

Computational Study of NaVOPO₄ Polymorphs as Cathode Materials for Na-Ion Batteries: Diffusion, Electronic Properties, and Cation-Doping Behavior

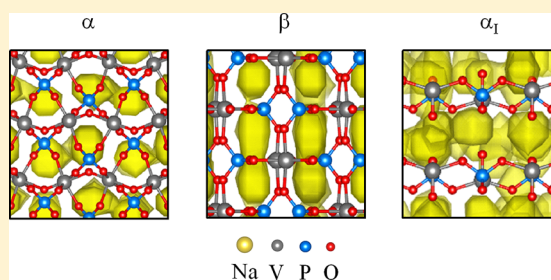
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Supporting Information

ABSTRACT: Rechargeable sodium-ion batteries have gained considerable interest as potential alternatives to lithium-ion batteries, owing to their low cost and the wide abundance of sodium. Phosphate compounds are promising materials for sodium-ion batteries because of their high structural stability. Vanadium phosphates have shown high energy densities as cathode materials, but their Na-ion transport and cation-doping properties are not as yet fully understood. Here, we have combined density functional theory calculations and molecular dynamics techniques to study the diffusion, electronic properties, and cation doping of the α -, β -, and α_1 -NaVOPO₄ polymorphs. The calculated Na-ion activation energies of these compounds (0.3–0.5 eV) are typical for Na-based cathode materials and the simulations predict Na-ion diffusion coefficients of 10⁻¹¹–10⁻¹² cm² s⁻¹. The cell voltage trends show an operating range of 3.1–3.3 V vs Na/Na⁺, with the partial substitution of vanadium by other metals (Al³⁺, Co²⁺, Fe³⁺, Mn⁴⁺, Ni²⁺, or Ti⁴⁺) increasing the cell voltage by up to 0.2–1.0 V vs Na/Na⁺. Our study provides new quantitative insights into the electrochemical behavior of a potentially important class of phosphate cathode materials for sodium-ion batteries.



1. INTRODUCTION

The development of lithium-ion batteries has enabled a host of new technologies, particularly portable electronic devices. In recent years, sodium-ion batteries have begun to receive interest with the aim of developing low-cost and sustainable batteries based on the high abundance and easy accessibility of sodium, especially for grid-scale storage systems for intermittent renewable energy.^{1–5}

Considerable effort has been expended on the exploration of new cathode materials with high reversible capacity, rapid Na insertion/extraction, and cycling durability.^{3,6–8} A large variety of materials, including layered metal oxides, polyanionic compounds, and Prussian blue analogs, have been studied as cathodes for Na-ion batteries.^{3,9} In particular, vanadium phosphate materials, such as Na₃V₂(PO₄)₃, Na₃V₂(PO₄)₂F₃, and NaVPO₄F, show good electrochemical performance and they possess a versatile structure.^{10–12} They are considered promising cathode compounds owing to their high structural stability, long-term cycling, and low volumetric expansion during Na⁺ insertion/extraction.¹³

Song et al. explored monoclinic α -NaVOPO₄ as a cathode for Na-ion batteries.¹⁴ More recently, Manthiram and co-workers synthesized and tested two new NaVOPO₄ polymorphs, i.e., the β and α_1 phases, both of which exhibited a higher potential and reversible capacity than the α phase.^{15,16} The new β and α_1 polymorphs have both been synthesized from the lithium counterparts, via delithiation and sodiation

chemical processes, but it was found that the new phases are thermodynamically less stable than the α phase.

The α_1 phase has the highest ionic conductivity among the three polymorphs, making it a promising cathode for Na-ion batteries, although the Na-ion transport mechanisms and electronic properties of the NaVOPO₄ polymorphs are not yet fully characterized. Li et al. designed a high-energy Na-ion battery based on structured Na₂Ti₃O₇ and layered α_1 -NaVOPO₄ compounds as the anode and cathode materials, respectively.¹⁷ This cell battery showed excellent reversible capacity, rate capability, and cycling stability. Lin et al.¹⁸ published a comparison of VOPO₄ polymorphs investigating their stability and electrochemistry of Li and Na intercalation.

Here, we report the diffusion, electronic properties, and cation doping of the α -, β -, and α_1 -NaVOPO₄ polymorphs studied by an effective combination of ab initio calculations and classical molecular dynamics (MD) simulation techniques. We were able to reproduce the experimental structural parameters of the three polymorphs. The Na-ion transport mechanisms and voltage trends from metal doping were also investigated and the doped structures show an increase in the cell voltage of up to 0.2–1.0 V vs Na/Na⁺. We found that the α_1 phase has the highest Na-ion diffusion coefficient and the

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lowest activation energy for Na-ion migration among the three polymorphs.

2. METHODS

We have employed a combination of ab initio techniques based on density functional theory (DFT) and interatomic potential-based molecular dynamics (MD) simulations, extending our successful work on related battery materials.^{19–25} All DFT calculations were performed using the Vienna ab initio simulation package (VASP).^{26–29} We have used projector-augmented wave pseudopotentials^{30,31} and the Perdew–Burke–Ernzerhof exchange correlation functional revised for solids (PBEsol),³² setting the kinetic energy cut-off at 520 eV. A *k*-point grid of $7 \times 7 \times 7$ was used to converge the forces and energies of the bulk material. The DFT+U methodology was applied to account for the d orbitals of the metal atoms, with effective Hubbard values of $U_{\text{eff}} = U - J = 4.0, 3.3, 4.3, 3.9, 6.0,$ and 4.2 eV ($J = 1$ eV) for V, Co, Fe, Mn, Ni, and Ti, respectively.^{11,33,34} In addition, van der Waals corrections were included, using the DFT-D3 method of Grimme,³⁵ as these have been shown to influence cell voltage calculations in some polyanionic systems.¹⁹

Previous computational studies have shown that such methods are suitable to compute accurate cell voltage trends²⁰ as well as to determine transport and defect properties in Li- and Na-ion batteries.^{36–38} For all compounds, the cell voltage vs Na/Na⁺ of the V⁴⁺/V⁵⁺ redox couple was calculated using the following equation

$$V = E[\text{NaVOPO}_4] - E[\text{VOPO}_4] - \mu[\text{Na}] \quad (1)$$

where $E[\text{NaVOPO}_4]$ and $E[\text{VOPO}_4]$ are the total energies of the NaVOPO₄ and VOPO₄ structures, respectively. The chemical potential of sodium, $\mu[\text{Na}]$, was calculated using metallic sodium, which is the standard practice for cell voltage calculations. We also used eq 1 to compute the cell voltage vs Na/Na⁺ of the NaV_{1-x}M_xOPO₄ doped compounds, where we assumed that the fully desodiated structures (V_{1-x}M_xOPO₄) can be formed.

The MD simulations were performed with the LAMMPS code³⁹ and the calculations were carried out on a large supercell made up of $7 \times 7 \times 7$ unit cells, consisting of 10 976 atoms. The initial configuration of the supercell contained 10% Na vacancies plus corresponding V⁵⁺ species, which were randomly distributed. Pre-equilibrium runs of 4 ps using a time step of 2 fs with the NPT ensemble (constant number of particles, constant pressure, and constant temperature) were first used to obtain stable configurations. Data collection runs were then carried out using the NVT ensemble (constant number of particles, constant volume, and constant temperature) and a time step of 1 fs for long runs of 10 ns, at temperatures in the range of 300–1400 K. The interatomic potentials used in the MD calculations are listed in Table S1. The mean squared displacement (MSD) of the Na ions was computed first to derive the diffusion coefficients (D_{Na}) according to

$$D_{\text{Na}} = \left(\frac{1}{6t} \right) \langle [r(t)]^2 \rangle \quad (2)$$

where t is time and $\langle [r(t)]^2 \rangle$ is the MSD.

3. RESULTS AND DISCUSSION

3.1. Structural and Electronic Analysis. Lii et al. first reported the synthesis and structural characterization of NaVOPO₄.⁴⁰ The magnetic behavior of this compound was described by O'Connor et al. as anti-ferromagnetically coupled $S = 1/2$ one-dimensional (1D) chains⁴¹ with the structure of the α -VOPO₄ polymorph. Vanadyl phosphate (VOPO₄) crystallizes in several different structures, namely as $\alpha/\alpha_1/\alpha_{11}$, β , γ , δ , ϵ , and ω -VOPO₄.^{42–48} So far, only three sodium-containing products have been synthesized: α (monoclinic),⁴⁰ β (orthorhombic),¹⁵ and α_1 (tetragonal)¹⁶ NaVOPO₄.

The α structure of NaVOPO₄ consists of VO₆ octahedral chains running along the *c* axis, linked with PO₄ tetrahedra (Figure 1). The VO₆ octahedra show four almost equal V–O bond distances in the equatorial plane (1.97–2.01 Å), and one short and one long apical V–O distances (1.68 and 2.09 Å, respectively). Three of the four P–O bond distances in the PO₄ tetrahedra are similar (1.56–1.58 Å), whereas the other distance is slightly shorter (1.52 Å). The Na⁺ cations are in the intersections of the VO chains, surrounded by seven O atoms with Na–O distances ranging from 2.25 to 2.92 Å.

In the β phase, distorted VO₆ octahedra form infinite chains along the *a* axis, while the V–O bonds in the *bc* planes are connected via shared corners with four PO₄ tetrahedra (Figure 1). Short (1.64 Å) and long (2.37 Å) V–O distances alternate along the *a* axis to form the vanadyl-type symmetry. The V–O bonds in the equatorial plane are in the range of 1.93–2.06 Å. As in the α phase, three of the P–O bonds in the PO₄ tetrahedra have similar bond lengths (1.55–1.56 Å), with the other one being slightly shorter (1.53 Å). The Na⁺ cations are surrounded by six O atoms with Na–O distances ranging from 2.23 to 2.36 Å.

Finally, the α_1 -NaVOPO₄ structure consists of VOPO₄ sheets stacked along the *c* direction. In the VOPO₄ planes, PO₄ groups and distorted VO₅ polyhedra are alternatively arranged by a corner-sharing oxygen to form [VOPO₄]_∞ chains in the *ab* plane (Figure 1). The VO₅ square-pyramidal groups show four equal V–O distances (1.99 Å) and a short apical vanadyl distance (1.63 Å). They also show a very long sixth V–O distance (3.48 Å). In the case of the PO₄ groups, all of the P–O distances are equal (1.55 Å). The Na cations are located between the VOPO₄ sheets and surrounded by six O atoms with Na–O distances ranging from 2.30 to 2.55 Å.

A comparison between the experimental and computed cell parameters and bond lengths can be found in Table 1 (all bond lengths are given in Table S2). The computed values are within 1% of the experimental values, except in the case of the α_1 phase. In this case, the experimental values are not available for the NaVOPO₄ stoichiometry and are referred to as the α_1 -Na_{0.8}VOPO₄ compound; hence, the computed cell parameters and bond lengths are slightly different from the experimental data. The interlayer distance between the VOPO₄ sheets in the α_1 phase can vary up to 0.6 Å depending on the Na loading.

Turning to the electronic structure, the density of states (DOS) of the α phase is shown in Figure 2. The DOS of the β and α_1 phases, which are similar to the DOS of the α phase, can be found in Figure S1. As the NaVOPO₄ compounds are described as anti-ferromagnetically coupled chains,^{40,41} the compounds have a zero total spin and the DOS are symmetric. The electronic structure corresponds to one unpaired electron per V=O formula unit and the vanadyl chains show short-range anti-ferromagnetic exchange in the crystal lattice.

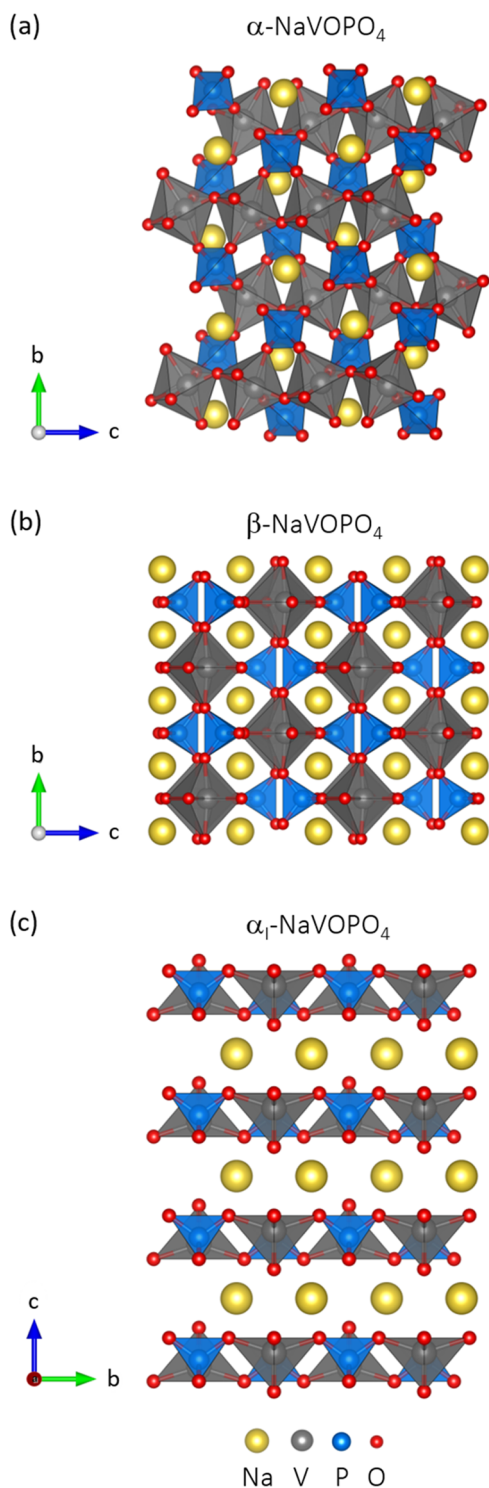


Figure 1. Polyhedral representations of the (a) α -, (b) β -, and (c) α_1 -NaVOPO₄ polymorphs showing VO₆ octahedra (in α and β phases), VO₅ units (in α_1 phase), and PO₄ tetrahedra in all phases.

Although we model the magnetic state as determined experimentally, a detailed analysis of the magnetic properties is not the focus of this study.

The valence band is described mainly by V 3d and O 2p states, whereas the conduction band is mainly made up of V 3d states. The P atoms have a relatively small contribution to both valence and conduction bands. Below the Fermi level, from -0.5 to 0.0 eV, the total DOS shows a similar contribution

from the V 3d and the O 2p states, which correspond to the short V=O bonds. The band gaps of the sodiated compounds are in the range of 1.5 – 2.5 eV, whereas the values of the desodiated compounds are all similar (~ 2 eV). These values are in good agreement with previous DFT+U results of different VOPO₄ polymorphs (1.3 – 2.2 eV).⁴⁹

3.2. Na-ion Diffusion Rates and Pathways. MD simulations were performed over long time scales to examine long-range Na-ion transport properties. Lin et al. computed the migration barriers of Na and Li ions in VOPO₄ polymorphs using the climbing image nudged elastic band method.¹⁸ This practice is well established in the literature,^{50,51} but it fails to capture the long-range dynamics of alkali-ion transport through the structure, which we have sought to elucidate here. From the MSD analysis, we observe that in the α phase, Na-ion diffusion takes place preferably in the a and c directions. In the case of the β phase, the b direction is preferred, in accord with experimental suggestions.¹⁵ Finally, Na-ion diffusion in the α_1 phase does not show any preferred direction, with the three directions being equally probable.

The MD simulations were performed over a range of temperatures (300 – 1400 K), covering a wider range than the operating temperatures of a typical battery and much wider than current experiments. At 300 K, the diffusion coefficients of the α -, β -, and α_1 -NaVOPO₄ polymorphs were calculated as 1.3×10^{-11} , 6.7×10^{-12} , and 5.7×10^{-11} cm² s⁻¹, respectively. To the best of our knowledge, there are no experimental diffusion coefficients of the NaVOPO₄ compounds for direct comparison. Nevertheless, the computed diffusion coefficients are similar to those found in other Na-ion cathode materials, such as Na_xCoO₂ (10^{-11} cm² s⁻¹),⁵² Na_xMnO₂ (10^{-11} cm² s⁻¹),⁵³ and Na₂CoSiO₄ (10^{-12} cm² s⁻¹).⁵⁴ The computed diffusion coefficients as a function of temperature can be used to derive migration activation energies (E_a) from an Arrhenius plot, as shown in Figure 3.

Ion migration activation energies of 0.35 , 0.51 , and 0.32 eV were derived for the α -, β -, and α_1 -NaVOPO₄ polymorphs, respectively. These values indicate favorable Na-ion migration, especially in the α_1 phase. Our findings cannot be compared with the literature as neither experimental activation energies nor conductivity studies of these compounds are available. However, these values are smaller than the activation energy in the related NaTiOPO₄ compound, which is 1.1 ± 0.1 eV in the temperature range of 480 – 800 K.⁵⁵

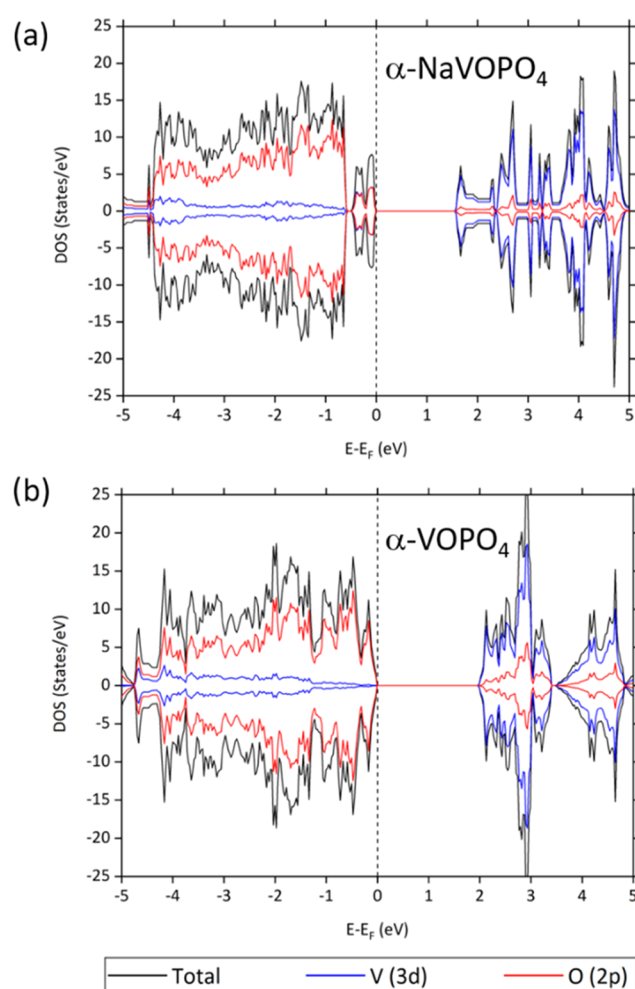
Lin et al.¹⁸ computed the migration barrier of β -NaVOPO₄ as 0.54 eV, which is in good agreement with our computed value of 0.51 eV. However, direct comparison is not appropriate for the α_1 -NaVOPO₄ compound, since Lin et al. computed the migration barriers of three different 1D diffusion pathways, whereas our calculated value is for a three-dimensional (3D) diffusion pathway.

The diffusion trajectories are visualized in Figure 4 by plotting accumulated Na-ion densities, indicating the lattice sites most frequently crossed by Na ions during the MD simulations. These results confirm that Na ions are highly mobile, with all of the Na sites involved in bulk diffusion. In the case of the α phase, the Na diffusion takes place in two-dimensional (2D) channels, mainly in the b and c directions. In the β phase, the Na ions move in the 1D channels along the b axis. Finally, the α_1 phase shows the highest Na mobility, taking place in the 3D channels. Our overall results showing high diffusion rates, low migration energies, and favorable 3D diffusion pathways for α_1 -NaVOPO₄ makes this phase a

Table 1. Comparison of Computed and Experimental Cell Parameters and Bond Lengths in Å of α -, β -, and α_1 -NaVOPO₄ Polymorphs

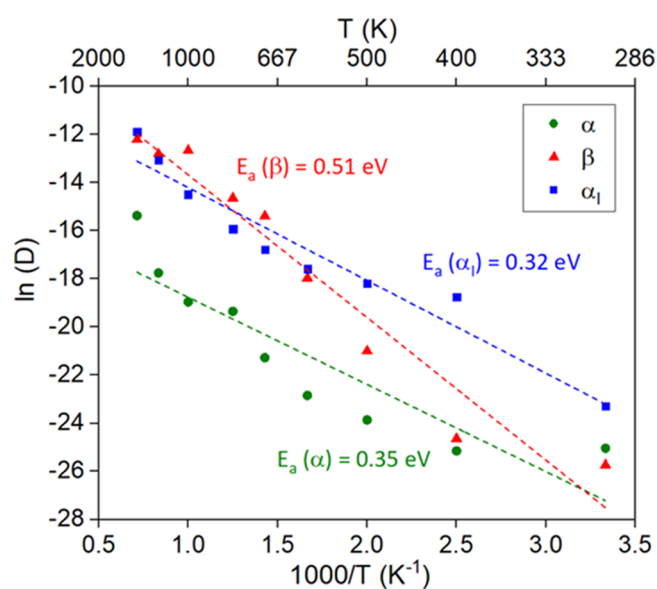
	α -NaVOPO ₄		β -NaVOPO ₄		α_1 -NaVOPO ₄	
	comp.	exp. ¹⁴	comp.	exp. ¹⁵	comp.	exp. ^{16 a}
<i>a</i>	6.509	6.518	7.587	7.539	6.432	6.298
<i>b</i>	8.434	8.446	6.415	6.374	6.432	6.298
<i>c</i>	7.105	7.115	7.670	7.621	5.048	5.119
V–O	1.678	1.681	1.641	1.630	1.638	1.739
	2.000 ^b	2.003 ^b	1.994 ^b	1.981 ^b	1.992 ^b	2.108 ^b
	2.088	2.091	2.370	2.355	3.481	2.936
P–O	1.512	1.514	1.532	1.522	1.545 ^b	
	1.568 ^b	1.570 ^b	1.555 ^b	1.545 ^b		
Na–O	2.446 ^b	2.450 ^b	2.229 ^b	2.284 ^b	2.382 ^b	
symmetry	monoclinic		orthorhombic		tetragonal	
space group	P2 ₁ /C		Pnma		P4/nmm	

^aCell parameters and bond lengths of α_1 -Na_{0.8}VOPO₄ polymorph. The P–O and Na–O distances have not been reported. ^bMean values.

**Figure 2.** Density of states (DOS) of (a) sodiated α -NaVOPO₄ and (b) desodiated α -VOPO₄.

promising Na-ion cathode material. We recognize the stability issues with the α_1 phase, but we consider that our predictions certainly warrant further electrochemical investigation of this promising material.

3.3. Cell Voltage Trends on Cation Doping. DFT+U was used to compute the cell voltage of the α -, β -, and α_1 -NaVOPO₄ polymorphs as well as the doped materials. To carry out the calculations, Na ions were removed from the

**Figure 3.** Arrhenius plot of Na-ion diffusion coefficients vs temperature for NaVOPO₄ polymorphs.

optimized structure to have vacancy concentrations of 0, 25, 50, 75, and 100%, and various vacancy configurations were considered. The voltage was then calculated using eq 1 with the lowest energy configuration. The computed voltages of the α -, β -, and α_1 -NaVOPO₄ polymorphs are 3.3, 3.1, and 3.1 V (vs Na/Na⁺), respectively. These are in good agreement with the experimental values of 3.6, 3.3–3.4, and 3.4 V (vs Na/Na⁺), respectively.^{14–16}

We have also investigated how doping on the vanadium site affects the cell voltage of the NaVOPO₄ polymorphs. The voltage trends of NaV_{1-x}M_xOPO₄ (M = Al³⁺, Co²⁺, Fe³⁺, Mn⁴⁺, Ni²⁺, or Ti⁴⁺) vs Na/Na⁺ with *x* values of 0, 0.25, and 0.50 are depicted in Figure 5. These cations were chosen as they have been used as doping agents for different vanadium phosphate compounds, including Li₃V₂(PO₄)₃ and Na₃V₂(PO₄)₃.^{56–64} The doped materials show higher capacity and capacity retention than the pristine compounds. Also, the addition of the cation dopants has been shown to enhance Li- and Na-ion diffusion, and have a structural stabilization effect.

Our computed cell voltage values of some of the doped structures are above the voltage stability window for organic

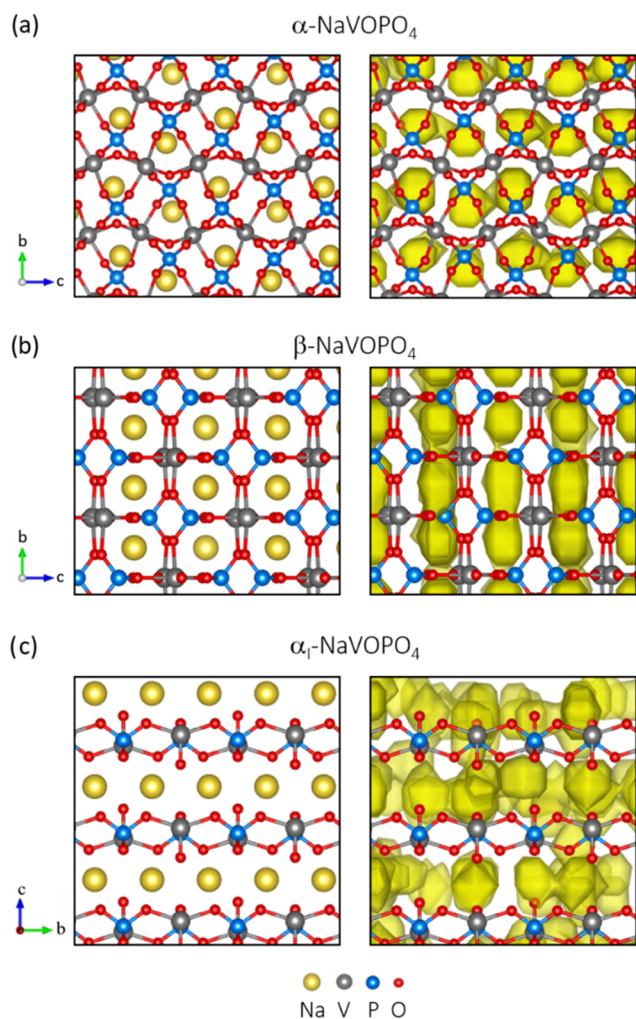


Figure 4. Na density plot from MD calculations at 700 K showing the initial structures (left) and Na diffusion pathways (right) of the (a) α -, (b) β -, and (c) α_1 -NaVOPO₄ polymorph structures. Na-ion density is plotted in yellow.

Na-ion electrolytes (~ 3.5 V).⁶⁵ In the case of the α phase, the Co-, Mn-, and Ti-doped structures, when $x = 0.25$, are the only materials within this electrochemical window. When $x = 0.50$, all of the doped structures have cell voltage values above 3.5 V vs Na/Na⁺. For the β phase, all of the doped structures ($x = 0.25$) are within the stability window, but only Mn- and Ti-doped structures ($x = 0.50$) have voltage values of ~ 3.5 V vs Na/Na⁺. Finally, all of the doped α_1 materials ($x = 0.25$ and 0.50) show computed voltages within the electrochemical stability window. We have also observed that in the doped systems, where the cation has a lower oxidation state than 4+, some of the vanadium centers are oxidized to V⁵⁺ to compensate for the charge. Overall, the Mn⁴⁺ and Ti⁴⁺ cations seem to be the more suitable dopants to increase the cell voltage of the NaVOPO₄ polymorphs within the optimal operating voltage window.

4. CONCLUSIONS

NaVOPO₄ vanadyl phosphates are among the most promising cathode materials for sodium-ion batteries because of their good electrochemical performance. We have studied the diffusion, electronic properties, and cation-doping behavior of the α -, β -, and α_1 -NaVOPO₄ polymorphs. Our fundamental

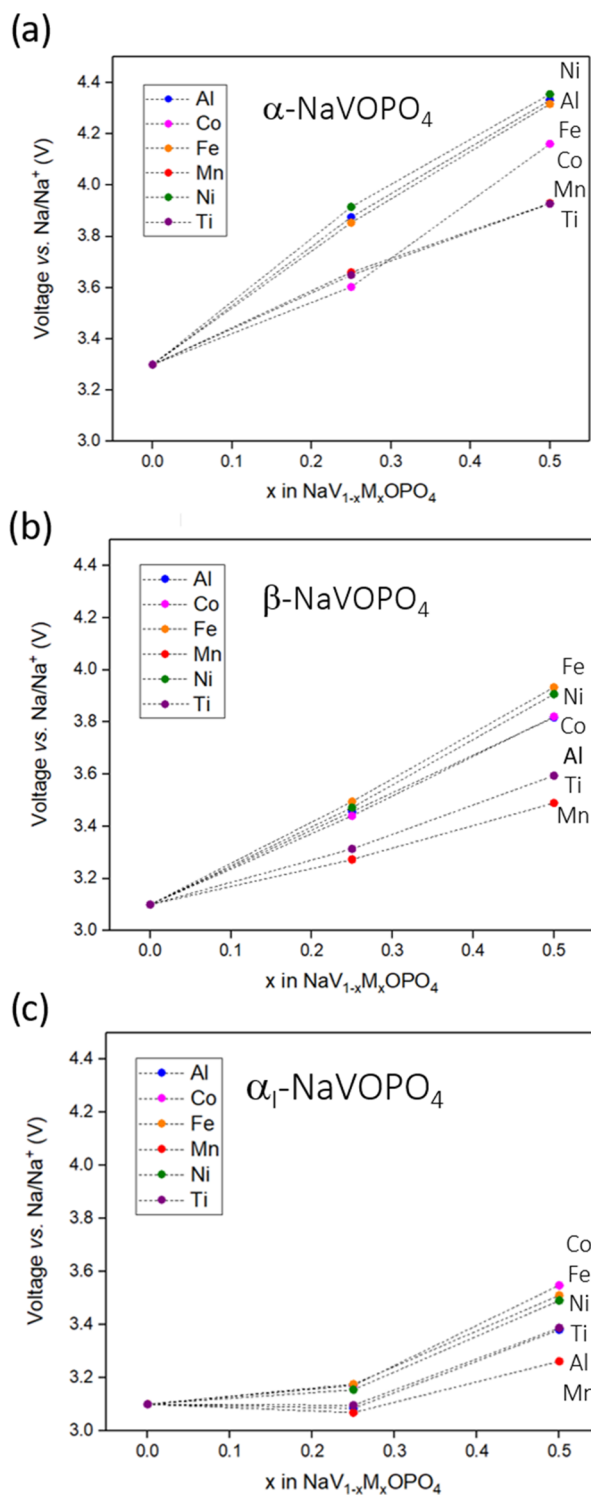


Figure 5. Trends in cell voltage (vs Na/Na⁺) as a function of increasing dopant ($M = \text{Al}^{3+}$, Co^{2+} , Fe^{3+} , Mn^{4+} , Ni^{2+} or Ti^{4+}) concentration on the V site in the (a) α -, (b) β -, and (c) α_1 -NaVOPO₄ polymorphs.

study shows good reproduction of the observed experimental structures. From large-scale MD calculations, we have derived low Na-ion activation energies of 0.3–0.5 eV, and diffusion coefficients (D_{Na}) at 300 K of 10^{-11} – 10^{-12} cm² s⁻¹ for the three NaVOPO₄ polymorphs. From analysis of the migration pathways, the α , β , and α_1 phases show Na-ion diffusion along 2D, 1D, and 3D channels, respectively. Among the three

polymorphs, the α_1 phase has the most favorable Na-ion conductivity, activation energy, and 3D pathways, making it a promising cathode material.

The computed cell voltages of 3.3, 3.1, and 3.1 V vs Na/Na⁺ for the α -, β -, and α_1 -NaVOPO₄ compounds, respectively, agree well with the reported electrochemical data. Cation doping (Al³⁺, Co²⁺, Fe³⁺, Mn⁴⁺, Ni²⁺, and Ti⁴⁺) at the vanadium site is predicted to increase the cell voltage. The Mn- and Ti-doped structures of the α and β phases show an increase in the cell voltage within the electrochemical stability window of current liquid electrolytes. In the case of the α_1 phase, all of the doped structures show cell voltages within the electrochemical stability range. Overall, the fundamental insights presented in this study will aid the improvement of phosphate cathodes for sodium-ion batteries.

■ ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jpcc.8b07797.

Density of states of β and α_1 -(Na)VOPO₄ polymorphs, interatomic potential parameters table, computed and experimental bond lengths of the three polymorphs and polyhedral representation of the doped materials (PDF)

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Notes

The authors declare no competing financial interest.

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■ REFERENCES

- (1) Kundu, D.; Talaie, E.; Duffort, V.; Nazar, L. F. The Emerging Chemistry of Sodium Ion Batteries for Electrochemical Energy Storage. *Angew. Chem., Int. Ed.* **2015**, *54*, 3431–3448.
- (2) Fang, C.; Huang, Y.; Zhang, W.; Han, J.; Deng, Z.; Cao, Y.; Yang, H. Routes to High Energy Cathodes of Sodium-Ion Batteries. *Adv. Energy Mater.* **2016**, *6*, No. 1501727.
- (3) Kim, H.; Kim, H.; Ding, Z.; Lee, M. H.; Lim, K.; Yoon, G.; Kang, K. Recent Progress in Electrode Materials for Sodium-Ion Batteries. *Adv. Energy Mater.* **2016**, *6*, No. 1600943.

(4) Hwang, J.-Y.; Myung, S.-T.; Sun, Y.-K. Sodium-Ion Batteries: Present and Future. *Chem. Soc. Rev.* **2017**, *46*, 3529–3614.

(5) Ni, Q.; Bai, Y.; Wu, F.; Wu, C. Polyanion-Type Electrode Materials for Sodium-Ion Batteries. *Adv. Sci.* **2017**, *4*, No. 1600275.

(6) Yabuuchi, N.; Kubota, K.; Dahbi, M.; Komaba, S. Research Development on Sodium-Ion Batteries. *Chem. Rev.* **2014**, *114*, 11636–11682.

(7) Han, M. H.; Gonzalo, E.; Singh, G.; Rojo, T. A Comprehensive Review of Sodium Layered Oxides: Powerful Cathodes for Na-Ion Batteries. *Energy Environ. Sci.* **2015**, *8*, 81–102.

(8) Zhang, X.; Zhang, Z.; Yao, S.; Chen, A.; Zhao, X.; Zhou, Z. An Effective Method to Screen Sodium-Based Layered Materials for Sodium Ion Batteries. *npj Comput. Mater.* **2018**, *4*, No. 13.

(9) Li, F.; Zhou, Z. Micro/Nanostructured Materials for Sodium Ion Batteries and Capacitors. *Small* **2018**, *14*, No. 1702961.

(10) Lim, S. Y.; Kim, H.; Shakoor, R. A.; Jung, Y.; Choi, J. W. Electrochemical and Thermal Properties of NASICON Structured Na₃V₂(PO₄)₃ as a Sodium Rechargeable Battery Cathode: A Combined Experimental and Theoretical Study. *J. Electrochem. Soc.* **2012**, *159*, A1393–A1397.

(11) Shakoor, R. A.; Seo, D.-H.; Kim, H.; Park, Y.-U.; Kim, J.; Kim, S.-W.; Gwon, H.; Lee, S.; Kang, K. A Combined First Principles and Experimental Study on Na₃V₂(PO₄)₂F₃ for Rechargeable Na Batteries. *J. Mater. Chem.* **2012**, *22*, 20535–20541.

(12) Barker, J.; Saidi, M. Y.; Swoyer, J. L. A Sodium-Ion Cell Based on the Fluorophosphate Compound NaVPO₄F. *Electrochem. Solid-State Lett.* **2003**, *6*, A1–A4.

(13) Fang, Y.; Zhang, J.; Xiao, L.; Ai, X.; Cao, Y.; Yang, H. Phosphate Framework Electrode Materials for Sodium Ion Batteries. *Adv. Sci.* **2017**, *4*, No. 1600392.

(14) Song, J.; Xu, M.; Wang, L.; Goodenough, J. B. Exploration of NaVOPO₄ as a Cathode for a Na-Ion Battery. *Chem. Commun.* **2013**, *49*, 5280–5282.

(15) He, G.; Huq, A.; Kan, W. H.; Manthiram, A. β -NaVOPO₄ Obtained by a Low-Temperature Synthesis Process: A New 3.3 V Cathode for Sodium-Ion Batteries. *Chem. Mater.* **2016**, *28*, 1503–1512.

(16) He, G.; Kan, W. H.; Manthiram, A. A 3.4 V Layered VOPO₄ Cathode for Na-Ion Batteries. *Chem. Mater.* **2016**, *28*, 682–688.

(17) Li, H.; Peng, L.; Zhu, Y.; Chen, D.; Zhang, X.; Yu, G. An Advanced High-Energy Sodium-Ion Full Battery Based on Nanostructured Na₂Ti₃O₇/VOPO₄ Layered Materials. *Energy Environ. Sci.* **2016**, *9*, 3399–3405.

(18) Lin, Y.-C.; Hidalgo, M. F. V.; Chu, I.-H.; Chernova, N. A.; Whittingham, M. S.; Ong, S. P. Comparison of the Polymorphs of VOPO₄ as Multi-Electron Cathodes for Rechargeable Alkali-Ion Batteries. *J. Mater. Chem. A* **2017**, *5*, 17421–17431.

(19) Eames, C.; Clark, J. M.; Rouse, G.; Tarascon, J. M.; Islam, M. S. Lithium Migration Pathways and Van Der Waals Effects in the LiFeSO₄OH Battery Material. *Chem. Mater.* **2014**, *26*, 3672–3678.

(20) Islam, M. S.; Fisher, C. A. J. Lithium and Sodium Battery Cathode Materials. Computational Insights into Voltage, Diffusion and Nanostructural Properties. *Chem. Soc. Rev.* **2014**, *43*, 185–204.

(21) Armstrong, A. R.; Lyness, C.; Panchmatia, P. M.; Islam, M. S.; Bruce, P. G. The Lithium Intercalation Process in the Low-Voltage Lithium Battery Anode Li_{1+x}V_{1-x}O₂. *Nat. Mater.* **2011**, *10*, 223–229.

(22) Yuan, Y.; Zhan, C.; He, K.; Chen, H.; Yao, W.; Sharifi-Asl, S.; Song, B.; Yang, Z.; Nie, A.; Luo, X.; et al. The Influence of Large Cations on the Electrochemical Properties of Tunnel-Structured Metal Oxides. *Nat. Commun.* **2016**, *7*, No. 13374.

(23) Clark, J. M.; Nishimura, S.; Yamada, A.; Islam, M. S. High-Voltage Pyrophosphate Cathode: Insights into Local Structure and Lithium-Diffusion Pathways. *Angew. Chem., Int. Ed.* **2012**, *51*, 13149–13153.

(24) Dawson, J. A.; Canepa, P.; Famprikis, T.; Masquelier, C.; Islam, M. S. Atomic-Scale Influence of Grain Boundaries on Li-Ion Conduction in Solid Electrolytes for All-Solid-State Batteries. *J. Am. Chem. Soc.* **2018**, *140*, 362–368.

- (25) Dawson, J. A.; Attari, T. S.; Chen, H.; Emge, S. P.; Johnston, K. E.; Islam, M. S. Elucidating Lithium-Ion and Proton Dynamics in Anti-Perovskite Solid Electrolytes. *Energy Environ. Sci.* **2018**, *11*, 2993–3002.
- (26) Kresse, G.; Hafner, J. Ab Initio Molecular Dynamics for Liquid Metals. *Phys. Rev. B* **1993**, *47*, 558–561.
- (27) Kresse, G.; Hafner, J. Ab Initio Molecular-Dynamics Simulation of the Liquid-Metal-Amorphous-Semiconductor Transition in Germanium. *Phys. Rev. B* **1994**, *49*, 14251–14269.
- (28) Kresse, G.; Furthmüller, J. Efficiency of Ab Initio Total Energy Calculations for Metals and Semiconductors Using a Plane-Wave Basis Set. *Comput. Mater. Sci.* **1996**, *6*, 15–50.
- (29) Kresse, G.; Furthmüller, J. Efficient Iterative Schemes for Ab Initio Total-Energy Calculations Using a Plane-Wave Basis Set. *Phys. Rev. B* **1996**, *54*, 11169–11186.
- (30) Blöchl, P. E. Projector Augmented-Wave Method. *Phys. Rev. B* **1994**, *50*, 17953–17979.
- (31) Kresse, G.; Joubert, D. From Ultrasoft Pseudopotentials to the Projector Augmented-Wave Method. *Phys. Rev. B* **1999**, *59*, 1758–1775.
- (32) Perdew, J. P.; Ruzsinszky, A.; Csonka, G. I.; Vydrov, O. A.; Scuseria, G. E.; Constantin, L. A.; Zhou, X.; Burke, K. Restoring the Density-Gradient Expansion for Exchange in Solids and Surfaces. *Phys. Rev. Lett.* **2008**, *100*, No. 136406.
- (33) Tsirlin, A. A.; Nath, R.; Abakumov, A. M.; Furukawa, Y.; Johnston, D. C.; Hemmida, M.; Krug von Nidda, H.-A.; Loidl, A.; Geibel, C.; Rosner, H. Phase Separation and Frustrated Square Lattice Magnetism of $\text{Na}_{1-x}\text{VOPO}_4\text{F}_{0.5}$. *Phys. Rev. B* **2011**, *84*, No. 014429.
- (34) Heath, J.; Chen, H.; Islam, M. S. MgFeSiO_4 as a Potential Cathode Material for Magnesium Batteries: Ion Diffusion Rates and Voltage Trends. *J. Mater. Chem. A* **2017**, *5*, 13161–13167.
- (35) Grimme, S.; Antony, J.; Ehrlich, S.; Krieg, H. A Consistent and Accurate Ab Initio Parametrization of Density Functional Dispersion Correction (DFT-D) for the 94 Elements H-Pu. *J. Chem. Phys.* **2010**, *132*, No. 154104.
- (36) Deng, Y.; Eames, C.; Nguyen, L. H. B.; Pecher, O.; Griffith, K. J.; Courty, M.; Fleutot, B.; Chotard, J.-N.; Grey, C. P.; Islam, M. S.; et al. Crystal Structures, Local Atomic Environments, and Ion Diffusion Mechanisms of Scandium-Substituted Sodium Superionic Conductor (NASICON) Solid Electrolytes. *Chem. Mater.* **2018**, *30*, 2618–2630.
- (37) Deng, Y.; Eames, C.; Chotard, J.-N.; Lalère, F.; Seznec, V.; Emge, S.; Pecher, O.; Grey, C. P.; Masquelier, C.; Islam, M. S. Structural and Mechanistic Insights into Fast Lithium-Ion Conduction in $\text{Li}_4\text{SiO}_4\text{--Li}_3\text{PO}_4$ Solid Electrolytes. *J. Am. Chem. Soc.* **2015**, *137*, 9136–9145.
- (38) Fisher, C. A. J.; Kuganathan, N.; Islam, M. S. Defect Chemistry and Lithium-Ion Migration in Polymorphs of the Cathode Material $\text{Li}_2\text{MnSiO}_4$. *J. Mater. Chem. A* **2013**, *1*, 4207–4214.
- (39) Plimpton, S. Fast Parallel Algorithms for Short-Range Molecular Dynamics. *J. Comput. Phys.* **1995**, *117*, 1–19.
- (40) Lii, K. H.; Li, C. H.; Chen, T. M.; Wang, S. L. Synthesis and Structural Characterization of Sodium Vanadyl(IV) Orthophosphate NaVOPO_4 . *Z. Kristallogr. - Cryst. Mater.* **1991**, *197*, 67–73.
- (41) O'Connor, C. J.; Soghomonian, V.; Haushalter, R. C.; Wang, Z.; Zubieta, J. One-Dimensional Antiferromagnetic Behavior in AVOPO_4 (A = NH_4 , Na) Prepared from Hydrothermal Conditions. *J. Appl. Phys.* **1994**, *75*, 5859–5861.
- (42) Amorós, P.; Marcos, M. D.; Roca, M.; Alamo, J.; Beltrán-Porter, A.; Beltrán-Porter, D. Crystal Structure of a New Polymorph in the V–P–O System: Is $\omega\text{-VOPO}_4$ a Dynamically Stabilised Metastable Network? *J. Phys. Chem. Solids* **2001**, *62*, 1393–1399.
- (43) Girgsdies, F.; Schneider, M.; Brückner, A.; Ressler, T.; Schlögl, R. The Crystal Structure of $\delta\text{-VOPO}_4$ and Its Relationship to $\omega\text{-VOPO}_4$. *Solid State Sci.* **2009**, *11*, 1258–1264.
- (44) Bordes, E. Crystallochemistry of V–P–O Phases and Application to Catalysis. *Catal. Today* **1987**, *1*, 499–526.
- (45) Girgsdies, F.; Dong, W.-S.; Bartley, J. K.; Hutchings, G. J.; Schlögl, R.; Ressler, T. The Crystal Structure of $\epsilon\text{-VOPO}_4$. *Solid State Sci.* **2006**, *8*, 807–812.
- (46) Dupré, N.; Wallez, G.; Gaubicher, J.; Quarton, M. Phase Transition Induced by Lithium Insertion in $\alpha\text{-I}$ and $\alpha\text{-II-VOPO}_4$. *J. Solid State Chem.* **2004**, *177*, 2896–2902.
- (47) Dupré, N.; Gaubicher, J.; Le Mercier, T.; Wallez, G.; Angenault, J.; Quarton, M. Positive Electrode Materials for Lithium Batteries Based on VOPO_4 . *Solid State Ionics* **2001**, *140*, 209–221.
- (48) Lim, S. C.; Vaughey, J. T.; Harrison, W. T. A.; Dussack, L. L.; Jacobson, A. J.; Johnson, J. W. Redox Transformations of Simple Vanadium Phosphates: The Synthesis of $\epsilon\text{-VOPO}_4$. *Solid State Ionics* **1996**, *84*, 219–226.
- (49) Sun, W.; Du, J. Structural Stability, Electronic and Thermodynamic Properties of VOPO_4 Polymorphs from DFT+U Calculations. *Comput. Mater. Sci.* **2017**, *126*, 326–335.
- (50) Mueller, T.; Hautier, G.; Jain, A.; Ceder, G. Evaluation of Favorable-Structured Cathode Materials for Lithium-Ion Batteries Using High-Throughput Computing. *Chem. Mater.* **2011**, *23*, 3854–3862.
- (51) Matts, I. L.; Dacek, S.; Pietrzak, T. K.; Malik, R.; Ceder, G. Explaining Performance-Limiting Mechanisms in Fluorophosphate Na-Ion Battery Cathodes through Inactive Transition-Metal Mixing and First-Principles Mobility Calculations. *Chem. Mater.* **2015**, *27*, 6008–6015.
- (52) Shibata, T.; Kobayashi, W.; Moritomo, Y. Sodium Ion Diffusion in Layered Na_xCoO_2 . *Appl. Phys. Express* **2013**, *6*, No. 097101.
- (53) Shibata, T.; Kobayashi, W.; Moritomo, Y. Sodium Ion Diffusion in Layered Na_xMnO_2 ($0.49 \leq x \leq 0.75$): Comparison with Na_xCoO_2 . *Appl. Phys. Express* **2014**, *7*, No. 067101.
- (54) Treacher, J. C.; Wood, S. M.; Islam, M. S.; Kendrick, E. $\text{Na}_2\text{CoSiO}_4$ as a Cathode Material for Sodium-Ion Batteries: Structure, Electrochemistry and Diffusion Pathways. *Phys. Chem. Chem. Phys.* **2016**, *18*, 32744–32752.
- (55) Geifman, I. N.; Nagorniy, P. G.; Rotenfeld, M. V. EPR of V^{4+} in Lithium (Sodium) and Titanium Oxyphosphate and Superionic Conductivity of These Single Crystals. *Ferroelectrics* **1997**, *192*, 87–91.
- (56) Ren, M.; Zhou, Z.; Li, Y.; Gao, X. P.; Yan, J. Preparation and Electrochemical Studies of Fe-Doped $\text{Li}_3\text{V}_2(\text{PO}_4)_3$ Cathode Materials for Lithium-Ion Batteries. *J. Power Sources* **2006**, *162*, 1357–1362.
- (57) Kuang, Q.; Zhao, Y.; An, X.; Liu, J.; Dong, Y.; Chen, L. Synthesis and Electrochemical Properties of Co-Doped $\text{Li}_3\text{V}_2(\text{PO}_4)_3$ Cathode Materials for Lithium-Ion Batteries. *Electrochim. Acta* **2010**, *55*, 1575–1581.
- (58) Deng, C.; Zhang, S.; Yang, S. Y.; Gao, Y.; Wu, B.; Ma, L.; Fu, B. L.; Wu, Q.; Liu, F. L. Effects of Ti and Mg Codoping on the Electrochemical Performance of $\text{Li}_3\text{V}_2(\text{PO}_4)_3$ Cathode Material for Lithium-Ion Batteries. *J. Phys. Chem. C* **2011**, *115*, 15048–15056.
- (59) Zhang, Y.; Huo, Q.; Lv, Y.; Wang, L.; Zhang, A.; Song, Y.; Li, G.; Gao, H.; Xia, T.; Dong, H. Effects of Nickel-Doped Lithium Vanadium Phosphate on the Performance of Lithium-Ion Batteries. *J. Alloys Compd.* **2012**, *542*, 187–191.
- (60) Zhang, L.-L.; Liang, G.; Peng, G.; Huang, Y.-H.; Wang, L.; Qie, L.; Croft, M. C.; Ignatov, A.; Goodenough, J. B. Insight into Fe Incorporation in $\text{Li}_3\text{V}_2(\text{PO}_4)_3/\text{C}$ Cathode Material. *J. Electrochem. Soc.* **2012**, *159*, A1573–A1578.
- (61) Tao, D.; Wang, S.; Liu, Y.; Dai, Y.; Yu, J.; Lei, X. Lithium Vanadium Phosphate as Cathode Material for Lithium Ion Batteries. *Ionics* **2015**, *21*, 1201–1239.
- (62) Lai, C.; Chen, Z.; Zhou, H.; Lu, Y.; Li, H. Mn-Doped $\text{Li}_3\text{V}_2(\text{PO}_4)_3$ Nanocrystal with Enhanced Electrochemical Properties Based on Aerosol Synthesis Method. *J. Mater. Sci.* **2015**, *50*, 3075–3082.
- (63) Sun, H.-B.; Zhang, L.-L.; Yang, X.-L.; Liang, G.; Li, Z. Investigation of Co-Incorporated Pristine and Fe-Doped $\text{Li}_3\text{V}_2(\text{PO}_4)_3$ Cathode Materials for Lithium-Ion Batteries. *Dalton Trans.* **2016**, *45*, 15317–15325.

(64) Zhang, B.; Chen, H.; Tong, H.; Wang, X.; Zheng, J.; Yu, W.; Zhang, J.; Li, J.; Zhang, W. Synthesis and Electrochemical Performance of Ni Doped $\text{Na}_3\text{V}_2(\text{PO}_4)_3/\text{C}$ Cathode Materials for Sodium-Ion Batteries. *J. Alloys Compd.* **2017**, *728*, 976–983.

(65) Ponrouch, A.; Dedryvere, R.; Monti, D.; Demet, A. E.; Ateba Mba, J. M.; Croguennec, L.; Masquelier, C.; Johansson, P.; Palacin, M. R. Towards High Energy Density Sodium Ion Batteries through Electrolyte Optimization. *Energy Environ. Sci.* **2013**, *6*, 2361–2369.