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Accurate mass and radius determinations of a cool subdwarf in an eclipsing binary

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ABSTRACT

Cool subdwarfs are metal-poor low-mass stars that formed during the early stages of the evolution of our Galaxy. Because they are relatively rare in the vicinity of the Sun, we know of few cool subdwarfs in the solar neighbourhood, and none with both the mass and the radius accurately determined. This hampers our understanding of stars at the low-mass end of the main-sequence. Here we report the discovery of SDSS J235524.29+044855.7 as an eclipsing binary containing a cool subdwarf star, with a white dwarf companion. From the light-curve and the radial-velocity curve of the binary we determine the mass and the radius of the cool subdwarf and we derive its effective temperature and luminosity by analysing its spectral energy distribution. Our results validate the theoretical mass-radius-effective temperature-luminosity relations for low-mass low-metallicity stars.

Introduction

Cool subdwarfs are metal-poor, low-mass main-sequence stars of spectral type from mid K to late M. They are generally referred to as sdM/sdK stars. The low metallicity in cool subdwarfs decreases the opacity of their outer layers resulting in a small radius as compared to a main-sequence star of the same effective temperature¹. Thus, cool subdwarfs have lower luminosities than dwarfs of the same effective temperature and lie below the main sequence on the Hertzsprung-Russell diagram². The low metallicity of cool subdwarfs implies that they are typically very old ($\gtrsim 10$ Gyr)³ and are part of old Galactic populations such as the thick disc, the halo and the bulge⁴. Hence, cool subdwarfs formed in the first phases of our Galaxy and therefore carry important information regarding its structure and chemical evolution. Moreover, the analysis of the spectral energy distribution (SED) of cool subdwarfs improves our understanding of the role of metallicity in the opacity structure and evolution of cool atmospheres⁵. Depending on their metallicity, cool subdwarf stars are divided into three sub-classes: sd (subdwarfs), esd (extreme subdwarfs) and usd (ultra subdwarfs)⁶, with the metallicity content decreasing from the sd to the usd stars. Specifically, the iron abundance [Fe/H] ranges from -0.34 to -0.87 dex for sd stars, from -0.87 to -1.36 dex for esd stars and it is lower than -1.36 dex for usd stars⁷. This classification is based on the strength of the TiO and CaH bands in the observed spectra⁸.

In order to understand the nature of these rare and important objects, it is essential to determine their most basic stellar parameters such as masses and radii. To that end, and despite their intrinsic low luminosity, modern large-scale surveys such as the Sloan Digital Sky Survey (SDSS)⁹ and the Large Sky Area Multi-Object Fiber Spectroscopic Telescope (LAMOST)¹⁰ have identified ~ 5000 cool subdwarfs during the last few years^{11,12}. A recent ground-based spectroscopic survey allowed radii determinations of 88 cool subdwarfs via the analysis of their SEDs and the use of *Gaia* parallaxes⁶. However, we currently know of only six cool subdwarfs for which dynamical masses have been measured¹⁴. Moreover, it has to be stressed that no mass *and* radius values for a single cool subdwarf have been measured to date. Thus, the bottom-end of the main sequence remains unconstrained for metal-poor stars.

Here we report the discovery of SDSS J235524.29+044855.7 (hereafter SDSS J2355+0448) as an eclipsing binary containing a cool subdwarf, with a white dwarf companion. SDSS J2355+0448 was originally identified as a white dwarf candidate¹⁵ and later re-discovered as part of our systematic search of white dwarf plus low-mass main sequence binaries within the SDSS and LAMOST spectroscopic data bases^{16,17} (see the optical spectrum in Figure 1). Eclipsing binaries offer the opportunity to

measure directly the masses and radii of the two components with unprecedented precision^{16,19}. This is the case for the cool subdwarf in SDSS J2355+0448.

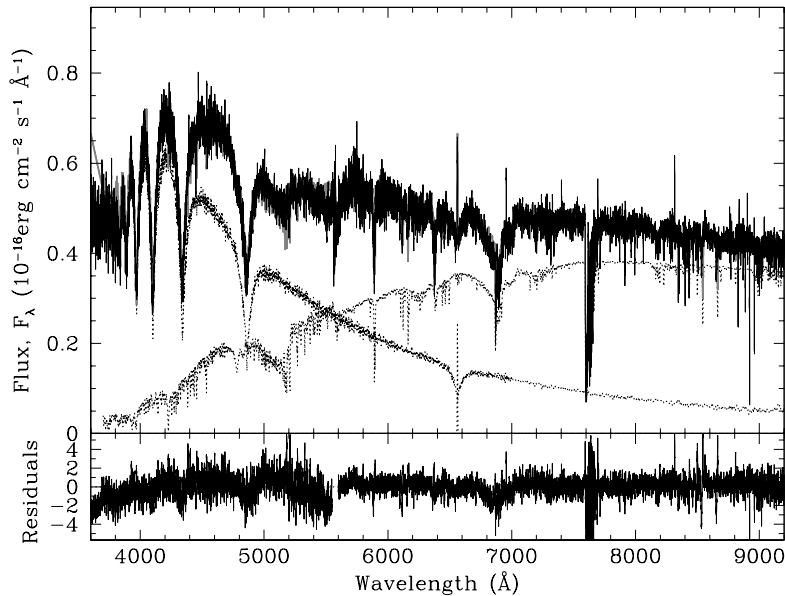


Figure 1. Top panel: X-Shooter optical spectrum of SDSS J2355+0448 (black solid lines). The hydrogen Balmer absorption lines of a DA white dwarf can be clearly seen in the blue. At longer wavelengths the spectrum is mostly featureless, with the exception of the broad CaH molecular band at $\sim 6800\text{\AA}$, typical of cool subdwarfs. The strong $H\alpha$ emission arises most likely due to magnetic activity of the cool subdwarf and/or from wind accretion onto the white dwarf. The two-component template spectra (white dwarf and cool subdwarf) that best fit the observed spectrum are shown as black dotted lines. The bottom panel shows the residuals from the fit. The spectrum has been binned by a factor of five for clarity.

Results

Available photometry from the Catalina Sky Surveys²⁰ revealed the binary star SDSS J2355+0448 to be eclipsing with an orbital period of 2.15 hours. We were awarded Director’s Discretionary Time at the 8.2m Very Large Telescope to obtain X-Shooter spectra covering the entire optical plus near-infrared wavelengths of the target (see the Methods section for a description of the observations). From the spectra we derived the white dwarf effective temperature and surface gravity (hence its cooling age), the systemic velocity of the binary, the radial-velocity curve amplitude of the cool subdwarf and its metallicity class, and we estimated the cool subdwarf’s $[\text{Fe}/\text{H}]$ abundance.

We were also awarded time on the 10.4m Gran Telescopio Canarias equipped with HiPERCAM² to sample the orbital light curves in five filters (see also the Methods section for a description of the observations). The data revealed not only the primary but also the secondary eclipse (i.e. the transit of the white dwarf in front of the cool subdwarf). The latter is crucial in fixing the orbital inclination and stellar radii relative to the orbital separation. The analysis of the HiPERCAM light-curve, together with the radial-velocity curve of the cool subdwarf, allowed precise determinations of the masses and radii of both stellar components as well as measurements of the SDSS magnitudes for the cool subdwarf. These magnitudes, together with available near-infrared photometry of the binary, permitted the effective temperature and the bolometric luminosity of the cool subdwarf to be determined via SED fitting.

The fitted and derived stellar and binary parameters of SDSS J2355+0448 are provided in Table 1.

The white dwarf stellar parameters

The optical spectrum of SDSS J2355+0448 (top panel of Figure 1) clearly shows the white dwarf and cool subdwarf components. To derive the stellar parameters of the white dwarf via Balmer-line fitting (namely the effective temperature and the surface gravity) it is necessary to subtract the cool subdwarf contribution. To that end we applied a decomposition/fitting routine³ to the individual X-Shooter optical spectra of the binary. Note that we did not use a combined optical X-Shooter spectrum for this purpose since we were not able to measure the radial velocities of the white dwarf, and hence the Balmer lines in a combined spectrum would have suffered from orbital smearing.

The decomposition/fitting routine first fits the two-composite spectrum with a grid of observed cool subdwarf⁵ and white dwarf³ templates and subtracts the best-fitted cool subdwarf template, appropriately scaled in flux (see the best two-composite fit to one of our X-Shooter spectra in the top panel of Figure 1). In a second step, the routine fits both the normalised Balmer lines and the whole spectrum (continuum plus lines) of the residual white dwarf spectrum with a white dwarf model atmosphere grid⁷ to derive the white dwarf effective temperature and surface gravity (see Supplementary Figure 1). For further details on our decomposition/fitting routine we point the reader to the Methods section.

Parameter	units	value	uncertainty
Orbital period	days	0.089 778 006 5	0.000 000 002 4
Binary inclination	degrees	89.7	0.2
Binary separation	R_{\odot}	0.711	0.003
Mass ratio	M_{sd} / M_{WD}	0.335	0.002
Centre of WD eclipse	MJD(BTDB)	58074.107 683 0	0.000 008 7
<i>Gaia</i> parallax	mas	1.89	0.46
Bayesian distance ²³	pc	541	-124 +216
Right ascension	deg	358.85133	
Declination	deg	4.81539	
SDSS g	mag	19.59	0.01
WD T_{eff}	K	13,247	200
WD $\log g$	dex	7.680	0.075
WD cooling age	Gyr	0.40	0.09
WD mass	M_{\odot}	0.4477	0.0052
K_{sd}	km s^{-1}	296.5	3.3
γ_{sd}	km s^{-1}	-117.7	2.7
sd T_{eff}	K	3,650	50
sd bolometric luminosity	L_{\odot}	4.3×10^{-3}	2.4×10^{-3}
sd spectral sub-type		sdK7	± 1 subclass
sd [Fe/H] abundance	dex	-1.55	0.25
sd mass	M_{\odot}	0.1501	0.0017
sd radius (towards WD)	R_{\odot}	0.1821	0.0007
sd volume-averaged radius	R_{\odot}	0.1669	0.0007

Table 1. Fitted and derived stellar and binary parameters for SDSS J2355+0448. sd and WD stand for cool subdwarf and white dwarf, respectively. We also include the right ascension and declination of the binary, the SDSS g -band magnitude, the *Gaia* parallax and the distance.

In most cases, the best-fitted template of the cool subdwarf was that of an sdK7 spectral type, although the sdM1 and sdM3 templates also provided good fits to some of the spectra. We emphasise that, at this stage, we are not aiming at determining the spectral type of the cool subdwarf, but only the stellar parameters of the white dwarf by subtracting the cool subdwarf flux contribution. The white dwarf effective temperatures obtained in this way from our X-Shooter optical individual spectra range from $12,882 \pm 29$ K to $13,335 \pm 94$ K and the surface gravities between 7.59 ± 0.03 and 7.76 ± 0.03 dex. Taking the average values we find $13,247 \pm 76$ K and 7.68 ± 0.03 dex, respectively. It has to be noted however that the uncertainties obtained are underestimated due to systematic errors in flux calibration, in the normalization process and/or in the model atmosphere grid used. Hence, we take more conservative uncertainties of 200 K and 0.075 dex in our spectroscopic values of effective temperature and surface gravity, respectively. For completeness, we interpolated the averaged values of effective temperature and surface gravity in white dwarf cooling sequences for low metallicities¹⁸ to derive a (model dependent) spectroscopic white dwarf mass of $0.457 \pm 0.015 M_{\odot}$ and a cooling age of 0.40 ± 0.09 Gyr. The spectroscopic white dwarf mass is in agreement with the mass obtained from our light-curve fitting method (see Table 1).

The radial-velocity curve of the cool subdwarf

We determined the radial velocities of the cool subdwarf by fitting a second-order polynomial plus a triple-Gaussian line profile to the Ca II absorption triplet at $\sim 8500 \text{\AA}$ sampled by our optical X-Shooter spectra (see the Methods section for a full description of the procedure). Periodograms calculated from the radial velocities to investigate the periodic nature of the velocity variations displayed a clear peak at 11.139 d^{-1} as well as a couple of weaker aliases due to the sampling pattern of

the observations (Figure 2, top panel). We carried out sine-fits of the form

$$V_r = K_{sd} \sin \left[\frac{2\pi(t - T_0)}{P_{orb}} \right] + \gamma \quad (1)$$

to the radial-velocity data set, where γ is the systemic velocity, K_{sd} is the radial velocity semi-amplitude of the cool subdwarf, T_0 is the time of inferior conjunction of the cool subdwarf, and P_{orb} is the orbital period. The sine-fit assumed the frequency corresponding to the strongest peak in the power spectrum as the orbital period of the binary, i.e. 2.154 hours, in agreement with the orbital period measured from the Catalina Sky Survey²⁰ light curves. The radial-velocity curve folded over the orbital period is illustrated in the bottom panel of Figure 2.

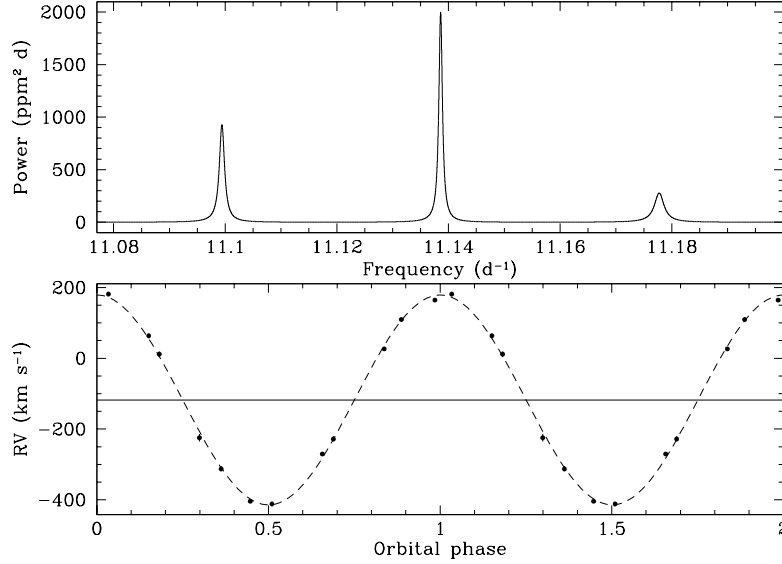


Figure 2. Periodogram obtained from the radial-velocity data of the cool subdwarf in the binary SDSS J2355+0448, derived from X-Shooter spectroscopy. A clear peak at 11.139 d^{-1} can be seen. Bottom panel: the radial-velocity curve folded over the period provided by the periodogram in the top panel. The radial-velocity $\pm 1\sigma$ error bars are shown but are too small to see.

The mass and radius of the stellar components

The high-speed light curves of SDSS 2355+0448 (see Figure 3) revealed a sharp eclipse of the white dwarf, with an ingress/egress lasting 80 seconds and a total eclipse duration of 11 minutes. As was already apparent from the spectroscopy, the white dwarf dominates the overall flux in the u_s and g_s bands, resulting in a deep eclipse and little out-of-eclipse variation. At longer wavelengths the tidally distorted shape of the cool subdwarf results in a double-peaked ellipsoidal modulation signal away from the eclipse. In the i_s band we detect the secondary eclipse (Figure 3). All of these features allowed us to constrain the stellar and binary parameters with minimal use of theoretical models.

We fitted the light curves using the LCURVE code¹¹, which is specifically designed for fitting the light curves of compact binary systems (see the Methods section for a detailed description of the light curve model and fitting procedure). Due to the lack of a direct measurement of the radial-velocity semi-amplitude of the white dwarf we were unable to determine the masses and radii of both stars completely independent of theoretical models. We therefore forced the radius of the white dwarf to follow a theoretical mass-radius relationship when fitting the light curve, hence the parameters of the cool subdwarf are only dependent upon the well tested white dwarf mass-radius relationship¹⁶.

The effective temperature and the bolometric luminosity of the cool subdwarf star

The Virtual Observatory SED Analyzer (VOSA)²⁸ is a tool that compares observed photometry, gathered from a significant number of compliant VO catalogues, to different collections of theoretical model spectra for measuring the stellar parameters (effective temperature, surface gravity, metallicity, bolometric luminosity) of a given object/s. We used VOSA to derive the effective temperature and bolometric luminosity of the cool subdwarf in SDSS J2355+0448. A description of the methodology employed by VOSA is provided in the Methods section.

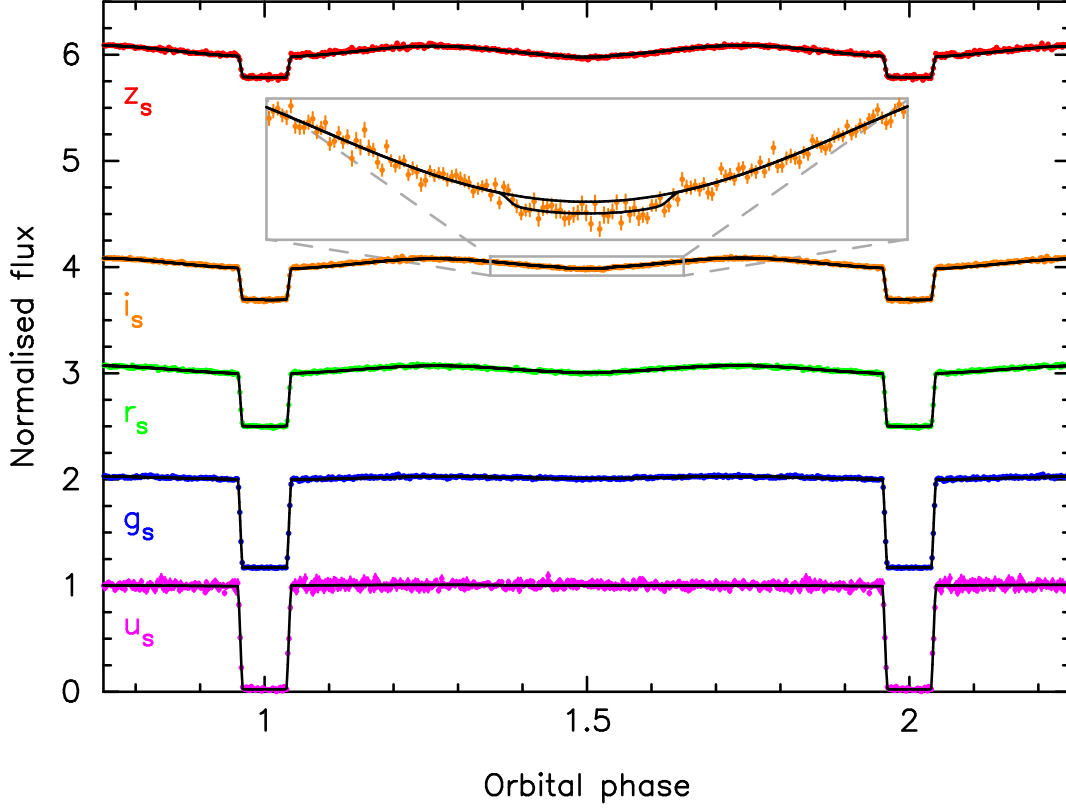


Figure 3. Phase-folded HiPERCAM light curves of SDSS J2355+0448 with model fits over-plotted (black lines). The g_s , r_s , i_s and z_s band data have been binned by a factor of three and offset vertically for clarity. We show a zoom-in to the i_s band light-curve, which displays the secondary eclipse (i.e. the transit of the white dwarf in front of the cool subdwarf). Over-plotted is our best fit model with the secondary eclipse turned on and off to demonstrate its depth. The error bars represent $\pm 1\sigma$ uncertainties.

Given that the white dwarf and the cool subdwarf are spatially unresolved, we did not make use of VOSA to gather available optical photometry, since those values correspond to the magnitudes of the binary system and not to the cool subdwarf. Hence, we derived the optical magnitudes of the cool subdwarf from our HiPERCAM light curves during eclipse, when the flux contribution from the white dwarf is zero. The HiPERCAM magnitudes were converted into SDSS $ugriz$ photometry. Colour terms between the HiPERCAM and the SDSS photometric systems were determined by folding main-sequence template spectra²⁹ through theoretical band-passes for HiPERCAM. We also considered the publicly available near-infrared hk UKIDSS³⁰ magnitudes of SDSS J2355+0448, where the white dwarf flux contribution is negligible (the yj magnitudes do show signs of contamination from the flux of the white dwarf, as revealed from the X-Shooter residual cool subdwarf spectrum that results from subtracting the best-fit white dwarf model spectrum; see Fig 4) and the far-infrared WISE³¹ w_1w_2 magnitudes, where the white dwarf flux contribution is also negligible. For each catalogue we adopted a search radius of $3''$. No 2MASS³², VISTA³³ or extra infra-red magnitudes from other surveys were found for our target. In this way we built the observational SED of the cool subdwarf from the optical to the far-infrared wavelength range.

Two physical parameters were obtained from the VOSA SED fits, the effective temperature and the bolometric luminosity. The effective temperature was constrained to be 3600–3700 K, depending on the adopted model. Considering that the intrinsic error provided by VOSA is 50 K, we assumed a value of 3650 ± 50 K for the cool subdwarf. The luminosities varied from $(4.2 \pm 2.4) \times 10^{-3} L_\odot$ to $(4.4 \pm 2.4) \times 10^{-3} L_\odot$ and we thus adopted a value of $(4.3 \pm 2.4) \times 10^{-3} L_\odot$. The large luminosity uncertainty is directly related to the distance error. These calculated values of effective temperature and bolometric luminosity translate into a radius of $0.164 \pm 0.050 R_\odot$ from the Stefan-Boltzmann equation, in good agreement with the radius derived from the light-curve fitting ($0.1669 \pm 0.0007 R_\odot$).

For illustrative purposes, in Figure 4 we show the observational SED built together with the synthetic spectrum that best fits the photometric data. The synthetic spectrum is an excellent match to the observed SED.

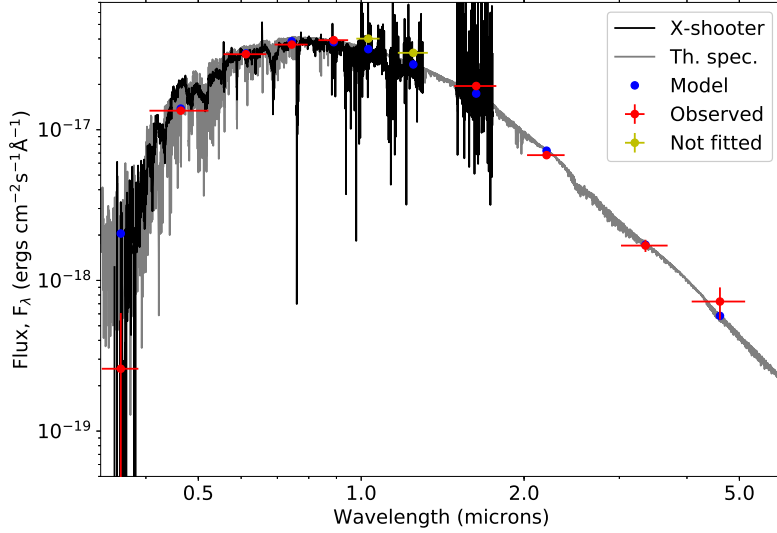


Figure 4. The observational SED of the cool subdwarf in SDSS J2355+0448 (black line, note the white dwarf contribution has been subtracted) and its best-fit model performed by VOSA (gray line). The observational photometric points are shown in red (optical points are obtained by us directly from the light curve during white dwarf eclipse) and the blue dots are the synthetic photometry. The yellow dots are UKIDSS yj photometry that have not been used in the fit due to white dwarf flux contamination. The error bars represent $\pm 1\sigma$ uncertainties.

The metallicity class and the [Fe/H] abundance of the cool subdwarf star

The parameter $\tau_{\text{TiO}/\text{CaH}}$ ^{6,34} is a good indicator of the metallicity class of a dwarf star. It is based on the flux ratio at specific wavelength ranges and quantifies the weakening of the TiO band strength due to the effect of metallicity. In order to calculate a reliable value of this ratio for the cool subdwarf, we subtracted the white dwarf contribution from the X-Shooter spectrum of SDSS J2355+0448. In this case, since we have measured the radial velocities of the cool subdwarf, we were able to correct the orbital motion of the star and hence combine all spectra to one single (averaged) spectrum. To subtract the white dwarf's flux contribution we considered a white dwarf model atmosphere spectrum of the same effective temperature and surface gravity values as derived for the white dwarf in this system (see Table 1), obtained by interpolating these parameters in our full white dwarf model atmosphere grid⁷ and scaled in flux. We thus calculated a value of $\tau_{\text{TiO}/\text{CaH}} = 0.095$ from the residual cool subdwarf spectrum, i.e. an ultra-low metallicity usd spectral class^{6,34}. Using three different calibrators, this translates into an iron abundance of $[\text{Fe}/\text{H}] = -1.6 \pm 0.2 \text{ dex}$ ⁵, $-1.1 \pm 0.2 \text{ dex}$ ³⁵ and $-1.5 \pm 0.3 \text{ dex}$ ⁷. The possible value for the [Fe/H] abundance of the cool subdwarf ranges then from -0.9 to -1.8 dex . However, a usd metallicity class implies $[\text{Fe}/\text{H}] < -1.35 \text{ dex}$ ⁷ and we hence assume the [Fe/H] abundance should be within -1.35 and -1.8 dex , i.e. $[\text{Fe}/\text{H}] = -1.55 \pm 0.25 \text{ dex}$. We also made use of iSpec²⁵, an open source framework for spectral analysis, to attempt to determine the [Fe/H] abundance of the cool subdwarf star. However, the value obtained is subject to large uncertainties ($[\text{Fe}/\text{H}] = -2.1 \pm 2 \text{ dex}$) due to the relatively low signal to noise ratio as well as the intermediate resolution of our spectra (see the Methods section for details).

To determine the spectral sub-type of the usd star we re-applied our decomposition/fitting routine to the averaged X-Shooter optical spectrum, using a usd spectral library of 27 templates⁶ instead. The spectral sub-type obtained in this way for the low-metallicity star is usdK7.

The past and future evolution of SDSS J2355+0448

Given its short orbital period, the binary star SDSS J2355+0448 has very likely evolved in the past through a common envelope phase³⁷. The young cooling age of the white dwarf implies such an event took place very recently and that for most of its life the binary star was very likely composed of two low-mass low-metallicity main-sequence stars. The low mass measured for the white dwarf implies the common envelope phase truncated the evolution of the white dwarf precursor when it was ascending the giant branch. Thus, the white dwarf core is expected to be composed mainly of helium. It has to be noted however that the common envelope phase is not expected to have modified the parameters of the cool subdwarf. This is because secondary stars are not envisaged to be able to accrete the overflowing material during a common envelope episode due to their long thermal time-scales²⁹, a hypothesis that seems to be observationally confirmed²⁰. Because the common envelope truncated the evolution of the white dwarf progenitor, we are not able to derive the white dwarf's progenitor mass using an initial-to-final mass relation for single stellar evolution^{40,41} nor derive a total age for the system. It is important to emphasise however that

the current age of SDSS J2355+0448 is likely to be very old ($\gtrsim 10$ Gyr) given the low metallicity of the star. Indeed, the space velocity with respect to the local standard of rest $(U, V, W) = (-36.5 \pm 29.3, -208.3 \pm 24.8, 3.7 \pm 17.3)$ km/s derived from *Gaia* data adopting the systemic velocity we measured for the binary is consistent with halo membership for this object, although we cannot rule out a thick disk origin¹¹. Due to the short orbital period, the cool subdwarf in SDSS J2355+0448 is tidally locked to the white dwarf (the ellipsoidal modulation can clearly be seen in Figure 3), therefore its rotational period is commensurate with the orbital period. This fast rotation induces chromospheric activity on the cool subdwarf (see a light-curve displaying a flare in Supplementary Figure 2).

We used the binary stellar evolution code `binary_c`^{27,28} (see a full description in the Methods section), based on the BSE code²⁹, to predict the future evolution of SDSS J2355+0448. The results obtained indicate that a phase of stable mass transfer will ensue in $\simeq 800$ Myr. The system will then become a semi-detached cataclysmic variable. We note however that the evolutionary timescale prior to the onset of mass transfer should be taken with caution since the angular momentum loss mechanism/s that bring the two stars closer are not yet fully understood.

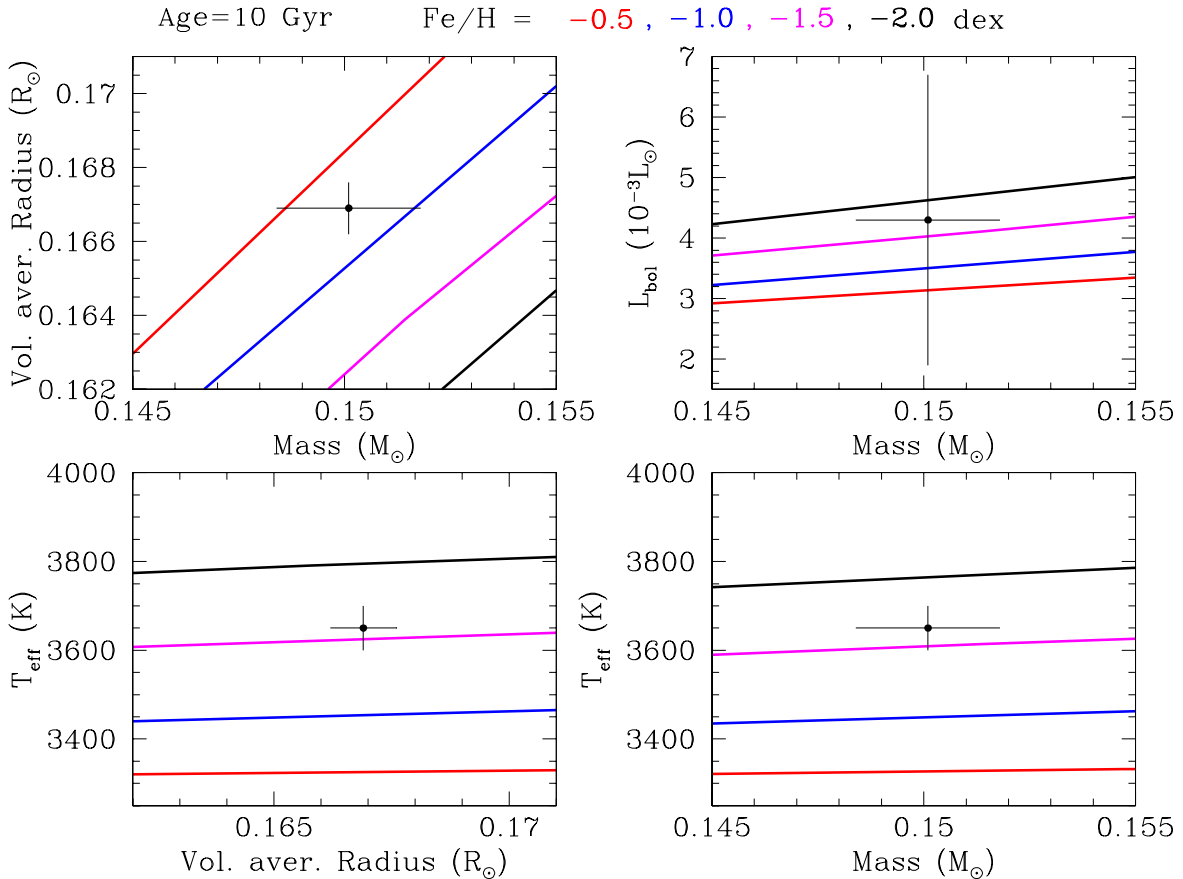


Figure 5. The observed stellar parameter relations of the cool subdwarf in SDSS J2355+0448 (black solid dots; the error bars represent $\pm 1\sigma$ uncertainties) as compared to the theoretical relations^{44,45} for an age of 10 Gyr and $[\text{Fe}/\text{H}]$ values from -0.5 to -2.0 dex (solid lines).

Discussion

We show a comparison between the observed parameter relations for the cool subdwarf in SDSS J2355+0448 and those expected from the theoretical Dartmouth isochrones^{44,45} in Figure 5. Inspection of the Figure reveals that the theoretical relations agree well with our measured values when assuming an $[\text{Fe}/\text{H}]$ abundance of -1.5 dex (a value which is in excellent agreement with our estimate of -1.55 ± 0.25 dex), except for the theoretical mass-radius relation, which yields a slightly overestimated radius for the measured mass. This could be due to uncertainties in the adopted limb-darkening coefficients for the cool subdwarf when performing our light-curve fit (see the Methods section for further details). Alternatively, an over-sized radius could be a consequence of the cool subdwarf star being magnetically active (see Supplementary Figure 2).

Over-inflated radii are often measured for magnetically active low-mass main-sequence stars of solar metallicity²⁰. It is also important to note that the measured radius of the cool subdwarf is undersized compared to solar metallicity models^{45,46}, which is consistent with the theory that cool subdwarfs should have smaller radii for a given effective temperature (see Supplementary Figure 3).

In this paper we have studied in detail the cool subdwarf in the eclipsing binary SDSS J2355+0448. The precise mass and radius we have determined for this star together with the effective temperature and luminosity we have calculated have allowed us to validate the theoretical models of low-mass low-metallicity stars.

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Methods

Observations and their reduction

SDSS J2355+0448 was observed with the medium resolution echelle spectrograph X-Shooter¹ on the 8.2m Very Large Telescope (VLT) in Chile on the nights of the 12th of June 2018 and the 8th of July 2018. X-Shooter consists of three detectors (UVB, VIS and NIR) which obtain simultaneous spectra from the ultraviolet atmospheric cutoff ($\sim 3000\text{\AA}$) to the K band (~ 2.5 microns). SDSS J2355+0448 was observed for a full binary orbit on both nights, recording a total of 12 UVB and VIS spectra and 28 NIR spectra. Exposure times were kept short (1073s, 1088s, 480s in the UVB, VIS and NIR arms respectively) to minimise the amount of orbital smearing of the lines. Due to the faintness of the binary in the near-infrared ($J = 17.5$) the NIR arm spectra have very low signal-to-noise and were not used in any subsequent analysis. The data were reduced using the latest release of the X-Shooter reduction pipeline (version 2.9.3). Standard reduction steps were used to debias, flat-field, extract and wavelength calibrate the data. The spectra were flux calibrated using spectra of the spectrophotometric standard star Feige 110 obtained in twilight at the end of both nights. Finally, all spectra were placed on a heliocentric wavelength scale.

High-speed multi-band photometry of SDSS J2355+0448 was obtained using HiPERCAM² mounted on the 10.4m Gran Telescopio Canarias (GTC). HiPERCAM is a quintuple-beam imager equipped with frame-transfer CCDs allowing simultaneous u , g , r , i and z band imaging at frames rates of up to 1000 frames per second. Note that HiPERCAM uses modified versions of the SDSS filters with much higher throughput, known as Super-SDSS filters. These are denoted as u_s, g_s, r_s, i_s, z_s to distinguish them from the standard SDSS filters ($ugriz$). Exposure times of 5s were used in the g_s, r_s, i_s and z_s bands and 15s in the u_s band. SDSS J2355+0448 was observed for a full orbit on the night of the 5th of October 2018, and 50 minutes of data were obtained around the secondary eclipse on the nights of the 31st of October 2018 and 1st of November 2018. The data were reduced using the dedicated HiPERCAM pipeline, including debiasing, flat-fielding and fringe correction in the z_s band. Differential photometry was performed using the nearby star SDSS J235517.21+045057.1 as a reference source. All times were converted to the barycentric dynamical timescale, corrected to the solar system barycentre, MJD(BTDB).

The spectral decomposition/fitting technique

The decomposition/fitting routine used in this work³ was developed to derive spectroscopic stellar parameters of white dwarf plus M dwarf binaries, namely the spectral sub-type of the M dwarf and its radius, and the effective temperature (T_{eff}), surface gravity ($\log g$), mass and radius of the white dwarf. It uses an evolution strategy⁴ to decompose the observed spectrum into the two stellar components. To that end it optimises a fitness function (i.e. a weighted χ^2). The only difference between the original routine and the one employed in this work is adopting a series of cool subdwarf template spectra^{5,6} instead of the original 10 M dwarf templates.

The routine fits first the entire spectrum and selects the best-fit cool subdwarf template, which is scaled in flux and subtracted. Consequently, the residual white dwarf spectrum is fitted with a grid of hydrogen-rich white dwarf model atmosphere spectra⁷. The grid includes 1,339 spectra covering the 6,000-100,000 K T_{eff} and the 6.5-9.5 dex $\log g$ values. The fit is performed to the normalised H β to H10 Balmer lines (the H α line is excluded in this process since it covers a wavelength range of largest residual contamination from the cool subdwarf). A bi-cubic spline interpolation to the χ^2 values on the $T_{\text{eff}} - \log g$ grid is used to derive the best-fit T_{eff} and $\log g$. The errors (1σ uncertainties) are calculated projecting the $\Delta\chi^2 = 1$ contour around the χ^2 of the best fit into the T_{eff} and $\log g$ axes. This results in a range of parameters which are averaged into symmetric error bars (see the top panels of Supplementary Figure 1).

Since the equivalent widths of the Balmer lines of white dwarfs reach a maximum for effective temperatures near 13 000 K, the Balmer line profile fits provide two sets of T_{eff} and $\log g$ values, which are generally known as the “hot” and “cold” solutions. In other words, similar fits can be achieved on both temperature sides at which the maximum equivalent width takes place. To break this degeneracy the routine makes use of the model spectra grid for fitting the entire spectrum over the wavelength range 3850 – 7150 Å (see the bottom panel of Supplementary Figure 1). The red part of the spectrum is not considered by the fit due to possible distortions in the residual white dwarf spectrum arising from subtraction of the cool subdwarf. The T_{eff} and $\log g$ values derived from the fit to the whole spectrum are used to discard one of the “hot”/“cold” solutions. In the case of SDSS J2355+0448, the best-fit T_{eff} and $\log g$ from the whole spectrum agrees with the one obtained by the “hot” solution (see the top-right panel of Supplementary Figure 1).

The radial-velocity fitting method and the periodogram

We fitted the CaII absorption triplet at $\sim 8500\text{Å}$ sampled by the X-Shooter VIS arm spectra with a triple-Gaussian absorption profile of fixed separation (see an example in Supplementary Figure 4). To that end we fixed the width of each Gaussian, however we set the three amplitudes and the radial velocity of the cool subdwarf star as free parameters. This fitting method has been shown to provide both accurate and precise M dwarf radial velocities in binary systems with white dwarf companions such as the one studied in this work⁸.

We run a Lomb-Scargle periodogram⁹ to the radial velocities of the cool subdwarf in SDSS J2355+0448, which unfortunately contained several aliases as a consequence of the sampling pattern of the observations. We thus tried the ORT/TSA¹⁰ command in MIDAS, which provided a periodogram with a clear pick at 11.139d^{-1} . The ORT/TSA routine uses a grid of trial periods to fold and phase-bin the data and subsequently fits the folded radial velocity curve with a series of Fourier terms.

The light-curve fitting method

We fitted the HiPERCAM light curves of SDSS J2355+0448 (see Figure 3) using a code written for binaries containing white dwarfs^{11,12}. Each stellar component in the binary is subdivided into small elements by the program. This is performed by following a geometry that is fixed by the radius of the considered star as measured along the direction of centres towards the other star. The code takes into account limb- and gravity-darkening, gravitational microlensing, Roche geometry distortion, irradiation effects and eclipses. It uses a non-linear four-parameter model to implement limb-darkening¹³, of the form

$$\frac{I(\mu)}{I(1)} = 1 - \sum_{k=1}^4 a_k (1 - \mu^{\frac{k}{2}}), \quad (2)$$

being $\mu = \cos \phi$ (where ϕ is the angle between the emergent flux and the line of sight), and $I(1)$ the monochromatic specific intensity at the centre of the stellar disk. Supplementary Table 1 lists the adopted limb-darkening coefficients for the white dwarf¹⁴ and cool subdwarf¹⁵.

The model requires a set of additional parameters to be defined, namely the binary inclination i , the mass ratio $q = M_{\text{sd}}/M_{\text{WD}}$, the orbital period P_{orb} , the sum of the unprojected stellar orbital speeds $V_s = (K_{\text{WD}} + K_{\text{sd}})/\sin i$, the mid-time when the white dwarf eclipse occurs T_0 , the radii of the stars scaled by the orbital separation R_{WD}/a and R_{sd}/a , and the temperatures of the stars $T_{\text{eff,WD}}$ and $T_{\text{eff,sd}}$ (is has to emphasised that temperatures are flux scaling parameters, therefore correspond only approximately to the real temperatures). All these parameters were considered as free when fitting the HiPERCAM light curves, the only exceptions were the white dwarf temperature, which was fixed at 13,250 K (Table 1) and the orbital period, which was fixed to the value found from the Catalina Sky Survey results. We phase-folded all of our HiPERCAM observations in order to combine data taken on different nights.

The information provided by the profile of the white dwarf eclipse is not sufficient to determine the radii of both stars as well as the orbital inclination. As a consequence, the fitting program requires additional information¹⁶ to break the degeneracy between the scaled radii and the inclination. This can be provided by the distorted shape of the cool subdwarf owing to its proximity to the white dwarf, which results in a double-peaked feature in the light-curve known as ellipsoidal modulation. Unfortunately, the fits to this double-peaked modulation highly depend on the adopted limb-darkening coefficients for the cool subdwarf as well as the presence of any star-spots. This is a particularly large problem in the case of the cool subdwarf star in SDSS J2355+0448 because of the uncertainty in its metallicity. Adopting the limb darkening parameters for a $[\text{Fe}/\text{H}] = -1$ dex or $[\text{Fe}/\text{H}] = -3$ dex star changes the resulting mass and radius values by 10 and 15 per cent from the $[\text{Fe}/\text{H}] = -2$ dex parameters (note that only these three $[\text{Fe}/\text{H}]$ abundance values are available for acquiring the limb-darkening coefficients¹⁵), meaning that fits relying on the amplitude of the ellipsoidal modulation are quite uncertain.

We managed to break the degeneracy between the scaled radii and the inclination by measuring the depth of the secondary eclipse (see Figure 3), an approach that allowed us to measure precise parameters for the stars. It has to be stressed that following this procedure considerably alleviates the dependence of the measured parameters with the adopted limb-darkening

coefficients for the cool subdwarf star, i.e. the resulting masses and radii change by only 1.5 and 2 per cent in this case depending on the adopted value of $[\text{Fe}/\text{H}]$, comparable to our measured uncertainties. However, the lack of a direct determination of the radial velocity semi-amplitude of the white dwarf K_{WD} implied that we were not able to measure the masses and radii of the white dwarf and the cool subdwarf independently of any theoretical model. Fortunately, a recent observational study shows that the white dwarf measured radii in eclipsing binaries are in excellent agreement with theoretical expectations¹⁶. Therefore, we adopted the white dwarf’s radius to follow the theoretical mass-radius relationship for a 13,250 K helium-core white dwarf with a thick surface hydrogen envelope¹⁷ when fitting the HiPERCAM light curves. We allowed some departure from the relation to account for a 500 K uncertainty in the white dwarf temperature. Note that the radii of very low metallicity ($[\text{Fe}/\text{H}] < -3$ dex) white dwarfs are 1-2 per cent larger than solar metallicity white dwarfs¹⁸, which is comparable to the departure allowed to account for the temperature uncertainty.

For determining the distributions of our model parameters we employed the Markov Chain Monte Carlo (MCMC) method¹⁹. We based the likelihood of accepting a model on a combination of the χ^2 of the light-curve fit to the data and an additional prior probability whereby we ensure that k_{sd} is consistent with the spectroscopic result and that the white dwarf’s radius is consistent with the mass-radius relationship outlined above. For each band, the approximate best parameters and covariances were determined using an initial MCMC chain. These approximate best parameters were then considered as the starting values for longer chains which were employed to derive the final model values and their uncertainties. We simultaneously run four chains in order to ensure that they converged on the same values, with the initial approximated best parameters slightly perturbed. From each chain, the 50,000 first points were classified as a “burn-in” phase and were removed for the subsequent analysis. Each chain had a total length of 250,000 points.

The full light curves and model fits are shown in Figure 3. The parameters that result from the u_s and g_s band fits have associated large uncertainties since these bands are dominated by the white dwarf flux and therefore contain relatively little information regarding the inclination. The secondary eclipse is only detected in the i_s band and therefore the tightest constraints come from these data.

It is important to emphasise the light-curve fitting code provides both the tidally-distorted radius of the cool subdwarf (towards the white dwarf) as well as its volume-averaged radius (Table 1). We adopted the latter in our analysis, which is expected to make the effects of tidal distortion negligible when comparing the observed to the theoretical relations for this star²⁰.

The VOSA spectral energy distribution fitting routine

Different statistical tests may be employed by VOSA for determining which model fits best the observational data. In our case, we used the χ^2 statistical test between the model spectra and the observed photometry to derive the effective temperature and luminosity of the cool subdwarf. Good fits are achieved by VOSA when the parameter $V_{\text{gfb}} < 10-15$. V_{gfb} is defined as the modified reduced χ^2 and it is calculated by forcing $\sigma(F_{\text{obs}}) > 0.1 \times F_{\text{obs}}$, where $\sigma(F_{\text{obs}})$ is the error of F_{obs} (the observed flux).

The SED was compared to three different grids of synthetic spectra, namely BT-Settl, BT-NextGen (AGSS2009) and BT-NextGen (GNS93)²¹. We note that we did not use other available libraries within VOSA due to the lack of models at low metallicities. During the fitting we accounted for interstellar extinction²² and used the Bayesian distance²³ derived from the measured *Gaia* parallax and its uncertainty²⁴ as the distance (541_{-124}^{+216} pc). We fixed the surface gravity to be within the range 5–5.5 dex, thus covering the 5.16 dex value that results from our mass and radius determinations from the light curve fit. Finally, the metallicity (i.e. Fe/H abundance) was assumed to be lower than -1 dex, consistent with that of an usd star. In all cases $V_{\text{gfb}} < 15$, with our best-fit model achieving $V_{\text{gfb}} = 6.6$, which corroborates the goodness of our fit.

VOSA uses the bolometric flux and the distance to determine the luminosity. The bolometric flux is obtained integrating the flux using the observational photometric points. In cases where the SED is not covered by the observational photometry, VOSA uses the best-fit theoretical model.

The iSpec [Fe/H] determination

The metallicity, in particular the $[\text{Fe}/\text{H}]$ abundance, of the cool subdwarf of SDSS J2355+0448 was additionally estimated using iSpec²⁵, a code for the treatment and analysis of stellar spectra. iSpec allows determining the atmospheric stellar parameters (including the effective temperature, surface gravity, metallicity, micro- and macro-turbulence, rotation) and individual chemical abundances for FGKM stars via two different methods: (1) the synthetic spectral fitting technique and (2) the equivalent widths method. Here, we adopted the synthetic spectral fitting technique. This is implemented by iSpec via minimizing the χ^2 between a given observed spectrum and an adopted library of synthetic spectra. We applied the synthetic spectral fitting technique to the observed (combined and white dwarf subtracted) X-Shooter spectrum of SDSS J2355+0448.

iSpec requires the user to mask the lines and corresponding segments to be used in the fitting. To that end we used the Fe I, Fe II, Ca I, Ca II, Na I, Na II, K I, K II absorption lines located within the 5500–9000 Å wavelength range sampled by the combined and white dwarf subtracted X-Shooter VIS arm spectrum. To do the computation of the χ^2 , iSpec used the GES (*Gaia* ESO survey) atomic line lists. The synthetic spectra were computed using the MARCS²⁶ model atmosphere library

and the SPECTRUM code within iSpec. An initial set of atmospheric parameters is also required prior to the fitting. We used $T_{\text{eff}} = 3650 \text{ K}$ (based on our VOSA fitting results), $\log g = 5.16 \text{ dex}$ (based on the mass and radius determined from the light curve fitting), $[M/H] = -1.55 \text{ dex}$ (we used the $[\text{Fe}/\text{H}]$ abundance derived from the $\tau_{\text{TiO}/\text{CaH}} = 0.095$ ratio as a proxy for metallicity), $[\alpha/\text{Fe}] = 0 \text{ dex}$, micro-turbulence velocity $V_{\text{mic}} = 1.05 \text{ km s}^{-1}$, macro-turbulence velocity $V_{\text{mac}} = 4.21 \text{ km s}^{-1}$, $v \sin(i) = 94.3 \text{ km s}^{-1}$ (obtained from the measured orbital period of the binary and radius of the cool subdwarf, together with the known binary inclination), limb darkening coefficient = 0.6, resolution $R = 8,900$ (set by our X-Shooter VIS spectrum) and radial velocity = 0 km s^{-1} (since the rest-frame radial velocity correction was performed before the fitting). The initial guesses of T_{eff} , $\log g$, $v \sin(i)$, R and radial velocity were fixed during the fitting process and the maximum number of iterations was set to 10. This resulted in a value of $[\text{Fe}/\text{H}] = -2.1 \pm 2 \text{ dex}$ for the cool subdwarf star.

The binary_c stellar evolution code

We predict the future evolution of SDSS J2355+0448 by means of the binary stellar evolution code `binary_c`^{27,28}, a software for the evolution of single and binary stars, calculations of stellar populations and nucleosynthesis analysis. `binary_c` updates and enhances the BSE (Binary Star Evolution) code²⁹, providing stellar evolution for stars in the range 0.1 to $100 M_{\odot}$. In order to simulate the evolution of a given binary star, `binary_c` requires a set of initial parameters such as the mass, stellar type (i.e. main sequence star, white dwarf, etc.), metallicity and rotational velocity of each star, as well as the orbital period, eccentricity and orbital separation of the binary. In all cases, except for the rotational velocity of the white dwarf and the metallicity of the stars, the input parameters are tightly constrained from our observations (note that the eccentricity must be zero for such a close binary star) and we hence used the observed values as input parameters in the simulation. We assumed a rotational velocity of 0 km s^{-1} for the white dwarf and we considered an $[\text{Fe}/\text{H}]$ abundance of -1.55 dex for the cool subdwarf. Additional parameters/assumptions are required by `binary_c` regarding explosions (not relevant in our case), Roche-lobe overflow, common envelope efficiency, winds and nucleosynthesis (also not relevant in our case). In those cases we assumed the standard values as provided by `binary_c`. We note however that modifying these assumptions had no dramatic effect in the evolutionary paths expected for SDSS J2355+0448, except slight changes in the evolutionary timescales.

Code availability statement

The spectral/decomposition routine and the radial-velocity fitting method used in this work are not publicly available. The light-curve fitting method is available at <https://github.com/trmrsh/cpp-lcurve>. MIDAS is available at <https://www.eso.org/midas/>. VOSA is available at <http://svo2.cab.inta-csic.es/theory/vosa/>. iSpec is available at <https://www.blancocuaresma.es/iSpec/>. The `binary_c` stellar evolution code is available at https://www.ast.cam.ac.uk/~rgi/binary_c.html. The X-Shooter reduction pipeline (version 2.9.3) is available at <https://www.eso.org/sci/software/pipelines/xshooter/> and the dedicated HiPERCAM pipeline at <https://github.com/HiPERCAM/hipercam>.

Data availability statement

Based on observations made with the Gran Telescopio Canarias (GTC), installed in the Spanish Observatorio del Roque de los Muchachos of the Instituto de Astrofísica de Canarias, in the island of La Palma (program GTC21-18B). Based on observations made with ESO Telescopes at the La Silla Paranal Observatory under programme ID 2100.D-5022(A).

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Figures 1, 3 and 4 and Supplementary Figures 1, 2 and 4 have associated raw data. The data that support the plots within this paper and other findings of this study are available from the corresponding author upon reasonable request.

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Author contributions statement

All authors have contributed to the work presented in this paper. A.R.M. performed the decomposition and fitting of the spectra, carried out the entire spectral analysis (except the one required by *iSpec*), conducted the VOSA analysis and led the writing of the manuscript. S.G.P. reduced all the spectroscopic and photometric data and carried out the light-curve analysis. V.S.D. and S.P.L. performed the GTC observations. J.J.R. conducted the *iSpec* analysis. V.S.D., S.P.L. and T.R.M. contributed to the development of HiPERCAM, a vital instrument for obtaining the results of this work. S.T. carried out the *binary_c* simulation and calculated the cooling age of the white dwarf. A.R.M., S.G.P. and J.J.R. discovered the system. All authors reviewed the manuscript.

Additional information

Competing Interests. The authors declare that they have no competing financial interests.

Parameter	g_s	r_s	i_s	z_s
WD a_1	0.6882	0.6126	0.5782	0.5530
WD a_2	0.1635	0.0232	-0.1761	-0.3300
WD a_3	-0.4165	-0.1818	0.0999	0.3024
WD a_4	0.1915	0.0823	-0.0386	-0.1209
sd a_1	-0.4633	-0.6869	-0.3228	-0.1407
sd a_2	2.3583	3.9532	2.9078	2.2760
sd a_3	-1.4110	-3.7931	-2.8289	-2.2345
sd a_4	0.1903	1.1713	0.8566	0.6676
sd grav. darkening	1.1211	0.7539	0.6513	0.5731

Table 2. Limb- and gravity-darkening coefficients used during our light curve fitting for the g_s , r_s , i_s and z_s bands. The white dwarf limb-darkening coefficients (WD a_1 to WD a_4) are for a $T_{\text{eff}} = 13,250$ K, $\log g = 7.75$ dex white dwarf. The cool subdwarf limb-darkening (sd a_1 to sd a_4) and surface gravity (sd grav. darkening) coefficients are for a $T_{\text{eff}} = 3,650$ K, $\log g = 5.0$ dex, $[\text{Fe}/\text{H}] = -2.0$ dex star.

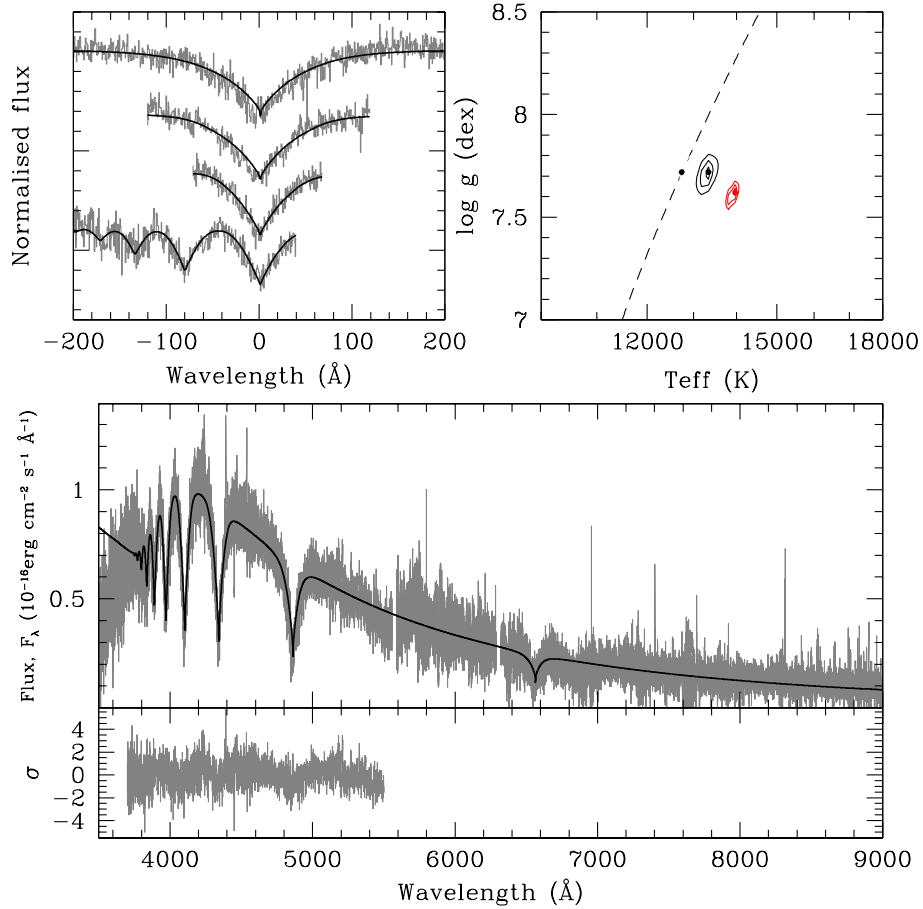


Figure 6. Spectral model fits to the residual white dwarf spectrum of SDSS J2355+0448, obtained after subtracting the best-fit cool subdwarf template (Figure 1). Top left panel: from top to bottom the best-fit (black line) to the normalised $H\beta$ to $H10$ (gray) line profiles. Top right panel: 3, 5, and 10σ χ^2 contour plots in the $T_{\text{eff}} - \log g$ plane. Black contours indicate the best line profile fits, whilst red contours the best-fit to the entire spectrum. The maximum $H\beta$ equivalent width is indicated by a dashed line. Black dots indicate the best “hot” and “cold” line profile solutions, the red dot indicates the best fit to the whole spectrum. Bottom panel: the residual white dwarf spectrum after subtracting the cool subdwarf (gray line) together with the best-fit white dwarf model (black line) and the residuals (gray line, bottom). The fit to the whole spectrum selects the “hot” solution.

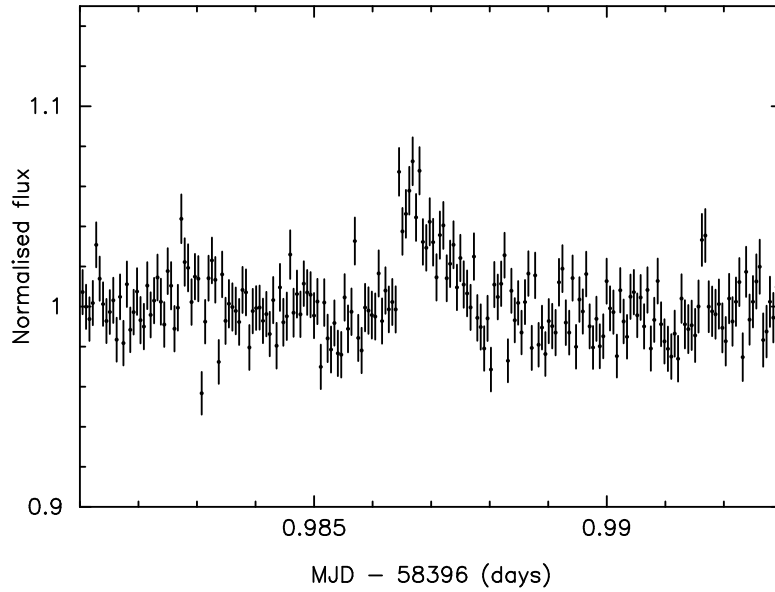


Figure 7. g_s -band HiPERCAM light-curve of SDSS J2355+0448 displaying a flare originating in the surface of the cool subdwarf star. The error bars represent $\pm 1\sigma$ uncertainties.

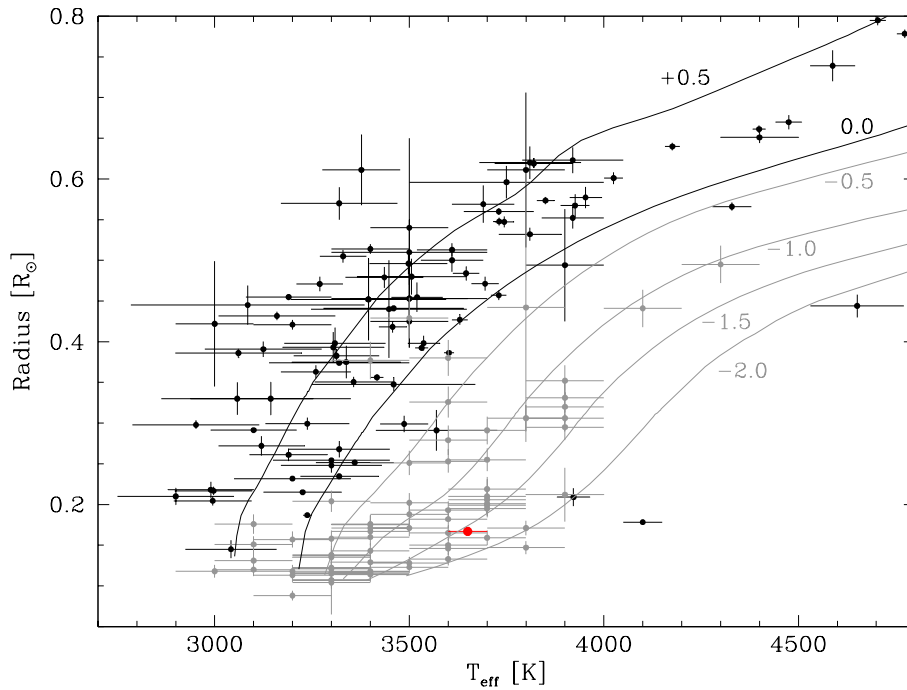


Figure 8. Radius-effective temperature plot for a compilation of low-mass solar-metallicity stars (black) and for a compilation of cool subdwarfs (grey). The solid lines are the Dartmouth theoretical tracks for 10 Gyr and the indicated $[\text{Fe}/\text{H}]$ abundances (in dex units). The red solid dot represents the cool subdwarf studied in this work. The error bars represent $\pm 1\sigma$ uncertainties.

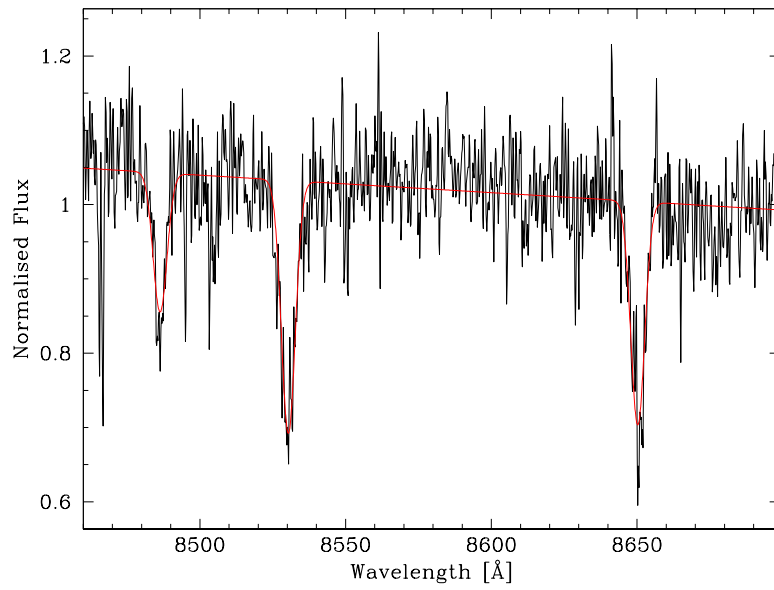


Figure 9. Fit (red solid line) to the normalised Ca II triplet at $\sim 8500\text{\AA}$ of a X-Shooter spectrum (black solid lines).