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## On the limits of coercivity in permanent magnets

J. Fischbacher, A. Kovacs, H. Oezelt, M. Gusenbauer, T. Schrefl, L. Exl, D. Givord, N. M. Dempsey, G. Zimanyi, M. Winklhofer, G. Hrkac, R. Chantrell, N. Sakuma, M. Yano, A. Kato, T. Shoji, and A. Manabe

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## On the limits of coercivity in permanent magnets

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The maximum coercivity that can be achieved for a given hard magnetic alloy is estimated by computing the energy barrier for the nucleation of a reversed domain in an idealized microstructure without any structural defects and without any soft magnetic secondary phases. For  $\text{Sm}_{1-z}\text{Zr}_z(\text{Fe}_{1-y}\text{Co}_y)_{12-x}\text{Ti}_x$  based alloys, which are considered an alternative to  $\text{Nd}_2\text{Fe}_{14}\text{B}$  magnets with a lower rare-earth content, the coercive field of a small magnetic cube is reduced to 60% of the anisotropy field at room temperature and to 50% of the anisotropy field at elevated temperature (473 K). This decrease of the coercive field is caused by misorientation, demagnetizing fields, and thermal fluctuations. *Published by AIP Publishing.* [<http://dx.doi.org/10.1063/1.4999315>]

Permanent magnets are an important material for energy conversion in modern technologies. Wind power and hybrid and electric vehicles require high performance permanent magnets. In motor applications, the magnet should retain a high magnetization and coercive field at an operating temperature around 450 K. At this temperature, the magnetization and the anisotropy field of  $\text{Sm}_{1-z}\text{Zr}_z(\text{Fe}_{1-y}\text{Co}_y)_{12-x}\text{Ti}_x$  are higher than those of  $\text{Nd}_2\text{Fe}_{14}\text{B}$ .<sup>1</sup> In addition, the rare earth to transition metal ratio of the  $\text{SmFe}_{12}$  based magnets is lower. Therefore, magnets based on this phase are considered as a possible alternative to  $\text{Nd}_2\text{Fe}_{14}\text{B}$  magnets.<sup>2</sup> At high temperature, thermal fluctuations may reduce the coercive field. In this work, we numerically compute the reduction of coercivity by thermal fluctuations in  $\text{Sm}_{1-z}\text{Zr}_z(\text{Fe}_{1-y}\text{Co}_y)_{12-x}\text{Ti}_x$ . For comparison, we also include results for  $\text{Nd}_2\text{Fe}_{14}\text{B}$ . The letter is organized as follows. We first review the different effects that reduce the coercive field in permanent magnets. Then, we present a numerical method for the computation of the coercive field including thermal fluctuations, which is based on finite element micromagnetics. We introduce the concept of the activation volume which is widely used in the experimental analysis of coercivity in permanent magnets. Then, we present numerical results for  $\text{Nd}_2\text{Fe}_{14}\text{B}$  and  $\text{Sm}_{1-z}\text{Zr}_z(\text{Fe}_{1-y}\text{Co}_y)_{12-x}\text{Ti}_x$ .

Besides thermal fluctuations, several other effects reduce the coercive field of modern permanent magnets. Kronmüller *et al.*<sup>3</sup> refer to the difference between the anisotropy field of a magnet and its coercive field as a discrepancy from theory. Aharoni<sup>4</sup> predicted that the coercive field of a hard magnet decreases with increasing width of surface defects with zero anisotropy. The corresponding minimum coercive field is 1/4 of the anisotropy field which is reached

for a defect width greater than  $5\sqrt{A/K}$ , where  $A$  is the exchange constant and  $K$  is the anisotropy constant. Even smaller coercive fields may occur if the anisotropy increases gradually from zero to its maximum value as shown by Becker and Döring<sup>5</sup> and Hagedorn.<sup>6</sup>

In addition to defects, local demagnetizing fields reduce the coercivity of permanent magnets. Grönfeld and Kronmüller<sup>7</sup> show that the local demagnetizing field may reach values of the order of the saturation magnetization,  $M_s$ , near the edges of a hard magnetic grain. The total field which is essential for the switching of a grain is the sum of the local demagnetizing field and the external field. Therefore, the local demagnetizing field leads to a further reduction of coercivity.

A further reduction of the coercive field as compared to the ideal nucleation field,  $H_N = 2K/(\mu_0 M_s)$ , may result from dynamic effects.<sup>8</sup> When the external field or the internal effective field is changing at a rate much faster than the energy dissipation in the system, the system cannot follow fast changes in the energy landscape and thus does not reach the nearest metastable state. Instead, a path through the energy landscape that brings the system into a reversed magnetic state may be taken. Leineweber and Kronmüller<sup>9</sup> show that dynamic effects can reduce the ideal nucleation field by up to 20%.

In this work, we focus on thermal fluctuations and calculate the reduction of coercivity caused by these fluctuations. Magnetization reversal in a permanent magnet is the process by which an external field creates a reversed nucleus near structural defects. Thermal fluctuations assist the formation of the reversed nucleus and thus reduce the coercive field. The formation of the nucleus is associated with an energy barrier. Before magnetization reversal, the system is in a local energy minimum. With the increasing external field,

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the energy barrier that separates the local minimum from the reversed magnetic state decreases.<sup>10</sup> Taking into account thermal activation, the system can overcome an energy barrier,  $E$ , within a time  $\tau = \tau_0 \exp(E/(k_B T))$ .<sup>5</sup> Here,  $k_B = 1.38 \times 10^{-23}$  J/K is the Boltzmann constant. The time constant  $\tau_0$  is the inverse of the attempt frequency  $f_0$ . Often, it is assumed that the magnet can overcome an energy barrier of  $25k_B T$  within the time  $\tau = 1$  s which gives an attempt frequency of  $f_0 = 7.2 \times 10^{10}$  s<sup>-1</sup>.<sup>11</sup> Then, the coercive field is the critical value of the external field,  $H$ , at which the energy barrier  $E(H)$  reaches  $25k_B T$ .

Using numerical micromagnetics, we compute the energy barrier as a function of the applied field. We discretize the magnet's microstructure with tetrahedral finite elements. Minimizing the energy for varying external fields gives the magnetic states along the demagnetization curve. For energy minimization, we apply the non-linear conjugate gradient method as described by Fischbacher and co-workers.<sup>12</sup> The coercive field obtained from the computation of the demagnetization curve is  $H_0$ . This is the field at which the energy barrier is zero. We now want to compute the energy barrier for a field  $H < H_0$ . We apply the string method<sup>13</sup> in order to compute the minimum energy path that connects the local minimum at field  $H$  with the reversed magnetic state. A path is called a minimum energy path, if for any point along the path the gradient of the energy is parallel to the path. In other words, the component of the energy gradient normal to the path is zero. The magnetization configurations along the path are described by images. Each image is a replica of the total system. The minimum energy path over a saddle point is found iteratively. A single iteration step consists of two moves. First, each image is relaxed<sup>14</sup> by applying a few steps of the conjugate gradient method, and then, the images are moved along the path so that the distance between the images is constant. We use an energy weighted distance and truncate the path<sup>15</sup> so that there are more images next to the saddle point. We repeat the computation of the minimum energy path for different applied fields and obtain  $E(H)$ . We compute  $H_c(T)$  by the intersection of the  $E(H)$  curve with the line  $E = 25k_B T$  (see Fig. 1).

Path finding algorithms are well established both in chemical physics and in micromagnetics.<sup>13</sup> As shown in

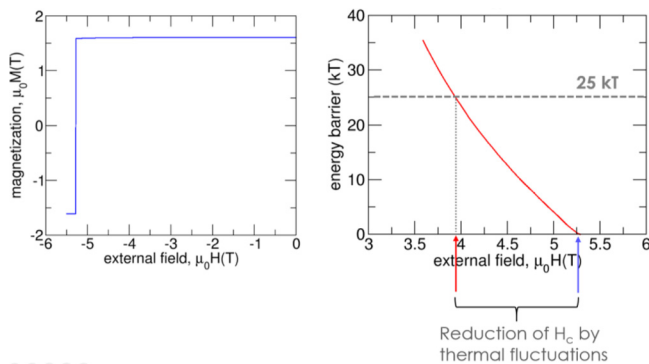


FIG. 1. Left: Computed demagnetization curve for a  $\text{Nd}_2\text{Fe}_{14}\text{B}$  cube at  $T = 300$  K with an edge length of 40 nm. Right: Energy barrier as a function of the external field. At the coercive field, the energy barrier crosses the  $25k_B T$  line.

Fig. 1, the applied algorithms are self-consistent. The switching field obtained by a classical micromagnetic method is equal to the critical field at which the computed energy barrier vanishes. Please note that the computation of the demagnetization curve by energy minimization<sup>16</sup> and the computation of the minimum energy path use the same computational grid and the same numerical minimization algorithm. Thermal fluctuations at the atomistic level are taken into account by using temperature dependent intrinsic magnetic properties such as  $M_s(T)$ ,  $K(T)$ , and  $A(T)$ .

The above numerical scheme takes into account thermal activation over finite energy barriers. Skomski *et al.*<sup>17</sup> reported another mechanism of coercivity reduction by thermal fluctuations. Spin waves interact with small soft magnetic structural defects which in turn cause a reduction of coercivity. The corresponding change in coercivity was found to be less than one percent. In our analysis, this effect is not taken into account.

We can express the coercive field as

$$H_c = \alpha H_N - N_{\text{eff}} M_s - H_f. \quad (1)$$

Expression (1) is reminiscent of the micromagnetic equation<sup>3</sup> often used to analyze the temperature dependence of coercivity in hard magnets. The coefficient  $\alpha$  expresses the reduction in coercivity due to defects, misorientation, and intergrain exchange interactions.<sup>18</sup> The microstructural parameter  $N_{\text{eff}}$  is related to the effect of the local demagnetization field near sharp edges and corners of the microstructure. The fluctuation field  $H_f$  gives the reduction of the coercive field by thermal fluctuations.<sup>19</sup> In this work, we will quantify the different effects that reduce the coercivity according to (1). In particular, we are interested in the limits of coercivity. By computing  $\alpha$ ,  $N_{\text{eff}}$ , and  $H_f$  for a perfect hard magnetic particle without any defect, we can estimate the maximum possible coercive field for a given magnetic material and microstructure. This is especially important considering the current effort to search for new hard magnetic phases with reduced rare-earth content.<sup>2</sup> In addition, one might take into account the thermal fluctuation field to know how much magnetic anisotropy is enough for a permanent magnet.<sup>20</sup> The coercive field which would be measured in the absence of thermal activation is  $H_0 = \alpha H_N - N_{\text{eff}} M_s$ .

The height of the energy barrier as a function of field,  $E(H)$ , can be derived from viscosity measurements, series expansion, or micromagnetic simulations. Néel<sup>21</sup> derived a series expansion of the form  $E = c(H_0 - H)^m$  to describe the field dependence of the energy barrier, where  $c$  is a constant. Analyzing the micromagnetic free energy, Skomski *et al.*<sup>22</sup> showed that physically reasonable exponents are  $m = 3/2$  and  $m = 2$ . The numerical algorithm presented above does not make any prior assumption on how the energy barrier changes with the field. Instead, we compute  $E(H)$  for a finite element model of a magnetic material numerically. For the analysis of experimental data, the energy barrier is often expressed by a linear approximation  $E(H) = v\mu_0 M_s (H_0 - H)$ .<sup>23</sup> The activation volume  $v$  is not necessarily related to a physical volume. Solving  $E(H) = 25k_B T$  for  $H$  gives the coercive field. Thus, we can write (1) as<sup>24</sup>

$$H_c = \alpha H_N - N_{\text{eff}} M_s - \frac{25k_B T}{v \mu_0 M_s}. \quad (2)$$

The last term in (2) is proportional to the magnetic viscosity coefficient<sup>25,26</sup>  $S_v = k_B T / (v \mu_0 M_s)$ , which can be measured experimentally. Traditionally, equations of form (2) have been used to analyze the temperature dependence of the coercivity.<sup>27,28</sup>

The viscosity coefficient can be written as  $S_v = -k_B T / (\partial E / \partial H)$ .<sup>11</sup> Thus, we can define the activation volume as

$$v = -\frac{1}{\mu_0 M_s} \frac{\partial E}{\partial H}. \quad (3)$$

In this work, we will use (3) to compute the activation volume, whereby  $E(H)$  is computed by finite element micro-magnetic simulations.

From the comparison of the numerical results with Equation (1), we can numerically determine the microstructural parameters  $\alpha$ ,  $N_{\text{eff}}$ , and the fluctuation field  $H_f$ :

- (1) We compute the demagnetizing curve but we switch off the demagnetizing effects by neglecting the magnetostatic self-energy in the total energy. This gives  $H_0^* = \alpha H_N$  and we can derive  $\alpha = H_0^* / H_N$ .
- (2) We compute the demagnetizing curve taking into account the magnetostatic energy term. This gives  $H_0 = \alpha H_N - N_{\text{eff}} M_s = H_0^* - N_{\text{eff}} M_s$  and we compute  $N_{\text{eff}} = (H_0^* - H_0) / M_s$ .
- (3) We compute the coercive field including thermal activation by  $E(H_c) = 25k_B T$ . The fluctuation field,  $H_f = H_0 - H_c$ , represents the reduction in coercivity due to thermal activation effects.

We are particularly interested in the limits of coercivity for a given magnetic material. Therefore, we apply the above procedure for a perfect, nano-sized hard magnetic cube without any defects. The edge length of the cube is 40 nm. However, we apply the magnetic field one degree off the easy axis which is parallel to one edge of the cube. First, we apply the method for  $\text{Nd}_2\text{Fe}_{14}\text{B}$ . Then, we will show the limits of coercivity for  $\text{Sm}_{1-x}\text{Zr}_x(\text{Fe}_{1-y}\text{Co}_y)_{12-x}\text{Ti}_x$  magnets. Table I gives the intrinsic magnetic properties used for the

TABLE I. Intrinsic magnetic properties used for the simulations. The table gives the anisotropy constant  $K$  (MJ/m<sup>3</sup>), the saturation magnetization  $\mu_0 M_s$  (T), and the exchange constant  $A$  (pJ/m) for different temperatures  $T$  (K). For  $\text{Nd}_2\text{Fe}_{14}\text{B}$ , the material properties are taken from Hock<sup>29</sup> and Durst and Kronmüller.<sup>30</sup> For  $\text{Sm}_{1-x}\text{Zr}_x(\text{Fe}_{1-y}\text{Co}_y)_{12-x}\text{Ti}_x$  compounds, the material properties are taken from Kuno *et al.*<sup>1</sup> The exchange constant is estimated.

| Material   | $T$ | $\mu_0 M_s$ | $K$  | $A$  |
|--|-----|-------------|------|------|
| $\text{Nd}_2\text{Fe}_{14}\text{B}$  | 300 | 1.61        | 4.30 | 7.7  |
| $\text{Nd}_2\text{Fe}_{14}\text{B}$  | 450 | 1.29        | 2.09 | 4.89 |
| $\text{SmFe}_{11}\text{Ti}$  | 300 | 1.26        | 5.17 | 10   |
| $\text{Sm}(\text{Fe}_{0.75}\text{Co}_{0.25})_{11}\text{Ti}$                                | 300 | 1.42        | 4.67 | 10   |
| $\text{Sm}(\text{Fe}_{0.75}\text{Co}_{0.25})_{11.5}\text{Ti}_{0.5}$                        | 300 | 1.58        | 4.57 | 10   |
| $(\text{Sm}_{0.8}\text{Zr}_{0.2})(\text{Fe}_{0.75}\text{Co}_{0.25})_{11.5}\text{Ti}_{0.5}$ | 300 | 1.63        | 4.81 | 10   |
| $\text{SmFe}_{11}\text{Ti}$  | 473 | 1.02        | 2.80 | 6.5  |
| $\text{Sm}(\text{Fe}_{0.75}\text{Co}_{0.25})_{11}\text{Ti}$                                | 473 | 1.28        | 2.54 | 8.1  |
| $\text{Sm}(\text{Fe}_{0.75}\text{Co}_{0.25})_{11.5}\text{Ti}_{0.5}$                        | 473 | 1.45        | 2.61 | 8.4  |
| $(\text{Sm}_{0.8}\text{Zr}_{0.2})(\text{Fe}_{0.75}\text{Co}_{0.25})_{11.5}\text{Ti}_{0.5}$ | 473 | 1.50        | 2.79 | 8.4  |

simulations. For the simulation, the mesh size was 1.5 nm. Without soft magnetic defects, the numerically calculated reversal field computed without magnetostatic interactions corresponds to an analytic switching field estimated by Stoner and Wohlfarth,<sup>31</sup>  $H_0^* = f(\psi_0) H_N$ . Here,  $\psi_0$  denotes the angle between the applied field and the negative anisotropy direction and  $f(\psi_0) = \{\cos^{2/3}(\psi_0) + \sin^{2/3}(\psi_0)\}^{-3/2}$ .<sup>32</sup> The agreement between the finite element results without the magnetostatic energy term and the Stoner-Wohlfarth switching field was already shown previously.<sup>12</sup> For  $\text{Nd}_2\text{Fe}_{14}\text{B}$  at 300 K, we obtain  $\mu_0 H_0^* = 6.09$  T. The self-demagnetizing field reduces the coercive field to  $\mu_0 H_0 = 5.29$  T. Finally, with thermal fluctuations, the coercive field is  $\mu_0 H_c = 3.94$  T. Therefore, we can conclude that in  $\text{Nd}_2\text{Fe}_{14}\text{B}$ , the maximum possible coercive field of a cubic grain is only 60% of the ideal nucleation field  $H_N$ . The values of  $\alpha$ ,  $N_{\text{eff}}$ ,  $\mu_0 H_f$ , and  $\mu_0 S_v$  are 0.91, 0.5, 1.35 T, and 0.054 T, respectively.

Figure 1 shows the computed demagnetizing curve for the  $\text{Nd}_2\text{Fe}_{14}\text{B}$  cube and the energy barrier as a function of the external field computed with the intrinsic magnetic properties at  $T = 300$  K. Static energy minimization for the decreasing external field gives a switching field of  $\mu_0 H_0 = 5.29$  T. This is exactly the field at which the energy barrier reaches zero. The reduction of coercivity owing to thermal fluctuations is 25%. Using (3), we can compute the activation volume,  $v = (4.38 \text{ nm})^3$ , from the slope of the  $E(H)$  curve. The activation volume can be compared with the domain wall width,  $\delta = \pi \sqrt{A/K}$ , which is 4.2 nm, giving  $v = 1.12 \delta^3$ .<sup>33</sup> Figure 2 gives the minimum energy path and the magnetization configuration at the saddle point of the energy landscape. At the saddle point, a small nucleus, which has an extension  $a$ , is formed. Interestingly, the volume of the reversed nucleus,  $(1/8)(4\pi a^3/3)$ , roughly corresponds to the activation volume  $v$  as given by (3). For the small perfect cube, the computed coercivity, the viscosity coefficient, and the activation volume are higher than the experimental values found in  $\text{Nd}_2\text{Fe}_{14}\text{B}$  based magnets.

For comparison with experiments, we performed a similar simulation of a granular  $\text{Nd}_2\text{Fe}_{14}\text{B}$  ensemble consisting of 64 polyhedral grains with an average grain size of 60 nm. We generated the grain structure from a centroid Voronoi tessellation, using the software tool Neper.<sup>34</sup> The grains of the  $\text{Nd}_2\text{Fe}_{14}\text{B}$  model system were separated by a weakly ferromagnetic grain boundary phase with  $\mu_0 M_s = 0.5$  T. The thickness of the grain boundary phase was approximately 3 nm. Grain boundaries in hot deformed  $\text{Nd}_2\text{Fe}_{14}\text{B}$  magnets were found to contain up to 55 at. % Fe.<sup>35</sup> The average

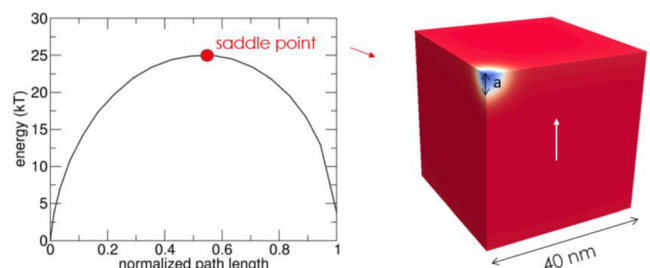


FIG. 2. Left: Minimum energy path for a  $\text{Nd}_2\text{Fe}_{14}\text{B}$  cube at  $T = 300$  K with an edge length of 40 nm. Right: Magnetization configuration of the saddle point with a reversed nucleus of size  $a$ .

misorientation angle of the grains was 15 degrees. For this magnet, the values for the coercive field without magnetostatic interactions  $\mu_0 H_0^*$ , the intrinsic coercivity  $\mu_0 H_0$ , and the coercivity computed with thermal activation taken into account  $\mu_0 H_c$  were 3.24 T, 2.88 T, and 2.64 T, respectively. The resulting values of  $\alpha$ ,  $N_{\text{eff}}$ , and  $\mu_0 H_f$  were 0.48, 0.22, and 0.24 T, respectively. The reduction of coercivity owing to thermal fluctuations is 8%. The computed viscosity coefficient  $\mu_0 S_v = 0.0094$  T and the computed activation volume  $v = (7.9 \text{ nm})^3$  are very close to values measured by Villas-Boas *et al.*<sup>28</sup> for a mechanically alloyed  $\text{Nd}_{15.5}\text{Dy}_{2.5}\text{Fe}_{65}\text{Co}_{10}\text{Ga}_{0.75}\text{B}_{6.25}$  magnet at room temperature. Figure 3 shows the saddle point configuration computed from the minimum energy path. The reversed nucleus is formed in the grain boundary near the edge of the magnet. This is the location where the demagnetizing fields are the strongest.

A comparison of the numerical results reveals a striking increase in the activation volume from the small cube to the multigrain system which is mainly caused by the presence of the soft magnetic grain boundary phase. Whereas the small cube is a perfect hard magnetic particle, a 3 nm thick soft magnetic phase separates the grains in the granular magnet. In addition, the demagnetizing field from the neighboring grains is acting on the soft phase where magnetization reversal will be initiated. The soft layer present between hard grains in the multigrain structure makes the spatial variation of the magnetic energy more progressive than in the small cube. Thus, a larger volume (by a factor of 6 in the present case) corresponds to the  $25k_B T$  energy term provided by thermal activation. As evidenced by Eqs. (1) and (2), the fluctuation field is subsequently reduced by the same factor. By moving from the ideal cube to a realistic structure, the activation volume increases and the thermal reduction of coercivity decreases. However, the more realistic structure of the magnet also reduces the intrinsic coercivity  $H_0$ .

Finally, we computed the limits of coercivity for SmFe-based magnets which are considered as candidates for high performance magnets with a rare earth content smaller than  $\text{Nd}_2\text{Fe}_{14}\text{B}$ . For various  $\text{Sm}_{1-z}\text{Zr}_z(\text{Fe}_{1-y}\text{Co}_y)_{12-x}\text{Ti}_x$  compounds, we computed the effects that reduce the ideal nucleation field towards the maximum possible coercive field. The

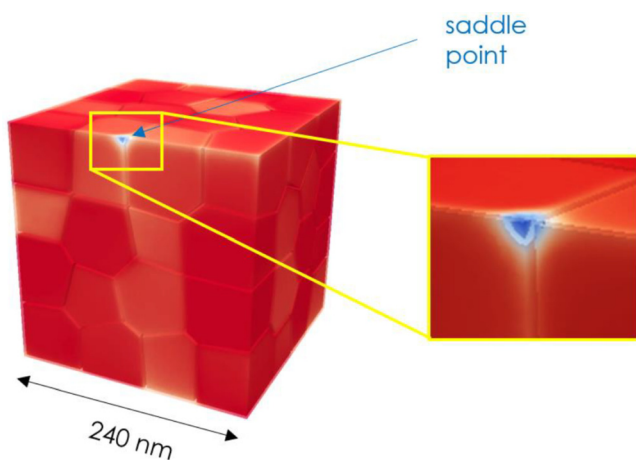


FIG. 3. Saddle point of the energy for thermally assisted reversal of a multigrain  $\text{Nd}_2\text{Fe}_{14}\text{B}$  magnet. The reversed nucleus is formed at the grain boundary near the outer edge of the magnet.

intrinsic material parameters used for the simulations are listed in Table I. Again, the sample was a cube with an edge length of 40 nm. The field was applied at an angle of one degree. Figure 4 shows the ideal nucleation field, the coercive field without demagnetizing effects, the intrinsic coercive field, and the coercivity computed with thermal activation at room temperature and at elevated temperature. At  $T = 473$  K, the maximum possible expected coercive field for  $(\text{Sm}_{0.8}\text{Zr}_{0.2})(\text{Fe}_{0.75}\text{Co}_{0.25})_{11.5}\text{Ti}_{0.5}$  is  $\mu_0 H_c = 2.61$  T. This can be compared with the computed coercivity limit for  $\text{Nd}_2\text{Fe}_{14}\text{B}$  at  $T = 450$  K which is  $\mu_0 H_c = 1.88$  T. These limits were computed for a small cubic grain without any soft magnetic defects. Rounding the edges of the cube will improve the coercivity owing to a reduction in the local demagnetizing field near the edges and corners.

Using numerical micromagnetics, we computed the effects that reduce the ideal nucleation field of permanent magnets towards the coercive field. We found that even for a magnet with perfect structure, a small cube without surface defects, coercivity is reduced to 60% at room temperature and 50% at 473 K of the ideal nucleation field by the small misalignment angle (one degree), demagnetizing field, and thermal activation. In the case of a more realistic grain assembly, the coercive field is reduced by the presence of intergranular defects (represented here by a soft magnetic layer). However, the effect of thermal activation is significantly reduced, as explained above. Therefore, a competition between two antagonistic effects is revealed: as one approaches ideal hard magnetic properties, the drop in coercivity due to defects is

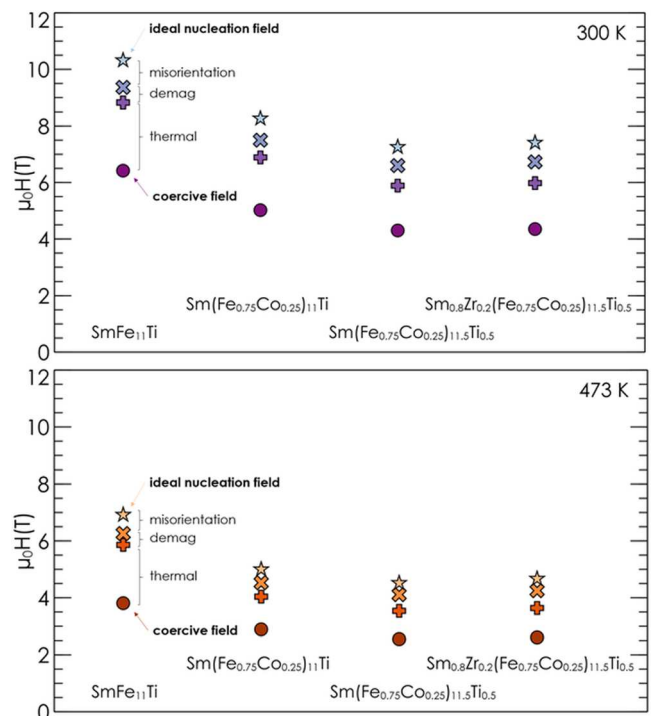


FIG. 4. Reduction of the ideal nucleation field in various  $\text{Sm}_{1-z}\text{Zr}_z(\text{Fe}_{1-y}\text{Co}_y)_{12-x}\text{Ti}_x$  compounds at  $T = 300$  K and  $T = 473$  K of a small magnetic cube without structural defects. The fields indicated by stars are the ideal nucleation fields. Symbol  $\times$  denotes the field taking into account misorientation. The switching fields computed by Brown's equation<sup>16</sup> are represented by the symbol  $+$ . The circles indicate the critical field at which the energy barrier reaches  $25k_B T$ . All fields were computed for a cube with an edge length of 40 nm.

reduced but the drop due to thermal activation is increased. In real materials, defects play a major role, whereas coercive field reduction due to thermal activation is of secondary importance at least up to 300 K.

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- <sup>1</sup>T. Kuno, S. Suzuki, K. Urushibata, K. Kobayashi, N. Sakuma, M. Yano, A. Kato, and A. Manabe, *AIP Adv.* **6**, 025221 (2016).
- <sup>2</sup>S. Hirosawa, M. Nishino, and S. Miyashita, *Adv. Nat. Sci.: Nanosci. Nanotechnol.* **8**, 013002 (2017).
- <sup>3</sup>H. Kronmüller, K.-D. Durst, and M. Sagawa, *J. Magn. Magn. Mater.* **74**, 291–302 (1988).
- <sup>4</sup>A. Aharoni, *Phys. Rev.* **119**, 127 (1960).
- <sup>5</sup>R. Becker and W. Döring, *Ferromagnetismus* (Springer, 1939).
- <sup>6</sup>F. Hagedorn, *J. Appl. Phys.* **41**, 2491 (1970).
- <sup>7</sup>M. Grönfeld and H. Kronmüller, *J. Magn. Magn. Mater.* **80**, 223 (1989).
- <sup>8</sup>T. Leineweber and H. Kronmüller, *J. Magn. Magn. Mater.* **192**, 575 (1999).
- <sup>9</sup>T. Leineweber and H. Kronmüller, *Phys. B* **275**, 5 (2000).
- <sup>10</sup>M. E. Schabes, *J. Magn. Magn. Mater.* **95**, 249 (1991).
- <sup>11</sup>P. Gaunt, *Philos. Mag.* **34**, 775 (1976).
- <sup>12</sup>J. Fischbacher, A. Kovacs, H. Oezelt, T. Schrefl, L. Exl, J. Fidler, D. Suess, N. Sakuma, M. Yano, A. Kato *et al.*, *AIP Adv.* **7**, 045310 (2017).
- <sup>13</sup>L. Zhang, W. Ren, A. Samanta, and Q. Du, *NPJ Comput. Mater.* **2**, 16003 (2016).
- <sup>14</sup>A. Samanta and E. Weinan, *Commun. Comput. Phys.* **14**, 265 (2013).
- <sup>15</sup>M. F. Carilli, K. T. Delaney, and G. H. Fredrickson, *J. Chem. Phys.* **143**, 054105 (2015).
- <sup>16</sup>W. F. Brown, *Micromagnetics* (Interscience Publishers, 1963).
- <sup>17</sup>R. Skomski, P. Kumar, G. C. Hadjipanayis, and D. J. Sellmyer, *IEEE Trans. Magn.* **49**, 3229 (2013).
- <sup>18</sup>H. Kronmüller, M. Becher, M. Seeger, and A. Zern, in *Proceedings of the 9th International Symposium Magnetic Anisotropy and Coercivity in Rare-Earth Transition Metal Alloys*, edited by F. Missell, V. Villas-Boas, H. Rechenberg, and F. Landgraf (São Paulo, Brazil, 1996), p. 1.
- <sup>19</sup>D. Givord, P. Tenaud, and T. Viadieu, *IEEE Trans. Magn.* **24**, 1921 (1988).
- <sup>20</sup>R. Skomski and J. Coey, *Scr. Mater.* **112**, 3 (2016).
- <sup>21</sup>L. Néel, *J. Phys. Radium* **11**, 49 (1950).
- <sup>22</sup>R. Skomski, J. Zhou, R. D. Kirby, and D. J. Sellmyer, *J. Appl. Phys.* **99**, 08B906 (2006).
- <sup>23</sup>R. Skomski, *Simple Models of Magnetism* (Oxford University Press on Demand, 2008).
- <sup>24</sup>H. Kronmüller and M. Fähnle, *Micromagnetism and the Microstructure of Ferromagnetic Solids* (Cambridge university press, 2003).
- <sup>25</sup>R. Street and J. Woolley, *Proc. Phys. Soc.* **69**, 1189 (1956).
- <sup>26</sup>E. Wohlfarth, *J. Phys. F* **14**, L155 (1984).
- <sup>27</sup>M. Becher, M. Seeger, J. Bauer, and H. Kronmüller, in *Magnetic Hysteresis in Novel Magnetic Materials*, edited by G. Hadjipanayis (Springer, 1997), p. 657.
- <sup>28</sup>V. Villas-Boas, J. Gonzalez, F. Cebollada, M. Rossignol, D. Taylor, and D. Givord, *J. Magn. Magn. Mater.* **185**, 180 (1998).
- <sup>29</sup>S. Hock, Ph.D. thesis, Universität Stuttgart, 1988.
- <sup>30</sup>K.-D. Durst and H. Kronmüller, *J. Magn. Magn. Mater.* **59**, 86 (1986).
- <sup>31</sup>E. C. Stoner and E. Wohlfarth, *Philos. Trans. R. Soc., A* **240**, 599 (1948).
- <sup>32</sup>H. Kronmüller, K.-D. Durst, and G. Martinek, *J. Magn. Magn. Mater.* **69**, 149 (1987).
- <sup>33</sup>D. Givord, A. Lienard, P. Tenaud, and T. Viadieu, *J. Magn. Magn. Mater.* **67**, L281 (1987).
- <sup>34</sup>R. Quey, P. Dawson, and F. Barbe, *Comput. Methods Appl. Mech. Eng.* **200**, 1729 (2011).
- <sup>35</sup>H. Sepehri-Amin, T. Ohkubo, S. Nagashima, M. Yano, T. Shoji, A. Kato, T. Schrefl, and K. Hono, *Acta Mater.* **61**, 6622 (2013).