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Recent north magnetic pole acceleration towards Siberia caused by flux lobe elongation

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Abstract

The wandering of Earth's north magnetic pole, the location where the 6 magnetic field points vertically downwards, has long been a topic of scien-7 tific fascination. Since the first in-situ measurements in 1831 of its location 8 in the Canadian arctic, the pole has drifted inexorably towards Siberia, ac-9 celerating between 1990 and 2005 from its historic speed of 0-15 km/yr to 10 its present speed of 50-60 km/yr. In late October 2017 the north magnetic 11 pole crossed the international date line, passing within 390 km of the geo-12 graphic pole, and is now moving southwards. Here we show that over the 13 last two decades the position of the north magnetic pole has been largely 14 determined by two large-scale lobes of negative magnetic flux on the core-15 mantle-boundary under Canada and Siberia. Localised modelling shows that 16 elongation of the Canadian lobe, likely caused by an alteration in the pattern 17 of core-flow between 1970 and 1999, significantly weakened its signature 18 on Earth's surface causing the pole to accelerate towards Siberia. A range 19 of simple models that capture this process indicate that over the next decade 20 the north magnetic pole will continue on its current trajectory travelling a 21 further 390-660 km towards Siberia. 22

Historical determinations of the pole position, for example by Ross in 1831 [1],
and later by Amundsen in 1904 [2], relied on ground surveys, searching for the

location where the horizontal component of magnetic field H was zero and a mag-25 netic needle pointed directly down to the center of the Earth [3]. Such direct deter-26 minations are difficult, especially if the pole position is not on land and because of 27 field fluctuations due to currents in the high latitude ionosphere [4]. More recently 28 the magnetic pole position has been determined from global models of the geo-29 magnetic field [5] built using measurements made by both satellites and by a net-30 work of ground observatories. The accuracy of such pole determinations, which 31 depends on the quality and distribution of the contributing observations along with 32 the ability to remove the external magnetic field, has steadily improved over time; 33 since 1999 there has been continuous monitoring of the geomagnetic field from 34 space by a series of dedicated satellite missions, most recently the Swarm mission 35 [6]. In Fig 1 we show the path of the pole since 1840 from the COV-OBS.x1 36 [7] and CHAOS-6-x8 [8] geomagnetic field models alongside in-situ historical 37 measurements. The location of the magnetic pole is a characteristic of the core-38 generated magnetic field that is spherically-radially attenuated through the mantle, 39 which may be considered as an electrical insulator on the time-scales of relevance 40 here. The magnetic pole's position is thus only an indirect indicator of the state of 41 Earth's dynamo. However the specific geometry of the magnetic field on Earth's 42 surface is of broad societal importance, as was demonstrated recently by the need 43 for a high-profile irregular update in 2019 of the world magnetic model used for 44 navigation in many mobile devices [9]. 45

⁴⁶ **Recent movement of the north magnetic pole**

Compared with its meandering position prior to the 1970s, over the past 50 years 47 the north magnetic pole has travelled along a remarkably linear path that is un-48 precedented in the recent historical record [10; 11; 12], guided along a trough of 49 low horizontal field [10; 13]. Using high-resolution geomagnetic data from the 50 past two decades [8], Figs 2a,d show that this trough connects two patches of 51 strong radial magnetic field at high latitude centred on Canada and Siberia. The 52 importance of these two patches in determining the structure of the field close to 53 the north magnetic pole has been well known for several centuries [14]. Both the 54 path of the north magnetic pole and the crucial Canadian and Siberian magnetic 55 patches are characteristics of the large-scale field [12], already evident when the 56 field is truncated at spherical harmonic degree l=6 (Figs 2b,e). Considered in iso-57 lation from the remainder of the global field, each Earth-surface patch of strong 58 radial field would define a magnetic dip pole close to its centre point. The present 50 two-patch structure of the high latitude geomagnetic field then defines two ends 60

of a linear conduit of near vertical field along which the north magnetic pole can readily travel.

Between 1999 and 2019, the Siberian patch showed a slight intensification from a minimum value of -60.5 to -60.6 μ T, while the Canadian patch decreased significantly in absolute value from a minimum of -59.6 to -58.0 μ T (Fig 2a,d). Together, these caused the direction of travel of the north magnetic pole to be towards Siberia.

Although the magnetic field on Earth's surface is linearly related to the struc-68 ture of the field on the core-mantle boundary (CMB), the geometric attenuation 69 through the mantle means that this relationship is not a simple mapping. For ex-70 ample, the north magnetic pole does not correspond to a location on the CMB 71 where the horizontal field vanishes, but rather reflects a non-local averaging of 72 the field as shown in Figures 2b,c and 2e,f. The important Canadian and Siberian 73 surface patches are also spatial averages over regions dominated by the large-74 scale lobes of intense magnetic flux underneath Canada and Siberia on the CMB 75 that are themselves fundamental features of the geodynamo process (Figs 2c,f) 76 [15]. We find that the time-dependent position of the pole along the conduit is 77 largely governed by a balance or tug-of-war between the competing influences 78 of the Canadian and Siberian lobes on the CMB. The angular offset between the 79 pole and these controlling flux lobes at mid to high latitudes (50 - 70° N) is in ac-80 cord with the relevant Green's functions for Laplace's equation under Neumann 81 boundary conditions [16; 17]. 82

Localised flux lobe elongation

We now probe the physical mechanism that underpins the recent shift in balance 84 between the two flux lobes. Changes in the CMB radial magnetic field over 1999-85 2019 (movie S1) show that the Canadian flux lobe (marked A, Fig 3c) elongated 86 longitudinally and divided into two smaller joined lobes (A' and B) within the 87 marked wedge (Fig 3a). Although lobe B has a higher intensity compared to lobe 88 A, importantly the spatial lengthscale of the magnetic field within the wedge has 89 decreased. The transfer of magnetic field from large to smaller scales caused the 90 weakening of the Canadian patch at Earth's surface because smaller scales attenu-91 ate faster through the mantle with distance from the source. At the same time the 92 increasing proximity of lobe B to the Siberian lobe enhanced the Siberian surface 93 patch (Fig 3d). To demonstrate that this elongation effect is the primary cause of 94 the recent north magnetic pole movement, we performed a numerical experiment 95 where we isolated geomagnetic variation over the period 1999-2019 to within the 96

wedge (Figs 3a,c), the geomagnetic field being held fixed at its 1999 structure 97 elsewhere, and calculated the geomagnetic signature on the Earth's surface (see 98 methods). This simple model reproduces the weakening of the large-scale part of 90 the Canadian flux lobe at the CMB (Fig 3b) and the concomitant weakening of 100 the Canadian patch at Earth's surface (Fig 3d), in accord with Fig 2; it also repro-101 duces the growth of the Siberian surface patch. Furthermore, it accounts for 961 102 km of the 1104 km (87%) distance travelled by the north magnetic pole over 1999-103 2019. In a similar vein, we conducted additional numerical experiments (see figs 104 S1, S2 and methods) to test two other localised mechanisms previously proposed 105 to explain the recent north magnetic pole movement: those of intense geomag-106 netic secular variation under the New Siberian Islands [16] and the influence of 107 a polar reversed-flux-patch on the CMB [11]. Both of these hypotheses produce 108 only small movements of the pole (travelling respectively 142 km and 16 km over 109 1999-2019). Prior to 1990, and at least as far back as 1940 (movie S2), the COV-110 OBS.x1 geomagnetic model shows that the Canadian flux lobe was quasi-stable, 111 consistent with the slowly moving magnetic pole. In the 1990s, vigorous elonga-112 tion leading up to the flux lobe splitting post 1999 resulted in the observed rapid 113 change in speed of the north magnetic pole. 114

Interpretation in terms of core-flow

Time variation of the geomagnetic field arises through a combination of core-flow 116 and magnetic diffusion. The reconfiguration of the Canadian flux lobe requires 117 a change in the signature in either or both of these two effects within the core 118 under Canada, although inference of any single underlying dynamical process is 119 non-unique. Here we base our interpretation on the frozen-flux assumption which 120 asserts that over decadal timescales the impact of core-flow is likely dominant 121 [18], and is consistent with the formation and advection of lobe B (Fig 3a). Fig 122 4a-c shows snapshots of the radial magnetic field with streamlines showing direc-123 tion and magnitude of the large-scale core surface flow in 1970, 1999 and 2017, 124 depicting flow changes in this region during the acceleration phase of the north 125 magnetic pole. The presented flow models are the ensemble means of a series 126 of flows inferred by probabilistic inversions of both ground-based observatory 127 and satellite data, with a parameterisation of the unknown magnetic diffusion and 128 sub-grid scale induction processes [19; 20; 21]. In 1970, an intense large-scale 129 flow transported magnetic flux northwards under the east-coast of North Amer-130 ica, connecting to a polar westwards flow around a section of the inner-core tan-131 gent cylinder. Importantly, only a small part of the northward flow at that time 132

passed through the Canadian flux lobe. By 1999 the flow had altered into a broad 133 trans-North-America stream that converged and strengthened under Alaska: this 134 differential velocity was efficient at elongating (by stretching) the Canadian lobe 135 westwards. By 2017 the flow under Alaska had further strengthened, advection 136 and further stretching acting to separate the Canadian lobe into two pieces. Our 137 interpretation based on the presented ensemble mean flow is reinforced by the 138 fact that the basic sequence of events described above occurs in all flow ensemble 139 members. 140

The strengthening azimuthal flow under the Bering Straits, a key part of the 141 core-flow changes described above, may also be associated with the appearance 142 of an intense tangent-cylinder jet in this region, which has a clear observational 143 signature in the small-scale magnetic field (above spherical harmonic degree 11) 144 after 2004 [22]. However, such a tangent cylinder jet is in itself too localized 145 at high-latitude to be responsible for the elongation of the Canadian lobe in the 146 1990s that caused the rapid acceleration of the north magnetic pole. Instead it 147 seems that alteration in the global gyre structure [23; 24] beneath North America 148 began the elongation and contemporaneous north magnetic pole acceleration. 149

Future predictions and historical perspectives

Fig 1 shows a prediction of the future north magnetic pole position from a va-151 152 riety of models: linear extrapolations from 2019 of the World Magnetic Model (v2) [9] and CHAOS-6-x8 [8], and predictions based on the two end-member pro-153 cesses generating geomagnetic secular variation, frozen-flux induction and pure 154 magnetic diffusion (see methods). All the models are based on recently observed 155 secular variation including the elongation of the Canadian flux lobe, and all pre-156 dict a continuation of the current trajectory of the pole, with the greatest change 157 in position being from one flow ensemble member (660 km) and the minimum 158 change in position from the World Magnetic Model (v2) (390 km). 159

Will the north magnetic pole ever return to Canada? Given the delicate bal-160 ance between the Canadian and Siberian flux lobes controlling the position of 161 the pole along the trough of weak horizontal field, it would take only a minor 162 readjustment of the present configuration to reverse the current trend. Predictions 163 of the magnetic field over decade to century timescales are on the horizon using 164 data assimilation methods [25; 26; 27], but these are still under development and 165 for now it is most informative to look at its past behaviour as a guide. Recon-166 structions of the historical and archeomagnetic field over the past few thousand 167 years are inherently smoothed in time and based on sparse data, but nevertheless 168

can resolve the large-scale field patches that control the location of the magnetic 169 north pole. These reconstructions show that although the northern hemisphere has 170 largely been dominated by two flux patches, occasionally a three-patch structure 171 has arisen which would have had an effect on the pole's position [28; 29; 30]. 172 Over the last 400 years, the pole has meandered quasi-stably around northern 173 Canada, but over the last 7000 years it seems to have chaotically moved around 174 the geographic pole, showing no preferred location [12]. Analogues of the recent 175 acceleration may have occurred at 4500 BC and 1300 BC when the speed reached 176 about 3-4 times the average seen in these reconstructions. The most recent of 177 these events coincided with the pole moving towards Siberia (from a region close 178 to Svalbard) where it remained stable for several hundred years. For now, a con-179 clusive answer to the future location of the north magnetic pole will have to await 180 detailed monitoring of the geomagnetic field from the Earth's surface and space 181 in the coming years. 182

183 Methods

The isolation of geomagnetic secular variation in specific regions on the CMB 184 as shown in Figs 3, S1 and S2 is achieved using a physical grid: inside the 185 shown wedge the radial component of the geomagnetic field is allowed to evolve, 186 whereas outside it is frozen at its initial state. We transform to an equivalent 187 divergence-free magnetic-potential representation based on spherical harmonics, 188 which allows upward continuation of the magnetic field to the Earth's surface. The 189 latitude-longitude grid has L+1 Gauss-Legendre points in colatitude, and 3L+1190 equally spaced points in longitude, where the maximum spherical harmonic de-191 gree is L = 13. Note that any monopolar component or discontinuities caused 192 by adjoining two distinct magnetic field structures are removed by the projection 193 adopted. 194

To predict the north magnetic pole position using the large-scale flow ensem-195 ble of [20; 21], for each ensemble member all spherical harmonic flow coefficients 196 are extrapolated 2019-2029 using a simple linear best fit through their values from 197 2014-2018. The rate of change of geomagnetic field is then computed from the 198 induction equation using the time-dependent large-scale flow along with a static 199 correction term. The geomagnetic field is then evolved through time using a first 200 order time-stepping scheme and the position of the north magnetic pole evaluated 201 using a descent method in the horizontal magnitude. The correction term is cho-202 sen so that the Gauss coefficients (to degree 13) of the modelled rate of change of 203 geomagnetic field at 2019 match those from CHAOS-6-x8. Its static nature relies 204 upon on the assumption that both diffusion, and any small-small scale interactions 205 not captured in the large scale flow models, are time-independent over a 10-year 206 period. A purely-diffusive prediction is based on the model of [31], in which a 207 magnetic field diffuses from its initial state. The model is described by two ra-208 dial basis functions for each poloidal spherical harmonic mode up to a maximum 209 spherical harmonic degree 13. The coefficients describing the initial field (here 210 taken to be in 2014) are chosen by fitting to CHAOS-6-x8 over the time period 211 2014-19. The model is then evolved beyond 2019 according to the diffusion equa-212 tion; over this time period it differs from the linear extrapolation of CHAOS-6-x8. 213 Note that this procedure is not sensitive to the specific choice of time window: a 214 model fit over 2018-19 from an initial state in 2018 (not shown) is visually almost 215 indistinguishable from that fit over 2014-19. 216

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Data availability

- ³⁰⁴ The CHAOS-6-x8 and COV-OBS.x1 geomagnetic field models on which this
- ³⁰⁵ study is based can be found at:
- 306 http://www.spacecenter.dk/files/magnetic-models/
- ³⁰⁷ The flow models of Barrois et al. employed here can be found at:
- 308 https://geodyn.univ-grenoble-alpes.fr/

Code availability

All codes are freely available by request from P.W. Livermore (email: p.w.livermore@leeds.ac.uk).

Author contributions

- ³¹² PWL and CCF devised the study; calculations were performed by PWL and MB.
- ³¹³ CCF derived the CHAOS-6-x8 field model. PWL and CCF analysed the geomag-
- netic field and core flow models, interpreted the results and wrote the paper. All
- authors commented on the manuscript.

316 Author information

- The authors declare that they have no competing financial interests.
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Figure 1: Historical movement and predicted future path of the North Magnetic pole in stereographic projection. Solid blue shows the pole's evolution according to the COV-OBS.x1 (1840-1998) and CHAOS-6-x8 (1999-2019) geomagnetic field models, with green circles indicating recent decadal positions; red circles mark in-situ measurements (1831-2007) [13; 4]. The international date line is shown by the dotted black line on the 180° meridian. Predictions (see methods) 2019-2029 are: linear extrapolation from the World Magnetic Model v2 [9] as black, linear extrapolation from CHAOS-6-x8 as magenta, a purely-diffusive model based on fitting geomagnetic secular variation over 2014-2019 in orange [31] and frozen-flux evolution using an ensemble of large-scale flows [20; 21] as white.



Figure 2: A comparison of the structure of the geomagnetic field and the north magnetic pole position in orthographic projection between 2019 (a-c) and 1999 (d-f). (a,d): contours of the radial field on the Earth's surface overlaid with contours of H in turquoise (values [2,4,6,8] μ T) and the north magnetic pole as a red star with its dotted tail showing the path 1840-1999, solid tail 1999-2019. (b,e): as (a,d) but truncated to spherical harmonic degree 6. (c,f): structure of the geomagnetic field to degree 6 on the core-mantle-boundary, shown by contours of radial field overlaid with contours of H in turquoise (values [50,100] μ T).



Figure 3: Experiment demonstrating the effect of elongation of the Canadian CMB flux lobe on the large-scale surface field and pole position. (c) contours of the radial component in 1999 according to CHAOS-6-x8. (a) radial component of a composite field projected into a divergence-free spherical-harmonic representation, comprising the structure in 2019 within the magenta wedge and the structure in 1999 elsewhere; (b) radial field on the CMB, as in (a) but truncated to degree 6, note the similar structure to Fig 2(c) demonstrates that flux lobe elongation explains the change in the Canadian surface patch; (d) radial field on the Earth's surface with the north magnetic pole (red star), whose tail indicates its path since 1999, produced only by changes within the wedge.



Figure 4: Local core surface dynamics around the Canadian flux lobe in stereographic projection. Shown are contours of the radial magnetic field, the north magnetic pole position and path since 1840, flow streamlines with arrows and the wedge within which flux lobe elongation occurs in (a) 1970, (b) 1999 and (c) 2017. The 1970 magnetic field and flow data is from COV-OBS.x1 and the ensemble mean flow of [19; 21]; those from 1999 are from CHAOS-6-x8 and the ensemble mean flow of [19; 21]; those from 2017 are from CHAOS-6-x8 and the ensemble mean of [20; 21]. The inner-tangent cylinder is marked in gold at about 69° N.