

# Scale-free topology optimization for software-defined wireless sensor networks: A cyber-physical system

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Ru Huang<sup>1</sup>, Xiaoli Chu<sup>1,2</sup>, Jie Zhang<sup>1,2</sup> and Yu Hen Hu<sup>3</sup>

## Abstract

Due to the limited resource and vulnerability in wireless sensor networks, maximizing the network lifetime and improving network survivability have become the top priority problem in network topology optimization. This article presents a wireless sensor networks topology optimization model based on complex network theory and cyber-physical systems using software-defined wireless sensor network architecture. The multiple-factor-driven virtual force field and network division-oriented particle swarm algorithm are introduced into the deployment strategy of super-node for the implementation in wireless sensor networks topology initialization, which help to rationally allocate heterogeneous network resources and balance the energy consumption in wireless sensor networks. Furthermore, the preferential attachment scheme guided by corresponding priority of crucial sensors is added into scale-free structure for optimization in topology evolution process and for protection of vulnerable nodes in wireless sensor networks. Software-defined wireless sensor network-based functional architecture is adopted to optimize the network evolution rules and algorithm parameters using information cognition and flow-table configure mode. The theoretical analysis and experimental results demonstrate that the proposed wireless sensor networks topology optimization model possesses both the small-world effect and the scale-free property, which can contribute to extend the lifetime of wireless sensor networks with energy efficiency and improve the robustness of wireless sensor networks with structure invulnerability.

## Keywords

Software-defined wireless sensor network, scale-free network, topological optimization, super-nodes, cyber-physical systems

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## Introduction

Wireless sensor networks (WSN)<sup>1</sup> is a major component in cyber-physical systems (CPS),<sup>2</sup> which showing powerful potentials in interfacing with the physical world and making its control much easier, achieved by the integrations of network, computation, and communication capabilities to the components of physical world. Interacted heterogeneous physical devices (e.g. sensor and actuator) are key physical elements in CPS.<sup>3,4</sup> The heterogeneities reflect the diversity in capabilities, complexities, types, and mobility among sensors in CPS. It is crucial for CPS to support the ability of heterogeneity tolerance.

From the perspective of network functional architecture, most current traditional network topology

<sup>1</sup>School of Information Science and Engineering, East China University of Science and Technology, Shanghai, China

<sup>2</sup>Department of Electronic and Electrical Engineering, The University of Sheffield, Sheffield, UK

<sup>3</sup>Department of Electrical & Computer Engineering, University of Wisconsin-Madison, Madison, WI, USA

### Corresponding author:

Ru Huang, School of Information Science and Engineering, East China University of Science and Technology, Shanghai 200237, China.  
Email: huangrabbitt@ecust.edu.cn



optimization researches limited to non-software-defined network architecture are based on distributed algorithms, which result in the generation of a large quantity of network loads, reduction of life cycle, and lack of adaptability in the network evolution due to dynamic topology changes. Traditional network architecture does not support the dynamistic, scalability and heterogeneity in WSN cyber system and is lack of the feedback control functional component, which can efficiently exert impact on WSN physical system. Software-defined wireless networks (SDWNs) architecture<sup>5,6</sup> presents an innovative framework for decoupling the original closed system, which can achieve novel feedback control in CPS with logical centralized control and physical distributed control to decouple control plane and data plane. The combination of SDWNs-based architecture and WSNs' function, that is, software-defined wireless sensor network (SDWSN) based on programmable control of common hardware and software, enables flexible task configuration. Motivated by the advantages in SDWSN technology, we propose a SDWSN-based cyber-physical system framework (SD-CPSF) via introducing the software-defined network technology and actuator-based functional component into existing WSN infrastructure.

Based on SD-CPSF, the functionality, reliability, adaptability, compatibility, and autonomy can be efficiently improved in WSN. Sensors in WSN with limited energy supply always deploy in harsh environment to achieve the classical application of CPS. Consequently, sensors often suffer from fail due to natural hazards and energy resource depletion. The breakdown of some sensors can greatly damage the functionality of WSN. It is crucial for WSN to improve the ability of fault tolerance.

Network topology structure has intrinsic characteristics, which can impact on WSN's performance. Therefore, build robust network topology to improve the survivability and energy efficiency of WSN is crucial.

Network robustness has become one of the most central topics in the complex network research.<sup>7</sup> Fault tolerance is well known as the typical scale-free network properties,<sup>8</sup> which can help to defend against random failure caused by energy depletion and environmental disturbances in CPS application. Complex network theories<sup>9</sup> provide new research ideas and methods to establish a reliable and energy-efficient network topology model by exploring the statistical properties inherited in networks.

Comprehensively considering the characteristic of node heterogeneity, resource scarcity, and structure vulnerability in WSN, we propose a novel WSNs topology optimization model according to scale-free complex network theory-based network evolution algorithm and SD-CPSF-based network functional architecture. We take the improvement of robustness of WSN as the

design goal for WSN topology optimization, which help to prolong network lifetime and enhance the network invulnerability.

The contributions of our researches in the article mainly focuses on the improvement on adaptive ability, invulnerability, and energy efficiency on WSN, via introducing SDWN architecture and complex network theory (scale-free and small-world theory) based strategies in topology optimization and evolution mechanism.

The rest of the article is organized as follows. Section "Related work" states a summary of related work on network topology control. Section "System model and functional framework" elaborates the system model based on cognitive SDWSN prototype and its functional architecture. Section "Topology initialization based on super-nodes configuration" presents an implementation of topology initialization. In section "Topology evolution based on improved scale-free network model," an optimal topology evolution model is proposed based on improved scale-free theory model and specific mathematical analysis on proposed evolution model is presented. Network structure characteristics are evaluated through experiments in comparison with BA model<sup>10</sup> in section "Experimental results and analysis." Finally, conclusion is drawn in section "Conclusion."

## Related work

In the last decades, sufficient efforts have been devoted to design vulnerability-tolerant and energy-efficient topology construction mechanism in WSN. Wang et al.<sup>11</sup> adjusted the structure of scale-free network via optimizing the entropy distribution to enhance the anti-attack capability of scale-free network. However, the topology model did not take into account the problem of imbalanced energy consumption and finally reduced the network life cycle. In Sun et al.,<sup>12</sup> the survivability was improved when building a WSNs topology by controlling network node's saturation and residual energy. However, sensors with high load in networks were prematurely dead due to excessive energy consumption, and the network life cycle would be shortened. The research<sup>13</sup> was proposed to make the network tend to be more in sync by optimizing the network topology symmetry, which focused more on network model synchronization and lack of utilizing other statistical characteristics in WSNs revealed by the complex network theory. The literature<sup>10</sup> proposed a new topology of network evolutionary model based on BA scale-free network, which was with high robustness on random failures of node. However, clustering coefficient value keeps small while the average path length remains relatively large in proposed model, which lack of energy efficiency. In the literature study,<sup>14</sup> WSNs topology was optimized using conceptual cluster feature and

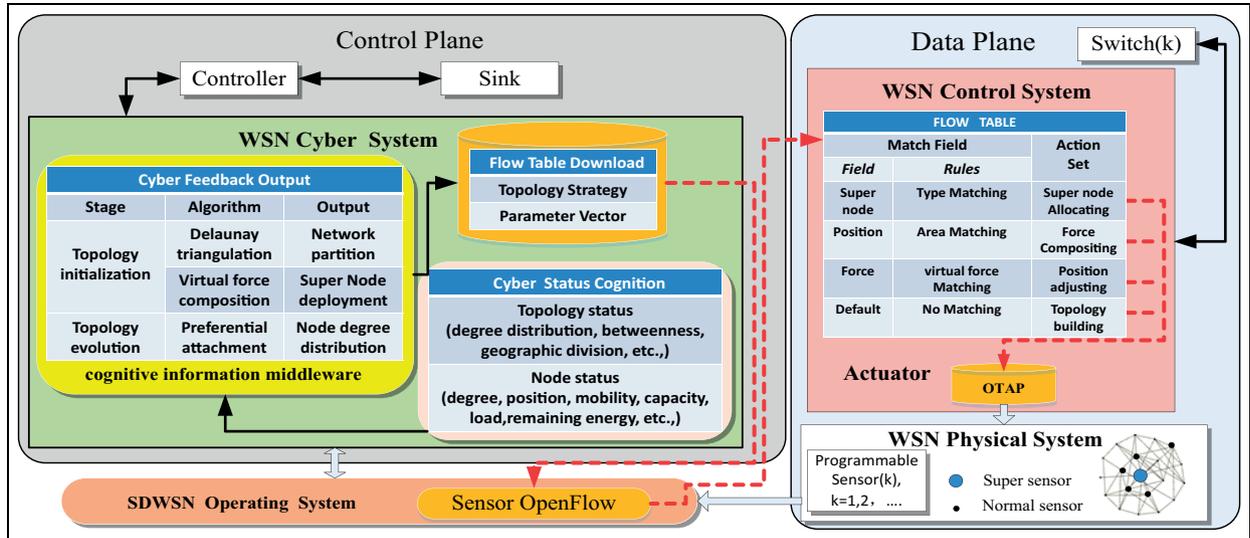


Figure 1. Software-defined network-based CPS framework for WSN topology optimization.

edge betweenness in small-world model via introducing special threshold mechanism, so as to equip with a high clustering coefficient and obvious cluster structure after network optimization, but this work took little change on average path length.

Based on the complex networks theory, a new weighted local WSNs evolution model<sup>15</sup> was designed to deduce intensity distribution and weight distribution meeting the power-law; however, the dynamic changes in network topology were not considered. In research works,<sup>11</sup> the impact of the residual energy on network growth was considered in process of complex network models evolution, but the invulnerability in network model was not analyzed. Jian et al.<sup>13</sup> proposed two scale-free network models based on local world model, where the new sensors with high energy level had the priority to be connected, but the dynamic changes in network topology due to the expense of limited resource were not taken into account.

The above researches based on complex network theory focus on the topology control methods to homogeneous and tight coupling network architecture; however, none of those methods have been designed from the viewpoint of network heterogeneity and network functional architecture in CPS.

## System model and functional framework

WSN is abstracted into a weighted directed graph,  $G(V, L, I)$ , which forms a reverse multicast tree rooted at Sink, which has non-replenished enough energy, higher storage capacity and stronger computing ability. In  $G$ ,  $V$  is the set of vertexes and maintains a hierarchical cluster. Sensors in  $V$  own heterogeneous functional characteristics (energy, perception radius, mobility,

computing, and storage capacity) are grouped into super and normal node types. Normal sensors without moving-ability in data plane are randomly distributed in environment monitoring area and have low average energy level, while super-nodes with moving-ability have several times the energy equivalent and communication radius as normal sensors.  $L$  consists of a set of wireless links and  $I$  is the set of vertex weights, which denote the diversity for crucial level of sensors in  $V$ . SDWSN applies decoupled network architecture and has the ability of heterogeneity tolerance. By introducing SD-CPSF into WSN, cyber feedback functions performed by actuators are added into WSN control system and the constituted elements in WSN physical system can be endowed with software defined networks based (SDN-based) functional characteristic. SD-CPSF-based system functional framework for WSN topology optimization is shown in Figure 1.

Cyber feedback and control process are illustrated as follows. Sensors in data plane gather the information on WSN physical system to the Sink entities, which can develop control algorithms based on WSN cyber system to produce strategy commands and instruct actuators to achieve the control on WSN physical system. The main idea of feedback control is to exploit cognitive information middleware (CIM) to reinforce learn the physical dynamics in WSN. Then, utilizing the output functional model determines the actions that yield the optimal topology control behaviors.

Based on SDN technology, Sink takes the role of controller to manage network services according to SDN protocol and develop topology optimization strategies based on WSN cyber system in control plane.

The core functionality module in the control plane of SD-CPSF is a CIM,<sup>16</sup> which performs knowledge-

guided reinforcement learning<sup>17</sup> for mining heterogeneous information in WSN cyber system. The following procedures should be executed after the cyber-learning phase has been finished in CIM. Controller outputs the strategy rules and optimal algorithm parameters constituted by vector form to the data plane using pipelined flow-table mode. Then, topology evolution process should be executed based on the optimized algorithm parameters (e.g. parameters of particle swarm and virtual force algorithm (VFA) calculated by CIM). Specifically, each switch, which is designed as software-defined virtual sensor and acts as actuator in data plane, performs the appropriate topology evolution matching rules (i.e. flow-table entries) and configures the sensors in data plane to realize the position optimization of super-node for network initial configurations and scale-free model optimization for network evolutionary.

Other sensors in data plane can be provided with programmable ability and become cluster members to execute the specific actions guided by controller strategies and transmitted by switches using Over-the-Air Programming (OTAP) technique.<sup>18</sup>

Total optimal topology generation process in logical field reflects the functionalities decoupling between control plane and data plane, where supported SDN protocol, Sensor OpenFlow,<sup>19</sup> enables the communication between the data plane and a remote controller (Sink). Correspondingly, the topology optimization process in temporal field is divided into two stages. First, in the cyber-learning phase, Sink takes the role of controller to collect the network status information based on the packet-in messages from the data plane and perform the configuring and scheduling in network resource (e.g. position adjustment for super-node, preferential attachment for edge) using particle swarm and VFA.

Topology building process reveals a tradeoff between resource efficiency and computational complexity, SDN-based design can yield very low complexity, which efficiently reduce the information exchange for topology optimization process over the cyber-world, which can effectively reduce energy consumption in the process of topology optimization and improve the re-configurability and scalability of network topology. The fundamental functionalities of proposed SD-CPSF reflect the interaction between physical world and cyber systems in WSN using SDN technology.

## Topology initialization based on super-nodes configuration

### Network division using particle swarm method

According to Delaunay triangulation,<sup>20</sup> which uses computational geometry to mathematically abstract

two-dimensional network region, we propose an optimal planar triangulation with geometric criteria to divide entire network with  $N$  sensors into  $a$  zones via particle swarm algorithm.<sup>21</sup> In each zone, super and normal sensors join the network in accordance with a certain proportion, and then, normal sensors are distributed around certain super-nodes, which form like a spider web-like structure according to initial topology generation algorithm.

At the first step, determining a first region division line network, the whole network is divided into two different sub-regions via zone dividing line determined by equation (1)

$$L_\theta = (x, y, \theta) \quad (1)$$

wherein the point  $(x, y)$  belongs to  $L_\theta$  and  $\theta$  denotes the angle between  $L_\theta$  and  $x$ -axis. Values of particle parameters  $x, y, \theta$  are randomly assigned.

Particle swarm optimization (PSO) is introduced in network division problem by iteratively improving candidate solutions with regard to given measure of quality. Fitness function in PSO can efficiently adjust plurality of different fitness values to determine the latest search results and corresponding particles used as global minimum plurality. The proposed fitness function in PSO is defined as mean squared error (MSE) form using norm  $\|R\|_{p\text{-norm}(p=2)}$

$$\begin{aligned} \text{fitness} &= \|(n_1 - f_1 N)^2 + (n_2 - f_2 N)^2\|_{2\text{-norm}} \\ \text{s.t. } f_i &= \frac{a_i}{a} \quad (i = 1, 2) \end{aligned} \quad (2)$$

where  $a_i$  is the expected number of super-nodes, which denotes the number of reserved super-nodes in corresponding divided zone and  $n_i (i = 1, 2)$  is the number of sensors belongs to corresponding zone  $i$ .  $N$  denotes the number of sensor nodes in entire WSN and  $a$  indicates the number of divided zones. Determining a plurality of different fitness values, a minimum fitness value is compared with the latest search results and the corresponding particles may be used as global minimum  $P_{gd}$ ; similarly, individual particle obtains the smallest extreme value  $p_{\lambda id}^t$  and then updates the algorithm parameters as equation (3) to get the optimal non-inferiority solution set.

$$\begin{aligned} v_{\lambda id}^{t+1} &= w_t * v_{\lambda id}^t + c_1 * r_1 * (p_{\lambda id}^t - X_{\lambda id}^t) + c_2 * r_2 * (P_{gd}^t - X_{\lambda id}^t) \\ \text{s.t. } X_{\lambda id}^{t+1} &= X_{\lambda id}^t + v_{\lambda id}^{t+1} \\ \lambda &= x, y, \theta \\ w_t &= \begin{cases} \frac{k_1 * (w_{\min} - w_{\max})}{M} * t + w_{\max}, & (0 < t < \frac{M}{k_1 + k_2}, k_1 > 0, k_2 > 0) \\ \frac{k_2 * (w_{\min} - w_{\max})}{M} * t + \frac{k_1 * w_{\max} + k_2 * w_{\min}}{k_1 + k_2}, & (0 < \frac{M}{k_1 + k_2} \leq t < M) \end{cases} \\ w_t &\in [w_{\min}, w_{\max}] \end{aligned} \quad (3)$$

where  $X_{id}$  and  $X_{yid}$  denote the position of the particles;  $X_{\theta id}$  is the dividing line inclination;  $v_{xid}$ ,  $v_{yid}$ ,  $v_{\theta id}$  represent the corresponding search speed in three dimensions  $x$ ,  $y$ ,  $\theta$ ;  $c_i$ ,  $i = 1, 2$  and  $w_t$  denote learning factor and inertia weight factor, respectively;  $r_1$  and  $r_2$  are random numbers in the range  $[0, 1]$ ; and  $t$  is the number of iterations. Since the standard PSO algorithm has disadvantages like premature convergence and slow evolution,<sup>22</sup> it is necessary to make appropriate adjustment on parameters in particle update formula to update local optimum and track global optimum in solution.

In equation (3),  $w_t$  is defined as the PSO inertia weight factor, which can be used to regulate global and local search capabilities in network division optimization by solving the premature convergence and slow evolution problem. Therefore, a self-adaptive learning method is proposed to take  $w_t$  linearly varies as the number of iterations  $t$  at different intervals, which enables  $w_t$  to maintain a larger value at preliminary search to improve the global search ability and to keep a smaller value at late search to improve the local search accuracy. The search process is terminated until the particles get the right value of  $x$ ,  $y$ , and  $\theta$  to find fitness function, which approximates zero. In this case, the entire area can be divided into two parts. After the first region segmented, two sub-regions continue to be segmented according to similar partition algorithm until  $a$  zones with equal size are produced.

Compared with classical topology segmentation in WSN,<sup>23</sup> the above program can make use of SDWSN architecture to achieve ‘‘coarse-grained’’ network segmentation step, which depends on the smaller number of network border switches and does not need to calculate the path information of the entire network, which helps to significantly reduce computational complexity and substantial reduction in information exchange between the control plane and switches in data plane.

### Virtual force-oriented deployment of super-nodes

VFA<sup>24</sup> abstracts the mobile sensors into virtual charged particles to simulate distance-threshold-based virtual compositional force. Motivated by the principle of VFA, the multiple factors driven virtual force are utilized to optimize the deployment of super-nodes in WSN physical system, which can promote the rational allocation of resources within WSN to reduce the topological fragility using percolation theory.

In the first step of VFA, super-nodes adjusts its location in adjacent sub-target zone based on composition force, which is constructed by  $F_{ni}$ ,  $F_{bj}$ , and  $F_{ji}$ . Specifically,  $F_{ni}$  denotes the force generated between super-nodes and normal sensors within the same zone  $\Phi$ ;  $F_{bj}$  indicates the impact of adjacent sub-region boundary set  $\varphi$  on super-nodes.  $F_{ji}$  represents the force

created by other members in super-nodes set  $\Omega$ . When the properties of force exhibit gravity or repulsion, corresponding virtual force will take a positive value or negative value, respectively.

Based on the above analyses, super sensor  $i$  is driven by virtual composition force shown as equation (4) to find out subinterval and continually adjust its deployment position in the sub-region until force  $F_i$  is less than a given threshold.

$$F_i = \left\| \sum_{n \in \Phi} F_{ni} + \sum_{b \in \varphi} F_{bi} + \sum_{j \in \Omega} F_{ji} \right\|_{p\text{-norm}}$$

$$s.t. F_{ni} = k_{ni} * \left( \frac{k_n * \psi_n}{E_n} \right), n \in \Phi \subset \mathbf{G}$$

$$F_{bi} = k_{bi} * |i_{addr} - D_b|, b \in \varphi \subset \mathbf{G}$$

$$F_{ji} = k_{ji} * (|i_{addr} - j_{addr}| - d_s), j \in \Omega \subset \mathbf{G}$$

$$i \in \Omega \subset \mathbf{G}$$
(4)

wherein  $F_{ni}$  indicates the impact level on virtual force caused by the interaction between super-nodes and normal sensors in zone  $\Phi$ .  $E_n$ ,  $k_n$ ,  $\psi_n$  represents the remaining energy level, node degree and node betweenness of sensor  $n \in \Phi$ , respectively. And  $\psi_n$  is defined as the number of shortcut paths across the sensor. The value of control parameter  $k_{ni}$  takes 1 when super sensor  $i \in \Phi$ ; otherwise, it takes 0.  $F_{bi}$  denotes the corresponding component virtual force produced by sub-region boundaries, which are generated by network partition algorithm (mentioned in section ‘‘Network division using particle swarm method’’), and reflects the relation between the initial super-nodes position and the corresponding sub-target zone boundary.  $|i_{addr} - D_b|$  represents the Euclidean distance between the location of super-node  $i$  and the centroid  $D_b$  of sub-region  $\varphi$ .  $k_{bi}$  is a gain coefficient parameter that indicates the relationship between the actual density and the expected density of sensors in adjacent sub-regions.

$F_{ji}$  represents the interaction force between two different super-nodes in  $\Omega$ , where  $|i_{addr} - j_{addr}|$  is the Euclidean distance between super-node  $i$  and  $j$ , and  $d_s$  is a fixed times of super-nodes’ communication radius.

The above deployment process performed by the position adjustment of super-nodes is intrinsically determined by reconfiguring redundant network resources (capacity, energy, load, etc.) to fragile physical elements (sensor or link) in WSN, which can improve the network survivability and energy efficiency according to complex network theory-based percolation process,<sup>25</sup> which can provide the ability of network to properly perform even when a fractional components and small-world effect, which shows a small average shortest path length and a large clustering coefficient in properties of network topology.

## Topology evolution based on improved scale-free network model

Based on SD-CPSF, a WSN topology optimal model (WTOM) according to complex theory is proposed via introducing super-nodes driven initial topology deployment and crucial-node associated topology evolution, which possesses both the small-world effect and the scale-free property.<sup>26</sup>

### WTOM generation algorithm

Suppose the network has originally deployed isolated  $m_0$  normal sensors and  $a_0$  super-nodes in each time step,  $m(m < m_0)$  sensors are newly added to networks according to a certain rule, wherein the new added sensor  $\nu$  with node degree  $m$  is probably a super-node with probability  $p$  or a normal node with probability  $(1 - p)$ . Super-nodes have the priority to connect newly added sensors with inherent advantages. Then, local world  $\Theta$  is constructed by the  $M(M \geq m)$  sensors, which are within the communication range and with the latest joining time. The newly added node  $\nu$  is connected with existing super-nodes in local world  $\Theta$  or normal node  $i$  in neighborhood  $O_\nu$ .

Comprehensively considering the influencing factors in network evolution, we define  $I_i$  as the integrated influence factor (see equation (5)) of sensor  $i$  in the process of network evolution. The greater the value of  $I_i$ , the large the probability of  $\prod(k_i)$  is obtained. Therefore, the preferential attachment probability will be greatly affected by the crucial level of selected sensor in network topology generation

$$I_i = f(E_i) * k_i * \psi_i * (1 + \beta_i), \quad I_i \in \mathbf{I} \quad (5)$$

$$s.t. \quad f(E_i) = n * E_i, (1 \leq n \leq 8)$$

wherein,  $f(E_i)$  denotes the remaining energy level of sensor  $i$ . when  $n = 1$ ,  $i$  is a normal node, otherwise, it becomes a super-node with  $n > 1$ .  $\psi$  denotes the node betweenness, which is defined as the number of shortest paths through sensor  $i$ . From the perspective of overall network structure,  $\psi_i$  is a measure of centrality in network and indicates node's critical level in the global network routing.  $k_i$  is the node degree of sensor  $i$ . Parameters  $\beta_i$  obeys (0-1) distribution and reflects the super-nodes-related influence on network evolution, if the newly added sensors connect existing super-nodes with high probability, then  $\beta_i \rightarrow 1$ , otherwise  $\beta_i \rightarrow 0$ .

The connection probability based on integrated influence factor is shown as follows

$$\prod(k_i) = \frac{I_i}{\sum_{j \in O_\nu} I_j} \quad (6)$$

$$s.t. \quad i, j \in (O_\nu \cup \Omega) \cap \Theta$$

$$I_i, I_j \in \mathbf{I}$$

### Algorithm 1. WTOM generation.

- 
- 1: Set the initial configuration of SD-WSN with size  $N$ ; //Initial setting
  - 2: Divide the network based on equation (1) to equation (3); // Network partition
  - 3: Deploy the super-nodes based on equation (4); //Super-nodes configuration
  - 4: while network size  $< N$  do
  - 5: Add new sensors into network according to equation (5) in each time step;
  - 6: Build the local world; //Network growth
  - 7: Choose preferential attachment based on equation (6); // Network evolution
  - 8: Repeat the evolution steps until the required network size is met;
  - 9: Output the WSN topology optimal model; //Topology optimization
  - 10: end while
- 

Network topology optimization mechanism is achieved by repeating the algorithm steps from 2 to 4 until the required network size is met and the corresponding evolutionary process can produce small-world effect, directly affecting the energy saving performance of CPS for monitoring application.

## Mathematical analysis on topology optimal model

Dynamic characteristics in scale-free network model can be analyzed based on continuous field theory.<sup>27</sup> Given the nature of continuous performance in proposed model WTOM, more detailed characteristics can be captured and predicted according to the degree distribution, which is denoted as time-varies and obtained via continuous approximation field method.

At each time step, the increment of node degree is in accordance with the following ratio

$$\frac{\partial k_i}{\partial t} = m \prod(k_i) = \frac{M}{m_0 + t} \frac{m^* I_i}{\sum_{j \in O_\nu} I_j}, \quad (M \geq m) \quad (7)$$

Initial boundary conditions of equation (6) are substituted as  $k_i(0) = m$ , and then, the solution of differential equation (7) can be obtained as follows

$$k_i(t) = m^* \left( \frac{m_0 + t}{m_0 + t_i} \right)^{\sum_{j \in O_\nu} I_j / M^* m^* I_i} \quad (8)$$

The average node degree in local world is shown as  $\sum_{j \in O_\nu} k_j = M \langle k \rangle$ , and when time meets the situation  $t \rightarrow +\infty$ , the average node degree is described as

$$\langle k \rangle = \frac{2m^* t}{t + m_0} \approx 2m \quad (9)$$

Time  $t$  obeys uniform distribution  $P(t_i) = 1/(m_0 + t)$ ; therefore, the distribution of node degree tends to equation (10), which follows power-law and displays scale-free phenomena in physical infrastructures

$$p(k) \approx Y * m^{Y-1} * k^{-Y}$$

$$s.t. \quad Y = \frac{2 * \sum_{j \in O_v} f(E_j) * \psi_j * (1 + \beta_j)}{M * f(E_i) * \psi_j * (1 + \beta_i)} + 1 \quad (10)$$

The probability of super-node chosen to construct network is limited in the range  $0 \leq p < 0.1$ , when the conditions ( $p = 0$  and  $n = 1$ ) are met and the deduced result is described as  $Y = 3$ . Therefore, the generated network with WTOM is actually reduced to an improved BA<sup>28</sup> networks, which can improve both the robustness and energy efficiency in network topology with percolation theory-based super-nodes optimal deployment<sup>29</sup> and scale-free theory-based node degree optimal distribution. Taking the upper bound of coding running time and the amount of nested loops into account, the analysis on WTOM algorithm complexity is mathematically transformed into a solution on topology evolution problem with solving asymptotic order in corresponding recursive equation. Based on the maximum incremental coding running time calculated according to cyclic iteration steps in WTOM topology generation, where the upper limit of created edges in evolution process is subjected to proposed preferential attachment and the average path length is increased approximately logarithmically with the network size  $N$ , WTOM algorithm complexity is finally deduced as  $O(N * \log_2 N)$ .

## Flow-table driven control in WSN physical system

In proposed SD-CPSF, the specific mobile behavior of super-nodes is driven by composite virtual force and the optimal deployment principle is achieved according to “force field” (virtual force matching rule and threshold) set in flow-table entry. Furthermore, network evolution process is instructed by the preferential attachment probability stored in “default field.” Based on the functional module for cyber cognition and mining, WTOM is designed by controller in control plane and downloaded into switches in data plane via flow-table mode using OTAP. Based on the topology policies determined by WTOM, switches are acted as actuators in CPS to output the cyber feedback control on the physical system and the corresponding control processes by flow-table mode. As a result, super-nodes move to the suitable location and normal sensors choose preferential attachment to perform specific topology optimization actions.

**Table 1.** Parameters of simulation experiment.

Parameters	Value
Total number of sensors, $N$	140
Node distribution area, $A$ (m <sup>2</sup> )	$120 \times 120$
Local world nodes, $M$	100
Ordinary isolated nodes, $m_0$	3
Added edges, $m$	3
Maximum transmission radius, $R_{maxn}$ (m)	40
Super-node maximum transmission radius, $R_{maxs}$ (m)	80
Normal node initial energy, $E_o$ (J)	0.2
Data fusion energy, $E_{elec}$ (J)	$50 \times 10^{-9}$
Amplifier power consumption, $E_{mp}$	$1.3 \times 10^{-15}$
Circuit power consumption, $E_{fs}$	$10 \times 10^{-12}$
Gain coefficient, $k_g$	1.5
Mutual position relationship parameter, $k_m$	1.2
Density-dependent gain coefficient parameters, $k_d$	0.4
Gain coefficient between super-nodes, $k_s$	1.4
Learning factor, $c_1$	2.5
Learning factor, $c_2$	3

## Experimental results and analysis

We do experiments to evaluate the performance of proposed WTOM in SD-CPSF by analyzing the network characteristics including average path length, clustering coefficient, energy consumption, and life cycle.

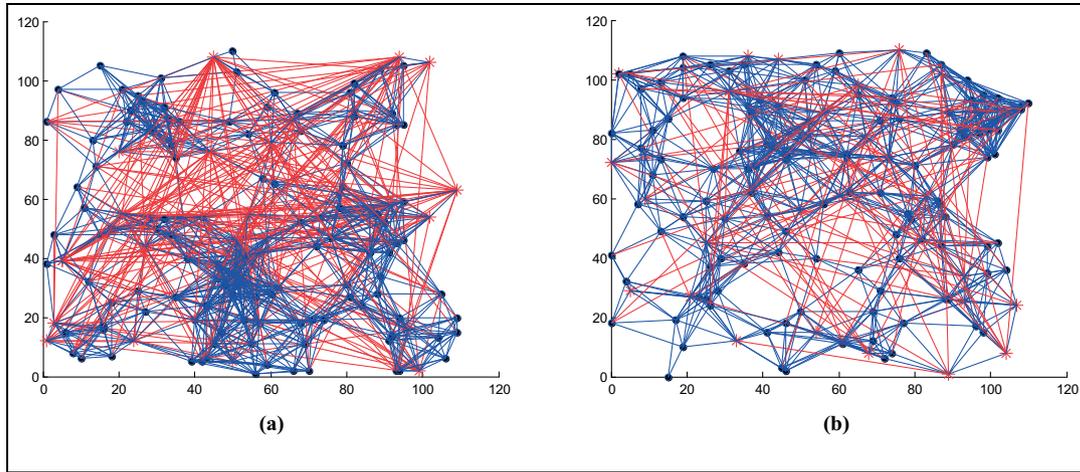
The network simulator NS3<sup>30</sup> and network building tool Gephi<sup>31</sup> are used to construct the experiment environment and analyze the performance of the proposed topology optimization mechanism using SDWSN prototype. Table 1 lists experimental parameters.

### Performance comparison on network topology

This simulation situation is divided into two groups of comparison counterparts, the first group is in accordance with WTOM based on preferential attachment probability model and the second topology generation model is formed according to the BA scale-free model.<sup>28</sup> The red edges in Figure 2(a) denote the edges built by crucial nodes-dependent preferential attachment mechanism, which includes the set of shortcut paths created by super-nodes in networks. The red edges in Figure 2(b) represent the edges constructed by node degree-based attachment method.

The set of blue lines in Figure 2 belongs to subset of the communication sides created by the network evolution process. The union set of blue and red edges constitute together the basic network communication topology.

Table 2 shows that the selected energy-rich sensor has the higher node degree and energy-barren sensor has the lower node degree in WTOM than the

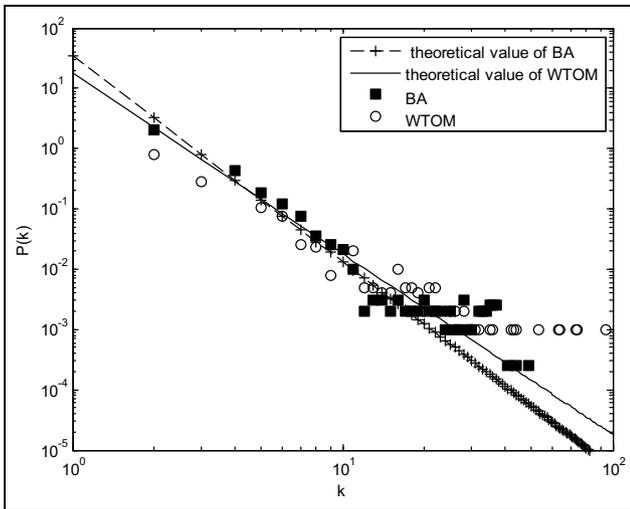


**Figure 2.** Network topology: (a) WTOM ( $N = 100, p = 0.05$ ) and (b) BA model ( $N = 100, p = 0$ ).

**Table 2.** Corresponding variety in degree with energy-diversity sensors in WTOM and BA model.

Node ID	Energy-rich sensors					Energy-barren sensors				
	13	40	67	94	110	25	53	77	86	112
Node degree in WTOM	23	16	25	29	12	19	13	9	17	11
Node degree in BA	6	11	7	5	2	21	18	14	19	16

WTOM: wireless sensor networks topology optimization model.



**Figure 3.** Degree distribution of WTOM ( $p = 0.045$ ) and BA model ( $p = 0$ ).

corresponding sensor with the same node ID in BA model. The main reason is that super-nodes with higher energy level in WTOM can contribute to build more shortcut paths to balance network energy consumption and result in the decrease in the average node degree of energy-barren sensors in networks.

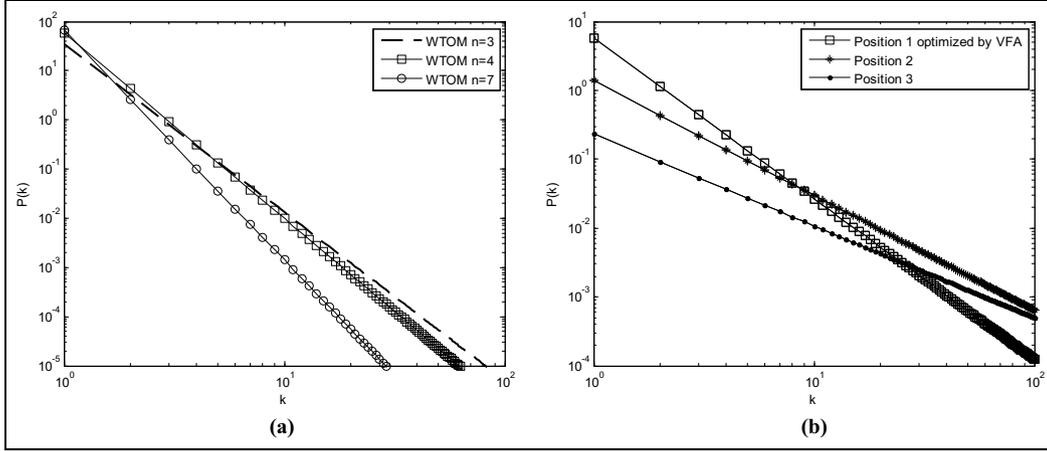
The topological properties with power-law degree distribution, large clustering coefficient and

disassortative degree correlation should contribute to improve the robustness in WSN network structure.

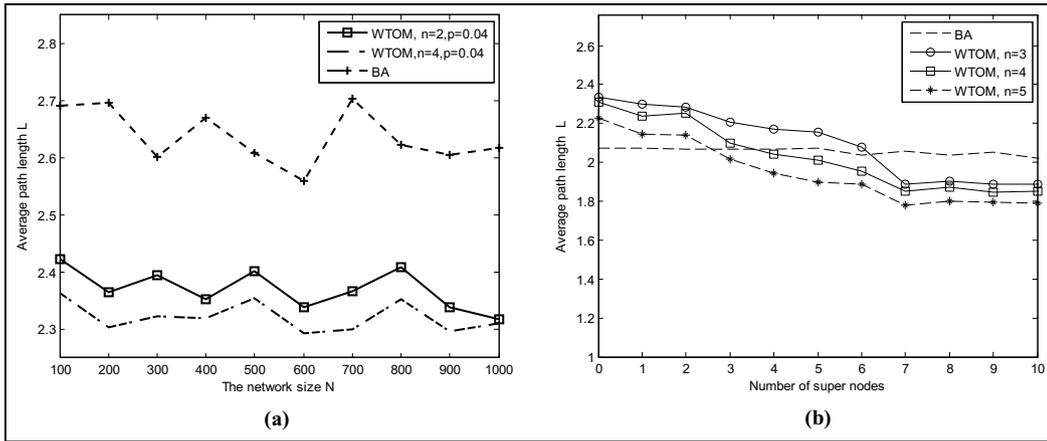
### Comparison of degree distribution

The scenery of sensors death caused by exhausted energy and environment interferes is similar as the networks suffer from random attack. The degree distribution of formed topology follows a power-law with exponential cutoff, which can help to enhance the fault tolerance and reliability of WSN.

Figure 3 shows that both WTOM and BA have the similar scale-free structure characteristic on the distribution of node degree, that is to say, sensors with high degree are with small distribution probability, while other sensors with small degree are with large distribution probability. According to the analysis on degree distribution of WTOM, there exists of flat status within a certain degree range, but the network reflects the scale-free feature in overall degree distribution. The main reason is that super-nodes play an important role in network evolution mechanism, which contribute to smooth the exponential degree distribution and the amount of sensors with higher degree is reduced. This helps to reduce sensors' premature death rate due to large energy consumption caused by high sensor degree. When  $p = 0$ , there is no super-node in network and WTOM has the similar functions as BA model.



**Figure 4.** Degree distribution of WTOM: (a) influence of super-nodes' energy level for degree distribution of WTOM ( $n = 3$ ,  $n = 4$ ) and (b) influence of super-nodes' position for degree distribution of WTOM.



**Figure 5.** Average path length: (a) average path of WTOM and BA model ( $n = 2, p = 0.05$ ;  $n = 3, p = 0.05$ ;  $n = 1, p = 0$ ) and (b) influence of the quantity for the average path of WTOM ( $n = 3$ ;  $n = 1$ ).

From Figure 4(a), we can see that the total failure rate of sensors can also be greatly reduced by adding appropriate initial energy to super-nodes adjusted by taking different values of parameter  $n$ . The super-node with higher energy level can do more contribution than the one with lower level to smooth the distribution of node degree and achieve balanced network energy consumption. Figure 4(b) shows the influence of super-nodes' position for the degree distribution in WTOM, which can be seen that the node degree distribution tends to be more uniform as the position of super-nodes optimized by VFA.

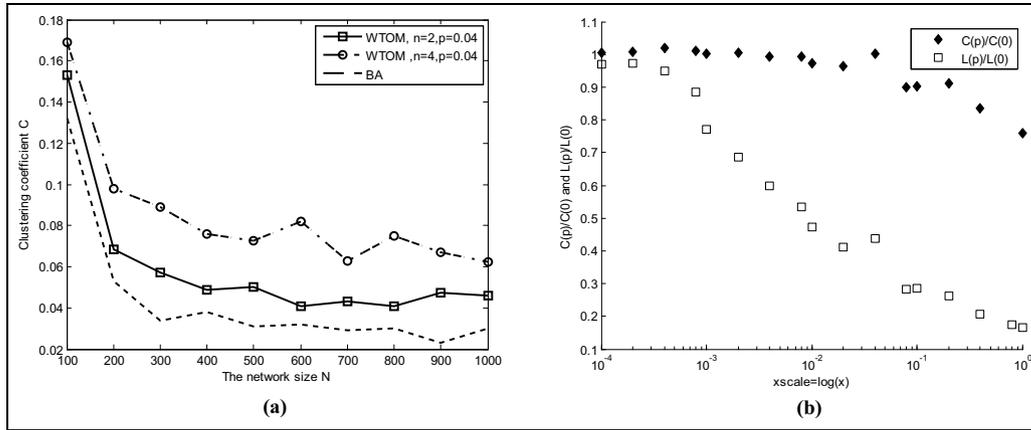
### Analysis on small-world effects

WTOM can find the weak disorder in the distribution of link length and reduce the average path length via

optimally deploying the super-nodes in WSN. Figure 5 focuses on the analysis on small-world effects in WTOM, which are inherent in the law of proposed WSN topology evolution. Figure 5(a) shows that the increase in initial energy of super-nodes can effectively reduce the average path length (shown as equation (11)) and the average hops of information transfer process in WSN.

$$L = \frac{1}{N} \sum_{i=1}^N D_i \quad (11)$$

where  $D_i$  represents the average number of hops when sensor  $i$  sends data to Sink along the shortcut path. Figure 5(b) indicates that an appropriate increase in the number of super-nodes can help to reduce  $L$  by the introduction of small-world effect with the short average network path length, but the amplitude range of  $L$



**Figure 6.** Small-world characteristics: (a) clustering coefficient of WTOM and BA model ( $n = 2, p = 0.04$ ;  $n = 4, p = 0.04$ ) and (b) small-world characteristics in WTOM.

**Table 3.** Maximum connected component of branch  $\psi$  versus lifetime cycles.

Parameters	Variety in value of parameters										
Cycles $r$	300	340	380	420	460	500	540	580	620	660	700
WTOM	100	100	99	97	96	94	76	49	41	32	20
BA model	100	100	91	82	73	61	49	42	33	21	10

WTOM: wireless sensor networks topology optimization model.

should hardly change when the number of super-nodes reaches a certain threshold. In comparison, the average path length of BA network is not sensitive to the number of super-node, because there are no special considerations on the effect of super-nodes in the construction of network topology.

### Comparison in the effect of clustering coefficient

Figure 6(a) shows the fact that WTOM has a larger clustering characteristic than BA model, which contributes to improve the robustness in local network connection denoted as an invulnerability indicator in WSN and the value of clustering coefficient  $C$  (see equation (12)) increases with the initial energy of super-nodes

$$C = \frac{1}{N} \sum_i \frac{2 * l_i}{k_i - (k_i - 1)} \quad (12)$$

Clustering coefficient of the entire network represents the average interconnected probability between any pair of connected sensors and is defined as the ratio of total number of connections  $l_i$  to the number of connections between  $k_i$  neighbors of sensor  $i$  divided by the actual presence among neighbor sensors fully connected.

Figure 6(b) indicates the change processes in average path length and clustering coefficient of the network with sensors = 120 and average vertex degree = 10. We can see that when the adjusting probability of edge remains a very small value, the average path length has been substantially shortened, while the opposite branch coefficient nearly not changes in value. This means that the network state has already reflected notable characteristic in small-world model, that is, network structure features ranged between random and ordered architecture show a high degree of group property in local range and a short average path length in global range.

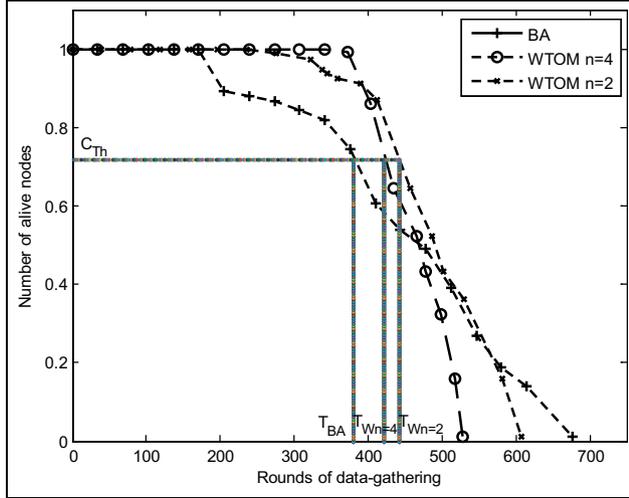
### The comparison in robust of invulnerability

The comparison with the robustness in invulnerability of WSN between WTOM ( $p = 0.1$ ) and BA model is shown in Table 3, which provides the statistics result on the model-related value  $\psi$  (denoted by maximum number of sensors belong to the maximal connection branch fraction) changing with the number of cycles.

As can be seen from Table 3, WTOM has the better robustness in network survivability compared with BA model in the course of data gathering. The main reasons are that the failure of WSNs is mainly caused by

**Table 4.** Life time versus the number of super-nodes.

Parameter	Variety in the value of parameters										
Probability $p$	0	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09	0.1
Number $a$	0	1	2	3	4	5	6	7	8	9	10
Cycle $r$	443	474	471	481	479	475	509	488	541	562	598

**Figure 7.** Network lifetime.

the energy depletion node, while WTOM takes the residual energy and degree distribution into consideration in topology construction procedure and also takes the protection of critical sensors into account, which conducts to maintain network connectivity, thereby improving the robustness of network survivability.

### Comparison in network lifetime

The lifetime of WSN is defined that at least 70% sensors are alive to support environment monitoring functionality in CPS service application. The lifetime is also an important index to reflect the energy efficiency of network. Figure 7 plots the average survival ratio of sensors to the number of data-gathering rounds for WTOM and BA model. The survival rate of sensors in a network can be used to evaluate the total energy consumption in data-gathering mechanism for CPS service. The lifetime of SDWSN is denoted as the duration of network operations (e.g. data gathering) while the sensors survival rate is above an application-based threshold ( $C_{th} \in [0.6, 0.8]$ ). In Figure 7, we set  $C_{th} = 0.72$  and denote the network lifetime achieved by BA, WTOM ( $n = 4$ ), and WTOM ( $n = 2$ ) as  $T_{BA}$ ,  $T_{Wn=4}$ , and  $T_{Wn=2}$ , respectively. We can see that  $T_{BA} < T_{Wn=2} < T_{Wn=4}$ , with WTOM achieving the highest average node survival

rate among the three schemes. This is mainly because the small-world features have been introduced into the topology evolution in WTOM, which can efficiently reduce the average path length for data routing and consequently improve the efficiency of energy utilization in WSN, which helps to prolong network lifetime. Furthermore, the energy efficiency can be further improved by increase the energy level of super-nodes in WTOM.

Table 4 shows that the network lifetime cycles should be prolonged with the more super-nodes being added into network using WTOM, which also contribute to increase the invulnerability of WSN.

The negative performance that some sensors with high node degree easily exhaust their energy leading to network fragmentation in BA model is covered by introducing small-world-based super-nodes deployment and energy-aware network evolution with SDN-based mechanism in WTOM. Therefore, the overall routing performance and structure robustness of global network are optimized, which finally help to achieve energy efficiency and robustness in WSN.

### Conclusion

Based on complex network theory and SDWN framework, an optimization WSN topology model is proposed to improve the invulnerability for fault tolerance, the adaptability for heterogeneity compatibility, and the energy efficiency for lifetime extendancy in WSN.

By introducing virtual force driven super-nodes deployment mechanism, redundant network resources can be reconfigured and allocated to vulnerable crucial network element, and small-world phenomenon can be produced according to complex network theory-based percolation process, which can improve the survivability and energy efficiency in WSN. According to resource-driven preferential attachment mechanism in topology evolution strategy, the formed network can show the scale-free-based topology structure characteristics, which can efficiently defend against random failure caused by node breakdown or network attack.

The experimental results show that compared with the original BA model, the proposed optimal network model can efficiently prolong the lifetime of WSN by reducing the amount of exchanged information

benefited from SDN-based functional architecture and shortening the average path length due to small-world effects created by rational deployment of super-nodes. In terms of survivability, the invulnerability of WSN can be enhanced by the scale-free-based network topology characteristic.

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