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Article

# Intra-MRI Extraction of Diagnostic Electrocardiograms Using Carotid Magnetohydrodynamic Voltages

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**Abstract:** The electrocardiogram (ECG) is commonly utilized for patient monitoring during magnetic resonance imaging (MRI) despite known magnetohydrodynamic voltage (VMHD) overlays, which often eclipse the true sinus rhythm and render the signal to be non-diagnostic. This can complicate MRI gating and at-risk patient monitoring, causing alternative low-fidelity signals to become preferred. We aimed to develop a method of isolating the true sinus rhythm from VMHD in order to enable the use of high-fidelity ECGs during MRI procedures. Twelve-lead ECGs were acquired in two healthy volunteers ( $n = 2$ ) in a 3T MRI scanner, while a secondary single lead monitor was positioned across the left common carotid artery to directly record VMHD while cancelling out the true sinus rhythm. Carotid MHD was used to adaptively train a least mean squares filter to update a 12-lead ECG VMHD template and produce: (1) clean 12-lead ECGs and (2) an accurate stroke volume (SV) estimate. The adaptive filtering method was shown to reduce VMHD in 12-lead ECGs. This was demonstrated by an average cross-correlation of 0.81 across all ECG leads calculated between filtered ECG taken inside the MRI scanner and the ECG taken outside the MRI scanner. Residual noise formed <5% of the R-wave amplitude. Additionally, the method required only a short training phase. A method to extract real sinus rhythm beats from intra-MRI 12-lead ECGs was presented and shown to provide accurate dynamic measurements of induced VMHD using flow in the carotid artery as a source of dynamic feedback.

**Keywords:** electrocardiogram; magnetohydrodynamic; physiological monitoring; MRI

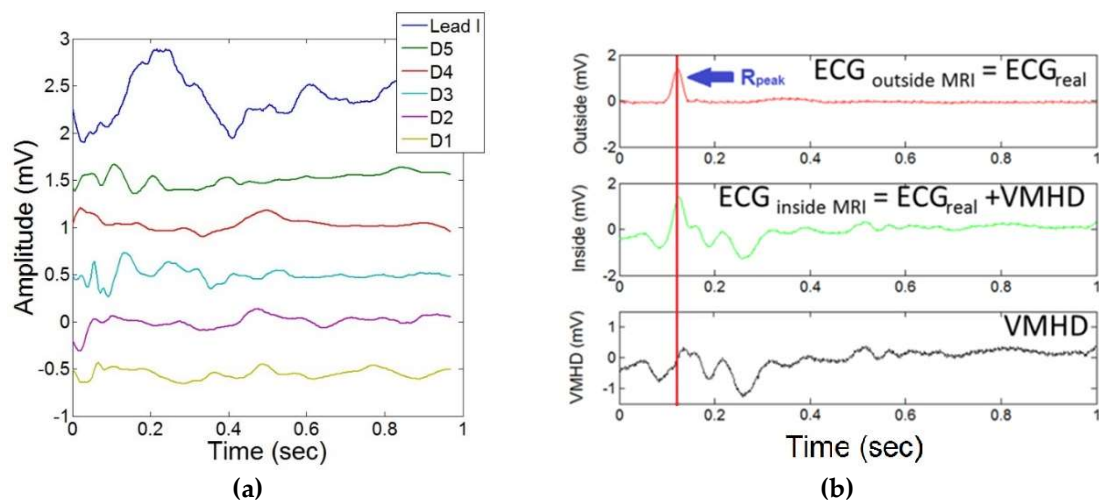
## 1. Introduction

The electrocardiogram (ECG), while considered to be a standard in the monitoring of patient heart activity, is known to be of non-diagnostic quality in the isocenter of a magnetic resonance imaging (MRI) scanner [1]. This causes a great level of difficulty in the synchronization of cardiac activity with the MRI scanner during cardiac cine acquisition using QRS complex detection techniques, and in patient monitoring during MRI procedures and guided interventions, especially in the case of high-risk patients such as those with histories of ischemia or stroke [2–5].

Conventional ECG monitoring systems and advanced signal processing techniques have been developed to acquire ECG traces in the presence of gradient artifacts that may occur during MRI scanning procedures [5,6]. Despite the prevention of voltages related to MRI gradient ramp signal induction, further ECG distortion is known to occur due to a magnetohydrodynamic (MHD) effect generated by interactions between the static magnetic field of the MRI ( $B_0$ ) and blood plasma electrolytes ejected into the aortic arch during early systole [1,3,5,7–11].

In an effort to improve the success of cardiac cine acquisition, techniques for QRS complex detection have been developed and validated with MHD voltages (VMHD) superimposed upon ECG traces, such as the 3DQRS method and techniques based in the vectorcardiography (VCG) frame of reference [2], whereas the 12-lead ECG is represented as a dipole moment in the heart [12].

These methods allow for more effective cardiac gating, but they do not allow for separation of the true ECG ( $ECG_{real}$ ) from VMHD. Several studies have been performed using independent component analysis (ICA), which has demonstrated some success despite being limited through the relatively small number of discrete noise sources considered in the model and the use of simulated VMHD [13–15]. Preliminary studies have been performed to quantify all contributions to the net recorded intra-MRI signal through dictionary learning for sparse approximations (Figure 1a) [16,17]. However, results from this approach have presented difficulties in filter training for  $ECG_{real}$  extraction. The conventional method of  $ECG_{real}$  extraction involves the subtraction of ECGs recorded inside the MRI from those recorded outside the MRI (Figure 1b) [18]. This method is flawed because it is based on the assumption that  $ECG_{real}$  does not vary once the subject is placed inside the MRI, which is not necessarily the case.



**Figure 1.** Conventional methods of  $ECG_{real}$  extraction during intra-MRI ECG acquisition. (a) Sparse-encoded dictionary learning method for separation of contributions to the net magnetohydrodynamic (MHD) effect (blue line) by dictionary elements (D1–D5) in a single ECG lead (lead I): contributions are attributed to flow along the aortic arch and in peripheral vasculature. (b) Performance of MHD subtraction technique using a constant  $ECG_{real}$  template for MHD-ECG separation during 12-lead ECG data acquisition inside the MRI bore, which does not account for variations in  $ECG_{real}$ .

This study proposes a new methodology for extraction of  $ECG_{real}$  from recordings obtained inside the MRI, improving upon a method of adaptive filtering using a least means square (LMS) implementation. The proposed method utilizes a dynamic source of pure MHD to train adaptive filters and update a 12-lead ECG MHD template to perform  $ECG_{real}$  extraction rather than relying entirely on initial training coefficients without additional feedback. In addition, the training sequence only requires the acquisition of one dataset outside of the MRI bore (head-in), as opposed to prior studies which require two datasets (feet-in and head-in) [5,10], potentially halving the time required for training. This will allow for an increased level of accuracy in  $ECG_{real}$  extraction and estimation of MHD-derived metrics in real time [19].

## 2. Materials and Methods

### 2.1. Study Population

The study was conducted using data acquired from two healthy volunteers during exercise stress testing ( $n = 2$ ) in a Siemens Skyra 3T MRI (Siemens AG, Berlin, Germany). Informed consent was obtained from each subject as per Institutional Review Board standards.

### 2.2. Data Acquisition

Data was recorded to establish a baseline with each subject supine on the scanner table outside of the MRI bore. Each subject was then inserted head-first into the MRI bore until the heart was at the isocenter of the scanner. Twelve-lead ECG traces were acquired during 20-second breath-holds using an ECG recorder modified to be MRI-compatible [5], and a secondary monitor was used to acquire single lead bipolar VMHD signals with approximately 4-inch lead spacing from the subject in the left common carotid artery. Phase contrast MRI (PCMR) cines were similarly acquired in each subject during exercise stress testing in the ascending aorta and in the common carotid artery at rest and during exercise stress to evaluate the relationship between induced VMHD and blood flow in both the ascending aorta and the left common carotid artery. All PCMR cines were obtained with the following parameters: VENC: 150 cm/s; TR/TE/flip: 37.00 ms/4.00 ms/15°; field-of-view: 300 mm by 243 mm; slice thickness: 3 mm.

#### 2.2.1. Correlation between Aortic and Carotid MHD

In order to select the proper source of dynamic feedback for the system, the correlation was quantified between induced aortic VMHD extracted from 12-lead ECGs and four MHD sources using a single bipolar lead at the surface of the human body: (1) left common carotid artery (Left-Right and Superior-Inferior lead placement); (2) left femoral artery; (3) across the chest; and the (4) axillary artery. All ECG recordings were acquired inside a 3T MRI. Correlation between extracted MHD from 12-lead ECGs recorded inside the MRI and each source was computed and used to determine the optimal source of intra-MRI dynamic feedback. Furthermore, average flow was quantified in the ascending aorta and the carotid artery using conventional PCMR during exercise stress testing to predict induced VMHD based on superimposing an MHD term on 12-lead ECG traces acquired outside of the MRI bore, whereas MRI derived flow ( $q$ ) and a unique proportionality constant ( $\alpha_i$ ) for each lead ( $i = 1:12$ ) were used to predict induced VMHD which occurs in 12-lead ECG (Equation (1)) [18].

$$VMHD = \alpha_i B_0 q, \text{ for leads } i = 1 : 12. \quad (1)$$

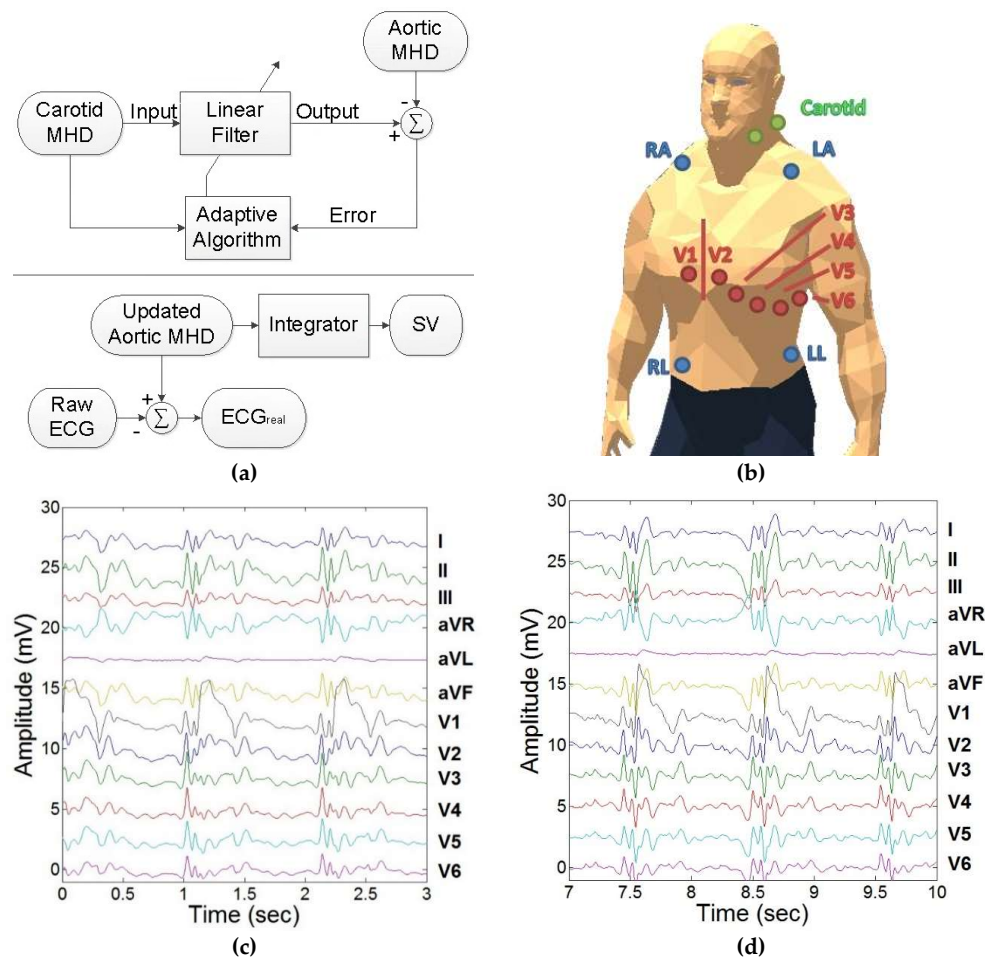
Predicted VMHD values based on MRI-derived blood flow and actual VMHD measured from body surface electrodes were analyzed statistically to justify usage of carotid MHD as the dynamic feedback term.

#### 2.2.2. Adaptive Filter Training

In order to properly utilize the dynamic feedback provided from the carotid MHD, twelve adaptive LMS filters were trained (length, step size) to update the morphology of the carotid MHD to match the morphology of VMHD obtained from 12-lead ECGs (aortic MHD). An aortic MHD template was obtained from the subtraction of 12-lead ECGs obtained inside and outside of the MRI bore. The aortic MHD template obtained at the baseline heart rate was used to update the morphology of carotid MHD (Figure 2a (top)). Carotid MHD was phase compensated to match VMHD obtained from the 12-lead ECG (Figure 2b), and input into an LMS adaptive filter to train the LMS adaptive filter coefficients to minimize the least mean squares error between the two signals. The dynamic feedback generated from the carotid MHD allows for the updated 12-lead aortic MHD to respond more quickly to changes in cardiac activity and reduce error associated with variations in heartbeats.

Following the initial training of the LMS filter coefficients, the aortic MHD template can be updated in real time (Figure 2c,d) and then used to extract  $ECG_{real}$  from the 12-lead ECG recordings obtained in real time inside the MRI bore, and to obtain a more accurate estimate of MHD-derived metrics as previously demonstrated for stroke volume (SV) estimation (Figure 2a (bottom)) [11,19].

To evaluate the proposed method, a twelve-lead ECG was acquired inside the MRI bore and  $ECG_{real}$  extraction was performed. Then a twelve-lead ECG was acquired outside the MRI bore to set the “gold standard.” The correlation was determined between the filtered ECG obtained inside the MRI bore and the unfiltered ECG obtained outside the MRI bore.



**Figure 2.** Development of a dynamic feedback method for higher accuracy real-time 12-lead ECG monitoring and estimation of MHD-derived SV inside the MRI bore. (a) (Top) Adaptive filtering method to morph the carotid artery MHD trace into the aortic MHD trace. (Bottom)  $ECG_{real}$  and SV estimation derived from aortic MHD developed from carotid MHD. (b) Single bipolar carotid lead and 12-lead ECG placement. (c) 12-lead ECG acquired inside the 3T MRI. Each lead contains  $ECG_{real}$  and induced MHD voltage (VMHD) components. (d) Updating the morphology of carotid MHD to match aortic MHD using trained adaptive least means square (LMS) filters as acquired in 12-lead ECGs at 3T.

### 2.2.3. Evaluation during Exercise Stress Testing

In order to evaluate the efficacy of the proposed methodology of dynamic physiological feedback, a series of exercise stress tests were performed in each subject. Following the training stage, subjects were positioned head-first into the bore of the MRI, and baseline scans of the aortic arch and the carotid artery were performed. Three datasets were acquired at varying levels of cardiac activity: (1) baseline; (2) elevated; and (3) return to baseline. An MRI-compatible exercise band was used to elevate each

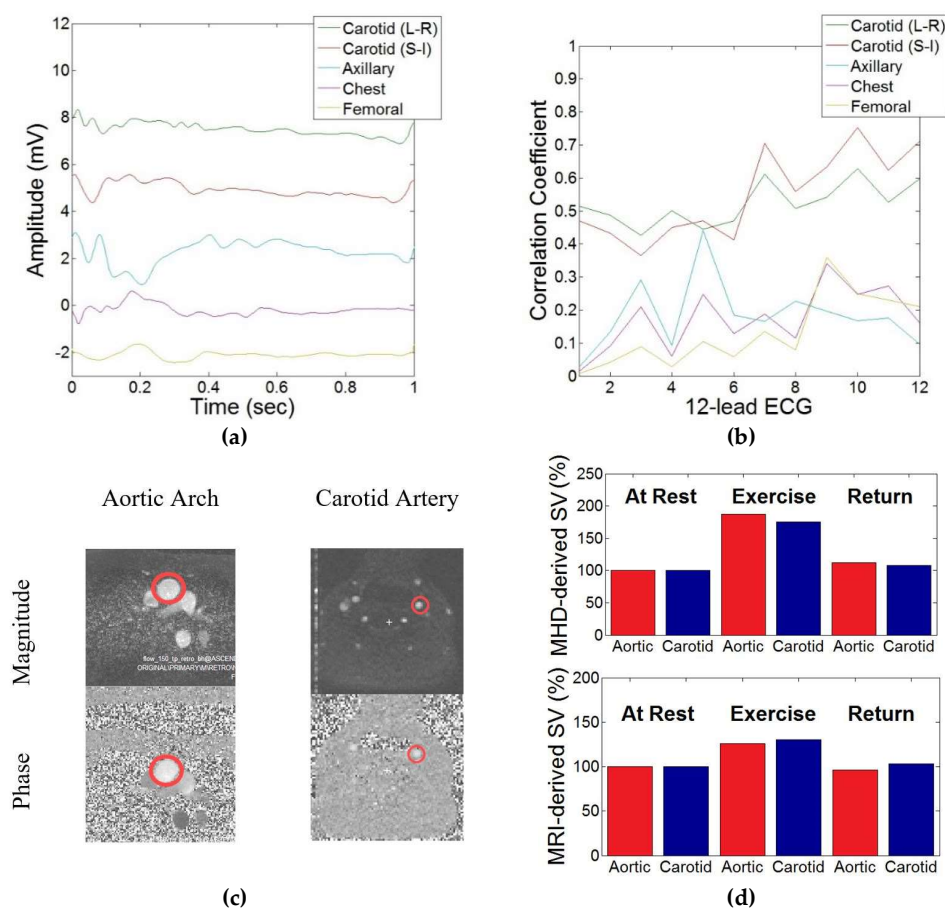


subject’s heart rate by 50%, at which point data collection was performed. A period of 30 min after the induced stress was allowed for the subject to return to baseline heart rate. Extraction of  $ECG_{real}$  was performed on the dataset during the period of exercise stress testing, and a Pearson’s ranked correlation coefficient was calculated to determine efficacy of  $ECG_{real}$  extraction.

### 3. Results

#### 3.1. Correlation between Aortic and Carotidal MHD

Figure 3a shows the VMHD obtained from single lead MHD sources acquired from carotidal (Left-Right and Superior-Inferior lead placements), femoral, chest, and axillary arterial vasculature. The correlations between the VMHD from each single lead MHD source and the VMHD from the 12-lead ECG are plotted in Figure 3b. The conventional PCMR scans of the ascending aorta and the common carotid artery obtained during exercise stress testing are displayed in Figure 3c.



**Figure 3.** Demonstration of correlation between induced MHD in the aortic arch and the common carotid artery in the selection of a source of dynamic system feedback. (a) Induced MHD voltages obtained from peripheral vasculature. (b) Cross-correlation index obtained between each peripheral vasculature MHD source and MHD extracted from each lead in the 12-lead ECG. On the x-axis, the numbers 1–12 represent the 12 leads used in standard 12-lead ECG in the following order: I, II, III, aVR, aVL, aVF, V1, V2, V3, V4, V5, and V6. This lead numbering system is defined in Table 1. (c) Phase contrast MR (PCMR) transverse plane images of the aortic arch and left common carotid artery used to estimate systolic magnitude (top) and phase (bottom). (d) MHD (top) and flow (bottom) in the aortic arch and the common carotid artery during exercise stress testing, illustrating close relationship between flow in the vessels.

Extracted flow and VMHD from the carotid artery and the aortic arch were each shown to have a similar increase during exercise stress testing (Figure 3d). MRI-derived flow showed a lower percent increase in SV as compared to MHD-derived flow, which was attributed to the increased acquisition time required by PCMR scanning as opposed to the real-time beat-to-beat estimation provided using VMHD.

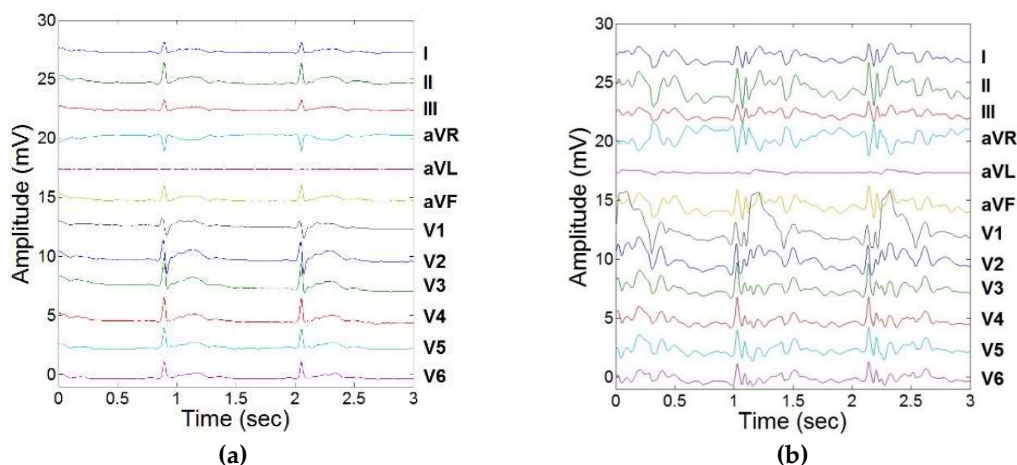
Cross-correlation coefficients between MHD obtained from the left common carotid artery and the 12-lead ECG maintained a mean coefficient greater than each alternate peripheral vasculature source, with a minimized standard deviation in correlation coefficients in the Left-Right lead placement as opposed to the Superior-Inferior lead placement (Table 1). The first column in Table 1 defines the numbering system used in this paper for the 12 leads in standard 12-lead ECG.

**Table 1.** Correlation coefficients obtained between 12-lead MHD and peripheral vasculature.

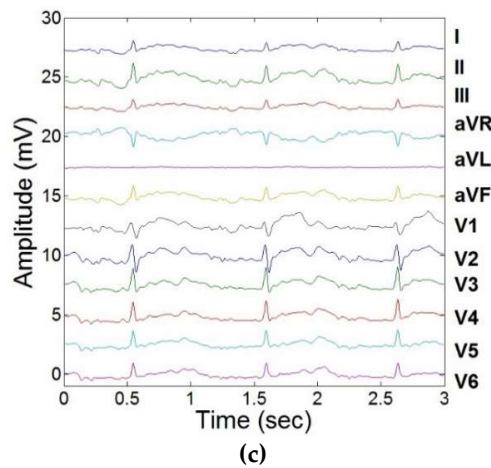
Lead Number	Lead Name	Carotid (L-R)	Carotid (S-I)	Axillary	Chest	Femoral
1	I	0.51	0.47	0.03	0.01	0.01
2	II	0.49	0.43	0.13	0.09	0.04
3	III	0.43	0.37	0.29	0.21	0.09
4	aVR	0.50	0.45	0.09	0.06	0.03
5	aVL	0.45	0.47	0.44	0.25	0.10
6	aVF	0.47	0.41	0.18	0.13	0.06
7	V1	0.61	0.70	0.17	0.19	0.14
8	V2	0.51	0.56	0.23	0.11	0.08
9	V3	0.54	0.63	0.20	0.34	0.36
10	V4	0.63	0.75	0.17	0.25	0.25
11	V5	0.53	0.62	0.18	0.27	0.23
12	V6	0.60	0.71	0.10	0.16	0.21
<b>Mean</b>		0.52	0.55	0.18	0.17	0.13
<b>Standard Deviation</b>		0.06	0.13	0.11	0.10	0.11

### 3.2. Adaptive Filter Training

Figure 4 presents the ECGs acquired to evaluate the ECG<sub>real</sub> extraction method. The unfiltered ECG acquired outside the MRI bore is shown in Figure 4a and the unfiltered ECG acquired inside the MRI bore is shown in Figure 4b. ECG<sub>real</sub> was then extracted from the ECG acquired inside the MRI bore with the filtering technique, and the result is shown in Figure 4c.



**Figure 4.** Cont.



**Figure 4.** Training of LMS adaptive filters to remove induced MHD signals, and response to real-time feedback from carotidal MHD. (a) 12-lead ECG acquired outside the MRI bore. (b) 12-lead ECG acquired inside the 3T MRI. (c) Extracted 12-lead ECG<sub>real</sub> using adaptive filtering and carotidal feedback.

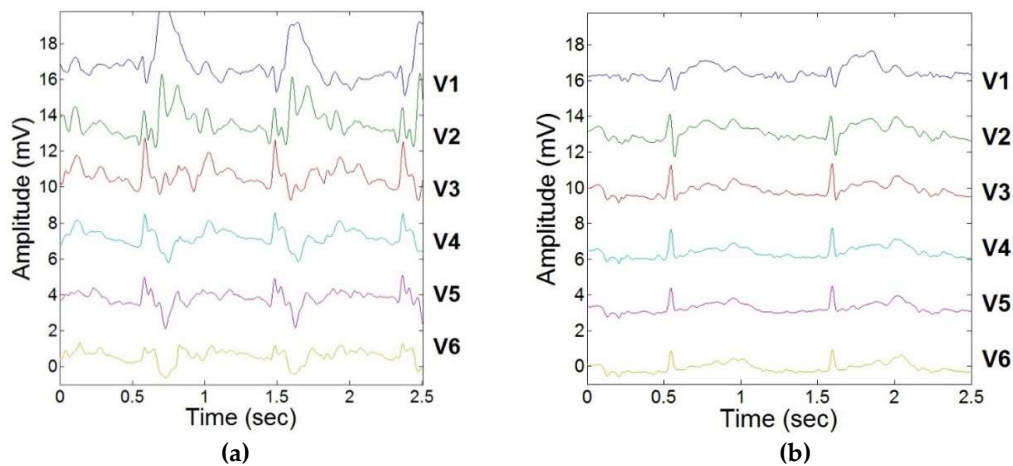
The extracted 12-lead ECG<sub>real</sub> after the filter training stage was found to correlate well with the “gold standard” ECG obtained outside the MRI, with an average cross-correlation index across all leads of 0.81 (Table 2).

**Table 2.** Cross-correlation coefficients between ECG<sub>real</sub> and ECG<sub>real</sub> extracted intra-MRI.

Lead	I	II	III	aVR	aVL	aVF	V1	V2	V3	V4	V5	V6
<b>Correlation Coefficient</b>	0.79	0.77	0.72	0.78	0.78	0.76	0.87	0.91	0.89	0.86	0.85	0.76

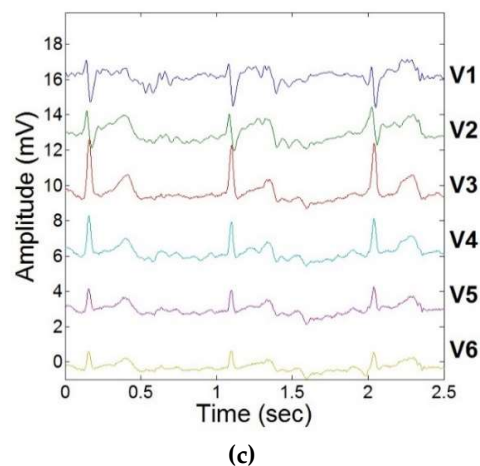
### 3.3. Evaluation during Exercise Stress Testing

The results of ECG<sub>real</sub> extraction performed using carotidal dynamic feedback during exercise stress testing are illustrated in Figure 5. Variations in ECG segments were observed due to the elevated heart rate. This more accurate separation of ECG<sub>real</sub> will in turn allow for increased accuracy in estimating MHD-derived metrics, such as stroke volume. There was less than a 5% variation in R-peak between filtered ECGs obtained inside the MRI and ECGs obtained outside the MRI scanner in all subjects.



**Figure 5.** Cont.





**Figure 5.**  $ECG_{real}$  extraction during exercise stress testing using adaptive filtering schema and dynamic carotidal VMHD feedback. (a) 12-lead ECG acquired inside the MRI prior to  $ECG_{real}$  extraction. (b) 12-lead ECG acquired inside the MRI during a resting heart rate. (c) 12-lead ECG acquired inside the MRI during exercise.

## 4. Discussion

### 4.1. Discussion

A method to extract ECG signals with reduced VMHD from intra-MRI 12-lead ECGs was presented and shown to provide accurate dynamic measurements of induced VMHD using flow in the carotid artery as a source of dynamic feedback. The addition of the dynamic feedback allows for a shorter filter response time to heartbeat variability, and the potential to more accurately estimate  $ECG_{real}$  and VMHD-derived metrics such as stroke volume.

VMHD was acquired using a single-lead ECG monitor from several different vasculature sources on the human body in order to determine an optimal flow source which induces VMHD with a similar morphology to that observed in 12-lead ECGs. The left common carotid artery was observed to have the highest correlation with regards to signal morphology of the aortic MHD extracted from 12-lead ECGs and was therefore selected as the source of dynamic feedback for training of adaptive filters to more accurately separate  $ECG_{real}$  and VMHD intra-MRI. The adaptive filtering schema presented was able to morph carotidal VMHD to match the aortic MHD template, and provide dynamic cardiac feedback to increase the accuracy of physiological monitoring during exercise stress testing.

This method will allow for advanced physiological monitoring within the MRI and has the potential to reduce the time associated with cardiac imaging by increasing the accuracy of cardiac ECG gating through improved MHD suppression.

### 4.2. Limitations

Although the dynamic feedback was shown to be useful in the extraction of  $ECG_{real}$ , this method does require the addition of a secondary physiological monitor to provide diagnostic quality ECG traces. This hardware constraint can potentially inhibit the ability of the proposed methodology to become widely used in practice and in conjunction with modern MRI-compatible 12-lead ECG recorders.

### 4.3. Future Work

To more thoroughly and rigorously test the proposed methodology, the experiments should be conducted on a larger group of subjects and expanded to a wider subject population, including individuals of varying physical fitness and gender. Additionally, the subject population should include not only healthy subjects but also subjects with pathologies such as cardiac disorders and arrhythmias.

This data should then be further evaluated by a cardiologist to validate the ability to acquire diagnostic quality ECGs using the proposed methodology.

## 5. Conclusions

Real-time 12-lead ECGs were acquired and filtered of the magnetohydrodynamic effect through the addition of a dynamic feedback term to a conventional adaptive filtering schema. The feedback term allowed for dynamic changes in induced VMHD to be assessed using a single bipolar lead positioned on the left common carotid artery and for a demonstrated level of accuracy during induced stress.

**Author Contributions:** Zion Tsz Ho Tse conceived and designed the experiments; T. Stan Gregory and Kevin James Wu performed the experiments and analyzed the data; John N. Oshinski contributed MRI scanning resources and analysis tools; T. Stan Gregory wrote the paper.

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