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1 **Title:** Dynamical links between small- and large-scale mantle heterogeneity:  
2 seismological evidence

3

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16 **Abstract**

17

18 We identify PKP•PKP scattered waves (also known as P'•P') from earthquakes

19 recorded at small-aperture seismic arrays at distances less than 65°. P'•P' energy

20 travels as a PKP wave through the core, up into the mantle, then scatters back down

21 through the core to the receiver as a second PKP. P'•P' waves are unique in that they

22 allow scattering heterogeneities throughout the mantle to be imaged. We use array-

23 processing methods to amplify low amplitude, coherent scattered energy signals

24 and resolve their incoming direction. We deterministically map scattering

25 heterogeneity locations from the core-mantle boundary to the surface. We use an

26 extensive dataset with sensitivity to a large volume of the mantle and a location  
27 method allowing us to resolve and map more heterogeneities than have previously  
28 been possible, representing a significant increase in our understanding of small-  
29 scale structure within the mantle. Our results demonstrate that the distribution of  
30 scattering heterogeneities varies both radially and laterally. Scattering is most  
31 abundant in the uppermost and lowermost mantle, and a minimum in the mid-  
32 mantle, resembling the radial distribution of tomographically derived whole-mantle  
33 velocity heterogeneity. We investigate the spatial correlation of scattering  
34 heterogeneities with large-scale tomographic velocities, lateral velocity gradients,  
35 the locations of deep-seated hotspots and subducted slabs. In the lowermost 1500  
36 km of the mantle, small-scale heterogeneities correlate with regions of low seismic  
37 velocity, high lateral seismic gradient, and proximity to hotspots. In the upper 1000  
38 km of the mantle there is no significant correlation between scattering  
39 heterogeneity location and subducted slabs. Between 600 and 900 km depth,  
40 scattering heterogeneities are more common in the regions most remote from slabs,  
41 and close to hotspots. Scattering heterogeneities show an affinity for regions close  
42 to slabs within the upper 200 km of the mantle. The similarity between the  
43 distribution of large-scale and small-scale mantle structures suggests a dynamic  
44 connection across scales, whereby mantle heterogeneities of all sizes may be  
45 directed in similar ways by large-scale convective currents.

46 **Keywords:** seismology; deep Earth; scattering; mantle structure; mantle dynamics;  
47 seismic arrays

48

49 **1. Introduction**

50           The high frequency ( $\sim 1$  Hz) seismic wavefield provides evidence of  
51 kilometre scale structure within the Earth [Cleary and Haddon, 1972]. Seismic  
52 energy that is not explained by wave propagation in smoothly varying velocity  
53 models of the Earth has been attributed to reflections and scattering from sharply  
54 contrasting volumetric heterogeneities and roughness on interfaces [Chang and  
55 Cleary, 1981]. The interaction of the wavefield with discrete, small-scale variations  
56 in elastic properties and/or density can divert seismic energy onto new paths, often  
57 generating precursors or postcursors (coda) to the main seismic phases that travel  
58 in the great circle plane. The size of the scatterers that can be imaged is dependent  
59 upon the wavelength that is analysed; for the teleseismic high-frequency P-  
60 wavefield above 1 Hz they are typically on the order of 1 to 10 km.

61           Global imaging of Earth's small-scale heterogeneities is difficult due to the  
62 uneven distribution of earthquake sources and seismic receivers, and the low  
63 amplitude of the scattered signals involved. Scattering can be studied using single  
64 stations, but with this approach the location of the scattering heterogeneity can be  
65 ambiguous [Wen, 2000]. Alternatively, seismic arrays, i.e., 3 or more closely located  
66 sensors, can resolve the incoming direction of scattered waves, thus it is possible to  
67 deterministically locate heterogeneities [Thomas et al., 1999; Rost and Earle, 2010;  
68 Frost et al., 2013]. In the last few decades a number of studies have started to  
69 unravel the distribution of small-scale heterogeneities of Earth's mantle. Hedlin et al.  
70 [1997], and later Mancinelli and Shearer [2013, 2016] studied the depth  
71 distribution of heterogeneity within the mantle through analysis of PKP pre- and  
72 postcursors recorded at single stations. Using a stochastic Rayleigh-Born scattering

73 approach, Mancinelli and Shearer [2013, 2016] developed a global model of  
74 scattering heterogeneity containing 0.1% root-mean-square velocity variations in  
75 the deepest 1200 km of the mantle with heterogeneity scale sizes ranging from 2 to  
76 30 km.

77 This work is complemented by studies that deterministically map small-scale  
78 scattering heterogeneity within the upper and lower mantle. These studies have  
79 noted lateral variations in heterogeneity distribution, as well as variations in  
80 amplitudes of scattered waves. Scattered P-to-P (P•P, where the “•” represents the  
81 location of scattering) and P-to-S (P•S) waves are sensitive to heterogeneities in the  
82 upper half of Earth’s mantle; they have been used to map scattering heterogeneity in  
83 regions influenced by recent subduction [Kaneshima and Helffrich, 1998; Bentham  
84 and Rost, 2014]. Scattering in the lowermost mantle has also been observed to vary  
85 laterally [Waszek et al., 2015]. Strong scattering has been observed in regions  
86 beneath mantle hotspots [Wen, 2000], near small, regional ultra-low velocity zone  
87 (ULVZ) structures [Yao and Wen, 2014], beneath subduction zones [Miller and Niu,  
88 2008], and near the edges of LLSVPs [Frost et al., 2013]. A near-global study of  
89 PK•KP – a PKP wave that is back-scattered in the lower mantle onto a second PKP  
90 path – suggests a spatial correlation between scattering and LLSVP edges in the  
91 lowermost 300 km of the mantle [Rost and Earle, 2010; Frost et al., 2017].

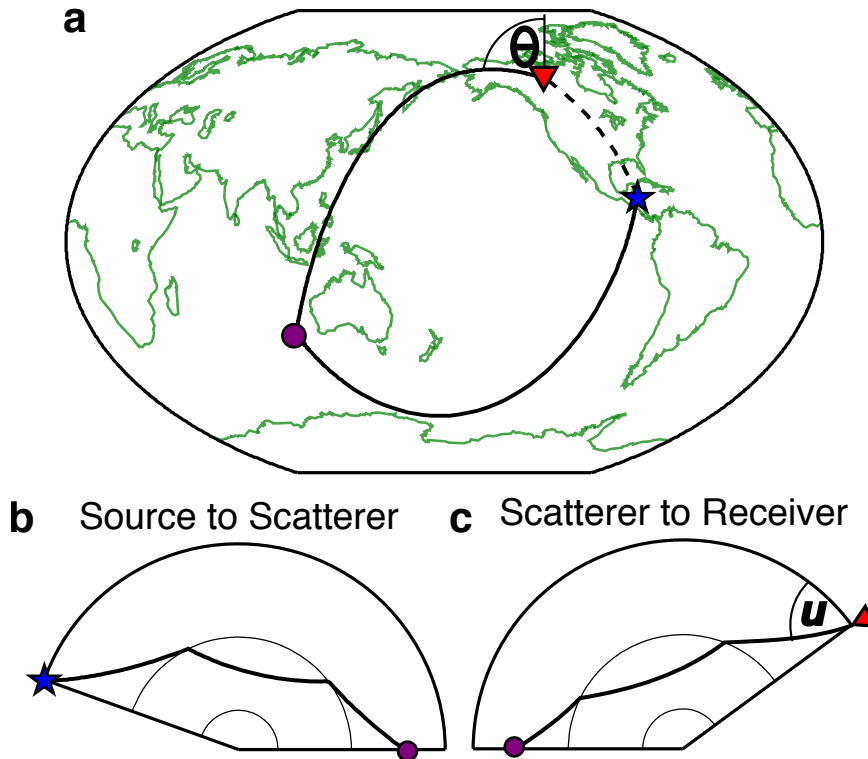
92 The volume of the mantle that can be investigated for scattering  
93 heterogeneity is controlled by the specifics of the seismic probe. PK•KP can be used  
94 to investigate the lower mantle close to the CMB [Chang and Cleary, 1981; Rost and  
95 Earle, 2010; Frost et al., 2017]. The direct wave PKPPKP (also called P’P’) results

96 from a PKP wave ( $P'$ ) reflecting from the underside of the surface, back into the  
97 Earth as a second PKP wave, along the great-circle path (GCP). This phase can be  
98 preceded by scattered energy called PKP•PKP ( $P'•P'$ ), caused by back-scattering of  
99 PKP at any depth in the mantle [Rost et al., 2015]. Like PK•KP,  $P'•P'$  has an unusual  
100 scattering geometry (Fig. 1) and can scatter from locations off the GCP, and the  $P'$   
101 segments need not be symmetric to each other.  $P'•P'$  is the continuation of PK•KP  
102 towards the surface, thus this phase is able to sample the whole mantle from CMB to  
103 crust (Fig. 2). We extend our earlier work and investigate the mantle upwards from  
104 the CMB to the surface to deterministically map the vertical and lateral distribution  
105 of scattering heterogeneities throughout the mantle. In contrast to other scattering  
106 probes, the unusual (and versatile) raypath geometry of  $P'•P'$  allows the study of  
107 previously unsampled regions of the Earth.

108         The internal structure of the Earth and the nature of mantle convection are  
109 inherently connected across scales [e.g. Tackley 2015]. The distribution of large-  
110 scale mantle structure as imaged by seismic tomography has been investigated  
111 using thermo-chemical geodynamic models, which indicate that downwelling of cold,  
112 dense slabs at subduction zones moves and shapes the hot, convecting piles of  
113 seismically slow material at the CMB, forming the Large Low Shear Velocity  
114 Provinces (LLSVPs) [McNamara and Zhong, 2005; Li et al., 2014; Domeier et al,  
115 2016]. The LLSVPs, if compositionally distinct, may modulate mantle dynamics  
116 through thermal instabilities that result in mantle plumes that rise up causing  
117 hotspot volcanism [Thorne et al., 2004; French and Romanowicz, 2015].  
118 Furthermore, calculations suggest that mantle plumes may be spatially correlated

119 with the LLSVPs [Thorne et al., 2004; Doubrovine et al., 2016]. Geodynamic  
120 modelling of thermo-chemical structures in the deep mantle indicates that small-  
121 scale heterogeneities (as small as kilometre-sized) can be passively transported in  
122 the large-scale flow [Brandenburg and van Keken, 2007; Li et al., 2014, Mulyukova  
123 et al., 2015]. Furthermore, geochemical analysis of intraplate volcanism suggests  
124 that heterogeneities situated in the deep Earth may be transported to the surface by  
125 entrainment in mantle convection [Williams et al., 2015]. Therefore, there is  
126 compelling evidence that the distribution of small-scale seismic structure in the  
127 mantle is linked to the large-scale structures.

128         Here we use a global collection of earthquakes recorded at seismic arrays to  
129 identify  $P'\bullet P'$  and deterministically locate the position of the causative volumetric  
130 scattering heterogeneity within the mantle. We investigate the relationship between  
131 scattering heterogeneity and other seismologically imaged structures in the mantle.  
132 We use our observations to understand the distribution of small-scale  
133 heterogeneities throughout the whole of the mantle, and the connection with  
134 dynamic processes.



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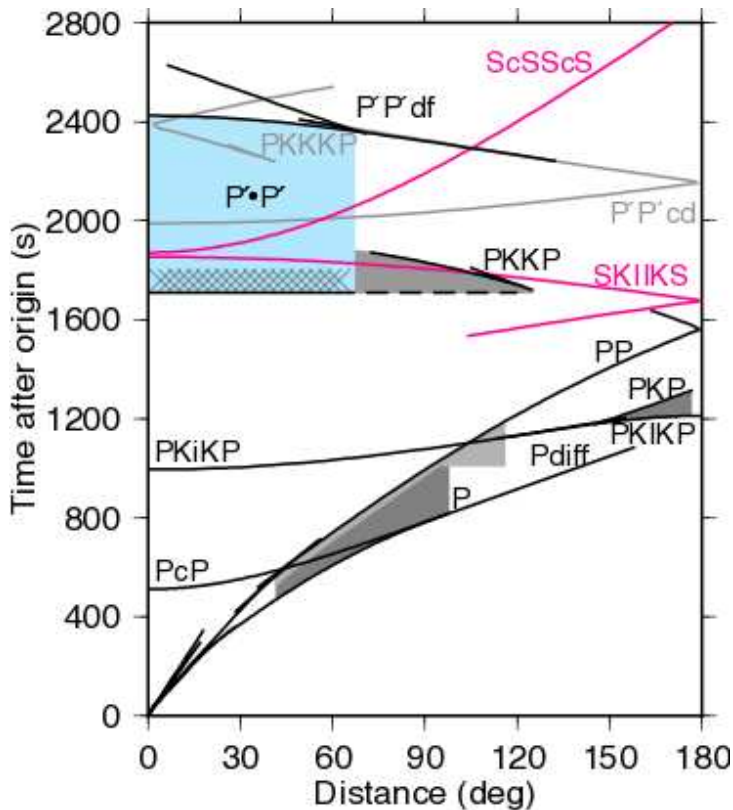
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**Figure 1:** PKP•PKP ( $P'•P'$ ) example path. **(a)** A  $P'•P'$  path from the source (star) to a scattering point in the mantle (circle) and then to the receiver (triangle).  $P'•P'$  travels along two great-circle paths (solid lines) to and from the scattering point, off the great-circle path between the source and receiver (dashed line). PKP ray paths from **(b)** source to scatterer ( $PKP_{ab}$ ) and **(c)** scatterer to receiver ( $PKP_{bc}$ ). The two PKP legs may be symmetric or asymmetric (as in this case) and can scatter from any depth in the mantle from the CMB to the surface. Rays observed at the surface arrive from a specific direction known as the back-azimuth,  $\theta$ , measured relative to North, or the relative back-azimuth measured from the GCP, and from a vertical incidence angle, referred to as the slowness,  $u$ .

[SINGLE OR 1.5 COLUMN FIGURE]



152  
 153 **Figure 2:** Travel-time curve displaying  $P'\bullet P'$  and other scattered phases in the high-  
 154 frequency seismic wavefield. Black lines mark major P-wave phases. The blue region  
 155 marks the time and distance region investigated for  $P'\bullet P'$  waves in this study.  
 156 Hatched region marks time and distance region investigated for  $PK\bullet KP$  in Frost et al.,  
 157 [2017]. Grey and pink lines mark the P- and S-waves, respectively, that may  
 158 contaminate the  $P'\bullet P'$  study region. Other P- and S-waves are not shown for clarity.  
 159 Differently shaded grey regions denote time and distance regions previously  
 160 investigated for other scattered waves. Adapted from Rost et al., [2015].

161 [SINGLE COLUMN FIGURE]

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## 163 **2. Data**

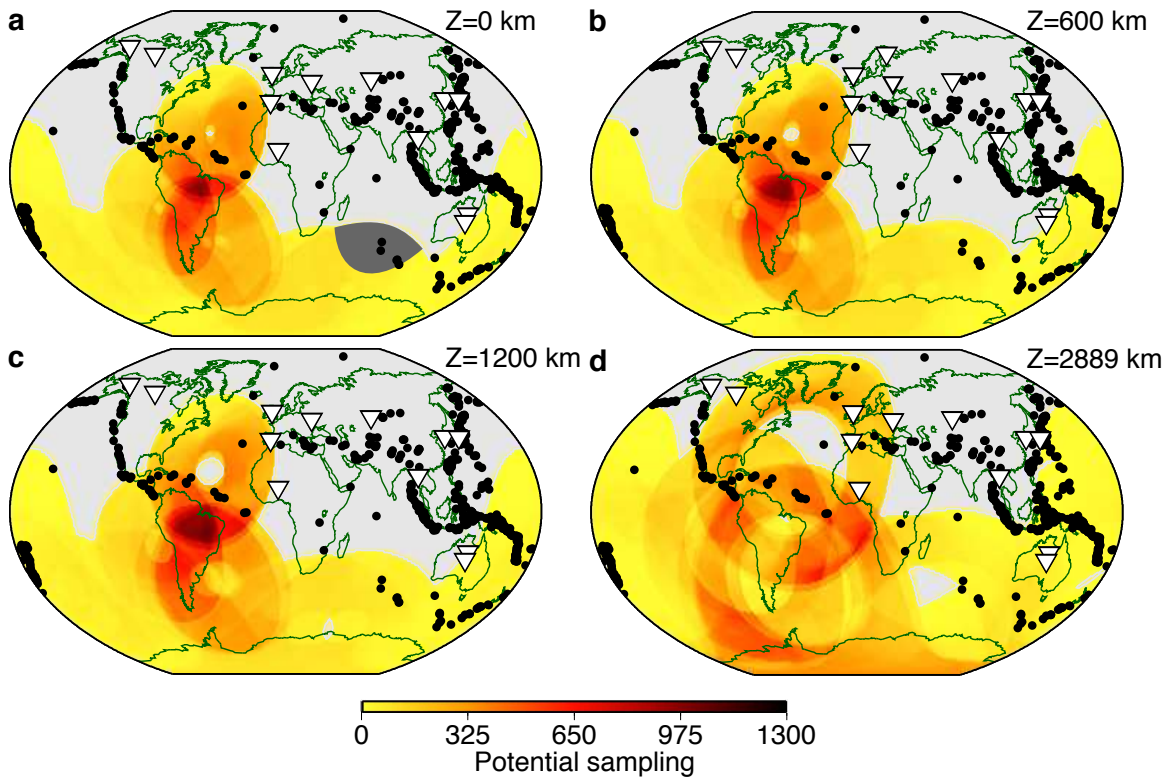
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166 We collect data from 643 earthquakes at any depth with magnitudes  $M \geq 6$   
 167 recorded at up to 12 small and medium aperture arrays within  $65^\circ$  of any event (Fig.  
 168 3). The arrays contain a mixture of short period and broadband instruments; we use  
 only the most common instrument type in each array. These arrays were designed

169 to determine the directivity of short-period P-waves thus are ideally suited for  
170 analysis of high-frequency scattered waves. The aperture of an array controls its  
171 directivity resolution, thus we select only arrays with apertures of 10km to 30 km to  
172 ensure that we are able to resolve well the incoming direction of waves.

173         Each event-array pair has a specific geographical volume of the mantle from  
174 which possible  $P' \bullet P'$  scattered waves can be detected (Fig. 3). The size and shape of  
175 the sampling region at any given scattering depth is dependent on the event-array  
176 distance. Using estimations of the potential scattering volumes combined for all  
177 source-array pairs, we develop a “potential sampling density map” of our dataset for  
178 different depths, which represents the abundance of scatterers we would detect if  
179 the actual distribution of scattering in the Earth distribution were uniform. The  
180 potential scatterer sampling distribution of the dataset is uneven, but in contrast to  
181 other probes, the southern hemisphere is well covered throughout the depth of the  
182 mantle, allowing investigation of the relationship between scattering  
183 heterogeneities and the South and Central American subduction zones, and the  
184 African and Pacific LLSVPs.



185  
 186 **Figure 3:** Earthquakes (dots) and arrays (triangles) in our dataset and resultant  
 187 potential  $P' \bullet P'$  scattering sampling. The 643 events and up to 12 arrays yielded  
 188 1715 event-array pairs. Global sampling distributions are constructed by  
 189 summation of the potential scattering sampling for all source-array pairs at: **(a)**  
 190 the surface (0 km depth); **(b)** transition zone (600 km depth); **(c)** mid-mantle (1200 km  
 191 depth); and **(d)** the Core-Mantle Boundary (2889 km depth). Sampling is densest in  
 192 the mid-mantle and most geographically extensive in the lowermost mantle. Grey  
 193 wedge in **(a)** displays an example of the potential scattering regions for a single  
 194 event-array pair.

195 [2 COLUMN FIGURE]

196

197

### 198 **3. Methods**

199

200 We investigate energy associated with mantle scattering in a time window

201 from the first possible arrival of  $P' \bullet P'$  at  $\sim 1700$ s after the earthquake origin time

202 (for a surface focus event) corresponding to scattering at the CMB, up to the first

203 possible arrival of the direct wave  $P' \bullet P'_{df}$  at  $\sim 2400$ s, which is the earliest  $P' \bullet P'$  GCP  
204 phase, reflecting from the underside of the surface on the antipodal side (Fig. 2).  
205  $P' \bullet P'$  scattering related to interactions with small-scale mantle heterogeneity is  
206 feasible for any time and distance in this window (blue shaded region in Fig. 2).

207 We de-trend the data and discard any discontinuous traces i.e. gaps in the  
208 recording. The remaining traces are filtered with a 2<sup>nd</sup> order bandpass between 0.5  
209 and 2 Hz to enhance the frequencies most associated with small-scale scattering in  
210 past studies that investigated frequency content [Mancinelli et al., 2016; Frost et al.,  
211 2017]. We search for scattered signals within the wavefield data using fk-analysis  
212 (frequency-wavenumber), which performs a grid-search over incoming directions  
213 to maximise coherence (the similarity of two or more signals in the frequency  
214 domain) of the signal stacked across the array, calculated in the frequency domain  
215 [Capon, et al., 1967]. We search over slownesses from 0 to 8 sec/deg and back-  
216 azimuths between  $-180^\circ$  to  $180^\circ$  relative to the GCP. By selecting signals with the  
217 highest coherence we determine the best fitting slowness vector (a combination of  
218 the back-azimuth,  $\theta$ , and the horizontal slowness,  $\underline{u}$ ) of the incoming signals in the  
219 scattering search time-window (1700s to 2400s after earthquake origin). To  
220 improve the resolution of the slowness vector of incoming signals, as well as to  
221 further increase the prominence of signals above the noise, we apply the F-statistic  
222 to the fk-analysis (Fig. 4) [Blandford, 1974; Selby, 2011]. The F-statistic calculates  
223 the ratio of the amplitude of the stacked signal to the sum of the differences between  
224 the stack and each trace used to form the stack. The F-trace has the effect of  
225 penalising stacks that differ from individual input traces i.e. signals that are

226 incoherent across the array. Thus, the best fitting slowness and back-azimuth from  
227 the grid-search are those that produce the most representative stack of the  
228 individual array traces. By performing these calculations in the frequency domain  
229 we increase efficiency by reducing the number of transformations required between  
230 the time and frequency domains. However, the fk approach returns a single value of  
231 coherence from each slowness vector averaged across the whole time window, thus  
232 collapsing the time axis. Combining the F-statistic with traditional fk-analysis results  
233 in much-improved slowness vector resolution, even for the small-aperture arrays  
234 used here [Frost et al., 2013]. Thus the origin of the scattered energy can be more  
235 precisely estimated.

236         We measure the slowness and back-azimuth of the most coherent signals  
237 received at the array in consecutive 50 s long time windows (Fig. 4). This window  
238 length gives depth resolution comparable to that obtained in global tomography  
239 models, and is sufficient to identify broad-scale trends in scattering distribution,  
240 both laterally and with depth. We assume the arrival time of a signal to be the  
241 middle of the 50 s time window, and given that scattering of  $P' \bullet P'$  from a range of  
242 depths can arrive at the array with similar travel-times, each 50 s time window that  
243 we investigate is sensitive to scattering from a 50 to 200 km thickness of the mantle.  
244 The thickness of the scattering region that each time window is sensitive to  
245 decreases with scattering depth hence, at shallower depths, there is overlap in  
246 depth sensitivity between windows – adjacent time windows can contain energy  
247 scattered from the same depth (albeit from different locations).

248 Mantle scattered  $P' \bullet P'$  waves are expected to arrive with slownesses  
249 between 2.1 and 4.4 s/deg. The range of directions from which  $P' \bullet P'$  waves can be  
250 observed is dependent upon the event-array distance and scattering depth. Array  
251 analyses permit recognition and omission of contaminating waves by determination  
252 of the incoming direction of energy, compared with the directions possible for  $P' \bullet P'$ .  
253 We compute the expected arrival times for possible contaminating waves: direct  
254 phases, depth phases, and multiple reflections of both P- and S-waves. We do not  
255 calculate multiples reflecting off upper mantle discontinuities (i.e. a downgoing  
256 wave reflecting off the 660 km discontinuity, then reflecting back down from the  
257 410 km discontinuity). Contaminating waves would likely be detected along the  
258 GCP (we take both minor and major arc arrivals into account). In contrast,  $P' \bullet P'$   
259 scattered energy most commonly arrives off the GCP, allowing clear identification of  
260 the scattered arrivals. However, at short event-array distances it is possible for  $P' \bullet P'$   
261 to arrive along the GCP; these situations can be predicted and extra care is taken to  
262 exclude contaminating phases. As there are few phases that can arrive within the  
263  $P' \bullet P'$  window (Fig 2), we would expect few time windows to be contaminated by  
264 other seismic phases. Nonetheless, we discard any time window where we both  
265 observe a signal within 20 degrees of the GCP (in major or minor arc directions) and  
266 any known seismic wave is predicted to arrive in the same time window and along  
267 the same backazimuth (i.e. minor or major great-circle path) (e.g Fig. 4d). Of all  
268 identified signals, only 2% match the time and direction predicted for known  
269 seismic phases, and thus are discarded.

270           The wavefield may also be contaminated by foreshocks or aftershocks to the  
271 analysed events, thus we exclude from further analysis any scattered signals where  
272 any magnitude  $\geq 6$  earthquake occurs within two hours of the origin time of the  
273 studied earthquake (11% of identified scattered signals). As a further test we  
274 remove any scattered signal that could be contaminated by a magnitude  $\geq 5$  event  
275 but find no systematic difference in the distribution of scattering heterogeneity. Our  
276 focus on core wave arrivals with slownesses from 2.1 to 4.4 s/deg helps to exclude  
277 contamination from smaller, closer events, which have higher slownesses associated  
278 with more horizontal incoming energy (and the discarding of GCP signals further  
279 minimizes energy from small local events contributing to data we analyse).  
280 Therefore, we are certain that our data selection prevents any contamination of the  
281 results by local and regional events. Lithospheric scattering directly beneath the  
282 array may redirect high slowness contaminating energy to lower slownesses typical  
283 of mantle scattering that we consider here. However, the direct contaminating wave  
284 would arrive in the same time window as the lithospheric scattered energy, and  
285 would likely be more coherent with an obviously inappropriate slowness. This  
286 allows a straightforward identification (and removal) of energy scattered from  
287 lithospheric structure.

288           After contaminated time windows have been removed, scattered signals are  
289 identified. We pick time windows containing energy prominently above the  
290 background noise level in f-k space and consistent with the directivity criteria for  
291  $P' \bullet P'$  scattering (e.g. Fig. 4b). We identify the slowness and back-azimuth of the  
292 scattered signal, and select the time at the middle of the 50 s long window as

293 scattered travel time; therefore, we only identify one scattered signal per 50 s  
294 window. If multiple  $P' \bullet P'$  signals are observed in the same time window we retain  
295 the signal with the highest coherence, as this will be the best spatially resolved.  
296 Multiple waves arriving at a similar time, either scattered or direct, may interfere  
297 causing the apparent arrival direction of energy at the array to be incorrect. The  
298 apparent signal would likely appear blurred across directions, thus we only select  
299 signals with tightly resolved slowness and back-azimuth (within the capabilities of  
300 the array).

301         The back-azimuth, slowness, and time information for each scattered signal  
302 are used to calculate a scattering location in the mantle. The back-azimuth of a  
303 signal indicates the horizontal direction along which the wave travelled while the  
304 slowness defines a discrete path for a 1D Earth model, and the travel-time relates to  
305 the scattering depth (Fig. S1). Thus there is a trade-off between the distance and  
306 depth of a scattered path, hence we attempt to fit both slowness and travel-time  
307 simultaneously with a grid search. We ray trace backwards from the array along the  
308 observed back-azimuth to a range of possible scattering depths and distances, and  
309 then ray-trace from these scattering locations to the source. Possible scattering  
310 locations are spaced every  $0.01^\circ$  in distance between the minimum and maximum  
311 possible path lengths of PKP along the resolved back-azimuth and 50 km in depth  
312 from the CMB to the surface. We model the scattering location by minimising the  
313 misfit between the calculated slowness and time for each potential scattering  
314 location and the observed values. Mapped scattering heterogeneity locations are  
315 discarded if traced rays to the solution location do not well fit the observed

316 slowness and time: if the squared slowness misfit (observed minus predicted) plus  
317 twice the squared time misfit is greater than 10, i.e. a weighting factor of 2 is used  
318 for travel time misfit and therefore we favour fitting scattering locations with small  
319 travel-time misfits. The misfit value selected fits signals within the slowness  
320 resolution limit of the arrays. Overall, of the original 4319 identified scattered  
321 signals, we discard signals contaminated by other events (11% of the original  
322 population), other phases (2%), and poorly fit signals (44%), leaving 1876 mapped  
323 scattering heterogeneities.

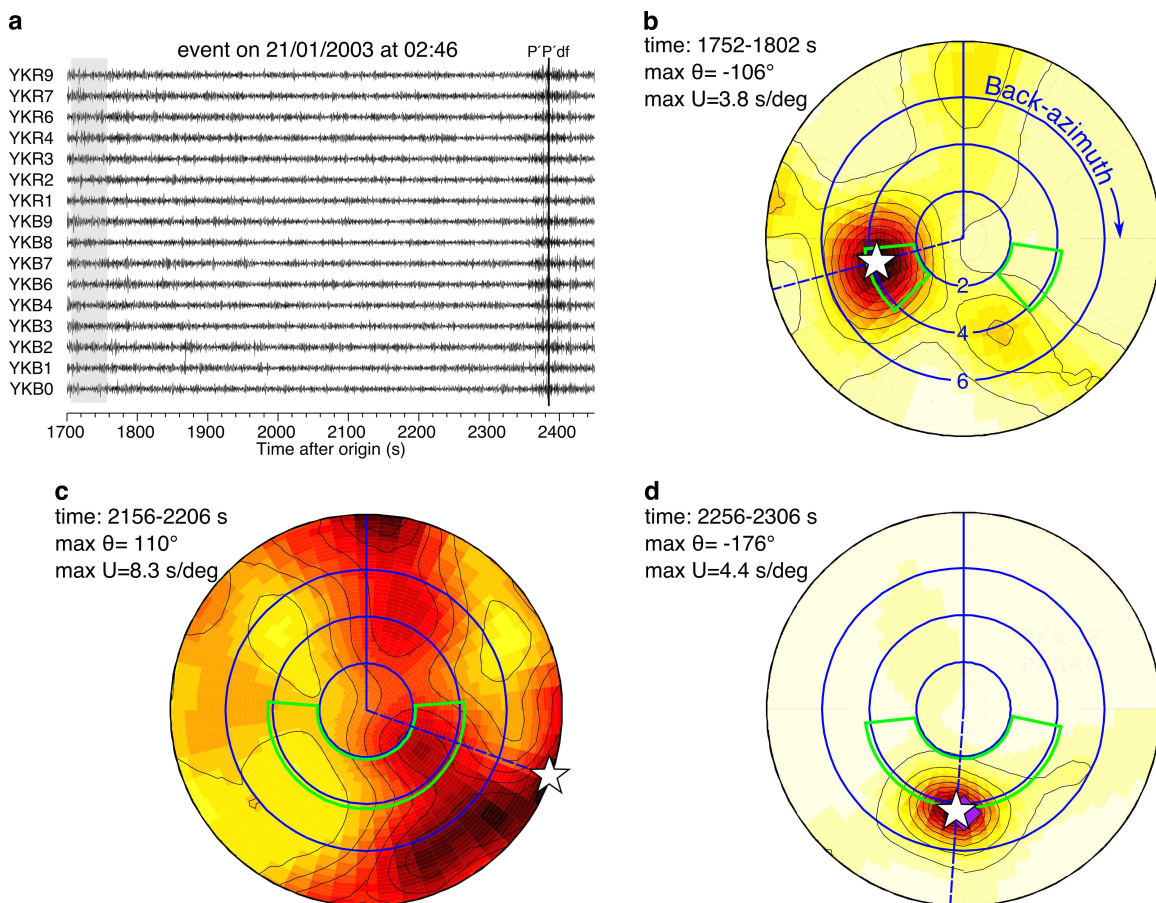
324         Due to the uncertainty in travel-time (from using the middle of the 50 s time  
325 window) and the uncertainty in slowness (due to the ability of the arrays to resolve  
326 the incoming direction) we determine the dimensions of the region that contains the  
327 heterogeneity based on these limitations. We calculate scattering locations for  
328 signals arriving at the start and end of the 50s time window, and with slowness  
329 variation of  $\pm 0.3$  s/deg relative to that measured at the array (estimated from the  
330 slowness spacing of the grid-search). This defines a region around the best fitting  
331 heterogeneity location that is, on average,  $\pm 100$  km laterally and vertically. For mid-  
332 mantle scattering at high slowness values ( $\sim 1000$ - $1800$  km depth), the error  
333 regions can occasionally grow to values as large as  $\pm 800$  km laterally and  $\pm 500$  km  
334 vertically but this larger misfit is only relevant for around 5% of the solution  
335 scattering locations, thus the majority of the scattering heterogeneities identified in  
336 our dataset are located to within  $\pm 100$  km vertically and laterally.

337         Sub-surface structure beneath the majority of the arrays used in this study  
338 has been demonstrated to have an insignificant effect on the resolved slowness and

339 back-azimuth (Bondar et al., 1999). Nevertheless, removing scattering  
 340 heterogeneities observed at Chiang Mai array, which is most affected by sub-surface  
 341 structure, dominantly reduces scattering in the upper 200 km of the mantle and  
 342 causes no significant change in our conclusions on the relationship with lower  
 343 mantle structure.

344

345



346

347 **Figure 4:** Array data are shown for **(a and b)** a magnitude 6.5 event, 24 km depth,  
 348  $52^\circ$  away from Yellowknife array, and **(c and d)** a magnitude 7.8 event, 0 km depth,  
 349  $37^\circ$  away from Warramunga array. **(a)** The time window for P'•P' scattering (1700-  
 350 2450 sec for this event, blue region in Fig. 2). The predicted time of the direct phase,  
 351 P'P'<sub>df</sub>, is shown by the vertical line, marking the end of the scattering window used  
 352 here. Data are filtered between 0.5 and 2.0 Hz. The grey shaded time window

353 corresponds to information shown in **(b)**. **(b)** f-k processing of the 50 sec time  
 354 window shown grey in **(a)**, displayed in terms of back-azimuth ( $\theta$ , azimuthal axis)  
 355 and slowness ( $u$ , radial axis outwards from 0 to 8 s/deg with rings marking 2 to 6  
 356 s/deg). Back-azimuth is measured relative to the great-circle path (vertical blue  
 357 line). The white star shows the maximum coherence in the f-k analysis, arriving with  
 358 relative back azimuth =  $-106^\circ$  (blue dashed line). The 90% coherence contour is  
 359 roughly  $\pm 10^\circ$  wide in back-azimuth and  $\pm 0.5$  s/deg in slowness around the  
 360 maximum. The green regions show the range of possible slownesses and back-  
 361 azimuths for  $P' \bullet P'$  waves scattering at this distance and the median depth of  
 362 scattering for this time window (from the shape of the potential scattering regions,  
 363 grey regions in Fig. 3). **(c)** f-k processing of a time window showing no clear  $P' \bullet P'$   
 364 waves. **(d)** f-k processing of a time window that is likely contaminated by the direct  
 365 phase PKKKP (predicted slowness and back-azimuth marked by purple diamond).  
 366 Time windows **(c)** and **(d)** are not picked for further processing.

367 [2 COLUMN FIGURE]

368  
 369  
 370

#### 371 **4. Results**

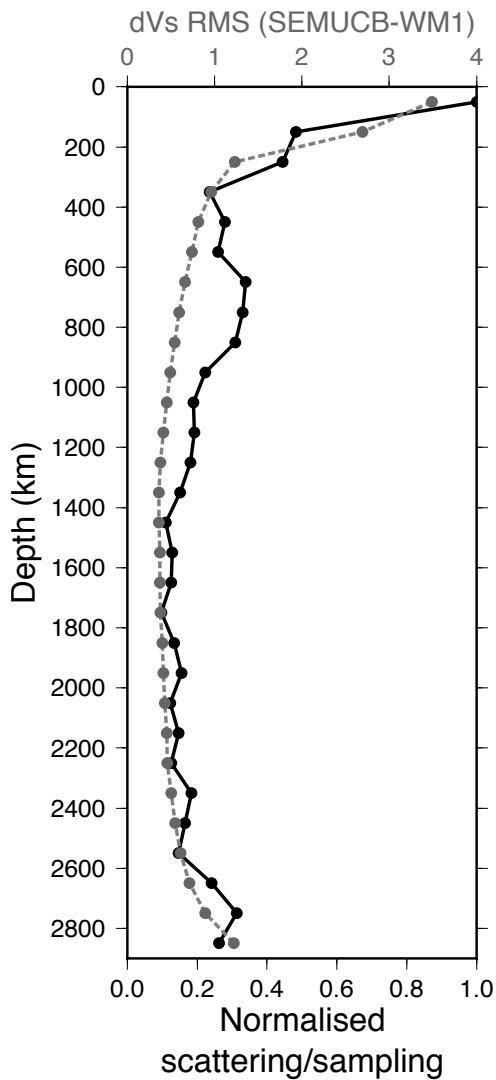
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 373

The mapped locations of scattering heterogeneities are unevenly distributed  
 374 in the mantle, both laterally and with depth. This is not unexpected given that the  
 375 potential sampling capacity of our dataset also varies in location and depth (Fig. 3).  
 376 We divide the number of mapped scatterers by the potential sampling density (Fig.  
 377 3) in order to compare relative scattering density for different regions. This  
 378 normalised scattering population shows that heterogeneities are distributed  
 379 throughout the mantle, but more abundant scattering heterogeneity is present in  
 380 the uppermost and lowermost mantle (Fig. 5). The radial scatterer distribution also  
 381 shows a small increase in scattering heterogeneity between 600 and 900 km depth,

382 just below the transition zone, and a minimum in the mid-mantle between 1400 to  
 383 1800 km depth.

384 We find that the radial abundance of small-scale scattering heterogeneity  
 385 matches the RMS amplitude of large-scale tomographic velocities (Fig. 5): scattering  
 386 is most common and the RMS variation of tomographic velocities is highest in the  
 387 uppermost and lowermost mantle. This correlation holds roughly for all  
 388 tomographic models (Fig. S2).

389  
 390



391

392 **Figure 5:** Normalised scattering heterogeneity density with depth (number of  
393 scatterers divided by number of samples in each 100 km thick layer) for the  
394 complete dataset (black, lower x-axis) and RMS of the shear velocity perturbations  
395 from the global tomographic model SEMUCB-WM1 (grey and dashed, upper x-axis)  
396 [French and Romanowicz, 2014]. The depth distribution of small-scale scattering  
397 heterogeneity roughly correlates with the RMS of long-wavelength dVs  
398 perturbations. Both lines are scaled to fit the same axis.

399 [SINGLE COLUMN FIGURE]

400

401

402 We investigate possible spatial correlation between the resolved scattering  
403 heterogeneities and large-scale mantle features, which may be interpreted as  
404 proxies for dynamic processes, as in Frost et al., [2017]. We compare the location of  
405 scattering heterogeneity to geographical regions beneath hotspots, subducted slabs,  
406 regions of high and low tomographic velocities, and regions of high and low lateral  
407 tomographic velocity gradients. The high/low velocities and gradients from  
408 tomographic models likely relate to the locations of LLSVPs and subducted slabs in  
409 the mantle. The spatial locations of scattering heterogeneities are shown,  
410 normalised by sampling, in the Supplementary Material, while the absolute latitude,  
411 longitude, and depth information for each scattering heterogeneity is shown in  
412 Supplementary Table 1

413

414

#### 415 4.1 Relationship between scattering heterogeneities and mantle structure

416 We compare the distribution of scattering heterogeneity with S-wave  
417 tomographic models, both because they are the basis for the definition of the Large

418 Low Shear Velocity Provinces, and also show consistency between models [Garnero  
419 et al., 2016]. We use several tomographic models: GyPSuM [Simmons et al., 2010],  
420 SEMUCB-WM1 [French and Romanowicz, 2014], S40RTS [Ritsema et al., 2011], and  
421 TX2011 [Grand, 2002]. Additional comparisons with P-wave models are shown in  
422 the supplementary material (Figs. S7-9). We calculate lateral velocity gradients from  
423 tomographic models, revealing abrupt changes in mantle structure, which thus  
424 serve as a proxy for boundaries of the LLSVPs [Thorne et al., 2004, Garnero et al.,  
425 2016]. We calculate gradients over a distance of  $10^\circ$  as the resulting gradients well  
426 replicate the margins of the LLSVPs found in forward modelling studies [Garnero et  
427 al., 2016 and references therein].

428         We use hotspots from the study of Courtillot et al. [2003]. French and  
429 Romanowicz [2015] analysed the tomographic model SEMUCB-WM1 [French and  
430 Romanowicz, 2014] and characterised hotspots based on associated tomographic  
431 velocity anomalies. We use the 20 hotspots that were labelled as either “primary” or  
432 “clear” meaning that the hotspot overlies a column of low velocities from the CMB to  
433 1000 km depth with dVs less than -1.5% or less than -0.5 %, respectively.

434         We use slab locations from the Regionalized Upper Mantle (RUM) model,  
435 which locates slabs at depth using intra-slab seismicity [Gudmundsson and  
436 Sambridge, 1998]. When comparing with scattering heterogeneity locations we use  
437 slab locations at the surface (zero depth). Slabs move only a small amount laterally  
438 as they subduct ( $\leq 5^\circ$  relative to the plate boundary at the surface [Steinberger et al.,  
439 2012]), which is unlikely to strongly influence our correlations.

440 To account for differences in the magnitude, range, and pattern of velocity  
441 anomalies and velocity anomaly gradients between tomographic models, and  
442 differences in the number of locations in of maps of hotspot and slab locations, we  
443 convert maps of tomographic velocities to maps of percentage cumulative area on a  
444 sphere sorted by decreasing velocity anomaly (from fast to slow). For example, the  
445 20% area corresponds to the area of the 20% highest tomography velocities of a  
446 given depth shell (Fig. 6). We only consider the regions of the tomographic models  
447 that match the regions sampled by the  $P'\bullet P'$  dataset at each depth. In this way, the  
448 highest and lowest velocities in several tomographic models with inherently  
449 differing amplitudes of velocity variation can be directly compared. We establish  
450 geographical area percentages associated with the locations of hotspots and  
451 subducted slabs by computing the cumulative area surrounding the features within  
452 specific distances from them (within the area sampled by the  $P'\bullet P'$  dataset). For  
453 example, the first 20% area for slabs corresponds to the region closest to slabs that  
454 adds up to 20% of the Earth's surface area; conversely the last 20% area indicates  
455 that amount of surface area furthest from slabs.

456 To estimate correlations between the abundance of small-scale scattering  
457 and subducted slabs, hotspots, tomographic velocities and gradients, we compare  
458 the location of these features to the distribution of scattering heterogeneity. For  
459 each 100 km depth shell, we count scattering heterogeneities in each 20% area  
460 division from the feature of interest. To account for the variability in sampling  
461 coverage of our dataset (Fig. 3), we count our estimation of potential scatterers  
462 (afforded by our event-array distributions) in the same 20% area regions, and

463 calculate the ratio of the number of observed-to-potential heterogeneities. This  
464 allows us to construct a map of normalised scattering prevalence, thus effectively  
465 removing the bias of our uneven sampling.

466         The first set of comparisons is displayed in Fig. 7 as a cumulative histogram  
467 as a function of depth. In the upper 200 km of the mantle, scattering heterogeneities  
468 are most common in regions of high velocity (Fig. 7a), which is evident from the  
469 horizontal width of the light and dark blue shading being greater than the width of  
470 the light and dark red shading over the same depth range. In the lower mantle,  
471 especially in the deepest 500 km or so, the opposite is true: scattering  
472 heterogeneities are more abundant in low velocity regions (as evident by wider red  
473 shading). Regions of the lowermost mantle with high seismic velocities show  
474 virtually no correlation with scattering heterogeneities. Scattering is slightly more  
475 common in regions of high seismic velocity between 600 and 900 km depth.

476         In the deepest 200 km of the mantle, scattering heterogeneities are more  
477 common in regions of high lateral seismic velocity gradients (Fig. 7b: the width of  
478 the black and dark blue shading is significantly greater than the light green colors).  
479 In the lowest ~1000 km of the mantle, scattering heterogeneities are in greater  
480 abundance in the 20% area around hotspots than in any other bin; there is also a  
481 slight increase in mapped heterogeneities beneath hotspots in the mid-mantle  
482 between 600-900 km depth (see the wide red colors shading, Fig. 7c). Our mapped  
483 scattering heterogeneities show little correlation with regions surrounding the  
484 surface location of slabs, except in areas furthest from slabs in the 600-900 km  
485 depth range (indicated by the wide orange-yellow shading, Fig. 7d). In the upper

486 200 km of the mantle, scattering strongly correlates with high seismic velocities and  
487 proximity to slabs (Figs. 7a and 7d, blue and yellow shading, respectively), which, at  
488 these shallow depths is most closely related to the location of continents. While the  
489 precise locations of the heterogeneities is different, the heterogeneities resolved  
490 with  $P' \bullet P'$  show a very similar distribution in the lowermost 300 km of the mantle  
491 to those heterogeneities resolved with  $PK \bullet KP$  in an earlier study [Frost et al., 2017].

492 To test the robustness of these correlations we determine how likely they are  
493 to have been produced by chance. We rotate the tomographic models (of velocity  
494 and lateral gradient), and hotspot and slab locations by a random angle about a  
495 randomly located pole of rotation. We then recompute the correlations between the  
496 rotated geographical features and the distribution of the unrotated scattering  
497 heterogeneities. The random rotation is repeated 200 times for each tomography  
498 model, as well as for the hotspot and slab locations, to calculate the range of possible  
499 correlations. The mean and standard deviation of the range of correlations at each  
500 depth is computed, assuming Gaussian statistics. We compare this with the original,  
501 unrotated data in Fig. 8, and consider any correlation to be statistically significant if  
502 the correlation value between scatterers and regions of the unrotated phenomena  
503 plots outside one standard deviation from the mean correlation of the rotated  
504 phenomena (demonstrating that at least 84% of the random correlations are a  
505 lower value). When we do not assume a distribution and instead calculate the  
506 proportion of samples above and below one standard deviation of the data, we find  
507 very similar patterns of significant observations. Using this metric, we define the  
508 following correlations as significant and unlikely the product of chance:

- 509 (1) An increased correlation with scatterers in regions of low velocity at depths  
510 greater than 1800 km (solid red line in the left panel of Fig. 8a)
- 511 (2) An increased abundance of scattering heterogeneities in regions of high  
512 velocity gradient in the deepest few hundred km of the mantle, as well as  
513 between 1600-2000 km depth (solid red line in the right panel of Fig. 8b).
- 514 (3) An increased abundance of heterogeneities close to surface hotspot locations  
515 at depths greater than 2100 km depth (solid red line in left panel of Fig. 8c).
- 516 (4) A decreased abundance of heterogeneities far from surface hotspot locations  
517 at almost all depths greater than 800 km depth (solid red line in right panel  
518 of Fig. 8c).

519 There is no significant correlation seen between scatterer locations and slab  
520 locations, except an increase in correlation between heterogeneities and large  
521 distances from slabs between 600 and 900 km depth, which matches the depth  
522 range of the increased correlation with low velocity gradients (solid red lines in  
523 left panel of Fig. 8b and right panel of 8d), and an increased correlation between  
524 heterogeneities and large distances from slabs throughout much of the lower  
525 mantle (which is what one expects if correlations are strong for low velocities).

526

#### 527 *4.2 Dependence upon choice of model*

528 When comparing small-scale scattering locations with tomographically  
529 derived high or low velocities, the results may depend upon the choice of the  
530 tomography model. In our previous analysis, we compared the distribution of  
531 scattering heterogeneities to tomography model SEMUCB-WM1 [French and  
532 Romanowicz, 2014]. We further explore the relationship between our mapped fine-

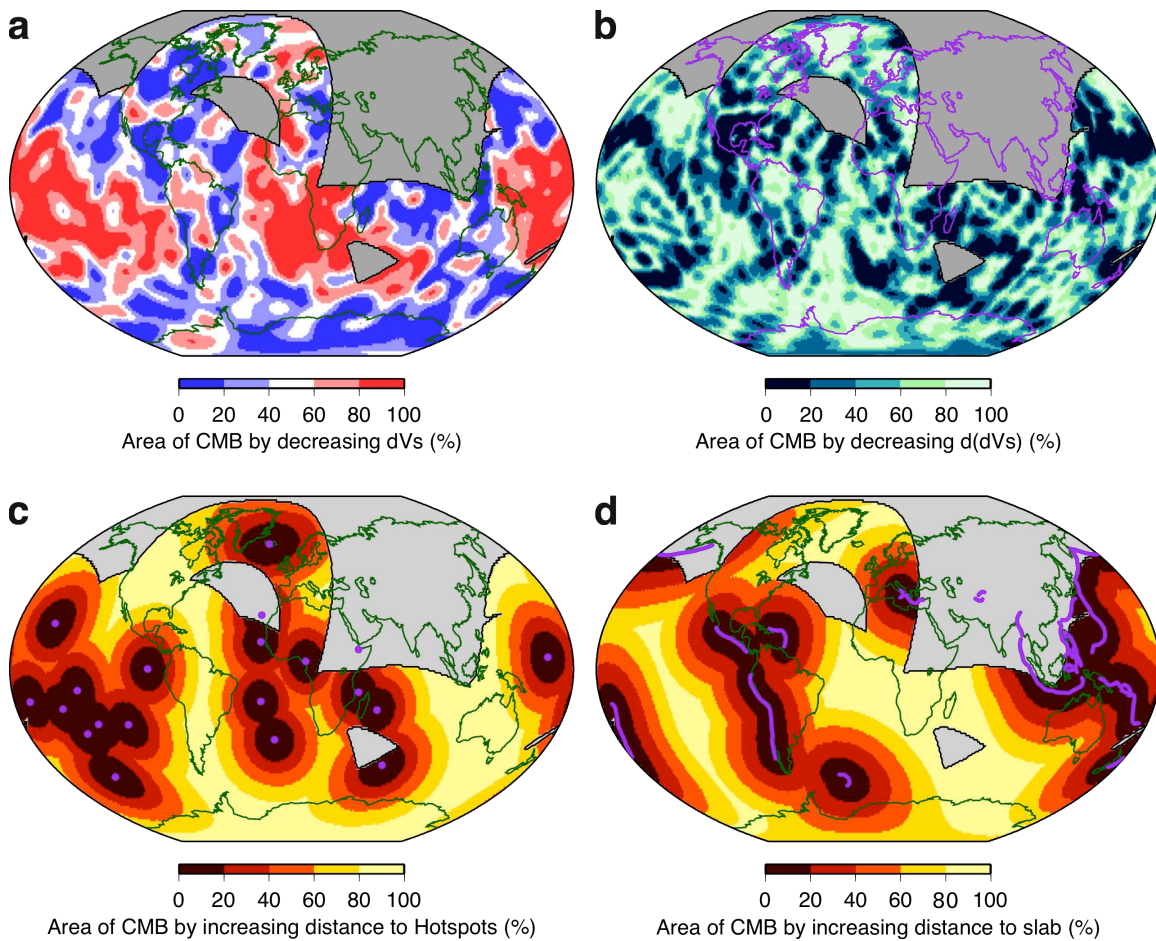
533 scale scattering heterogeneities with large-scale structures in other tomography  
534 models: GyPSuM, S40RTS, and TX2011 (Figs. S4-6 and S7-9 for P-wave models). We  
535 find small differences in precise depths and magnitudes of correlations with  
536 different models, but the correlation between scattering and low velocities at depths  
537 below 1600 km, and with high velocities at depths of 200 km and shallower and the  
538 robustness of these correlations are consistent between models.

539         To test the dependence of correlation on the pattern of hotspots, in addition  
540 to comparing with rotated hotspot locations, we create a population of randomly  
541 located hotspots, equal in number to the primary and clear hotspots from Courtillot  
542 et al., [2003] and French and Romanowicz [2015]. We find that a synthetic  
543 population generates no preferential spatial correlation with the scattering  
544 heterogeneities (Fig. S10). Furthermore, when the population of random hotspot  
545 locations is rotated to test the robustness of the correlation, the correlation of the  
546 random population very often falls well within the one standard deviation range of  
547 the rotated data (Fig. S12). This implies that the observed correlation between  
548 hotspot locations and scattering heterogeneities in the lower mantle is caused by  
549 the specific distribution of hotspots.

550         We test the influence of our decision to use only the surface slab locations of  
551 the RUM model. We calculate the spatial correlation between scattering  
552 heterogeneities and slab locations as described above, but use slab locations at the  
553 depth of the heterogeneity. When considering scattering heterogeneities at depths  
554 greater than that which the slab is mapped to we use the location of the slab at the  
555 last mapped depth and project this position vertically down to the CMB. This

556 method of vertical extrapolation likely still misrepresents the locations of slabs:  
 557 some amount of lateral movement at greater depths is evident in tomographic and  
 558 geodynamic models but is typically on the order of a few degrees [e.g. French and  
 559 Romanowicz, 2014 and Steinberger et al., 2012]. Nonetheless, we find no significant  
 560 difference in the correlations between using the surface slab location and slab  
 561 locations with depth (Fig. 7 and Figs. S11 and S12).

562



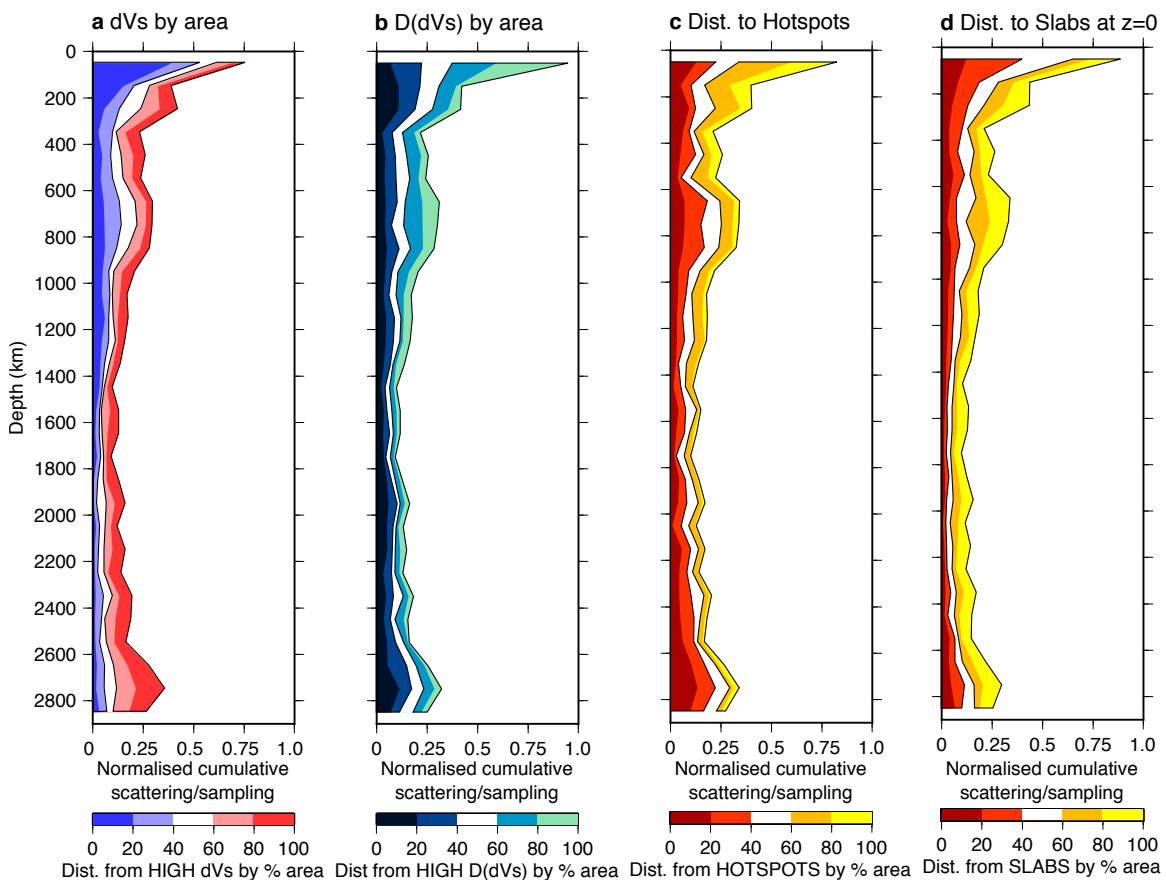
563  
 564 **Figure 6:** Tomography and distance from subduction zones and hotspots by  
 565 percentage area calculated for sampling at the CMB. (a) The magnitude of the  
 566 velocity anomalies in SEMUCB-WM1 [French and Romanowicz, 2014] in the area  
 567 sampled by our dataset at the CMB displayed by decreasing anomaly (from fast blue

568 areas to slow red areas) in regions occupying 20% of the area of the CMB. (b) The  
 569 magnitude of the lateral velocity gradient decreasing from high to low in 20% area  
 570 regions. (c) Distance from hotspots (connected to plumes identified as either  
 571 primary or clear in the analysis of French and Romanowicz [2015]). (d) Distance  
 572 from slabs (at zero depth slice in RUM [Gudmundsson and Sambridge, 1998]. Black  
 573 line marks the extent of the sampled area (as in Figure 3d).

574 [2 COLUMN FIGURE]

575

576



577

578 **Figure 7:** Scattering abundance (bar width) with depth compared with the

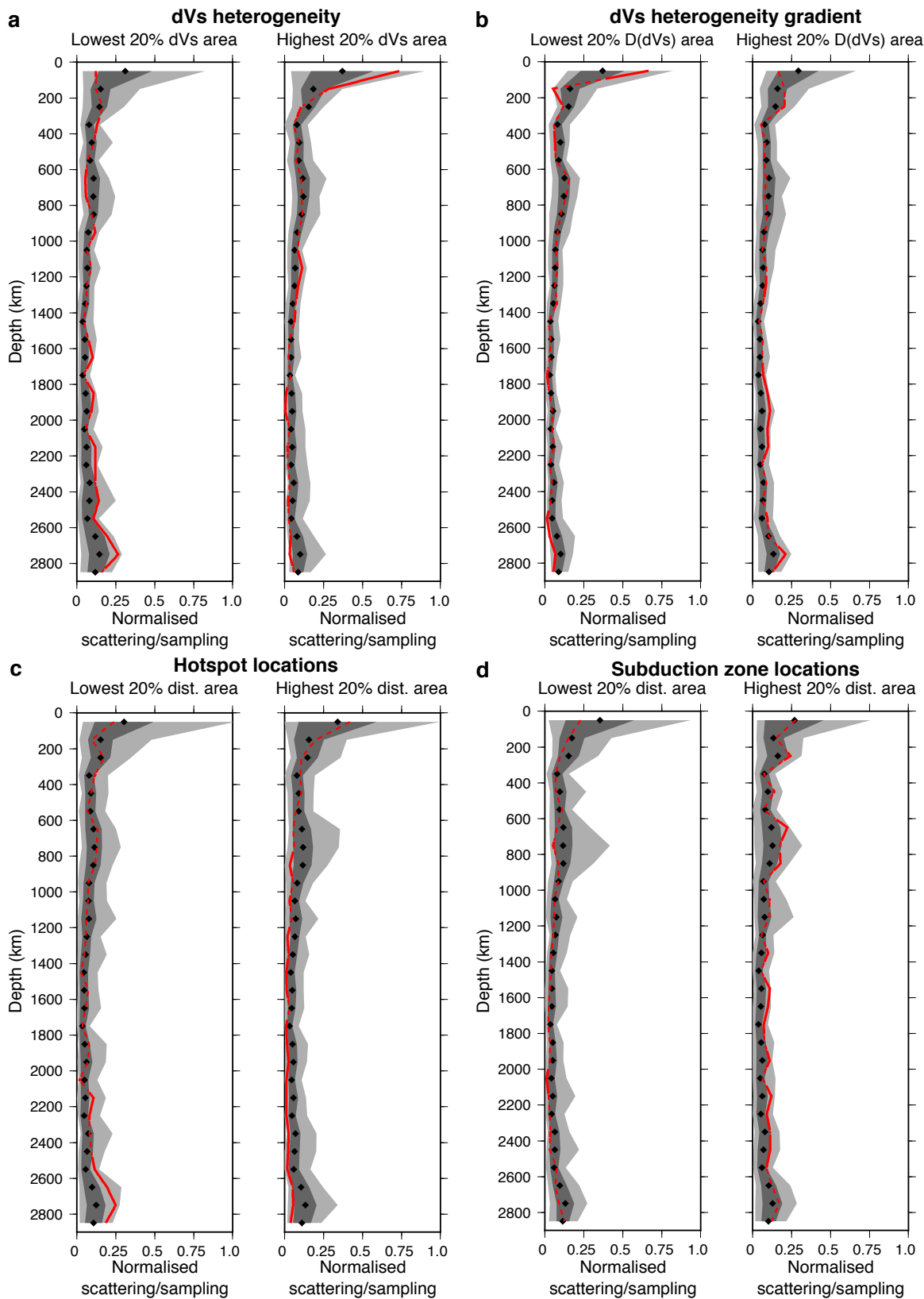
579 distribution of large-scale heterogeneity throughout the mantle (colour scale).

580 Scattering abundance is calculated cumulatively across all areas, is divided by

581 sampling, and is normalised to unity, representing the maximum scattering  
582 abundance at any depth. **(a)** Scattering heterogeneity and tomographic velocity  
583 anomalies (from SEMUCB-WM1 [French and Romanowicz, 2014]) sorted from  
584 highest (blue) to lowest (red) measured as a function of surface area in 20% area  
585 bins. **(b)** Scattering heterogeneity and lateral tomographic velocity gradient sorted  
586 from highest (dark blue) to lowest (light green). **(c)** Scattering heterogeneity and  
587 distance from hotspots from low to high (red and yellow, respectively). **(d)**  
588 Scattering heterogeneity and distance from slabs from low to high (red and yellow,  
589 respectively). Scattering heterogeneity in the lower mantle shows an affinity for  
590 both low seismic velocities and hotspots. Black lines encapsulate the highest and  
591 lowest 40% area regions.

592 [2 COLUMN FIGURE]

593



594

595

**Figure 8:** Scattering abundance with depth, divided by sampling, showing the

596

unrotated model (red line) compared with rotated models (grey). The unrotated

597 model (red line) is dashed when within one standard deviation (dark gray shading)  
598 of the mean of the spatial correlations (black diamonds) with the rotated models,  
599 and solid when outside this level. The lighter shaded region marks the range of all  
600 correlations with the randomly rotated phenomena. Comparisons are shown for: **(a)**  
601 tomographically derived velocity heterogeneity from SEMUCB-WM1 for the 20%  
602 area corresponding to the lowest (left panel) and highest velocities (right panel).  
603 Correlation between increased scattering abundance and low velocities appears  
604 robust in the deepest mantle, and correlation to high velocities is robust in the  
605 shallowest 200 km of the mantle, as well as around 1200 km depth. **(b)** As in **(a)**  
606 except correlations are between observed scattering and rotated shear velocity  
607 gradients in model SEMUCB-WM1. Correlations are most significant for the  
608 strongest gradients (right panel) at the base of the mantle. **(c)** As in **(a)** except  
609 correlations are between scatterers and distance to rotated hotspot regions.  
610 Correlations are most significant in the deepest mantle in close proximity to being  
611 beneath hotspots (left panel). **(d)** as in **(c)** except correlations are between  
612 scatterers and distance to rotated slab regions. Our random rotation test shows no  
613 significant correlation between scatterers and proximity to slabs.

614 [2 COLUMN FIGURE]

615

616

617 **5. Discussion**

618

619 In this study we mapped scattering heterogeneities and explored their  
620 geographical relationship to tomographic velocities and gradients, as well as  
621 hotspots and slabs. Our results may be interpreted in terms of the distribution of  
622 mantle heterogeneity, which we will discuss here.

623

624 *5.1 Possible origins of scattering heterogeneity in the mantle*

625

626 We observe scattering from small-scale heterogeneity throughout the  
627 mantle, with increased heterogeneity at the top and bottom of the mantle. Seismic  
628 waves can be scattered by volumetric heterogeneity with sharp impedance  
629 contrasts, when the heterogeneity has a minimum scale length comparable to the  
630 wavelength of the incident wave. Our method is not capable of resolving the precise  
631 partitioning of the incident wavefield into scattered versus transmitted energy,  
632 since we do not have a consistent reference phase to compare to the amplitude of  
633 the scattered wave. Thus we are unable to constrain the properties of the  
634 heterogeneities (e.g. impedance contrast). Nonetheless, the frequencies of waves  
635 that we study (between 0.5 and 2.0 Hz) imply that observed scattering  
636 heterogeneities have a minimum scale length of one to tens of km.

637 A variety of structures could scatter the energy observed in our data. We can  
638 use the distribution and sizes of scattering heterogeneities to address the feasibility  
639 of possible causes. Material undergoing phase changes such as from bridgmanite to  
640 post-perovskite (pPv) in the lower mantle (or the back transformation) [Murakami  
641 et al., 2004; Oganov and Ono, 2004], as well as transitions of olivine to wadsleyite to

642 ringwoodite to perovskite through the upper mantle transition zone could provide  
643 an impedance contrast with the ambient mantle. The bridgmanite to pPv phase  
644 transition is predicted to occur in the deepest few 100 km of the mantle, and only in  
645 relatively cold regions of the mantle for a standard pyrolitic composition, thus  
646 would not be appropriate to explain scattering at all depths and locations, unless  
647 mineralogical alterations are considered [Lay et al. 2006]. The phase transition is  
648 controlled by temperature, composition, and pressure. While pressure is assumed  
649 hydrostatic, local changes in composition, perhaps by contamination of the mantle  
650 by subducted mid-ocean ridge basalt (MORB), may influence the pPv transition  
651 [Grocholski et al., 2012], possibly causing the transition to occur locally in the  
652 vicinity of the MORB contamination. Metastability of phase transitions due to  
653 chemical heterogeneity [Catalli et al., 2009] could allow transformed minerals to  
654 persist outside of their expected stability range. High thermal conductivity in the  
655 lower mantle [Stackhouse et al., 2015] renders small-scale temperature changes an  
656 unlikely cause of spatially limited occurrence of the pPv transition. While many  
657 morphologies and scale lengths of pPv regions can be envisioned that could  
658 contribute to wave field scattering observed here, the details of such processes are  
659 not constrained. However, pPv should not be stable in the upper mantle, and thus  
660 cannot explain observed scattering there. Nonetheless, pPv remains a viable  
661 contributor to wavefield scattering in the deepest mantle.

662         The subduction process continuously introduces compositional  
663 heterogeneity into the mantle. Scattering has previously been mapped in the upper  
664 mantle and lower mantle in the proximity of subduction zones [Kaneshima and

665 Helffrich, 1998; Rost and Earle, 2010; Miller and Niu, 2008; Bentham and Rost,  
666 2014]. We do not observe a robust preference of scattering heterogeneity in upper  
667 mantle regions of subduction over other regions. While we do observe slightly  
668 increased scattering in regions associated with subduction at around 600 to 900 km  
669 depth (Fig. 7a), this does not appear to be statistically significant (Fig. 8a, right  
670 panel). Nonetheless, the increased concentration of scattering heterogeneity  
671 between 600 and 900 km depth shows robust spatial correlation with regions away  
672 from subduction zones and areas of low amplitude lateral velocity gradient (Figs. 7  
673 and 7). In some tomographic models subducting slabs are observed to flatten at a  
674 similar depth, between ~800-1200 km depth [e.g. French and Romanowicz, 2015].

675       Oceanic crust may be responsible for scattering throughout the mantle.  
676 Subducted oceanic crust may remain unmixed due to slow chemical diffusion rates  
677 [Olson et al., 1984] and is only homogenised into the mantle through mechanical  
678 stirring. If the observed scattering heterogeneities are oceanic crust then the  
679 dispersal of heterogeneities throughout the mantle must be faster than stirring and  
680 removal of heterogeneities since scattering heterogeneity is also observed in  
681 regions that have not been influenced by subduction for a long time.

682       The iron spin transition affects the velocity and density of iron-bearing  
683 mantle materials [Lin et al., 2005]. Recently, this has been observed to occur over a  
684 60 GPa pressure range (~600 to 2000 km depth) [Holmstrom and Stixrude, 2015]  
685 and thus would likely not generate discrete heterogeneities capable of causing  
686 scattering.

687 Products of chemical reactions between core and mantle materials are  
688 predicted to have physical properties in contrast with the ambient mantle [Knittle  
689 and Jeanloz, 1989] thus may be capable of causing seismic scattering. Experiments  
690 demonstrate that such mantle material enriched in iron would likely be denser than  
691 the ambient mantle [Wicks et al., 2010]. An interesting possibility is the  
692 development of a reaction product layer that would inhibit further interaction with  
693 the core; for this case, products are likely to be constrained to a very limited  
694 thickness close to the CMB, on the order of a few meters to kilometers [Kanda and  
695 Stevenson, 2006]. However, flow in the deep mantle could generate thicker  
696 accumulations of reaction products [Mao et al., 2006], which could scatter waves. In  
697 addition, ULVZs are commonly imaged to have vastly reduced seismic velocities of  
698 up to -10% dVp and -30% dVs, and increased density of +10-20% relative to the  
699 surrounding mantle [e.g., McNamara et al., 2010]. Partial melt of mantle material has  
700 been proposed as an explanation of ULVZs [Williams and Garnero, 1996]. Partial  
701 melt may be denser than the solid state [Ohtani and Maeda, 2001] as well as having  
702 strongly reduced seismic velocities. While ULVZs and CMB reaction products could  
703 explain deeper scattering heterogeneities, simulations have suggested that dense  
704 material may also be entrained up to 200 km above the CMB, dependent on density,  
705 viscosity, and vigor of mantle flow [Bower et al., 2011]. CMB topography or  
706 roughness might cause scattering [Chang and Cleary, 1981; Mancinelli et al., 2016],  
707 but this could not explain heterogeneities we map up off of the CMB throughout the  
708 mantle. LLSVPs may be compositionally distinct from the surrounding mantle [e.g.  
709 Garnero et al., 2016], and dynamical flow models predict that the LLSVP material

710 will be gradually entrained into mantle flow on small length scales [Li et al., 2014;  
711 Williams et al., 2015; Mulyukova et al., 2015]. Thus, depending on the LLSVP  
712 properties and entrained heterogeneity scale, this process might give rise to  
713 scattering. Geodynamic models also predict that surrounding ambient mantle  
714 material can be downward entrained into the LLSVPs, thus offering an origin of  
715 scattering within LLSVP regions.

716

### 717 5.2 Distribution of scattering heterogeneity

718

719         The distribution of small-scale volumetric heterogeneities is likely strongly  
720 dependent on the dynamic properties and processes within the Earth. In numerical  
721 simulations of mantle dynamics small-scale heterogeneity, particularly that derived  
722 from subducted oceanic crust, tends to be concentrated in regions of upwelling from  
723 the lower mantle around plumes and downwelling from the surface around  
724 subduction zones (Fig. 1 of Li et al., [2014]). The same focusing beneath upwellings  
725 is expected for basal heterogeneities [McNamara et al., 2010] (e.g., compositionally  
726 distinct ULVZ material, CMB reaction products, and entrained LLSVP material).  
727 Furthermore, large-scale mantle heterogeneity may influence radial small-scale  
728 heterogeneity distribution by modifying the convective flows in which the  
729 heterogeneities could be entrained [Li et al., 2014].

730         As wavelength at some fixed frequency is a function of the local velocity,  
731 which changes with depth, and the wavelength of scattering structure that can be  
732 resolved is dependent on the incident frequency, it follows that in band limited data,  
733 the resolvable scattering wavelength changes with depth. We filter all data between  
734 0.5 and 2.0 Hz, therefore, we resolve scattering heterogeneity with wavelengths

735 between about 7-28 km at the CMB, decreasing to about 3-12 km at the surface.  
736 Stirring of initially larger-scale heterogeneity is suggested to lead to a cascade of  
737 heterogeneity sizes, increasing in abundance with decreasing scale [Olson et al.,  
738 1984]. A previous study of the scale of scattering heterogeneities in the lowermost  
739 mantle found the most common scale-length to be 4-7 km, but other scales were  
740 also present [Frost et al., 2017]. Despite the limited frequency range used in this  
741 study, we are likely imaging heterogeneity of a similar size (around 7 km)  
742 throughout the mantle.

743         The similarity between scattering heterogeneity abundance and tomographic  
744 amplitude (Fig. 5) may arise from processes relating to convection and chemical  
745 differentiation that likely generate strong lateral velocity variations on continental  
746 scales and smaller through stirring and diffusion. Lower mantle anomalies manifest  
747 at a range of spatial scales (LLSVPs, ULVZs,  $D''$ , CMB reaction products), and stirring  
748 and entrainment may further decrease their size [Olson et al., 1984, Li et al., 2014],  
749 leading both to high-amplitude large-scale velocity anomalies and abundant small-  
750 scale scattering. Upper mantle heterogeneity related to subduction, magmatism, and  
751 convective processes are also likely to occur across scales. In addition to increased  
752 scattering at the top and bottom of the mantle, we also observe a slight but marked  
753 increase in scattering abundance from 600-900 km depth, independent of the  
754 tomographic velocity structure, which may relate to slab subduction processes or  
755 large-scale vertical viscosity changes [Rudolph et al., 2015].

756

## 757 **6. Conclusion**

758

759           Through analysis of the high-frequency seismic wavefield we map the  
760 distribution of small-scale seismic heterogeneity, on the order of  $\sim 1\text{-}10$  km in size,  
761 throughout Earth's mantle. We deterministically locate vastly more scattering  
762 heterogeneities than has been done previously, significantly improving our  
763 understanding of small-scale mantle structure. The spatial distribution and scale-  
764 length of this scattering heterogeneity suggests it may be the product of several on-  
765 going processes in the mantle. These include oceanic crust disseminated throughout  
766 the mantle, entrainment of basal heterogeneities such as ULVZ material or core-  
767 mantle reaction product, and compositionally distinct LLSVP material swept into  
768 mantle flow. Subducted MORB may suitably explain all scattering observations  
769 without scattering contributions from other sources. However, we cannot rule out  
770 that scattering is caused by a mixture of heterogeneities with different origins in  
771 different regions and depths. While small-scale heterogeneity appears present in  
772 much of the mantle, we find increased scattering heterogeneity within the  
773 uppermost 200 km of the mantle and the lowermost 300 km of the mantle, similar  
774 to heterogeneity amplitudes seen in tomography models. We find no statistically  
775 significant correlation between scattering and subducting slabs in the upper 1000  
776 km of the mantle. In the lower mantle (from around 1500 km depth down to the  
777 CMB), scattering is most common in regions related to the LLSVPs and close to  
778 deeply sourced mantle hotspots. Meanwhile, scattering is rare in regions far from  
779 deeply sourced mantle hotspots. This suggests that large-scale convective lower  
780 mantle structures may entrain and concentrate small-scale heterogeneity in regions  
781 of upwelling, downwelling, and stagnant flow.

782  
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789

790

791

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