

Energy Metrics to Evaluate the Energy Use and Performance of Water Main Assets

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Abstract: Managing aging infrastructure has become one of the greatest challenges for water utilities, particularly when faced with selecting the most critical pipes for rehabilitation from amongst the thousands of candidates. The aim of this paper is to present a set of novel yet practical energy metrics that quantify energy interactions at the spatial resolution of individual water mains to help utilities identify pipes for rehabilitation. The metrics are demonstrated using a benchmark system and two large, complex systems. The results show that the majority of pipes have a good energy performance but that an important minority of outlier pipes have a low energy efficiency and high energy losses due to friction and leakage. Pumping and tank operations tend to drive energy efficiency and energy losses in pipes close to water sources while diurnal variation in demand drives energy performance of mains located far away from water sources. The new metrics of energy lost to friction and energy lost to leakage can provide information on energy performance in a pipe than is complementary to the traditional measures of unit headloss and leakage flow.

Keywords: Energy efficiency, energy metrics, friction loss, leakage loss, pipe rehabilitation, water distribution systems.

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22 **Introduction**

23 Water distribution systems play host to a multitude of energy interactions on an hourly and
24 daily basis. Pumps and reservoirs supply mechanical energy to the system, while water demand,
25 pipe leaks, and frictional headloss provide output pathways for energy to leave the system, either
26 in the form of work or heat. As water main assets in a system age and deteriorate, they become
27 less energy efficient, with more energy leaving the system via unwanted pipe leaks and through
28 frictional headloss (Fontana et al., 2012; Kleiner and Rajani, 2001). The challenge in managing
29 a large, aging water distribution system is to prioritize interventions so that investment returns
30 the largest gain in system performance (Alvisi and Franchini, 2009 and 2006, Dandy and
31 Engelhardt, 2001).

32 Energy has long been used as a key concept to understand the performance of engineering
33 systems (Pelli and Hitz 2000; Lambert et al., 1999). Energy use as a modeling concept is
34 germane to understanding the energy performance of water main assets in distribution systems
35 because power and energy in water distribution systems depend on pressure and flow – two
36 quantities that are monitored continuously by water utilities (Dziedzic and Karney, 2015;
37 AWWA, 2009; Boulos et al., 2006). While most municipalities extensively monitor their
38 systems, few have a firm understanding of the energy efficiency of their systems. Even fewer
39 municipalities have the capability to use pressure and flow data to understand the impact of
40 infrastructure upgrades and operational changes on the energy efficiency of their systems
41 (Engelhardt et al., 2000; Roshani and Fillion, 2013; Hashemi et al., 2012).

42 To date, previous research has been focused on characterizing the system-wide energy
43 dynamics in distribution systems. Colombo and Karney (2002) showed that diurnal
44 demand/pressures can affect the manner in which fissures and cracks in pipes conduct leakage.

45 Results demonstrated that the more distant the leakage sources are from the water sources, the
46 higher is the energy lost from leakage and friction. While, the presence of storage was shown to
47 have a negligible effect on leakage energy, the location of the tanks did influence the leakage
48 level and pumping energy (Colombo and Karney 2005). The research underscored the important
49 role of water mains, and their proximity to pumps and tanks, on the energy balance of a system.

50 Energy metrics developed thus far have focused on the system-wide energy performance of
51 systems. Pelli and Hitz (2000) developed energy indicators to relate system-wide energy
52 efficiency to pump efficiency and reservoir location, without considering leakage impacts.
53 Cabrera et al. (2010) presented a set of metrics to characterize the system-wide energy
54 performance that includes losses to friction, leakage, and overpressure. These energy metrics
55 provide a useful set of tools to help water utility managers better understand how far their
56 systems are from an ideal energy-efficient state but fall short of being able to identify individual
57 pipes that are problematic. Building upon their earlier work, Cabrera et al. (2014b) presented
58 additional metrics to assess the energy efficiency of a pressurized system and procedures to
59 prioritize interventions on a system-wide basis. Dziejczak and Karney (2014) examined the
60 energy dynamics of groups of pipes and pumps in the Toronto distribution system. While these
61 researchers also solved the energy balance to examine the frictional losses in individual pipes of
62 the Toronto system, they did not examine the efficiency, leakage, and other energy
63 characteristics of these pipes. The current paper extends this research direction by considering
64 energy transformations that take place in the individual pipes of a distribution system.

65 The aim of this paper is to present a set of novel energy metrics that quantify energy
66 interactions in a distribution system at the spatial resolution of individual water mains. These
67 pipe-level metrics can be applied to: 1) characterize the energy performance in water mains in an

68 unimproved state to establish a benchmark prior to any rehabilitation work; 2) plan infrastructure
69 upgrades and operational changes in areas that exhibit a low energy efficiency alongside
70 information on cost, water quality, and pipe break history, and; 3) characterize the impact of
71 infrastructure upgrades and operational improvements on the energy performance of water mains
72 in a system. In this paper, the new pipe-level metrics are applied to a large *ensemble* of water
73 mains across three distribution systems to examine how system operation and system
74 improvements impinge on the spatial and temporal patterns of energy performance in drinking
75 water mains.

76 **Energy Use in a Pipe**

77 To develop a set of energy metrics, it is instructive to consider the hydraulic grade line with
78 energy inputs and outputs in a single pipe as indicated in Figure 1. Here, the pipe conveys a flow
79 Q (m^3/s) at an upstream pressure head H_s (m). The pipe delivers a pressure head H_d (m) to a
80 downstream user that imposes a demand Q_d (m^3/s) in the pipe. Users downstream of a pipe
81 impose a demand Q_d (m^3/s) that exceeds the minimum needed water use Q_{\min} (m^3/s), which
82 represents the most efficient use of water by the user given best-available water technologies
83 (Vickers 2001). There are a number of reasons for this inefficient water use including household
84 leaks, inefficiencies in appliances, theft of water (AWWA 2009), water waste through inefficient
85 industrial processes (Morales et al. 2011; Friedman et al. 2011), user perception of appropriate
86 water use (Hoekstra and Chapagain 2007), and unnecessary lawn and garden watering (Askew
87 and McGuirk 2004). For the sake of generality, the pipe can have a leak that produces a leakage
88 flow rate of Q_l (m^3/s). The pipe also conveys an additional flow $Q_{\text{ds}}=Q-Q_d-Q_l$ (m^3/s) to users
89 further downstream of the pipe. The upstream pressure head H_s (m) supplied to the pipe is
90 greater than the minimum required pressure head H_{\min} (m) needed to provide an acceptable

91 service to the downstream user. The difference between supplied head H_s (m) and pressure head
 92 delivered H_d (m) is made up of local losses H_{local} (m) (e.g., valves, in-line turbines, blockages)
 93 and the combined frictional head loss due to demand Q_d (m³/s), leakage Q_l (m³/s), and the
 94 additional flow Q_{ds} (m³/s) to provide water service to downstream users. The pressure head
 95 delivered to downstream users H_d (m) is made up of the minimum pressure head required, H_{min}
 96 (m), and surplus head, $H_{surplus}$ (m).

97 The energy components indicated in Figure 1 are defined in Table 1 and described below.

$$E_{supplied} = E_{delivered} + E_{ds} + E_{leak} + E_{friction} + E_{local} \quad (\text{Joules}) \quad (1)$$

98 where $E_{supplied}$ = energy supplied to the upstream end of the pipe (Joules); $E_{delivered}$ = energy
 99 delivered to the user (in Joules) to satisfy demand Q_d (m³/s) at pressure head H_d (m); E_{ds} = energy
 100 that flows out of the pipe to meet downstream user demands (Joules); E_{leak} = leak energy
 101 (Joules); E_{local} = local energy losses (Joules). The term α is equal to 1.85 in the Hazen-Williams
 102 friction loss model and $\alpha = 2$ in the Darcy-Weisbach model; K = pipe resistance and Δt = the
 103 hydraulic time step (3,600 seconds or 1 hour) used in the 24-hour diurnal simulation.

104 **Methods**

105 *Metrics to Evaluate Energy Performance at the Pipe Level*

106 Five metrics have been developed to characterize the gross and net energy efficiencies,
 107 energy needed by user, energy lost to friction, and energy lost to leakage in the pipes of a water
 108 distribution network.

109 Gross and Net Efficiencies: The gross energy efficiency (GEE) in Equation 2 compares the
 110 energy delivered to the users serviced by a pipe to the energy supplied to that pipe. The
 111 theoretical maximum value for GEE is 100 percent, which means that all the energy supplied to
 112 the pipe is delivered to its user, even though this is impossible to achieve in practice. The

113 theoretical minimum value for GEE is 0 percent, which means that none of the energy supplied
114 to the pipe is delivered to its users, as all the energy is lost along the pipe.

$$GEE = \left(\frac{E_{\text{delivered}}}{E_{\text{supplied}}} \right) \cdot 100\% \quad (2)$$

115 The net energy efficiency (NEE) in Equation 3 compares the energy delivered to users
116 serviced by a pipe to the net energy in that pipe. Here, net energy is defined as the energy
117 supplied to the pipe minus the energy supplied to users located downstream of the pipe and not
118 directly serviced by the pipe. The maximum value of NEE is 100 percent, where all the energy
119 supplied (exclusively to the pipe) is delivered to its users. The theoretical minimum value is 0
120 percent, where none of the energy supplied to the pipe is delivered to its users.

$$NEE = \left(\frac{E_{\text{delivered}}}{E_{\text{supplied}} - E_{\text{ds}}} \right) \cdot 100\% \quad (3)$$

121 Energy Needed by User: The energy needed by the users (ENU) at a node in Equation 4
122 compares the energy delivered to the users serviced by a pipe against the minimum energy
123 needed by those users. A value of ENU below 100 percent indicates that there is an insufficient
124 level of energy to meet the service expectations of the users (either in the form of flow, pressure
125 head, or both), and a value of 100 percent means that energy delivered to the users is equal to the
126 minimum energy needed to meet their service expectations. Values of ENU above 100 percent
127 denote a surplus energy over and above the level needed.

$$ENU = \left(\frac{E_{\text{delivered}}}{E_{\text{need}}} \right) \cdot 100\% \quad (4)$$

128 The minimum mechanical energy in the water needed to meet the minimum needs of the
129 downstream user in Equation 4 is calculated by integrating the minimum needed power by a

130 defined period of use Δt

$$E_{\text{need}} = \gamma Q_{\text{min}} H_{\text{min}} \Delta t \quad (\text{Joules}) \quad (5)$$

131 where γ = unit weight of water (approximately 9,810 N/m³ at 18°C); Q_{min} = minimum water
132 use needed by users (m³/s); H_{min} = minimum pressure head required to deliver acceptable water
133 service to users (m); Δt = time step over which minimum needed power is integrated (seconds).
134 (Note that integration can be used to calculate minimum energy needed over a continuous diurnal
135 demand period.). Determining the minimum water use (Q_{min}) is difficult because minimum water
136 use varies between individual users within the same user type (Friedman et al. 2013). The
137 minimum pressure head (H_{min}) required is usually determined by water utility standards but in
138 reality can vary across users depending on their subjective perception of the minimum pressure
139 required to perform their individualized water use activities (Mays 2002, City of Toronto 2009,
140 Region of Peel 2010, Denver Water 2012). In this paper, the minimum pressure of approximately
141 30 metres (m) commonly imposed by North American water utilities (City of Toronto, 2009;
142 Region of Peel, 2010; Denver Water, 2012) was used to calculate the minimum mechanical
143 energy.

144 Energy Lost to Friction: The energy lost to friction (*ELTF*) in Equation 6 compares the
145 magnitude of friction loss in the pipe (to satisfy the demand and leakage at the end of the pipe,
146 and demands downstream of the pipe) to the net energy supplied to the pipe. This indicator can
147 be used to characterize the effectiveness of pipe relining, pipe replacement, and leak repair to
148 reduce frictional losses. The metric *ELTF* can range between 0 and 100 percent, where a value of
149 0 percent means that there are no frictional energy losses in the pipe, and a value of 100 percent
150 means that all the net energy supplied to the pipe is lost to friction along the pipe.

$$ELTF = \left(\frac{E_{\text{friction}}}{E_{\text{supplied}} - E_{\text{ds}}} \right) \cdot 100\% \quad (6)$$

151 Energy Lost to Leakage: The energy lost to leakage (*ELTL*) in Equation 7 compares the
 152 magnitude of energy lost to leakage relative to the net energy supplied to the pipe. The leakage
 153 term in the numerator includes leak energy, E_{leak} , and the frictional energy loss along the pipe
 154 required to meet the leakage flow, Q_l , at the end of the pipe $E_{\text{friction(leak)}}$ (see Table 1). The *ELTL*
 155 metric can range between 0 and 100 percent, where a value of 0 percent means that there is no
 156 energy loss due to leakage in the pipe and a value of 100 percent means that all the net energy
 157 supplied to the pipe is lost to leakage and friction to satisfy the leak in the pipe. The *ELTL* metric
 158 can be used to characterize the effectiveness of leakage repair and pressure management in
 159 reducing leakage energy loss.

$$ELTL = \left(\frac{E_{\text{leak}} + E_{\text{friction(leak)}}}{E_{\text{supplied}} - E_{\text{ds}}} \right) \cdot 100\% \quad (7)$$

160 *Calculation of Energy Metrics*

161 The pipe-level energy metrics presented above are evaluated by following a number of steps.
 162 First, the EPANET2 (Rossman 2000) network solver is used to calculate the hydraulic head at
 163 model nodes and pipe flow in model links over a diurnal period. Because the pipe flow direction
 164 may change over a day, the hydraulic head at both ends of each pipe are compared at each time
 165 step and the node with the higher hydraulic head is identified as the upstream node. Further, to
 166 correctly recognize to which pipes a node is an upstream node and to which pipes a node is a
 167 downstream node, the mechanical energy that a pipe delivers to the users at its downstream node
 168 (multiple-link node) is proportional to its flow rate and is weighted by its flow rate into its
 169 corresponding downstream pipes, such that

$$(E_{\text{delivered}})_{i,j} = \gamma \left(\frac{Q_i}{\sum_{k=1}^m Q_k} \right) D_j H_j \Delta t \quad (\text{joules}) \quad (8)$$

170 where $(E_{\text{delivered}})_{i,j}$ = energy delivered by pipe i to multiple-link node j (joules); D_j = demand at
 171 downstream multiple-link node j located downstream of pipe i (m^3/s); H_j = hydraulic head at
 172 multiple-link node j located downstream of pipe i (m); Q_i = flow in pipe i (m^3/s); m = number of
 173 $k = 1, 2, 3, \dots, m$ upstream pipes connected to the multiple-link node j . For example in Figure 2a,
 174 upstream pipes P-1 and P-2 with flow rates of 1.3 litres per second (L/s) and 1.6 L/s are
 175 connected to downstream node J-1 (multiple-link node) with a demand of 2.1 L/s. Pipes P-3 and
 176 P-4 are located downstream of node J-1. The mechanical energy ($\gamma D H \Delta t$) delivered by Pipe 1
 177 is weighted by the ratio of its flow to the total flow conveyed by the upstream pipes, or
 178 $1.3/(1.3+1.6)$.

179 Once the upstream and downstream nodes of each pipe have been determined, and the energy
 180 delivered to each node resolved as described above, the hydraulic heads and pipe flows
 181 simulated over the diurnal period are used to calculate the energy components in Table 1 to
 182 evaluate the pipe-level metrics in Equations 2-7. An example is shown in Equation 9 where
 183 hourly values of $E_{\text{delivered}}$ and E_{supplied} are aggregated together throughout the day to calculate a
 184 single value of GEE that is representative of the entire day

$$GEE = \left[\frac{(E_{\text{delivered}})_{t=1} + (E_{\text{delivered}})_{t=2} + \dots + (E_{\text{delivered}})_{t=24}}{(E_{\text{supplied}})_{t=1} + (E_{\text{supplied}})_{t=2} + \dots + (E_{\text{supplied}})_{t=24}} \right] \cdot 100\% \quad (9)$$

185 *Hydraulic Proximity Indicator*

186 In the following sections of this paper, the proximity of a pipe to a water source is considered as
 187 a factor that can influence the energy performance of a pipe. In anticipation of this, an indicator
 188 that characterizes the hydraulic proximity of a pipe to a nearby water source is defined in

189 Equation 10. The hydraulic proximity indicator is based on the general observation that hydraulic
190 head or pipe flow (or both) tend to decrease as one moves away from a water source to the
191 periphery of the system where pipes generally convey smaller flow to downstream users. The
192 hydraulic proximity indicator is a function of the role of the pipe (transmission or distribution)
193 and its location relative to the water source of the system or pressure zone in which it is found. It
194 is important to note that hydraulic proximity is not an indicator of the linear distance that
195 separates a pipe from a water source, but rather an indirect indicator of the proximity of a water
196 main asset to a water source.

$$\text{Proximity Indicator} = Q \cdot H_s \text{ (m}^4 \text{ / s)} \quad (10)$$

197 in which Q is the pipe flow (m³/s) and H_s is the hydraulic head provided at the upstream node of
198 a pipe (m) calculated with the EPANET2.0 hydraulic model. (All heads are calculated according
199 to a fixed datum of 0 m.) High values of the hydraulic proximity indicator as defined in Equation
200 10 suggest that the water main is located near a water source, whereas low values suggest that
201 the main asset is located away from a water source.

202 **Application of Pipe-Level Metrics to Three Distribution Systems**

203 The new pipe-level metrics were applied to a large *ensemble* of water mains across three
204 distribution systems to examine how system operation and system improvements impinge on the
205 spatial and temporal patterns of energy performance in drinking water mains. System #1 (Figure
206 2b) is reported in Cabrera et al. (2010) and comprises 14 pipes (40 km), an elevated tank and a
207 pumping station controlled by minimum and maximum tank levels. The system has a total daily
208 demand of 79.8 ML/day with peaks at 8 am (peaking factor of 1.3) and 4 pm (peaking factor of
209 1.3) (Figure 3). Approximately 15 percent of the total demand is lost to leakage throughout the
210 day. The leakage is assigned to the nodes using emitter coefficients in EPANET2.0 (Cabrera et

211 al., 2010). Leakage is thus a function of time and pressure. At each time step, EPANET2 is used
212 to calculate pressure head and leakage loss to evaluate the energy lost to leakage (*ELTL*). The
213 average daily pressure in System #1 is approximately 35 m.

214 System #2 (Figure 4a) is a medium-sized distribution system in the US Midwest that includes
215 1,183 pipes (166 km), 4 pumping stations and 4 elevated tanks. The water distribution system is
216 comprised of three pressure zones to overcome an elevation difference of 99.7 m to serve a
217 population of 20,000 people. The system has a total daily demand of 237.9 ML/day with an 8 am
218 morning peak (peaking factor of 1.25) and a 10 pm evening peak (peaking factor of 1.67) (Figure
219 3). The daily mean pressure is 57 m and higher than in System #1. No leakage is considered in
220 this network.

221 System #3 (Figure 4b) is a large distribution network in the US Midwest that comprises
222 27,231 pipes (5,500 km), 28 pumping stations, and 27 elevated tanks that serves approximately 1
223 million customers. This system has a total daily demand of 12,765 ML/day with an 8 am
224 morning peak (peaking factor of 1.18) and a 9 pm evening peak (peaking factor of 1.40). The
225 system has an average nodal pressure of 53 m. Leakage is modelled as a constant demand
226 assigned by area to model nodes based upon the results of a detailed leakage study conducted by
227 the water utility.

228 **Results**

229 *System #1*

230 System #1 is a simple system and thus an ideal network with which to demonstrate the new
231 pipe-level metrics by way of two management scenarios (Figure 2b). The first scenario is the
232 Baseline (B) scenario where the pipes are unimproved. The second scenario is the Leakage
233 Reduction (L) scenario where pipe leakage is reduced by 50 percent by reducing emitter

234 coefficients in the model. In this paper, the energy metrics are dimensionless and expressed as a
235 percentage of i) energy supplied to the pipe (E_{supplied}), or ii) minimum energy needed at the
236 downstream node (E_{need}), or iii) the net energy in the pipe ($E_{\text{supplied}} - E_{\text{ds}}$). For the sake of
237 consistency, numerical values of the metrics that range between 0 and 30 percent are considered
238 “low”, while values that range between 30 and 70 percent are considered “moderate”, and values
239 that range between 70 and 100 percent are considered “high”.

240 Baseline Scenario (No Improvements): The baseline results in Table 2 indicate that the
241 presence of both frictional losses and leakage in the system produce low to moderate values of
242 GEE that range between 8 to 45 percent. This association is evident in the pipes closest to the
243 source and that carry higher flow rates (e.g., pipes 11, 12, 111, and 113) because these pipes
244 must convey flows destined to locations further downstream in the network. Similarly, the
245 presence of leakage in the system produces values of NEE that range between 29 to 76 percent.

246 The results in Table 2 indicate that pipes 22 and 113 have an ENU that ranges from 110 to
247 113 percent. These pipes are located between the tank (dominant source of water in this system)
248 and the highest nodal demand at junction J-22, and thus the large energy surplus reflects the
249 delivery of water to this location from the source. The pipes 31, 121, and 122 located further
250 away from the elevated tank tend to have less surplus energy, and these pipes show an energy
251 deficit and a numerical value of ENU that ranges between 91 to 97 percent; these pipes deliver
252 less energy to their users due to water losses between the sources and these demand locations.

253 The baseline values of $ELTF$ suggest that friction losses comprise 39 to 66 percent of net
254 energy in pipes 11 and 111, both of which are in close proximity to the pumping station and
255 carry high flows. Friction comprises 1.3 to 8.0 percent of net energy in the other pipes that
256 convey smaller flows. Also, the results for leakage losses and $ELTL$ suggest that pressure and not

257 leak size (as reflected in the emitter coefficient), drives the level of leakage and results in high
258 values of *ELTL*. For example, even though pipes 113 and 123 both have a low value of emitter
259 coefficient, their proximity to the tank in a high-pressure zone causes them to have a high
260 leakage levels and high values of *ELTL* that range from 18.8 to 22.2 percent.

261 The results also show that *NEE* in Pipe 121, located far from the tank, is driven almost
262 exclusively by the demand at the downstream node of this pipe (*NEE* = 55 to 61 percent from 12
263 am to 6 am; *NEE* = 75 to 82 percent from 6 am to 6 pm), whereas the net efficiency in Pipe 11
264 near the pump is influenced by the pumping and tank operations of the system (*NEE* = 10 to 20
265 percent during pumping periods of 12 am to 3 am and 1 pm to 5 pm). This finding highlights
266 how the proximity to pumps and tanks and the role of pipes in the global hydraulic performance
267 affects the net efficiency and energy lost to friction observed in individual pipes.

268 Leakage Reduction Scenario (from 15 to 8 percent of demand): The results for the leakage
269 reduction scenario in Table 2 indicate that reducing leakage flow from 15 to 8 percent produces a
270 0.2 to 11.0 percent increase in the *GEE* relative to baseline because it narrows the gap between
271 energy delivered and energy supplied. This relationship is especially true for the pipes located
272 further downstream (e.g., pipes 121, 122, 123, 31 and 32). Similarly, all pipes see a 3.9 to 18.8
273 percent increase in *NEE* relative to baseline as a result of leakage reduction. A reduction in
274 leakage also increases the *ENU* (or reduces the energy deficit) by 1.7 to 10.1 percent relative to
275 baseline because energy lost to leakage is decreased in the pipes. In most pipes, a reduction in
276 leakage is tantamount to reduced pipe flow and therefore less energy lost to leakage and friction.
277 For example, a reduction in leakage produces a 0.8 to 8.0 percent decrease in *ELTF* in pipes 112,
278 113, and 121 relative to baseline. However, in smaller pipes located further downstream in the
279 system (e.g., pipes 31, 32), the friction losses tend to increase because of an increase in pipe

280 flow—a result of reduction in leakage between the water source and these pipes. Lastly, a
281 reduction in leakage causes a 47.2 to 57.3 percent decrease in *ELTL* in all pipes.

282 *System #2*

283 In System #2, the energy metrics were evaluated only for those pipes (approximately 600
284 pipes or 60 percent of the total number of pipes) that have a non-zero downstream demand.
285 Because leakage was not modelled for this system, only metrics *GEE*, *NEE*, *ENU*, and *ELTF*
286 were evaluated for the baseline scenario; the impact of interventions such as leakage reduction
287 on energy dynamics was not considered. System #2 was simulated with assumed leakage levels
288 (no leakage, 15 percent, 30 percent) and the results (not shown) suggest that the presence of
289 leakage produces a similar frequency distribution of the numerical values of the four energy
290 metrics as shown in Figures 5 and 9. The absence of leakage data for System #2 does not
291 preclude the comparison of energy dynamics in System #2 with the other two systems (Systems
292 #1 through #3).

293 The histogram results in Figure 5 show that the *GEE* follows a bimodal distribution. Here,
294 over 60 percent of the pipes have a low value of *GEE* that ranges from 0 to 10 percent while
295 approximately 14 percent of the pipes have a high value of *GEE* that ranges from 90 to 100
296 percent. It is noted that low values of *GEE* in Figure 6a do not necessarily point to a poor energy
297 performance as these pipes tend to be located near the major system components and supply a
298 large number of users downstream. Pipes with a high *GEE* tend to be located near dead-end
299 zones where most of the energy supplied to the pipe is used to satisfy demand at the downstream
300 node of the pipe. Over 90 percent of the pipes have a *NEE* that ranges from 90 to 100 percent
301 (Figure 5). Figure 6b indicates that there are trunk mains and distribution mains near pumps and
302 tanks with low to high values of net efficiency (0.1 to 80 percent).

303 The majority of pipes (almost 80 percent) exhibit a low *ELTF* between 0 and 10 percent
304 (Figure 5). However a minority of pipes (almost 15 percent) had high frictional energy losses,
305 with *ELTF* between 90 and 100 percent. These pipes are large-diameter trunk mains that carry
306 large flows with a high average unit headloss, and are located in close proximity to a pump or
307 tank. (In this paper, average unit headloss is calculated by taking the arithmetic average of unit
308 headloss in a pipe over the 24-hour diurnal period.)

309 The energy performance of two representative pipes (Pipes 463 and 926 – see Figures 4a
310 and 6) during the 24-hour diurnal period was also examined (Figure 7). Pipe 463 is a 300 mm CI
311 water main located near pumping station P1 in System #2 and conveys flows between 15-86 L/s
312 throughout the service day. Not surprisingly, the *ELTF* in Pipe 463 varies in lockstep with the
313 flow in the pipe, whereby *ELTF* varies between 0.1 to 3 percent during low-demand periods
314 and *ELTF* varies between 5 to 27 percent during high-demand periods. The net energy efficiency
315 in Pipe 463 varies widely during the 24-hour diurnal period, with values of *NEE* between 72 and
316 86 percent during high-demand periods and values between 92 to 100 percent during low-
317 demand periods. By contrast, Pipe 926 is a 150 mm CI main located near the periphery of the
318 system (Figure 4a). This pipe conveys a near-constant flow of less than 0.10 L/s. Not
319 surprisingly, *ELTF* is correspondingly low (near 0 percent throughout the whole day in Figure 7)
320 and the net energy efficiency of this pipe is at a near-constant level of 100 percent. The results
321 suggest that the energy performance (in this case efficiency and friction) of a pipe is contingent
322 on the proximity of that pipe to a pump or tank.

323 The influence of the distance between a pipe and a major component on the energy performance
324 of that pipe was examined further. This was done by plotting *ELTF* calculated with Equation 6
325 and the max/min hourly value of energy lost to friction (*ELTF*-max, *ELTF*-min, Equation 9)

326 observed over the 24-hour diurnal period against the hydraulic proximity indicator (Equation 10)
327 in Figure 8 for an *ensemble* of 684 pipes. The results suggest that *ELTF* is smaller in distribution
328 mains located further away from water sources that convey low flows and incur small losses
329 (*ELTF*-min near 0 percent). Pipes located close to water sources tend to have a value of *ELTF*-
330 max of 100 percent (this occurs during the peak demand period). Figure 8 shows a high variation
331 in *ELTF*-max in pipes located far away from water sources. This variability is likely owing to
332 differences in diameter, roughness, and service flows across the smaller water distribution mains
333 located on the periphery.

334 *System #3*

335 The energy metrics were evaluated for over 21,000 pipes, which represents approximately 77
336 percent of pipes in System #3. In general, the findings for System #3 are similar to those for
337 System #2 in that the frequency distribution of the numerical values of metrics follows a bimodal
338 shape (Figure 9). The bimodal nature of the results emphasizes the variability of energy
339 performance in complex systems when compared to a simpler system like System #1. The
340 majority of pipes exhibit a good energy performance (high net energy efficiency, small frictional
341 losses) and a minority of outlier pipes exhibit a poor energy performance (low efficiency, high
342 losses).

343 The histogram in Figure 9 indicates that approximately 80 percent of pipes have a value of
344 *GEE* that ranges between 0 and 20 percent. As noted before, low values of *GEE* do not
345 necessarily point to a poor energy performance; in these trunk pipes the majority of the energy
346 supplied to the pipe is transferred to users well downstream of the pipe and only a small fraction
347 of the energy is delivered to users at the end of the pipe. Figure 9 also indicates that 2 percent of
348 pipes have a value of *GEE* that ranges between 90 and 100 percent. In these distribution mains

349 near cul-de-sac areas, most of the energy is transferred to users directly at the end of the pipe.
350 Approximately 90 percent of pipes have a *NEE* that ranges between 9 and 100 percent (Figure 9)
351 but a minority of pipes (4 percent) have a low to moderate net energy efficiency that ranges
352 between 10 and 50 percent. A detailed analysis showed that no single factor accounted for the
353 low values of net energy efficiency in these pipes.

354 More than 95 percent of pipes have an *ENU* that ranges between 100 and 120 percent (Figure
355 9) and over 90 percent of pipes have a low *ELTF* that ranges between 0 and 10 percent. Leakage
356 performance for this system is good with over 95 percent of pipes having a low *ELTL* that ranges
357 between 0 and 10 percent. Despite this generally good performance, there are a small number of
358 outlier pipes (approximately 3 percent of total) with a moderate to high *ELTF* that ranges
359 between 40 and 100 percent. Many of these poorly performing pipes were found to be large-
360 diameter trunk mains that convey large flows from water sources to the rest of the system. A
361 small number of pipes (2.5 percent of total) were also found to have a moderate to high *ELTL*
362 that ranges between 40 and 100 percent, and this is a direct result of the assigned leakage values
363 from the water utility leakage study.

364 The diurnal variation of *NEE* and *ELTF* in select pipes of System #3 were examined (results
365 not shown). As before, the results suggest that proximity to a water source and magnitude of pipe
366 flow conveyed by the pipe are both factors that have a large impact on the diurnal variation of
367 net energy efficiency and energy lost to friction. Generally, pipes located far away from water
368 sources convey little flow (with small headloss) and have values of *NEE* near 100 percent and
369 *ELTF* near 0 percent throughout the day. In larger trunk mains located closer to water sources
370 with comparatively high flow rates, *NEE* and *ELTF* track closely with diurnal variations in
371 pumped flow in these pipes, as was also observed in System #2.

372 The influence of the distance between a pipe and a major component on the energy
373 performance of that pipe was examined in System #3. Figure 10 plots the *ELTL* and the max/min
374 value of energy lost to leakage (*ELTL*-max and *ELTL*-min over a 24-hour period) for each pipe
375 (y-axis) against the hydraulic proximity indicator (x-axis). The values of the energy loss metrics
376 *ELTL*, *ELTL*-max, and *ELTL*-min are moderate (30 to 60 percent) near water sources (proximity
377 ranges between 3,000 and 6,000 m⁴/s) and moderate to high (30 to 100 percent) at the periphery
378 of the system (proximity ranges between 0 and 250 m⁴/s). This relationship can be explained by
379 two factors: 1) the trunk water mains close to a water source have a low level of leakage while
380 the smaller distribution mains near the periphery of the system have a higher level of leakage,
381 and 2) the values of net energy supplied to the pipe ($E_{\text{supplied}} - E_{\text{ds}}$, denominator of *ELTL*) are
382 large and outweigh the energy lost due to leaks ($E_{\text{leakage}} + E_{\text{friction(leak)}}$, numerator of *ELTL*)
383 because of the low level of leakage at locations near water sources. There is also a high degree of
384 variability in the values of *ELTL* and *ELTL*-max near the periphery of the system as shown in
385 Figure 10 (proximity ranges between 0 and 250 m⁴/s).

386 *Comparison of Energy Metrics With Average Unit Headloss and Pressure Head*

387 The usual practice is to use average unit headloss to identify pipes with high frictional line
388 losses and pressure head (or excess pressure head) to identify which pipes are delivering excess
389 mechanical energy to customers. Here, the energy lost to friction (*ELTF*) was compared to
390 average unit headloss to assess their effectiveness in identifying pipes with high frictional energy
391 losses. To do this, the five pipes with the highest values of *ELTF* and the five pipes with the
392 highest values of average unit headloss were selected from the *ensemble* of 1,183 pipes in
393 System #2 and their corresponding annual frictional energy loss was calculated. (Annual
394 frictional energy loss was calculated by multiplying the frictional energy loss in a pipe over the

395 24-hour diurnal period and multiplying this daily energy use by 365 days.) This was repeated for
396 System #3 (*ensemble* of 21,156 pipes). The results in Table 3 indicate the five pipes with the
397 highest values of *ELTF* and average unit headloss sorted in descending order of annual frictional
398 energy loss. Table 3 indicates that in System #2, *ELTF* and average unit headloss identified the
399 same four pipes (69, 159, 117, 41) with the highest annual frictional energy loss, and in System
400 #3, *ELTF* and average unit headloss both identified pipe 3464 as having the highest annual
401 frictional energy loss. It is noted that average unit headloss identified four pipes with higher
402 annual frictional energy loss than the *ELTF*. A possible reason for this is that average unit
403 headloss relates more directly to annual frictional energy loss than *ELTF*.

404 In Table 4, the energy needed by user (*ENU*) and energy lost to leakage (*ELTL*) were
405 compared to pressure head to determine their effectiveness in identifying pipes that experience
406 the highest energy losses to leakage. Similar to the above, the five pipes with the highest values
407 of *ENU* and the highest values of pressure head were selected from the *ensemble* of pipes in
408 System #3 and sorted in descending order of annual energy lost to leakage. (Annual energy lost
409 to leakage was calculated by multiplying the leak energy at the downstream node of a pipe over
410 the 24-hour diurnal period and multiplying this daily energy use by 365 days.) The results in
411 Table 4 suggest that the pipes identified with *ENU* and *ELTL* had higher values of annual energy
412 lost to leakage than those identified with pressure head. The metrics of gross energy efficiency
413 (*GEE*) and net energy efficiency (*NEE*) were not compared to average unit headloss and pressure
414 head. The interested reader can find the model data and the implementation code for the new
415 energy metrics in the supplemental data files appended to this manuscript.

416

417 **Discussion**

418 Previous research has shown that reducing leakage flow in distribution systems produces a
419 corresponding reduction in energy use (Colombo and Karney 2002, 2005). Cabrera et al. (2010)
420 found that leak-free systems required less energy per cubic metre of water delivered. Not
421 surprisingly, the observations made in System #1 of this paper corroborate these observations,
422 whereby a 50 percent reduction in leakage flow produced a near proportional decrease in energy
423 lost to leakage and improved gross and net efficiency and reduced energy lost to friction.
424 Additional observations on more realistic and more complex systems are needed to verify that
425 this near one-to-one relationship holds for most systems.

426 The analysis of Systems #2 and #3 showed that the statistical distribution of energy
427 performance of the pipes in these two large systems is bimodal where the majority of pipes have
428 a good energy performance (high efficiency, low energy losses) but that an important minority of
429 outlier pipes also have a poor energy performance (low efficiency, high energy losses to friction
430 and leakage). The research of Dziedzic and Karney (2014) showed an asymmetrical energy
431 performance across the Toronto distribution system such that water mains immediately
432 downstream of treatment works had higher energy dissipation rates than pipes located further
433 away from treatment plants. The results of the current paper corroborate this previous finding. In
434 all three systems examined, pipes near components tended to have low gross and net efficiencies
435 and high energy losses due to friction and leakage, while pipes located far away from
436 components had high gross and net efficiencies and low friction and leakage losses. Pipes near
437 components that experienced surplus pressures generally met the minimum energy needed by the
438 users ($ENU > 100$ percent) even if their *ELTL* was generally high. However, pipes in lower-
439 pressure regions further away from components generally fell short of meeting the minimum

440 energy needed by the users ($ENU < 100$ percent) and showed lower energy losses to leakage.

441 The findings of this paper showed that there is also a strong diurnal variation in energy
442 inputs and outputs at the scale of the individual pipe. For all systems examined, the diurnal
443 variation of energy efficiency and energy lost to friction in pipes close to components tended to
444 be influenced heavily by pumping periods and tank-draining periods when pipe flows and losses
445 were high in these pipes. Diurnal variation of energy efficiency and energy lost to friction in
446 pipes located far away from components tended to be more influenced by diurnal variation in
447 demand. These pipes had a low efficiency and high frictional losses during high-demand periods
448 and high efficiency and low frictional losses during low-demand periods. These finding support
449 the previous research that showed wide diurnal variations in global energy efficiencies in the
450 Toronto distribution system, where low frictional losses and high efficiencies were observed in
451 the night time when demand was low (Dziedzic and Karney 2014).

452 The results of this study also showed that the new metrics of *ELTF*, *ENU*, and *ELTL* may be
453 complementary indicators of energy performance in a pipe to the traditional indicators of average
454 unit headloss and pressure head. The results showed that the average unit headloss was on the
455 whole more successful than the *ELTF* metric in identifying pipes with the highest annual energy
456 frictional losses. This shows that average unit headloss is still an important measure because it is
457 directly tied to the pumping costs borne by a water utility. Nevertheless, the *ELTF* metric could
458 be used to evaluate the contribution of frictional losses relative to energy lost to leakage and
459 energy lost at the point of demand in pipes selected for rehabilitation with the average unit
460 headloss variable. Arguably, this could help water utilities understand the relative importance of
461 friction in the context of other energy losses in their system.

462 The results also suggested that the *ENU* and *ELTL* metrics are more successful than pressure

463 head in identifying the pipes that have the greatest energy losses to leakage. This is because *ENU*
464 and *ELTL* account for both flow and pressure head at the point of leakage that drive the
465 mechanical energy that exits the system. These results suggest that *ENU* and *ELTL* have the
466 potential to be good indicators of energy lost to leakage in distribution systems. However, the
467 results of System #1 suggest that it is the pipes that have both high pressure and high leakage
468 flow which tend to have the highest energy loss to leakage. For this reason, the results of this
469 study suggest that pressure head or leakage flow alone are not good indicators of energy lost to
470 leakage.

471 While the location of the pipe in the system has been found to have an important influence
472 on energy use, there are likely synergistic effects between the proximity to a water source and
473 other factors such as pipe diameter, pipe flow, leakage level, unit headloss that work together to
474 determine energy performance in a pipe. This paper did not examine the underlying, combined
475 effects of these key factors on the energy performance of pipes.

476 In order for the metrics of this paper to provide an accurate picture of energy performance in
477 water mains, a calibrated network model is needed with good pipe data (e.g., wall roughness and
478 diameter) and good data on the magnitude and spatial distribution of leakage. It is noted that
479 many municipalities in Canada and the US do not have good spatially-disaggregated data on
480 leakage and pipe roughness/diameter in their typically large pressure zones. Increasingly, these
481 municipalities are quantifying leakage levels and pipe flows by metering small well-defined
482 DMA (district metering area) areas that are smaller in size than traditional pressure zones. DMA
483 sectorization and flow/leak monitoring is already well-established in European countries and
484 other parts of the world and the metrics can be applied with good accuracy in these jurisdictions.

485 **Conclusion**

486 Previous research has shown the usefulness of energy metrics to examine the global or system-
487 wide energy performance of water distribution systems (Cabrera et al. 2010; Cabrera et al.
488 2014a, 2014b; Dziedzic and Karney 2014) and the balance between inputs and outputs of energy
489 through friction and leakage losses. The current paper offered a complementary approach in the
490 form of novel metrics that resolve energy performance at the spatial scale of the individual water
491 main. The results of the paper showed that average unit headloss is on the whole more successful
492 than *ELTF* in identifying pipes with high frictional energy losses, but that the new *ENU* and
493 *ELTL* metrics are more successful than pressure head in identifying pipes that experience the
494 highest energy losses to leakage. These metrics have the potential to assist water utilities in
495 understanding the energy performance of unimproved pipes alongside cost, structural and water
496 quality concerns. While outside the scope of this paper, water utilities can potentially leverage
497 this pipe-level energy analysis to perform life-cycle costing that compares the cost of pipe
498 rehabilitation against the surplus energy cost (from leakage and frictional losses) incurred in a
499 pipe when not rehabilitated (do-nothing option) to characterize the payback period of the
500 rehabilitation intervention.

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581

582 Table 1. Energy inputs and outputs linked to fluid flow in a pipe.

583 Table 2. Numerical values of metrics *GEE*, *NEE*, *ENU*, *ELTF*, and *ELTL* for the baseline and
584 leakage reduction scenarios in System #1 (reported in Cabrera et al. (2010)). *GEE*: Gross Energy
585 Efficiency; *NEE*: Net Energy Efficiency; *ENU*: Energy Needed by User; *ELTF*: Energy Lost to
586 Friction; *ELTL*: Energy Lost to Leakage.

587 Table 3. Pipes with the highest values of average unit headloss and energy lost to friction (*ELTF*)
588 in System #2 (*ensemble* of 1,183 pipes) and System #3 (*ensemble* of 21,156 pipes). (Pipes are
589 sorted by annual frictional energy loss in descending order.)

590 Table 4. Pipes with the highest values of pressure, energy needed by user (*ENU*), and energy lost
591 to leakage (*ELTL*) in System #3 (*ensemble* of 21,156 pipes). (Pipes are sorted by annual energy
592 lost to leakage in descending order.)

593

594 Table 1.

595

Energy Components	Equations
Energy supplied	$E_{\text{supplied}} = \gamma Q H_s \Delta t$
Energy delivered	$E_{\text{delivered}} = \gamma Q_d H_d \Delta t$
Minimum energy needed to meet the end-user demand in an pipe	$E_{\text{need}} = \gamma Q_d H_{\text{min}} \Delta t$
Energy that flows out of pipe to meet downstream demands	$E_{\text{ds}} = \gamma Q_{\text{ds}} H_d \Delta t$
Leak energy	$E_{\text{leak}} = \gamma Q_l H_d \Delta t$
Energy lost to friction to meet demand	$E_{\text{friction(demand)}} = \gamma [K (Q_d)^\alpha] Q_d \Delta t$
Energy lost to friction to meet leakage	$E_{\text{friction(leak)}} = \gamma [K (Q_l)^\alpha] Q_l \Delta t$
Energy lost to friction (meet d/s demand)	$E_{\text{friction(ds)}} = \gamma [K (Q_{\text{ds}})^\alpha] Q_{\text{ds}} \Delta t,$ where $Q_{\text{ds}} = Q - Q_d - Q_l$

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607 Table 2.

Pipe	GEE (percent)		NEE (percent)		ENU (percent)		ELTF (percent)		ELTL (percent)	
	B	L	B	L	B	L	B	L	B	L
11	8	9	29	29	103	106	66	68	4	2
12	8	8	52	52	106	108	39	42	7	3
113	22	23	73	73	110	115	8	8	19	9
123	42	47	70	70	101	111	4	4	22	11
111	22	24	48	48	103	108	39	40	10	5
121	45	48	73	73	97	104	5	5	14	7
122	43	47	72	72	91	98	2	2	18	9
22	37	37	76	76	113	116	6	7	9	5
21	33	35	75	75	104	109	5	6	12	6
31	37	39	73	73	95	102	1	2	15	7
32	42	45	71	71	104	112	2	2	18	9
112	33	36	74	74	106	111	7	7	15	7

608 B = baseline scenario; L = leakage reduction scenario.

609

610 Table 3.
611

Pipe ID	Average Unit Headloss (m/km) ^c	Annual Frictional Energy Loss (MWh) ^d	Pipe ID	<i>ELTF</i> (Percent) ^e	Annual Frictional Energy Loss (MWh) ^d
System #2					
69 ^a	470.8	2,971.6	69 ^a	99.9* ^f	2,971.5
159	277.1	963.3	159	99.9*	963.3
431	131.3	644.4	117	99.9*	178.8
117	88.9	178.8	41	99.9*	150.0
41	478.2	150.0	P-97	99.9*	59.9
System #3					
3464 ^b	3.9	39,552.0	3464 ^b	99.9* ^f	39,552.0
26688	2.3	28,081.6	10959	99.9*	1,313.0
9706	0.1	3,908.0	8735	99.9*	894.7
10942	0.2	1,804.4	11236	99.9*	326.0
11209	0.1	1,097.2	26528	99.9*	307.3

612

613 a. Pipes with the highest average unit headloss and energy lost to friction (*ELTF*) in the *ensemble* of 1,183
614 pipes in System #2 were sorted by annual frictional energy loss in descending order.

615 b. Pipes with the highest average unit headloss and energy lost to friction (*ELTF*) in the *ensemble* of 21,156
616 pipes in System #3 were sorted by annual frictional energy loss in descending order.

617 c. Average unit headloss was calculated by taking the arithmetic average of hourly values of unit headloss in a
618 pipe over the 24-hour diurnal period.

619 d. Annual frictional energy loss was calculated by multiplying the frictional energy loss in a pipe over the 24-
620 hour diurnal period and multiplying this daily energy use by 365 days.

621 e. Energy lost to friction (*ELTF*) was calculated by taking the arithmetic average of hourly values of *ELTF* in a
622 pipe over the 24-hour diurnal period.

623 f. Numerical values of *ELTF* were truncated to the tenth of a percent in the table.

624
625

626 Table 4.
627

Pipe ID ^a	Average Pressure Head (m) ^b	Annual Energy Lost to Leakage (MWh) ^g	Pipe ID ^a	Metric (Percent)	Annual Energy Lost to Leakage (MWh) ^g
Metric: <i>ENU</i> ^{c,d}					
14509	94.3	10.5	6873	123.0	17.5
14510	91.9	10.3	3443	123.4	15.8
P1379	163.1	7.3	19728	122.4	8.3
10942	92.3	6.3	19729	122.8	7.7
26572	98.8	5.3	6882	123.1	7.5
Metric: <i>ELTL</i> ^{e,f}					
14509	133.4	10.5	9540	99.0	52.2
14510	130.0	10.3	11538	97.4	15.5
19729	124.3	7.7	5898	97.8	15.2
10942	130.5	6.3	P423	99.5	11.1
19732	125.6	6.1	5877	100.0	10.2

628 a. Pipes with the highest average pressure head in the *ensemble* of 21,156 pipes in System #3 were sorted by
629 annual energy lost to leakage in descending order.

630 b. Average pressure head was calculated by taking the arithmetic average of hourly pressure head values in the
631 upstream and downstream nodes of a pipe over the 24-hour diurnal period.

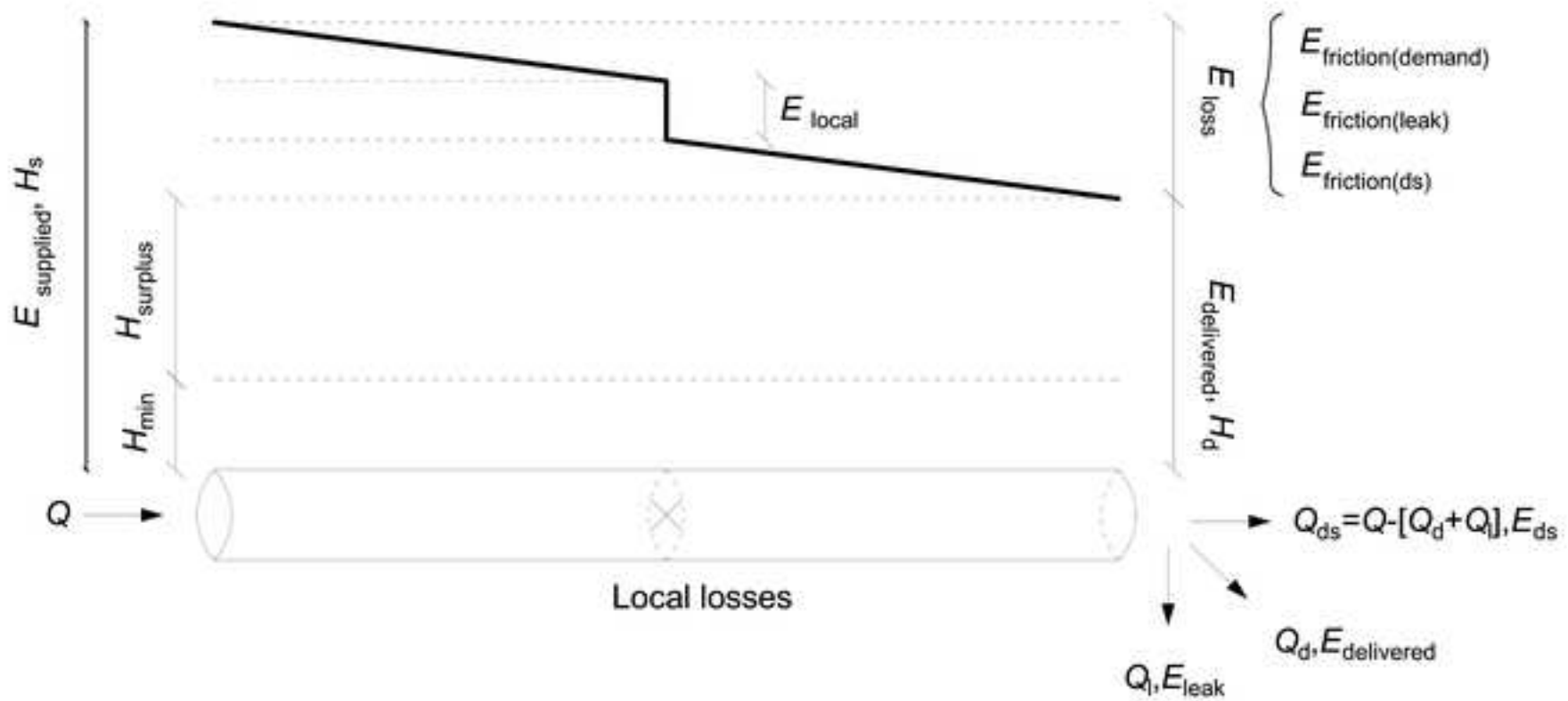
632 c. Energy needed by user (*ENU*) was calculated by taking the arithmetic average of hourly *ENU* values in a
633 pipe over the 24-hour diurnal period.

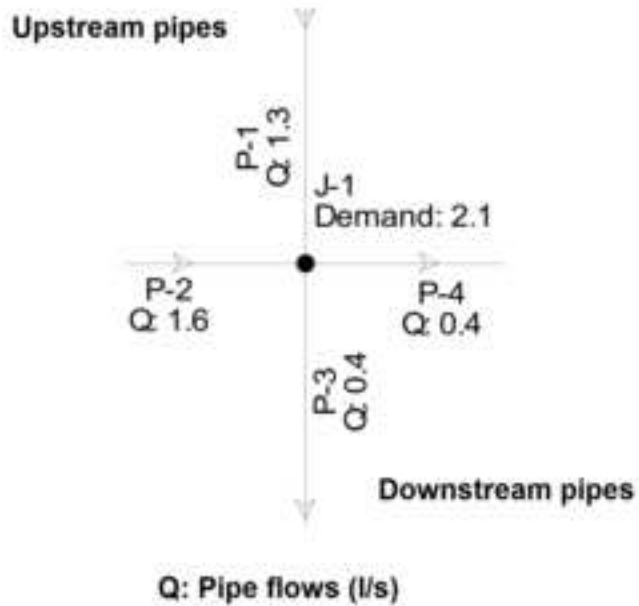
634 d. Pipes with the highest energy needed by user (*ENU*) in the *ensemble* of 21,156 pipes in System #3 were
635 sorted by annual energy lost to leakage in descending order.

636 e. Energy lost to leakage (*ELTL*) was calculated by taking the arithmetic average of hourly *ELTL* values in a
637 pipe over the 24-hour diurnal period.

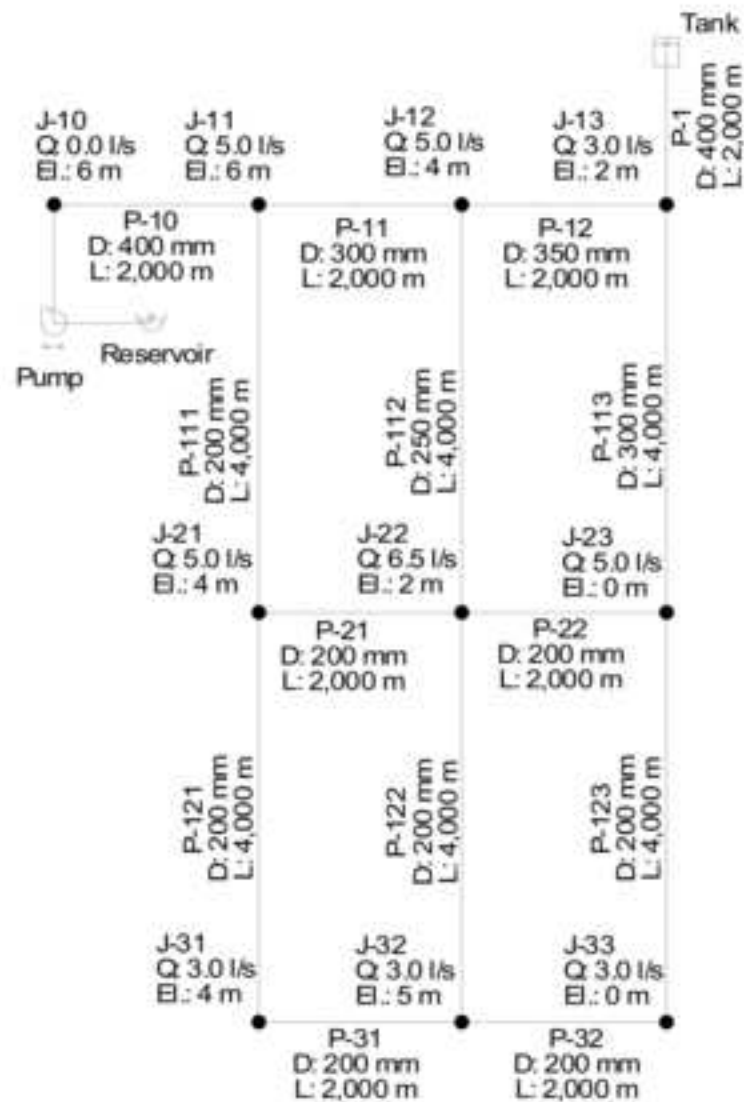
638 f. Pipes with the highest energy lost to leakage (*ELTL*) in the *ensemble* of 21,156 pipes in System #3 were
639 sorted by annual energy lost to leakage in descending order.

640 g. Annual energy lost to leakage was calculated by multiplying the leak energy (E_{leak} indicated in Table 1) at
641 the downstream node of a pipe over the 24-hour diurnal period and multiplying this daily energy use by 365
642 days.





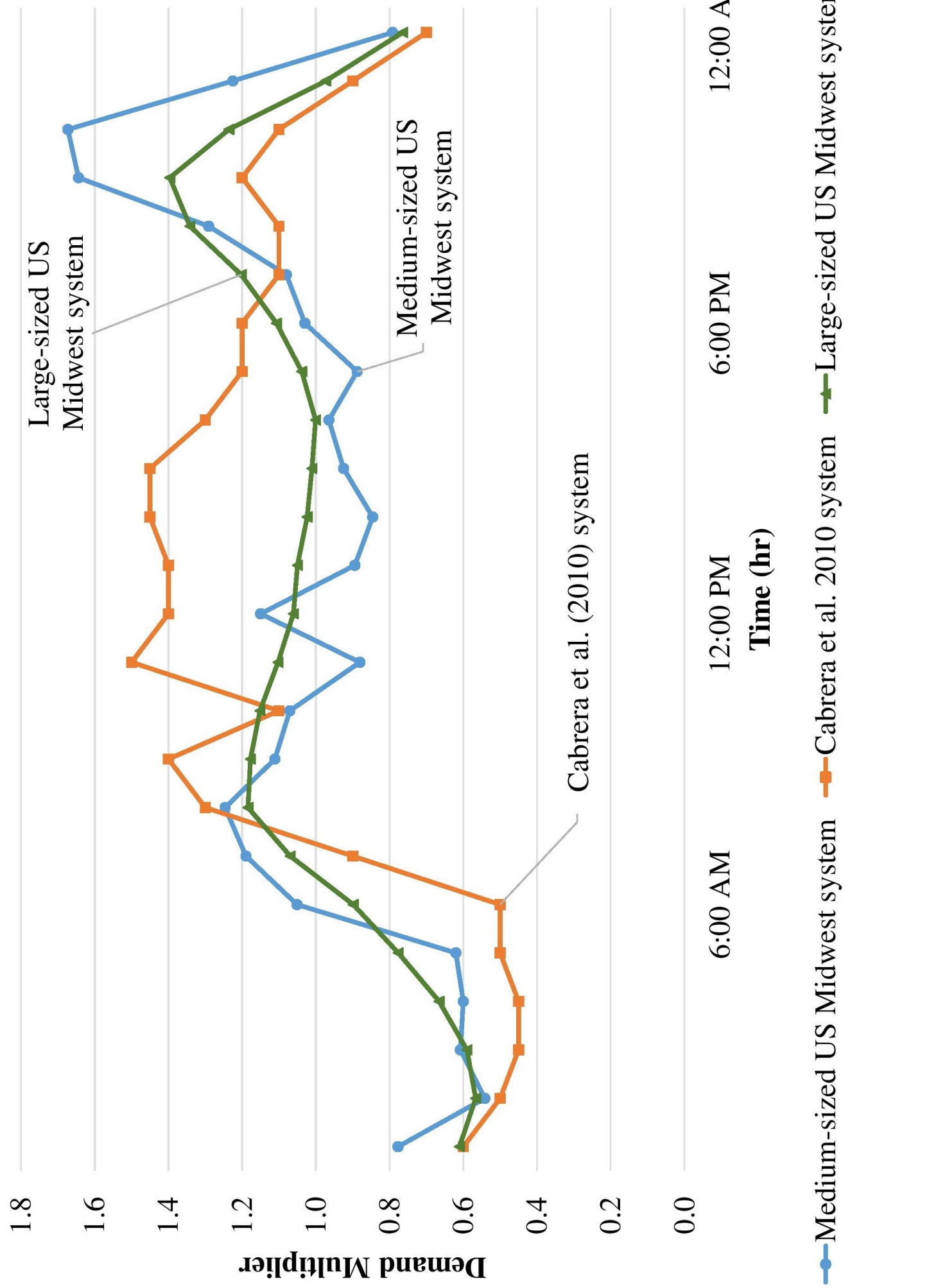
(a)



D: Pipe diameter (mm)
 L: Pipe length (m)
 El: Node elevation (m)
 Q: Nodal base demand (l/s)

(b)

Figure 3



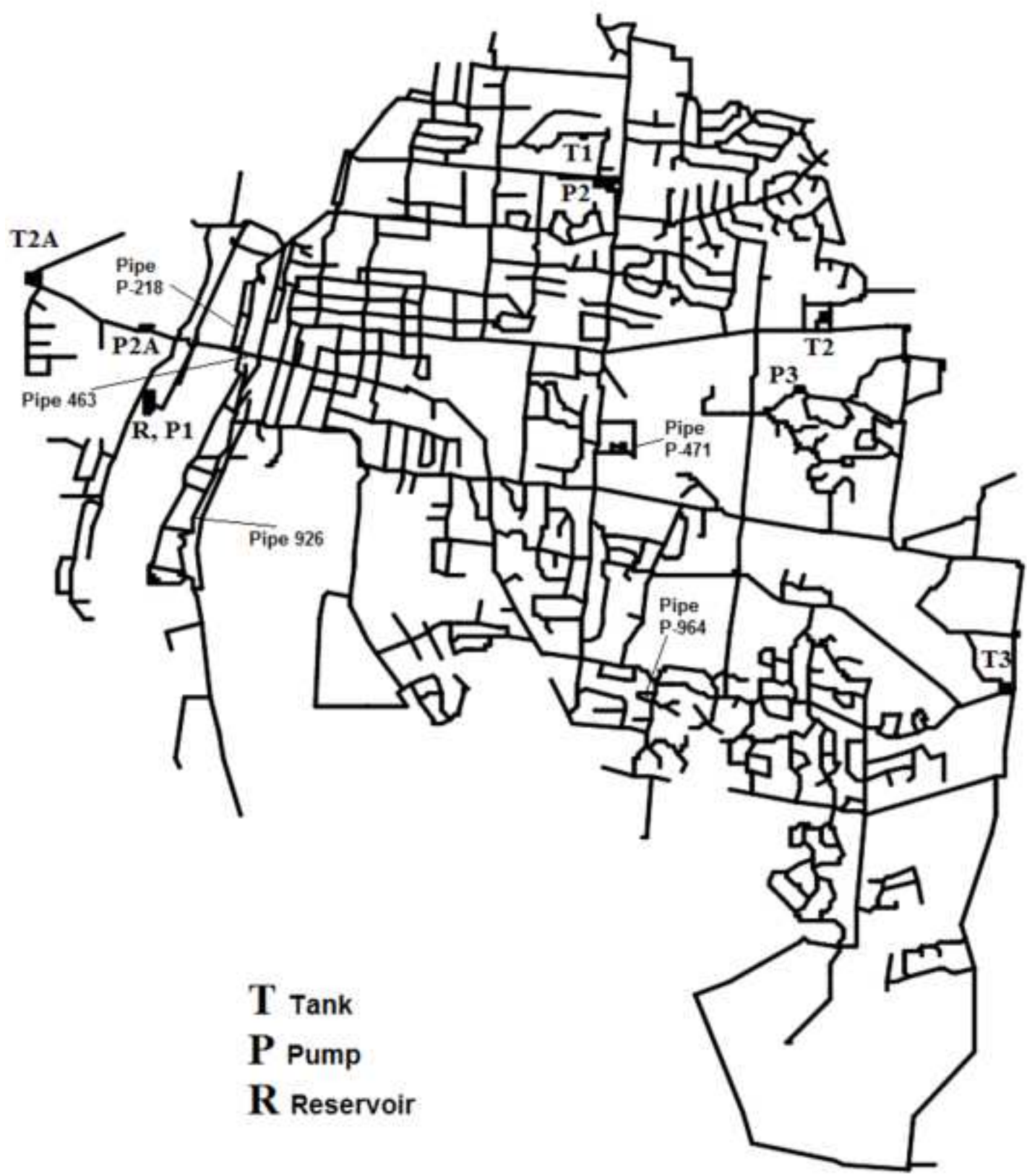
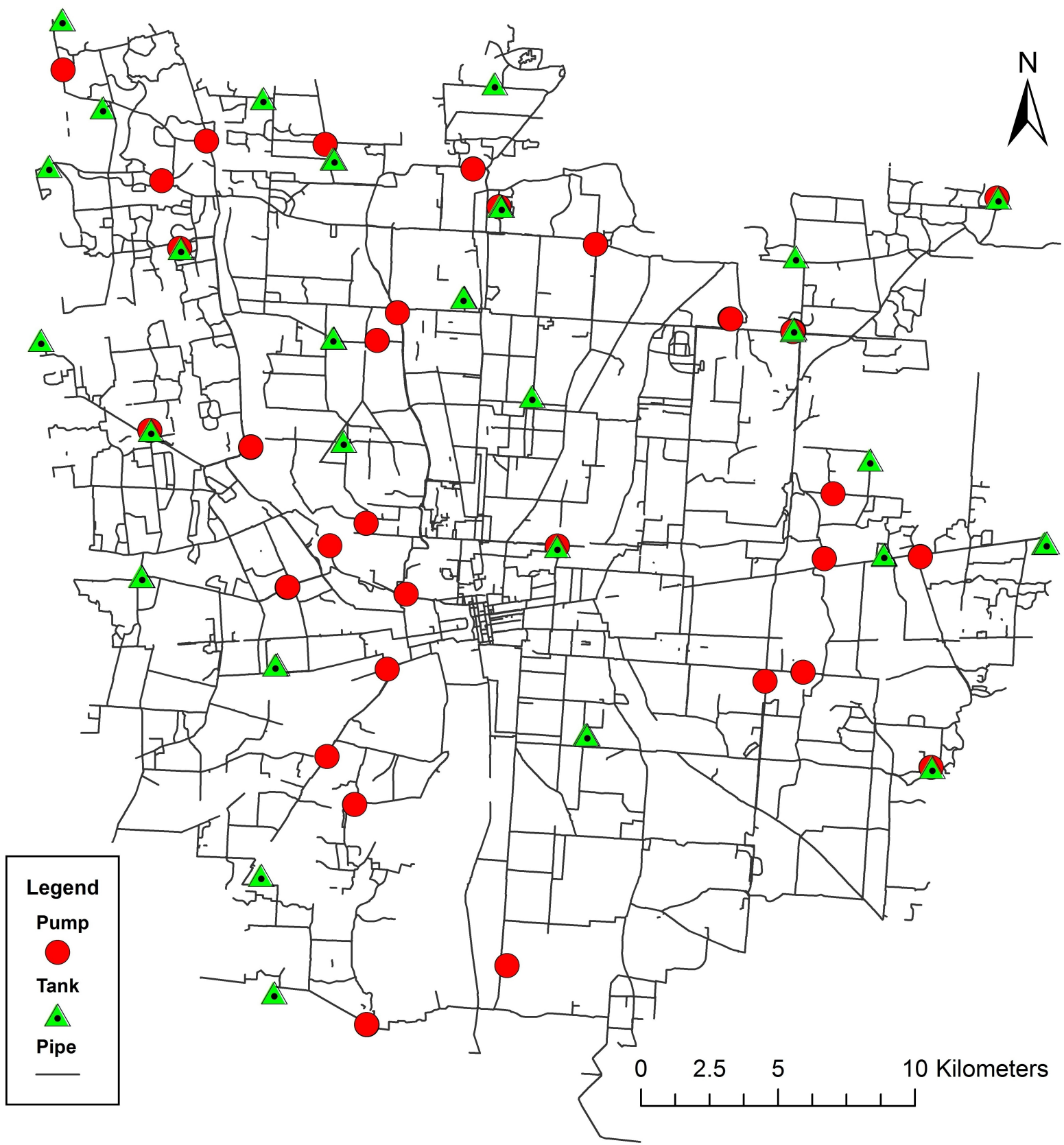
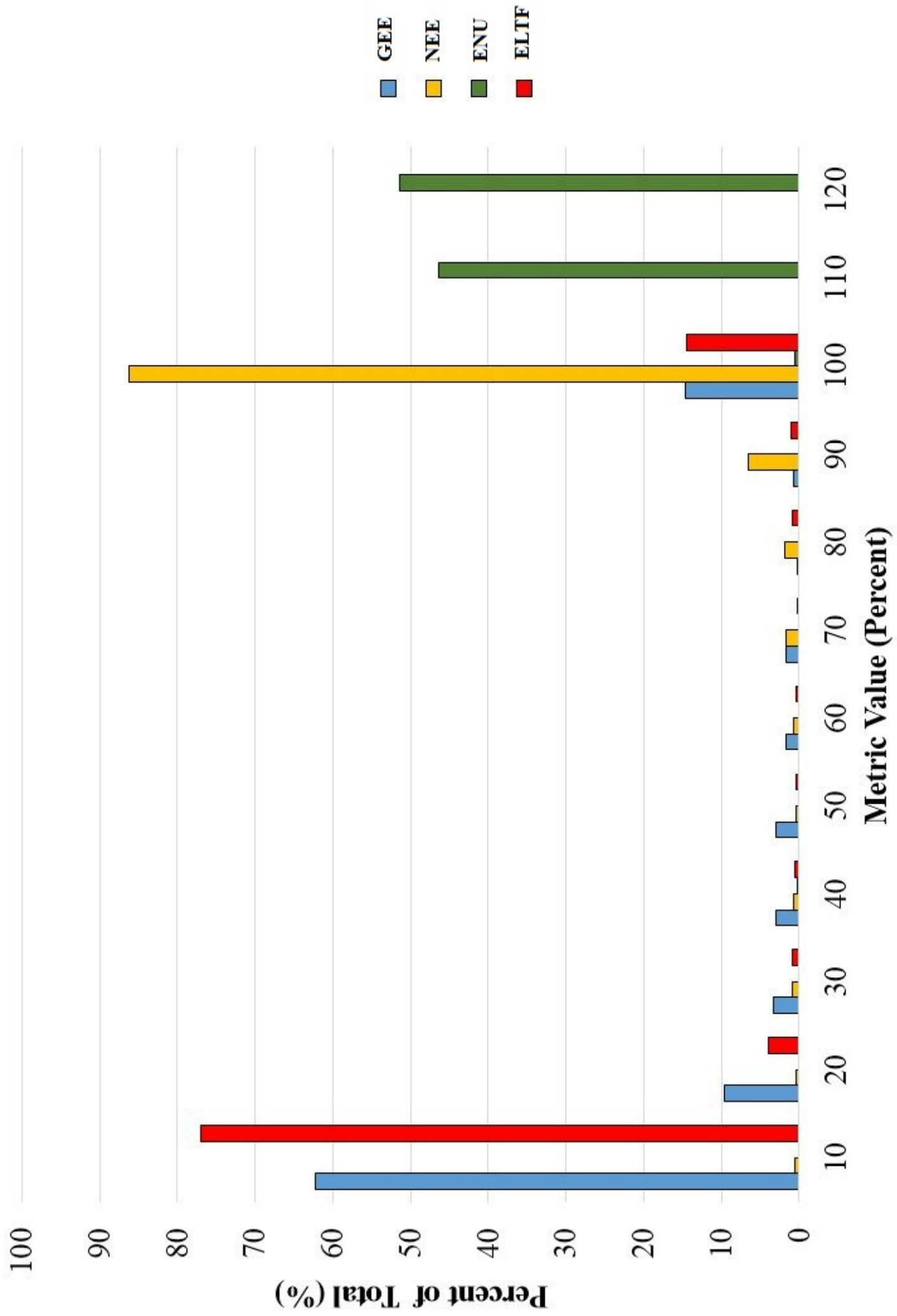
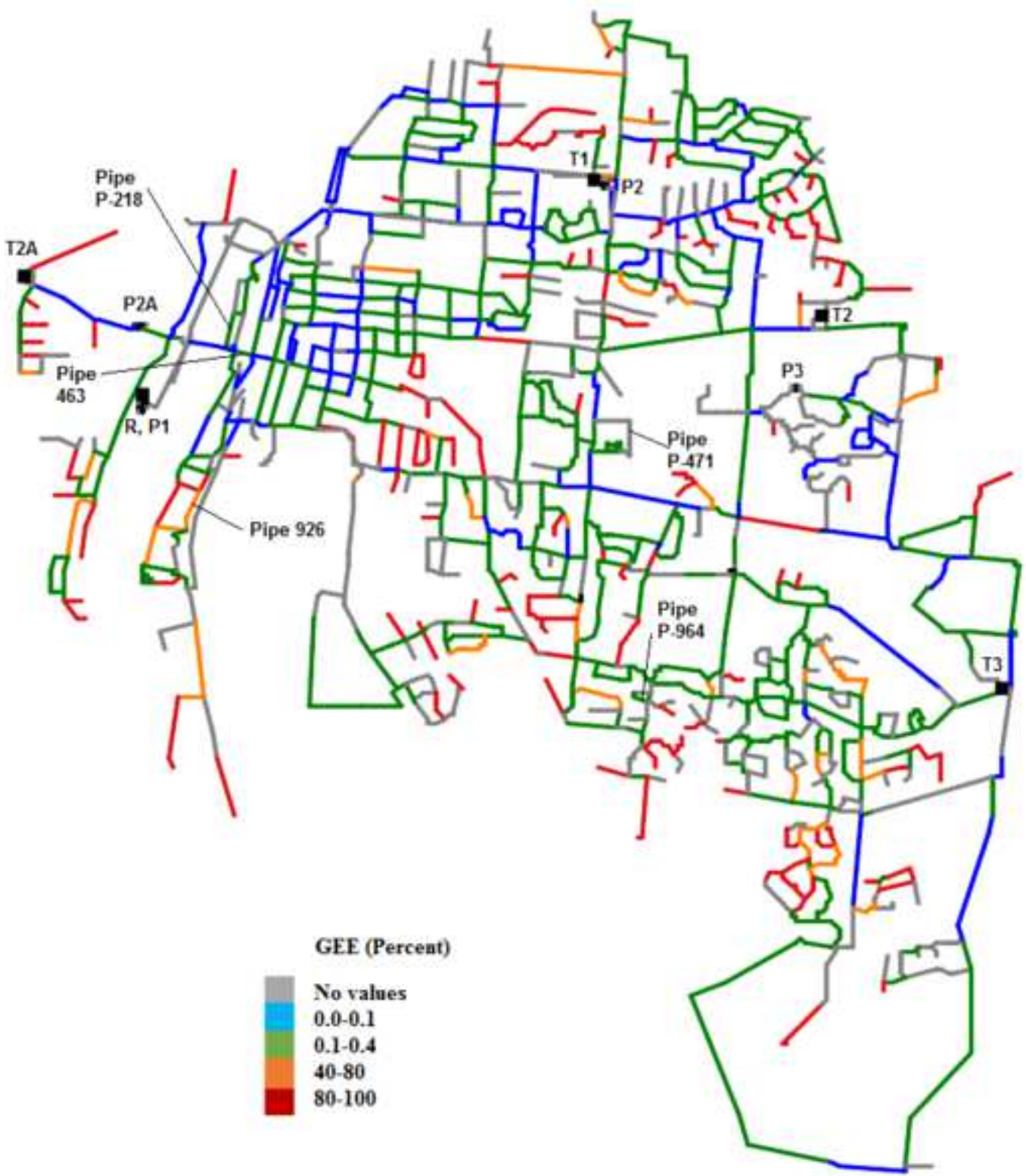


Figure 4b







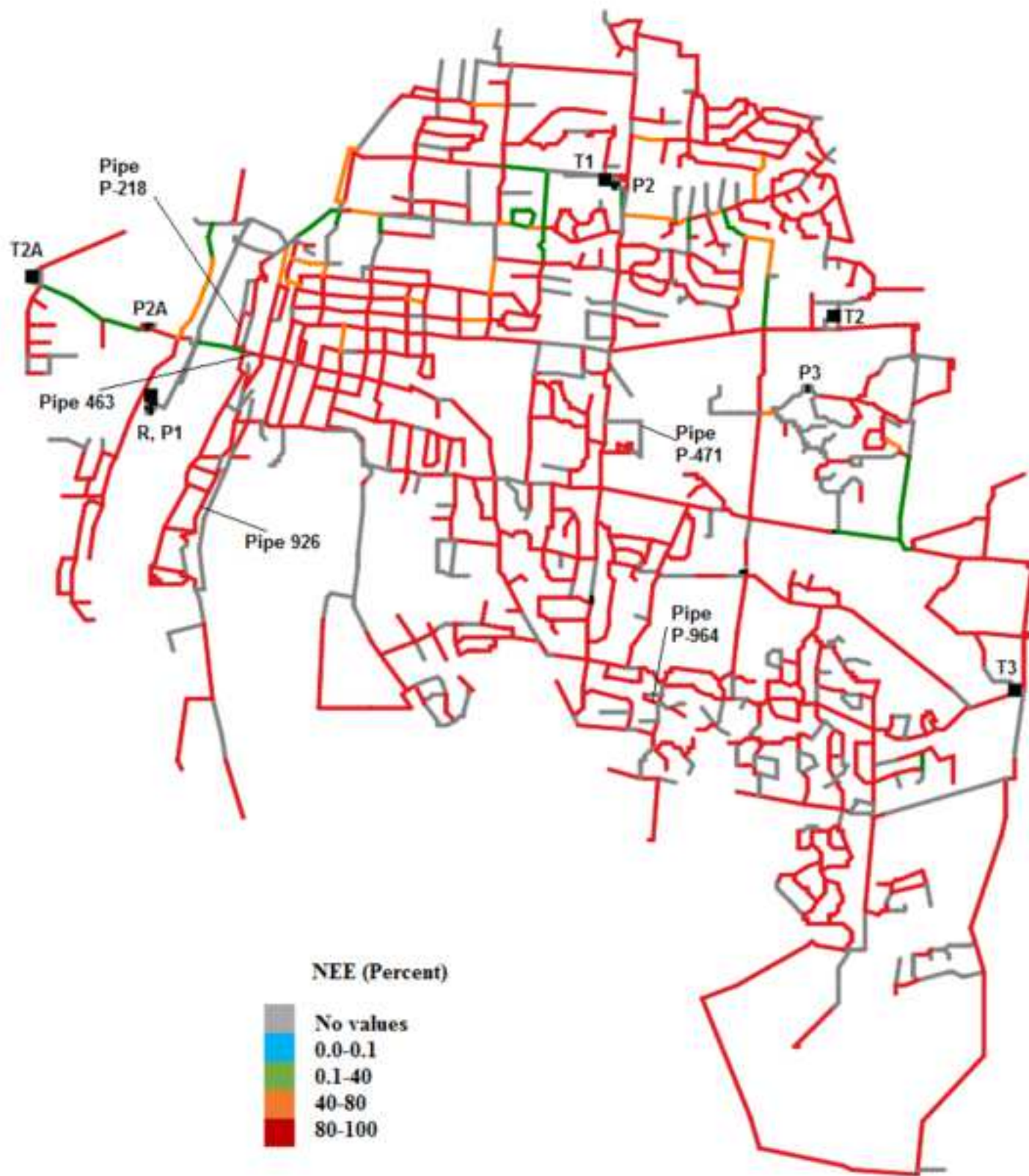


Figure 7

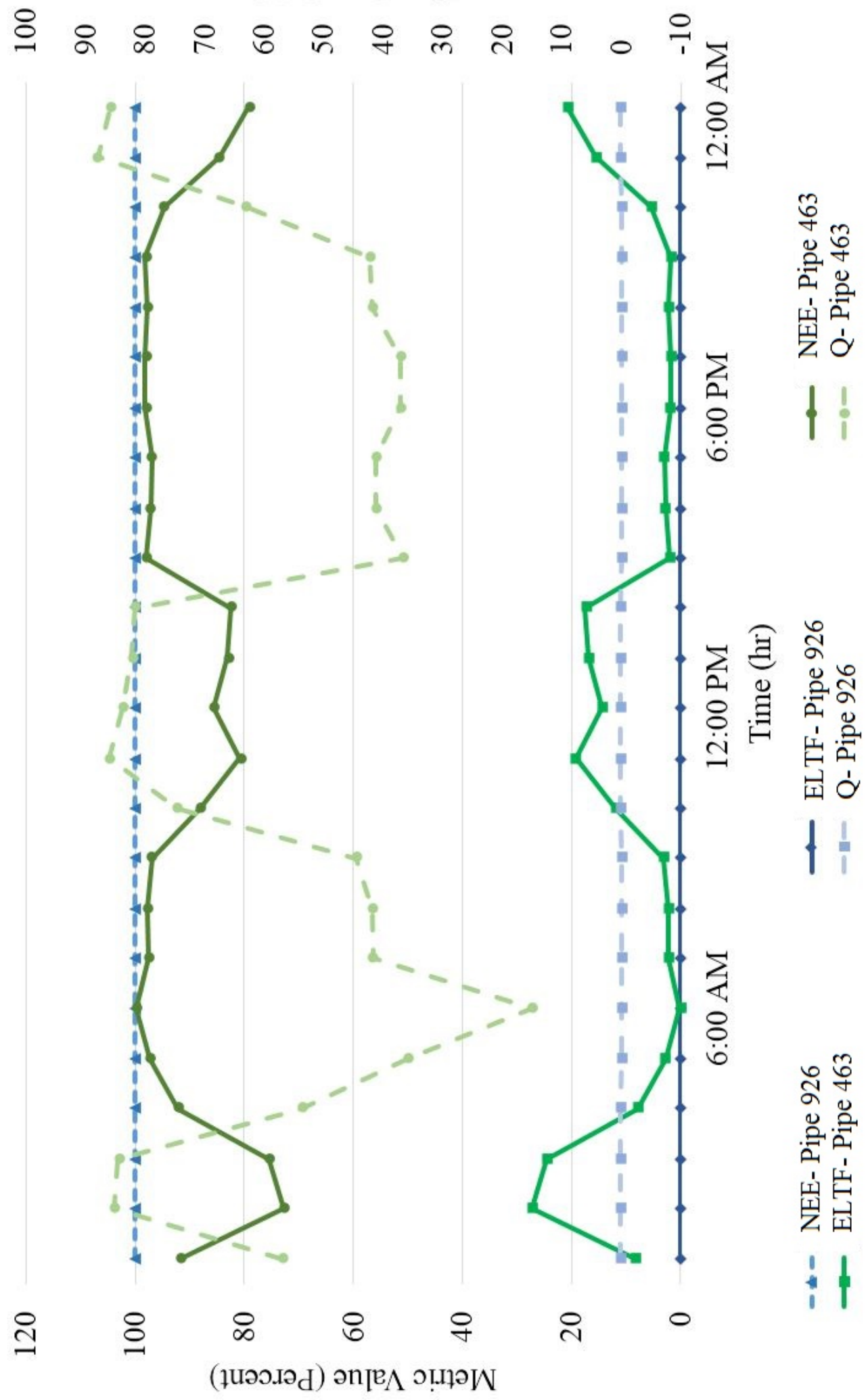
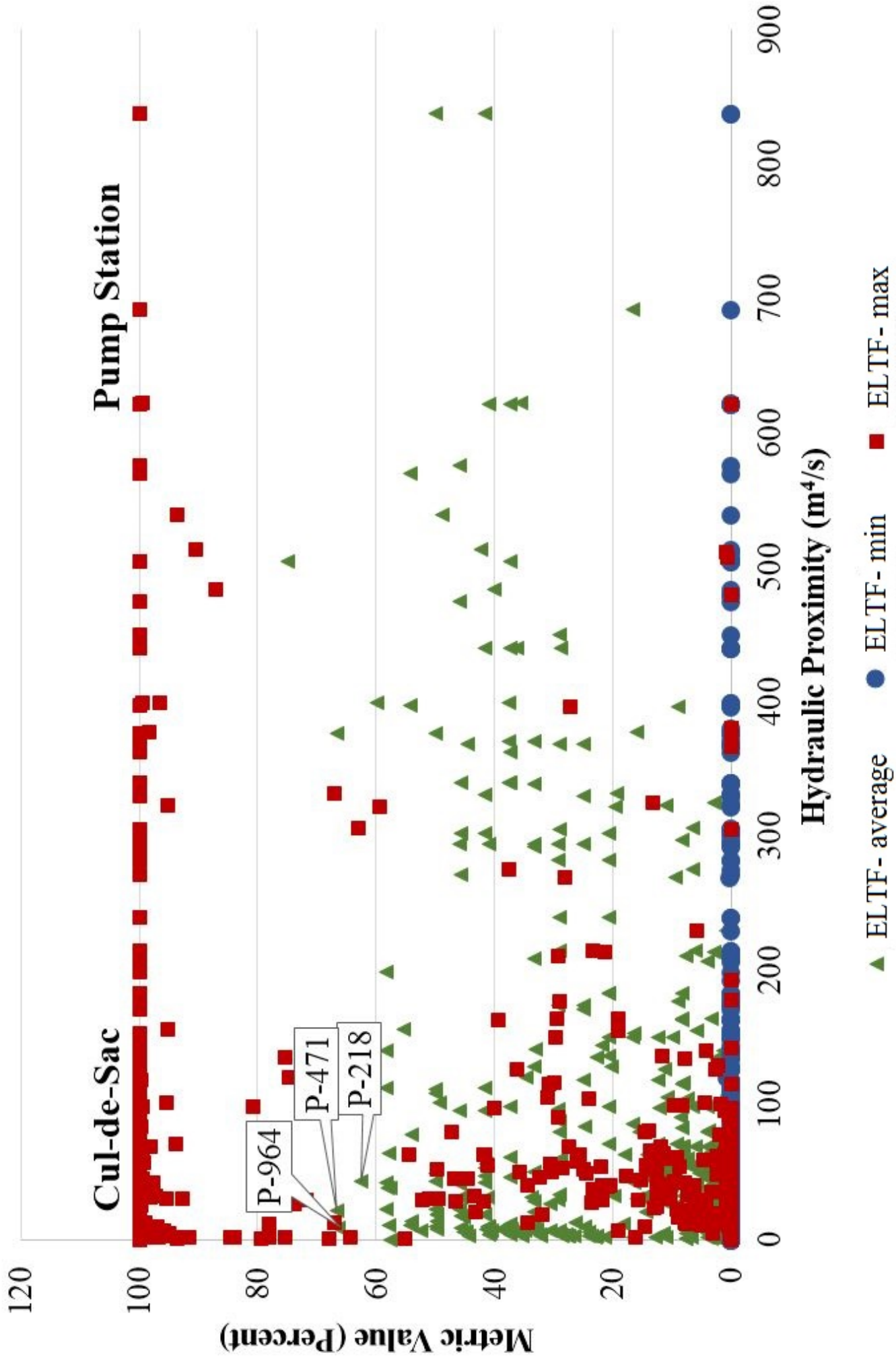
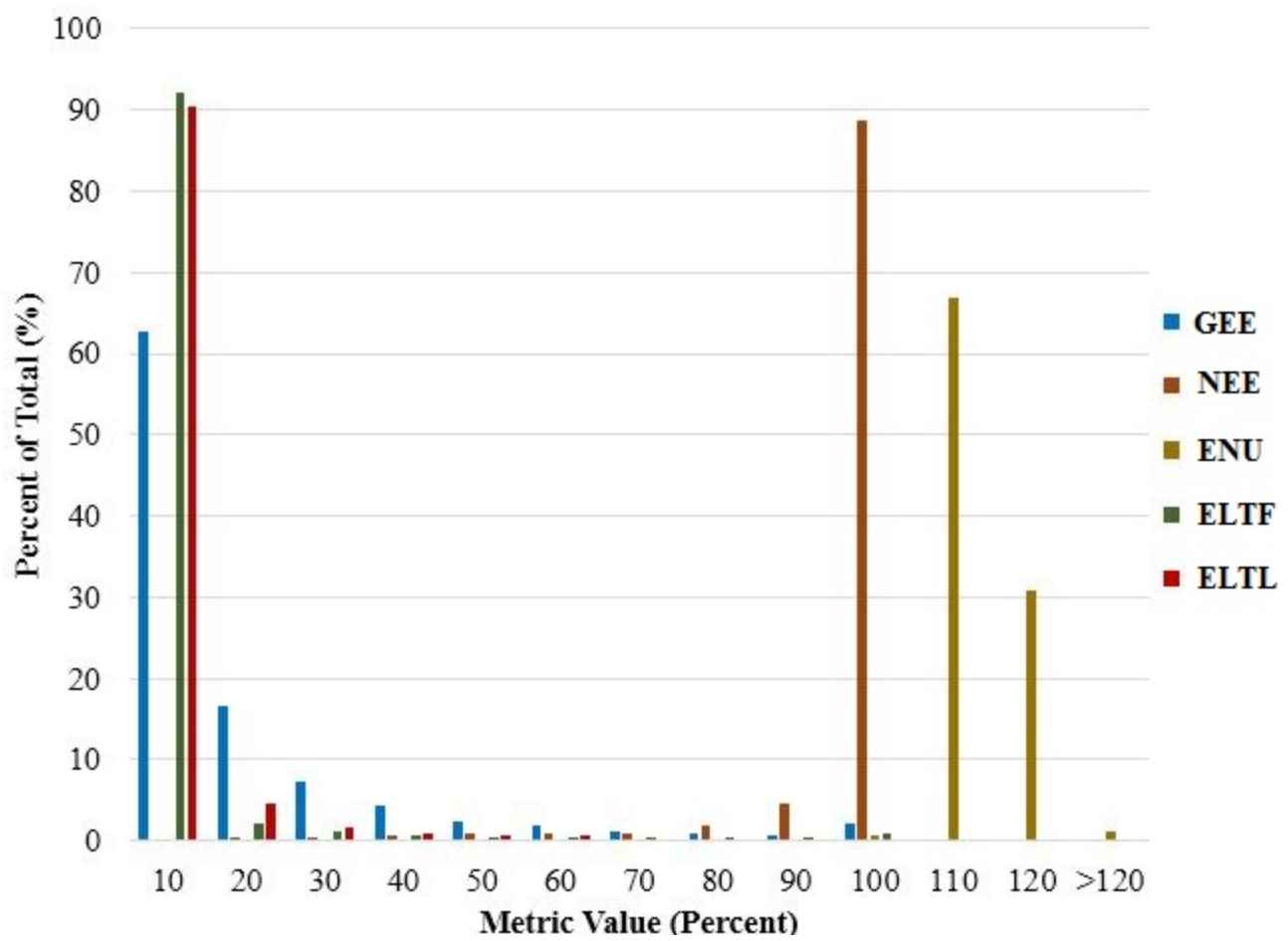


Figure 8





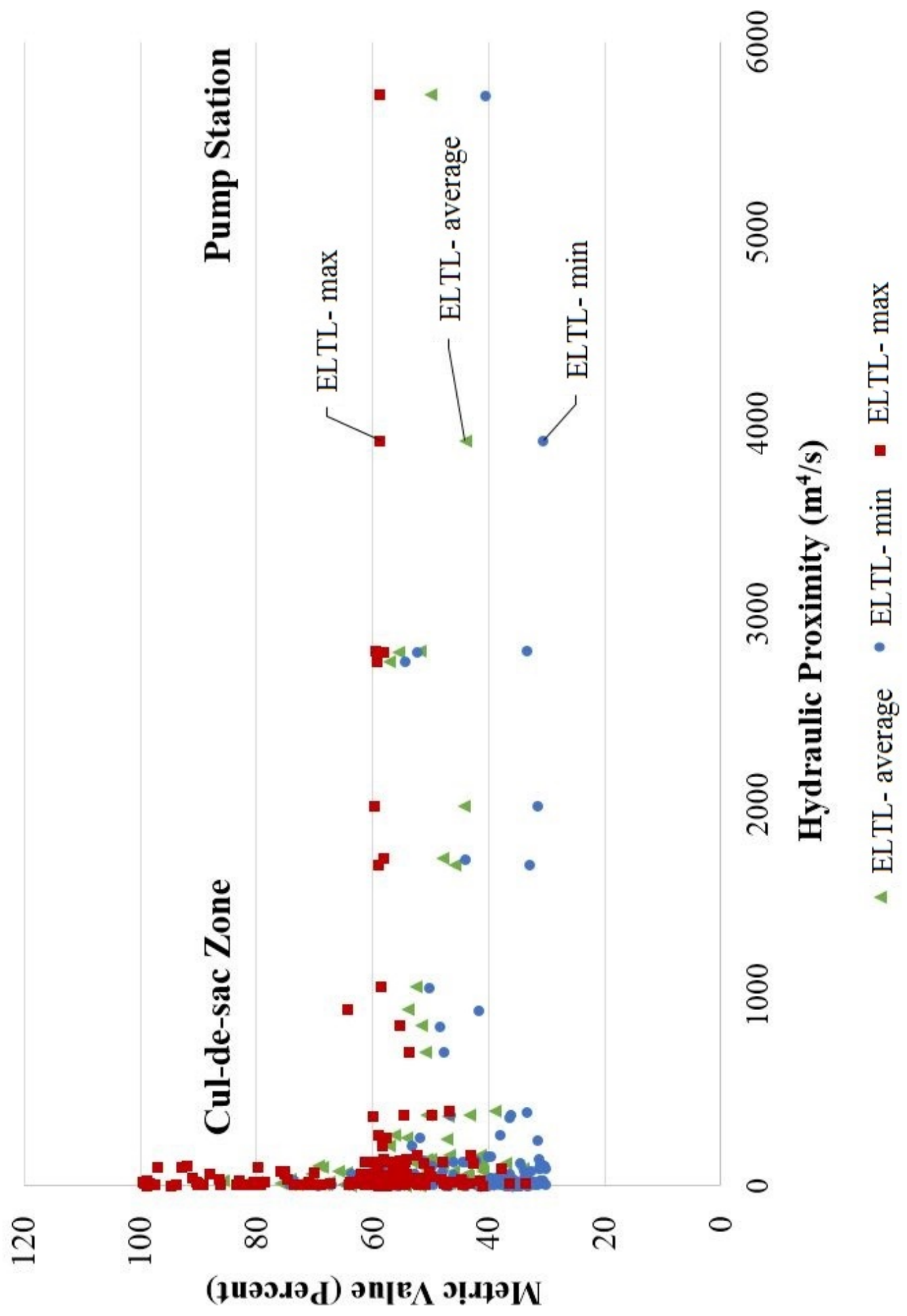


Figure 1. Hydraulic grade line and energy inputs and outputs in a pipe.

Figure 2. a) Example calculation of energy delivered at a model node connected to upstream and downstream pipes; b) model layout of System #1 (reported in Cabrera et al. (2010)) (L = pipe length; D = pipe diameter; P-10 = pipe ID; J-10 = node/junction ID; Q = pipe flow; $El.$ = node elevation).

Figure 3. Diurnal demand pattern for Systems #1 through #3 (24-hour period).

Figure 4. a) Model layout of System #2 (medium-sized US Midwest); b) model layout of System #3 (large-sized US Midwest).

Figure 5. Histogram that indicates the percentage of pipes with numerical values of gross energy efficiency (GEE), net energy efficiency (NEE), energy needed by the users (ENU) and energy lost to friction ($ELTF$) in System #2 (medium-sized US Midwest) for the baseline scenario.

Figure 6. a) Numerical values of gross energy efficiency (GEE) and (b) net energy efficiency (NEE) in pipes of System #2 (medium-sized US Midwest) for the baseline scenario.

Figure 7. Hourly values of net energy efficiency (NEE) and energy lost to friction ($ELTF$) in Pipe 463 (near pump station P1) and Pipe 926 (located further away from pump station P1) over the 24-hour diurnal period in System #2 for the baseline scenario. (Flow in Pipes 463 and 926 are also indicated.)

Figure 8. Energy lost to friction ($ELTF$) (as calculated in Eq. 6) and max/min values of energy lost to friction observed over the 24-hour diurnal period ($ELTF$ -max, $ELTF$ -min) versus proximity to a pump or tank component in System #2 (medium-sized US Midwest) for the baseline scenario.

Figure 9. Histogram that indicates the percentage of pipes with numerical values of gross energy efficiency (GEE), net energy efficiency (NEE), energy needed by users (ENU), energy lost to friction ($ELTF$), and energy lost to leakage ($ELTL$) in System #3 (large-sized US Midwest) for the baseline scenario.

Figure 10. Energy lost to leakage ($ELTL$) (as calculated in Eq. 7) and max/min values of energy lost to leakage observed over the 24-hour diurnal period ($ELTL$ -max, $ELTL$ -min) versus proximity to a pump or tank in System #3 (large-sized US Midwest) for the baseline scenario.