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1 Pulse pile-up identification and reconstruction for liquid scintillator 2 based neutron detectors

3

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25

26 **Abstract:** The issue of pulse pile-up is frequently encountered in nuclear experiments involving
27 high counting rates, which will distort the pulse shapes and the energy spectra. A digital method of
28 off-line processing of pile-up pulses is presented. The pile-up pulses were firstly identified by detecting
29 the downward-going zero-crossings in the first-order derivative of the original signal, and then the
30 constituent pulses were reconstructed based on comparing the pile-up pulse with four models that are
31 generated by combining pairs of neutron and γ standard pulses together with a controllable time
32 interval. The accuracy of this method in resolving the pile-up events was investigated as a function of
33 the time interval between two pulses constituting a pile-up event. The obtained results show that the
34 method is capable of disentangling two pulses with a time interval among them down to 20 ns, as well
35 as classifying them as neutrons or γ rays. Furthermore, the error of reconstructing pile-up pulses could
36 be kept below 6% when successive peaks were separated by more than 50 ns. By applying the method
37 in a high counting rate of pile-up events measurement of the NEutron Detector Array (NEDA), it was
38 empirically found that this method can reconstruct the pile-up pulses and perform neutron- γ
39 discrimination quite accurately. It can also significantly correct the distorted pulse height spectrum due
40 to pile-up events.

41

42 **Keywords:** pile-up; digital; first-order derivative; neutron- γ discrimination; liquid scintillator.

43 **1. Introduction**

44 High counting rates in radiation detectors is a common fact in nuclear
45 spectroscopy as well as in nuclear reaction studies. For such applications involving
46 high counting rates, the pile-up effect, in which more than one event occur
47 simultaneously or closely spaced in time, becomes a severe issue. It results in two or
48 more recorded signals partially or even completely overlapping, thus leading to a
49 decrease in the counting efficiency, distortion of the pulse shape, and deterioration in
50 the energy resolution.

51 Typically, pile-up events are diminished by reducing the pulse width with
52 shaping networks, at the expense of a poorer performance in terms of
53 signal-to-noise ratio. Since compressing signal pulses can only reduce the probability
54 of the occurrence of pile-up but cannot totally eliminate it, hardware-based pile-up
55 rejectors are often employed to identify the inevitable pile-up events and then discard
56 them [1-4]. Although rejectors of this type can reduce the spectral distortions arising
57 from pile-up to some extent, they negatively impact on the system throughput.
58 Furthermore, some recorded events correspond to the pile-up of pulses that almost
59 completely overlap, so that the recorded amplitude distribution is still distorted
60 compared with the true event spectrum.

61 With the availability of digital signal processing techniques, digital treatments of
62 pile-up have been introduced and adopted which yield significant advantages over
63 conventional analog approaches. However, these are typically quite complex and not
64 yet routinely employed in standard spectroscopy systems in which the pulse analysis
65 is carried out in real time. The digital methods offer the possibility of preserving and
66 analyzing in detail all the information carried by the overlapping pulses rather than
67 simply rejecting them and tolerating the losses due to pile-up [5]. Various developed
68 algorithms, such as the fitting method [6,7] and the deconvolution method [8], have
69 successfully disentangled pile-up pulses with good accuracy, provided that a
70 minimum time interval of around 40-50 ns exists between the two successive pulses
71 constituting a pile-up event. Not only these methods compensate for the counting
72 losses and correct the spectral distortions resulting from pile-up, but they are also
73 capable of recovering original information on the type and energy of the constituent
74 particles of the pile-up events. However, most of the methods are somewhat limited
75 by analytical and computational complexity. For instance, the fitting process of the
76 pulse based on an exponential analytic model has to be performed by trial and error,
77 as sometimes it is hard for the fitting to converge to the correct solution. In this study,
78 the aim is to propose an easy-implemented and efficient method of pulse pile-up
79 identification and reconstruction for signals from liquid scintillators similar to the
80 type that are used by the neutron detector array NEDA [9-12]. The ongoing NEDA
81 project addresses the physics of neutron-deficient as well as neutron-rich nuclei using
82 both intense stable and radioactive ion beams. The full version of NEDA will consist
83 of around 350 closely packed liquid scintillator detectors of type BC-501A, mainly in
84 conjunction with large γ -ray arrays like AGATA [13,14]. For use in nuclear structure
85 experiments, NEDA should have the capability to run at high counting rates, which

86 leads to a significant fraction of pile-up events, while retaining a high neutron
87 efficiency and an excellent neutron-gamma ($n\text{-}\gamma$) discrimination performance. In order
88 to meet these requirements, the pile-up issue has to be dealt with appropriately in
89 NEDA. Specifically, the idea is to identify pile-up pulses and then perform $n\text{-}\gamma$
90 discrimination on an event-by-event basis by taking advantage of high speed signal
91 sampling and digital signal processing. Therefore, data have been acquired with the
92 experimental setup described in Section 2 to develop the approach of pile-up
93 identification and reconstruction in NEDA. The principles and validation of the
94 proposed approach are given and discussed in Section 3. The application of the
95 approach in a high counting rate measurement is described in Section 4 and the
96 conclusions in Section 5.

97 **2. Experiment**

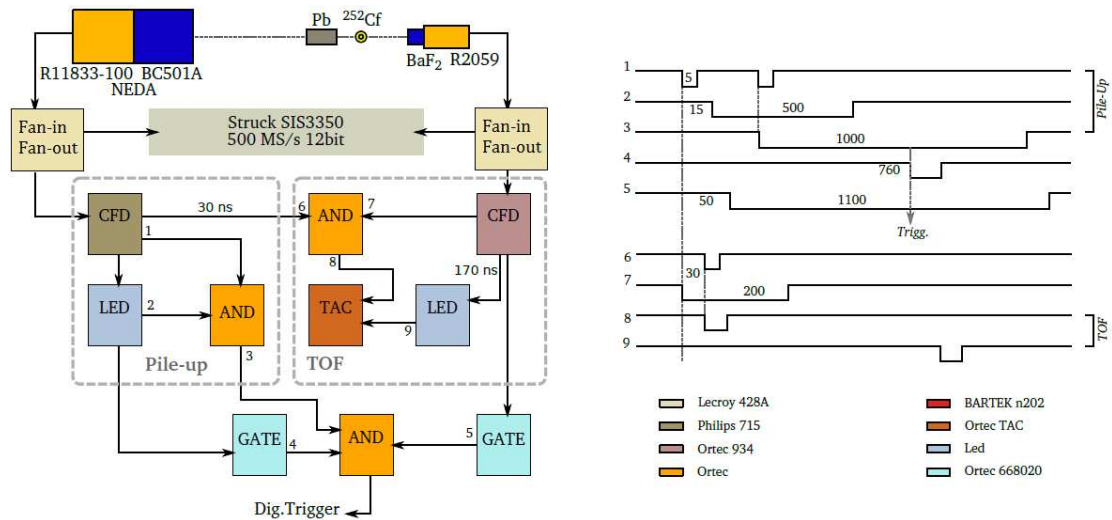
98 Two experiments were carried out at Laboratori Nazionali di Legnaro. The first
99 was performed in order to acquire large numbers of single neutron or γ ray pulses,
100 which were later used to extract standard neutron- and γ -induced pulses, and to
101 generate synthetic pile-up pulses, aiming at developing the approach of pile-up
102 identification and reconstruction in Section 3. The second experiment was performed
103 in order to acquire large numbers of real pile-up pulses, which were later used to
104 further evaluate the proposed method as shown in Section 4.

105 The experimental setup is illustrated in Fig. 1. The first experiment is almost the
106 same as that of our previous work [10] except that only a single photomultiplier tube
107 (PMT) of type Hamamatsu R11833-100 was used in this measurement. This 8-stage,
108 5 in. diameter PMT, shielded with μ -metal from magnetic fields, was coupled to a
109 cylindrical 5 inch by 5 inch detector cell containing liquid scintillator of type
110 BC-501A. The high voltage was set to get a signal amplitude of about 1 V/MeV using
111 a ^{60}Co source, which had an activity of about 2 MBq. A lead brick with a thickness of
112 5 cm was put between the source and the BC-501A detector to reduce the counting
113 rate originating from γ rays without losing too many neutrons, thus keeping the
114 counting rate of the PMT R11833-100 at around 2 kHz. A trigger and time reference
115 detector consisting of a cylindrical 1 inch by 1 inch BaF_2 scintillator coupled to a 2
116 inch R2059 PMT was placed very close to the ^{252}Cf source for detection of γ rays.
117 The threshold of the constant fraction discriminator (CFD) was set to approximately
118 30 keVee (keV electron equivalent). With the outputs of the two CFD units fed into
119 the LeCroy 465 coincidence unit, a coincidence between the signals from the
120 BC-501A and BaF_2 detectors was created, which was used as a trigger for the data
121 acquisition system (GASIFIC) [15] and as a start signal for the time-to-amplitude
122 converter (TAC). The counting rate of the BaF_2 detector was about 200 kHz and the
123 coincidence rate was about 200 Hz. The TAC module was subsequently stopped by
124 the delayed signal from the BaF_2 detector and measured the time-of-flight (TOF)
125 difference between the detected γ rays and neutrons in the detectors. Signals from
126 both detectors were digitised with a Struck SIS3350 digitiser [16] that has a 500 MHz
127 sampling rate and 12-bit resolution (effective number of bits = 9.2). The analog TAC
128 signals were digitised by a Struck SIS3302 digitiser working at a sampling rate of 100

129 MHz and with 16-bit resolution (effective number of bits ≈ 13).

130 In addition, a high count rate experiment was carried out by adding a pile-up
 131 selector block to the first experimental setup (Fig. 1). In this measurement, the lead
 132 brick was removed, and the distance between the BC-501A and the ^{252}Cf source was
 133 readjusted, which gave a count rate of 200 kHz in the BC-501A detector. Pile-up
 134 events are validated by a logic AND (see signal 3 on the right), from the coincidence
 135 of the NEDA CFD (signal 1) with the same signal delayed by 15 ns (to avoid
 136 self-triggering) and wide open 500 ns (signal 2). To have the system triggered by the
 137 first signal in the pile-up event, the CFD is further delayed with a gate delay generator
 138 module (signal 4) and sent to another AND module in coincidence with signal 3. The
 139 final trigger is then validated with a coincidence from the BaF_2 . TOF is measured with
 140 a TAC module, started with the coincidence (signal 8) of the two detector CFDs
 141 (signals 6 and 7), triggered by the NEDA signal, and stopped with the BaF_2 signal
 142 delayed (signal 9). For the stop signal, a 170ns delay cable was used in order to
 143 account for slow neutrons. As the logic signal is integrated through the cable, a
 144 leading-edge discriminator (LED) was used afterwards to restore its step shape. The
 145 trigger rate was about 200 Hz in this experiment. With this setup, pulses with intervals
 146 ranging from 10 ns to 500 ns were recorded.

147 In this study, the digital signals from the BC-501A detector, as well as the TOF
 148 information, were used for pile-up investigations.



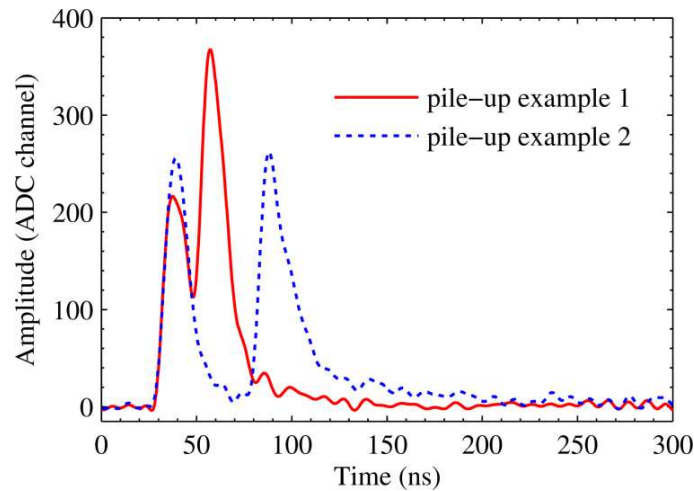
149
 150 **Fig. 1.** Block scheme of the experimental setup (left) and the logic signals produced
 151 (right).
 152

153 3. Principles and validation of the approach

154 3.1. Preprocessing of the signals

155 The 500 MHz sampling rate and 12-bit resolution of the Struck SIS3350 digitiser
 156 allow detailed analysis and processing of the pulse waveforms from the BC-501A
 157 detector, originating from either neutrons or γ rays. Fig. 2 gives two examples of
 158 pile-up pulses after preprocessing, including CFD timing, baseline restoration and
 159 filtering. For each waveform, a range of 300 ns of the pulse was used for the analysis,

160 as beyond this time span the first pulse has decayed to a negligible level [17], so that
 161 the occurrence of a second pulse does not constitute a pile-up event. The start time of
 162 the pulses constituting the pile-up event was determined by implementing a digital
 163 CFD. The CFD method firstly attenuated the original signal to 20% of the first peak
 164 amplitude, and then summed it with the delayed and inverted original signal. Finally,
 165 the point that this sum signal crosses the zero axis was extracted, which is
 166 independent of the pulse amplitude and corresponds to the time at which the original
 167 pulse reaches 20% of its first peak amplitude. It can be seen in Fig. 2 that after the
 168 CFD timing, the waveforms are well time aligned on the leading edge of the first peak.
 169 Moreover, the baseline shift has been eliminated from each pulse by subtracting the
 170 average value of the sampling points in the pre-trigger range of the waveform. A
 171 small amount of severely distorted pulses with heavily fluctuating baselines have been
 172 discarded (<1% of the total). In addition, a low-pass finite impulse response (FIR)
 173 digital filter has been applied to the pulses to remove high-frequency noise [18].

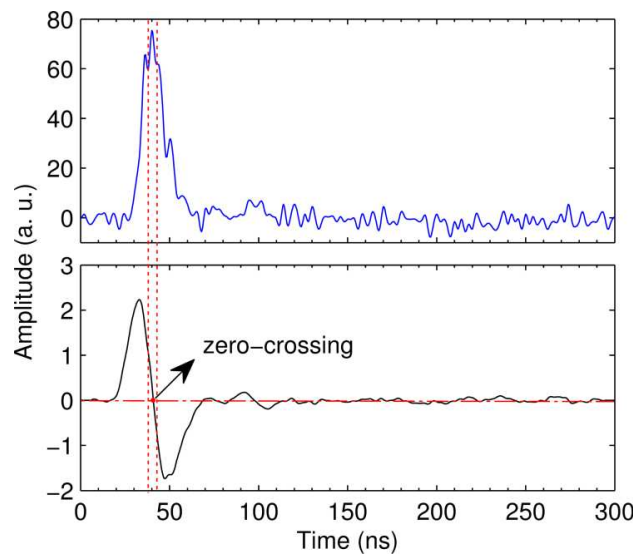


174
 175 **Fig. 2.** Pile-up waveforms after the digital CFD time-aligning, baseline restoration, and filtering.
 176

177 3.2. Pile-up pulse identification

178 When two or more peaks are detected within the duration of a recorded pulse
 179 (300 ns in the present work), a pile-up event is identified. The common way of
 180 detecting peaks is to search and find local maxima in the overlapping pulses, which
 181 may misidentify the spikes in the waveforms as pile-up events. In particular, the low
 182 energy signals are more likely to trigger false identifications because they are quite
 183 noisy due to the scintillation statistics, and to the electronic noise and the quantisation
 184 effects of the digitiser [19]. As shown in the upper plot of Fig. 3, the individual pulse
 185 will be misinterpreted as a pile-up event by the maximum peak search method, as
 186 more than two peaks can be detected. Therefore, another peak search method is
 187 proposed here. It is based on the fact that the first-order derivative is the slope of the
 188 original waveform and thus has a downward-going zero-crossing, which corresponds
 189 to the peak maximum of the original waveform. Since the presence of spikes in the
 190 original waveform will cause many false zero-crossings, the first-order derivative was
 191 smoothed using a moving-average filter prior to searching for downward-going
 192 zero-crossings [20]. Then, only those zero-crossings whose slope exceeds a certain

193 threshold at a point where the original signal exceeds a certain amplitude threshold
194 are counted. In this way the method detects only the desired peaks and ignores peaks
195 that are too small, too wide, or too narrow, which are mostly random noises. If two or
196 more peaks are detected in a signal, it is determined that a pile-up event has occurred.
197 It should be noted that the position of the peak is not exactly equivalent to the position
198 of the zero-crossing due to the fact that the smoothing can distort the waveform of the
199 first-order derivative slightly. The position and height of each peak are determined by
200 least-squares fitting of a segment of the original unsmoothed signal in the vicinity of
201 the zero-crossing. Fig. 3 shows an individual pulse and its first-order derivative to
202 illustrate the process of pile-up identification using the first-order derivative method,
203 in which the only one true peak is correctly detected.



204

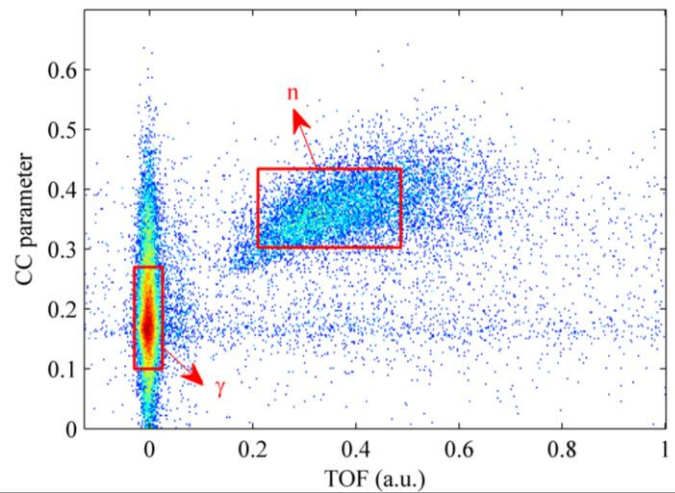
205 **Fig. 3.** An original waveform (upper panel) and its smoothed first-order derivative (lower panel).

206

207 3.3. Pile-up pulse reconstruction

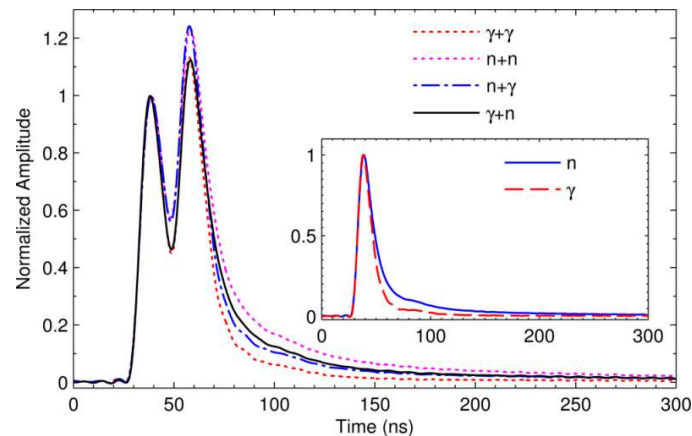
208 Once a pile-up event is identified using the first-order derivative method
209 described above, the next step is to resolve the overlapping pulses and reconstruct the
210 individual constituent pulses. Most of the existing pile-up resolving methods process
211 the first component and the second component of a pile-up event separately. The
212 fitting method, for instance, firstly recovers the first constituent pulse of a pile-up
213 event using a fitting procedure, and subsequently subtracts it from the original pile-up
214 pulse to obtain the second constituent pulse. In contrast, the approach proposed in this
215 paper treats the overlapping pulses that give rise to a pile-up event as a whole, which
216 is the combination of a single neutron or γ pulse. In this way there are only four
217 possible types of pile-up events under consideration, i.e. $n+n$, $\gamma+\gamma$, $n+\gamma$, $\gamma+n$, which
218 means the combinations of the particle types of the first pulse and the second pulse.
219 The main principle of the approach is to build four corresponding models by
220 combining neutron and γ standard pulses with varying amplitude and time spacing,
221 which are then used to compare with the pile-up pulse, and the model that has the
222 highest degree of agreement with the pile-up pulse is determined as the type of the
223 pile-up event. The neutron and γ -ray standard pulses were obtained by averaging a

224 large number of neutron and γ -ray pulses respectively, which were extracted from n- γ
 225 discrimination results of both the digital Charge Comparison (CC) [21] method and
 226 the TOF measurement, as illustrated in Fig. 4. Although the TOF measurement is very
 227 efficient to distinguish neutrons from γ rays, some misclassification cases still exist
 228 due to accidental coincidences and to the emission of delayed γ rays from the
 229 spontaneous fission of ^{252}Cf . Therefore, the digital CC pulse shape discrimination
 230 (PSD) method, based on comparing the integrated charge over two different time
 231 periods of the pulse, was used to complement the TOF measurement to acquire as
 232 pure neutron and gamma-ray pulses as possible. The CC parameter in Fig. 4
 233 represents the ratio between the tail integral and the total integral, of which the start
 234 points and end points have been optimised using the method of our previous work
 235 [10].



236
 237 **Fig. 4.** Density plot of the n- γ discrimination parameter of the CC method versus the TOF of each pulse
 238 recorded by the experimental equipment.

239
 240 Figure 5 shows the normalized standard neutron- and γ -induced pulses, as well
 241 as four pile-up models generated by adding pairs of standard pulses together separated
 242 by a time interval of 20 ns. It can be seen that the pulse shapes of the resulting pile-up
 243 models are quite distinguishable from each other, even though the constituent
 244 standard pulses have normalized amplitudes and the same time intervals. Thus, these
 245 differences in shape introduce the possibility of pile-up reconstruction based on the
 246 four pile-up models.



248 **Fig. 5.** Four pile-up models generated by adding pairs of neutron or γ standard pulses (shown in the
249 inset), which are separated by a time interval of 20 ns.

250

251 For an observed pile-up pulse waveform, two parameters can be easily estimated
252 from its shape, i. e. the amplitude ratio A_r and time intervals T_i between the second
253 peak and the first peak. The four pile-up models are constructed continuously until
254 their A_r and T_i agree with those of the pile-up pulse using an iterative algorithm
255 proceeding as follows:

256 (1) The A_r and T_i of the detected pile-up pulse are obtained with the first-order
257 derivative method described in section 3.2.

258 (2) The pile-up pulse is normalized to the amplitude of its first peak.

259 (3) A standard pulse (neutron or γ) is added with another standard pulse (neutron or γ)
260 multiplied by $k=(0.7+n)\cdot A_r$ (the initial value of n is set to 0) with the temporal
261 separation of T_i to form four types of models.

262 (4) For each model, the sum pulse is normalized to the amplitude of its first peak, and
263 then the amplitude ratio between the second peak and the first peak A_r' , which is
264 the amplitude of the second peak after the normalization, is obtained.

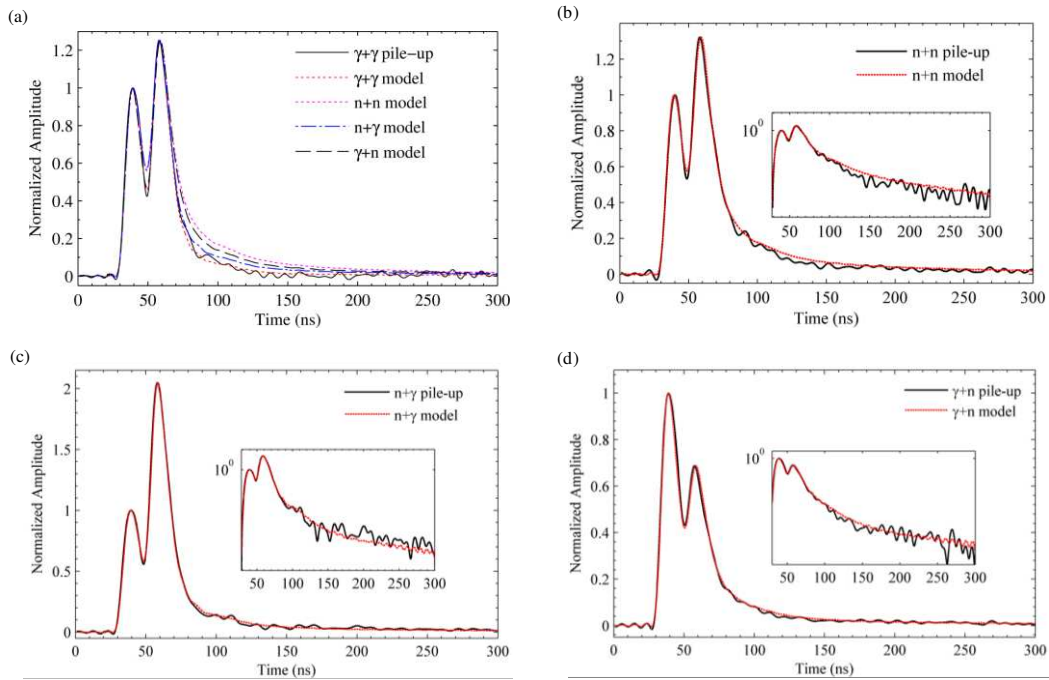
265 (5) If A_r' is smaller/bigger than A_r , then n is increased/decreased by 0.001 and the
266 process continues from step 3. If A_r' is equal to A_r , the iteration ends and the four
267 models come to convergence.

268 Subsequently, the four models are evaluated point-by-point to the pile-up pulse
269 that is normalized to the amplitude of its first peak respectively, and the model which
270 has the minimum difference is determined as the type of the pile-up pulse
271 ($\gamma+\gamma/n+n/n+\gamma/\gamma+n$). In order to evaluate the difference, the factors of “minimum
272 absolute value of the sum of point differences”, “minimum sum of absolute values of
273 point differences”, “minimum sum of quadratic point differences”, and “minimum
274 sum of quadratic relative point differences” were used respectively, it turned out that
275 the method has the highest correct percentage when using the factor of “minimum
276 absolute value of the sum of point differences”. The reason is that this factor takes
277 into account plus-minus differences, while other factors make all differences positive.
278 While in this case, the factor is used to evaluate the degree of fitting between the
279 model and the pile-up pulse, so it's better to include both negative and positive
280 differences. Therefore, the “minimum absolute value of the sum of point differences”
281 is chosen as the factor to compare between the pile-up pulse and the models. After the
282 model type is determined, the original constituent pulses giving rise to the pile-up
283 event are reconstructed as the first standard pulse multiplied by A_1 (amplitude of the
284 first peak of the pile-up pulse) and the second standard pulse multiplied by $k\cdot A_1$.

285 For a proof of principle testing, synthetic pile-up data have been generated for
286 four pile-up types respectively by randomly choosing pairs of single pulses of known
287 types and adding them together with a controllable temporal separation, ranging from
288 20 ns to 60 ns in steps of 4 ns. The dataset for each case consisted of 10,000
289 synthesized pile-up pulses. The single pulses of known types were acquired by
290 performing n- γ discrimination with the combination of the CC method and the TOF
291 measurement as shown in Fig. 4, with no extra threshold other than the CFD hardware

292 threshold of approximately 30 keVee. The dynamic range of these pulses, defined as
 293 the ratio between the maximum and minimum amplitude pulses, was found to be
 294 around 50. Four examples of the recovery of pile-up signals separated by 20 ns
 295 between two peaks are given in Fig. 6, which shows the normalized pile-up pulses,
 296 along with the corresponding models. It can be seen that the pile-up pulses all fit very
 297 well with the corresponding models both on a linear scale, as well as on a logarithmic
 298 scale shown in the insets. It is also clear from Fig. 6(a) that the other three models
 299 except the $\gamma+\gamma$ model are distinct from the pile-up pulse in shape, mainly in the tail
 300 and the valley between the two peaks.

301

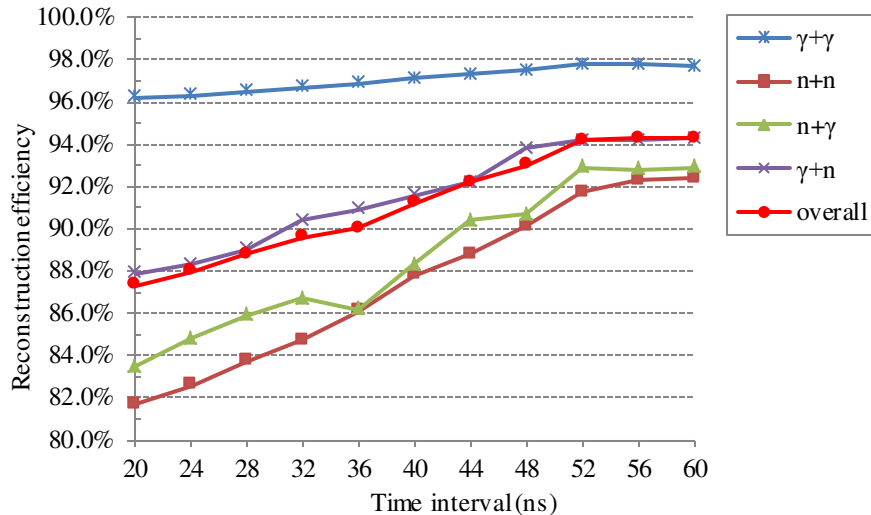


302

303

304 **Fig. 6.** Four types of pileup pulses which are separated by 20 ns and fitted with the
 305 corresponding models: (a) $\gamma+\gamma$, (b) $n+n$, (c) $n+\gamma$, and (d) $\gamma+n$.

306 Furthermore, the efficiency of the pile-up reconstruction method as a function of
 307 the time interval between two pulses constituting a pile-up event has been investigated
 308 using the synthetic pile-up data. Figure 7 illustrates the percentages of correctly
 309 reconstructed pile-up events for each type with varying time intervals between two
 310 constituent pulses, as well as the overall correct percentage for pile-up events
 311 comprising of same counts of pulses belonging to the four pile-up types, which is
 312 more realistic in practical nuclear experiments. It was found that a good performance
 313 in resolving pile-up events can be obtained from a time interval of 20 ns onwards. The
 314 overall correct percentage is around 90% with time intervals from 20 ns to 48 ns,
 315 while the error of reconstructing pile-up events can be kept below 6% when
 316 successive peaks are separated by more than 50 ns. It should be noted that this method
 317 almost failed to reconstruct pile-up pulses with time intervals below 20 ns, as the
 318 reconstructing accuracy deteriorated sharply from 20 ns downwards.



320 **Fig. 7.** The percentages of correctly reconstructed pile-up events versus the separation time between the
 321 two constituent pulses.

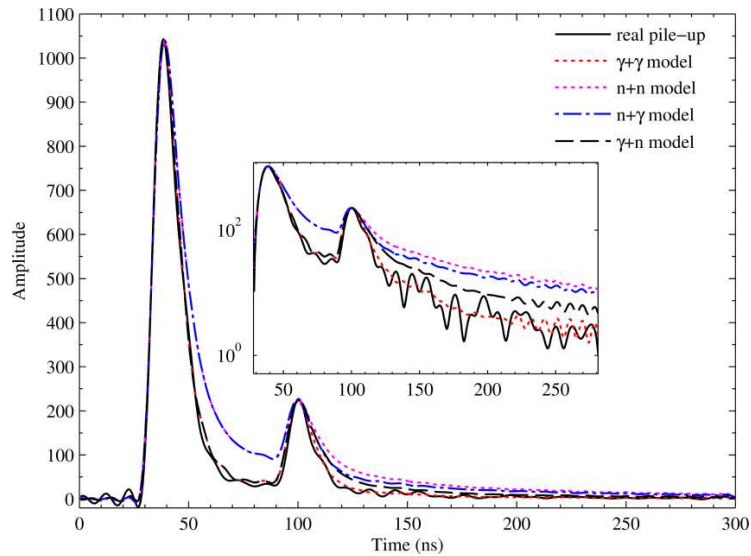
322 The results also indicate that the efficiency of the pile-up identification and
 323 reconstruction method depends on the type of pile-up pulses, and the time interval
 324 between the two constituent pulses. In general, the correctly reconstructed fractions of
 325 all types of the pile-up events improve as the time intervals increase. Meanwhile, the
 326 performance of the method varies among different types of pile-up events, while the
 327 type of $\gamma+\gamma$ has the highest efficiency. This is reasonable as the pulse width of the
 328 standard γ -ray pulse is relatively narrow compared with that of the standard neutron
 329 pulse, thereby leading to less information lost in a pile-up pulse with a certain time
 330 interval between two peaks. For each case there are always some mistakenly
 331 reconstructed pile-up events that are caused by two reasons. One is the intrinsic
 332 limitation of the method when dealing with extreme cases, in which the pulse
 333 amplitude ratio is too large or the pulse temporal separation is too small. The other
 334 one is the type of pulses that are used for generating synthetic pile-up data sets can
 335 contain some misinterpreted neutron-gamma events, even though both the CC method
 336 and the TOF measurement were combined to discriminate them. Therefore, some
 337 correct reconstruction cases could be misclassified as wrong cases, as the pre-known
 338 types of the constituent pulses are in themselves wrong. However, the large
 339 percentages of correctly reconstructed pile-up events has demonstrated the
 340 effectiveness of this method, allowing it to be used for correcting the spectra distorted
 341 by pile-up events as shown in next section.

342 **4. Application of the new method to NEDA data**

343 In order to further evaluate the performance of the pulse pile-up identification
 344 and reconstruction method presented, it has been applied to the pile-up events from
 345 the high count-rate measurement described in Section 2.

346 By applying the approach of pulse pile-up identification and reconstruction to the
 347 experimental data, 66916 pile-up events have been detected in a total of 92239 events,
 348 which account for approximately 72.5% of the total events. It was empirically found

349 that the method was able to locate the positions and to measure the amplitudes of the
 350 peaks in the pile-up events automatically and reconstruct them accurately, even
 351 though the peaks were randomly spaced in time and vary in amplitude. It should be
 352 noted that reconstruction processing here was restricted to the pile-up pulses arising
 353 from two events. Figure 8 shows an example of real pile-up identification and
 354 reconstruction. Despite the large pulse amplitude ratio between the two peaks, the
 355 result of resolving the pile-up event is quite satisfactory.

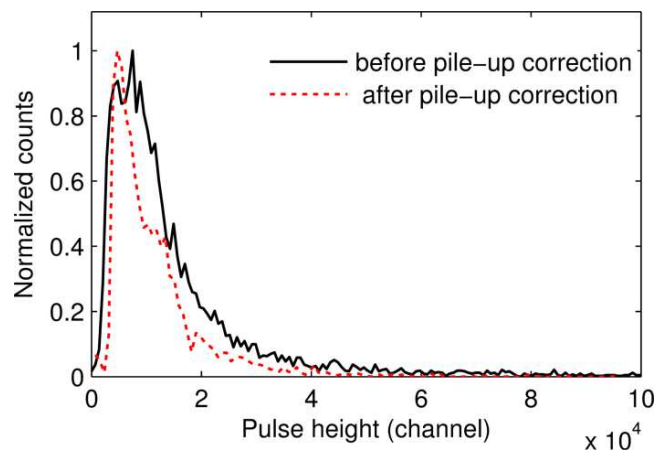


356

357 **Fig. 8.** A case of pile-up identification and reconstruction in the high counting rate measurement.

358

359 Rather than discarding the pile-up pulses, the new method can now allow them to
 360 be included in spectral analysis. Figure 9 shows the neutron pulse height spectra of
 361 ^{252}Cf before and after the pile-up correction, obtained by summing sampling points
 362 over the whole pulse width. Severe spectral distortions can be seen in the pulse height
 363 spectrum of the signals without pile-up correction. These distortions owing to pile-up
 364 events have been corrected significantly after applying the pulse pile-up identification
 365 and reconstruction method.



366

367 **Fig. 9.** The neutron pulse height spectra of ^{252}Cf before and after the pile-up correction (66916 pile-up
 368 events have been detected and reconstructed in a total of 92239 events).

369

370 **5. Conclusions**

371 A new method designed to deal with digital pulse pile-up identification and pulse
372 reconstruction is presented in this paper. The digitised waveforms used for developing
373 and validating the method were acquired with an experimental setup consisting of a
374 ^{252}Cf source, a BC-501A detector and a SIS3530 digitiser with a sampling rate of 500
375 MHz and with 12-bit resolution. When identifying pile-up events by searching for the
376 downward-going zero-crossings in the smoothed first-order derivative of the original
377 pulse, the method was less vulnerable to fluctuations in the signal compared with the
378 conventional maximum peak search method. Moreover, rather than discarding the
379 detected pile-up pulses, as is the case in hardware-based pile-up rejectors, this method
380 allows the reconstruction of the individual components of the pile-up events
381 employing four models that are generated by combining pairs of neutron and γ
382 standard pulses. Tests performed both on synthetic and experimental data
383 demonstrated that the method was capable of recovering two overlapping signals with
384 a high accuracy even when they are spaced in time as close as 20 ns. However, it
385 should be noted that the method can only be applied to pile-up events where two
386 pulses overlap. Since this method can provide reliable information of the constituent
387 particles of the pile-up events, thus avoiding losses of counting statistics and
388 distortions of pulse height spectra, it is of practical use to eliminate pulse pile-up
389 effects on the neutron-gamma discrimination performance of liquid scintillator
390 detectors used at high count rates.

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