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# Self-Calibration of Phase Current Sensors with Sampling Errors by Multipoint Sampling of Current Values in a Single PWM Cycle

Jiadong Lu, *Member, IEEE*, Yihua Hu, *Senior Member, IEEE*, Jinglin Liu, *Member, IEEE*, and Huiqing Wen, *Senior Member, IEEE*

**Abstract**—The accuracy of current sensors is most crucial for the performance of an interior permanent magnet synchronous motor (IPMSM) drive. However, it may have sampling errors that are unavoidable for an actual drive. Therefore, to cope with this problem, this paper proposed a self-calibration strategy for phase-current sensors by utilizing the proposed topology and the correlation among the multiple current values obtained by current sampling values during one single pulse width modulation (PWM) cycle, making minor changes for the cablings of conventional current sensors in the premise of not affecting the normal operation of the drive, and abandoning complex observers or filters for easing computational burden. Besides, its effectiveness was verified by experimental results on a 5kW IPMSM motor prototype, which showed that such sampling errors could be well estimated and eliminated.

**Index Terms**—Current sampling error, drive, error compensation, interior permanent magnet synchronous motor (IPMSM), inverter, self-calibration.

## I. INTRODUCTION

INTERIOR permanent magnet synchronous motor (IPMSM) is attracting more and more attention due to its outstanding features such as high power density, high reliability and high efficiency [1]-[5]. Current measurement is essential for the normal operation of all closed-loop controlled electric machines including induction machines, permanent magnet synchronous machines, and synchronous reluctance machines [6]-[9]. The pre-installed multiple current sensors in IPMSM drives usually include the one at the DC-bus side and the two

(at least) at the phase side in a vector-controlled system [10]. The DC-bus current sensor is utilized for over-current protection and the phase current sensors serve as the detecting elements for current closed-loop control [11]. In a sense, the normal operation of these sensors determines the proper operation of the system. If any of them fails, the whole system is likely to collapse [12]-[15]. Under these circumstances, fault-tolerant control (FTC) strategies were proposed and successfully used to solve the problem of current sensor faults [16]-[21].

However, although these sensors are intact, their high measurement accuracy cannot be guaranteed [22], which is a more common reality. The cause behind this phenomenon is the sampling errors of current sensors, which can be explained from two aspects: 1) it is uncertain which sensor is in poor condition (i.e. has a degraded accuracy); 2) it is uncertain how inaccurate the sensor is. The measurement errors of current sensors are usually divided into offset errors and scaling errors [23], which are unavoidable in practice and will degrade system performance [24]. More seriously, these errors and the sampling circuits are probably imbalanced, which may further deteriorate the system performance [25]. All in all, the problem of sampling errors can cause serious consequences. Therefore, many studies have focused on the analysis and compensation of current measurement errors [26]-[35].

In [24] and [26], both band-pass filters (BPFs) and low-pass filters (LPFs) that are used to analyze DC output voltage ripples can be applied to screen out offset and scaling errors. The frequency characteristics of the output voltage in the current closed control loop are utilized to derive the offset and scaling errors in [27]. The speed fluctuation caused by the above mentioned sampling errors will be reflected in the output variable of the speed controller, which is also the reference value for the current controller. Therefore, in [28]-[30], the comparison between the reference and feedback values of the current controller is used to estimate the current measurement errors. In [31], two controllers are established by analyzing the d-q axis currents to estimate the sampling errors of the current sensor. To sum up, all these literatures use the variables within the control loop to estimate the current sensor sampling errors. In [34] and [35], a single current sensor based system is considered for the problem of sampling errors. In these two literatures, offset errors are eliminated by using the current

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J. Lu and J. Liu are with the School of Automation, Northwestern Polytechnical University (NWPU) and Shaanxi Key Laboratory of Small & Special Electrical Machine and Drive Technology of NWPU, Xi'an 710129, China. (E-mail: j.d.lu@nwpu.edu.cn, jinglinl@nwpu.edu.cn).

Y. Hu is with the Department of Electronic Engineering, University of York, York YO10 5DD, U.K. (E-mail: yihua.hu@york.ac.uk).

H. Wen is with the Department of Electrical and Electronic Engineering, Xi'an Jiaotong-Liverpool University, Suzhou 215123, China. (E-mail: Huiqing.Wen@xjtlu.edu.cn).

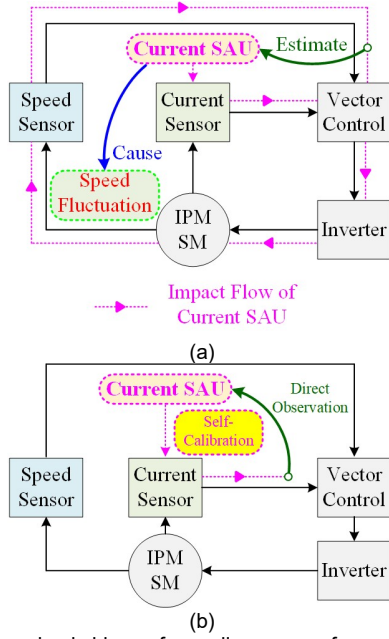


Fig. 1. Common basic ideas of sampling errors of current sensors and calibration method: (a) previous methods, (b) proposed self-calibration method.

characteristics of the single current system on the unique  $\alpha$ - $\beta$  axis.

At present, the main solution of this problem is to analyze its impacts on system performance, such as speed fluctuation or torque ripple. As a torque sensor is not usually installed in the system due to its high cost, the speed feedback information is essential for the aforementioned strategies. This is because the problem of sampling errors causes the speed fluctuation with one and two times the frequency of the fundamental one. The basic ideas of the previous and the newly proposed methods are illustrated in Fig. 1.

In Fig. 1(a), the sampling errors of current sensors can result in the speed fluctuation of the motor, which is in turn utilized to estimate such sampling errors. The involving methods have high requirements for the speed/position sensor. Besides, several observers or digital filters are usually needed to calibrate sampling errors. In this case, three problems will emerge: 1) the computational burden for the main processing unit, which is either a digital signal processor (DSP) or a microprocessor, is increased. 2) It takes a long time to estimate the sampling errors of current sensors, with an estimation accuracy susceptible to load changes. 3) If an inertial load is driven, the schemes for estimation on these sampling errors are likely to fail, because in an inertial system, the problems caused by such sampling errors are mainly reflected in torque ripples rather than in speed fluctuations.

Aiming at solving the aforementioned problems faced by the estimation on sampling errors of current sensors, we proposed in this paper a self-calibration strategy by multipoint sampling of current values in a single PWM cycle, as shown in Fig. 1 (b). The proposed method only requires the current information from one single pulse width modulation (PWM) cycle, with the rest calculation processes conducted only by few operations.

This means that it requires neither complex digital filters nor observers. Therefore, the proposed strategy does not add additional computational burden to the system. In addition, its independence from the speed or position feedback information as another feature may prevent its calibration accuracy from being affected by the load type. Besides, it needs no additional hardware devices and does not affect the normal operation of the drive - no matter the PWM generating method or current sampling for control.

The structure of this paper is as follows. In Section II, the problem of the sampling errors of current sensors and the proposed calibration topology are briefly illustrated, respectively. In Sections III & IV, the calibration strategy for both the offset and scaling errors of the two phase-current sensors are analyzed, respectively. In Sections V, the current chopping effect is analyzed. In Section VI, experimental validation is presented. The conclusion is given in Section VII.

## II. PROPOSED SELF-CALIBRATION TOPOLOGY FOR SAMPLING ERRORS OF CURRENT SENSORS AND ITS BASIC PRINCIPLES

### A. Types of the sampling errors of current sensors

A three-phase three-wire IPMSM drive usually consists of two phase-current sensors, i.e. phase-A & B current sensors. These two sensors can directly measure the corresponding current signals, whereas the phase-C current can only be calculated according to the other two current values ( $i_A + i_B + i_C = 0$ ). This is an ideal situation where there are no sampling errors. By taking the current offset and scaling errors into consideration, the relations between the measured three-phase currents,  $i_{AM}$ ,  $i_{BM}$  and  $i_{CM}$ , and the ideal ones,  $i_A$ ,  $i_B$  and  $i_C$ , are given by

$$\begin{cases} i_{AM} = k_A \cdot i_A + f_A \\ i_{BM} = k_B \cdot i_B + f_B \\ i_{CM} = -i_{AM} - i_{BM} \end{cases} \quad (1)$$

where  $k_A$ ,  $k_B$  and  $f_A$ ,  $f_B$  are the scaling and offset errors of phase-A & B current sensors, respectively.

It can be seen from (1) that due to the uncertainty of the four parameters for sampling errors of current sensors, the actually measured three-phase current values contain some errors, which will finally degrade the system performance [25]. In an ideal situation, if no such errors exist ( $k_A = k_B = 1$ ,  $f_A = f_B = 0$ ), the measured three-phase current values will be the same as the ideal ones. Unfortunately, these errors are unavoidable in practice [25]. For this reason, we aim to develop a calibration strategy for these errors in this paper.

### B. Proposed Calibration Topology

In this paper, we proposed a self-calibration strategy based on the topology given in Fig. 2. In this figure,  $i_{DC}$  as the current at the DC-bus side is used for over-current protection.  $i_U$  denotes the current of the DC-bus capacitor.  $i_P$  and  $i_N$  are the positive and negative currents at the input end of the inverter. Meanwhile, the positive directions of the current sensors are



TABLE III  
ESTIMATION EQUATIONS FOR OFFSET ERRORS.

Sector	$f_A$	$f_B$
I	$-i_{AM\_V1}+2i_{AM\_V7}$	$i_{BM\_V1}-i_{BM\_V2}+i_{BM\_V7}$
II	$-i_{AM\_V2}+i_{AM\_V3}+i_{AM\_V7}$	$-i_{BM\_V3}+2i_{BM\_V7}$
III	$i_{AM\_V4}$	$-i_{BM\_V3}+2i_{BM\_V7}$
IV	$i_{AM\_V4}$	$-i_{BM\_V4}+i_{BM\_V5}+i_{BM\_V7}$
V	$i_{AM\_V5}-i_{AM\_V6}+i_{AM\_V7}$	$i_{BM\_V6}$
VI	$-i_{AM\_V1}+2i_{AM\_V7}$	$i_{BM\_V6}$

$$\begin{cases} i_{BM\_V1} = -k_B \cdot i_C + f_B \\ i_{BM\_V2} = k_B \cdot (i_B - i_C) + f_B \\ i_{BM\_V7} = k_B \cdot i_B + f_B \end{cases} \quad (4)$$

It can be seen from (3) and (4) that the offset errors of the two phase-current sensors can be simply extracted from the sampled currents:

$$\begin{cases} f_A = -i_{AM\_V1} + 2i_{AM\_V7} \\ f_B = i_{BM\_V1} - i_{BM\_V2} + i_{BM\_V7} \end{cases} \quad (5)$$

### B. Sectors II, ..., VI

Similar to the situations in Sector I, the two offset errors in Sectors II, ..., VI can also be calculated, which are given in Table III.

## IV. CALIBRATION METHOD FOR SCALING ERRORS

In this section, the self-calibration strategy for the scaling errors of the two phase-current sensors is presented, and the specific methods in the six output vector sectors (Sector I, ..., VI) are given.

### A. Sector I

The measured currents under the active basic vectors are given in (3) and (4). Here, we define two variables  $A_{S1}$  and  $B_{S1}$ :

$$\begin{cases} A_{S1} = i_{AM\_V1} - i_{AM\_V2} = -k_A \cdot i_B \\ B_{S1} = i_{BM\_V1} - i_{BM\_V2} = -k_B \cdot i_B \end{cases} \quad (6)$$

From (6), it can be seen that the relationship between scaling errors  $k_A$  and  $k_B$  can be easily obtained:

$$\frac{k_A}{k_B} = \frac{A_{S1}}{B_{S1}} \quad (7)$$

It should be noted that in this paper, the absolute values of  $k_A$  and  $k_B$  cannot be obtained. Whereas, by applying (7), we can balance the scaling error differences between the two current sensors. Yet what is important is that the detrimental effect of scaling errors on system performances (which cause speed fluctuations and torque ripples with two times the fundamental frequency) can be eliminated upon balancing the scaling errors

TABLE IV  
ESTIMATION EQUATIONS FOR SCALING ERRORS.

Sector	$k_A/k_B$	$A_{Sx}$	$B_{Sx}$
I	$A_{S1}/B_{S1}$	$A_{S1}=i_{AM\_V1}-i_{AM\_V2}$	$B_{S1}=i_{BM\_V1}-i_{BM\_V2}$
II	$A_{S2}/B_{S2}$	$A_{S2}=i_{AM\_V2}-i_{AM\_V3}$	$B_{S2}=i_{BM\_V2}-i_{BM\_V3}$
III	$A_{S3}/B_{S3}$	$A_{S3}=i_{AM\_V3}-i_{AM\_V4}$	$B_{S3}=i_{BM\_V3}-i_{BM\_V4}$
IV	$A_{S4}/B_{S4}$	$A_{S4}=i_{AM\_V4}-i_{AM\_V5}$	$B_{S4}=i_{BM\_V4}-i_{BM\_V5}$
V	$A_{S5}/B_{S5}$	$A_{S5}=i_{AM\_V5}-i_{AM\_V6}$	$B_{S5}=i_{BM\_V5}-i_{BM\_V6}$
VI	$A_{S6}/B_{S6}$	$A_{S6}=i_{AM\_V6}-i_{AM\_V1}$	$B_{S6}=i_{BM\_V6}-i_{BM\_V1}$

[27].

### B. Sectors II, ..., VI

Similar to the situations in Sector I, the relationship between the scaling errors  $k_A$  and  $k_B$  in Sectors II, ..., VI can also be calculated, which are given in Table IV.

### C. Compensation of Scaling Errors

Different from the offset errors, which can be compensated right after the estimation on the current values, the scaling errors have a slightly complicated compensation process. This is because they cannot be directly estimated - only the proportional relationship between the sampling values of all phase-current sensor can be estimated. As a result, more steps need to be carried out to estimate the scaling errors. From Table IV, the value of  $k_A/k_B$  is first obtained, and we thus assume that:

$$k = \frac{k_A}{k_B} \quad (8)$$

The relationship between the two scaling errors is a proportional one. Thus, in order to balance them, we need to multiply and divide their current detection values by the same compensation parameter, respectively. In this paper, we define the compensation parameter as  $x$ , and the compensation law is given in (9).

$$\begin{cases} i_A' = x \cdot (k_A \cdot i_A) \\ i_B' = \frac{1}{x} \cdot (k_B \cdot i_B) \end{cases} \quad (9)$$

where  $i_A'$  and  $i_B'$  are the compensated phase-A & B currents.

The balance law of the proposed method is that the two current sampling values should have the same gain coefficient after balancing. It should be noted that in (9) the offset errors have been compensated in advance. According to the balance law and (9), the value of  $x$  can be easily obtained:

$$\begin{aligned} x \cdot k_A = \frac{1}{x} \cdot k_B \\ \Rightarrow x = \sqrt{\frac{k_B}{k_A}} \end{aligned} \quad (10)$$

Finally, the compensation law is given in (11).

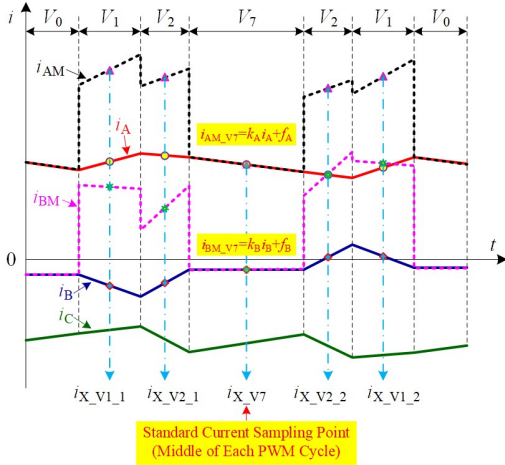


Fig. 3. The current chopping effect on the proposed strategy (Sector I).

$$\begin{cases} i_A' = \sqrt{\frac{k_B}{k_A}} \cdot (k_A \cdot i_A) = \sqrt{k_A \cdot k_B} \cdot i_A \\ i_B' = \sqrt{\frac{k_A}{k_B}} \cdot (k_B \cdot i_B) = \sqrt{k_A \cdot k_B} \cdot i_B \end{cases} \quad (11)$$

## V. CURRENT CHOPPING EFFECT, CURRENT MEASUREMENT DEAD ZONES AND OVERALL CONTROL STRATEGY

### A. Current Chopping Effect

The information on the proposed calibration strategy for current sampling errors only includes the measured current values within one PWM cycle under different switching states. In this Section, the current chopping effect and the current sampling method will be discussed.

In Section III & IV, we assume that the current chopping effect, which is unavoidable in practice, as shown in Fig. 3, is not considered, i.e., the measured currents are average values. In Fig. 3, which displays the waveforms of the three-phase currents and the two measured ones (Sector I),  $i_{X\_V1\_1}$  and  $i_{X\_V1\_2}$  are the current sampling values of the X (X stands for A, B, AM, BM) current under the respective two action periods of the vectors  $V_1$  and  $V_2$  (there are two symmetrical periods for  $V_1$  and  $V_2$  in each PWM cycle);  $i_{X\_V7}$  is the current sampling value of the X current under the action period of the vector  $V_7$ .

It can be seen from Fig. 3 that the measured currents are not sampled at the same time, which results in unexpected current sampling errors. The impact of the current chopping effect on the proposed strategy can be explained as follows.

In Table II, Table III and Table IV, the current values of  $i_{AM\_V7}$  and  $i_{BM\_V7}$  are all sampled at the middle of each PWM cycle (under the switching state of  $V_7$ ), which can be regarded as the average values of the corresponding current values during the PWM cycle:

$$\begin{cases} i_{AM\_V7} = k_A \cdot i_{A\_V7} + f_A = k_A \cdot \bar{i}_A + f_A \\ i_{BM\_V7} = k_B \cdot i_{B\_V7} + f_B = k_B \cdot \bar{i}_B + f_B \end{cases} \quad (12)$$

where  $\bar{i}_A$  and  $\bar{i}_B$  are the average values of  $i_A$  and  $i_B$  during the PWM cycle.

However, the values of other currents, i.e.,  $i_{X\_V1\_1}$ ,  $i_{X\_V1\_2}$ ,  $i_{X\_V2\_1}$  and  $i_{X\_V2\_2}$ , are not sampled at the middle of the PWM cycle, but at different sampling points in the PWM cycle instead. Therefore, the other current values are not equal to the corresponding average current values in the PWM cycle. Therefore, take  $i_{AM}$  as an example, in sector I,  $i_{AM\_V1\_1}$  is not equal to  $i_{AM\_V1}$ . If the current values of  $i_{AM\_V1\_1}$  and  $i_{AM\_V7}$  at different sampling points are used to estimate the offset error of phase A (Sector I), we can obtain the following inequation according to Table II, Table III and the above analysis:

$$\begin{aligned} f_A &= -i_{AM\_V1} + 2i_{AM\_V7} \\ &= -(2k_A \cdot \bar{i}_A + f_A) + 2i_{AM\_V7} \\ &\neq -(2k_A \cdot i_{AM\_V1\_1} + f_A) + 2i_{AM\_V7} \\ &= -i_{AM\_V1\_1} + 2i_{AM\_V7} \end{aligned} \quad (13)$$

where in this paper  $i_{A\_V1\_1}$  and  $i_{A\_V1\_2}$  are the transient values of  $i_A$  under the two symmetrical action periods of  $V_1$ .

From (13), it can be seen that if the transient current values are utilized to replace the average values in the proposed strategy, unexpected errors will emerge in the estimation results. Therefore, in this paper, the average value of the two currents sampled at the symmetrical points on both sides of the PWM midpoint is used to represent the corresponding average current value. Take  $i_{AM}$  in sector I as an example, we use the average values of  $i_{AM\_V1\_1}$  and  $i_{AM\_V1\_2}$  in Fig. 3 to represent the value of  $i_{AM\_V1}$  (due to the symmetrical current sampling method under the symmetrical PWM):

$$\begin{aligned} i_{AM\_V1} &= 2k_A \cdot \bar{i}_A + f_A \\ &= 2k_A \cdot \left( \frac{i_{A\_V1\_1} + i_{A\_V1\_2}}{2} \right) + f_A \\ &= \frac{2k_A \cdot i_{A\_V1\_1} + f_A}{2} + \frac{2k_A \cdot i_{A\_V1\_2} + f_A}{2} \\ &= \frac{i_{AM\_V1\_1} + i_{AM\_V1\_2}}{2} \end{aligned} \quad (14)$$

In (14), the current processing method is also applicable to the other current sampling values.

### B. Current Measurement Dead Zones And Drawbacks of The Proposed Strategy

Due to the dead time of the switching devices, diode recovery time and AD sampling time, the minimum duration  $T_{min}$  is required for each switching state, during which an action period for a precise current sampling is needed. Therefore, the regions that can be used to calibrate current sampling errors are limited. From Table III and Table IV, it can be seen that the action time for basic vectors should meet the following requirements: 1) the action time of  $V_7$  ( $T_7$ ) should be longer than



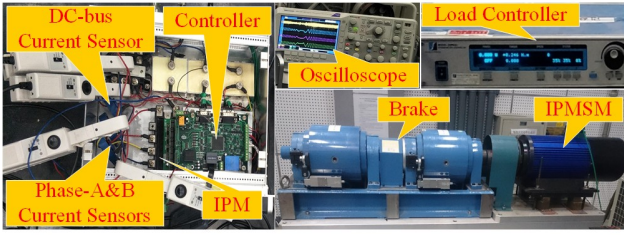


Fig. 6. The experimental setup.

TABLE V  
MAIN PARAMETERS OF IPMSM FOR EXPERIMENT.

Parameter	Value	Parameter	Value
Rated power	5 kW	Pole pairs	3
Inverter DC voltage	540 V	$d$ -axis Inductance	4.2 mH
Rated voltage	380 V	$q$ -axis Inductance	10.1 mH
Rated current	8.5 A	Phase resistance	0.18 $\Omega$
Efficiency	0.9	Maximum speed	3000 r/min
Rated torque	15 N·m	Voltage constant	125 V/(kr/min)

TABLE VI  
THE PARAMETERS OF SAMPLING ERRORS OF CURRENT SENSORS.

Parameter	Value	Parameter	Value
$f_A$	1.5 A	$f_B$	-2 A
$k_A$	0.9	$k_B$	1.2

the system, and their parameters are given in Table VI.

The phase-A & B currents in steady state with the problem of sampling errors are displayed in Fig. 7. When the motor runs at 3000 r/min with 15 N·m load, it can be seen that the actual phase currents fluctuate obviously with unbalanced waveforms.

The actual d-q axis currents with the problem of sampling errors are displayed in Fig. 8. The ripples on the d-q axis currents caused by this problem decrease the system performance.

The motor output speed ( $n$ ) and its harmonic components with the problem of sampling errors are displayed in Fig. 9. It can be seen from Fig. 9 (a) that the speed ripple caused by this problem reaches  $\pm 40$  r/min. By fast fourier transform (FFT), the harmonic components of the output speed are given in Fig. 9 (b). As can be noticed, the main harmonic orders are one and two times the fundamental frequency components, which reach 6 r/min and 11 r/min respectively. This is the same as what has been pointed out in the Introduction Section.

The waveforms of  $i_{AM}$  and  $i_{BM}$  with the problem of sampling errors are displayed in Fig. 10. During this period, the output voltage vector is within Sector VI, the PWM cycle period ( $T_s$ ) is marked with yellow shadow, and the action vectors of the seven-segment SVPWM are  $V_0$ ,  $V_1$ ,  $V_6$ ,  $V_7$ ,  $V_6$ ,  $V_1$  and  $V_0$ , respectively. According to the proposed strategy in Sector VI,  $i_{XM\_V1}$  and  $i_{XM\_V6}$  are sampled for calibration.  $i_{XM\_V7}$  is utilized for both the closed-loop control and calibration.

The measured current values are given in Table VII. The estimated parameters of the sampling errors of all current

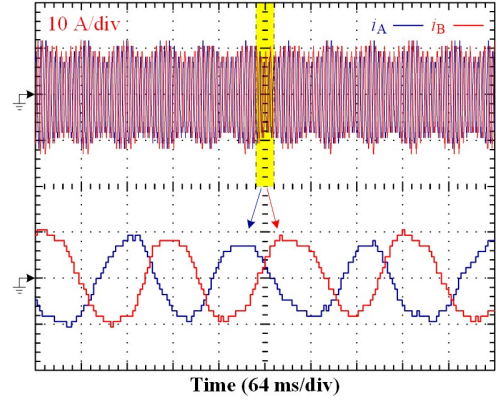
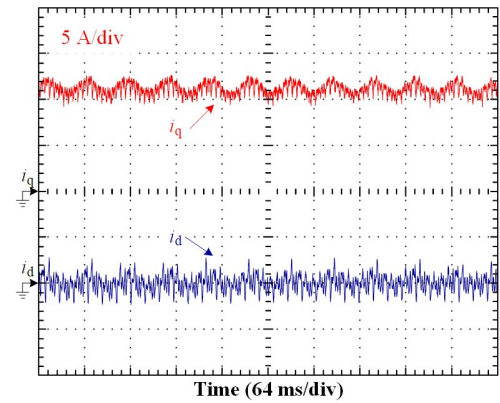
Fig. 7. Actual phase-A & B currents in steady state ( $n=3000$  r/min) with the problem of sampling errors.

Fig. 8. Actual d-q axis currents with the problem of sampling errors.

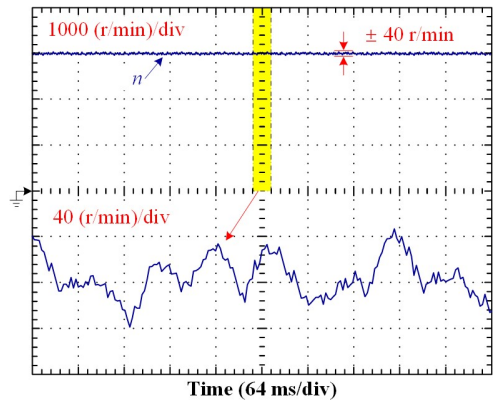


Fig. 9. Motor output speed with the problem of sampling errors: (a) output speed, (b) harmonic components.

sensors are also given in Table VII. Compared with the artificially introduced parameters, the estimated ones have high



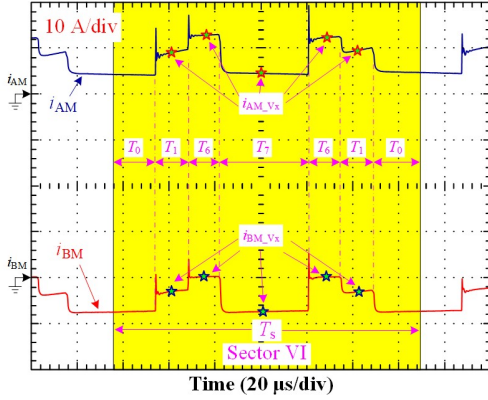


Fig. 10. Actually detected waveforms of  $i_{AM}$  and  $i_{BM}$  with the problem of sampling errors (Sector VI).

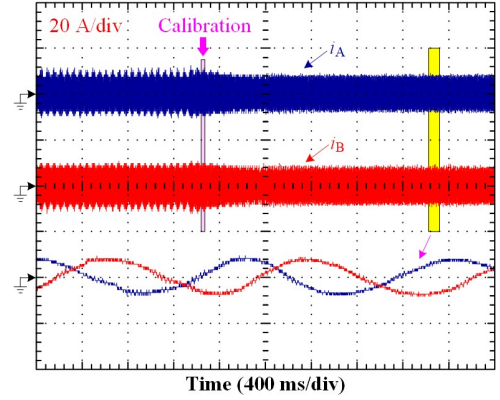


Fig. 11. The phase-A & B currents during the calibration.

TABLE VII  
THE MEASURED CURRENT VALUES AND THE ESTIMATED SAMPLING ERRORS OF CURRENT SENSORS.

Parameter	Value	Parameter	Value
$i_{AM\_V1}$	9.93 A	$i_{BM\_V1}$	-6.19 A
$i_{AM\_V6}$	12.96 A	$i_{BM\_V6}$	-2.05 A
$i_{AM\_V7}$	5.70 A	$i_{BM\_V7}$	-11.49 A
$f_A'$	1.47 A	$f_B'$	-2.05 A
$f_A' - f_A$	-0.03 A	$f_B' - f_B$	0.06 A
$k_A'/k_B'$	0.73	$(k_A'/k_B')/(k_A/k_B)$	0.98

estimation precision.

It should be noted that the estimation accuracy of the problem of sampling errors depends on several factors - first, the artificially introduced parameters of sampling errors for current sensors are not exactly the same as the actual ones; second, random sampling errors; third, other kinds of problems of sampling errors that are not considered in this paper.

By applying the proposed calibration strategy to the sampling errors, the waveforms of phase-A & B currents with the problem of sampling errors are presented in Fig. 11. It can be seen from this figure that after calibration, the phase-currents become balanced again. Therefore, the detrimental effect of this problem on the system performance can be finally eliminated.

The information on the motor output speed and its FFT analysis is given in Fig. 12. It can be seen from Fig. 12 (a) that the speed ripples are reduced from  $\pm 40$  r/min to  $\pm 5$  r/min. The remaining speed ripples may be caused by the imperfect control effect of the system. The FFT analysis of the output speed is given in Fig. 12 (b). It can be seen that the main harmonic components in Fig. 9 (b) are eliminated. Particularly, the first and second-order harmonic components are reduced from 6 r/min and 11 r/min to smaller than 0.01 r/min, with the maximum harmonic component of about 0.05 r/min. This means that good system performance is guaranteed.

By testing the estimation results under small sampling errors, which are given in Table VIII, the currents and speed show minor differences compared with the normal ones. However, the FFT analysis of torque ripples in Fig. 13 (a) shows that the main effect is reflected in the torque ripples under this

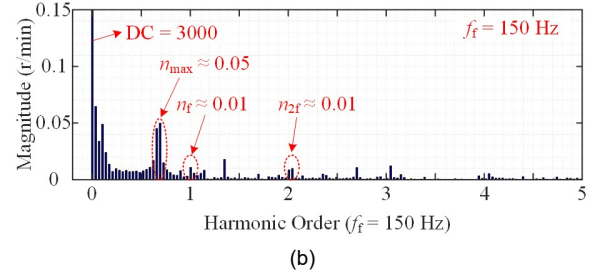
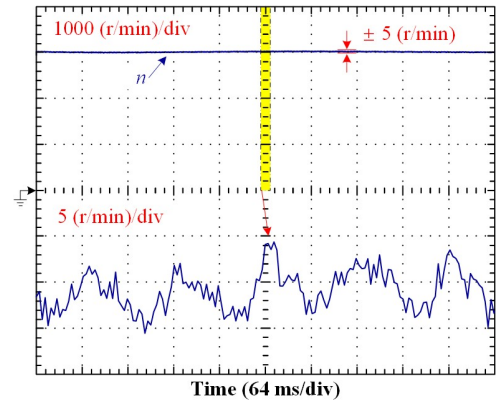


Fig. 12. The motor output speed after calibration of the sampling errors of current sensors: (a) output speed, (b) harmonic component.

TABLE VIII  
THE PARAMETERS OF SMALL SAMPLING ERRORS.

Parameter	Value	Parameter	Value
$f_A$	0.15 A	$f_B$	-0.2 A
$k_A$	0.95	$k_B$	1.05

condition, and that the one ( $T_f$ ) and two times ( $T_{2f}$ ) the fundamental frequency components are significant.

By applying the proposed strategy, the estimated current sampling errors are displayed in Table IX. It can be seen from this table that the estimated results are not good as the results in Table VII, but they can still reduce the current sampling errors to a certain degree. The FFT analysis of the torque ripples is illustrated in Fig. 13 (b). It can be seen from this figure that the components with one and two times of the fundamental frequency are almost eliminated.

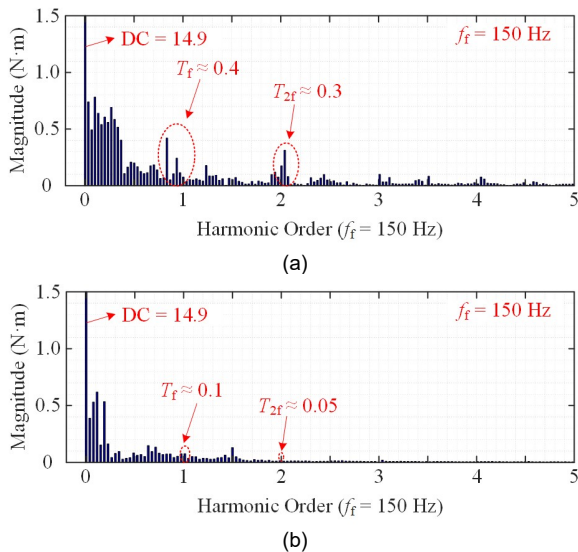


Fig. 13. Torque ripples FFT analysis with the problem of sampling errors: (a) before calibration, (b) after calibration.

## VII. CONCLUSION

In order to solve the problem of sampling errors of the current sensors that degrades system performance, this paper proposes a self-calibration strategy for phase-current sensors. The proposed strategy applies a topology that has been slightly changed based on the traditional one, in the premise of not affecting the normal operation of the system. Its effectiveness is verified by experimental results on a 5-kW IPMSM prototype. Phase-current waveforms are greatly improved after calibration of the problem above mentioned. The experimental results demonstrate that the speed ripples are significantly reduced by 87.5%.

- 1) The proposed calibration strategy to tackle the above-mentioned problem can be realized within 1 ms in one single PWM cycle.
- 2) The proposed strategy can be simply extended to other situations where all phase-current sensors are installed.
- 3) The normal operation of the system is not affected by applying the proposed strategy.
- 4) The proposed strategy accomplishes the online calibration of the problem of sampling errors of current sensors, while abandoning complicated observers and filters, which results in a simpler algorithm.
- 5) The proposed strategy might be applied to other types of motor drives by modification.
- 6) Good electromagnetic isolation measures can prevent the inverter itself and the additional cables from electromagnetic interference to the system.

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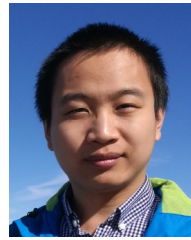
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TABLE IX  
THE ESTIMATED VALUES OF SMALL SAMPLING ERRORS.

Parameter	Value	Parameter	Value
$f_A'$	0.09 A	$f_B'$	-0.28 A
$f_A' - f_A$	-0.06 A	$f_B' - f_B$	-0.08 A
$k_A'/k_B'$	0.93	$(k_A'/k_B')/(k_A/k_B)$	1.03

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**Jiadong Lu** (M'19) was born in Pucheng, China, 1990. He received the B.S., the M.S. and the Ph.D. degrees in electrical engineering from Northwest Polytechnical University (NWPU), Xi'an, China in 2012, 2015 and 2018, respectively. Between 2017 and 2018, he was with the Department of Electrical Engineering, Electronics and Computer Science, University of Liverpool (UoL), U.K. as an Honorary Academic Researcher. Currently, he is an Associate

Research Fellow at the Department of Electrical Engineering, NWPU. His research interests include hybrid-fault-tolerant control techniques for permanent magnet synchronous motor drives, aging issue for motor drives and power electronics converters & control.



**Yihua Hu** (M'13-SM'15) received the B.S. degree in electrical engineering in 2003, and the Ph.D. degree in power electronics and drives in 2011, both at China University of Mining and Technology. Between 2011 and 2013, he was with the College of Electrical Engineering, Zhejiang University as a Postdoctoral Fellow. Between 2013 and 2015, he worked as a Research Associate at the power electronics and motor drive group, the University of Strathclyde. Between 2016 and 2019, he was a Lecturer at the Department of Electrical Engineering and Electronics, University of Liverpool (UoL). Currently, he is a reader at Electronics Engineering Department at University of York (UoY). He has published 85 papers in IEEE Transactions journals. His research interests include renewable generation, power electronics converters & control, electric vehicle, more electric ship/aircraft, smart energy system and non-destructive test technology. He is the associate editor of IEEE Transactions on Industrial Electronics, IET Renewable Power Generation, IET Intelligent Transport Systems and Power Electronics and Drives.



**Jinglin Liu** (M'01) received the B.Eng. degree in electrical engineering from Tsinghua University, Beijing, China, in 1986, and the M.Eng. and the Ph.D. degrees in electrical engineering from NWPU, Xi'an, China, in 1990 and 2002, respectively. Since 1994, he has been a Faculty Member with NWPU, Xi'an, where he is currently a Professor of Electrical Engineering. His research interests include electrical machines design and drives, power electronics, fault diagnosis, and motion control.



**Huiqing Wen** (M'13-SM'18) received his B.S. and M.S. degrees in Electrical Engineering from Zhejiang University, Hangzhou, China, in 2002 and 2006; and his Ph.D. degree in Electrical Engineering from the Chinese Academy of Sciences, Beijing, China, in 2009. From 2009 to 2010, he was an Electrical Engineer working in the Research and Development Center, GE (China) Co., Ltd., Shanghai, China. He is presently working as an Associate Professor at the Xi'an Jiaotong-Liverpool University, Suzhou, China. His current research interests include power electronics and renewable energy.