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The effect of explosive charge backing in close-proximity air-blast loading

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Abstract

This paper presents new insights into the influence of explosive charge backing on the impulse transfer and transient response characteristics of plates subjected to close-proximity air blast loading. The results of the combine experimental and computational studies show the critical influence of charge backing, which caused between a 3-5 times increase in the impulse transfer when the charge was metal-backed. The permanent deflections from the metal-backed detonations were larger than for air, but not to the same degree as the impulse increase. These findings demonstrate the important influence of charge backing, in close proximity detonations, which greatly exceeded anything previously measured. These valuable insights will assist blast protection engineers considering the effects of explosions in situations when the charge backing is something other than air, which is a frequent occurrence in explosion scenarios.

Keywords: blast response, plates, plastic deformation, transient response, charge backing

1. Introduction

After more than a decade of increased awareness of subversive activity, the public expects protection from the threat of explosions. Explosive threats can be accidental such as the recent blast in a Chinese industrial park that killed 19 people (1) and the tragic death of an American caused by an “exploding electronic cigarette” (2). Unfortunately, deliberate explosions, such as terrorist activity, landmine detonations or military action are far too common. A great deal of effort has gone into preventing deliberate explosive detonations, such as better pre-screening at airports and active mitigation methods in military systems. Despite this, terrorist attacks still caused the deaths of at least 25,673 people in 2016 (3), with explosions accounting for 54% of the attacks. Anti-vehicle landmines were involved in 169 incidents in 2017, injuring 321 people and killing 166 people (4).

32 Landmines are typically disc-shaped and have a diameter (D) to height (H) ratio of
33 approximately three. Most anti-vehicle landmines are buried or laid on the ground. This means
34 that the detonated explosives have a backing that influences the blast wave development. There
35 are also accounts of horizontally-mounted mines targeting vulnerable parts of passing vehicles
36 (5). Anti-personnel landmines are smaller than the anti-vehicle mines but cause more deaths because
37 of their ubiquitous use. The Landmine Monitor Report (5) recorded over 122,000 casualties
38 from anti-personnel landmines and explosive remnants of war (including 36,000 deaths) over
39 a twenty-year period (6).

40 Bare, disk-shaped (that is, high D/H ratio cylindrical), charges generate complex blast waves
41 that propagate away from the detonation location. The influence of charge shape decreases in
42 importance as stand-off distance (SOD) increases (7). The Hopkinson–Cranz scaled distance,
43 $Z = R/W^{1/3}$ (where R is the SOD from the charge to the target and W is the TNT equivalent
44 charge mass) is a dimensional scaled distance. Explosions are considered ‘near-field’ for $Z <$
45 $1 \text{ m/kg}^{1/3}$, and in this region the blast pressure and impulse distribution is extremely non-
46 uniform and fireball effects are significant (8) (9) (10). Spherical blast waves propagate in the
47 axial and radial directions after the detonation of a cylindrical charge (9) (8). Bridge waves can
48 form following detonations in free air, reinforced by interactions between the axial and radial
49 wave propagation (6).

50 Xiao et al (11) modelled the detonation of cylindrical TNT charges in free air with D/H values
51 ranging from 0.2 to 1 (which is too low for landmine detonations). When $Z = 0.7 \text{ m/kg}^{1/3}$, the
52 shock wave was highly focused in the axial direction when the cylinders were detonated at a
53 single end, rather than centre-detonated. Charge shape effects had insignificant effect on
54 pressure when $Z > 3.9 \text{ m/kg}^{1/3}$ and impulse effects could be neglected when $Z > 5.7 \text{ m/kg}^{1/3}$.
55 Qi et al (12) performed experimental and computational studies into the influence of charge
56 shape on the axial impulse generated and flight characteristics of a ball bearing during end-
57 detonations of PE4 cylinders. The overall axial impulse increased but the ball bearing velocity
58 decreased as D/H increased (for a constant charge mass).

59 Although surface bursts are frequent in practice, most studies consider free air detonations (for
60 example, references (6) (7) (9) (8), (11) (12)) while relatively few focus on surface bursts (13)
61 (14) (15) (16). Guerke and Scheklinski-Gluek (13) performed tests on cylinders of RDX
62 (D/H=0.2 and D/H=1) inclined at different angles to the ground for $0.5 \text{ m/kg}^{1/3} < Z < 32$
63 $\text{m/kg}^{1/3}$. Preliminary results attributed the variations between the cylindrical and hemispherical

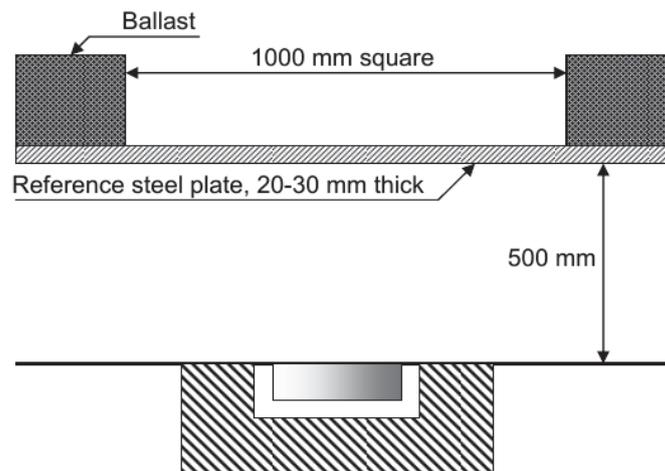
64 tests to differences in the time and shape of the detonation waves reaching the air. The pressure
65 propagation over distance (in the far-field) was observed to be a combination of the shock front
66 differences, the interaction between axial and radial blast waves and multiple pressure
67 reflections. Tancreto (14) investigated the effect of charge shape on the impulse and
68 overpressure generated from surface bursts involving the detonation of hemispherical and
69 cylindrical Composition B charges. Charge shape effects were significant, increasing both the
70 overpressure and impulse for $Z < 8 \text{ m/kg}^{1/3}$.

71 Xiao et al (15) performed similar work to the free air simulations reported in reference (11),
72 comparing hemispherical charge and cylindrical charge detonations on the ground. The model
73 results were validated using the data presented by Tancreto (14). The influence of the charge
74 shape was found to be significant for overpressures up to $Z = 4 \text{ m/kg}^{1/3}$, while the impulse
75 effect persisted until $Z = 8.0 \text{ m/kg}^{1/3}$ when the cylindrical charge was end detonated. The
76 impulse predictions were 20% higher in the far-field for cylindrical detonations (compared to
77 hemispherical ones).

78 Explosions in, or on, the ground transmit energy to their surroundings. This energy release
79 takes many forms, including heat, air and soil kinetic energy, soil deformation and work done
80 by expanding gaseous products. Several factors affect the energy partition. For example, when
81 an explosion occurs far under the surface of the ground, the energy is totally absorbed by soil
82 deformation, mechanical losses and thermal losses (16). At the other extreme is a surface
83 detonation on frozen soil, where very little energy is transmitted to the ground and the air shock
84 and impingement of the detonation products do much of the work on nearby structures. Many
85 factors influence the total impulse transfer to a structure, including moisture content and bulk
86 density of the soil (17) (18) (19) (20) (21), the size of the granular particles (20), the SOD (17),
87 (20) (22) (23) and the depth of burial (DOB) (17), (20) (22) (23).

88 Recently, Clarke et al (24) presented results from a detailed parametric study, comprising 40
89 tests at quarter scale, into the effect of charge placement, soil composition, moisture content
90 and geometrical confinement on the loading that arose from explosive detonations in soil. Part
91 of the study compared $D/H=3$, disk-shaped, 78g PE4 charge detonations with only air behind
92 the charge to results from soil backed surface detonations with the same charge geometry ($Z <$
93 $0.37 \text{ m/kg}^{1/3}$). The pressure was slightly more localised and exhibited a higher peak value when
94 the charge was soil-backed. There were no discernible differences in the total impulse, specific
95 impulse or time to peak pressure.

96 Commercial landmine protected vehicle testing allows for the use of controlled simulated
97 charges, as outlined in NATO Stanag 4569 AEP-55 Vol 2 (25). This provides a reference guide
98 for the standardised testing of vehicles subjected to simulated mine detonation. One of the
99 standard test methods involves mounting a charge on a metal backing plate, as shown in Figure
100 1. The target is a reference plate, with a span to thickness ratio of between 33 and 50,
101 manufactured from steel plate. Voisin *et al* (26) used the arrangement shown in Figure 1 to
102 compare the response of composite panels to simulated landmine loading, but do not consider
103 the influence of the backing plate on the loading or structural response.



104 Figure 1 A Proposed configuration for simulated mine detonation tests (25)

105 Extensive experimental studies have reported on the large permanent ductile deformation and
106 rupture of plates, beams and shells due to blast loading conditions in air. Jones (27), Nurick
107 and Martin (28; 29), and Chung Kim Yuen *et al* (30) present overviews of theoretical and
108 experimental studies of plates subjected to impulsive and/or air-blast loading. Comparable
109 information concerning the influence of a solid backing to an explosive charge on the impulse
110 imparted to a structure and the damage that ensues is not available.

111 This paper reports the results of experimental and computational studies on the influence of
112 charge backing on the impulse transfer and deformation characteristics of steel plates subjected
113 to air-blast loading. The paper provides detailed insights that are of great practical relevance to
114 blast protection engineers considering explosions on the ground or other solid backings, such
115 as landmine protection research. The paper is arranged as follows. The experimental
116 arrangements and test results are described in sections 2 and 3 respectively. Results from blast
117 tests on fully-clamped Domex steel plates are reported, including the transient response
118 obtained from high speed images recorded during the blast experiments. Section 4 describes

119 the computational modelling approach, involving LS-Dyna simulations of the experiments.
120 The simulation results are used, alongside the experiments, to provide important insights into
121 the influence of charge mass and charge backing type (either air or steel) on the impulse
122 transfer, transient response and permanent deformation of steel plates.

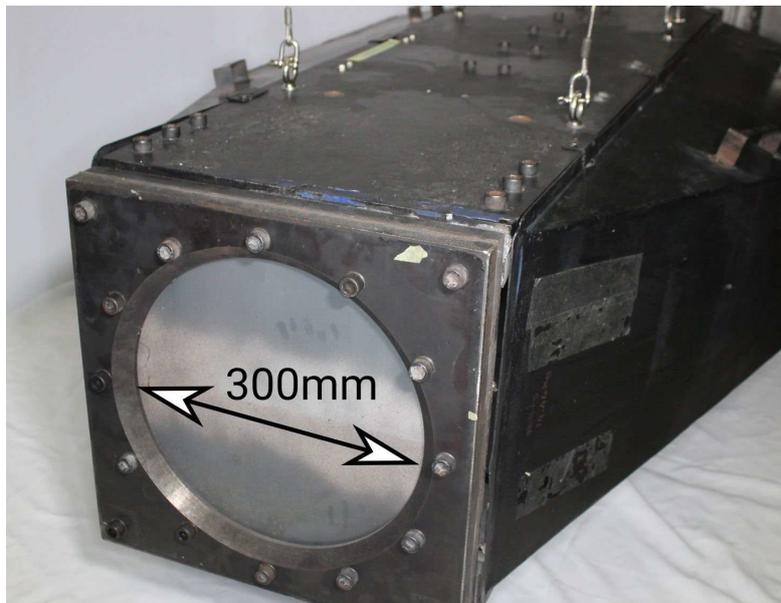
123 **2. Experimental Method**

124 **2.1 Test Specimens**

125 Following Curry and Langdon (31), square test plates, with a side length of 400 mm, were
126 manufactured from 3mm thick Domex 355MC, a high strength hot-rolled low alloy steel.
127 Results from quasi-static tensile tests found the following material properties: mean average
128 yield strength was 444 MPa, ultimate tensile strength was 627 MPa and the percentage
129 elongation at failure was 20%. Further details on the material characterisation are available in
130 references (32) (31). For blast testing, the 400 mm by 400 mm square plates were mounted
131 between two picture frame clamps as shown in Figure 2. When placed in the clamp frame, the
132 plates had a circular exposed area with a diameter of 300 mm.

133 **2.2 Air-blast loading**

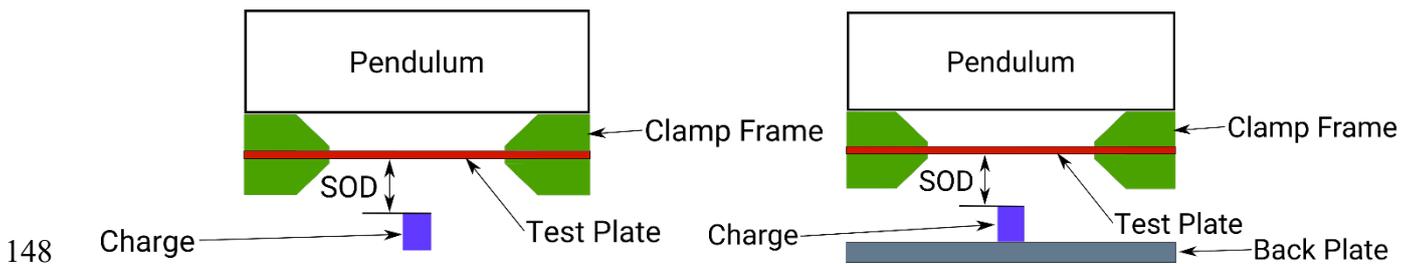
134 Each test plate was cleaned and painted with a speckle pattern for filming purposes. The plates
135 were bolted into a chamfered clamp frame, as shown in Figure 2. A 38 mm diameter cylinder
136 was moulded from Plastic Explosive #4 (PE4) for each experiment. The diameter was kept
137 constant while the charge height was varied depending on the charge mass. The SOD was
138 measured from the face of the charge. Two SODs, 40 mm and 50 mm, and two charge backing
139 configurations were used: (1) air backed charges, and (2) steel-backed charges. The two
140 configurations are shown in the schematics in Figure 3. The steel backing comprised a 20 mm
141 thick steel plate (400 wide and 400 mm long) on a compressed sand foundation. Each charge
142 was detonated at the centre of the rear face of the charge using an electrical detonator. For the
143 metal-backed charges, the detonator was pushed through a small hole in the centre of the steel
144 backing plate. The backing plate was inspected after each test and replaced if damaged.



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146 Figure 2 Photograph of a steel test plate and clamp frame on the horizontal pendulum (32)

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Figure 3: Schematics showing the test configurations (a) air-backed charges, (b) metal-backed charges

150 **2.3 Instrumentation**

151 Two high-speed monochrome IDT NRS4 cameras, filming at 30 000 fps, were used to record
 152 the rear plate surface during the blast experiments. The cameras were triggered with a custom
 153 built TTL trigger circuit that was activated by the detonation of the charge and an electrical
 154 synchronous trigger was employed. The cameras were mounted on a rail system to isolate them
 155 from vibration, as shown in Figure 4. Each camera was focused on the central strip through the
 156 middle of the test plate, resulting in data reflecting the transient displacement on the central
 157 midpoint as well as the cross section of the whole plate. Additional LED lights, covered by a
 158 diffuser, provided sufficient lighting to achieve good images for a 31 μ s exposure time. The
 159 impulse transferred to the plates was calculated using the maximum swing of the pendulum
 160 and a simple single-degree-of-freedom analysis. Metal shrouding was used around the
 161 pendulum to isolate the cameras from the intense light emissions and shock loading arising

162 from the detonation of plastic explosives. Following the experiments, the plates were scanned
163 using a 3D scanner to obtain surface plots of the deformed rear surface.



164 Figure 4: Photograph showing the high-speed imaging system mounted to the pendulum (shrouding
165 removed for clarity) (38)

166 The camera images were post-processed using the Dantec Dynamics Istra 4D DIC software
167 package. Prior to testing, calibration was performed to find the intrinsic and extrinsic imaging
168 parameters). Multiple images of the calibration target (which had a known checkerboard
169 pattern) were captured at different positions (using both cameras). The software then processed
170 these images and calculated the projection parameter of the entire system and additional
171 distortion parameters, using the pinhole model. The intrinsic and extrinsic calibration values
172 for the system were stored in a calibration file and imported into the analysis. Typically, eight
173 images were sufficient to calculate all calibration parameters accurately.

174 During post-processing, the specimen deformation was determined by tracking the movement
175 of the speckle pattern using a correlation algorithm to minimise the errors. For this set of tests,
176 an equivalence of 1 pixel = 0.3 mm meant that the worst uncertainty in the DIC data would
177 give an equivalent error of less than 1.5 mm in the deformation data. Subset sizes were fixed
178 at 19 pixels with a grid spacing of 5 pixels to ensure overlap in the subsets. Once a displacement
179 field was calculated for the area of interest, other information such as the strain field could be
180 calculated. All data presented in this paper are the unfiltered results exported from the DIC
181 software. Data was extracted along a centre line indicated on the plate using two markers, and
182 mid-point displacement was calculated. The data was post processed using a custom python

183 script to align and plot the displacement information for each line, and to align the profiles with
 184 the 3D scans of the plates. Further details regarding the DIC calibration, analysis and post-
 185 processing are available in references (32) (31).

186 **3. Blast test results**

187 The results from metal-backed charge detonation experiments are summarised in Table 1. The
 188 air-backed detonation test results are taken from Curry and Langdon (31) and are not repeated
 189 in the table. All the plates, regardless of charge backing type, exhibited Mode 1 (that is, large
 190 plastic deformation) failure without any indication of tearing or shearing failures.

191 Table 1: Summary of metal-backed detonation test results

SOD (mm)	Test designation	Charge Mass (g)	Impulse (Ns)	δPerm (mm)	δPeak (mm)
40	M25-40-01	25	126,9	38,4	42,7
	M20-40-01	20	131,7	35,6	40,8
	M20-40-02	20	118,9	33,3	
	M15-40-01	15	111,7	29,6	
	M15-40-02	15	106,2	28,0	
	M15-40-03	15	115,6	31,8	
	M15-40-04	15	110,2	31,5	37,2
	M15-40-05	15	117,2	28,2	33,4
	M10-40-01	10	92,2	21,9	
	M10-40-02	10	95,0	21,7	
	M10-40-03	10	93,1	26,0	31,8
50	M25-50-01	25	120,2	34,4	36,3
	M20-50-01	20	110,6	30,0	37,1
	M20-50-02	20	117,2	29,7	
	M20-50-03	20	106,7	26,0	
	M15-50-01	15	106,3	23,7	
	M15-50-02	15	104,0	23,6	
	M15-50-03	15	90,7	24,3	29,8
	M10-50-01	10	88,0	21,9	28,3
	M10-50-02	10	89,0	22,3	28,2
	M10-50-03	10	80,0	20,6	
	M10-50-04	10	88,0	21,2	

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3.1 Impulse transfer characteristics

Figure 5 shows graphs of impulse versus charge mass for the air and metal-back charge detonations at 40 and 50 mm SOD. As expected, there is a linear relationship between impulse and charge mass for each load condition. For a given SOD, the metal backing caused an increase in the impulse measured on the pendulum. Both the gradient and the intercept of the linear trend-lines increased when a metal-backing was introduced: the slope doubled and the intercept increased by 67 Ns for the 40 mm SOD and 57 Ns for the 50 mm SOD.

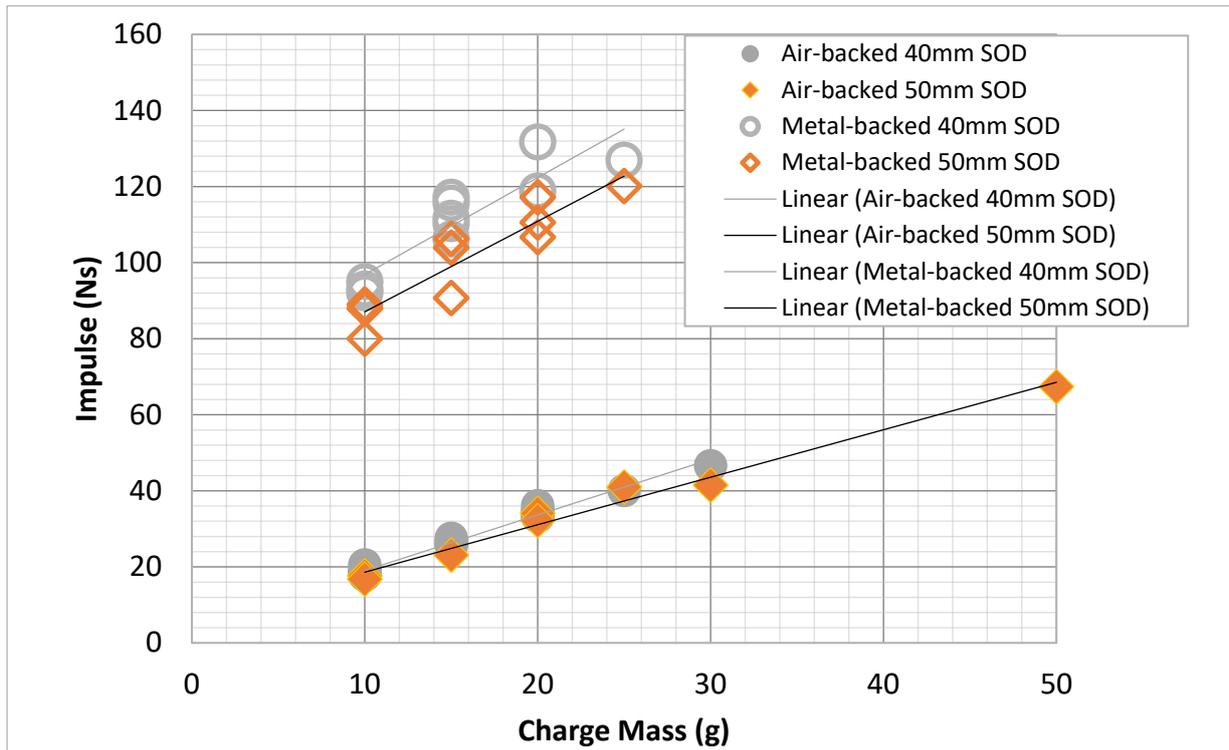
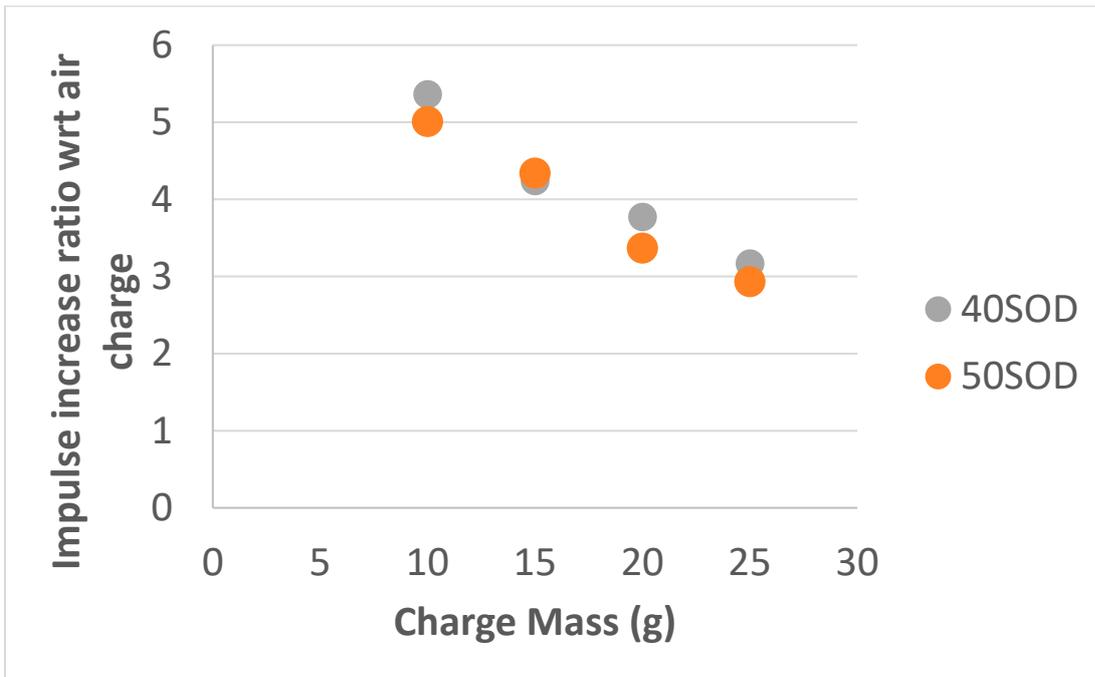


Figure 5: Graph of experimentally measured impulse versus charge mass

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The increase in impulsive loading imparted on the plates appears to be significant and varies slightly with an increase in charge mass. This was calculated with reference to the air charges and found to decrease with an increase in charge mass as shown in Figure 6 where the increase is seen to be more than 5 times for 10g charge and 3 times for 25g charges.



206

207 Figure 6 Impulse Increase ratio with respect to air charges for 40mm SOD and 50mm SOD

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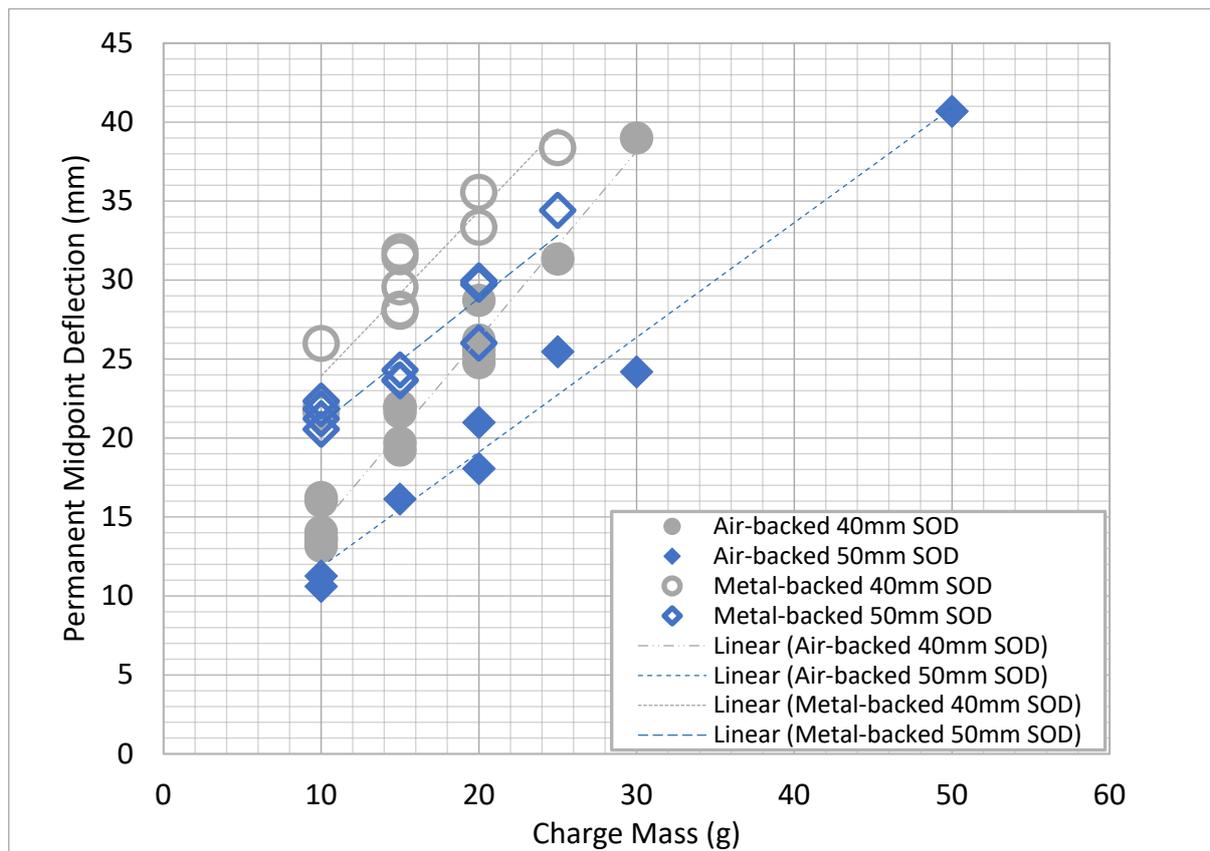
209 3.2 Permanent deflections

210 A summary of the permanent and transient deflections is shown in Table 2 for the metal-backed
 211 experiments. The peak transient deflections are larger than the permanent deflections, as
 212 expected, with a typical elastic recovery of 2-3 plate thicknesses (slightly larger than expected,
 213 except for the 25g metal-backed detonation at a 50 mm SOD). Membrane action and shear
 214 stresses would be present as deformation increases in the plate section but without any evidence
 215 of rupture due to these internal forces. This was desirable for tests involving high-speed
 216 cameras, as torn pieces of the plates could have damaged the camera system, and
 217 discontinuities such as cracks would have been difficult to process during digital image
 218 correlation.

219 A graph of final midpoint deflection versus charge mass is shown in Figure 7 for the two types
 220 of charge backing. The mid-point deflection increases linearly with increasing charge mass for
 221 a given charge backing and SOD combination. The metal backing increased the permanent
 222 mid-point deflection of the plates, as might be expected due to the large increase in impulse
 223 transfer. However, the difference in deflection is smaller than the rise in impulse, indicating
 224 that the relationship between impulse transfer and plate deflection is not straightforward. The
 225 physical reason for this is unclear.

Table 2: Average midpoint deflections obtained from the experiments

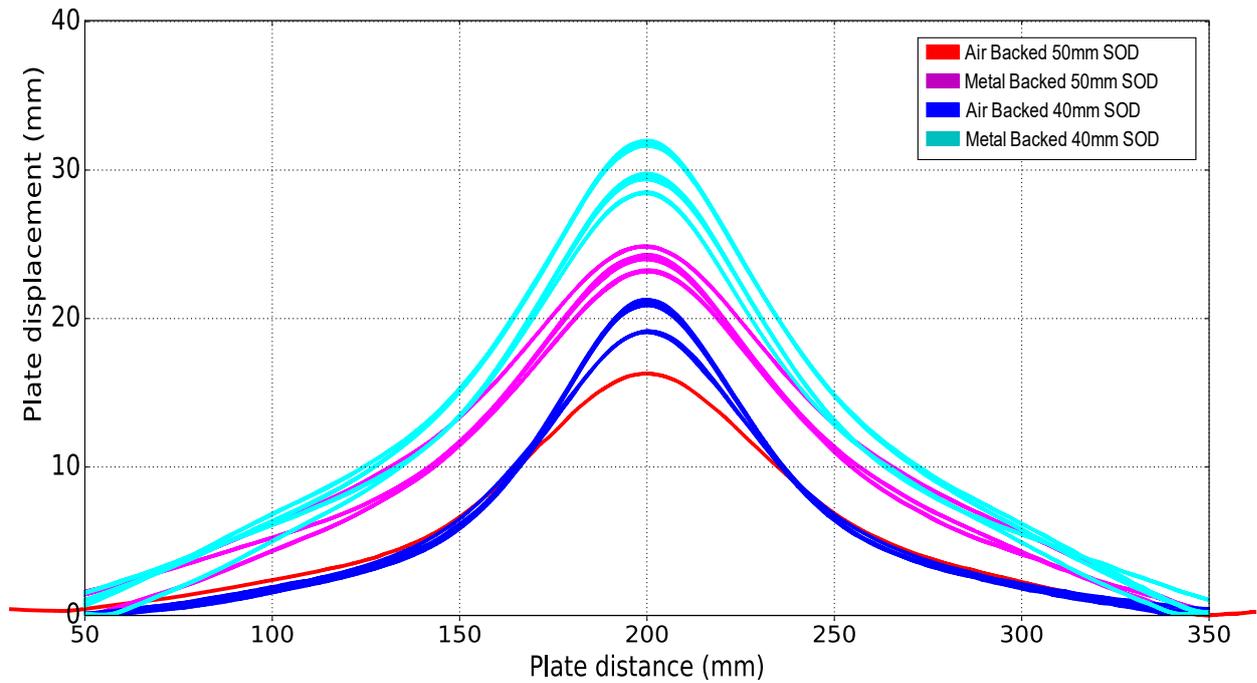
SOD	Charge Mass	Permanent Midpoint Displacement (mm)		Transient Maximum Midpoint Displacement (mm)	
		air-backed	metal-backed	air-backed	metal-backed
40	10	14.3	23.2	22.0	31.8
	15	20.9	29.8	25.3	33.4
	20	26.0	34.4	30.3	40.8
	25	31.3	38.4	36.3	42.7
50	10	11.3	21.5	-	28.2
	15	16.1	23.9	21.7	29.8
	20	19.5	28.6	24.7	37.1
	25	25.5	34.4	30.5	36.3
	30	24.2	-	-	-
	50	40.7	-	-	-



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Figure 7: Graph of experimentally measured permanent mid-point deflection versus charge mass

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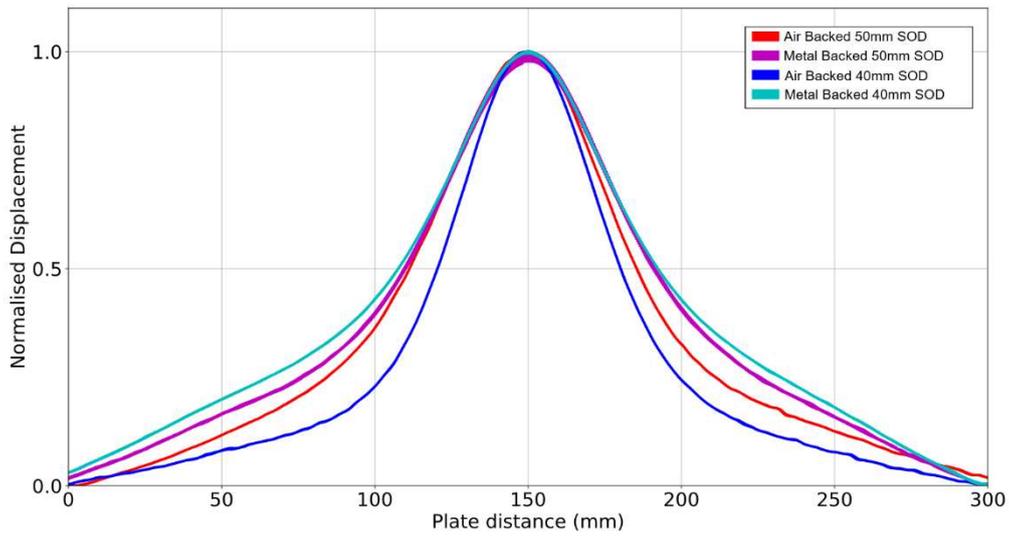


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230 Figure 8: Experimentally measured permanently deformed mid-line profiles from plates subjected to
 231 15g metal-backed detonations

232 The permanently deformed mid-line plate profiles for the 15g air and metal-backed charge
 233 detonation tests are shown in Figure 8. The profiles cluster according to SOD, indicating good
 234 repeatability of the loading and response. As expected, the 40 mm SOD plates exhibited higher
 235 deflection magnitudes due to load localisation. All the plates exhibited a localized central peak
 236 atop a global dome, with the metal-backed test plates appearing to be superficially similar to
 237 the air-blast loaded plates. The obvious difference is the mid-point displacement magnitude
 238 (which increased with decreasing SOD and with the presence of the metal backing).

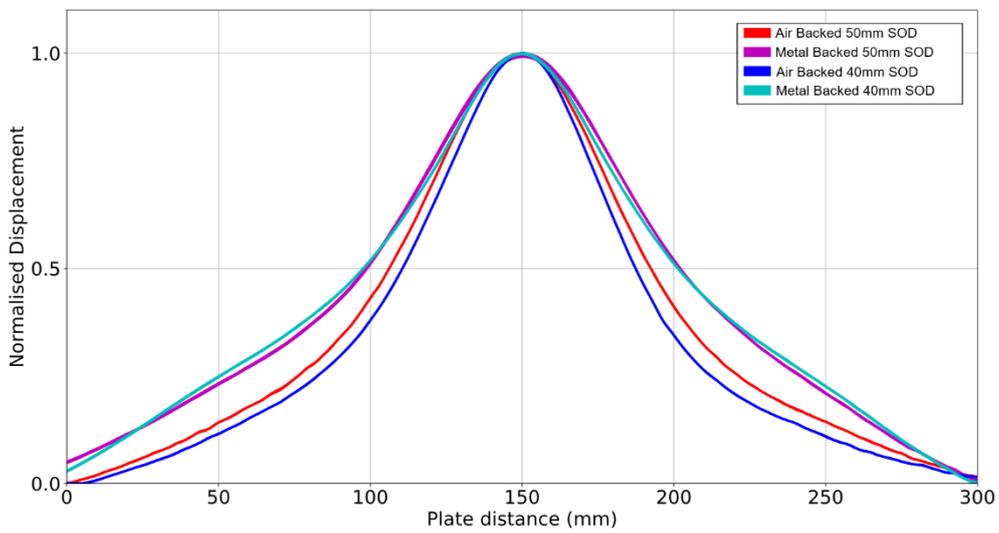
239 The differences in the profile shape become more obvious when the deflections are normalized
 240 against peak midpoint deflection, as shown in Figure 9. The air-backed plates exhibited a more
 241 localized deformation than the metal-backed plates. For air-backed detonations, the differences
 242 in profile shape due to SOD are most evident at 10g, shown in Figure 8a. At 20g and 25g, the
 243 air-backed test plate profiles are similar to each other (Figures 8b and 8c), whereas at 10g the
 244 profile of the 50 mm SOD air-backed test plates are similar to the 50 mm SOD metal-backed
 245 detonations. There is little discernible effect of SOD on profile shape for the metal-backed
 246 tests, especially at 20g and 25g. The metal-backed test plate deformation is more localised at
 247 10g but appears more conical at 25g.



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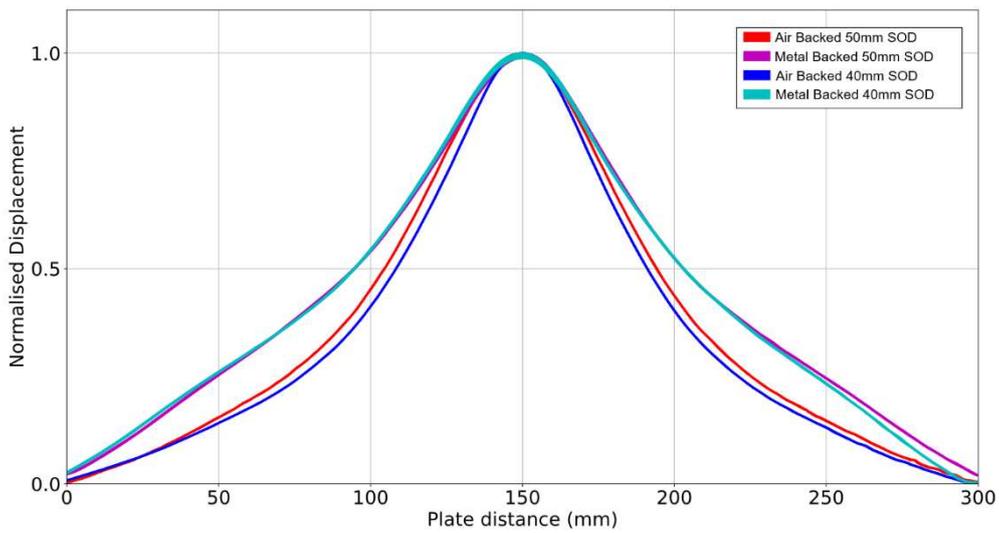
(a) 10g detonation



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(b) 20g detonation.



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(c) 25g detonations

254

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Figure 9: Normalised out-of-plane permanent displacement profiles for air and metal backed charge detonations

256 3.3 Transient deflections

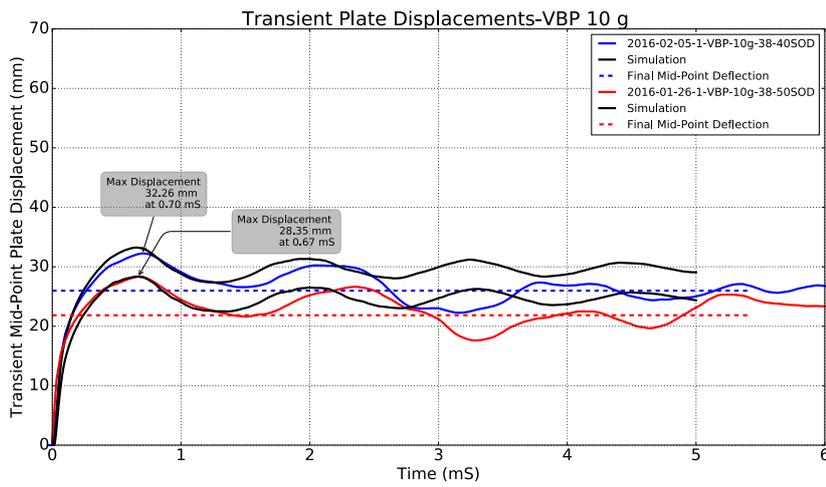
257 The transient data obtained using DIC is presented in two ways. Firstly, the transient deflection-
258 time histories of the midpoint are shown in Figure 10. Secondly, the evolution of the plate
259 profile is illustrated by looking at the out of plane displacement along the mid-line. This is
260 shown at discrete points in time together with the observed final deformation profile in Figures
261 10-14.

262 Figure 10a shows mid-point deflection-time histories from 10g metal-backed detonations at
263 different SODs with the red and blue curves representing the experimental results and the black
264 curves representing the simulation results (the simulations are discussed later in the paper). As
265 might be expected, the 50 mm SOD has a consistently lower magnitude transient response in
266 keeping with the permanent deflection observations. The peak mid-point deflections occurred
267 at similar times (approximately 700 μ s) in all tests, and the elastic vibration is similar. Figure
268 10b shows comparable results for 20 g metal-backed detonations. Once again, the 50 mm SOD
269 had a consistently lower magnitude displacement due to the increased SOD. The peak mid-
270 point deflections occurred at the same time and the elastic vibration was similar.

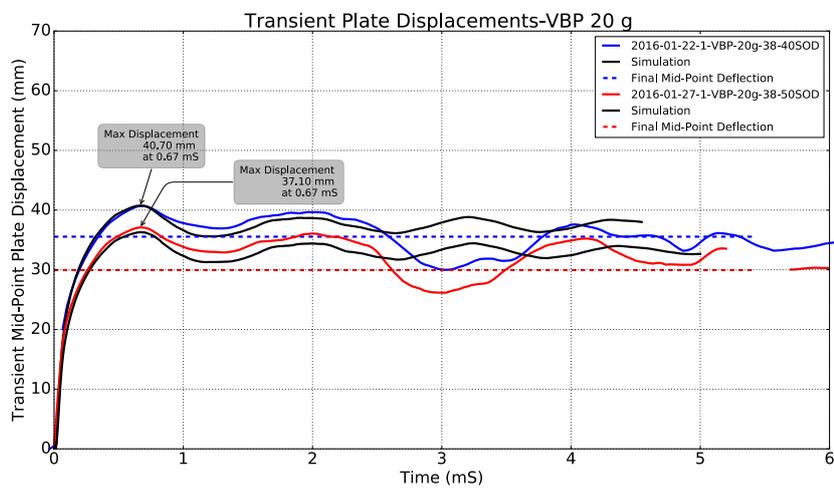
271 From Figure 10c, which shows mid-point deflection time histories from the 25 g air-backed
272 detonations, it is evident the elastic recovery of the test plates rebounds below the dashed line
273 of permanently deformed plate within the first 2 ms. This did not occur in the metal-backed
274 test plate responses (illustrated in Figure 10a and Figure 10b). The metal-backed rebound
275 characteristic is similar to responses observed in buried charge explosions that have a much
276 longer loading phase due to the ejecta impinging on the test plate (31) (22). The experiments
277 suggest there may be an extended loading duration for the metal-backed detonations that is not
278 present in the air-backed configuration.

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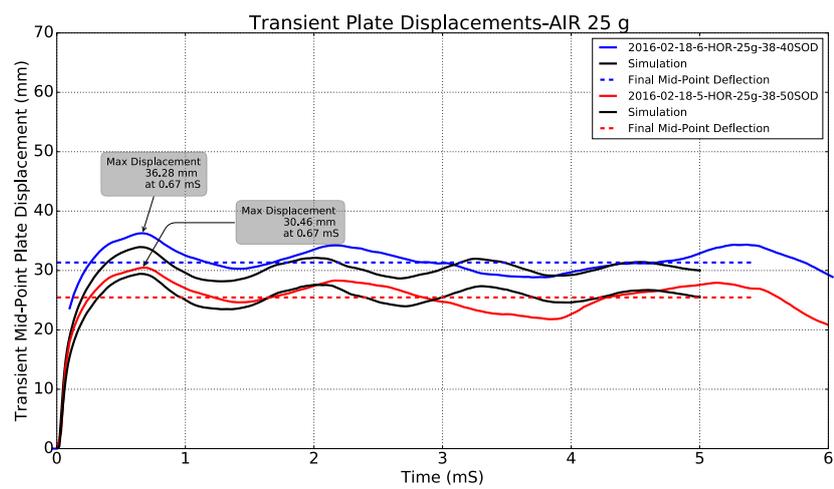
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282 (a)



283 (b)



284 (c)

285 Figure 10 Transient midpoint deflections obtained using DIC (a) 10 g metal-backed detonations (b)
286 20 g metal-backed detonations (c) 25 g air-backed detonations, 40 mm SOD

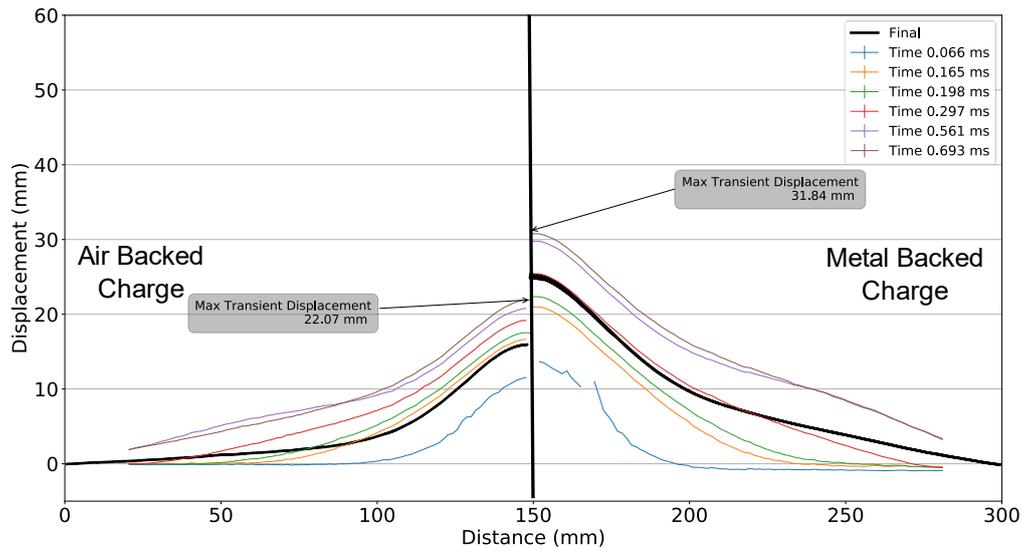
287 The transient deformation profiles for 10, 15, 20 and 25 g metal-backed detonations are shown
288 in Figure 11 to Figure 14 respectively. On the left hand side of each figure are the air-backed
289 test plates, while the metal back test plate profiles are shown on the right hand side of each
290 figure at the same discrete time intervals. Some of the early time curves at 66 μs (the blue
291 curves) are either slightly irregular or missing due to motion blur, particularly at higher charge
292 masses when the initial velocity of the plate was greater.

293 The evolution of the profile was similar for each charge mass, but the shape was more localised
294 deformation in the 40 mm SOD series. The metal backed plate deformation first appeared to
295 be localised to a 100mm diameter plastic hinge in the centre of the plate (at 66 μs). The plastic
296 hinge moved radially outward and transitioned into a more global and final profile later in the
297 response. The metal-backed plates exhibited greater deflections, with the difference in the early
298 time response most significant at lower charge masses. Apart from the deflection magnitude,
299 the early-time response was similar in the metal-backed and air-backed test plates, and also
300 similar to findings by Tiwari et al (33) for air-blasted plates.

301 After 165 μs , the plastic hinge had moved radially outwards and had a 150mm diameter. The
302 shape of the deformed section was conical between the midpoint and the plastic hinge. By 297
303 μs , the hinge reached a diameter of approximately 250mm and the general profile was bell-
304 shaped with a point of inflection forming at approximately 100mm diameter. Up to this point,
305 the air-back and metal-backed plates followed a similar response, albeit with different peak
306 deflection magnitudes. However, additional deformation along the plate periphery occurred in
307 the metal-backed plates later in the response that was not evident in the air-backed transient
308 deformation profiles.

309 This point of inflection in the central region became more noticeable and was most pronounced
310 at 561 μs as the plate approached its maximum transient deformation (for both air and metal-
311 back test plates). The plates reached maximum transient deformation between 660 and 700 μs ,
312 and the point of inflection became less significant. In all cases, it was evident that the transient
313 profile shape varied significantly from the permanently deformed shape measured post-test.
314 This underlines the importance of capturing the transient behaviour of blast-loaded structures,
315 even those made from materials with large plastic capacity such as steel, and has implications
316 for the validation of numerical models of blast-loaded steel structures.

317

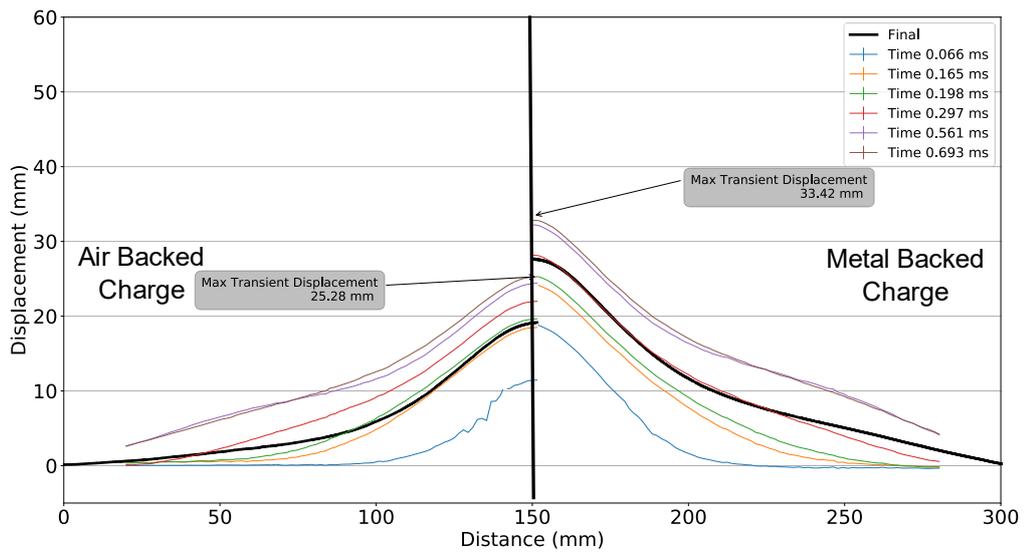


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Figure 11: The experimentally measured transient plate profiles for typical 10g detonations (50 mm SOD) for discrete time intervals (colour) and the final deformed plate profile (black).

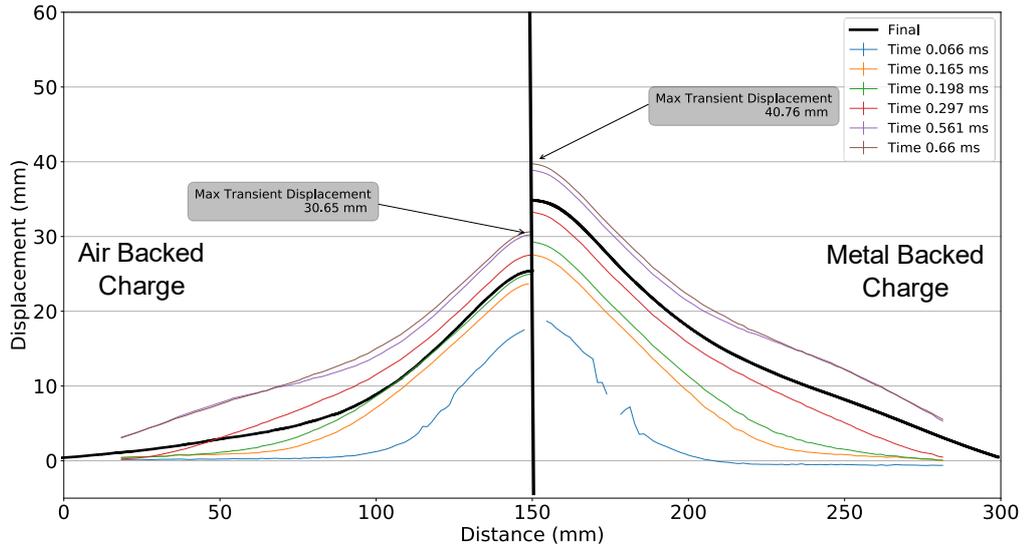


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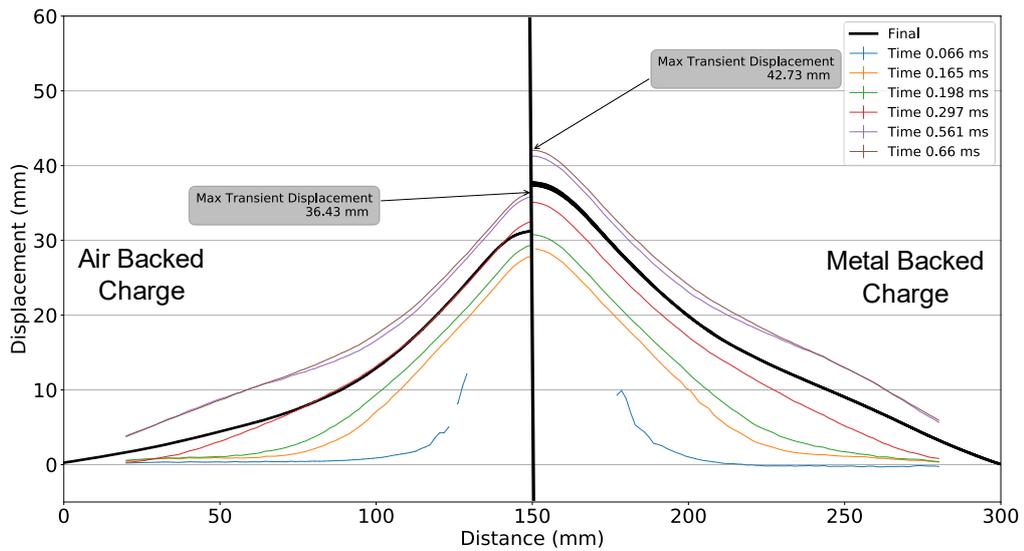
323

Figure 12: The experimentally measured transient plate profiles for typical 15g detonations (40 mm SOD) for discrete time intervals (colour) and the final deformed plate profile (black).



324

325 Figure 13: The experimentally measured transient plate profiles for typical 20g (40 mm SOD)
 326 detonations for discrete time intervals (colour) and the final deformed plate profile (black).



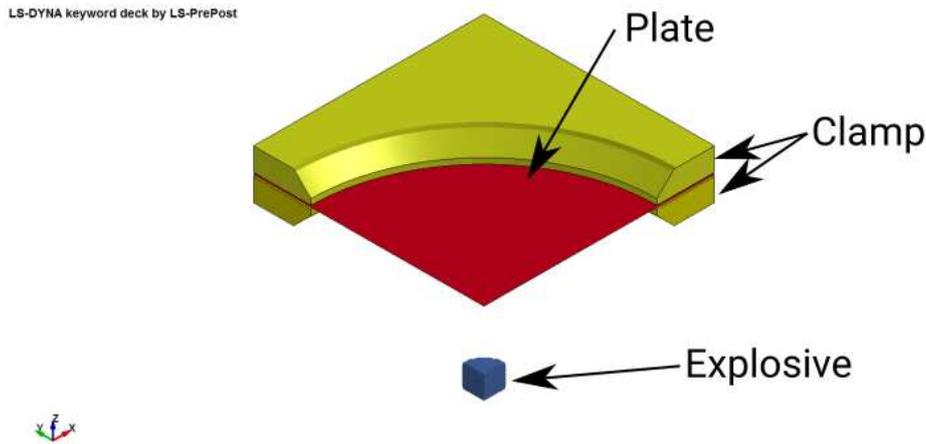
327

328 Figure 14: The experimentally measured transient plate profiles for typical 25g detonations (40 mm
 329 SOD) for discrete time intervals (colour) and the final deformed plate profile (black).

330

331 **4. Numerical simulations**

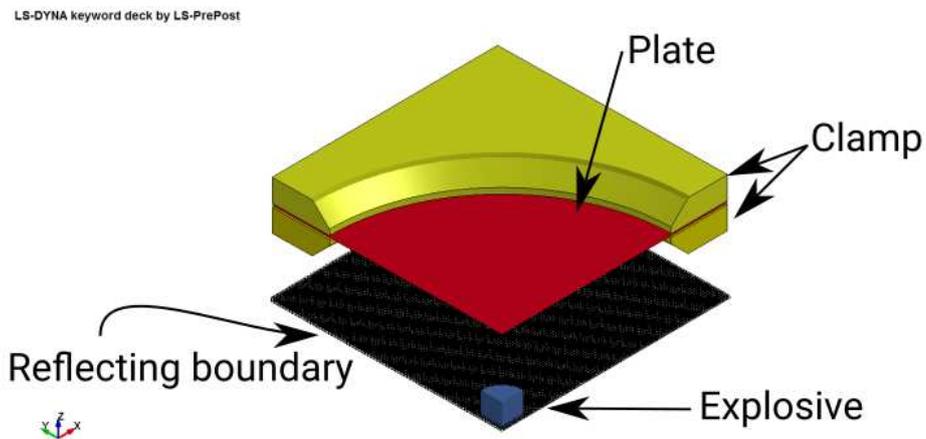
332 A numerical model was developed to aid in the understanding of the transient deformation of
333 the test plate. The test plate, clamp frame and explosive were modelled using the Multi Material
334 Arbitrary Lagrange Eulerian (MMALE) Fluid Structure Interaction (FSI) approach in LS-
335 Dyna. Figure 15 shows a quarter symmetry representation of the models (one for each charge
336 backing type).



337

338

(a) air-backed detonations



339

340

(b) metal-backed detonations

341

Figure 15: LS Dyna model schematics

342 **4.1 Model components**

343 The test plates were modelled using Lagrangian shell elements (ELFORM 16, fully integrated
344 shell elements) and a Johnson Cook (MAT15) material model which was calibrated using
345 tensile test data which depicted a fracture strain of 35-40% (32). A 2 mm element size was

346 chosen for the test plates as this offered the best compromise between minimising leakage
 347 forces and reasonable computational times. Table 3 presents the values used in the material
 348 formulations. The maximum plastic strain captured in any of the models was 15% which is
 349 well below the 35% noted for fracture of the material and no failure modelling was needed.

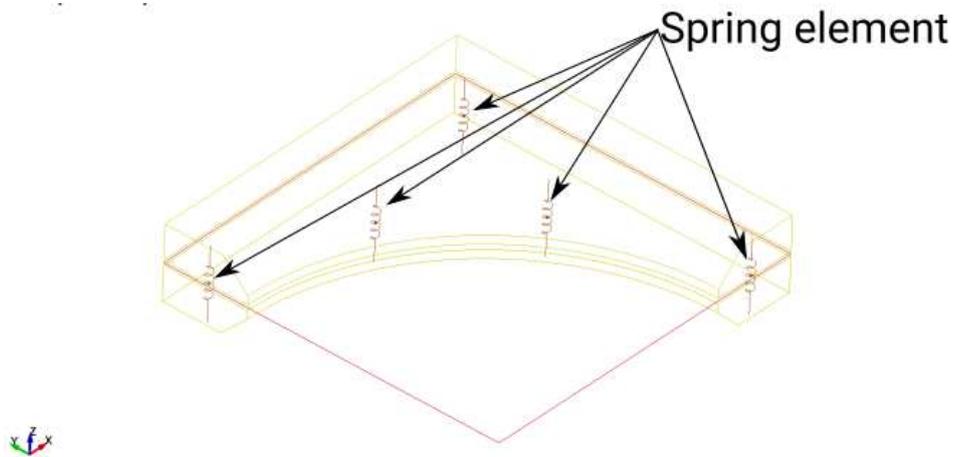
350 Table 3 Material formulation for the test plates. (31)

Material Parameters	Density	Youngs modulus	Poissons Ratio	Taylor Quinney	Specific heat	Reference strain rate
	P	E	V	X	C _p	ε' ₀
	7830 kg/m ³	206 GPa	0.29	0.9	452 KJ	0.0014
Numerical Model Parameters						
Johnson Cook Variable	A	B	n	C	m	
	352 MPa	642 MPa	0.5597	0.032	0.81	

351
 352 The clamp frames were modelled as an elastic material with a Youngs Modulus of 210 GPa.
 353 The bolted connections were modelled using spring elements to simulate the clamping force,
 354 which resulted in an equivalent bolted pressure of 240 MPa (similar to results reported by
 355 Gerretto (34)). Although this method is not as thorough as modelling the entire bolt and
 356 connection, it is effective in producing the clamping force between the two clamp frames that
 357 restrain the test plate. this method was considered suitable (and was computationally more
 358 efficient than a more complex representation) because no significant pull in or tearing failure
 359 was observed during the experiments. A schematic representation of the clamp plate assembly
 360 showing the spring elements is given in Figure 16. Contact between the plate and clamp frame
 361 was simulated using a surface-to-surface penalty-based contact algorithm with a coefficient of
 362 friction of 0.17, based on the findings of Gerretto (34).

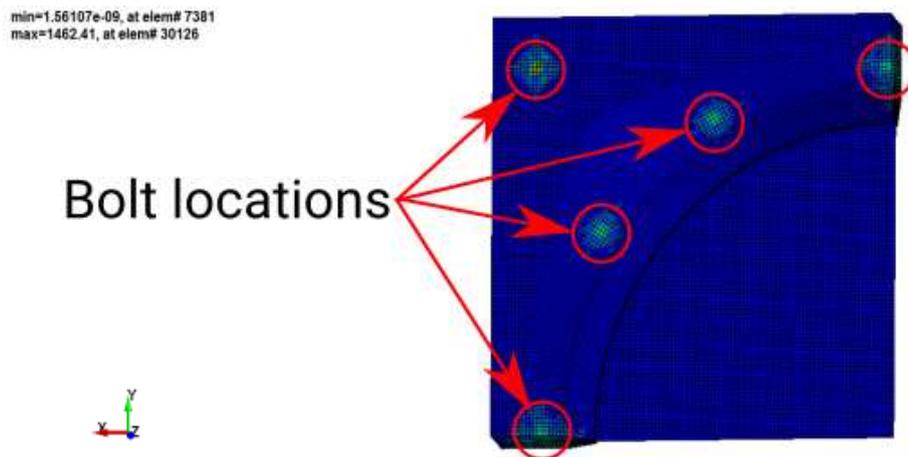
363 The air was represented as a 200x200x200mm block divided into 2mm cubed elements
 364 following the results of the mesh convergence study for a similar configuration (34). Geretto
 365 (34) found that the size of the air mesh had a much smaller effect than the size of the plate
 366 mesh. Two boundary conditions were imposed on this block (to represent the XZ and YZ
 367 symmetry conditions) and all other surfaces were defined as free boundaries, allowing out flow
 368 of the Eulerian air formulation. The air was modelled using an ideal gas equation of state and
 369 a null material. Tracer points were placed at 20 mm intervals from the plate centre (plus an
 370 additional point placed 10mm from the plate centre) to predict the pressure at discrete points

371 along the front face of the test plate. These points were selected to line up with the experimental
372 data collected by Rigby et al (24).



373

374 (a) schematic showing the springs used to represent the bolted connections



375

376 (b) effective stress contour plot showing the clamp bolt points (indicated by the red circles and
377 elevated stress regions) (12)

378 Figure 16 Representations of the clamp plate assembly

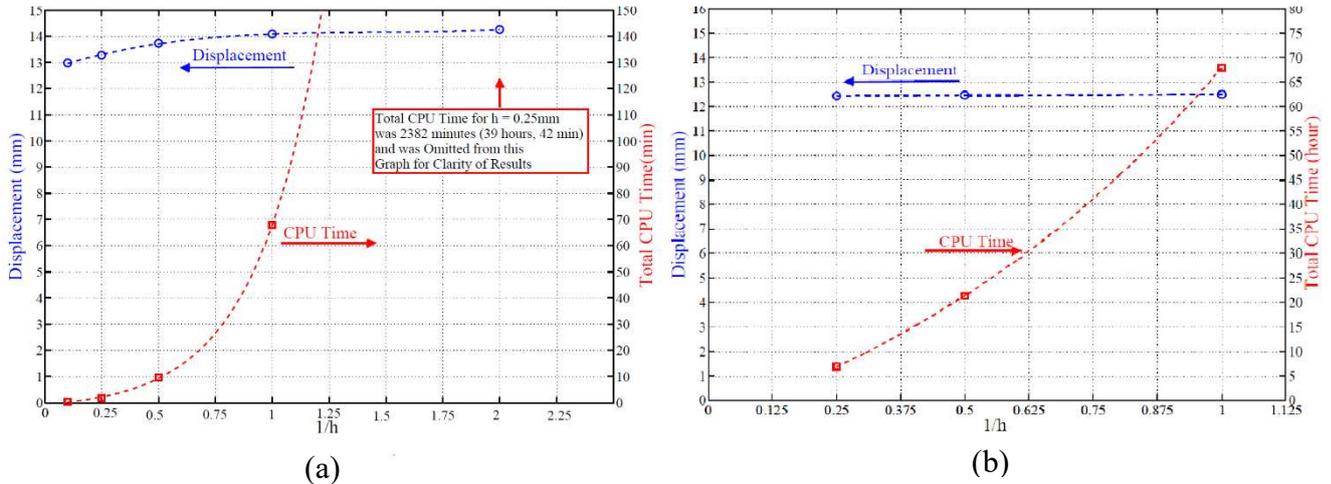
379 The PE4 was modelled as a cylinder using an initial volume fraction description, which filled
380 the container with the explosive material. The JWL equations of state, in conjunction with the
381 high explosive burn model, were used to describe the explosive shown in Table 4. The volume
382 of the explosive cylinder was discretised into elements that fill the air mesh. The coupling
383 between the explosive products and the test plate was modelled using a penalty-based
384 approach. The metal backing plate was numerically represented as a rigid reflecting boundary
385 condition imposed on the lower node set of the air block when required, by imposing
386 displacement conditions δx , δy and $\delta z = 0$ on the node sets. The ALE fluid flow through the

387 boundary was controlled by implementing *ALE_ESSENTIAL_BOUNDARY card that
 388 allows for no flow in all directions to be defined on an element set.

389 Table 4 Table of PE4 properties used

ρ_0 (kg/m ³)	D (m/s)	PCJ (GPa)	A (GPa)	B (GPa)	R_1	R_2	ω	E_0 (GPa)
1616	8193	28	609.77	12.95	4.5	1.4	0.25	9

390



391 (a)
 392 (b)
 Figure 17 Mesh sensitivity and convergence analysis for plate mesh (a) and air mesh (b)

393 A mesh sensitivity and convergence analysis was undertaken as shown in Figure 17, which
 394 varied the plate element size (a) and the air mesh size (b). For the plate study a simple spherical
 395 charge of 50g PE4 detonated 100mm from the target plate and the pressure was applied using
 396 CONWEP. The element length (h) was varied and the computational time required for
 397 reasonable convergence was observed. In the plate convergence study, element sizes of smaller
 398 than 2mm were found to cause leakage of the explosive products which started to pass through
 399 the plate. As a result, the plate mesh size of 2mm was chosen as it optimised the element
 400 leakage in the MMALE formulation.

401 The Air mesh refinement was assessed by varying the element length with the same
 402 configuration as the plate mesh, only the MMALE formulation was used. As changes in the air
 403 elements had very little effect, a 2mm Air mesh element size was chosen as it was
 404 computationally efficient while not effecting the predicted displacement of the plate.

405 **4.2 Running the simulations**

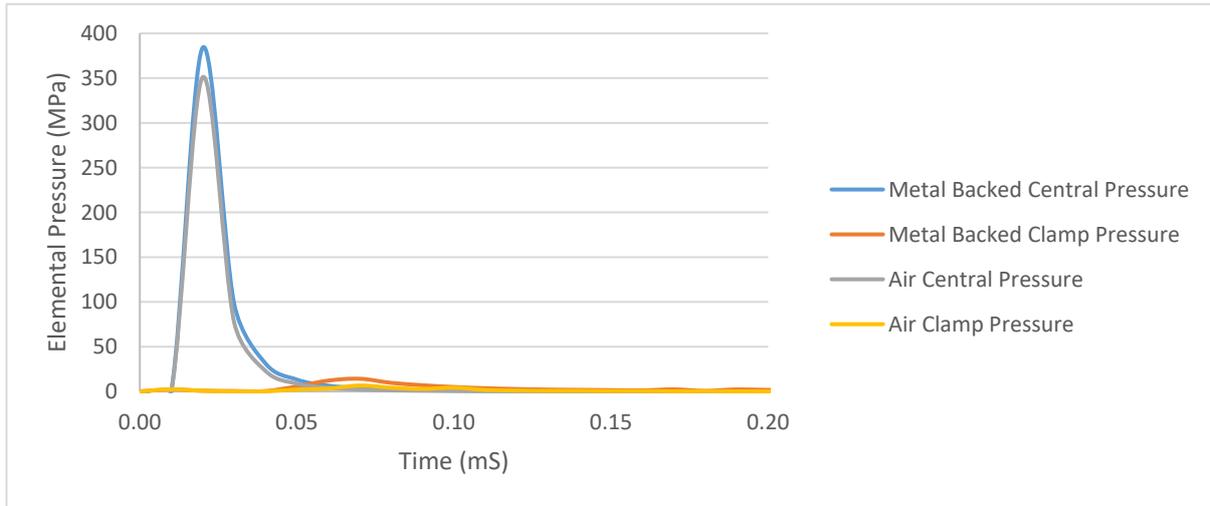


Figure 18 Comparison of the pressure time histories for the two simulations.

406 The simulations were executed in three phases (loading, deformation, damping). The three
407 phases are illustrated in a typical displacement-time history curve shown in Figure 18. The
408 second and third phases were initiated using a re-start in LS-Dyna that reads the final state of
409 the previous simulation step and modifies the input deck according to the contents of the restart
410 file. During the first phase (loading) the explosive detonated and the explosive products
411 expanded. The resulting pressure wave interacted with the plate, so complete interaction of the
412 MMALE and the test plate was needed. This phase was terminated after 450 μ s, which was
413 determined to be sufficient time for the impulse transfer to occur between the Eulerian blast
414 wave, the explosive products and the test plate. Pressure-time histories for the central elements
415 located 1mm before the target plate and the outer elements in the simulations located in the
416 corner of the clamp frame are shown in Figure 20 illustrating that the significant pressure
417 loading event is over inside the first 450 μ s that the MMALE was active in the simulation. No
418 significant pressure was measured in the simulations after 450 μ s. A 40 MPa peak pressure
419 difference for the two simulations was observed which had the same expected arrival time. The
420 Metal backed simulation shows a slightly longer and higher pressure loading in the centre of
421 the plate and a higher pressure loading at the clamp indicating a higher recirculation pressure.

422 The Eulerian elements were deleted from the simulation at the beginning of the second
423 (deformation) phase but the Lagrangian elements were allowed to deform. This phase was
424 extended to allow the simulated test plate to plastically deform into its final shape and then
425 elastically oscillate in a similar fashion to that seen in the experimental data. This phase ran

426 from 450 μ s to 5000 μ s. The final phase applied damping to the plate so that the elastic
427 oscillation of the test plate would settle to its final deformed shape.

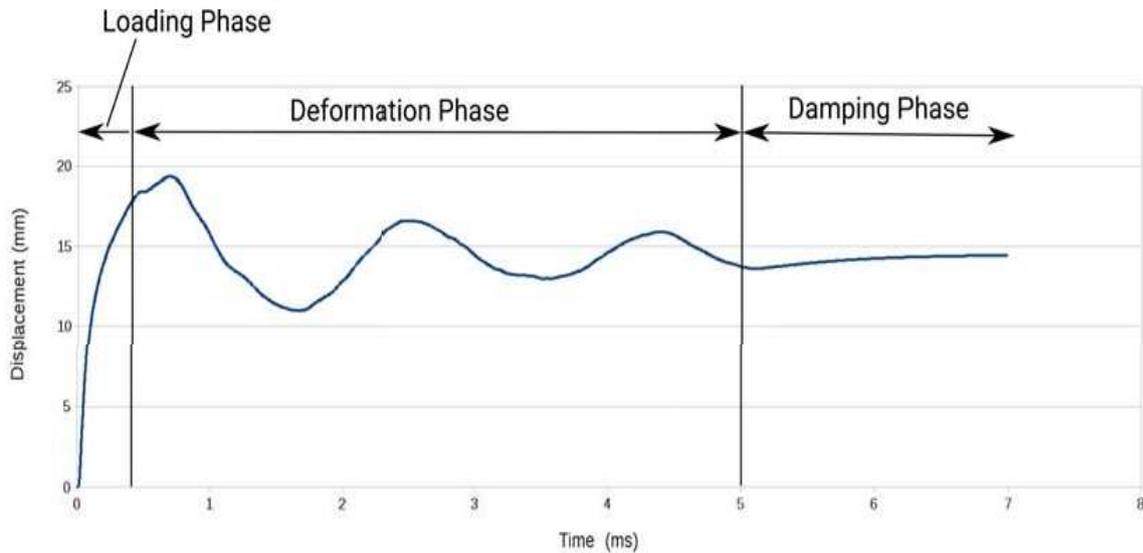
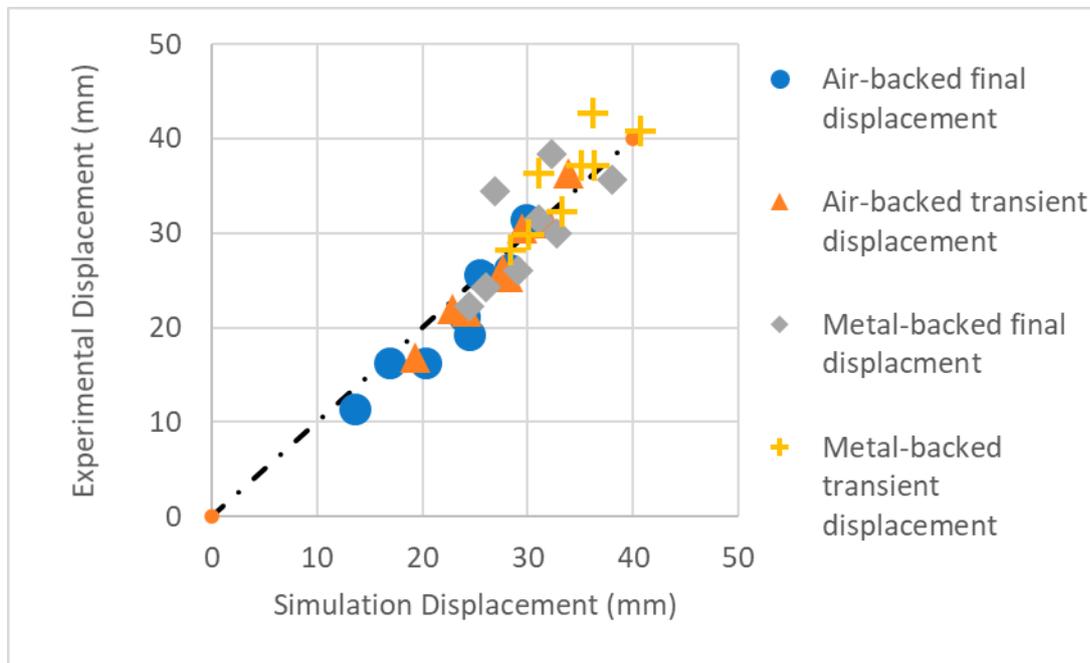


Figure 19: Graph of simulated mid-point deflection versus time, showing the three simulation phases

428 5. Insights from the numerical simulation results

429 The simulation results correlate well with the experimental results, as shown in Figure 21,
430 which clearly shows the linear relationship. While there is some scatter in the results, these lie
431 within one plate thickness of variation that is well within the accepted experimental variation
432 expected.



433
434 Figure 20: Correlation of experimental and simulation results for both 40mm and 50mm SOD,
435 showing transient and permanent deformation for air-backed and metal-backed charges.

436 The pressure profiles experienced by the plates are shown in Figure 20. The significant
 437 difference in the shape of the initial central loading of the plates can clearly be seen in Figure
 438 20 (a) where the regions in red are pressures higher than 20MPa on the left for the air charge
 439 and on the right for the metal backed charge. The high pressure region that interacts with the
 440 plate is clearly extending out over a larger central region in the metal backed charge. As this
 441 evolves and moves outward toward the clamp boundary the pressures in the air charge drop
 442 more than the metal backed charge and the zone located in the clamp boundary is only exposed
 443 to pressures of around 10 MPa while the metal backed charge is exposed to over 20 MPa
 444 pressures. This clearly shows the re-circulation effect and is one possible place where
 445 additional impulse is imparted on the plate without significantly contributing to the plate
 446 deformation.

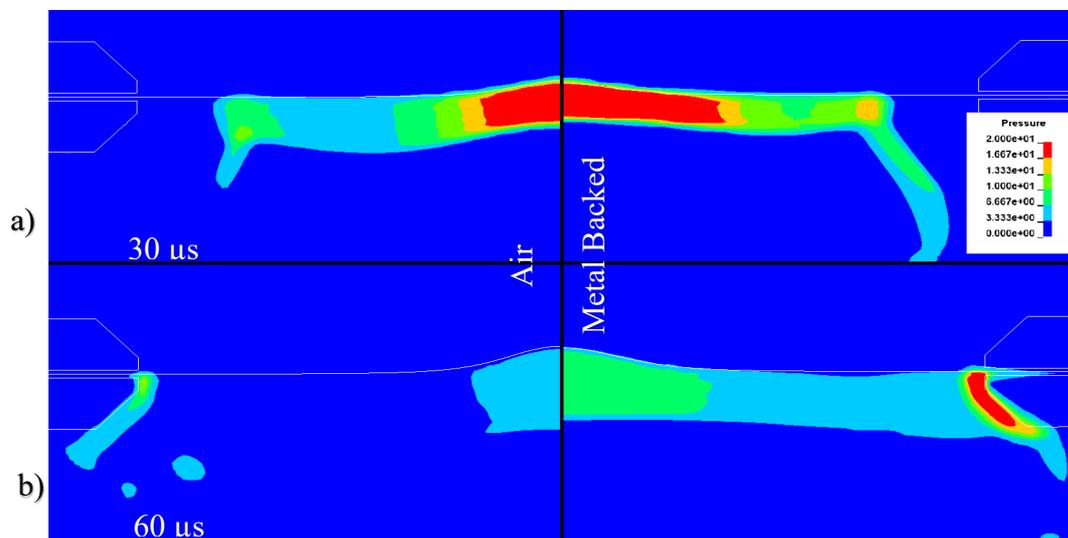


Figure 21 Pressure contours shown at 30 μs (a) and 60 μs (b) for 15g charges of both Air (left) and Metal backed (right) charges.

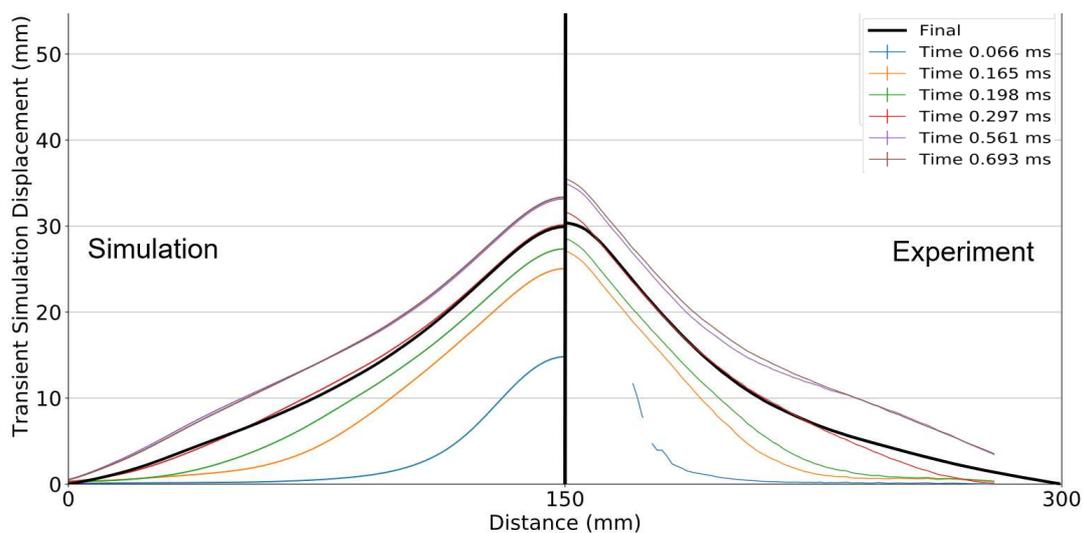


Figure 22: Comparison of simulated and experimental measured transient mid-line displacement profiles for 40 mm SOD, 25g air-backed detonation.

450 **5.1 Air-backed charge simulations**

451 The air backed charge simulations showed that it was possible to approximate the experimental
452 plate deformation results fairly well. The transient mid-point displacement histories were
453 similar to the experiments, illustrated by agreement between the curves shown in Figure 9c for
454 25g air-backed charge detonations. There is a slightly different period of post-peak oscillation
455 between the simulations and the experiments, with the simulated plate having a slightly shorter
456 period. This was attributed to the slight mismatch between the experimental clamp frame and
457 the more idealised simulated boundary condition.

458 While the permanent midpoint deflections did not always exactly match the experimental
459 conditions, they were within one plate thickness of the experimental results, considered to be
460 within the limits of experimental repeatability (29) (30). The simulations produced deformed
461 plate profiles that accurately reflected the experimental plate profiles. An example is shown in
462 Figure 22, for a 40mm SOD and 25g PE4 charge. which compares the transient mid-line
463 displacement profiles for the simulations and the experiment. The simulation slightly over-
464 predicts the peak and under-predicts the transient displacement magnitude at the plate centre.
465 The overall evolution of the profile is similar.

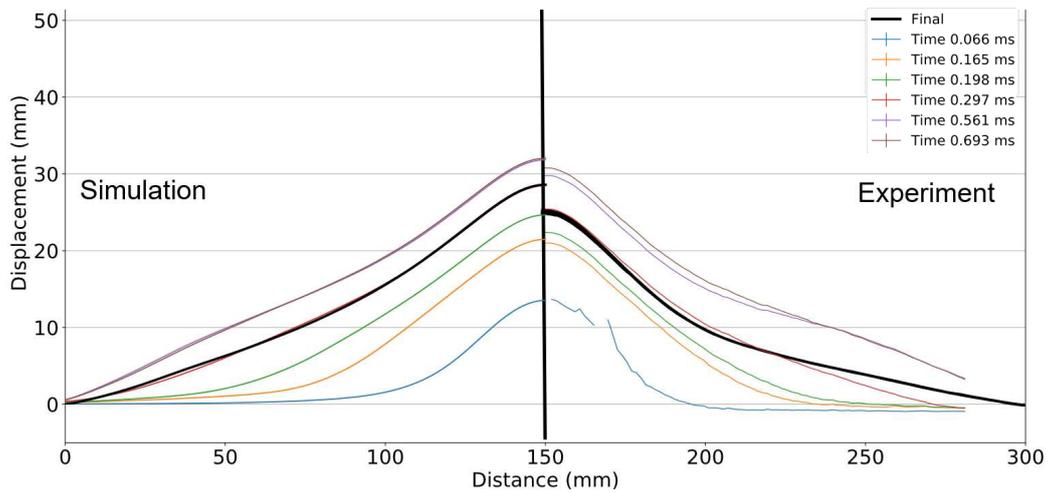
466 **5.2 Metal-backed charge simulations**

467 The metal-backed charge simulations closely approximated both the transient midpoint
468 deflections and the final midpoint deflections of the experiments, as evident in Figure 21. The
469 transient mid-point displacement histories were similar to the experiments, illustrated by
470 agreement between the curves shown in Figure 9a and 9b for the 10g and 20g metal-backed
471 charge detonations. The slight elongation in the second peak displacement evident in the
472 experimental at 20g was also present in the simulations, although there is some divergence in
473 the phase of oscillation beyond 3 ms, attributed to the clamp frame idealisation in the
474 simulations.

475 The transient and final deformed plate profiles for typical simulations of the metal-backed
476 charge configuration are shown in Figure 23. The transient displacement begins in the central
477 region, moving out to the edges, as previously described. As was evident in the air-backed
478 detonation simulations, there is a small over-prediction in the peak and final displacement
479 magnitudes. The very early-time response appears to match the experiment particularly well.

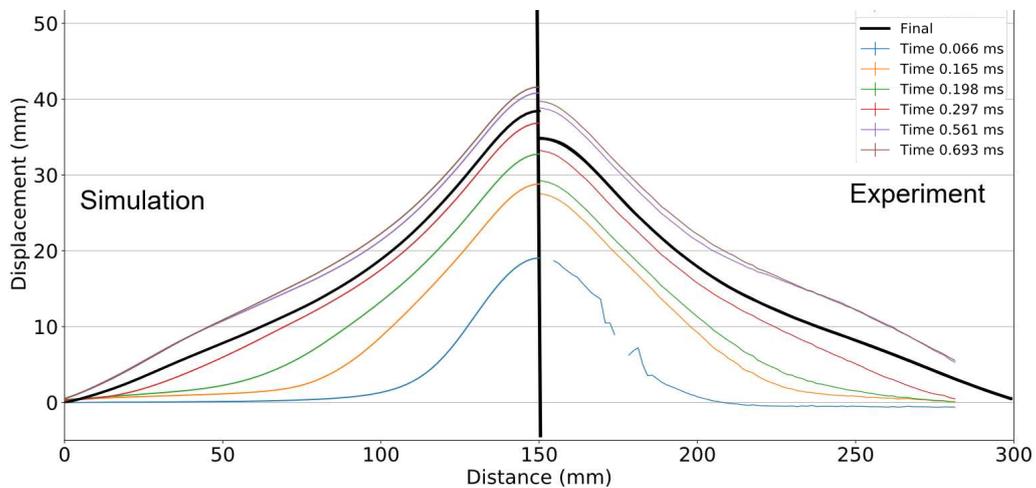
480 The metal-backed 40mm SOD detonations, across the charge range of 10-25g, have similar
481 normalised permanent plate displacement profiles compared to their experimental counterparts,

482 as shown in Figure 24. The black curves in Figure 24 represent the experimental results while
 483 the green curves represent the simulation results. The experimental response is slightly more
 484 localised. In general, the curves overlap well, with some small variations in the region of the
 485 experimental point of inflection, something that is less visible in the simulations. These figures
 486 illustrate how well the simulations captured the overall response of the experiments and lend
 487 credibility to the results obtained, particularly the early time impulse and pressure loading.



488
489

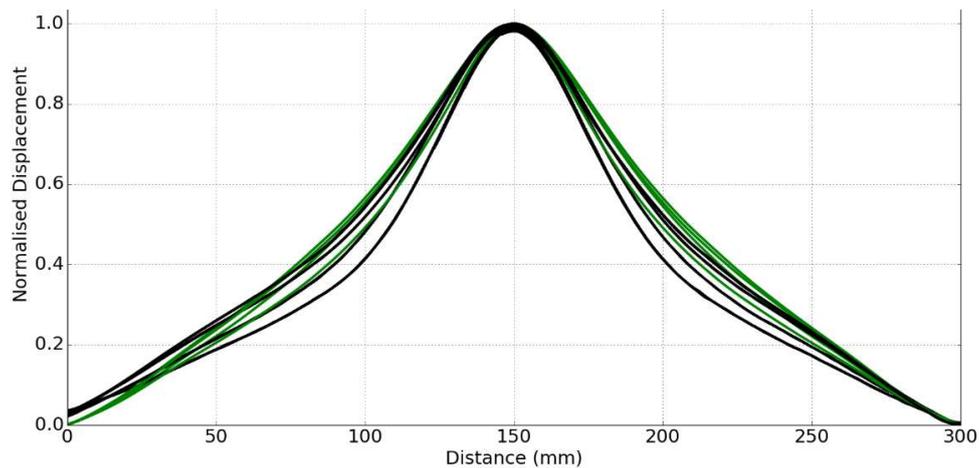
(a) 10 g PE4



490
491

(b) 20g PE4

492 Figure 23: Comparison of simulated and experimental measured transient mid-line displacement
 493 profiles for 40 mm SOD metal backed detonations



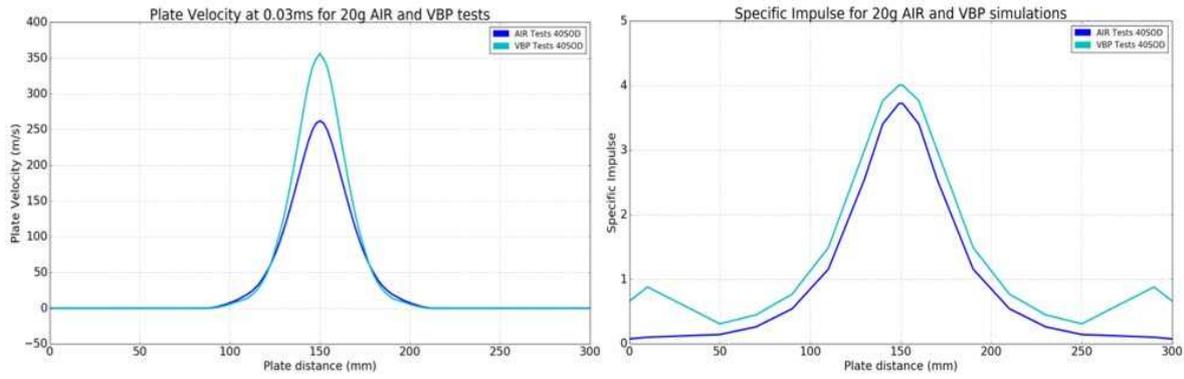
494

495 Figure 24 Normalised experimental (black) and simulation (green) final deformed plate profiles for
 496 the metal backed configuration at a 40 mm SOD.

497 **5.3 Influence of charge configuration on specific impulse and plate velocity distribution**

498 Figure 25 shows plate velocity and specific impulse predictions for 20 g detonations ($D/H =$
 499 3.5) for both charge configurations. The simulated pressures indicated that the pressure
 500 readings across the whole plate were higher for the metal-backed charge detonations. The
 501 specific impulse data, plotted in Figure 25b for a 20g detonation, represents the integral of the
 502 pressure-time data across the plate. There is a slight general increase in the impulse across the
 503 plate and a more marked increase in impulse along the periphery in the metal-backed
 504 detonation simulations. The increase shows that the clamp frame produced a recirculation
 505 effect (leading to pressure accumulation) along the clamp boundary (35) that was not present
 506 in the air-backed charge detonations. The air-backed charge simulations do not show the
 507 pressure accumulation along the boundary, so this is not the result of the clamp frame geometry,
 508 unlike the phenomenon noted in reference (36). Nor is it a straightforward charge height effect
 509 on the initial forward axial impulse, such as that observed by Kennedy (37).

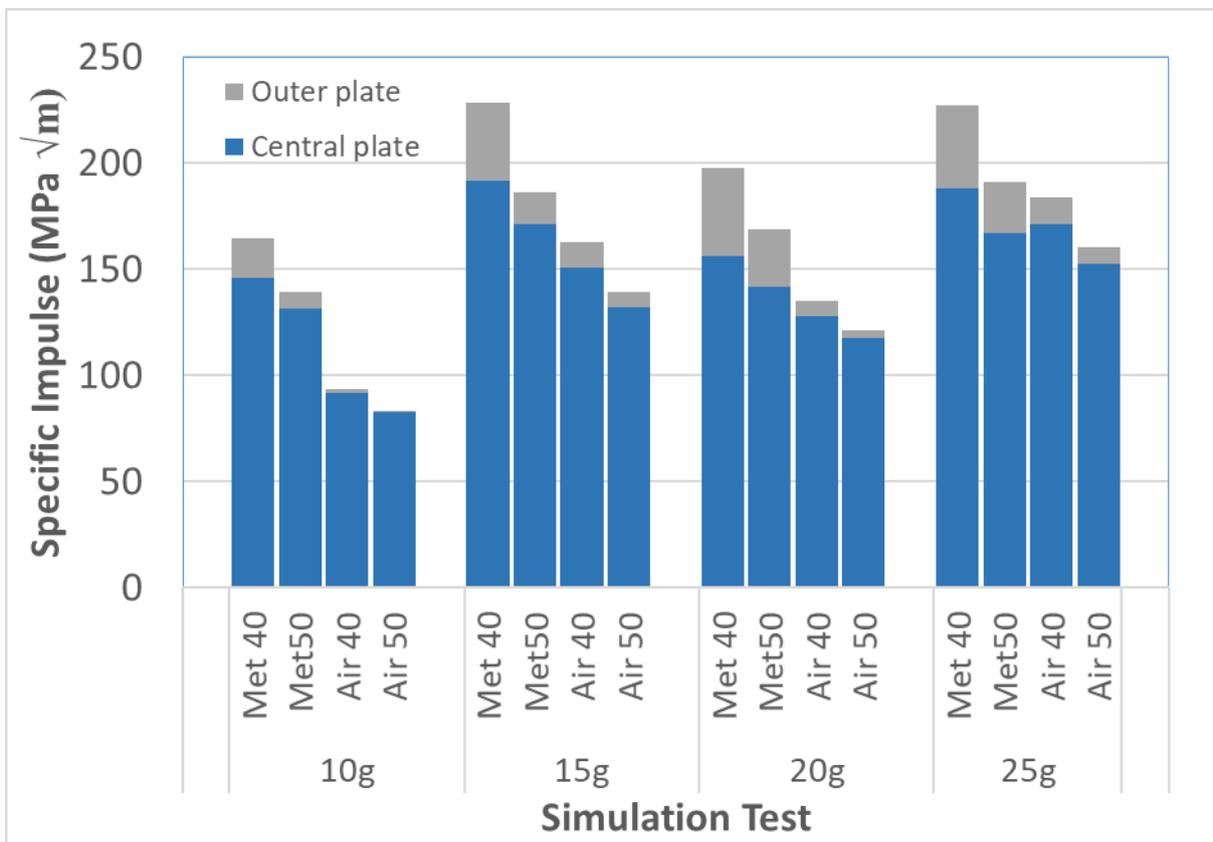
510 The metal backing caused reflected pressure from the rigid surface towards the test specimen
 511 in the region of the charge. This produced a localised increase in the initial plate velocity,
 512 shown in Figure 25a. The localisation effect of the metal backing caused a 40% increase in
 513 mid-point plate velocity 30 μs after detonation. The combination of recirculated pressure
 514 accumulation at the periphery and the pressure reflection from the detonation on the metal
 515 backing surface caused the increased impulse transfer to the plate. The recirculated pressure at
 516 the clamp is known to increase the impulse transfer without producing a similar increase in
 517 plate deflection (35). This is a reason why the experimentally obtained plate deflections did not
 518 increase as significantly as the impulse increased when the metal backing was used.



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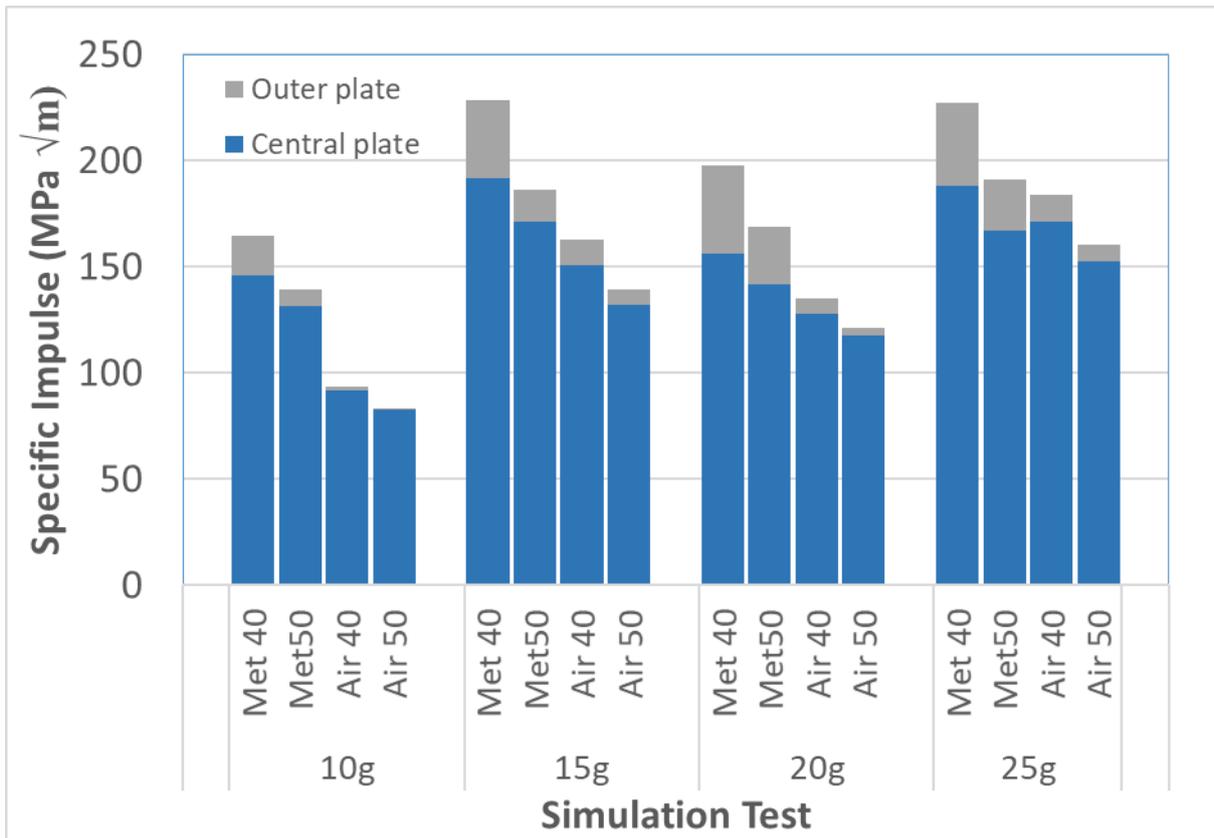
Figure 25: Graphs showing the simulated (a) plate velocity and (b) specific impulse distributions across the plate for the 20g detonations backed by air and metal 40mm SOD



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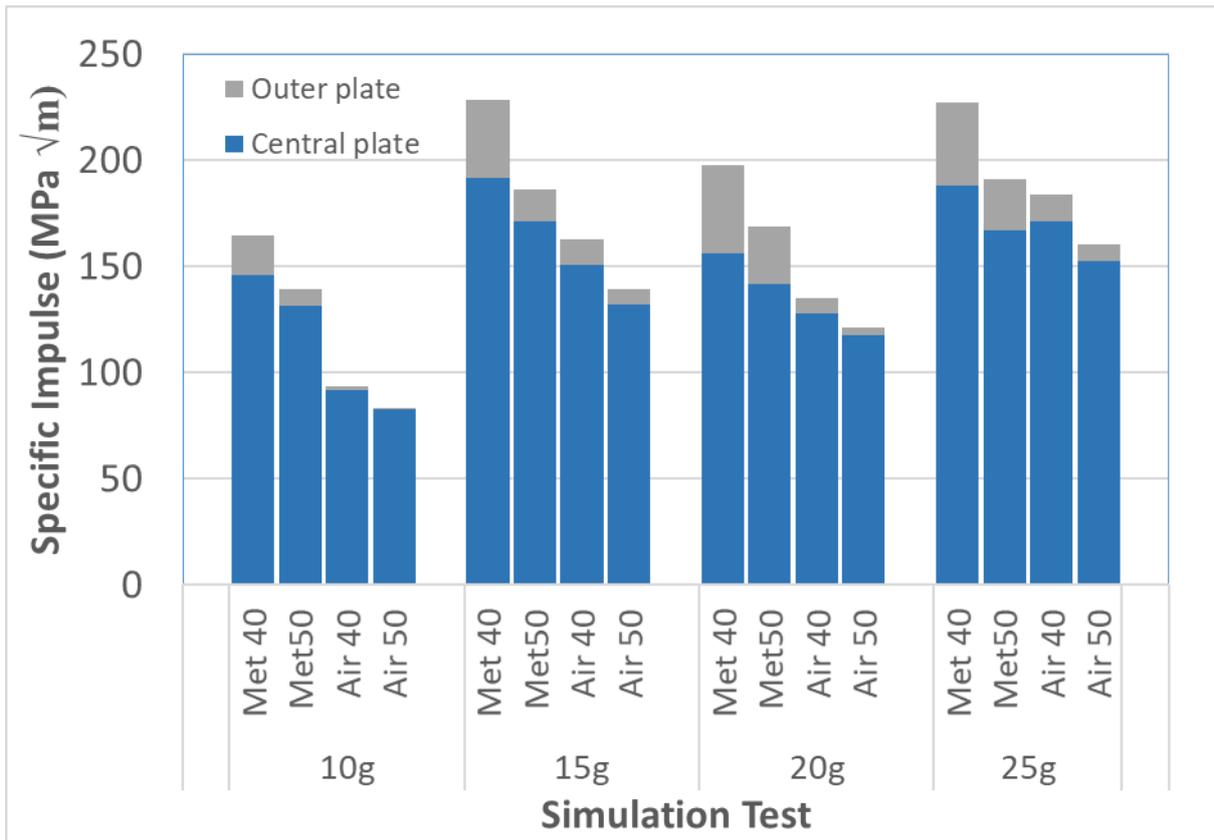
Figure 26: Bar chart showing the simulated specific impulses in the central region and the plate periphery for the air and metal backed detonations (blue indicates the central area, 200 mm diameter, and grey indicated a 50 mm wide outer annulus between the central area and the clamped boundary)



526

527 Figure 26 shows a bar chart of the specific impulse distribution in the two plate regions, for
 528 different charge masses, SODs and backing types. The blue part is the specific impulse for the
 529 central area (200 mm diameter) and the grey part indicates the specific impulse over a 50 mm
 530 wide outer annulus (between the central area and the clamped boundary). The results confirm
 531 that the observations from Figure 21 (for 20g detonations at 40 mm SOD) apply over the full
 532 range of tests reported herein. The central 200 mm diameter portion of the plates experienced
 533 an expected increase in impulse with a decrease in SOD. All curves follow the same trend with
 534 increasing charge mass, with different magnitudes due to the variation of SOD and charge
 535 backing. The influence of charge mass appears non-linear – there was an overall increase in
 536 central specific impulse with increasing charge mass, but with a dip in impulse occurring for
 537 the 20g charge mass. This decrease at 20g was observed for both the air and metal-backed
 538 detonations, and it attributed to charge shape effects at that specific aspect ratio that influence
 539 the blast wave propagation towards the plate.

540 When the specific impulse contribution from the outer 50mm portion of the circular plates was
 541 considered, a difference between the metal backed and air backed plates was evident in



542
 543 Figure 26. More impulse is imparted to the plates in the outer 50mm portion of the plates when
 544 the charge has a metal backing. The air-backed tests show the same dip in specific impulse at
 545 the periphery for the 20g detonation. This is not present in the specific peripheral impulse of
 546 the metal backed 20g detonations – the opposite trend is observed, with a significant rise in
 547 impulse at 20g. The periphery specific impulse was much larger at 40 mm SOD in the metal-
 548 backed plate, showing that SOD is a more influential factor when the charge has a solid
 549 backing, for the particular test range considered herein. The simulated specific impulse
 550 distributions and their sensitivity to SOD and charge backing explain the deformed plate
 551 profiles differences evident in the experiments.

552
 553 **6. Conclusions**

554 Experiments and simulations were performed to ascertain the influence of charge backing on
 555 the response of plates subjected to blast waves arising from the detonation of plastic explosives.
 556 The experiments showed that the impulse imparted to the test plates increased fivefold when

557 the charge was metal-backed. The permanent deflections from the metal-backed detonations
558 were larger than for air, but not to the same degree as the impulse increase.

559 The simulations revealed two reasons for the increased impulse transfer – pressure recirculation
560 along the clamp not present in the air-backed detonations, and a localised increase in the initial
561 plate velocity in the region of the charge. The localised increase in velocity was due to reflected
562 pressure from the metal back plate towards the test specimen just after detonation. This
563 influenced the deformation of the plate but did not account for the fivefold increase in impulse.
564 The pressure recirculation at the clamp occurred over a larger area and longer duration, causing
565 the impulse to increase without a corresponding rise in plate deflection. The metal-backed
566 detonations were more sensitive to SOD than the air backed detonations, with significantly
567 higher specific impulses at the plate periphery at the 40 mm SOD.

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577

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