and busy afternoon hours (17:00–19:00 h) and lower at night and midday. Weekly cycles showed that NO₂ concentrations were significantly lower on weekends (Sunday being the lowest) than on weekdays. Annual cycles of NO₂ showed higher concentrations in colder months (e.g., January, February, November and December) than the warmer months (e.g., June, July and August). All three AURN sites demonstrated the same temporal trends on diurnal, weekly and annual cycles. Diurnal and weekly cycles of NO₂ concentrations are controlled by road traffic flow, whereas annual cycles in addition to emissions are controlled by meteorological parameters. In winter, the temperature is low and the atmosphere is stagnant, which hinders the dispersion of air pollutants emitted locally. In contrast, in summer the atmosphere is more turbulent, encouraging both vertical and horizontal dispersion of pollutants.

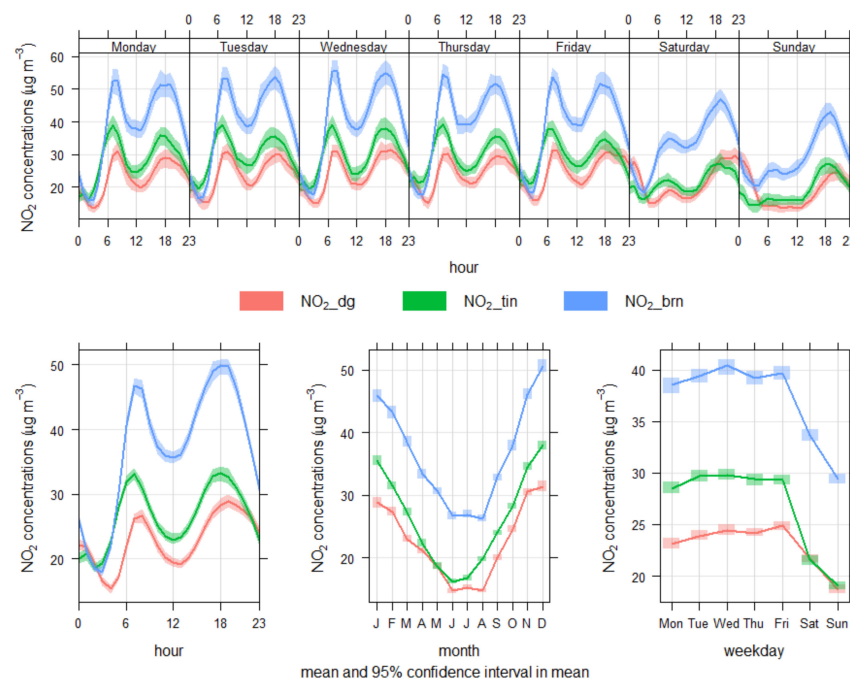


Figure 9. Time variation plots of NO₂ concentrations ($\mu\text{g}/\text{m}^3$) in Sheffield at the three AURN AQMS: Barnsley, Tinsley and Devonshire Green.

Figure 10 shows the temporal variability of NO₂ concentrations using data from five SSC sites: NO₂_fv (Firvale), NO₂_ke (King Ecgbert), NO₂_lf (Lowfield), NO₂_tins (Tinsley) and NO₂_wic (Wicker). SCC AQMSs demonstrated a temporal trend similar to AURN sites. In addition to some minor differences between different sites, NO₂ concentrations were significantly lower at the King Ecgbert site, which is a background site located outside the city centre in a quite location.

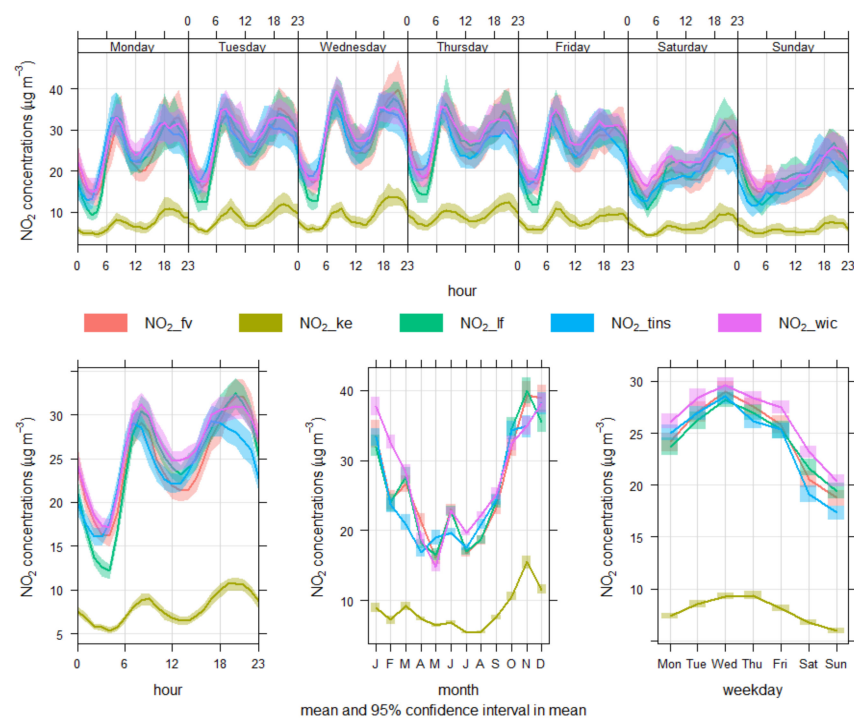


Figure 10. Time variation plots of NO_2 concentrations ($\mu\text{g}/\text{m}^3$) measured at SCC sites: Firvale, King Ecgbert, Lowfield, Tinsley and Wicker, from August 2019–September 2020.

To demonstrate temporal variability in NO_2 concentrations (Figure 11) measured by Envirowatch E-MOTEs, four E-MOTEs were selected: NO_2 _904 (Railway Station), NO_2 _902 (Harmer Lane/Sheaf Street), NO_2 _731 (Howard Street) and NO_2 _738 (Brook Hill, near Firth Court). These four sites were selected because NO_2 _904 presented an unusual time profile, whereas NO_2 _902, NO_2 _738 and NO_2 _731 showed a typical time variations similar to many other sensors. The diurnal, weekly and annual cycles followed almost similar pattern as those shown by AURN and SSC sites. However, there were some minor differences between various E-MOTEs installed at different locations within the city. Also, differences in winter vs. summer and weekend vs. weekday concentrations were much prominent in AURN sites than in E-MOTEs. NO_2 _904 demonstrated higher concentrations at all times, even at nights and weekend, as the taxi stand next to the train station remains busy at all times waiting for train passengers (probably with vehicles idle while waiting).

Figure 12 shows the diurnal, weekly and annual cycles of NO_2 concentrations measured by four AQMesh pods. The four AQMesh sites were: NO_2 _1999 (Malin Bridge School), NO_2 _2001 (London Rd), NO_2 _2003 (Brightside Lane) and NO_2 _204 (Hunter's Bar School). Here the diurnal and weekly cycles showed similar trends; however, the annual cycles were different from each other and from the ones shown by AURN and SSC AQMSs. The NO_2 _2001 annual cycle was particularly different as it showed higher concentrations in summer months than in winter months. However, weekly cycles presented normal trends, as expected and shown by AURN sites.

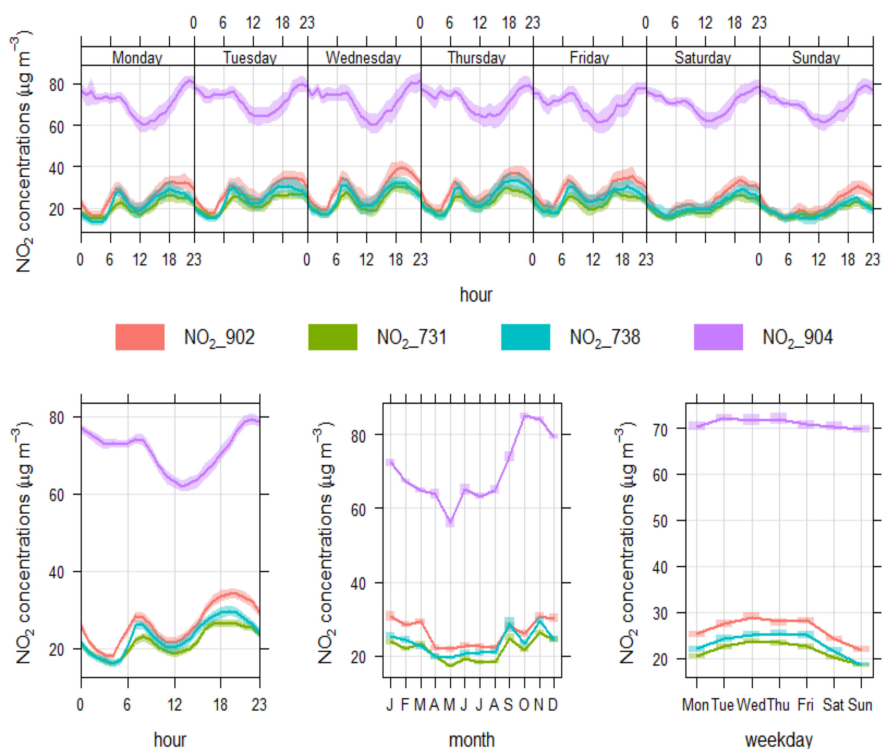


Figure 11. Time variation plots of NO₂ concentrations (µg/m³) measured by Envirowatch E-MOTEs.

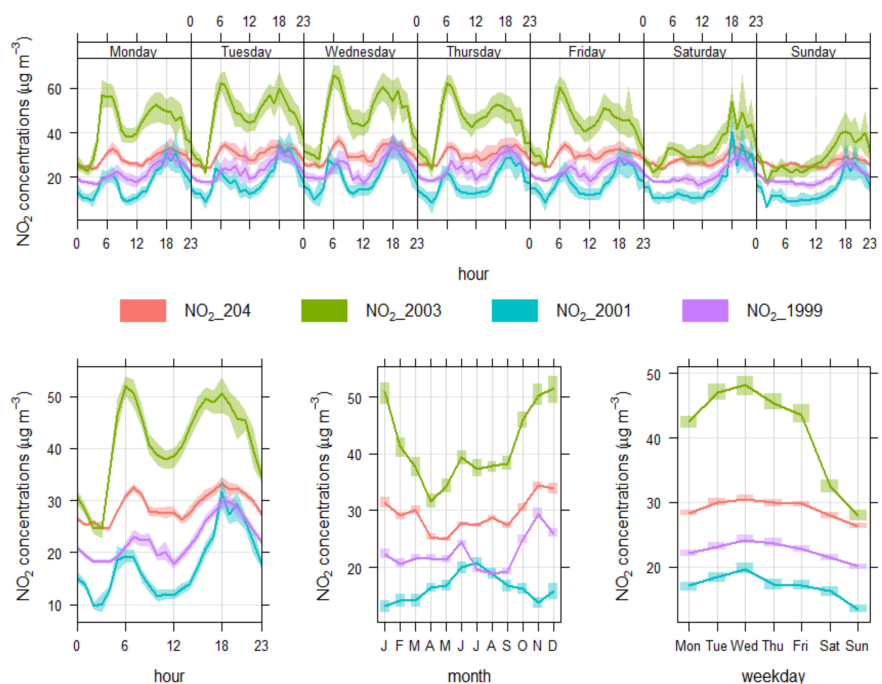


Figure 12. Time variation plots of NO₂ concentrations (µg/m³) measured by AQMesh pods.

3.2. Long-Term Trends in NO₂ Concentrations

The temporal trend in NO₂ concentrations was determined using the TheilSen function for the last 20 years (2000–2019) at Tinsley and for the last six years (2014–2019) at the Devonshire Green AQMS. Both of these sites are part of the AURN. Trends were expressed in µgm⁻³/year. Both non-adjusted (non-deseasonalised) and adjusted (deseasonalised) trends were calculated. Sheffield Tinsley demonstrated negative trends during the study period. Both adjusted and non-adjusted trends were negative and highly significant. The

non-adjusted trend was -0.94 ($-1.12, -0.78$) $\mu\text{gm}^{-3}/\text{year}$, whereas the adjusted trend was -0.95 ($-1.04, -0.86$) $\mu\text{gm}^{-3}/\text{year}$ (Figure 13). The temporal trend at the Devonshire Green site was also negative and highly significant. The non-adjusted trend was -1.21 ($-1.91, -0.41$) $\mu\text{gm}^{-3}/\text{year}$ and the adjusted trend was -1.26 ($-1.57, -0.83$) $\mu\text{gm}^{-3}/\text{year}$ (Figure 14).

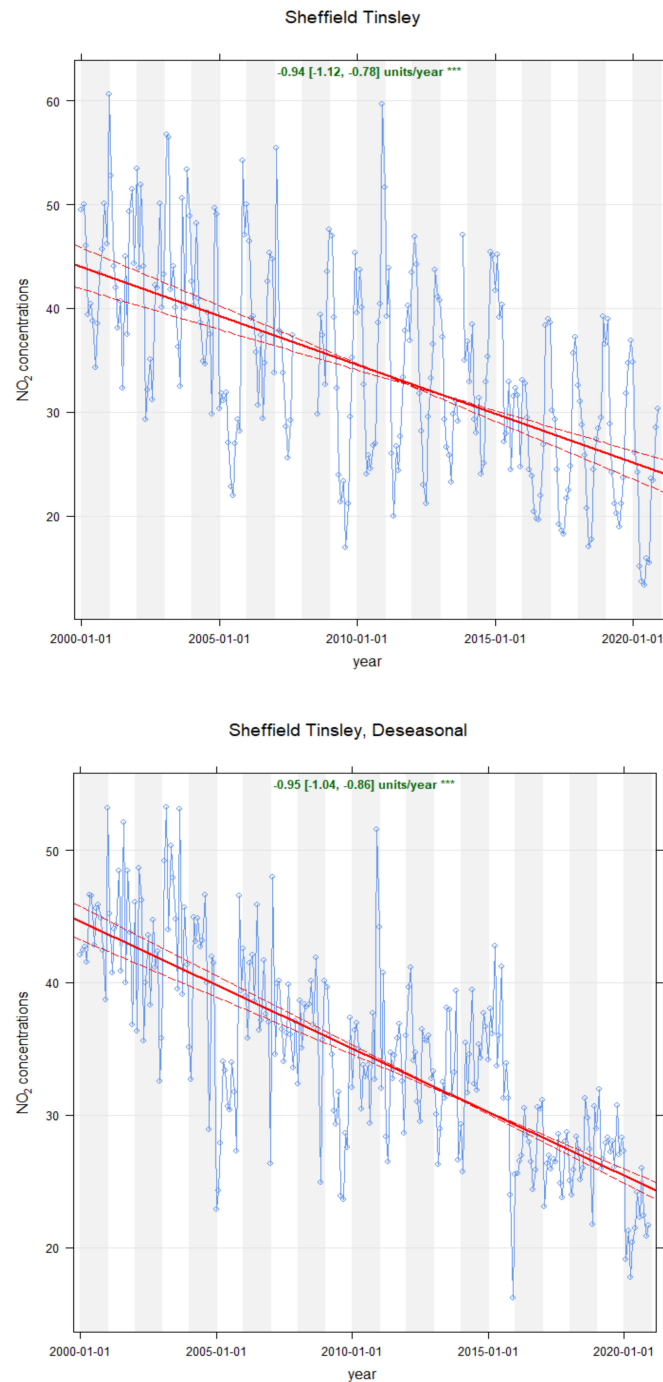


Figure 13. Long-term temporal trend for NO_2 concentrations ($\mu\text{g}/\text{m}^3$) (2000–2019) at the Sheffield Tinsley site, one of the AURN sites. *** shows that the trend is highly significant.

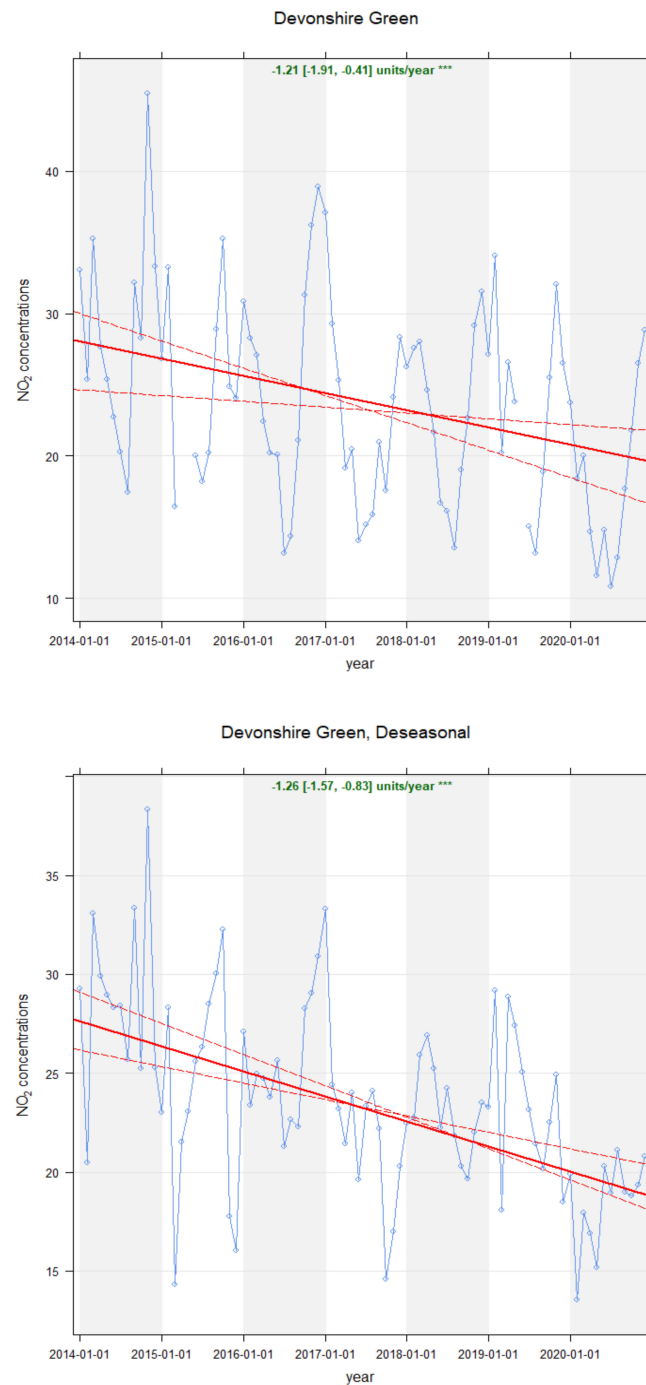


Figure 14. Long-term temporal trend for NO₂ concentrations ($\mu\text{g}/\text{m}^3$) (2014–2019) at the Sheffield Devonshire Green site. *** shows that the trend is highly significant.

At both AQMSs, NO₂ levels decreased during the study period. The reduction in air pollution levels could have been caused by reductions in pollutant emissions or changes in climatic conditions. However, when the trends were adjusted for the effect of changes in climatic conditions, the trends were still negative and slightly greater than the non-adjusted trends (Figures 13 and 14). This probably proves that reduction in NO₂ levels were due to reductions in emissions, showing that, despite the fact that the number of vehicles on roads has gone up, the amount of exhaust emissions has decreased. The reduction in exhaust emissions was probably caused by the stringent emission policies of the UK government. Although generally pollution levels have decreased, the reduction is not uniform spatially and temporally. For example, the trend at the Tinsley site was lower

($-0.94 \mu\text{gm}^{-3}/\text{year}$) than at the Devonshire Green site ($-1.21 \mu\text{gm}^{-3}/\text{year}$). However, it should be noted that at Devonshire Green the trend was determined for a shorter period. When a shorter period was also considered for Tinsley, i.e., from 2014 to 2019, the trend was $-1.65 \mu\text{gm}^{-3}/\text{year}$. This probably shows that reductions in pollutant concentrations have been greater more recently. However, the reductions are not enough and NO_2 levels still exceed air quality standards in several parts of the city. Therefore, more actions are required to further improve air quality in Sheffield to comply with air quality guidelines.

3.3. Time Series Modelling

Comparison of Linear and Nonlinear Time Series

The performances of two univariate nonlinear persistent models, NNNAR and SETAR, were compared to that of the linear ARIMA model. Several statistical metrics were calculated to assess the performances of these models (Table 3). Comparing their performances in Table 3, it can be observed that the ARIMA model performed better than the two nonlinear models. Correlation coefficients (r -values) for ARIMA, NNNAR and SETAR were 0.59, 0.45 and 0.44 and RMSE values were 8.61, 10.45 and 10.56, respectively, which show that there is probably no need for the use of a more complicated nonlinear model for air quality prediction, as ARIMA in this particular example performed better than the nonlinear counterparts. The nonlinear models are not discussed further. For more details on SETAR and NNNAR, readers are referred to Firat [36] and Waheeb et al. [37].

Table 3. Comparing the performances of different models, including both linear and nonlinear models, using the testing dataset (cross validation). MBE, MAE and RMSE are expressed in $\mu\text{g}/\text{m}^3$. r is the value of correlation coefficient.

Model	FAC2	MBE	MAE	RMSE	r
SETAR	0.90	-0.13	8.28	10.56	0.44
NNET	0.89	-0.29	8.12	10.45	0.45
ARIMA	0.91	-0.26	6.46	8.61	0.59

Here, we first discuss the univariate ARIMA model and then compare its performance with ARIMAX. The estimated parameters of the fitted ARIMA (1,1,1) model are shown in Table 4. The estimated parameters were used to predict NO_2 concentrations. A comparison of predicted and observed NO_2 concentrations for the testing (held-out) dataset is shown in Figure 15. As expected, the ARIMA model performed better when model performance was assessed based on the training dataset with r -value 0.68, MBE 0.07 and FAC2 0.93 than when the model performance was assessed using testing dataset having r -value 0.59, MBE -0.26 and FAC2 0.91.

Table 4. Estimating the parameters of the ARIMA (1,1,1) model for the NO_2 concentrations ($\mu\text{g}/\text{m}^3$) training dataset.

ARIMA Model Applied to Log_NO ₂ with p, d and q , Order of 1, 1, 1		
Coefficients	AR1 (ϕ)	MA1 (θ)
	0.5362	-0.9511
S.E.	0.0296	0.0117
Sigma square (σ^2) estimated as 0.148: log likelihood = -556.75, AIC = 1117.5		

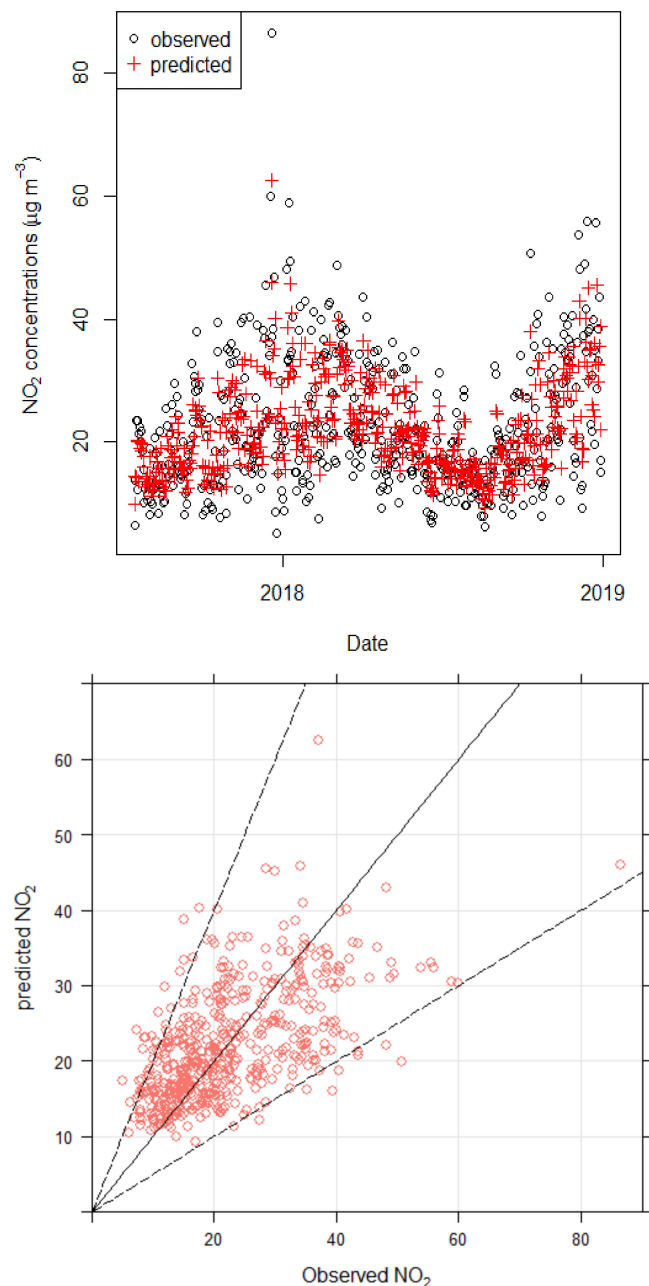


Figure 15. Predicted vs. observed daily average NO₂ concentrations ($\mu\text{g}/\text{m}^3$) using the ARIMA (1,1,1) model. Model performance was assessed against held-out testing data, which was not used for model fitting. No exogenous variable was used in the model. The solid line represents the 1:1 relationship, whereas the dashed lines represent the 1:0.5 and 1:2 relationships, between observed and predicted concentrations. The dashed lines show the points that are within a factor of two (FAC2).

Residual analysis was performed for the model. A plot of standardised residuals showed a rectangular scatter around a zero horizontal level with no trends, which showed the adequacy of the model. A quantile–quantile plot of the residuals showed that the data points followed the straight line closely, which led us to accept the normality of the error term. This was also confirmed by the histogram of the residuals, which appeared closed to normal (Figure not shown for brevity).

3.4. Outputs of ARIMAX Model

In addition to the autoregressive, moving average and differencing components used by univariate ARIMA, the more advanced ARIMAX model incorporates external variables, also known as exogenous regressors, into time series modelling. The exogenous variables incorporated into the ARIMAX model should be strongly correlated with the modelled variable. Here, in the first instance we used a single exogenous variable (NO concentrations) for modelling NO₂ concentrations and assessed how it improved the model performance compared to the ARIMA model developed in the previous section, which did not use any external variable. In the next step, NO and O₃ were used as exogenous variables and their effect was assessed on the model goodness of fit. Ideally, meteorological parameters such as temperature, relative humidity and wind speed should have been used in the model as well. However, due to data availability problems, they were not used as regressors in the model.

The estimated parameters of the ARIMAX (1,1,1) model are shown in Table 5. Various statistical metrics calculated for the fitted model and cross validation were significantly improved as compared to ARIMA model. The values of *r*, RMSE, MBE, MAE and FAC2 were 0.85, 7.11, 0.07, 6.53 and 0.96, respectively, for the fitted model. However, when the model performance was assessed using the testing dataset the values of *r*, RMSE, MBE, MAE and FAC2 were 0.70, 10.15, 7.81, − 6.84 and 0.88, respectively (Table 6). For further analysis, model diagnostics were carried out by analysing the residuals of the model. The residual plots, Q–Q plots and histogram of error terms showed that the residuals were normally distributed and that the model performance was adequate (Figures are not shown for brevity).

Table 5. Estimating the parameters of the ARIMAX (1,1,1) model for the NO₂ concentrations (µg/m³) training dataset, with NO as exogenous variable.

ARIMAX Model Applied to Log_NO ₂ with <i>p</i> , <i>d</i> and <i>q</i> , Order of 1, 1, 1 and Xreg as NO			
Coefficients	AR1 (φ)	MA1(θ)	XREG
	0.2533	−0.9689	0.4133
Sigma square (σ ²) estimated as 0.056: log likelihood = 20.82, AIC = −31.64			

Table 6. Model statistics showing the value of several metrics in assessed the model performance by comparing observed and predicted NO₂ concentrations (µg/m³) for testing and training data, using NO as exogenous variables. MBE, MAE and RMSE are expressed in µg/m³.

Statistics	FAC2	MBE	MAE	RMSE	<i>r</i>
Training data	0.96	0.07	5.53	7.11	0.85
Testing data	0.88	−6.84	7.81	10.15	0.70

Finally, we added two exogenous regressors (concentrations of NO and O₃) to the ARIMAX model for predicting NO₂ concentrations. The estimated parameters of the ARIMAX model along with the AIC value are given in Table 7. The values of different statistical metrics calculated for assessing the model performance are provided in Table 8, where *r*-values were 0.90 and 0.84 and RMSE values were 11.75 and 9.90 for the training and testing datasets, respectively. Graphical presentation showed a strong association between predicted and observed concentrations (Figure not shown for brevity). This showed that the exogenous variables helped improve the model performance significantly compared to univariate persistent models.

Table 7. Estimating the parameters of the ARIMAX (1,1,1) model for the NO₂ concentrations (µg/m³) training dataset, with NO and O₃ as exogenous variables.

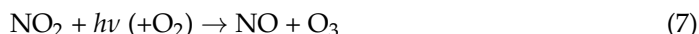
ARIMAX MODEL Applied to log_NO ₂ with <i>p</i> , <i>d</i> and <i>q</i> , Order of 1, 1, 1 and Xreg as NO and O ₃				
Coefficients	AR1 (φ)	MA1(θ)	XREG2 (NO _x)	XREG3 (O ₃)
	0.21	−0.985	0.839	−0.108
Sigma square (σ ²) estimated as 0.014: log likelihood = 866.86, AIC = −1721.73				

Table 8. Statistical metrics assessing the model performance by comparing observed and predicted concentrations for both the training and testing datasets, using NO and O₃ as exogenous variables. MBE, MAE and RMSE are expressed in µg/m³.

Statistics	FAC2	MBE	MAE	RMSE	<i>r</i>
Training data	0.65	−10.25	10.45	11.75	0.90
Testing data	0.73	−7.94	9.34	9.90	0.84

The above analysis showed that traditional time-series persistent models, e.g., ARMA or ARIMA, are useful tools for air pollution analysis and prediction; however they only depend on the behaviour of the past data without taking into account the effect of other pollutants and meteorological parameters that interact with the modelled pollutant. Therefore, these approaches fail to predict future levels accurately. The more advanced versions of these models, like ARIMAX, are able to analyse the effect of environmental factors and other pollutants and can result in better prediction by reducing the model error and strengthening correlations between modelled and observed concentrations.

The association of the NO₂ concentration with NO and O₃ concentrations is shown in the form of a scatter plot in Figure 16. The chemistry of NO₂ with O₃ and NO is shown in Equations (6) and (7).



Equations (6) and (7) define the chemistry of NO, NO₂ and O₃. In Equation (6), one molecule of O₃ is consumed and one molecule of NO₂ is produced. In contrast, in Equation (7), one molecule of NO₂ is consumed and one molecule of O₃ is produced, so no net chemistry occurs. NO₂ is positively correlated with NO ($r = +0.75$) and NO_x ($r = +0.89$) and negatively correlated with O₃ ($r = -0.68$). The negative association between NO₂ and O₃ is well known [13,45,46]. It shows that NO₂ concentration is strongly correlated with O₃ and other NO_x species. Therefore, adding O₃ and NO as exogenous regressors in the model can explain a significant proportion of NO₂ and improves the model performance.

Catalano et al. [47] developed an ARIMAX model and compared its performance to an artificial neural network (ANN). They modelled NO₂ concentrations at Marylebone Road, London, using several exogenous variables: traffic volume, wind speed, wind direction, temperature and lagged NO₂ concentrations. According to Catalano et al. [47], the ARIMAX model performed better than an ANN. The mean ratio of the predicted to the measured concentrations was 0.89 for the ARIMAX model and 0.86 for the ANN. Both models had the same correlation coefficient of 0.91; however, mean absolute percentage error (MAPE) values were 18.62 and 16.53 for the ARIMAX model and the ANN, respectively. This shows that the prediction of the ARIMAX model is comparable with a neural network and can be used for air pollution forecast in urban areas to provide timely warning of high air pollution levels to the public.

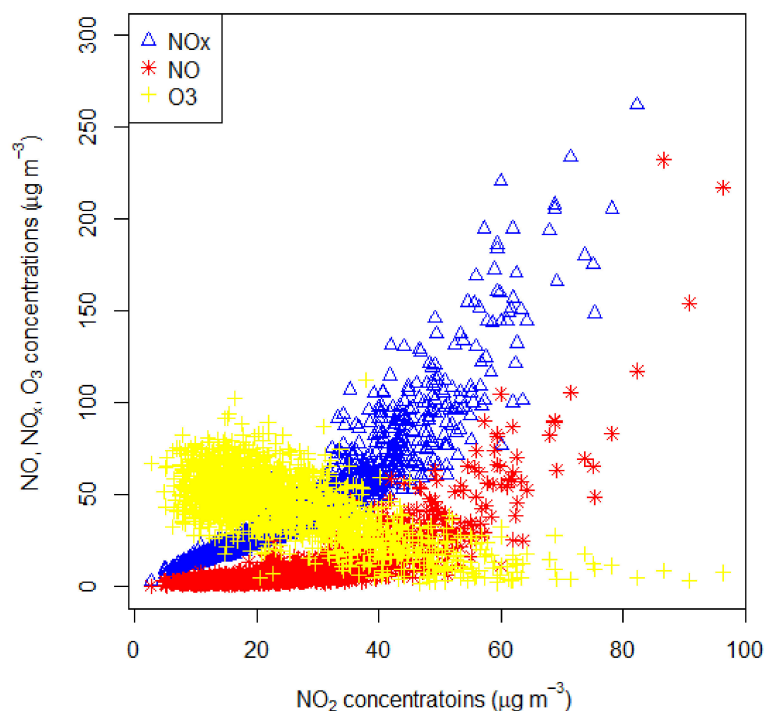


Figure 16. Scatter plot showing the association of NO_2 with NO , NO_x and O_3 concentrations ($\mu\text{g}/\text{m}^3$) at the Devonshire Green AQMS in Sheffield.

4. Conclusions

We have a network of AQMSs in Sheffield consisting of low-cost and reference sensors. Here, NO_2 concentrations measured by Envirowatch E-MOTEs, AQMesh pods and AURN and SCC AQMSs were analysed to characterise the temporal variability of NO_2 concentrations. Density plots are a useful tool for comparing and analysing the distributions of NO_2 concentrations measured by various sensors. Time variation plots were employed to characterise and compare the temporal variability of NO_2 concentrations measured at different monitoring sites. Time variation plots visualise how NO_2 concentrations vary during different time periods (e.g., diurnal, weekly and annual cycles) and help us understand their emission sources. Long-term data for NO_2 concentrations showed negative trends at both the Sheffield Tinsley and Devonshire Green sites, indicating that pollutant emissions decreased because of stringent emission policies. However, the reductions in pollution varied both spatially and temporally. Moreover, further smart interventions are required to cut emissions and improve air quality to comply with air quality guidelines.

NO_2 concentrations were modelled from the Devonshire Green AQMS in Sheffield using univariate linear and nonlinear and multivariate time series models with exogenous variables. The addition of exogenous variables to the ARIMAX model significantly improved the model performance. Model specification, fitting and diagnostics were discussed. Model performance was assessed by calculating several statistical metrics, including r , RMSE, MBE, FAC2 and MAE. The ARIMA model showed better performance than nonlinear persistent models, showing that linear models were not only easy to apply and interpret but also showed better performance than the more complicated models such as SETAR and NNNAR. The best model fit was achieved when NO_2 concentration was modelled using ARIMAX with two exogenous variables (NO and O_3). These variables were strongly correlated with NO_2 . NO was positively correlated, whereas O_3 was negatively correlated with NO_2 .

Time series models with exogenous regressors can be successfully used to predict future pollution concentrations, providing early warning for the public so that timely precautionary measures can be adopted. The main weakness of the study was that we did not provide full details of the low-cost sensors calibration. Ideally, several of these low-cost

sensors should have been collocated with reference sensors for detailed comparison and calibration. However, due to several practical problems (e.g., planning permission), this was not possible and the only calibration carried out was described in Munir et al. [44]. They compared the measurements of Envirowatch E-MOTEs with the measurements of an AURN site (Sheffield Devonshire Green). Future work will include installation of low-cost sensors, collocated with reference sensors for over a year, and a comparison of their measurements during different time periods. This study provides a detailed methodology for time series modelling, which can be used as an early warning tool for air pollution episodes, and compares different linear and nonlinear modelling approaches.

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