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# **Single breath-held acquisition of co-registered 3D $^{129}\text{Xe}$ lung ventilation and anatomical proton images of the human lung with compressed sensing**

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**Word count:** (1830 words, 3 figures, 2 tables)

**Running title:** Rapid acquisition of  $^{129}\text{Xe}$  and  $^1\text{H}$  lung MR images with CS

**Key Words:** hyperpolarized gases, lungs, compressed sensing

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**ABSTRACT:** (249/250 words max)

**Purpose:** To develop and assess a method for acquiring co-registered proton anatomical and hyperpolarized  $^{129}\text{Xe}$  ventilation MR images of the lungs with compressed sensing (CS) in a single breath-hold.

**Methods:** Retrospective CS simulations were performed on fully sampled ventilation images acquired from one healthy smoker to optimize reconstruction parameters. Prospective same-breath anatomical and ventilation images were also acquired in five ex-smokers with an acceleration factor of 3 for hyperpolarized  $^{129}\text{Xe}$  images, and were compared to fully sampled images acquired during the same session. The following metrics were used to assess data fidelity: mean absolute error (MAE), root mean square error (RMSE) and linear regression of the signal intensity between fully sampled and under-sampled images. The effect of CS reconstruction on two quantitative imaging metrics routinely reported (percentage ventilated volume %VV and heterogeneity score) was also investigated.

**Results:** Retrospective simulations showed good agreement between fully sampled and CS-reconstructed (acceleration factor of 3) images with MAE (RMSE) of 3.9% (4.5%). The prospective same-breath images showed a good match in ventilation distribution with an average R-squared of 0.76 from signal intensity linear regression and a negligible systematic bias of +0.1% in %VV calculation. A bias of -1.8% in the heterogeneity score was obtained.

**Conclusion:** With CS, high quality 3D images of hyperpolarized  $^{129}\text{Xe}$  ventilation (resolution  $4.2 \times 4.2 \times 7.5 \text{ mm}^3$ ) can be acquired with co-registered  $^1\text{H}$  anatomical MRI in a 15 s breath-hold. The accelerated acquisition time dispenses with the need for registration between separate breath-hold  $^{129}\text{Xe}$  and  $^1\text{H}$  MRI enabling more accurate %VV calculation.

**Key Words:** hyperpolarized  $^{129}\text{Xe}$  gas, lung MRI, compressed sensing

## INTRODUCTION

Lung ventilation MRI with hyperpolarized (HP) noble gases ( $^3\text{He}$  and  $^{129}\text{Xe}$ ) provides high spatial resolution images of inhaled gas distribution within the lungs. The technique has been shown to be sensitive to different obstructive lung diseases, e.g. chronic obstructive pulmonary disease (1-3), cystic fibrosis (4,5) and asthma (6-8). The acquisition of  $^1\text{H}$  MR images of the lung is usually performed in the same MRI session in order to observe lung anatomy and structure, but also to delineate the lung cavity for the calculation of the commonly reported percentage ventilated volume (%VV), which is the percentage of the thoracic cavity volume containing HP gas. Both structural and ventilation images are usually obtained in two separate breath-holds and therefore a registration step is required to align the two set of images (3). We have previously demonstrated that same-breath acquisition of both  $^1\text{H}$  structural and HP gas ventilation MRI (9) provides a more robust method to calculate %VV (10). This approach has been applied to HP  $^3\text{He}$  ventilation images with compressed sensing (CS) to further shorten the image acquisition time (11), which is important for patients with lung pathologies that make sustained breath-hold challenging. With the limited supply and rising cost of  $^3\text{He}$  gas,  $^{129}\text{Xe}$  provides a cost-effective alternative to  $^3\text{He}$  (6). But due to its lower gyromagnetic ratio, lower bandwidths are required to obtain reasonable SNR, which increases the acquisition time. As a result, same-breath whole lung coverage acquisition of HP  $^{129}\text{Xe}$  ventilation and  $^1\text{H}$  anatomical images has been challenging and only recently performed using non-Cartesian sampling strategies (12). The purpose of this work is to apply the CS technique (13) to accelerate the acquisition of 3D  $^{129}\text{Xe}$  ventilation images and enable same-breath acquisition of co-registered anatomical  $^1\text{H}$  images. Additionally, the effect of CS reconstruction on two quantitative imaging metrics routinely reported (%VV and heterogeneity score  $H_{\text{score}}$ ) is also investigated.

## METHODS

A fully sampled (FS) 3D HP  $^{129}\text{Xe}$  ventilation dataset was acquired on a GE HDx 1.5T MR scanner using 1 L of  $^{129}\text{Xe}$  at ~13% polarization from one healthy smoker (male, 31 years,  $\text{FEV}_1$  z-score > -1.64) in order to perform retrospective CS simulations and optimize the reconstruction parameters. A quadrature flexible transmit-receive  $^{129}\text{Xe}$  radiofrequency coil (CMRS, Brookfield, WI) was used and imaging parameters were as follows: 3D balanced steady-state free precession (bSSFP)

pulse sequence (14),  $96 \times 78 \times 32$  matrix,  $\text{FOV} = 40 \times 32.5 \times 24 \text{ cm}^3$ ,  $\text{TE/TR} = 3.6/7.6 \text{ ms}$ , bandwidth =  $\pm 8.06 \text{ kHz}$ , scan time of 19 s. An anatomical  $^1\text{H}$  image was acquired in a separate breath with a fast spoiled gradient recalled sequence (SPGR) with the same resolution,  $\text{FOV} = 40 \times 40 \times 24 \text{ cm}^3$ ,  $\text{TE/TR} = 0.6/1.9 \text{ ms}$ , bandwidth =  $\pm 83.3 \text{ kHz}$ , partial-Fourier encoding in the frequency direction and acquisition time of 6 s. The CS simulations were performed in MATLAB (MathWorks, Natick, MA) as described previously (15-17) by empirically testing different undersampling patterns for acceleration factors (AF) of 2, 3, 4 and 5 with different sets of weights that balance data fidelity, image total variation and image sparsity terms in the iterative reconstruction algorithm adapted from Lustig et al (13). The CS reconstruction fidelity was evaluated with different image metrics including mean absolute error (MAE), root mean square error (RMSE) and pixel by pixel linear regression of the signal intensity (images normalized between 0 and 1). The reconstructed and reference FS images at the original acquired size were used and a manually segmented ventilated volume served as the region of interest for the errors and linear regression calculation. The heterogeneity score  $H_{\text{score}}$  (18) was also evaluated.  $H_{\text{score}}$  is an imaging metric of the ventilation heterogeneity and was calculated as follows: for each pixel of the ventilated volume, a local coefficient of variation of the signal intensity in the surrounding pixels is computed  $H_{i,j,k}$ .  $H_{\text{score}}$  is then defined as the mean value of the distribution of  $H_{i,j,k}$ . Finally, %VV was also calculated for each AF and for the fully sampled DICOM images using a semi-automated segmentation software (19).

After CS optimization, additional separate breath FS and same-breath CS-accelerated prospective images of both  $^1\text{H}$  and HP  $^{129}\text{Xe}$  were acquired from five volunteers, all ex-smokers with a smoking history of at least 10 pack years. An AF of 3 (scan time of 6 s) was used for the prospective CS-accelerated  $^{129}\text{Xe}$  ventilated images. The gas mixture consisted of 500 mL of HP  $^{129}\text{Xe}$  (with recently optimized polarization of  $\sim 30 \%$  (20)) and 500 mL of  $\text{N}_2$  mixed into a 1 L Tedlar bag before being delivered to the volunteers in the MRI scanner for inhalation and imaging. All in vivo MRI experiments were performed under the approval of the UK national research ethics committee and the local NHS research office. %VV and  $H_{\text{score}}$  from FS and CS datasets were calculated and compared. Bland-Altman analyses were performed to compare FS and CS global  $H_{\text{score}}$  and slice by slice %VV for all subjects. SNR was calculated for the FS DICOM images selecting a region of interest with fairly homogeneous signal in a middle slice for both lungs. The noise was estimated in a region outside the lung and corrected for Rician distribution according to (21). Additionally,

CS and FS  $^{129}\text{Xe}$  ventilation images were registered to each other to evaluate pixel-by-pixel correlation of signal intensity in the ventilated volume.

## RESULTS

### CS simulations

A good preservation of the ventilation distribution was obtained in retrospectively undersampled and CS-reconstructed images. A summary of estimated errors and quantitative imaging metrics is presented in Table 1. As expected, increasing the AF from 2 to 5 reduced commonalities with the FS reference image, with MAE and RSME increasing from 3.3 to 4.9 %, and 3.8 to 5.9 %, respectively. %VV remained consistent with the FS image value of 94.8 % with differences lying between 0.6 % (AF=2) and 1.5 % (AF=5). A representative coronal slice of a  $^{129}\text{Xe}$  ventilation image for each AF is shown in Figure 1 with the corresponding difference map and pixel by pixel comparison of signal intensity. Linear regression gave the lowest  $R^2$  value of 0.86 for AF=5 and highest  $R^2$  value of 0.95 for AF=2. Image features such as vessels (appearing black on ventilation images) and lung edges were well preserved at low AF but became blurred at higher AF (4 and 5) due to the increased low-pass filtering effect of the CS reconstruction and an increasing loss in high spatial frequencies of the k-space data. High AF also resulted in more homogeneous signal distributions and reduction of  $H_{\text{score}}$  (Figure 2 and Table 1).

### Prospective acquisitions

The sampling pattern used for the prospective acquisition (AF=3) in the 5 volunteers is shown in Figure 2.a. The required total breath-hold time was reduced to 15 s (6 s for anatomical  $^1\text{H}$ , 6 s for HP  $^{129}\text{Xe}$  ventilation plus an additional 3 s delay for the scanner hardware to switch between the two transmit-receive frequencies). Figure 3 shows an example of the improved alignment between  $^{129}\text{Xe}$  (red) and  $^1\text{H}$  images (grayscale) due to the same breath acquisition that is facilitated by CS. Remaining misalignments of much smaller intensity between  $^1\text{H}$  and  $^{129}\text{Xe}$  scans were observed in 2 of the 5 subjects (see example of subject slightly relaxing diaphragm in the period between the back-to-back  $^{129}\text{Xe}$  and  $^1\text{H}$  acquisitions in Figure 3.d). However, these misalignments were of the order of the partial-voluming effect that is present in the anterior and posterior slices and could be improved with better breathing maneuver coaching. A comparison between FS and CS imaging

metrics derived for each subject is presented in Table 2. A mean (range)  $R^2$  value of 0.76 (0.42, 0.90) was obtained for the signal intensity linear regression after registration of the ventilated volumes. The lowest value of 0.42 obtained for subject 3 can be explained by a higher noise level (see SNR in Table 2) and an observed difference in lung inflation level between experiments that could be attributed to a sub optimal breathing maneuver performed by the subject. A mean absolute difference of 1.3 % in global %VV was found between prospective FS and CS data sets. When comparing %VV on a slice by slice basis for all subjects, a Bland-Altman analysis gave a negligible bias of +0.1 % with a confidence interval of -6.7 - 6.8 %. However, a consistently lower  $H_{\text{score}}$  value (Figure 3 and Table 2) was obtained from the CS reconstructed images as previously observed during the CS simulations. A Bland-Altman analysis of  $H_{\text{score}}$  of the 5 subjects was performed showing a bias of  $\sim -1.8$  % (-0.9 - 4.4 %).

## DISCUSSION

We have demonstrated the feasibility of acquiring 3D HP  $^{129}\text{Xe}$  lung ventilation images and anatomical  $^1\text{H}$  images in the same breath using compressed sensing. Results showed minimal estimated errors in the  $^{129}\text{Xe}$  ventilation distribution during CS simulations and a good qualitative and quantitative agreement was found between FS and prospective CS datasets for an AF of 3. While improving the reproducibility and the calculation of %VV through the benefits of obtaining  $^1\text{H}$  and  $^{129}\text{Xe}$  images inherently co-registered in the same breath-hold (10), CS also has a negligible influence on the derived %VV values. The mean absolute difference of 1.3 % in global %VV found between prospective FS and CS data sets is below the previously calculated mean inter-observer error in %VV calculation (2.3%) when analyzing FS images with the same software (19). It is also within the same-day reproducibility confidence interval of %VV measurement ( $\pm 1.52$  %) previously reported in Ebner et al (22). Our results are in line with Qing et al. (11) who previously reported that CS was a good candidate to accelerate the acquisition of  $^3\text{He}$  ventilation and  $^1\text{H}$  images in the same breath without compromising image fidelity. The assessment of the heterogeneity score  $H_{\text{score}}$  of the ventilation distribution however suggests that the resulting images tend to have less high spatial frequency detail than fully sampled images. This systematic difference was to be expected and has limited implications due to the fact that  $H_{\text{score}}$  is already inherently dependent on MRI sequence parameters, such as image resolution or kernel matrix size for local  $H_{i,j,k}$  calculation.  $H_{\text{score}}$  has recently been shown to be an alternative and meaningful

complementary marker to %VV for the description of the ventilation distribution in different population of patients with pulmonary diseases (23) and using CS for the data acquisition should not affect clinical results as long as the same sequence parameters are used between the patient groups being compared. The total acquisition time could be further reduced by applying CS to the proton images as well (e.g. as in (11)). An acceleration factor of 2 for  $^1\text{H}$  imaging for example (instead of current AF of 1.26 due to partial Fourier encoding) would decrease the total scan time from 15 to 13 s.

With the methods presented here we demonstrate the feasibility of acquiring high resolution ventilation images with 500 mL of HP  $^{129}\text{Xe}$  which further establishes the suitability of  $^{129}\text{Xe}$  for clinical imaging and assessment of pulmonary diseases. Further work will focus on the clinical application of the technique in patients with lung pathologies.

## ACKNOWLEDGMENTS

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**Tables:**

Table 1

Errors of the different reconstructions for the coronal image for acceleration factors (AF) of 2 to 5 (MAE: mean absolute error)

AF	MAE	RMSE	H <sub>score</sub>	% VV
1	-	-	15.5 %	94.8 %
2	3.3 %	3.8 %	13.6 %	95.4 %
3	3.9 %	4.5 %	12.6 %	95.5 %
4	4.1 %	4.9 %	12.0 %	95.9 %
5	4.9 %	5.9 %	11.6 %	96.3 %

Table 2

Summary of whole lung metrics and SNR for each subject imaged with FS and CS (AF=3) <sup>129</sup>Xe ventilation MRI

subject	1	2	3	4	5
% VV (FS)	97.5 %	92.2 %	89.6 %	96.1 %	96.6 %
% VV (CS)	98.3 %	93.5 %	90.6 %	93.5 %	95.6 %
H <sub>score</sub> (FS)	14.4 %	20.1 %	21.9 %	17.1 %	17.3 %
H <sub>score</sub> (CS)	13.4 %	18.2 %	18.0 %	16.7 %	15.6 %
r <sup>2</sup>	0.81	0.90	0.42	0.86	0.82
SNR (FS)	34.3	28.4	20.3	35.2	42.5

**Figure captions:**

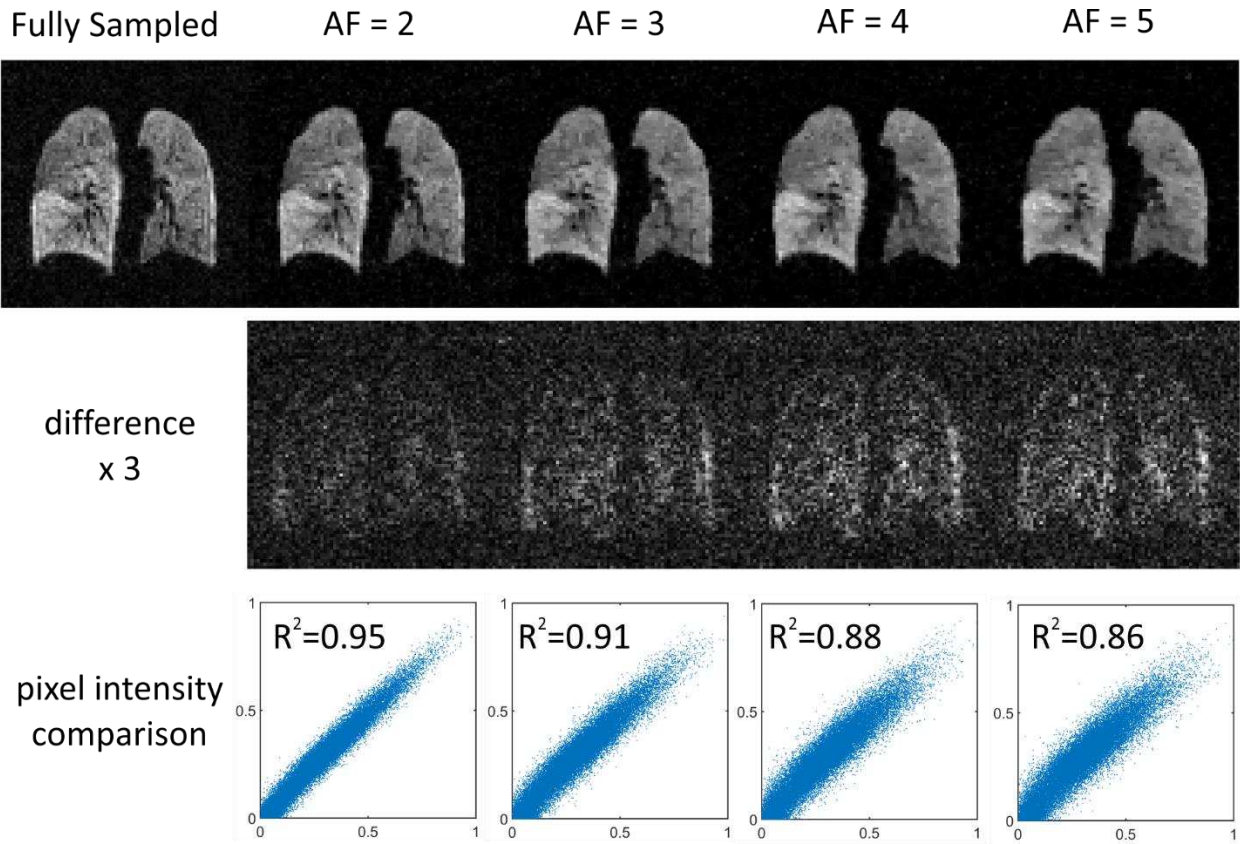


Figure 1: Representative slice of reconstructed dataset after retrospective undersampling (top row), difference images scaled by a factor 3 for reader's clarity (middle row) and pixel by pixel comparison of whole ventilated lung (bottom row) for different acceleration factors.

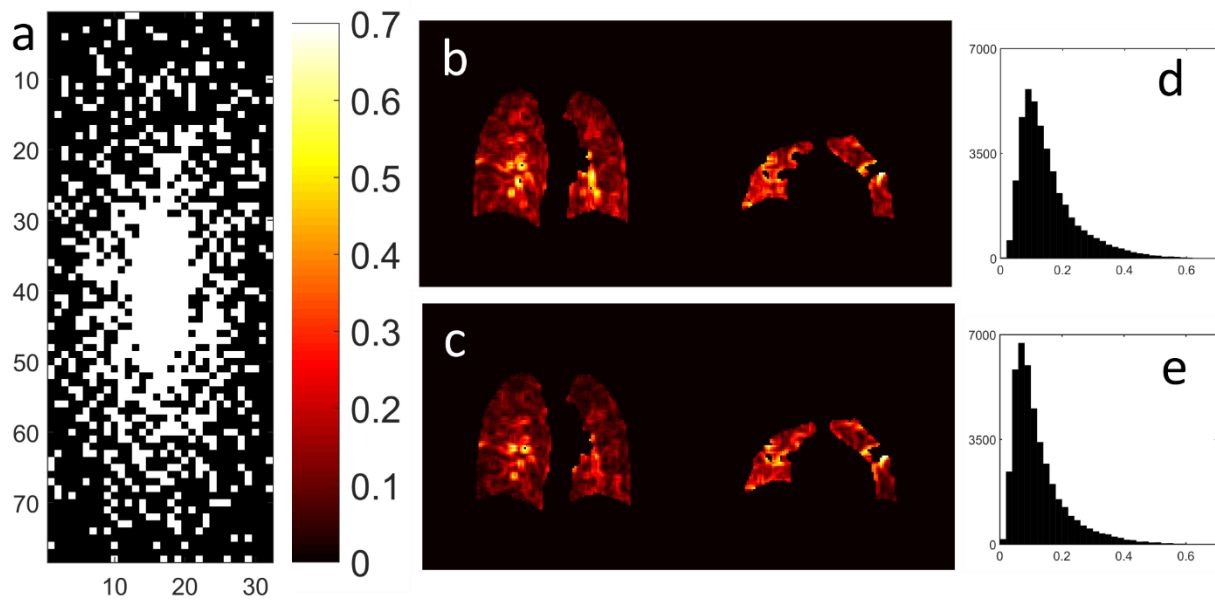


Figure 2: (a) Undersampling pattern for prospective acquisition (AF=3). (b) & (c): Example slices of  $H_{i,j,k}$  maps from FS and retrospective CS with AF = 3 respectively. (d) & (e): Corresponding FS and CS  $H_{i,j,k}$  histograms.

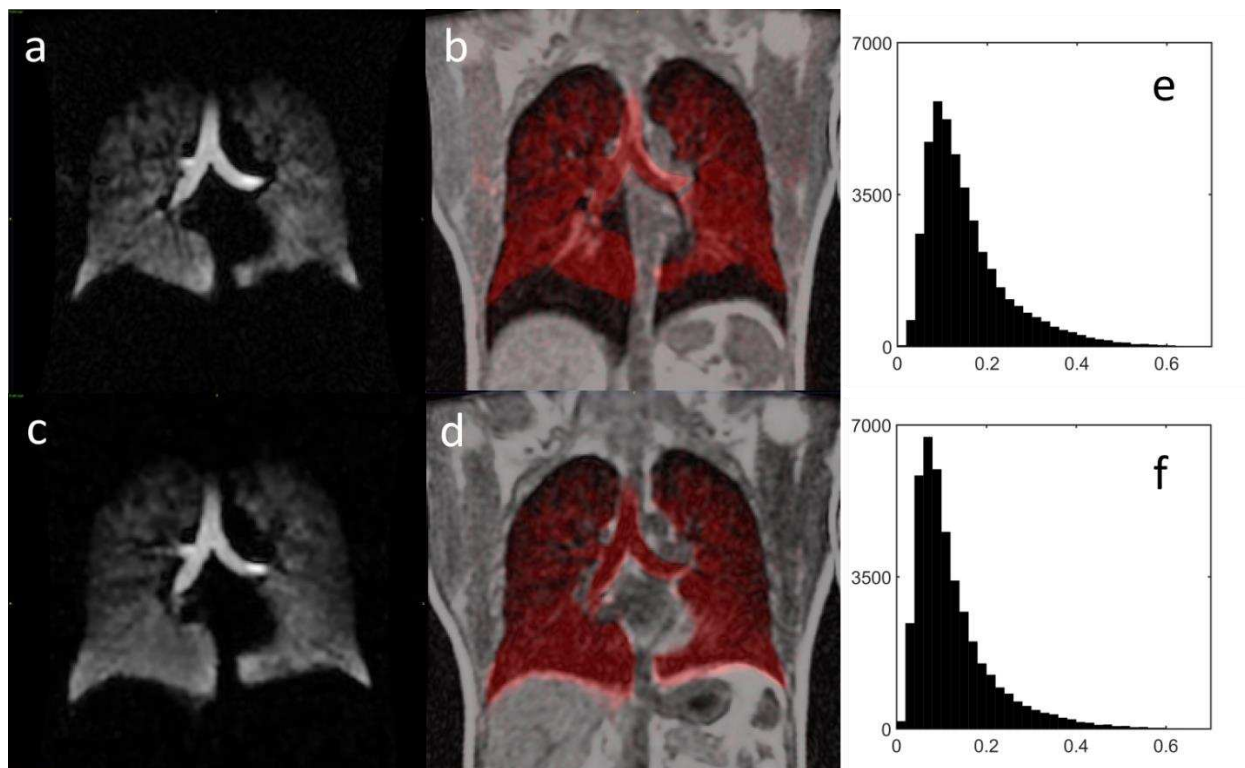


Figure 3: Example of unregistered separate breath FS  $^{129}\text{Xe}$  ventilation (a) and  $^1\text{H}$  images (b). The misalignment is highlighted in (b) by representing the  $^{129}\text{Xe}$  image (red) on top of the  $^1\text{H}$  image (grayscale). (c) & (d): corresponding same breath CS  $^{129}\text{Xe}$  and  $^1\text{H}$  images from the same subject. (e) & (f):  $^{129}\text{Xe}$   $H_{i,j,k}$  histograms from FS and CS images.