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Observation of extremely strong shock waves in solids launched by petawatt laser heating

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Understanding hydrodynamic phenomena driven by fast electron heating is important for a range of applications including fast electron collimation schemes for fast ignition and the production and study of hot, dense matter. In this work, detailed numerical simulations modelling the heating, hydrodynamic evolution and XUV emission in combination with experimental XUV images indicate shock waves of exceptional strength (200 Mbar) launched due to rapid heating of material via a petawatt laser. We discuss in detail the production of synthetic XUV images and how they assist us in interpreting experimental XUV images captured at 256 eV using a multi-layer spherical mirror.

I. INTRODUCTION

Strong, radiating shock waves are associated with the most violent processes in nature, such as supernovae¹, black hole mergers² and gamma-ray burst sources^{1,3}. Shock waves may even be critical to the generation of protogalactic seed magnetic fields⁴. Shock waves play a crucial role in conventional hot spot inertial confinement fusion (ICF)⁵ and alternative schemes such as shock⁶ and fast⁷ ignition. Producing such shock waves in the laboratory has long been one of the objectives of high power laser interaction experiments^{8–11}. The strongest shock waves that can be produced in the laboratory are those that result from the interaction of an ultra-high intensity ($> 10^{18} \text{ W cm}^{-2} \mu\text{m}^2$), high energy ($> 100 \text{ J}$) laser pulse with a dense target. In these interactions, solids are isochorically heated to temperatures in the range 0.01–0.8 keV¹², thus reaching transient pressures approaching 1 Gbar. In comparison, typical drive pressures achieved in the NIF ignition experiments peak above 100 MBar¹³. Such an interaction forms an integral

part of the fast ignition approach to inertial fusion^{7,14,15}, and as such an understanding of the formation of such shock waves is important for the further development of this approach to fusion¹⁶. The presence of such ultra-strong shock waves, which may have pressures of many hundreds of Mbar or more, can be inferred from spectroscopic measurements¹⁷.

In this paper we report the first images indicating such shock waves in dense material, formed from the XUV emission in the dense plasma. The rapidly decaying nature of the shock wave as it propagates through the plasma, coupled with the narrow acceptance wavelength of the imager employed, produce a temporally gated ring-like image of the expanding cylindrical shock front. This shock front is centred upon the region in which a beam of relativistic electrons, generated by the laser-plasma interaction, produce intense Ohmic heating for $< 1 \text{ ps}$ ^{12,18}. Based on simulations, we infer that the pressure associated with this shock front at the time it is imaged is approximately 200 Mbar. The pressure earlier in time is thought to exceed 1 Gbar.

A fast electron transport code was used to predict

target heating patterns in thin solid foils ($8\text{ }\mu\text{m}$ CH). The subsequent evolution of the target on the multi-ps timescale was modelled using the radiation hydrodynamics code h2d, and the data from this was post-processed using the collisional-radiative atomic kinetics and spectral code SPECT3D¹⁹, to generate synthetic XUV images. These images predict a distinct ring-like feature in the XUV due to the shock wave launched by the strong explosion of the heated region. The central region is heated supersonically by relativistic electron propagation and associated return currents drawn in the background plasma. These return currents, which are driven by the requirement to locally conserve charge, result in strong Ohmic heating of the dense plasma. Significant hydrodynamic motion only ensues after the heating process has completed, due to the very short (600 fs) duration of the laser pulse. XUV images obtained experimentally record a strong ring-like emission feature which correlate to the shock position around 20 ps after the laser pulse. The fully time-integrated imager is effectively gated purely by the physical behaviour of the system, as the emission in the narrow bandwidth of the imager is only significant for a few picoseconds, thereby capturing the shock wave at a particular moment in time.

Work by Robinson et al.²⁰ show that it is possible to use resistively structured targets, such as a wire of higher resistivity buried in a lower resistivity substrate, as a driver for hydrodynamic phenomena. The innovative diagnostic approach which has been developed as a part of this study may allow us to observe the resulting hydrodynamics in such targets. More generally, it may also enable wide range of hydrodynamic phenomena that are launched by fast electron heating to be observed and studied quantitatively.

II. THEORETICAL AND NUMERICAL STUDIES

In order to drive a strong cylindrical shock wave, a sufficiently columnar heating pattern must be achieved during the interaction of a PW laser pulse with a simple foil. The ZEPHYROS 3D hybrid code was used to understand under which conditions this was possible. ZEPHYROS^{21,22} is a 3D particle hybrid code, mainly based on the methods of Davies²³. The target studied was a homogeneous $8\text{ }\mu\text{m}$ thick CH foil. A fast electron beam was injected that modelled irradiation by a 600 fs laser pulse with a $10\text{ }\mu\text{m}$ FWHM spot, and a FWHM intensity of $5 \times 10^{20}\text{ Wcm}^{-2}$. The following assumptions were made in this modelling: 20-30% laser to fast electron energy conversion efficiency^{24,25}, exponential energy distribution with an average energy determined by ponderomotive scaling, and a characteristic angular divergence of 25° – 45° for the fast electrons²⁶. The resistivity curve used for the CH target is the one used by Davies in²³. Reflective boundaries were used throughout. The heating patterns after 1 ps typically showed heating right through the thickness of the target, and the variation

with depth could be reasonably well fit by,

$$T = (A \exp[-x/d] + B) \exp[-r^2/2L^2] \quad (1)$$

where x is in μm , $d=4\text{ }\mu\text{m}$, $A = 0.8$ – 2 keV , $B = 0.2$ – 0.6 keV , and L typically about $10\text{ }\mu\text{m}$ depending on the precise assumptions made in the transport simulation. An example of one of the results of these calculations is shown in figure 1.

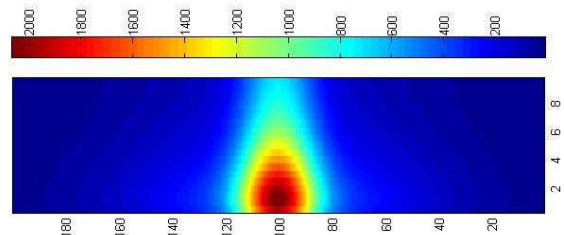


FIG. 1. Temperature profile from a 3D ZEPHYROS fast electron transport simulation showing the background temperature in eV (red corresponding to 2000 eV) at 1 ps in the x - y midplane of the box.

Such a heating pattern should be sufficiently columnar to launch a strong cylindrical shock wave, and this was confirmed by 2D radiation hydrodynamics simulations in which a uniform $8\text{ }\mu\text{m}$ slab of CH was initialized with the temperature profile obtained from the fast electron transport calculations (Eq.1). These simulations were carried out using h2d²⁷, a 2D r – z lagrangian radiation hydrodynamics code. The ‘baseline’ case that was used was $A = 2\text{ keV}$, $B = 0.6\text{ keV}$, and $L = 10\text{ }\mu\text{m}$. In general the simulations showed that the heated region would strongly cavitate and cause strong transverse compression, leading to a strong shock wave propagating out from the central heated region for tens of ps after the interaction. The results of the baseline simulation, in terms of the mass density at 20 ps, are shown in figure 2. In this figure the cavitation of the heated region can be seen between $r=0$ – $20\text{ }\mu\text{m}$ (where zero is the centre of the heated region), and the compressed region can be seen at $r \approx 20\text{ }\mu\text{m}$. The initial pressure of the heated region is close to 1 Gbar, and the pressure of the shock wave is still $>100\text{ Mbar}$ even after the shock wave has propagated $10\text{ }\mu\text{m}$ outward. The combination of the transport simulation and the radiation hydrodynamic simulations, lead to the conclusion that a strong cylindrical shock front should be launched in experimentally accessible interactions with thin foils.

The next consideration is whether or not this would lead to a detectable signal in commonly used plasma diagnostics. In this paper we consider the possibility of using XUV imaging to observe such shocks.

In order to ascertain whether observing signatures of strong shocks via XUV imaging was possible, the output of the radiation hydrodynamics simulations were post-processed using the SPECT3D code¹⁹. This was used to generate ‘synthetic’ time-integrated XUV images, specifically the XUV emission at 256 eV that would be detected

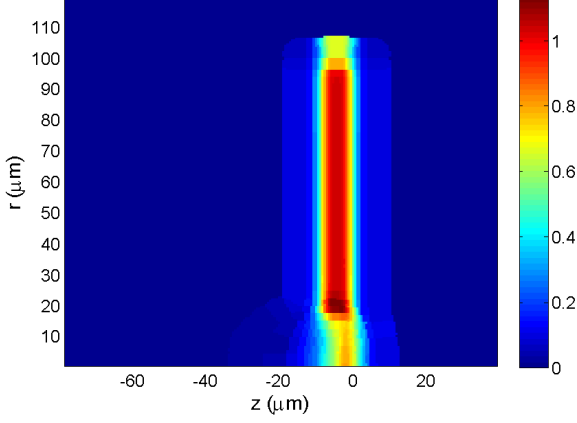


FIG. 2. Mass density profile (in g cm^{-3} ; red corresponding to 1 g cm^{-3}) at 20 ps from the baseline h2d radiation hydrodynamics simulation. The cavitation of the heated region can be seen from $r=0$ -20 μm in the foil where 0 is the centre of the heated region, and the compressed region lies at around $r = 20 \mu\text{m}$.

using the XUV imaging system available for experiments (i.e. looking at the target rear surface close to normal with multi-layer mirrors with a magnification of ≈ 10 –12 and a spatial resolution of $\approx 10 \mu\text{m}$). The synthetic image that is obtained from the baseline case is shown in figure 3. This shows a bright ring of emission associated with the radially expanding shock front. The image is strongly correlated with a particular time in the h2d simulation at which the shock front is at the same radius and the shock pressure is approximately 200 MBar. Although the target opacity is not negligible, there is sufficient transparency to allow clear observation of the emission from this region. From this it was concluded that the transverse explosion of the heated region would lead to a clear signal in time-integrated XUV measurements, which directly corresponds to the emission from a strong outwardly expanding cylindrical shock front at a time approximately 20 ps after the laser-solid interaction.

The result can be understood by considering the limit of an optically thin foil, and then considering only the free-free emission process. At a particular photon energy, $h\nu$, this will vary $\propto Z n_e^2 e^{-h\nu/k_B T} / \sqrt{k_B T}$ (neglecting the Gaunt factor). At a fixed density, this function has a weak maximum at $T = 512 \text{ eV}$ for $h\nu = 256 \text{ eV}$, and only falls sharply below about 200 eV. If one now considers the effect that the n_e^2 scaling has on the emission as the heated region cavitates and compresses the surrounding material then one can see that the dominant emission can actually come from the slightly cooler shell of compressed material, rather than the hotter but decompressed centre. In reality, the emission from the cooler region will be further enhanced by the carbon atoms retaining a substantial bound electron population.

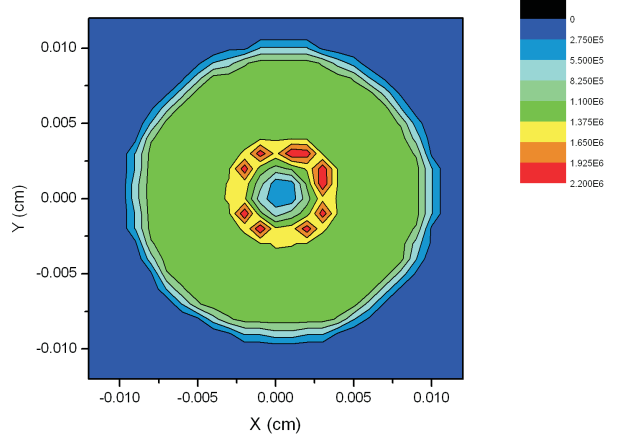


FIG. 3. A synthetic time-integrated XUV image obtained by post-processing the baseline radiation-hydrodynamic simulation output using the SPECT3D code (color scale is in arbitrary units). The imager is assumed to look at the target's rear surface along the target normal.

III. UNDERSTANDING EXPERIMENTAL STUDIES

This theoretical and numerical study predicts the possibility of clearly observing the transverse compression wave under conditions that closely resemble an experiment that was carried out using the Vulcan petawatt laser. The Vulcan PW²⁸ delivered up to 300 J of $\lambda = 1.05 \mu\text{m}$ light on to target in a pulse duration of 700 fs. The laser was focused on to target using an F/3 off axis parabolic mirror to a spot size of 7 μm diameter. Approximately 20% of the energy was contained within the central focal spot giving peak intensities up to $2.5 \times 10^{20} \text{ W cm}^{-2}$. The intensity contrast ratio of the ASE to the peak power of the laser was 5×10^{-8} , 1.5 ns ahead of the interaction pulse²⁹. The targets consisted of either 10 μm of CH with a 50 nm layer of Al on the rear surface, or a front layer of CH of thicknesses 4 μm , a thin tracer layer of Al (0.2 μm), and a layer of 4 μm CH at the rear.

Extreme ultra-violet radiation (XUV) emitted at 256 eV from the back surface was imaged and time-integrated^{30,31}. The radiation was focused using a spherical multilayer mirror (with a C-WC-Monel-W formulation) onto a Princeton Instruments 16-bit charge coupled device (CCD). The magnification was 12 and the spatial resolution was 10 μm . A series of XUV images were obtained in which the image shows a ring structure with a size of 148 μm . The vertical line out shows very clearly that this ring structure is real and distinct. This was observed in all types of target. In figure 5, an image and its accompanying lineout from a CH-Al-CH target are shown.

There is very good agreement between the theoretical predictions and the experimental observations, at least

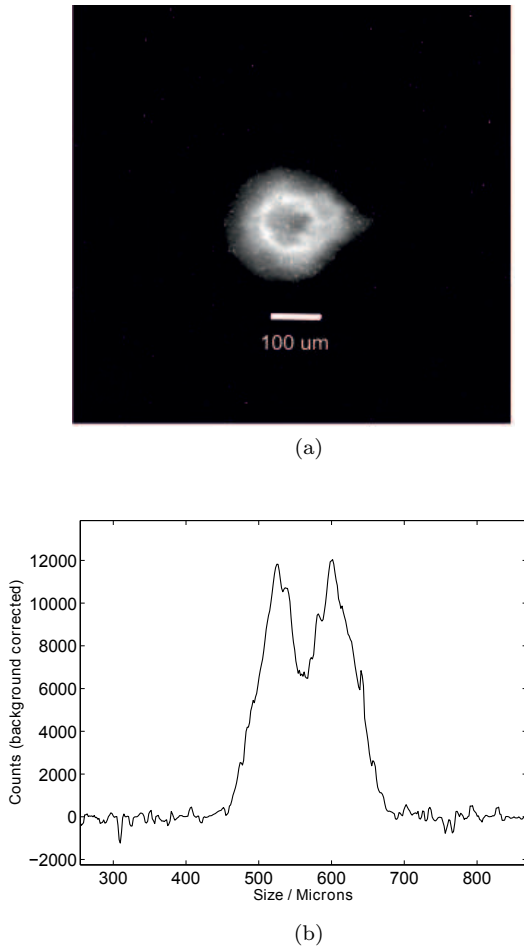


FIG. 4. (a) Time-integrated XUV image obtained by imaging the rear surface emission of a CH-Al-CH target showing a clear ring pattern. (b) Lineout of this time-integrated XUV image showing the actual signal height of ring relative to the centre.

in qualitative terms. In quantitative terms the largest difference is the diameter of the ring feature. The experimentally observed images show a ring feature with a diameter of 100–150 μm , whereas the synthetic image shows a ring with a diameter of only 50 μm . Although this is a noticeable discrepancy, it is easy to identify a number of points in the complex multi-stage numerical model that could give rise to this discrepancy. One simple point, for example, is the accuracy of fitting the temperature profile from the fast electron transport simulation. Another is reproducing the exact energy distribution within the focal spot. We therefore believe that increasingly accurate analysis will reconcile difference between the theoretical predictions and the experimental results.

In order to gain a better understanding of the impact of uncertainties in the temperature and focal spot profile we performed a parameter scan using a less computationally expensive version of our synthetic diagnostic using axis-symmetric 1-D radiation-hydrodynamics calcu-

lations instead of the 2-D calculations. We used the 1-D radiation-hydrodynamics code Hyades²⁷ to generate 1-D temperature and density profiles at a range of time intervals and then converted these to 2-D (r, z) data. This data was then post-processed using SPECT3D in the same way as before to generate the expected time-integrated XUV emission images. A range of hot-spot radii, temperatures and spatial geometries were explored. Figure 5 shows one of the results of these calculations, which shows much better quantitative agreement with the experiment. Here the diameter of the ring-like XUV emission features is 106 μm . The initial hot-spot here has a Gaussian spatial structure with a FWHM of 60 μm and a peak on-axis temperature of 2keV. It may be noted that the "hollowed-out" effect in the ring-like XUV emission is significantly less pronounced in these calculations as compared to the original calculations. This is due to the use of 1-D rather than 2-D radiation-hydrodynamics calculations which results in a greater optical depth on axis.

On the basis of the simulations that have been performed we are confident in claiming that the shock wave inferred from the XUV image had a pressure in excess of 100 Mbar.

Measurements were also taken from CH-Al-CH layers with a thicker front CH layer (8 μm , 30 μm , and 60 μm). A faint ring pattern could be observed in the target with an 8 μm front layer, but not in the case of a 30 μm front layer. In order to make similar observations in such thick targets, one would need columnar heating right up to the rear surface. However this would require a well collimated fast electron flow, and in CH this will only be possible if the fast electron divergence half-angle (i.e. the characteristic half-angle of the fast electron population at absorption) is less than 30° half-angle³². This emerges from both fast electron transport simulations and more basic criteria, such as the Bell-Kingham condition³³. Therefore the loss of the ring feature in these thicker targets is simply an indicator of the expected divergence in the fast electron flow. We also note that experiments carried out with pure Al foils do not exhibit the same time-integrated XUV emission patterns³¹, however it is unlikely that the same XUV emission pattern would be predicted by the composite numerical model due to differences in fast electron propagation, radiative cooling, and opacity.

It is likely that the effects studied in this paper have been observed in previous experiments, although on all previous experiments that report such annular XUV patterns, the observation has been attributed to other mechanisms. For example the observations of ring-patterns in XUV images obtained by Lancaster et al.³⁴ and Koch et al.³⁵ both attribute the observation to disruption of the fast electron propagation by the Weibel instability. In the case of Lancaster's results the similarity in target design and laser parameters means that those results can be directly attributed to the mechanisms that we describe in this paper.

This work is important to understanding the collima-

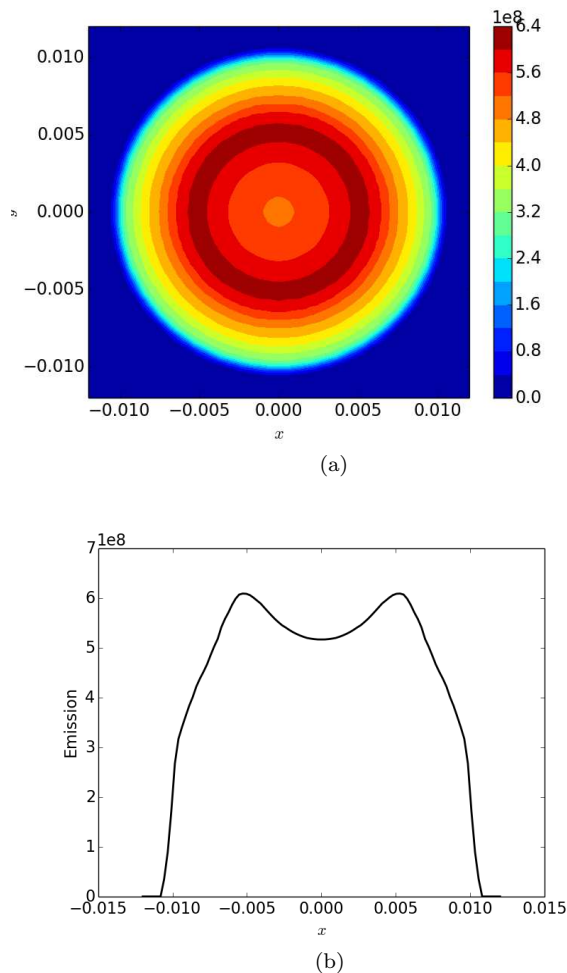


FIG. 5. (a) A synthetic time-integrated XUV image obtained using the SPECT3D code from initial conditions in the 1-D radiation hydrodynamics calculations of gaussian temperature profile HWHM of $30 \mu\text{m}$ peaking at 2keV (color scale is in arbitrary units) b) line out of synthetic time-integrated image shown in 5a

tion of fast electrons through various schemes and how this impacts the heating of matter, especially material tens or hundreds of microns away from the interaction. This technique could therefore be used as a test of fast electron collimation strategies^{22,36,37} to complement the standard approach of measuring K-alpha x-ray emission.

IV. CONCLUSIONS

In conclusion, we have described through a combination of XUV imaging and numerical modelling, measurements consistent with the formation of strong cylindrical shock waves solid targets irradiated by a PW laser launched by rapid fast electron heating. Detailed numerical modelling indicated that the shock wave should be observable as a ring-like feature in time-integrated XUV

images when it is at a strength of around 200 Mbar. This corresponded to an experiment that was carried out in which these ring-like patterns were very clearly observed in the XUV images. Such features are not observed in thicker targets because of divergence in the fast electron flow. Apart from the ability to produce images of plasma behaviour that is extremely difficult to directly observe, the methodology that has been employed here could be used as a test of fast electron collimation strategies. Given the early stage of development of the synthetic XUV diagnostic and the complexity of the chain of numerical calculations it requires, it is unsurprising that agreement to experiment is qualitative. On the basis of parameter scans using 1-D radiation hydrodynamics calculations post-processed using SPECT3D it was possible to reproduce the experimental XUV ring emission size more closely by making the initial temperature distribution more experimentally realistic.

V. ACKNOWLEDGMENTS

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