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# Exploring the formation of intrinsic $p$ -type and $n$ -type defects of CuO

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## Abstract

CuO (cupric oxide) is a well known  $p$ -type semiconductor, suitable for solar cell photovoltaic applications. However, due to the easy formation of defects and Cu-rich layers at the copper(II) oxide hetero-interface, commercial application is yet to be successfully implemented. Density functional theory calculations have been employed to study the formation of intrinsic defects and their effect on the electronic properties of CuO. Native impurities were observed, depending on the synthesis conditions, to render the conductivity to  $p$ -type or  $n$ -type at a low energetic cost, yet with states embedded deep in the electronic band gap. Respective defect pairs, effectively determining the majority charge carriers, were observed to cluster in near proximity of each other, lowering the formation energy substantially. Hydrogen passivation was illustrated to have a positive effect on deep defect states in  $p$ -type CuO, without affecting the  $n$ -type counterpart. Outlined results were found to support the experimentally observed low photo-response of CuO and further illustrate some of the difficulties related with achieving high-performance samples.

## 1 Introduction

Copper(II) oxide (CuO) is a strongly correlated transition metal oxide which shows active coupling between spin, charge, orbital, and vibrational degrees of freedom. It has been studied intensively since the discovery of cuprate high-temperature superconductors, due to the close resemblance of its structural, electronic, and magnetic properties [1–4]. In CuO, low-energy physics induces antiferromagnetism with two distinct Néel temperatures and multiferroicity, reflecting the presence of competing equilibrium phases lying close to each other in energy [5–7].

CuO is a  $p$ -type semiconductor, with promising potential as a non-toxic, stable, and abundant material for photovoltaic (PV) and photocatalytic applications. Owing to its favourable electronic band gap value of 1.4 eV [8–10], it was postulated as an ideal candidate for solar harvesting technologies. However, reports on CuO solar cells are relatively rare and the obtained power conversion efficiencies (PCE), of incident sunlight into usable electric currents,

37 yield values which are an order of magnitude lower than the estimated potential value based  
38 on the Shockley-Queisser limit (around 30 %) [11]. As demonstrated earlier [12–14], one single  
39 ideal value does not guarantee good applicability for solar harvesting (especially for oxides of  
40 copper), as this neglects a multitude of other factors (recombination, strong absorption onset,  
41 charge carrier lifetimes, etc.).

42 In practice, many photovoltaic energy converters use semiconducting materials in the form of  
43 a  $p$ - $n$  or  $p$ - $i$ - $n$  junction. Structures of heterojunction solar cells with  $p$ -type CuO typically involve  
44  $n$ -type Si, although their efficiencies measure values below 0.5 % [15]. The low performance  
45 was attributed to the formation of Cu-rich copper oxide, as well as an amorphous interfacial  
46 oxide layer occurring between CuO and Si. Slight improvement was observed in Al/Ti/ $n$ -Si/ $p$ -  
47 CuO/Ti/Al heterostructure solar cells, approaching efficiencies of 1 % [16]. Doping CuO with  
48 N and interfacing with  $n$ -Si was observed to improve the efficiency to 1.21 %, as a result of  
49 improved crystallinity and thinning of the interfacial Cu-rich layer [17].

50 It was not until recent that  $n$ -type CuO has been observed. This conductivity type, driven  
51 by an excess number of electrons, was detected in nanoscale non-stoichiometric CuO<sub>x</sub> deposited  
52 by reactive magnetron sputtering [18]. By depositing  $n$ -CuO<sub>x</sub> onto hydrogenated amorphous Si,  
53 efficiencies of 3.04 % and 4.78 % were observed. Efficiency values were enhanced because in this  
54 case the interfacial Cu-rich layer acts as an electron supply reservoir instead of a recombination  
55 source for holes in  $p$ -CuO.

56 Du *et al* [19] have reported single phase intrinsic  $n$ -type CuO films prepared by magnetron  
57 sputtering combined with a high-voltage and low-current technique. Increasing the substrate  
58 temperature was found to convert CuO from a  $p$ -type semiconductor at 75° C (348 K) to an  
59  $n$ -type semiconductor at 500° C (773 K). The  $n$ -type conductivity was assigned to oxygen va-  
60 cancies and interstitial copper atoms. Enhanced point-defect scattering rates with increasing  
61 temperature were identified as the main cause of the decrease in overall carrier mobility rates  
62 with increasing temperature. Singh *et al* [20] have reported the successful deposition of  $n$ -type  
63 CuO via spin-coating.  $n$ -type CuO was created at moderate oxygen partial pressures (metal  
64 excess phase), leaving the material oxygen-deficient in the form of oxygen vacancies. The an-  
65 nealing time was reported to be a crucial parameter, with CuO changing into Cu<sub>2</sub>O over a  
66 prolonged time. Further studies of  $n$ -type CuO included extrinsic impurity-driven conductivity  
67 change. Baturay and co-workers [21] observed  $p$ -type conductivity conversion into  $n$ -type in  
68 CuO thin films when doped with Co. Capacity-voltage measurements verified a change in po-  
69 larity at 3 % doping ratio, with no change in the band gap. Moreover, Wang *et al* [22] observed  
70 increased charge separation and transfer in a CuO semiconducting photocathode as a results of  
71 a simple O<sub>2</sub> treatment which rendered the material’s conductivity  $p$ -type.

72 Theoretically, despite a substantial number of publications studying the ground state prop-  
73 erties of CuO, the intrinsic defects still remain largely unexplored. Nolan *et al* [23] and Wu *et al*  
74 [24] studied the native defects within CuO using LSDA+ $U$  calculations. However, defects were  
75 studied in the conventional monoclinic cell and simple antiferromagnetic configuration, not nec-  
76 essionarily corresponding to the experimentally observed ground state. More recent, Wang *et al* [22]  
77 explored the influence of copper vacancies in CuO based photocathodes using GGA(PBE)+ $U$   
78 calculations. Nonetheless, none of the reported studies concerning the formation of defects in

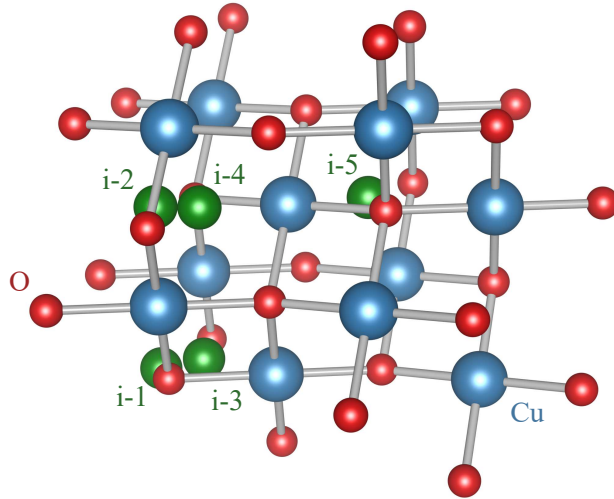


Figure 1: Crystal structure of the magnetic unit cell of CuO together with the five identified suitable positions for interstitial atoms.

79 CuO did not take into account the formation of competing phases, namely  $\text{Cu}_2\text{O}$  and  $\text{Cu}_4\text{O}_3$ ,  
 80 thereby most likely representing growth conditions for unphysical CuO compositions.

81 In the current work, native point defects, both simple and complex, were initialized within  
 82 the magnetic unit cell of CuO and their formation energies, as well as influence on the overall  
 83 electronic band structure explored. In order to do so, a comparative density functional theory  
 84 study was undertaken using Hubbard-corrected and hybrid exchange correlation functional  
 85 approximations. An attempt to answer some of the following questions is made: (i) which  
 86 defects occur intrinsically in CuO and which computational method describes them accurately?  
 87 (ii) does the model address the origin of experimentally observed  $n$ -type conductivity and, if  
 88 so, under which conditions?

## 89 2 Computational details

90 The results computed and presented in this work were were obtained from spin-polarized DFT-  
 91 based calculations performed with the Vienna Ab-initio Simulation Package (VASP) [25]. The  
 92 interactions between core and valence electrons were represented using the projector augmented  
 93 wave (PAW) method [26]. The general gradient approximation (GGA) [27] exchange-correlation  
 94 (XC) functional with the Perdew-Burke-Ernzerhof (PBE) parametrization was employed for  
 95 DFT+ $U$  within the formalism of Dudarev *et al* [28]. For the hybrid-DFT calculations, the  
 96 HSE XC functional was used [29–31], with a screening parameter of  $0.2 \text{ \AA}^{-1}$ . Long distance  
 97 dispersion corrections were included using the D3 approach of Grimme *et al* [32]. The plane  
 98 wave expansion cutoff was set to 450 eV and the force convergence criterion to cell relaxation  
 99 was  $0.01 \text{ eV/\AA}$ .  $\Gamma$ -centred Monkhorst-Pack [33] meshes ( $3 \times 5 \times 3$  for magnetic unit cell and  
 100 a single  $\Gamma$ -point for the  $2 \times 3 \times 2$  supercell) were employed to sample the Brillouin zone in  
 101 reciprocal space. Band structure calculations were performed on the optimized structure along  
 102 high-symmetry directions obtained from the Bilbao Crystallographic Server [34–36] and plotted

103 using the `Wannier90` code [37, 38]. The phase stability diagram of CuO for a range of ac-  
 104 cessible chemical potentials was computed using CPLAP (Chemical Potential Limits Analysis  
 105 Program)[39], taking into account its limiting competing phases. The extent of defect charge  
 106 distribution was studied using the Bader scheme as implemented in the Henkelman code [40–42].  
 107 Suitable defect positions were identified using the `PyCDT` package [43] Graphical drawings were  
 108 produced using `VESTA` [44].

109 The values for the effective Hubbard parameter ( $U_{\text{eff}}$ ) and the amount of the non-local exact  
 110 Hartree-Fock exchange used within the HSE XC functional were tuned according to the value  
 111 of the ground state electronic band gap and (spin only) magnetic moment of the respective Cu  
 112 atoms. Excitonic and spin-orbit coupling effects were not taken into account.

113 The formation energy of a defect  $X$  in charge state  $q$  is defined as [45, 46]:

$$E^f[X^q] = E_{\text{tot}}[X^q] - E_{\text{tot}}[\text{bulk}] - \sum_i n_i \mu_i + q(E_F + \varepsilon_{\text{VBM}}^{\text{H}}) + E_{\text{corr}}. \quad (1)$$

114  $E_{\text{tot}}[X]$  is the total energy derived from a supercell calculation containing the defect  $X$ , and  
 115  $E_{\text{tot}}[\text{bulk}]$  is the total energy for the perfect crystal using an equivalent supercell. The integer  $n_i$   
 116 indicates the number of atoms of type  $i$  (host atoms or impurity atoms) that have been added to  
 117 ( $n_i > 0$ ) or removed from ( $n_i < 0$ ) the supercell to form the defect, and  $\mu_i$  are the corresponding  
 118 chemical potentials of the considered species (related through  $\Delta\mu_i = \mu_i - \mu_i^{\circ}$ , where  $\mu_i^{\circ}$  is the  
 119 chemical potential of the element  $i$  in its standard phase). The chemical potentials represent  
 120 the energy of the reservoirs with which atoms are being exchanged.  $E_F$  represents the electron  
 121 chemical potential, which ranges from the valence to the conduction band edges,  $\varepsilon_{\text{VBM}}^{\text{H}}$  is the  
 122 eigenvalue of the valence band maximum of the pristine bulk material. Finally,  $E_{\text{corr}}$  is a  
 123 correction term that accounts for finite-size effect in the calculations of charged defects as well  
 124 as aligning of the band edges between the bulk and the defective supercells, performed using the  
 125 `SXDEFECTALIGN` code by Freysoldt *et al* [47]. The thermodynamic transition levels (ionization  
 126 levels) of a given defect,  $\varepsilon(q_1/q_2)$ , correspond to the Fermi-level position at which a given defect  
 127 changes from one charge state ( $q_1$ ) to another ( $q_2$ ):

$$\varepsilon(q_1/q_2) = \frac{E^f[X^{q_1}] - E^f[X^{q_2}]}{q_2 - q_1}. \quad (2)$$

128 The allowed values of  $\Delta\mu_i$  are determined from a set of thermodynamic limits. The upper  
 129 limit is given by  $\Delta\mu_i \leq 0$  where element  $i$  precipitates to its standard state, e.g.,  $\text{O}_2(\text{g})$  (referred  
 130 to half of the total energy of an oxygen molecule) and  $\text{Cu}(\text{s})$ . Also, to avoid the formation of  
 131 secondary solids, the chemical potentials must also be bound by:

$$2\Delta\mu_{\text{Cu}} + \Delta\mu_{\text{O}} \leq \Delta H_{\text{f}}(\text{Cu}_2\text{O}), \quad (3)$$

$$4\Delta\mu_{\text{Cu}} + 3\Delta\mu_{\text{O}} \leq \Delta H_{\text{f}}(\text{Cu}_4\text{O}_3), \quad (4)$$

132 with  $\Delta H_{\text{f}}$  being the standard enthalpy of formation at zero K. The total energies of the phases  
 133 competing with CuO, i.e.,  $\text{Cu}_2\text{O}$  and  $\text{Cu}_4\text{O}_3$ , were calculated using their respective unit cells.  
 134  $\text{Cu}_2\text{O}$  was modelled in a simple cubic non-magnetic cell, while for tetragonal  $\text{Cu}_4\text{O}_3$ , a primitive

135 cell containing 14 atoms was used together with the antiferromagnetic spin ordering leading to  
 136 the observed lowest energy configuration [48–50]. The calculated formation energies of CuO,  
 137 Cu<sub>2</sub>O and Cu<sub>4</sub>O<sub>3</sub> read -1.58 eV (1.35 eV), -1.70 eV (-1.46 eV), and -4.85 eV (-4.15 eV) calculated  
 138 using DFT+*U* (HSE) and are considerably close to experimental values of 1.59 eV [51], -1.75 eV  
 139 [51], and -4.88 eV [52], respectively.

140 In the case of CuO passivation, the solubility of the H species were limited by the formation  
 141 of an additional compound, copper(II) hydroxide:

$$\Delta\mu_{\text{Cu}} + 2\Delta\mu_{\text{O}} + 2\Delta\mu_{\text{H}} = \Delta H_{\text{f}}(\text{Cu}(\text{OH})_2). \quad (5)$$

## 142 3 Results and discussion

### 143 3.1 Modelling magnetic CuO

144 CuO crystallizes in a lower symmetry monoclinic crystal structure (space group *C2/c*, Num-  
 145 ber 15), compared to Cu<sub>2</sub>O. The conventional unit cell consists of eight atoms, four Cu atoms  
 146 and four O atoms. Each copper atom is coordinated by four oxygen atoms in an approximately  
 147 square planar configuration, while each oxygen atom is located at the centre of a distorted tetra-  
 148 hedron [53], with the following lattice parameters:  $a = 4.6837 \text{ \AA}$ ,  $b = 3.4226 \text{ \AA}$ ,  $c = 5.1288 \text{ \AA}$  [54].  
 149 Below 230 K, the magnetic ground state of CuO is a peculiar antiferromagnetic arrangement.  
 150 This ordering is described within an eight-formula magnetic unit cell whose lattice vectors are  
 151 obtained by expanding the conventional unit cell lattice vectors via the relation  $\mathbf{a}' = \mathbf{a} + \mathbf{c}$ ,  
 152  $\mathbf{b}' = \mathbf{b}$ , and  $\mathbf{c}' = -\mathbf{a} + \mathbf{c}$  [6].

153 As previously demonstrated by Rödl *et al* [6], the local magnetic moments that occur both  
 154 on the Cu and O atoms, as well as the electronic band gap, can be tuned depending on the  
 155 screened exchange parameter ( $\alpha$ ) in hybrid (HSE), or as a function of the on-site interaction  
 156  $U$  in PBE+ $U$  calculations. Moreover, a majority of works available in the literature employ  
 157 experimental lattice parameters within their simulations, which ensures consistency between  
 158 calculated and experimental crystal structures. However, experimental geometries are (usually)  
 159 not identical to minimum-energy geometries obtained by structural relaxations within a given  
 160 functional. This issue is particularly pronounced when hybrid density functionals are employed  
 161 [55], where calculation time increases dramatically (in the range of a thousand-fold) and system  
 162 size is limited to a few dozen atoms.

163 In order to examine the underlying effects of strain remnants within the magnetic CuO  
 164 simulation cell, various pre-relaxed, atomically-relaxed, and fully-relaxed geometries were tested  
 165 and their validity assessed. Furthermore, two differently ordered spin arrangements of the Cu<sup>2+</sup>  
 166 ions in CuO were considered, one along the  $z$  axis (AF<sub>Z</sub>, the most stable magnetic state) and one  
 167 along the  $x$  axis (AF<sub>X</sub>). These were taken following the nomenclature outlined by Rocquefelte  
 168 *et al* [1] to allow for easier comparison and validation with earlier works.

169 First, the influence of the  $U_{\text{eff}}$  parameter within DFT+ $U$  and the exact exchange  $\alpha$  within  
 170 hybrid DFT on the electronic (Kohn-Sham) band gap were assessed. Results for the two distinct  
 171 magnetic arrangements are summarized in Figure 2. Note the different values of  $U_{\text{eff}}$  and  $\alpha$   
 172 when fitting to the electronic band gap. For a fit to the low temperature band gap value of

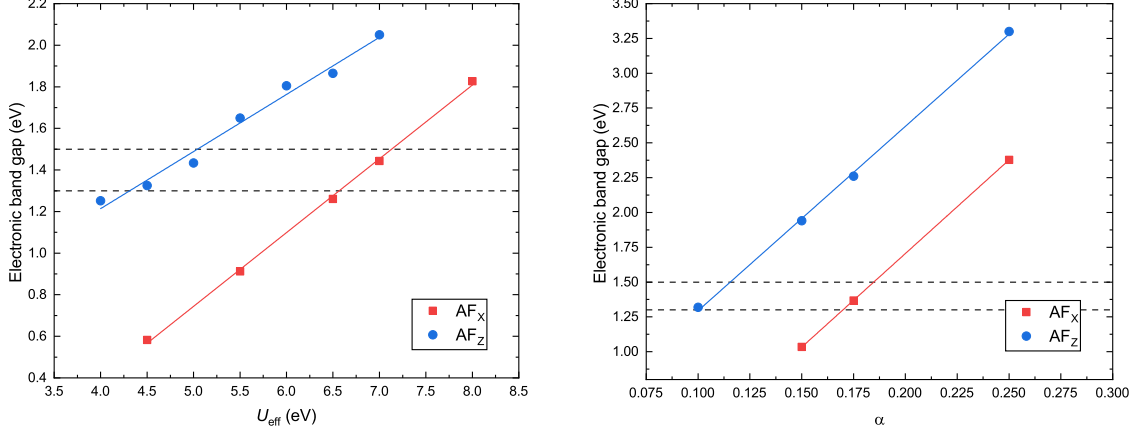


Figure 2: The electronic band gap dependence on the effective  $U$  parameter within DFT+ $U$  (left) and the exact exchange amount  $\alpha$  used for hybrid DFT calculations (right). The red filled squares refer to the AF<sub>x</sub> magnetic arrangement, while the blue filled dots represent the AF<sub>z</sub> magnetic configuration. The linear fit is merely an eye-guide for easier data readout. The dashed black lines indicate the range of experimentally available low-temperature values.

173 1.3 – 1.5 eV [56], a value of  $U_{\text{eff}} = 5$  eV and  $U_{\text{eff}} = 7$  eV can be read for the AF<sub>z</sub> and AF<sub>x</sub>  
 174 magnetic ordering, respectively. Similarly, for hybrid DFT calculations, values of  $\alpha \approx 0.125$   
 175 and  $\alpha \approx 0.175$  used within HSE are read for AF<sub>z</sub> and AF<sub>x</sub>. This explains the variety of  $U_{\text{eff}}$   
 176 and  $\alpha$  values in the existing literature that were used for bulk CuO calculations. Together  
 177 with the choice of an appropriate simulation cell and magnetic arrangement, defining a unique  
 178 simulation setup becomes a question of the physical properties under examination.

179 Furthermore, so far the simulation have included relaxation effects only up to the atomic  
 180 position level, i.e., lattice parameters and the cell volume were kept fixed. Starting from the  
 181 experimental lattice parameters of the CuO magnetic unit cell with two different magnetic  
 182 arrangements, calculations allowing for lattice cell shape relaxation were performed, in or-  
 183 der to circumvent the observed internal pressure left within the geometry of the system after  
 184 only atomic relaxation was performed. The pressure was in certain cases as high as  $\pm 2$  GPa  
 185 (20 kBar), depending on the system under study. Such values are large enough to drive lat-  
 186 tice instabilities and subsequent structural phase transitions [57]. Thus, care must be taken in  
 187 order to avoid and minimize internal lattice stress when dealing with CuO. Results of those  
 188 simulations are illustrated in Figure 3. Based on those results and discussion outlined above,  
 189 values of  $U_{\text{eff}} = 5.5$  eV for DFT+ $U$  and  $\alpha = 0.125$  for HSE were chosen for this study, as they  
 190 reproduce the electronic band gap and magnetic moments values accurately, minimizing the  
 191 internal pressure simultaneously. Surprisingly, allowing for the lattice parameters to change  
 192 during the relaxation run of AF<sub>x</sub>, the calculations proceed in such way that it converges to the  
 193 AF<sub>z</sub> geometry, indirectly confirming the most stable magnetic configuration.

### 194 3.2 Intrinsic defects of CuO

195 To explore the native defects in CuO, an antiferromagnetic  $2 \times 3 \times 2$  supercell (starting from the  
 196 magnetic unit cell) was created, which ensures minimal interaction between introduced defects,  
 197 located at least  $10 \text{ \AA}$  apart in each crystallographic direction. Furthermore, the differences  
 198 between DFT+ $U$  and HSE values of defect formation energies and impurity band positions

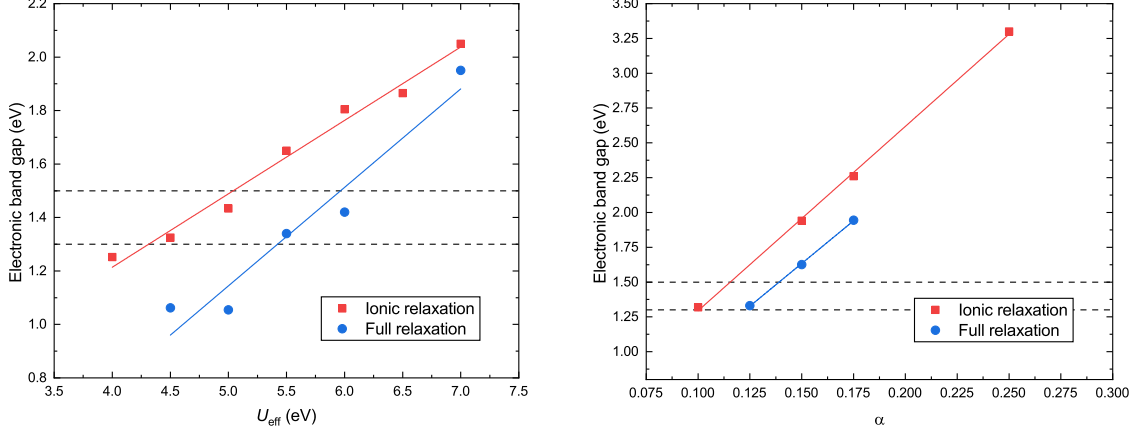


Figure 3: The electronic band gap dependence on the effective  $U$  parameter (left) and the exact exchange amount  $\alpha$  (right) for the  $\text{AF}_Z$  configuration. The red filled squares refer to the atomically relaxed geometry, while the blue filled dots represent the fully relaxed geometry (incorporating atomic, cell, and volume relaxation). The linear fit is merely an eye-guide for easier data readout. The dashed black lines indicate the range of experimentally available low-temperature values.

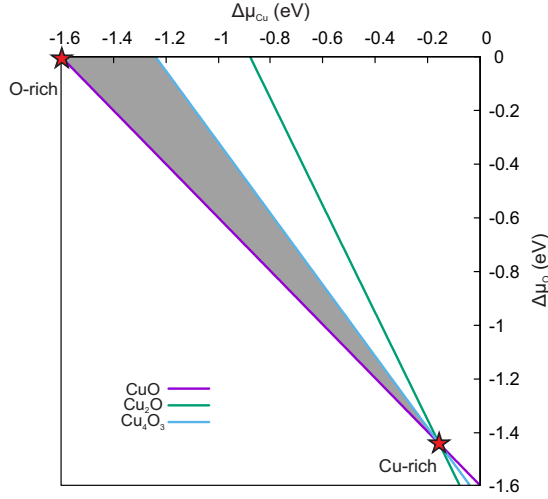


Figure 4: CuO stability limits in the range of allowed chemical potentials, emphasized within the grey-shaded area. The points highlighted with red stars indicate the chemical potential taken for the calculations to be carried out. Values were calculated from experimental formation enthalpies in order to assure transferability of results.

199 within the electronic structure are examined.

200 **Phase stability** Following the formalism outlined in equations (1)–(4), the boundaries for  
 201 chemical potentials were calculated and shown in Figure 4. To analyse the effect of employed  
 202 growth conditions on undoped CuO samples, two chemical potential limits were chosen: one  
 203 with O-rich/Cu-poor and the other with Cu-rich/O-poor conditions. The selected values read:

- 204 • O-rich/Cu-poor:  $\Delta\mu(\text{Cu}) = -1.594$ ,  $\Delta\mu(\text{O}) = 0.000$ .
- 205 • Cu-rich/O-poor:  $\Delta\mu(\text{Cu}) = -0.157$ ,  $\Delta\mu(\text{O}) = -1.437$ .

206 Simple native defects were introduced into the CuO magnetic supercell, including simple va-  
 207 cancies (labelled  $V_{\text{Cu}}$  and  $V_{\text{O}}$ ), anti-sites ( $\text{Cu}_{\text{O}}$  and  $\text{O}_{\text{Cu}}$ ), and interstitials in various positions  
 208 within the cell ( $\text{Cu}_i$  and  $\text{O}_i$ ).



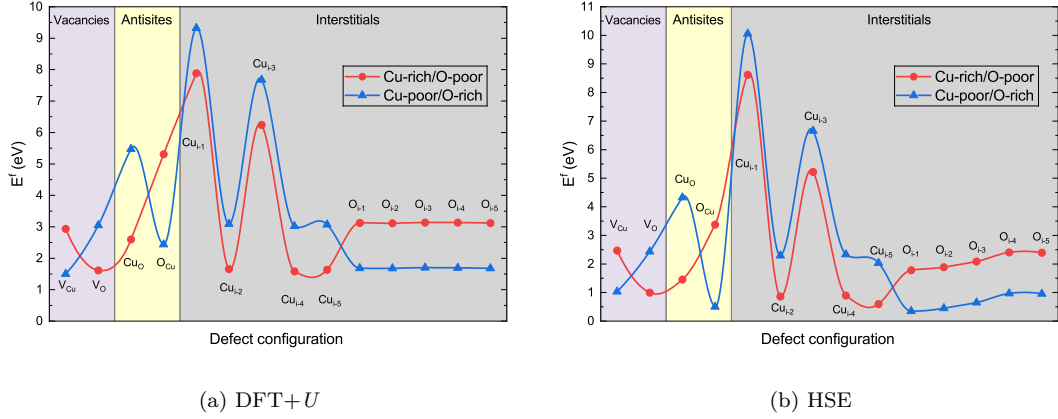


Figure 5: Calculated formation energies of simple native defects in CuO under different chemical potential limits, using two types of approximation for the XC functional. Symbols are the calculated values; the lines are aides to guide the eye.

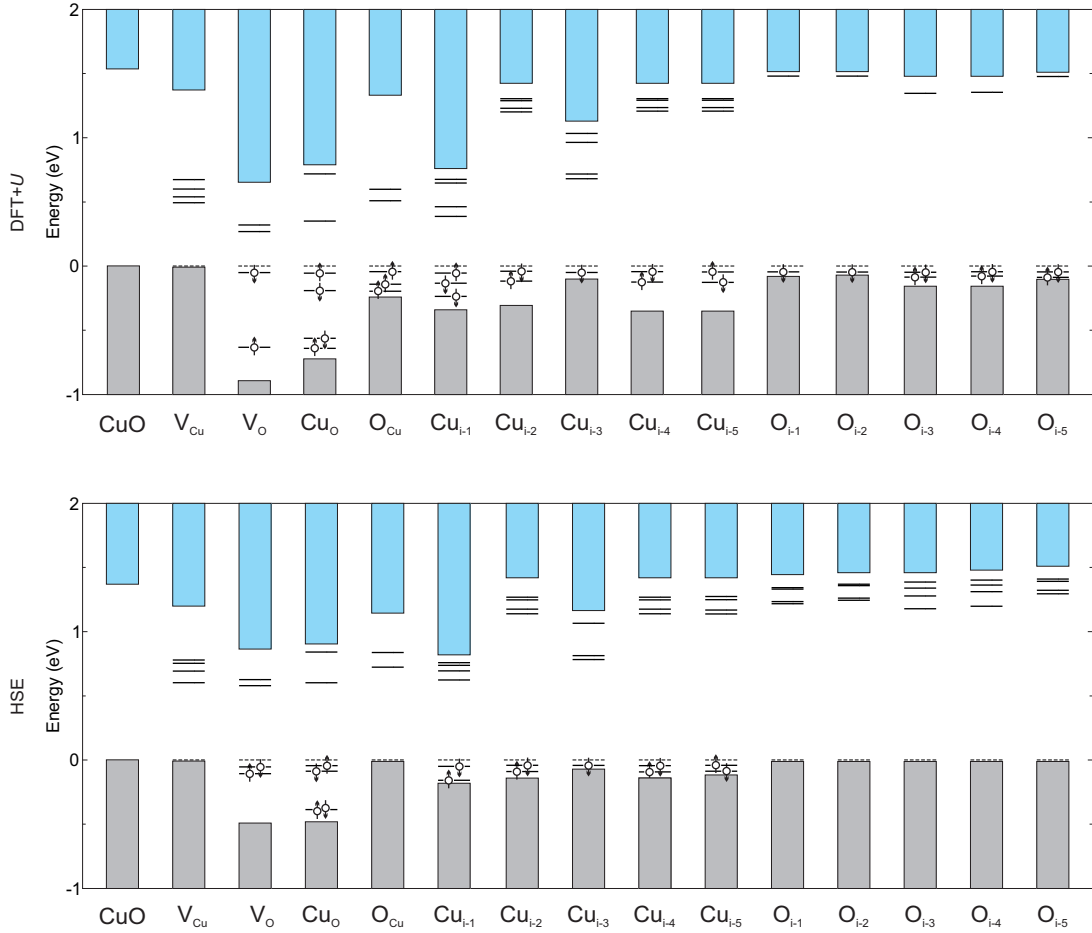


Figure 6: A cumulative schematic representation drawn from electronic densities of state (DOS) data calculated for clean and defective CuO. A comparison between DFT+U and HSE calculated values is illustrated in the top and bottom row. The grey and light-blue rectangular shapes correspond to the valence and conduction band, respectively, while short lines indicate positions of defect levels obtained from DFT+U and HSE calculations. The dashed line indicates the highest occupied band and up/down arrows represent different spin channels.

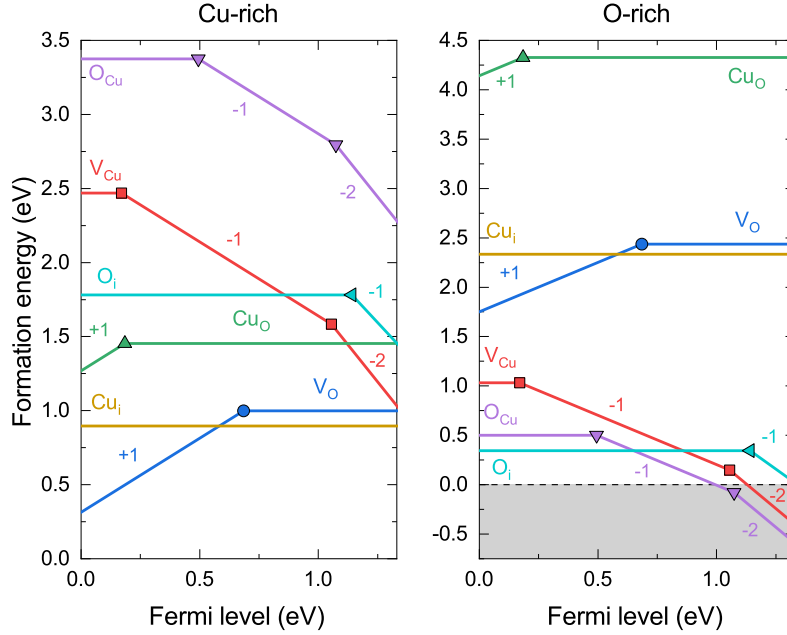


Figure 7: Calculated defect formation energies as a function of the Fermi-level position of native defects occurring in CuO under different chemical potential limits. The slope of the lines denotes the charge state and the solid dots represent the transition levels  $\epsilon$ .

209 **Intrinsic defects** Figure 5 displays the neutral formation energies for all the possible intrinsic  
 210 defects occurring in CuO. It is observed that the formation energy of defects varies depending  
 211 on growth environments, but features overall similar trends between DFT+ $U$  and HSE. Under  
 212 Cu-rich growth environments, the most favourable neutral defects are  $V_O$  and  $Cu_i$ , with the  
 213 hindmost depending on the position within the cell. On the other hand, under O-rich conditions,  
 214  $p$ -type defects  $V_{Cu}$ ,  $O_{Cu}$ , and  $O_i$  (which unlike their Cu counterparts do not depend on the  
 215 position within the cell) are favoured over all  $n$ -type defects. The differences in formation  
 216 energies between distinct growth conditions are large enough to allow for high performance  
 217 undoped samples of CuO with particular conductivity types to be created.

218 Figure 6 presents a cumulative schematic diagram drawn from electronic densities of state for  
 219 the considered defects within CuO, obtained using DFT+ $U$  and HSE calculations. Similar to  
 220 the formation energies, the overall trends are consistent between DFT+ $U$  and HSE calculations,  
 221 with the absolute values varying slightly. It is evident that the majority of defects introduces  
 222 states within the electronic band gap of CuO that are far from the band edges. Such states  
 223 are detrimental to the operation of devices relying on the promotion of electrons via photon-  
 224 absorption as they act as recombination centres rather than contributing to an increase in  
 225 carriers. In order to explore the full potential of intrinsic defects on the carrier generation and  
 226 compensation processes in CuO, the formation energies of intrinsic defects in various charged  
 227 states was studied. A plot of the defect formation energy as a function of the Fermi level position  
 228 for both considered growth environments is plotted in Figure 7. Since the difference between  
 229 the two utilized methods, DFT+ $U$  and HSE, was shown to be small, further discussions concern  
 230 only results based on HSE calculations.

231 In a Cu-rich environment, the most prominent intrinsic donors are  $V_O$  and  $Cu_i$  with forma-

232 tion energies around 1 eV. However,  $V_O$  behaves as a deep donor with a  $\varepsilon(+1/0)$  transition level  
 233 at 0.69 eV above the valence band maximum (VBM). Such behaviour of  $V_O$  in CuO corresponds  
 234 well to the extremely low carrier mobility of  $(0.482 - 1.727) \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  measured in  $n$ -type  
 235 CuO [19].  $\text{Cu}_i$ , despite requiring less energy than  $V_O$ , forms exclusively as a neutral defect,  
 236 with its ionization level located in the VBM, and is thus unlikely to provide effective charge  
 237 compensation in CuO. The lowest energy acceptor defect under Cu-rich conditions is  $V_{\text{Cu}}$ , yet  
 238 it lies too high in energy to compensate for the most prominent donor impurities.

239 Under O-rich conditions, acceptor defects dominate the native impurity landscape. The  
 240 lowest energy acceptor is the  $\text{O}_i$ , which together with the  $\text{O}_{\text{Cu}}$  and  $V_{\text{Cu}}$  are all found to form  
 241 up to 1 eV. Over the whole range of the electronic band gap those are not compensated by  
 242 any other defects, rendering the material entirely  $p$ -type in nature.  $V_{\text{Cu}}$  acts as a relatively  
 243 shallow acceptor with the  $\varepsilon(0/-1)$  transition at 0.17 eV above the VBM and a subsequent  
 244 deeper  $\varepsilon(-1/-2)$  transition at 0.28 eV below the conduction band minimum (CBM).  $\text{O}_{\text{Cu}}$   
 245 demonstrates two deep acceptor levels,  $\varepsilon(0/-1)$  at 0.49 eV and  $\varepsilon(-1/-2)$  at 1.07 eV above the  
 246 VBM. The calculated  $\varepsilon(0/-1)$  transition level of the  $\text{O}_i$  is found at 1.14 eV above the VBM, thus  
 247 limiting the otherwise high conductivity that could be expected due to very low cost involved  
 248 in the formation of these defects.

249 These results confirm the experimentally observed  $n$ -type conductivity of CuO, assigned to  
 250 O vacancies and interstitial Cu atoms [19, 20], as well as  $p$ -type conductivity assigned to Cu va-  
 251 cancies [21]. Unlike the case of  $\text{Cu}_2\text{O}$ , depending on the growth conditions, CuO can intrinsically  
 252 be created as an  $n$ -type (Cu-rich/O-poor environment) or  $p$ -type (O-rich/Cu-poor environment)  
 253 semiconductor. However, explored defects present in CuO show states deep in the electronic  
 254 band gap, thus acting as recombination and trap states rather than carrier concentration and  
 255 mobility promoters.

256 **The formation of defect pairs** Since a clear trend in occurrence of distinct defects is  
 257 observed,  $V_{\text{Cu}}$  or  $\text{O}_i$  under O-rich and  $V_O$  or  $\text{Cu}_i$  under Cu-rich conditions, the question whether  
 258 these defects would appear simultaneously. In order to verify this suggestion, defect pairs were  
 259 introduced into the simulation cell. Pairs were chosen according to the lowest formation energy  
 260 of their individual appearance under specific growth conditions. In addition, the possibility of  
 261 clustering effects was analysed by introducing defects in close proximity to each other and as  
 262 far away as possible across the simulation cell.

263 The calculated formation energies for neutral pairs of defects in CuO is shown in Figure  
 264 8. From these results, a clear trend of defect clustering over dispersion is noted, regardless of  
 265 the nature of the defect or employed computational scheme. Furthermore, particular defect  
 266 formation in close proximity demonstrates a lowering of the formation energy compared to  
 267 the sum of individual energies. For example, under Cu-rich conditions, the creation of a Cu  
 268 interstitial next to an already present O vacancy requires an energy of 2.38 eV (1.49 eV), which  
 269 is lower compared to the sum of individual defect formation energies  $E^f(\text{Cu}_i) + E^f(V_O) =$   
 270  $1.58 (0.99) \text{ eV} + 1.61 (0.89) \text{ eV} = 3.19 (1.88) \text{ eV}$ , calculated using DFT+ $U$  (HSE).

271 First, the case where defects are maximally dispersed through the cell is analysed. The  
 272 two defects were placed at a minimum distance of 8.32 Å in the case of  $\text{O}_i(V_{\text{Cu}})$  and 8.44 Å for

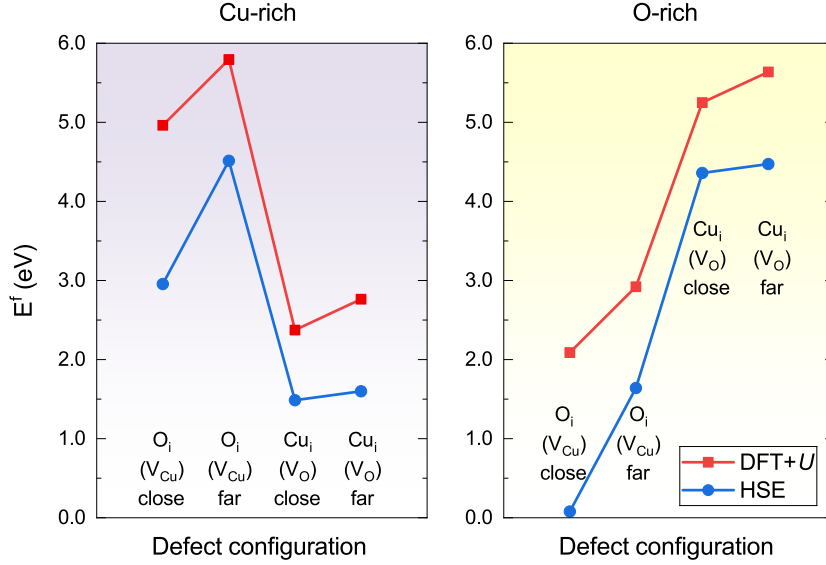


Figure 8: Formation energies for pairs of defects within CuO, under different growth conditions. The used notation specifies a newly induced defect into a cell where the one enclosed in brackets is already present. The pairs were chosen according to the lowest formation energies of individual defects illustrated earlier. A trend to form small clusters can be observed both under Cu-rich and O-rich conditions. Symbols are the calculated values; the lines are aides to guide the eye.

273  $\text{Cu}_i(\text{V}_\text{O})$ , which ensures that the overlap of respective wave functions is minimized as far as  
 274 possible within the supercell. The notation implies a defect introduced in the host cell where  
 275 the defect written in brackets was already present. As expected, defects introduced far away  
 276 across the cell do not interact significantly with each other. They localize around the defect  
 277 site, creating individual local distortions discussed in earlier paragraphs for single impurities,  
 278 as observed in the electronic densities of state in Figure 9.

279 Defects occurring in close proximity to each other exhibit different properties compared to  
 280 their dispersed analogues, due to strong overlap of interacting impurity wave functions. For  
 281  $\text{O}_i(\text{V}_{\text{Cu}})$ , the newly introduced O interstitial atom distorts the structure around the defect site  
 282 negligibly and forms a weak bond with the nearest lattice O atom ( $1.37 \text{ \AA}$ , which is comparable  
 283 to the separation length of the  $\text{O}_2$  molecule of  $1.208 \text{ \AA}$  [58]).  $\text{O}_i(\text{V}_{\text{Cu}})$  acts as a deep acceptor,  
 284 with the  $\varepsilon(0/-1)$  and  $\varepsilon(-1/-2)$  transition levels found at  $0.56 \text{ eV}$  and  $0.95 \text{ eV}$  above the VBM,  
 285 respectively.

286 In contrast, the addition of  $\text{Cu}_i$  around an existing  $\text{V}_\text{O}$  defect does not distort the structure  
 287 significantly. The  $\text{Cu}_i$  relaxes into the void left behind by the vacancy, easing the bond stress  
 288 induced by the interstitial on the nearest O and Cu atoms. This allows the structure to relax into  
 289 a more ordered one, hence lowering the formation energy of the defect complex by almost  $0.80 \text{ eV}$   
 290 ( $0.40 \text{ eV}$ ), as indicated before, obtained for DFT+U (HSE). The migration of the interstitial  
 291 Cu proceeds until a position where the Coulomb repulsion of the surrounding electrons (left  
 292 behind in the created O vacancy) is minimal. The  $\text{Cu}_i(\text{V}_\text{O})$  complex behaves as a deep donor,  
 293 analogous to the simple  $\text{V}_\text{O}$ , with the difference that the  $\varepsilon(+1/0)$  ionization level is found nearer  
 294 to the VBM, at  $0.34 \text{ eV}$ , compared to the individual O vacancy.

295 Following this discussion, a general tendency of defect clustering in CuO is observed. More

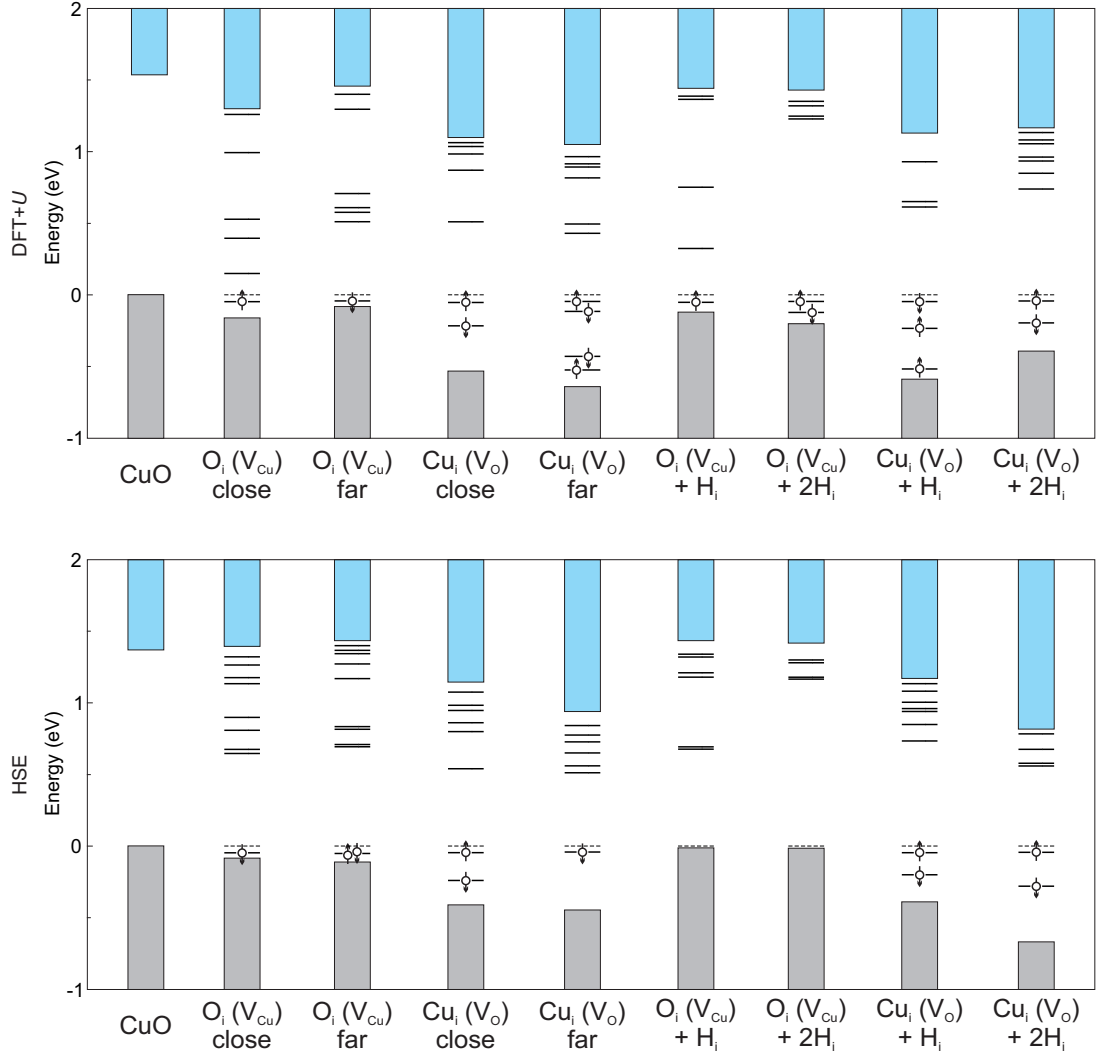


Figure 9: A cumulative schematic representation drawn from electronic densities of state (DOS) data calculated for clean, pairwise defective, and passivated CuO. A comparison between DFT+ $U$  and HSE calculated values is illustrated in the top and bottom row. The grey and light-blue rectangular shapes correspond to the valence and conduction band, respectively, while short lines indicate positions of defect levels obtained from DFT+ $U$  and HSE calculations. The dashed line indicates the highest occupied band and up/down arrows represent different spin channels.

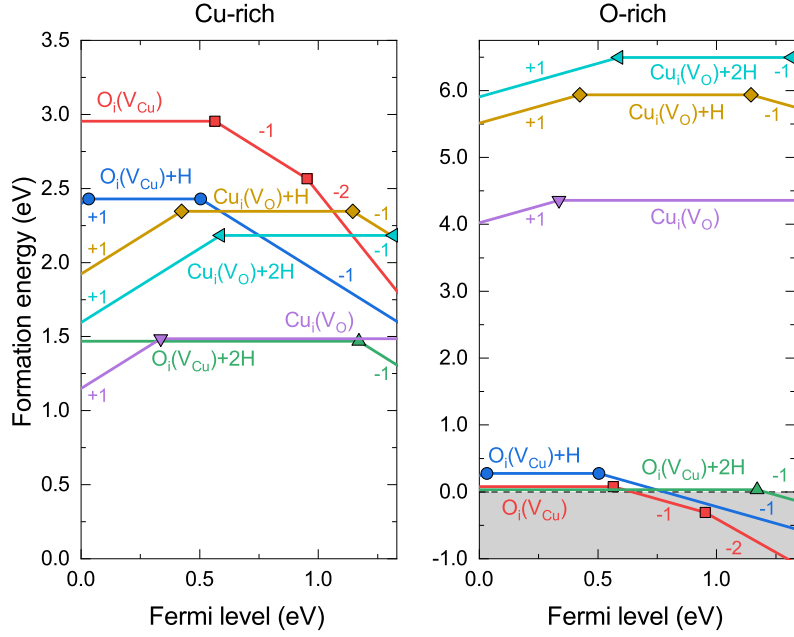


Figure 10: Calculated formation energies as a function of the Fermi-level position of clustered and passivated defects occurring in CuO under different chemical potential limits outlined earlier. The slope of the lines denotes the charge state and the solid dots represent the transition levels  $\varepsilon$ .

296 importantly, defects tend to create states located in the middle of the band gap, which is detri-  
 297 mental for any application requiring effective charge capture and separation processes. Deep  
 298 states favour recombination of created carriers, impairing the overall conductivity, regardless of  
 299 it being  $n$ -type or  $p$ -type.

300 **Intentional passivation** A further question emerging is whether the mid-gap states created  
 301 by intrinsic impurities can be removed whilst maintaining the desired conductivity type? One  
 302 mechanism through which one could influence the character of an impurity is called *passivation*.  
 303 It explains the often observed compensating nature of defects when donor dopants attract  
 304 impurities of the opposite kind – acceptors, and vice versa. The resulting complex is often  
 305 charge neutral and electrically inactive.

306 In order to test the system for eventual passivation effects, hydrogen was incorporated  
 307 interstitially into the CuO matrix with the most stable defects present, as identified earlier.  
 308 Hydrogen was chosen as the simplest possible impurity in order to track the changes that a single  
 309 electron/hole induce onto the defect complex. Furthermore, the ambiguity when modelling  
 310 hydrogen is drastically reduced compared to transition metal atoms or complex molecules,  
 311 which often rely on additional  $U_{\text{eff}}$  parametrization or exact exchange tuning.

312 In the initial setup, one H atom is placed into the vacancy site of the  $O_i(V_{\text{Cu}})$  defect complex  
 313 (favouring  $p$ -type conductivity). After structural relaxation, the (effectively interstitial) H atom  
 314 migrates towards the nearest neighbouring O closest to the vacancy site. The H atom binds  
 315 onto one of the three dangling O bonds left after the  $O_i(V_{\text{Cu}})$  defect complex was formed. This  
 316 removes the strain present in the cell along the  $c$  direction and the nearest atoms surrounding  
 317 the H site relax into their original crystallographic positions in a cell without defects. However,

318 two O dangling bonds along the  $a$ -axis remain present, with reduced repulsion effects due to  
 319 their missing analogues in the perpendicular direction. More importantly, two acceptor states  
 320 were removed from the electronic structure when compared to the case without interstitial H  
 321 (Figure 9).

322 Adding a further H atom into the vacancy site of the  $(\text{O}_i(\text{V}_{\text{Cu}})+\text{H})$  complex generates  
 323 defect behaviour similar to the case of a single interstitial H. The newly added H binds onto its  
 324 nearest neighbouring O atom left unpaired after the Cu vacancy was created. The surrounding  
 325 structure remains largely unaffected, with the two interstitial H atoms relaxing away from each  
 326 other due to active repulsion between identical charges. More importantly, this defect complex  
 327 configuration leads to removal of the impurity states previously present in the middle of the band  
 328 gap, leaving an electronic structure similar to that of simple interstitial O atoms, as observed  
 329 from Figure 9.

330 Figure 10 depicts a plot of the defect formation energy as a function of the Fermi-level  
 331 position for the H passivated complexes under Cu-rich and O-rich conditions. The singly H  
 332 passivated  $\text{O}_i(\text{V}_{\text{Cu}})$  defect behaves as an amphoteric defect with a shallow  $\varepsilon(+1/0)$  transition  
 333 level 0.03 eV above the VBM and a very deep  $\varepsilon(0/-1)$  transition at 0.50 eV above the VBM, ef-  
 334 fectively killing both  $p$ -type and  $n$ -type conductivity in the system. However, the  $(\text{O}_i(\text{V}_{\text{Cu}})+2\text{H})$   
 335 complex is found to have only one level in the band gap, the relatively shallow  $\varepsilon(0/-1)$  transi-  
 336 tion at 0.16 eV below the CBM. This unanticipated finding suggests that a varying amount of  
 337 incorporated H can lead to substantially different defect behaviour in CuO.

338 These results for CuO indicate consistent behaviour with those of earlier studies on  $\text{Cu}_2\text{O}$ ,  
 339 where a  $(\text{H}-\text{V}_{\text{Cu}})$  complex was found to be the most stable defect with a formation energy  
 340 of only 0.17 eV (results obtained using a HSE functional with 27.5% of exact exchange) [59].  
 341 Furthermore,  $\text{H}_i$  in  $\text{Cu}_2\text{O}$  was found to be an amphoteric impurity under both sets of conditions,  
 342 suppressing both  $p$ -type and  $n$ -type conductivity.

343 In the second considered case, interstitial H is placed into the O vacancy site of the  $\text{Cu}_i(\text{V}_\text{O})$   
 344 complex. This causes the nearest neighbouring Cu atoms to relax away from the interstitial  
 345 site. The resulting electronic structure remains largely unaltered, as noted from Figure 9.

346 Inserting an additional H into the vacancy site results in a stronger relaxation of surrounding  
 347 atoms, compared to the single H interstitial. The added H migrates into the layer beneath the  
 348 O vacancy (along the  $-a$  crystallographic axis) binding onto an O atom, causing the nearest  
 349 neighbouring Cu to relax towards the vacant O site. More importantly, the initial electronic  
 350 structure of the  $\text{Cu}_i(\text{V}_\text{O})$  complex remains unaffected. The two states remain present in the band  
 351 gap, as a consequence of the inability of H to counterbalance the larger structural distortion  
 352 originating from the interstitial Cu atom introduced in the first place. Both the  $(\text{Cu}_i(\text{V}_\text{O})+\text{H})$   
 353 and  $(\text{Cu}_i(\text{V}_\text{O})+2\text{H})$  defect complexes demonstrate amphoteric behaviour, with simultaneous  
 354 presence of donor and acceptor states in the band gap region. Also, a shifting trend of the  
 355  $\varepsilon(+1/0)$  and  $\varepsilon(0/-1)$  transitions towards higher Fermi-levels can be noted with increasing H  
 356 concentration.

357 Finally, the difference in passivation effects under different growth environments is dis-  
 358 cussed. Under O-rich conditions,  $p$ -type defects dominate the impurity landscape of H-doped  
 359 CuO. With an increasing H content,  $n$ -type defects are becoming prohibitively expensive to

360 create, with formation energies reaching more than 6 eV. Thus, interstitial H acts as a *p*-type  
361 promoter for CuO created in an O-rich environment. In contrast, under Cu-rich conditions,  
362 the formation energy of *n*-type defects increases with H doping, while at the same time the  
363 formation energy of *p*-type defects decreases. With increasing H content, the *n*-type defects are  
364 not only compensated for, but rather fully replaced by their *p*-type analogues, as observed from  
365 Figure 10.

## 366 4 Conclusion

367 A systematic comparative theoretical study of the DFT+*U* and hybrid-DFT formalism on the  
368 electronic and magnetic properties of CuO was undertaken. Various modelling parameters, such  
369 as the simulation cell, relaxation type, and magnetic configuration were optimized before the  
370 introduction of native point defects, both simple and complex, within the magnetic unit cell  
371 of CuO, followed by the evaluation of formation energies, as well as the effect on the overall  
372 electronic structure. Following the presented analysis, several significant conclusions can be  
373 drawn:

- 374 • Both DFT+*U* and HSE are able to describe the ground state of CuO accurately. However,  
375 care is required when tuning either the *U* parameter in DFT+*U* or  $\alpha$  in HSE accordingly  
376 to the type of simulation that is being undertaken.
- 377 • Furthermore, both DFT+*U* and HSE approximation yield similar trends in the formation  
378 energies of simple defect that are accessible for CuO.
- 379 • Intrinsically, CuO can be created either *p*-type or *n*-type, depending on the synthesis  
380 conditions employed. Despite their favourable formation energies, both *p*-type and *n*-type  
381 intrinsic defects show states embedded deep in the band gap, clarifying the ineffective  
382 photo-response utilization noted experimentally.
- 383 • Interstitial H is identified as a *p*-type promoter for CuO created under O-rich conditions,  
384 at the same time being detrimental for CuO formed under Cu-rich conditions suppressing  
385 all *n*-type intrinsic defects.

386 One of the main drawbacks while assessing the validity of the results outlined in this chapter  
387 is the lack of experimental evidence. Unlike Cu<sub>2</sub>O, for which various spectroscopic measure-  
388 ments of intrinsic defects are available, literature for CuO is scarce. Nevertheless, calculations  
389 reproduce well the observed conductivity types and the intrinsic defects underpinning them. It  
390 is expected that these results will stimulate further experimental attempts to obtain relevant  
391 transition levels and doped samples to further optimize the use of CuO as a photo-responsive  
392 material.

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402 in the Cardiff University data catalogue at <http://doi.org/10.17035/d.2019.0089582693>.

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