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# Observations of Turbulent Magnetic Reconnection within a Solar Current Sheet

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#### Abstract

Magnetic reconnection is a fundamental physical process in various astrophysical, space, and laboratory environments. Many pieces of evidence for magnetic reconnection have been uncovered. However, its specific processes that could be fragmented and turbulent have been short of direct observational evidence. Here, we present observations of a super-hot current sheet during the SOL2017-09-10T X8.2-class solar flare that display the fragmented and turbulent nature of magnetic reconnection. As bilateral plasmas converge toward the current sheet, significant plasma heating and nonthermal motions are detected therein. Two oppositely directed outflow jets are intermittently expelled out of the fragmenting current sheet, whose intensity shows a power-law distribution in the spatial frequency domain. The intensity and velocity of the sunward outflow jets also display a power-law distribution in the temporal frequency domain. The length-to-width ratio of current sheet is estimated to be larger than the theoretical threshold and thus ensures its occurrence. The observations therefore suggest that fragmented and turbulent magnetic reconnection occurs in the long stretching current sheet.

Key words: magnetic reconnection - Sun: coronal mass ejections (CMEs) - Sun: flares - turbulence

Supporting material: animation

#### 1. Introduction

Magnetic reconnection, referring to dissipation and connectivity change of the magnetic field, is capable of powering plasma heating, plasma motions, and particle acceleration in relativistic jets (Bloom et al. 2011), accretion disks (Balbus & Hawley 1998), solar and stellar flares (Sturrock 1966), and magnetospheres (Phan et al. 2006). In the past decades, abundant evidence for magnetic reconnection has been disclosed, including in situ measurements near the Earth (Wang et al. 2016) and remote sensing observations such as cusp-shaped flare loops (Masuda et al. 1994), inflows and downflows near the reconnection region (Yokoyama et al. 2001; Savage & McKenzie 2011; Takasao et al. 2012; Liu et al. 2013; Liu 2013; Xue et al. 2016), double hard X-ray coronal sources (Sui & Holman 2003), and changes in connectivity of coronal loops (Su et al. 2013; Yang et al. 2015; Li et al. 2016).

Unfortunately, the specific processes involved in magnetic reconnection, in particular what occur in the reconnection region, remain mysterious. Theoretically, magnetic reconnection is believed to take place in a localized region, i.e., the socalled current sheet, that has enhanced resistivity (Yamada et al. 2010; Priest 2014). In the Sweet-Parker model, the current sheet is limited to a long and thin region in which the reconnection proceeds steadily but too slowly to interpret the real energy release rate. Through invoking slow-mode shocks extending from a shortened Sweet-Parker current sheet, the Petschek model is able to significantly boost the reconnection rate (Petschek 1964). Nevertheless, the current sheet width in the Petschek model is of an ion inertial scale, which can hardly match the detectable width in observations. Therefore, it was proposed that the current sheet can be fragmented into many



magnetic islands by the tearing mode instability (Furth et al. 1963; Shibata & Tanuma 2001) and develops turbulence to achieve the fast reconnection (Lazarian & Vishniac 1999). However, such a picture has lacked direct observational evidence, even though it has been documented by numerical simulations (Kowal et al. 2009; Bárta et al. 2011; Shen et al. 2011) and indicated by various indirect observations such as simultaneous intermittent plasmoid ejections and hard X-ray/ radio bursts (Asai et al. 2004; Nishizuka et al. 2009; Takasao et al. 2016), the vortex above flare arcades (McKenzie 2013; Scott et al. 2016), and complex transition region line profiles with bright cores and broad wings (Innes et al. 2015).

In this study, we present a detailed analysis of a limb solar eruption on 2017 September 10 that produced an X8.2-class flare (SOL2017-09-10T16:06 UT) and a fast coronal mass ejection (CME). In particular, the presence of a thin and long hot plasma sheet underneath an erupting CME fits perfectly into the current sheet structure, as predicted in the theoretical model (Lin & Forbes 2000), and the dynamic behaviors of the plasma within and around the current sheet provide direct and solid evidence of the turbulent and intermittent nature of magnetic reconnection.

#### 2. Instruments

The data sets are primarily from Solar Dynamics Observatory (SDO; Pesnell et al. 2012). The Atmospheric Imaging Assembly (AIA; Lemen et al. 2012) on board SDO images the solar corona with a spatial resolution of 0.6 arcsec per pixel and a cadence of 12s at seven extreme ultraviolet (EUV) passbands. Here, we used the AIA data with a cadence of 24 s that have the normal exposure time. The data with a very short exposure time, in particular during the flare, usually have large uncertainties in intensity that can influence the differential emission measure (DEM) calculations and fast Fourier



**Figure 1.** Super-hot current sheet in the wake of an erupting bubble on 2017 September 10. (a) Top: a composition of the AIA 193 Å (red; temperature response peaks at ~1.6 and 18 MK), 131 Å (green; ~0.4 and 11 MK), and 171 Å (blue; ~0.6 MK) images showing an erupting bubble and induced current sheet at 15:53 UT. Middle and bottom: DEM-weighted average temperature and total EM maps showing that the erupting bubble has a high temperature (~8 MK) but low density at its center. (b) Images at the *Hinode*-XRT Al-poly, *SDO*-AIA 193 and 131 Å passbands, DEM maps at the temperatures of 2 and 20 MK, and the total EM map showing that the current sheet appears as a long and thin feature at 16:15 UT. The vertical dashed line in the AIA 193 Å image indicates the location of the slit used to construct the AIA time–distance plot in Figure 2(a). Note that we do not calculate the average temperature and EM of the flare loops and cross-shaped structure as shown in panels (a) and (b) because the flux is saturated there (white region). (c) The DEM of the current sheet (left) at five specific regions (small boxes in panel (b)) and the total EM (right) along five dashed lines as shown in the EM map of panel (b).

transform (FFT) analyses. The X-Ray Telescope (XRT; Golub et al. 2007) and EUV Imaging Spectrometer (EIS; Culhane et al. 2007) on board *Hinode* (Kosugi et al. 2007) provide the X-ray images and EUV spectra in the wavelength ranges of 170–210 Å (short) and 250–290 Å (long) with a spectral resolution of 0.0223 Å pixel<sup>-1</sup>, respectively. The *Geostationary Operational Environmental Satellite* records the soft X-ray 1–8 Å flux from the flare. In addition, the K-Cor instrument installed at the Mauna Loa Solar Observatory<sup>5</sup> and the Large Angle and Spectrometric Coronagraph (LASCO; Brueckner et al. 1995) on board the *Solar and Heliospheric Observatory* observe the white-light images of the CME and its trailing current sheet.

## 3. Results

### 3.1. Hot Flux Rope and Induced Super-hot Current Sheet

The early phase of the flare/CME eruption was fully captured by the AIA. At ~15:35 UT, a filament is activated to rise up. After ~15 minutes, it initiates the eruption of a nearby loop-like structure. Shortly afterward, the loop-like structure quickly expands and escapes away from the solar surface. Simultaneously, the overlying field constraining the loop-like structure is stretched outward. At ~15:53 UT, the loop-like structure ascends to a height of 90 Mm and appears as a well-defined bubble consisting of a ring-shaped envelop and a low emission cavity, both of which are visible at most EUV and X-ray passbands (top panel of Figure 1(a)). An elongated bright

structure connecting the bottom of the bubble and the top of the flare loops is observed. These features basically conform to the classic picture of eruptive flares (Sturrock 1966; Shibata et al. 1995; Chen 2011), in which the eruption of a twisted magnetic flux rope leaves behind a long and narrow current sheet (Lin & Forbes 2000). The bubble is most likely an edgeon manifestation of the forming flux rope as its axis is mostly along the line of sight (Cheng et al. 2011). The DEM analyses show that the cavity of the bubble has a low emission measure  $(EM \sim 10^{26} \text{ cm}^{-5})$ , though the temperature is relatively high  $(\sim 10 \text{ MK})$ . By contrast, the bubble envelope (or the ring) and the current sheet have a much higher EM ( $\sim 10^{27.5} \text{ cm}^{-5}$ ) and an even higher temperature ( $\sim 13$  MK). Such a temperature structure highly resembles the numerical results of the erupting flux rope energized by the reconnection in its trailing current sheet (Mei et al. 2012).

As the bubble escapes from the lower corona, the current sheet is further heated and extended. Its lower end ascends to a height of at least ~100 Mm around the flare peak time of ~16:15 UT (Figure 1(b)). The EM maps at different temperatures document that the extended current sheet mainly contains high-temperature plasma (Figure 1(b)), which is also confirmed by the EIS Fe XXIV 192.03 and 255.11 Å lines (with the formation temperature of ~18 MK). The plasma therein is primarily distributed near the temperature of 20 MK with a total EM of  $(1-5) \times 10^{27}$  cm<sup>-5</sup> (Figure 1(c)), which is similar to the temperature of supra-arcade downflows that are frequently observed when the current sheet is observed face-on (Hanneman & Reeves 2014). The corresponding density is calculated to be ~ $(0.6-1.3) \times 10^9$  cm<sup>-3</sup> assuming a depth of

<sup>&</sup>lt;sup>5</sup> https://www2.hao.ucar.edu/mlso/mlso-home-page



**Figure 2.** Evidence of inflows and turbulence. (a) The time-distance plot of the AIA 193 Å (red) and 171 Å (cyan) composited images showing the converging inflows, whose trajectories are tracked by the dashed lines. Their velocities range from 20 to  $100 \text{ km s}^{-1}$ . ((b) and (c)) Intensity and nonthermal velocity field of the EIS Fe XXIV 192.03 Å line. The imaging spectra are obtained by the EIS slit scanning the current sheet region from 16:09 UT to 16:18 UT. (d) The AIA 193 Å image shows the current sheet structure at 17:10 UT as indicated by the dotted line. (e) The spatial distribution of the normalized AIA 193 Å intensity along the dotted line in panel (d). The intensity is detrended with a moving average of 10 Mm to indicate the fast-varying structures. (f) The power spectrum of the detrended intensity variation as shown in panel (e) in the spatial frequency domain. The fitting spectral index  $\alpha$  in the range of 1–10 Mm is  $-1.16 \pm 0.22$ .

30 Mm (the size of the bubble) at the height of  $\sim 100-200$  Mm. Based on the distribution of the total EM along the direction perpendicular to the current sheet, the average width of the current sheet is estimated to be  $\sim 10$  Mm at the height of  $\sim 150$  Mm (Figure 1(c)), slightly larger than the width estimated by Savage et al. (2010).

#### 3.2. Fragmented and Turbulent Current Sheet

The EUV 171 Å observations disclose that the cool plasma (~1 MK) on both sides converges into the current sheet (Figure 2(a)). Shortly afterward, the plasma is strikingly heated and becomes visible in the AIA higher temperature passbands such as 193 and 131 Å (10–20 MK). The average velocity of the converging motion is  $\sim 100 \text{ km s}^{-1}$  in the early phase (15:55-16:00 UT) and subsequently decreases to  $\sim 20 \text{ km s}^{-1}$ , similar to previous estimations (Liu et al. 2013; Zhu et al. 2016; Li et al. 2017; Wang et al. 2017). The initial and faster inflows are possibly driven by the restoring force of the magnetic field, which was pushed aside by the erupting bubble before  $\sim 15:54$  UT. Besides the plasma heating, the Fe XXIV 192.03 Å line also displays a significant nonthermal broadening in the current sheet. The line width implies a nonthermal velocity of  $\sim 100-150 \text{ km s}^{-1}$  after subtracting the thermal velocity corresponding to a formation temperature of 18 MK (Figures 2(b) and (c)). Such large nonthermal velocity strongly indicates the existence of turbulent motions in the current sheet (also see Ciaravella & Raymond 2008; Doschek et al. 2014; Warren et al. 2018). It is also supported by the fact that the 193 Å intensity variation along the current sheet presents a fluctuation, which shows a power-law distribution in the spatial frequency domain after FFT (Figures 3(d) and (e)). The spectral index is estimated to be  $-1.16 \pm 0.22$  (Figure 3(f)).

The turbulent current sheet indicates that the sunward reconnection outflow jets, probably corresponding to magnetic islands expelled from the lower end of the current sheet, will show a power-law behavior. Figure 3(a) and the corresponding animation clearly show that the jets are intermittently shot out during the reconnection process. Each jet has an "Eiffel Tower" shape initially. Within a period of 2-5 minutes, probably driven by magnetic tension (Forbes & Acton 1996; Priest & Forbes 2002), each jet gradually comes to be cusp-shaped, and then continuously shrinks to a flare loop. The 193 Å intensities in the outflow regions also present intermittent fluctuations (Figures 3(b) and (c)). The FFT analysis shows that the temporal variation of the intensity (e.g., along the dashed line in Figure 3(b) obeys the power-law distribution with a spectral index around -1.60 (Figure 3(d)), very close to the spectral index of the turbulent current sheet (e.g., Bárta et al. 2011; Shen et al. 2011). It confirms our conjecture that the current sheet has been fragmented into different scaled structures, strongly suggestive of the existence of turbulence,



Figure 3. Intermittency and velocity diversity of the sunward outflow jets. (a) The AIA 193 Å running difference images (the time difference is 24 s) at 16:38 UT (top), 17:35 UT (middle), and 18:10 UT (bottom) displaying the reconnection outflow jets (white features) expelled from the lower end of the current sheet. ((b) and (c)) Time–distance plots of the original images and running difference images at the AIA 193 Å passband along the direction shown by the dashed line in panel (a). The white spicule-like features after ~16:00 UT as shown in panel (c) clearly display the sunward downflows. (d) The power spectrum of the normalized AIA 193 Å intensity in the outflow region as a function of frequency. The location is indicated by the dashed line in panel (b). Similar to Figure 2(f), the intensity is also detrended with a moving average of 60 minutes in order to show the high-frequency component. The spectral index ( $\alpha$ ) derived by linear fitting to the data in the range of 1–15 mHz is  $-1.63 \pm 0.07$ . (e) The velocity evolution for one reconnection outflow jets as a function of time. The *GOES* soft X-ray 1–8 Å flux is also plotted for comparison. (g) The power spectrum of the initial velocities as a function of frequency. The spectral index  $\alpha$  is  $-0.35 \pm 0.05$ . An animation of the AIA 193 Å running difference images (panel (a)) from 15:00 to 20:59 UT is available.

(An animation of this figure is available.)

with which the outflow jets are widely distributed in energies and sizes. Further evidence for a fragmented and turbulent reconnection is that the intensity variations at the other flaring regions also present the power-law distribution with spectral indices ranging from -1.2 to -1.8, quite different from that in the quiescent and pre-flare regions (see Figures 11–15 in the Appendix). It is worth noting that supra-arcade downflows may directly correspond to the sunward outflow jets (McKenzie 2000; Savage & McKenzie 2011; Reeves et al. 2015) or may be structures caused by Rayleigh–Taylor instabilities in the outflow region (Guo et al. 2014).

We find that the velocity of the sunward outflow jets also presents a dispersed distribution. The heights of the jets are measured through manually tracking their trajectories (as shown by Figure 16 in the Appendix). Almost all outflow jets have a large initial velocity but quickly slow down (Figure 3(e)). The initial velocities are diversely distributed, ranging from 100 to 800 km s<sup>-1</sup> (Figures 3(f) and 16), even in a short time period (16:00-16:30 UT), similar to previous estimations (Savage & McKenzie 2011). Interestingly, the FFT analysis indicates that the initial velocities also have a power-law spectrum with a spectral index of -0.35(Figure 3(g)). It implies that the reconnection that drives the outflow jets proceeds with a varying reconnection rate, probably modulated by turbulence. Taking an average value  $(20 \,\mathrm{km \, s^{-1}})$  of the inflow velocities near the flare peak time (16:00–16:15 UT), the reconnection rate (the ratio of the inflow

velocity to the outflow velocity) is estimated to range from 0.003 to 0.2. If the current sheet is fragmented into magnetic islands of different sizes (Shibata & Tanuma 2001), different reconnection rates and thus different kinetic energies of the outflow jets can be achieved. Moreover, the decelerations also have a wide distribution with its maximum up to 2000 m s<sup>-2</sup> (Figure 16), indicating that the upward magnetic pressure gradient force also varies with time that resists the downward magnetic tension and the Sun's gravity.

### 3.3. Largely Extended White-light Current Sheet

The K-Cor instrument of the Mauna Loa Solar Observatory provides the white-light images of the largely extended current sheet at its later phase. At 17:12 UT, the lower end of the current sheet is seen to join the tip of the cusp-shaped flare loops and is located at a height of  $\sim$ 140 Mm (Figure 4(a)), similar to the value measured in the EUV data. The apparent width of the current sheet is  $\sim$ 25 Mm, and the lower limit of the apparent length is 400 Mm (Figure 4(b)). It corresponds to a maximal reconnection rate of  $\sim$ 0.06, which, similar to the previous estimations (Savage et al. 2010; Ling et al. 2014; Seaton et al. 2017), is still smaller than the maximum value derived above. In fact, the original current sheet could be fragmented into magnetic islands due to tearing mode instability. Then, the real length of magnetic islands involved in each elementary reconnection process could be much



Figure 4. Extended current sheet and intermittent anti-sunward moving blobs. (a) White-light K image normalized with a radially graded filter observed by the Mauna Loa Solar Observatory showing the extended current sheet at 17:15 UT. (b) The brightness distributions of the current sheet along three perpendicular slits (in panel (a)). (c) Time–distance plots of the running difference images at the white-light K band along the direction of the current sheet. The dashed lines denote the trajectories of eight anti-sunward moving blobs. (d) The velocity evolution for blob 2 and blob 6. The errors of the velocities (vertical bars) are from the measurement uncertainties in height ( $\sim$ 23 Mm)



Figure 5. Loci curves of the emission in a small region in the current sheet, whose position is shown by the black box in Figure 1(c). The red line is the best fitting of the EM distribution derived by "xrt\_dem\_iterative2.pro." The gray dashed lines represent 100 MC solutions. The EM is calculated by Equation (2) in each temperature bin.

smaller. This is proved by the fact that the length-to-width ratio (>16) of the current sheet is much larger than the theoretical threshold of the tearing mode instability ( $2\pi$ ; Furth et al. 1963). The high-speed anti-sunward moving blobs also provide strong evidence for the existence of magnetic islands. Figure 4(c) shows that the blobs are intermittently formed in the current sheet at a height of ~200 Mm. The initial velocities are ~400 km s<sup>-1</sup> and then they gradually increase. Note that the width of the current sheet derived in the K corona is about 2.5 times larger than that in the EUV passbands. However, both are still much smaller than the values measured previously in the LASCO/C2 white-light coronagraph (~100 Mm at  $2R_{\odot}$ ; Lin et al. 2005, 2009, 2015; Ciaravella & Raymond 2008). Interestingly, the EUV current sheet is found to be located in the middle of the white-light sheet, implying that the former is

closer to the dissipation layer and thus has a higher temperature. Theoretically, the width of the diffusion layer is only tens of kilometers for Petschek-type magnetic reconnection with an anomalous resistivity. However, in observations, the apparent width of the current sheet can be seriously widened by turbulence, as well as slow-mode shock compression and projection effects (Ciaravella & Raymond 2008; Lin et al. 2015).

#### 4. Summary and Discussions

In the models of flux-rope-induced CME/flare eruptions (Shibata et al. 1995; Chen 2011), a pre-existing flux rope escapes away from the solar surface due to loss of equilibrium (Lin & Forbes 2000), leading to the formation of a CME and a flare at almost the same time (Zhang et al. 2001; Cheng et al. 2011). Magnetic reconnection acts as strong coupling between the CME and the flare as indicated by the simultaneity between the evolution of the CME velocity and the variation of the flare emission (Zhang et al. 2001). The linear bright feature in the wake of the erupting flux rope has been argued to be the induced current sheet, where electric current is enhanced and magnetic field is dissipated (Lin et al. 2015). Previous observations of the current sheet are mostly limited by the wavelength window that only responds to relatively narrow and low temperatures and/or the field of view that is not large enough (Ciaravella et al. 2003; Lin et al. 2005, 2009; Ciaravella & Raymond 2008; Savage et al. 2010; Ling et al. 2014; Seaton et al. 2017). Therefore, studies based on these observations are mostly speculative, in particular on the origin of the current sheet and its relation to the CME and flare. Moreover, the observations in those works could not provide further information on the detailed physical processes occurring in the current sheet; therefore, what kind of reconnection it is has seldom been addressed.



Figure 6. DEM maps of the erupting hot bubble at the temperatures of 20 MK, 10 MK, and 2 MK derived by the methods of M. A. Weber (a), I. G. Hannah (b), and M. C. M. Cheung (c), respectively.



Figure 7. Same as Figure 6, but for the current sheet.

In this study, we present a solar limb eruption event that displays a distinct picture of the CME/flare eruption with unprecedented clarity. Observations with a continuous field of view from 1 to  $30 R_{\odot}$  and multiwavelengths including the white-light, EUV, and X-rays enable us to reveal the origin of and specific processes involved in magnetic reconnection. We successfully detect almost all ingredients predicted by models during a single eruption including the erupting hot flux rope, super-hot current sheet, cusp-shaped flare loops, inflows, and

high-speed sunward and anti-sunward outflow jets, some of which have been detected in previous observations (Savage et al. 2010; Ling et al. 2014; Seaton et al. 2017; Liu et al. 2018; Yan et al. 2018). The high temperature of the flux rope envelope and the cusp-shaped flare loops probably originates from the collision of the outflow jets with the local dense plasma and/or the direct heating by slow-mode shocks at both ends of the current sheet (Liu et al. 2013). The high temperature of the current sheet, however, requires local



Figure 8. Fe XXIV 192.03 Å ( $\sim$ 18 MK), 255.11 Å ( $\sim$ 18 MK), Fe XXII 263.76 Å ( $\sim$ 14 MK), Fe XXII 253.17 Å ( $\sim$ 12 MK), Fe XVI 262.98 Å ( $\sim$ 3 MK), and Fe XV 284.16 Å ( $\sim$ 2 MK) line spectra showing the visibility and invisibility of the current sheet. The box in the upper left panel indicates the region where intensities and nonthermal velocities of the Fe xxiv 192.03 Å line are shown in Figure 2.



Figure 9. (a) AIA 193 Å images showing the evolution of the current sheet. (b) The spatial variation of the normalized AIA 193 Å intensity along the current sheet indicated by the dotted line in panel (a). (c) The power spectrum of the intensity variation as a function of spatial frequency with the oblique lines showing the power-law fitting to the range of 1–8 Mm.



Figure 10. Same as Figure 9, but for the AIA 131 Å passband.



Figure 11. AIA 193 and 131 Å images at 17:00 UT showing the post-flare loops and the current sheet. Slice 1 and slice 2 are used for creating the time-distance plots in Figures 12(a)-15(a).

heating by magnetic energy dissipation inside the current sheet itself.

The turbulent behavior of energy release in the current sheet is also revealed. A high Lundquist number, suggested by a large length-to-width ratio (>16) of the current sheet, leads to the generation of magnetic islands due to the tearing mode instability (Furth et al. 1963), which subsequently appear as intermittent sunward outflow jets and anti-sunward moving blobs when shot out of the current sheet. Simultaneously, the turbulence develops in the current sheet (Strauss 1988; Lazarian & Vishniac 1999). On the one hand, its effect helps achieve anomalous resistivity to boost the magnetic dissipation rate. On the other hand, it may mediate the formation of magnetic islands with their size and energy presenting a power-law distribution. This process finally makes the intensity and velocity of the sunward outflow jets exhibit a power-law distribution. In particular, the spectral index of the former is found to vary from -1.2 to -1.8, which suggests that the turbulence mediates the reconnection process in the current sheet, resulting in the formation of different scaled magnetic islands, consistent with previous numerical results (Kowal et al. 2009; Bárta et al. 2011; Shen et al. 2011). The deviation from the fully developed isotropic turbulence (with a Kolmogorov turbulence spectral index of -5/3) may be due to the role of magnetic field. The significant nonthermal motions shown in the Fe XXIV line are also evidence of the existence of turbulence. In summary, these observations show that the magnetic reconnection, at least in solar eruptions, does not proceed uniformly in space and time. Instead, the current sheet should be composed of fragmented structures in which



**Figure 12.** (a) Time-distance plot of the AIA 193 Å images along slice 1 in Figure 11. ((b) and (c)) The normalized 193 Å intensity variations as a function of time at the two outflow regions indicated by S1 and S2 in panel (a). It is also detrended with a moving average of 60 minutes in order to remove the feature of the decay reconnection process. ((d) and (e)) The power spectral densities of the intensities at S1 and S2 with the oblique lines indicating the power-law fitting to the range of 1-15 mHz.



Figure 13. Same as Figure 12, but for the AIA 131 Å passband.



Figure 14. (a) Time-distance plot of the AIA 193 Å images along slice 2 in Figure 11. ((b) and (c)) The normalized 193 Å intensity variations as a function of time at the two quiescent regions indicated by S1 and S2 in panel (a). ((d) and (e)) The power spectral densities of the intensities at S1 and S2.



Figure 15. Same as Figure 14, but for the AIA 131 Å passband.

magnetic reconnection dissipates magnetic energy in a turbulent way (Kontar et al. 2017) to heat the plasma and drive the outflow jets.

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Figure 16. (a) Time-distance plot of the AIA 193 Å running difference images with tracked trajectories of the erupting bubble (the first dashed line) and sunward moving outflow jets. ((b) and (c)) Histogram distributions of the initial velocities and the accelerations of the outflow jets.

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## Appendix Methodology and Uncertainties

*DEM reconstruction:* The DEM is resolved through six AIA passbands including 94 Å (Fe x, ~1.1 MK; Fe XVIII, ~7.1 MK), 131 Å (Fe VIII, ~0.4 MK; Fe xXI, ~11 MK), 171 Å (Fe IX, ~0.6 MK), 193 Å (Fe XII, ~1.6 MK; Fe XXIV, ~18 MK), 211 Å (Fe XIV, ~2.0 MK), and 335 Å (Fe XVI, ~2.5 MK). The code "xrt\_dem\_iterative2.pro" in Solar SoftWare (SSW; Freeland & Handy 1998), originally proposed by Weber et al. (2004) and later modified by Cheng et al. (2012), is used for reconstructing the DEM. The inputs are observed intensity  $I_i$  and the temperature response function  $R_i(T)$  of the passband *i*.  $I_i$  is written as

$$I_i = \int \text{DEM} \times R_i(T) dT + \delta I_i, \qquad (1)$$

where DEM denotes the plasma DEM, and  $\delta I_i$  is the uncertainty in the intensity  $I_i$ . The temperature range for doing the inversion is set as  $5.5 \leq \log T \leq 8.0$ . The EM is calculated as

$$\mathrm{EM} = \int \mathrm{DEM} \, dT,\tag{2}$$

where the temperature range of integration is set to be  $7.0 \le \log T \le 7.5$ . We performed 100 Monte Carlo (MC) solutions through adding a random noise (within the errors of

observed intensities) to the intensity  $I_i$  and then rerunning the routine. The results show that 100 MC solutions are converged in the range of  $7.0 \le \log T \le 7.5$  (Figure 5). The density *n* in the current sheet is obtained by

$$n = \sqrt{\mathrm{EM}/l}\,,\tag{3}$$

where l is the depth of the current sheet.

We also take advantage of the other two inversion methods independently developed by Hannah & Kontar (2012) and Cheung et al. (2015), respectively. It is found that the three methods give very similar results. The erupting bubble, in particular its envelope, primarily contains high-temperature plasma (Figure 6), while the background and foreground contribute some cool plasma emission. As for the current sheet, the results from the different methods are also consistent with each other, which all present a super-hot ingredient and the absence of cool plasma in the current sheet (Figure 7). It is noted that some discrepancies also exist. The code "xrt\_dem\_iterative2.pro" is able to reconstruct the super-hot current sheet with a pretty good clarity. However, in the region outside of the current sheet, it may overestimate the DEM values compared with the other two codes. Nevertheless, we do not think that it influences our results, at least qualitatively. The results are also consistent with Warren et al. (2018), who did the DEM inversion via the combination of AIA and EIS data and also found that the plasma in the current sheet has temperatures of about 20 MK and distributes in a relatively narrow temperature range.

The uncertainties in the DEM results come mainly from the uncertainties in the observed intensities, which are obtained by the routine "aia\_bp\_estimate\_error.pro" in SSW. The uncertainties of the intensities are a result of the uncertainties in the temperature response functions of AIA including non-ionization equilibrium effects (Imada et al. 2011), nonthermal populations of electrons, modifications of dielectronic recombination rates (Summers 1974; Badnell et al. 2003), radiative transfer effects (Judge 2010), and even unknown filling factor. After considering these effects, an uncertainty lower limit of

~20% for  $R_i(T)$  is derived (Judge 2010) and thus cannot significantly influence the results (Cheng et al. 2012).

Spectroscopic Analyses: The EIS data are processed via the routine *eis\_prep.pro* in the standard EIS software package with corrections for dark current, hot pixels, and cosmic-ray hits. It observed the flaring region near the west limb for a period starting before 15:35 UT (flare onset) through 16:53 UT that covers the rise and early decay phases of the flare. The 2 arcsec slit of EIS was used to scan over an area of 240 arcsec  $\times$  304 arcsec from west to east with a course step of 3 arcsec, yielding a spatial resolution of 3 arcsec  $\times$  1 arcsec. It took about 9 minutes in each run with an exposure time of 5 s at each step.

Here, we used the Fe XXIV 192.03 Å line with a formation temperature of 18 MK, in which the current sheet is most clearly visible. The Fe XXIV 192.03 Å line is believed to be blended with the Fe XI 192.02 Å line ( $\sim 1$  MK), but the blending could be safely ignored in large flares that contain hot plasmas. This can be verified by checking the relative strength of another line Fe XII 192.39 Å ( $\sim$ 1 MK) in the same spectral window, which is clearly separated from the Fe XXIV 192.03 Å. Theoretically, the Fe XII 192.39 Å line is stronger than the Fe XI 192.02 Å line. Therefore, when the emission at 192.02/ 192.03 Å is greater than that at Fe XII 192.39 Å, it should be mostly from the hot Fe XXIV 192.03 Å line. We examine all of the line profiles around the current sheet region and conclude that the emission is mainly contributed by the Fe XXIV 192.03 Å line (also see Li et al. 2018; Warren et al. 2018). In addition, we note that the Fe XXIV 192.03 Å line is saturated in some regions (mostly in flare loops) but not in the current sheet region under study. So we just discard those saturated line profiles in our study.

The spectra of some other lines, for example, Fe XXIV 255.11 Å ( $\sim$ 18 MK), Fe XXIII 263.76 Å ( $\sim$ 14 MK), Fe XXII 253.17 Å ( $\sim$ 12 MK), Fe XVI 262.98 Å ( $\sim$ 3 MK), and Fe XV 284.16 Å ( $\sim$ 2 MK) are also presented (Figure 8). It is seen that the current sheet is only visible in the high-temperature (>12 MK) lines, in particular in Fe XXIV 192.03 Å, which is consistent with the AIA imaging observations.

The Fe XXIV 192.03 Å line profiles show a good Gaussian shape, and we implement a single Gaussian fitting to obtain the nonthermal velocity by the formula

$$W = 1.665 \,\frac{\lambda}{c} \,\sqrt{\frac{2 \,k \,T_i}{M} + \xi^2}\,,\tag{4}$$

where *W* is the FWHM of the spectral line,  $\lambda$  is the line wavelength, *c* is the speed of light, *k* is the Boltzmann constant, *T<sub>i</sub>* is the ion temperature, and *M* is the ion mass. The instrumental width of EIS (2.5 pixels, or 0.056 Å) is also subtracted. Here, we adopt a fixed thermal temperature of  $T_i = T_{\text{max}} = 18$  MK. For comparison, we also use a DEMweighted average temperature that is place-dependent to derive  $\xi$  and find that the results are quite similar. The values are also consistent with that independently derived by Warren et al. (2018). Please see Li et al. (2018) for some selected Fe XXIV 192.03 Å line profiles and resulting fitting results.

*Fragmentation of the Current Sheet:* The fragmentation of the current sheet is also examined at different passbands and different times, as shown in Figures 9 and 10. It can be seen that the spatial variation of the 193 and 131 Å intensity (along the current sheet) presents a power-law behavior in the spatial

frequency domain  $(0.1-1.0 \text{ Mm}^{-1})$ . The spectral index varies from -1.0 to -1.4. This type of fluctuation is also known as red "noise," which is an intrinsic property of a random physical process, most likely due to turbulence, that can be described by a power-law spectrum with a negative slope (Vaughan 2005; Inglis et al. 2015; Ning 2017). It indicates that the current sheet has been fragmented into different scaled structures, most likely corresponding to magnetic islands of different sizes. As shown in Figures 9(b) and 10(b), the AIA 193 and 131 Å intensity has been detrended with a moving average of 10 Mm in order to remove the feature of the intensity decrease away from the flare region. We also test the different moving average values (5-20 Mm) and find that derived spectral index is not seriously influenced. It is also worth noting that, for the detrended data, the power in the low spatial frequency (e.g.,  $<0.1 \text{ Mm}^{-1}$ ) can be artificially suppressed (Gruber et al. 2011), but that is not used here. Of course, as mentioned above, the AIA 193 and 131 Å intensity also includes an uncertainty that mainly is caused by the nonlinear effects of the AIA response function. The uncertainty may have somewhat of an effect on the spectral index (Ireland et al. 2015).

Intermittency and Velocity Diversity of the Outflow Jets: We also inspect the power spectrum of the temporal variations of the AIA 193 and 131 Å intensity at many other locations. Figure 11 shows two slices that we used for creating the timedistance plots. We find that the temporal variations of the intensity at almost all locations do display a power-law distribution with the spectral index distributing in the range of -1.2 to -1.8 (e.g., Figures 12 and 13). By contrast, for the quiescent regions and pre-flare regions, the spectrum is flat, which denotes white noise that is nearly frequency-independent and mainly originates from random signals (e.g., Figures 14 and 15). Similar to the spatial frequency analysis, the nonlinear effects of the AIA passbands also influence the spectral index in the temporal frequency analysis (Ireland et al. 2015). Note that the cadence of the AIA data is not exactly uniform, but is found to be smaller than 0.05%. After carefully testing, we find that whether the non-uniformity is corrected or not does not significantly influence the FFT results.

Using the time-distance plot of the AIA 193 Å running difference images along the direction of the current sheet, we manually identified the trajectories of the sunward outflow jets, as shown in Figure 16(a). The initial speed is derived as an average of the first three points of the measured outflow speeds. The histogram distributions of the initial velocities and accelerations of the jets are displayed in Figures 16(b) and (c). One can clearly see that both of them have a wide distribution.

Height of the Lower End and X-point of the Current Sheet: The heights of the CME bubble are measured in the AIA field of view. Applying the first-order numerical derivative, the velocity as a function of time is derived (Figure 17). One can see that the CME bubble experiences a slow rise phase of ~10 minutes with an average speed of ~70 km s<sup>-1</sup> and a fast acceleration phase with an acceleration of ~2200 m s<sup>-2</sup> in the AIA field of view. The CME finally reaches a speed of over 3000 km s<sup>-1</sup> when leaving the LASCO field of view.<sup>6</sup>

The lower end of the current sheet is estimated to be at the height of  $\sim 100 \text{ Mm}$  above the solar surface ( $\sim 1100 \text{ arcsec}$ ) at

<sup>&</sup>lt;sup>6</sup> https://cdaw.gsfc.nasa.gov/CME\_list/halo/halo.html



Figure 17. Temporal evolution of the velocity of the erupting bubble with the errors indicated by the vertical bars.



Figure 18. Composition of the AIA 193 Å, white-light K, and LASCO C2 images showing a largely extended current sheet at 17:12 UT.

16:15 UT, where the outflow jets are expelled. One hour later (17:15 UT), the lower end is also seen by the white-light K coronagraph. The height is determined to be  $\sim$ 140 Mm. Considering that the lower end of the current sheet has an ascending motion as the CME erupts, its height will increase by 54 Mm in one hour if assuming a velocity of 15 km s<sup>-1</sup> (Mei et al. 2012). It roughly agrees with the difference between the heights derived in the EUV and white-light passbands at different instants.

The theoretical model of the flux-rope-induced CME/flare (Lin & Forbes 2000; Mei et al. 2012) also predicts an X-shaped null point existing in the current sheet. Magnetic islands are expected to run away from the null point along two opposite directions, manifesting as sunward outflow jets and anti-sunward fast moving blobs (e.g., Song et al. 2012; Chae et al. 2017), respectively. The jets and blobs have initial heights of ~100 Mm and ~180 Mm, respectively. It indicates that the height of the X-shaped null point is in the range of 100–180 Mm.

Uncertainty in the Reconnection Rate: The reconnection rate is calculated as the ratio of the inflow velocity to the outflow

velocity. We consider that the initial speed of the outflow jets is equivalent to the outflow speed. The error of the initial speed is about 100 km s<sup>-1</sup>. Thus, the uncertainty in the reconnection rate can be up to 50% when considering the initial velocities of 100–800 km s<sup>-1</sup> in the time period of 16:00–16:30 UT. If taking an average outflow speed of  $\sim$ 300 km s<sup>-1</sup> and the inflow speed of 20 km s<sup>-1</sup>, the average reconnection rate is about 0.07 ± 0.03.

Uncertainty in the Length of the Current Sheet: We estimate the length of the current sheet based on the distributions of the brightness along the direction perpendicular to the current sheet (Figure 4(a)). Figure 4(b) shows that the brightness distributions at three slices have a similar profile with an FWHM of about 25 Mm. It is found that the FWHM is nearly uniform in between the two slices located at 840 Mm and 1240 Mm, respectively. Outside this region, the FWHM gets larger. Thus, the distance between the two slices is regarded as the length of the current sheet. Note that such a length is a lower limit. On the other hand, the LASCO observations show that the current sheet may even extend to a height of  $8 R_{\odot}$  at 17:12 UT, i.e., the edge of the C2 field of view where the blobs are still seen to move along the stretched bright structure by the erupting CME (Figure 18). It corresponds to a length of 4900 Mm. Such a length can be regarded as an upper limit for the length of the current sheet. If the width remains to be 25 Mm, the upper limit of the length-to-width ratio for the current sheet is  $\sim 200$ . Whatever the case may be, the length-to-width ratio is much larger than the theoretical threshold for the tearing mode instability ( $2\pi$ ; Samtaney et al. 2009).

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