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Evaluating Knowledge Anchors in Data Graphs against Basic Level Objects

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Abstract. The growing number of available data graphs in the form of RDF Linked Data enables the development of semantic exploration applications in many domains. Often, the users are not domain experts and are therefore unaware of the complex knowledge structures represented in the data graphs they interact with. This hinders users' experience and effectiveness. Our research concerns intelligent support to facilitate the exploration of data graphs by users who are not domain experts. We propose a new navigation support approach underpinned by the subsumption theory of meaningful learning, which postulates that new concepts are grasped by starting from familiar concepts which serve as knowledge anchors from where links to new knowledge are made. Our earlier work has developed several metrics and the corresponding algorithms for identifying knowledge anchors in data graphs. In this paper, we assess the performance of these algorithms by considering the user perspective and application context. The paper address the challenge of aligning basic level objects that represent familiar concepts in human cognitive structures with automatically derived knowledge anchors in data graphs. We present a systematic approach that adapts experimental methods from Cognitive Science to derive basic level objects underpinned by a data graph. This is used to evaluate knowledge anchors in data graphs in two application domains - semantic browsing (Music) and semantic search (Careers). The evaluation validates the algorithms, which enables their adoption over different domains and application contexts.

Keywords: Data Graphs, Basic Level Objects, Knowledge Anchors, Usable Semantic Data Exploration.

1 Introduction

With the recent growth of linked data graphs, a plethora of interlinked domain entities is available for users' exploratory search tasks, such as learning and topic investigation [1]. Gradually, data graphs are also being exposed to users in different Semantic Web applications, taking advantage of the exploration of the rich knowledge encoded in the graphs. Among the applications for supporting user exploration, the two closest to the context of this paper are semantic data browsers [2–4] and semantic search systems [5, 6]. A broad range of users interact with such applications. Often, the users are not domain experts and struggle to formulate queries that represent their

needs. Furthermore, the users are usually exposed to an overwhelming amount of unfamiliar options for exploration of the data graph, which can lead to confusion, high cognitive load, frustration and a feeling of being lost. This hinders the users' exploration experience and effectiveness. A way to overcome these challenges is to suggest 'good' trajectories through the graph which can bring some utility to the users (e.g. increase effectiveness, improve motivation, or expand knowledge). Our work focuses on *knowledge utility* – expanding one's domain knowledge while exploring the graph.

Lay users, who are not experts in the corresponding domain, are unaware of the underlying complex knowledge structures encoded in a data graph [1, 7]. In other words, the *users' cognitive structures* about the domain may not match the *semantic structure of the data graph*. To address this challenge, we propose a novel approach to support graph exploration that can expand a users' domain knowledge. Our approach is underpinned by the subsumption theory for meaningful learning [8]. It postulates that a human cognitive structure is hierarchically organized in terms of highly inclusive concepts which can be used as anchors to introduce new knowledge [9]. A core algorithmic component for adopting subsumption theory for generating 'good' trajectories is the automatic identification of knowledge anchors in a data graph (KA_{DG}), i.e. entities that refer to anchoring concepts in human cognitive structures.

Our earlier research has developed several metrics and corresponding algorithms for identifying KA_{DG} , which are presented in detail in [10]. To utilize the KA_{DG} metrics in applications for data graph exploration, a systematic evaluation approach that examines the performance of the metrics is needed. Such an approach is presented in this paper. As the KA_{DG} should align with anchoring concepts in human cognitive structures, we develop an original way to derive such familiar concepts in a domain that corresponds to a data graph and considers the domain coverage of the graph. We adapt Cognitive Science experimental approaches of free-naming tasks to identify basic level objects (BLO) in human cognitive structures, i.e. domain concepts that are highly familiar and inclusive, so that people are able to recognize them quickly [11].

The evaluation approach presented in this paper contributes to developing usable semantic data graph exploration applications by providing:

- formal description of an algorithm for identifying basic level objects which correspond to human cognitive structures over a data graph;
- implementation of the BLO algorithm and utilization to evaluate KA_{DG} metrics over two application contexts for data graph exploration - semantic browsing (in musical instrument domain) and semantic search (in Career domain); and
- analysis of the performance of KA_{DG} metrics, including hybridization heuristics, using the benchmarking sets of BLO identified by humans.

The rest of the paper is structured as follows. Section 2 positions the work in the relevant literature and points at the main contribution. Section 3 briefly outlines the KA_{DG} metrics, summarizing [10]. An algorithm for identifying a benchmarking set of BLO is presented in Section 4. Sections 5 and 6 describe experimental studies where we apply the algorithm for identifying BLO using data graphs of two semantic exploration applications – music browser (MusicPinta) and career guidance (L4All). The BLO are used to evaluate the derived KA_{DG} . Section 7 discusses the evaluation findings, points at generality and applicability of the algorithms, and concludes the paper.

2 Related Work

Recent research on data exploration over the semantic Web examines different approaches to reduce users' cognitive load, especially when the users are exposed to complex domains which they are not familiar with. This has brought together research from Semantic Web, personalization, and HCI to shape user-oriented application for data exploration [1, 3, 6]. Personalized exploration based on user interests has been presented in [12]. A web-based graph visualization approach was used in [13] to help domain experts with analysis tasks. A co-clustering approach that organizes semantic links and entity classes was presented in [14] to support iterative navigation of entities over RDF data. The notion of relevance based on the relative cardinality and the in/out degree centrality of a graph node has been used to produce graph summaries [15]. Our work brings a new dimension to this research effort by looking at the *knowledge utility of the exploration*, i.e. providing ways to expand the user's awareness of the domain. This is crucial for the usability of semantic exploration applications, especially when the users are not domain experts.

Our approach is based on identifying knowledge anchors in data graphs. Relevant work on finding key concepts in a data graph was developed by research on ontology summarization [16] and formal concept analysis [17]. Ontology summarization aims at helping ontology engineers to make sense of an ontology in order to reuse and build new ontologies [18]. The closest ontology summarization approach to this paper's context is [19], which highlighted the value of cognitive natural categories for identifying key concepts. The work in [20] has formalized the main psychological approaches for identifying basic level concepts in formal concept analysis. In [10] we have operationalized these approaches, allowing automatic identification of KA_{DG} .

According to [18], there are two main approaches for evaluating a user-driven ontology summary: gold standard evaluation, where the quality of the summary is expressed by its similarity to a manually built ontology by domain experts, or corpus coverage evaluation, in which the quality of the ontology is represented by its appropriateness to cover the topic of a corpus. The evaluation approach used in [19] included identifying a gold standard by asking ontology engineers to select a number of concepts they considered the most representative for summarizing an ontology. To the best of our knowledge, there are no approaches that consider key concepts in data graphs which correspond to cognitive structures of lay users who are not domain experts. We identify such concepts in data graphs including both an automatic method to derive KA_{DG} and an experimental method to derive BLO that correspond to human cognitive structures. We evaluate KA_{DG} against benchmarking sets of BLO over the data graphs of two semantic exploration applications – browsing (Music) and search (Careers). By providing a systematic evaluation approach, the paper facilitates the adoption of the KA_{DG} metrics, and the corresponding hybridization methods, to enhance the usability of semantic web applications that offer user exploration of data graphs.

3 Identifying Knowledge Anchors in Data Graphs

A Data Graph DG describes entities (vertices) and attributes (edges), represented as *Resource Description Framework (RDF)* statements. Each statement is a triple of the form $\langle Subject, Predicate, Object \rangle$ [21]. Formally, a data graph is as a labeled directed graph $DG = \langle V, E, T \rangle$, depicting a set of RDF triples where:

- $V = \{v_1, v_2, \dots, v_n\}$ is a finite set of entities;
- $E = \{e_1, e_2, \dots, e_m\}$ is a finite set of edge labels;
- $T = \{t_1, t_2, \dots, t_k\}$ is a finite set of triples where each t_i is a proposition in the form of a triple $\langle v_s, e_i, v_o \rangle$ with $v_s, v_o \in V$, where v_s is the *Subject* (source entity) and v_o is the *Object* (target entity); and $e_i \in E$ is the *Predicate* (relationship type).

The set of entities V is divided further by using the subsumption relationship `rdfs:subClassOf` (denoted as \subseteq) and following its transitivity inference. This includes **category entities** ($C \subseteq V$ which is the set of all entities that have at least one subclass, at least one superclass, and at least one instance) and **leaf entities** ($L \subseteq V$ which is the set of entities that have no subclasses).

The set of edge types E is divided further considering two relationship categories: **hierarchical relationships** (H : is a set of subsumption relationships between the *Subject* and *Object* entities in the corresponding triples) and **domain-specific relationships** (D : represent relevant links in the domain, other than hierarchical links, e.g. in a Music domain, instruments used in the same *performance* are related).

Our work in [10] has formally adopted the Cognitive science notion of basic level objects [11], to describe two groups of metrics and their corresponding algorithms for identifying knowledge anchors in data graphs (KA_{DG}).

Distinctiveness metrics. These are adapted from the formal definition of cue validity, to identify the most differentiated categories whose attributes are associated exclusively with the category members but are not associated to the members of other categories. For example, in Figure 1, the AV value for entity v_2 is the aggregation of the AV values of entities (e_3, e_4, e_5) linked to members of v_2 ($v_{21}, v_{22}, v_{23}, v_{24}$) using the domain-specific relationship D . The AV value for e_3 equals the number triples between e_3 (*Source* vertex) and the members of v_2 (*Target* vertices v_{21}, v_{22}) via relationship D (2 triples), divided by the number of triples between e_3 (*Source* vertex) and all entities in the graph (*Target* vertices v_{12}, v_{21}, v_{22}) via relationship D (3 triples).

Distinctiveness metrics include:

- **Attribute Validity (AV)** – represents the proportion of relationships involving the category’s members.
- **Category Attribute Collocation (CAC)** – uses frequency of an attribute within the category’s members; gives preference to categories with many attributes shared by members.
- **Category Utility (CU)** - considers whether a category has many attributes shared by its members, and at the same time has attributes not related to many other categories.

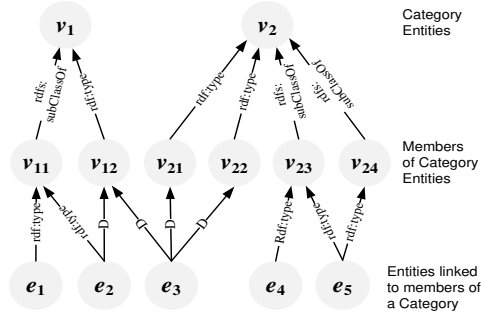


Fig. 1. A data graph showing entities and relationship types between entities.

Homogeneity Metrics. These metrics aim to identify categories whose members share many entities among each other. In this work, we have utilized three set-based similarity metrics [10]: **Common Neighbors (CN)**, **Jaccard (Jac)**, and **Cosine (Cos)**. For example (see Figure 1), consider the entity v_2 and the hierarchical relationship $rdf:type$ and the domain-specific relationship D . Entity v_2 has three entities (e_3, e_4, e_5) linked to its members ($v_{21}, v_{22}, v_{23}, v_{24}$), with *two* entities (e_3, e_5) shared among the four members through the hierarchical relationship $rdf:type$ and relationship D , whereas the entity v_1 has no entities shared by similar relationship types with its members (v_{11}, v_{12}). This indicates that entity v_2 is more homogenous than v_1 .

4. Identifying Basic Level Objects over Data Graphs

The notion of basic level objects was introduced in Cognitive Science research, illustrating that domains of concrete objects include familiar categories that exist at a highly inclusive level of abstraction in humans’ cognitive structures, more than categories at the superordinate level (i.e. above the basic level) or the subordinate level (i.e. below the basic level) [11, 22]. An example from [11] of a BLO is *Guitar* - most people are likely to recognize objects that belong to the category *Guitar* (*basic level*). However, users who are not experts in the music domain are unlikely to be able to recognize the category *Folk Guitar* (*subordinate level*) and name it with its exact name; instead, users may consider such objects equivalent to *Guitar* (closest basic level) rather than *Musical Instrument* (*superordinate level*).

4.1 Cognitive Science Experimental Approaches for Deriving BLO

While studying the notion of basic level objects, Rosch et al [11] conducted several experiments comprising free-naming tasks testing the hypothesis that object names at the basic level should be the names by which objects are most generally designated by adults. In a free-naming task, objects in a taxonomy are shown to a participant as a series of images in fixed portions of times, and the participant is asked to identify the

names of the objects shown in the images as quickly as possible. Three types of packets of images were shown to the participants: those in which one picture from each superordinate category appeared; one in which one image from each basic level category appeared; and one in which all images appeared. The participants overwhelmingly used names at the basic level while naming objects in the images [11].

To identify BLO, accuracy and frequency were considered. Accuracy considers whether a participant provides an accurate name for the object in the taxonomy, while frequency indicates how many times an object was named correctly by different participants. In the example of `Guitar`, when participants were shown members of `Guitar` (e.g. `Folk Guitar`, `Classical Guitar`) in a packet, they named them with their parent `Guitar` at the basic level more frequently than with names at the superordinate level (e.g. `Musical instrument`) or with their exact names (e.g. `Folk Guitar`, `Classical Guitar`) at the subordinate level.

The selection of object names used in the free-naming tasks in [11] was based on the population of categories of concrete nouns in common use in English. Every noun with a word frequency of 10 or greater from a sample of written English [23] was selected as a basic level object. A superordinate category was considered in common use if at least four of its members met this criterion.

However, the Cognitive Science approach for selecting BLO cannot be applied directly in the context of a data graph. The principal difference is that we need to constrain the human cognitive structures upon the data graph, as opposed to using a bag of words from popular dictionaries. This is because a data graph presents a lesser number of concepts from a domain, which belong to the graph scope, and there can be concepts that have been omitted. Moreover, the Cognitive Science studies included concrete domains where images of the objects could be shown to participants. Many semantic web applications utilize data graphs which include more abstract concepts for which images cannot be reliably shown to users (e.g. medical illnesses, environmental concepts, professions). Therefore, we adapt the Cognitive science experimental approach for deriving BLO to take into account the domain coverage of a data graph, which is applicable to any domain presented with a data graph.

4.2 Algorithm for Identifying BLO over Data Graphs

Following Cognitive Science experimental studies outlined above, we present two strategies with the corresponding algorithm for identifying BLO in a data graph.

Strategy 1. Takes into account whether a leaf entity $v \in L$ that has no subclasses is presented to a user and named with its parents (i.e. superclasses).

Strategy 2. Takes into account whether a category entity $v \in C$ that has one or more subclasses is presented and named with its exact name, or with the name of a parent that is a superclass or a category member (i.e. subclass that is not a leaf entity).

Algorithm 1 describes the two strategies for identifying BLO using accuracy and frequency. *Accuracy* refers to naming an entity correctly. It considers whether a user names an entity with its exact name, or with a parent (superclass) or with a category member (subclass) of the entity. *Frequency* indicates how many times a particular category was accurately identified by different participants.

The algorithm takes a data graph as input and returns two sets of BLO. For any class entity $v \subseteq V$, we identify the number of users to be asked to name the entity (line 2). For *Strategy 1* (lines 3-7), we consider accurate naming of a category entity (a parent) when a leaf entity $v \in L$ that is a member of this category is seen. For *Strategy 2* (lines 8-14), we consider naming a category entity $v \in C$ with its exact name (lines 10, 11) or a name of its superclasses (parents) or subclasses (members) (lines 12-13). In each strategy, we use a representation function $show(r, v)$ to create a representation of an entity v to be shown to the user. The representation of a leaf entity $v \in L$ (in Strategy 1) will consider the leaf itself (e.g. show a single label or a single image for the leaf entity), while the representation of a category entity $v \in C$ (in Strategy 2) will consider all (or some) of the category leaves (e.g. showing a random listing of a set of labels of entity leaves or showing a group of images of leaves as a collage).

Algorithm 1: Identifying Basic Level Objects in Data Graphs

Input $DG = \langle V, E, P \rangle$

Output two sets of entities: *Set1* and *Set2*

1. **for a set of entities** $v \subseteq V$ **do**
2. **for all** ($i := 1; i \leq n; i++$) *//show the entity v to n users*
3. **if** $v \in L$ **then** *//Strategy1*
4. $show(r, v)$ **and ask a user to name** v
5. **if** $answer(a, v) \in parent(p, v)$ **then** *//check accuracy*
6. $count_a++$ *//count frequency*
7. **end if;**
8. **else if** $v \in C$ **then** *//Strategy2*
9. $show(r, v)$ **and ask a user to name** v
10. **if** $answer(a, v) = label(b, v)$ **then** *//check accuracy*
11. $count_a++$ *//count frequency*
12. **else if** $answer(a, v) \in \{parent(p, v) \cup member(m, v)\}$ **then** *//check accuracy*
13. $count_a++$ *//count frequency*
14. **end if;**
15. **end if;**
16. **end for;**
17. **end for;**
18. $Set1 = \{answer(a, v) : v \in L \wedge count_a \geq k\}$ *//K is number of different users*
19. $Set2 = \{answer(a, v) : v \in C \wedge count_a \geq k\}$ *//K is number of different users*

For an entity v , the following SPARQL query is used to get the set of entity leaves:

```

SELECT ?leaf ?leaf_label
WHERE {{?leaf rdfs:subClassOf v.
       ?leaf rdfs:label ?leaf_label.
FILTER NOT EXISTS
       {?member rdfs:subClassOf ?leaf.}}
```

The two strategies in Algorithm 1 for obtaining BLO are applied as follows:

Strategy 1, when a user is shown a representation of a leaf entity $v \in L$ (line 4), the following steps are conducted:

- The function $answer(a, v)$ assigns a user's *answer* a to the leaf entity v .
- The function $parent(p, v)$ returns a set of labels (i.e. names) of the *parent(s)* p of the leaf entity v via the following SPARQL query:

```
SELECT ?parent_label ?label
WHERE {v rdfs:subClassOf ?parent.
       ?parent rdfs:label ?parent_label.}
```

- The algorithm in (line 5) checks if the user named the leaf entity v with one of its parents. If an accurate name of a parent was provided, then the frequency of the parent entity will be increased by one (line 6).

Strategy 2, when a user is shown a representation of a category entity $v \in C$ (line 9), the following steps are conducted:

- The function $answer(a, v)$ assigns a user's *answer* a to the category entity v .
- The function $parent(p, v)$ returns a set of labels of *parent(s)* p of the category entity v via SPARQL queries similar to Strategy 1 above.
- The function $member(m, v)$ returns a set of labels (i.e. names) of *member(s)* m of the category entity v via the following SPARQL query:

```
SELECT ?member_label
WHERE {?member rdfs:subClassOf v.
       ?member rdfs:label ?member_label.}
```

- The function $label(b, v)$ returns the *label* (i.e. name) of the category entity v via the following SPARQL query:

```
SELECT ?label
WHERE {v rdfs:label ?label.}
```

- The algorithm in (lines 10, 12) checks if the user named the category entity v with its exact name, or a name of its parents or its members. If there was accurate naming of the category, a parent or a member, the frequency of the category name (line 11), the parent name or the member name (line 13) will be increased by one.

4.3 Application Contexts Used for Experimental Evaluation

Linked Data graphs represented as a set of RDF triples can be ideal structures for Semantic exploration applications [24]. One class of applications is semantic data browsers which operate on semantically tagged content and present browsing trajectories using relationships in the underpinning ontologies [1, 2], supporting uncertain or complex information needs [3]. They enable the users to initiate a data exploration session from a single entry point in the graph and move through entities by following RDF links [2]. Another class of widely used semantic Web applications are semantic data search engines [25]. Such applications allow the users to enter search queries

though keyword-based search interfaces and provide the users with a list of search results obtained by using semantic queries automatically generated by the system [6].

In this paper, we present experimental studies over two different application domains for evaluating KA_{DG} metrics against BLO. The first study is in the context of a **semantic data browser in the Music domain**, called **MusicPinta** [2]. MusicPinta enables users to navigate through musical instruments extracted from DBpedia, and get information about these instruments together with musical performances and artists using these instruments. MusicPinta provides context for studying BLO in a concrete domain, as users can see images of musical instruments (as in [11, 26]). The second study is in the context of a **semantic search engine in Career guidance**, called **L4All** [27]. L4All is a proprietary semantic search application which enables learners to explore various career options to plan their career progression [27]. L4All provides context for studying basic level objects in an abstract domain, where the users cannot be shown concrete representations of the graph entities.

The data graphs of the two applications are used for the evaluation studies.

MusicPinta. The dataset includes several open sources. DBpedia¹ for musical instruments and artists - this dataset is extracted from dbpedia.org/sparql using CONSTRUCT and made available as open source at the sourceforge². DBTune³ for music-related structured data - this dataset is made available by the DBTune.org in linked data fashion. Among the datasets on DBTune.org we utilize: (i) Jamendo - a large repository of Creative Commons licensed music; (ii) Megatune - an independent music label; and (iii) MusicBrainz - a community-maintained open source encyclopaedia of music information. All datasets are available as RDF datasets and the Music ontology⁴ is used as a schema to interlink them. For the experimental study, we use the top level class Music Instrument and all its entities (classes and instances).

L4All. The dataset is drawn from the “LifeLong Learning in London for All” (L4All) project [27], bringing together experts from lifelong learning and careers guidance, content providers, and groups of students and tutors. It provided lifelong learners with access to information and resources that would support them in exploring learning and career opportunities and in planning and reflecting on their learning. The L4All dataset uses the ontology developed by the L4All project, and users’ data collected during the project (anonymised for privacy). Among five class hierarchies in the L4All ontology, the *Occupation* and *Subject* class hierarchies have the richest class representation and depth (see Table 1).

Table 1. Main characteristics of the MusicPinta and L4All data sets

Dataset	Hierarchy Root Class	Depth	No. of Classes	No. of Instances/leaves
MusicPinta	Instrument	7	364	256
L4All	Occupation	5	463	3737
	Subject	3	160	2194

¹ <http://dbpedia.org/About>

² <http://sourceforge.net/p/pinta/code/38/tree/>

³ <http://dbtune.org/>

⁴ <http://musicontology.com/>

5 MusicPinta: Evaluating $KADG$ against BLO

As a use case in a representative domain for evaluating knowledge anchors over a data graph, we used a typical semantic data browser, MusicPinta, which was developed in our earlier research [2]. Knowledge anchors would lead to extending MusicPinta to suggest exploration paths that can improve the user’s domain knowledge.

5.1 Obtaining BLO

To enable impartial comparison of the outputs of the $KADG$ algorithms and BLO, we conducted a user study in the Musical Instrument domain following Algorithm 1.

Participants. 40 participants, university students and professionals, age 18–55, recruited on a voluntary basis. None of them had expertise in Music.

Method. The participants were asked to freely name objects that were shown in image stimuli, under limited response time (10s). Overall, 364 taxonomical musical instruments were extracted from the MusicPinta dataset by running SPARQL queries over the MusicPinta triple store to get all musical instrument concepts linked via the `rdfs:subClassOf` relationship. The entities included: *leaf entities* (total 256) and *category entities* (total 108). Applying the two strategies in Algorithm 1, for each leaf entity, a representative image was collected from the Musical Instrument Museums Online (MIMO)⁵ to ensure that pictures of high quality were shown⁶. For a category entity, all leaves from that category entity were shown as a group in a single image (similarly to a packet of images in [11]). Ten online surveys⁷ were run: (i) leaf entities: eight surveys presented 256 leaf entities, each showed 32 leaves; (ii) category entities: two surveys presented 108 category entities, each showed 54 categories.

Free-naming task. Each image was shown for 10 seconds on the participant’s screen. She was asked to type the name of the given object (for leaf entities) or the category of objects (for category entities). The image allocation in the surveys was random. Every survey had four respondents from the study participants (corresponds to line 2 in Algorithm 1). Each participant was allocated only to one survey (either leaf entities or category entities). Figures 2-4 show example instrument images and participant answers (Figure 2 from Strategy 1, and Figures 3, 4 from Strategy 2).

Applying Algorithm 1 over the MusicPinta dataset, two sets of BLO were identified. *Set1* (Strategy 1) was derived from presenting leaf entities. We consider accurate naming of a category entity (parent) when a leaf entity that belongs to this category is seen. For example (see Figure 2), a participant was shown the image of `Piccolo trumpet`, a leaf entity in the data graph, and named it with its parent category `Trumpet`. This will be counted as an accurate naming and will increase the count for `Trumpet`. The overall count for `Trumpet` will include all cases when participants

⁵ <http://www.mimo-international.com/MIMO/>

⁶ MIMO provided pictures for most musical instruments. In the rare occasions when an image did not exist in MIMO, Wikipedia images were used instead.

⁷ The study was conducted with Qualtrics (www.qualtrics.com). Examples from the surveys are available at: <https://drive.google.com/drive/folders/0B5ShywKndSLXaVhrSWpiYVZ3WjA>

named `Trumpet` while seeing any of its leaf members. *Set2* (Strategy 2) was derived from presenting category entities. We consider naming a category entity with its exact name or a name of its parent or subclass member. For example (see Figure 3), a participant was shown the image of category `Trumpet` and named it with its exact name. This will increase the count for `Trumpet`. In Figure 4, a participant saw the category `Brass` and named it as its member category `Trumpet`.

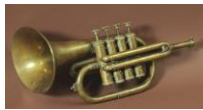


Fig. 2. An image of Piccolo trumpet (a leaf in the data graph) was shown to a user, who named it as “Trumpet”



Fig. 3. An image of Trumpet (a Category concept in the data graph with two subclasses) was shown to a user, who named it as “Trumpet”.



Fig. 4. An image of Brass (Category concept in the data graph) shown to a user, who named it as “Trumpet”.

In each of the two sets, entities with frequency equal or above two (i.e. named by at least two different users) were identified as potential BLO. The union of *Set1* and *Set2* gives BLO. It includes musical instruments such as: Bouzouki, Guitar and Saxophone. The BLO obtained from MusicPinta are available here⁸.

5.2 Evaluating KA_{DG} against BLO

Quantitative Analysis. We used the BLO identified to examine the performance of the KA_{DG} metrics. For each metric, we aggregated (using union) the KA_{DG} entities identified using the hierarchical relationships (H). We noticed that the three homogeneity metrics have the same values; therefore, we choose one metric when reporting the results, namely Jaccard similarity⁹. A cut-off threshold point for the result lists with potential KA_{DG} entities was identified by normalizing the output values from each metric and taking the mean value for the *60th percentile* of the normalized lists. The KA_{DG} metrics evaluated included the three distinctiveness metrics plus the Jaccard homogeneity metric; each metric was applied over both families of relationships – hierarchical (H) and domain-specific (D). As in ontology summarization approaches [19], a name simplicity strategy was applied to reduce noise when calculating key concepts (usually, basic level objects have relatively simple labels, such as chair or dog). The name simplicity approach we use is solely based on the data graph. We identify the *weighted median* for the length of the labels of all data graph entities $v \subseteq V$ and filter out all entities whose name length is higher than the median. For the MusicPinta data graph, the weighted median is 1.2, and hence we only included entities which consist of one word. Table 2 illustrates precision and recall values comparing BLO and KA_{DG} derived using hierarchical and domain specific relationships.

⁸ <https://drive.google.com/drive/folders/0B5ShywKndSLXaVhrSWpiYVZ3WjA>

⁹ The Jaccard similarity metric is widely used, and was used in identifying basic formal concepts in the context of formal concept analysis [29].

Table 2. MusicPinta: performance of the KA_{DG} algorithms compared to BLO.

Relationship types	Precision				Recall			
	AV	CAC	CU	Jac	AV	CAC	CU	Jac
Hierarchical	0.58	0.55	0.59	0.6	0.64	0.73	0.73	0.55
Domain-Specific	0.62	0.58	0.59	0.62	0.36	0.5	0.59	0.36

Hybridization. Further analysis of the False Positive(FP) and False Negative(FN) entities indicated that the algorithms had different performance on the different taxonomical levels in the data graph. This led to the following heuristics for hybridization.

Heuristic 1: Use Jaccard metric with hierarchical relationships for the most specific categories in the graph (i.e. the categories at the bottom quartile of the taxonomical level). There were FP entities (e.g. Shawm and Oboe) returned by distinctiveness metrics using the domain-specific relationship `MusicOntology:Performance` because these entities are highly associated with musical performances (e.g. Shawm is linked to 99 performances and Oboe is linked to 27 performance). Such entities may not be good knowledge anchors for exploration, as their hierarchical structure is flat. The best performing metric at the specific level was Jaccard for hierarchical attributes - it excluded entities which had no (or a very small number of) hierarchical attributes.

Heuristic 2: Take the majority voting for all other taxonomical levels. Most of the entities at the middle and top taxonomical level will be well represented in the graph hierarchy and may include domain-specific relationships. Hence, combining the values of all algorithms is sensible. Each algorithm represents a voter and provides two lists of votes, each list corresponding to hierarchical or domain-specific associated attributes (H, D). At least half of the voters should vote for an entity for it to be identified in KA_{DG} . Examples from the list of KA_{DG} identified by applying the above hybridization heuristics included `Accordion`, `Guitar` and `Xylophone`. The full KA_{DG} list is available here¹⁰. Hybridization improved Precision to 0.65 and Recall to 0.63.

6 L4All: Evaluating KA_{DG} against BLO

The Career domain is a suitable domain for studying basic level objects due to the richness of its ontological structures and the fact that the identification of knowledge anchors can facilitate users' exploration of such structures, as discussed in [28]. We followed Algorithm 1, conducting a study with human participants to identify BLO.

6.1 Obtaining BLO

Participants. 28 participants, university students and professionals, age 25–64, recruited on a voluntary basis. Most of them were experienced mainly in Computing.

Method. The experimental study for evaluating knowledge anchors in the L4All dataset included categories from the *Occupation* and *Subject* class hierarchies, for the reasons discussed above. Categories were represented to participants (corresponding

¹⁰ <https://drive.google.com/drive/folders/0B5ShywKndSLXaVhrSWpiYVZ3WjA>

to the $show(r, v)$ function in Algorithm 1) using names (i.e. labels) of the category's leaves. Overall, 623 class entities were extracted from the two class hierarchies (463 for *Occupation* and 160 for *Subject*) by running SPARQL queries to get all class entities linked via the `rdfs:subClassOf` relationship. The entities included: *leaves* (349 for *Occupation* and 141 for *Subject*) and *categories* (114 for *Occupation* and 19 for *Subject*). Seven online surveys⁷ were developed (six surveys presented the 114 category entities of the *Occupation* class hierarchy, with each survey showing 19 categories; and one survey presented the 19 categories of the *Subject* class hierarchy). The category allocation in each survey was random. Every survey had four respondents from the study participants. Each participant was allocated *only to one survey*.

Category identification task. A representation of each category was shown on the participant's screen and he/she was asked to identify the category name. The representation included a list of leaves' names of that category (at most four leaf names were shown on the participant's screen). The participant was provided with four different categories as candidate answers (including the category which the leaves belong to) and the participant was asked to select one category that he/she thinks the leaf entities belong to. The three additional candidate categories covered three levels of abstraction, namely: a parent from the superordinate level, a member from the subordinate level, and a sibling at the same category level. In cases where no parents or members could be added to the candidate answers, siblings were used instead.

Applying Strategy 2 in Algorithm 1 over the *Occupation* and *Subject* class hierarchies in the L4All dataset, we considered naming a category entity with its exact name or a name of its parents or its non-leaf subclass members shown to the participants. Figures 5 and 6 show examples of the category identification task from the *Occupation* and *Subject* class hierarchies respectively. For instance, the participant in Figure 5 saw two leaves (the category has two leaves only) of the category Housekeeping Occupation and the participant identified the category's parent Personal Service Occupation, which he/she thinks that the leaves belong to. This will increase the frequency for the category Personal Service Occupation. In Figure 6, a participant was shown the leaf names of the category Biological Sciences (four random leaves where selected among 9) and selected its exact name. This will increase the count for the category Biological Sciences.



Fig. 5. A representation of Housekeeping Occupation (a Category concept in the *Occupation* hierarchy with two subclasses) was shown to a user, who identified it as “Personal Service Occupation”.



Fig. 6. A representation of Biological Sciences (a Category concept in the *Subject* hierarchy with four random subclasses) was shown to a user, who identified it as “Biological Sciences”.

Category entities in the *Occupation* and *Subject* class hierarchies with frequency equal or above two (i.e. categories named by at least two different users) were identified as potential BLO. Examples of BLO from *Occupation* were Administrative, IT Service Delivery, Functional Managers and from *Subject* were Biological Sciences, Law, Medicine and Dentistry. The full KA_{DG} and BLO lists obtained from the L4All data set are available here¹¹.

6.2 Evaluating KA_{DG} against BLO

Quantitative Analysis. The KA_{DG} metrics developed in [10] were run over the *Occupation* and *Subject* class hierarchies and the metrics outputs of KA_{DG} were tested against the BLO identified. For each KA_{DG} metric, we aggregated (using union) the entities identified using the hierarchical relationships (`rdfs:subClassOf` and `rdf:type`). One domain-specific relationship was used by the metrics (`Job` for *Occupation* and `Qualification` for *Subject*). We normalized the metrics output values and took the 60th percentile of the normalized lists as a cut-off threshold point. Name simplification was applied using the *weighted medians* for the length of the labels of class entities in the *Occupation* and *Subject* class hierarchies (for *Occupation* = 3.2 and for *Subject* = 2.8) to filter out entities whose name length is higher than the median. Entities with name length greater than 3 were excluded (the names of the two class hierarchies - *Occupation* and *Subject* - and conjunctions, e.g. “and”, were not taken into account in counting the name length of entities).

Precision and *Recall* values for the metrics were identified (see Table 3). The three homogeneity metrics from [10] had the same values; therefore, we choose the Jaccard similarity metric in reporting the results (similarly to the MusicPinta analysis). Using the hierarchical relationships (`rdfs:subClassOf` and `rdf:type`), precision and recall values were good for *Occupation* (precision ranging from 0.72 to 0.79 and recall from 0.44 to 0.88) and very mixed for *Subject* (precision ranging from 0 to 1 and recall from 0 to 0.53). For the domain-specific relationships, the precision and recall were mixed for *Occupation* (precision ranging from 0 to 0.75 and recall from 0 to 0.76) and *Subject* (precision ranging from 0 to 1 and recall from 0 to 0.31).

By inspecting what caused the zero precision and recall values for the Category Utility (CU) distinctiveness metric and Jaccard (Jac) similarity metric, we noticed that none of these two metrics picked False Negative (FN) entities (i.e. potential KA_{DG}) using the domain-specific relationships (for *Occupation* and *Subject*) and using the hierarchical relationships (for *Subject*). The CU metric did not pick any FN entities since it multiplies the ratio [number of instances of a category divided by number of all entities, classes and instances in *Occupation*] with the total CU values for members of a category. Hence, the CU value will be decreased especially when there are 1000s of entities (i.e. classes and instances) in the graph. For instance, in the *Occupation* class hierarchy, the CU ratio for the FN category Sales Related Occupation is: 87 instances divided 4200 (463 classes + 3737 instances in the *Occupation* hierarchy), reducing the CU value for Sales Related Occupation to become

¹¹ <https://drive.google.com/drive/folders/0B5ShywKndSLXaVhrSWpiYVZ3WjA>

less than the 60th percentile cut-off point (0.01). The Jaccard similarity metric did not pick FN entities since each entity has instances linked with one instance only via a domain-specific relationship (e.g. *Job*). Hence, the categories will have no intersections among their instances, producing zero values in the Jaccard metric.

Table 3. KA_{DG} metrics performance using the two varieties of attribute types for the Occupation and Subject hierarchies in the L4All dataset

Class Hierarchy	Relationship type	Precision				Recall			
		AV	CAC	CU	Jac	AV	CAC	CU	Jac
Occupation	Hierarchical	0.72	0.76	0.79	0.79	0.52	0.88	0.44	0.44
	Domain-Specific	0.73	0.75	0	0	0.76	0.36	0	0
Subject	Hierarchical	1	1	0	0	0.53	0.53	0	0
	Domain-Specific	1	1	0	0	0.31	0.08	0	0

Hybridization. Analysis of the False Positive (FP) and False Negative (FN) entities indicated that the algorithms had different performance on the different taxonomical levels in the L4All data graph, which is formulated in the two heuristics below.

Heuristic 1: Use the AV and CAC distinctiveness metrics with hierarchical relationships for the categories at the bottom quartile of the class taxonomy. There were FN entities (e.g. *Sales Related* and *Science and Engineering Technicians*) returned by the AV and CAC homogeneity metrics using the domain-specific relationship *Job*, because these entities have a low number of instances (e.g. *Sales Related* has 87 instances and *Science and Engineering Technicians* has 50 instances; the median of instances per category is 144).

Heuristic 2: Take the majority voting for all other taxonomical levels. Most of the entities at middle and top taxonomical level are well represented in the graph hierarchy. Each metric represents a voter and provides two lists of votes, each list corresponding to hierarchical or domain-specific relationships. At least half of the voters should vote for an entity for it to be identified as KA_{DG} .

Examples of KA_{DG} identified by applying the above hybridization heuristics for Occupation and Subject class hierarchies are: for *Occupation* (*Engineering Professionals*, *Process Operatives*, *Science and Engineering Technicians*), and for *Subject* (*Business and Administrative Studies*, *Education*). The full lists of KA_{DG} identified are available here¹².

Hybridization increased performance, as follows: for *Occupation*, Precision = 0.77 and Recall = 0.92; for *Subject*, Precision = 1 and Recall = 0.53.

7 Discussion

This paper presents a systematic evaluation approach to validate KA_{DG} metrics against basic level objects derived by humans.

Algorithm for identifying BLO. The BLO algorithm presented in Section 4 is generic and can be applied over different application domains represented as data

¹² <https://drive.google.com/drive/folders/0B5ShywKndSLXaVhrSWpiYVZ3WjA>

graphs. In this paper, the algorithm is applied in two application domains for data exploration, Music and Careers, using the data graphs from two semantic exploration applications. Applying the BLO algorithm over two domains allows us to *illustrate two ways of instantiating the algorithm for obtaining BLO*. MusicPinta describes concrete objects - musical instruments - that can have digital representations (e.g. image, audio, video). An image stimulus was used to represent musical instruments, and free-naming tasks included showing image representations of graph entities and asking the users to quickly name the entities they see. In contrast, L4All comprises of abstract career categories, such as *Occupation* and *Subject*, which have text representations (i.e. labels of entities) but no clearly distinguishable images. In this case, a category verification task was used to obtain BLO by showing text representations of graph entities and asking the user to identify the matching entity given some answers.

An important component for applying the BLO is to identify appropriate stimuli to be used for representing graph entities and showing them to humans in either a free-naming task or in a category verification task. One of the main factors that affects choosing appropriate stimuli is how well the stimuli cover the entities in the data graph. In other words, the chosen stimuli should have representations for all entities in the graph hierarchies. For instance, the stimuli for MusicPinta were images - taken from an established source (MIMO⁵). The chosen stimuli have to be close enough to users' cognitive structures, so the users can understand the representation of entities.

The BLO algorithm over shallow graph hierarchies has some limitations. For instance, most categories (15 categories out of 19) in the *Subject* class hierarchy of the L4All ontology were identified as BLO. In a category verification task over a shallow hierarchy, finding candidate answers to be presented to users is challenging, especially when the shallow hierarchy does not contain the three levels of abstraction (basic, subordinate and superordinate). Furthermore, the identified BLO in data graphs can have confusing category labelling which reflect insufficiently articulated scope; for instance, vague names (e.g. 'European Language, Literature and related subject') or combining two categories in one (e.g. 'Mathematical and Computer Sciences'). Hence, the BLO algorithm is sensitive to the quality of the ontology. This points at another possible application of BLO - peculiarities in the output can indicate deficiencies of the ontology which can provide insights for re-engineering the ontology. An area of future work is to improve the L4All ontology by modifying the class labels and better articulating their scope.

Performance of KA_{DG} metrics. The identified BLO were used to examine the performance of the KA_{DG} metrics. Our analysis found that hybridization of the metrics notably improved performance. The hybridization heuristics for the upper level of the graph hierarchies tend to be the same - combine the KA_{DB} metrics using majority voting. However, the hybridization heuristics for the bottom level of the hierarchy differed depending on how instances at the bottom of the graph were associated through domain-specific relationships. The performance is sensitive to the appropriateness of the domain-specific relationships captured in the data graph. Examining the FP and FN entities for the hybridization algorithms for KA_{DG} led to the following observations:

Missing basic level entities due to unpopulated areas in the data graph. We no-

ticed that none of the metrics picked FN entities belonging to the bottom quartile of the taxonomies and having a small number of members (such as `Cello` in `MusicPinta` and `Construction Operatives` in the `Occupation` class hierarchy in `L4All` - `Cello` has only one subclass and `Construction Operatives` has 10 instances - mean number of instances in `Occupation` is 184). While these entities belong to the cognitive structures of humans and were therefore added to the BLO sets, one could question whether such entities would be useful knowledge anchors because of their relatively small number of members. These entities could lead the user to ‘dead ends’ within unpopulated areas of the data graph which may be confusing. We therefore see such FN cases as ‘good misses’ by the KA_{DG} metrics.

Selecting entities that are superordinates of entities in BLO. The FP included entities (such as `Reeds` in `MusicPinta` and `Secretarial` and `Related Occupation` in the `Occupation` class hierarchy in `L4All`) which are well represented in the graph (`Reeds` has 36 subclasses linked to 60 DBpedia categories; `Secretarial` and `Related Occupation` has 8 subclasses and 800 instances). Although these entities are not close to human cognitive structures, they provide direct links to entities in BLO (`Reeds` links to `Accordion`; `Secretarial` and `Related Occupation` links to `Administrative` and `Secretarial Occupation`). We therefore see such FP as ‘good picks’, as they provide *bridges* to BLO entities.

8 Conclusion and Future Work

Data graph exploration underpins semantic Web applications, such as browsing and search. Lay users who are not domain experts can face high cognitive load and usability challenges when exploring an unfamiliar domain because the users are unaware of the knowledge structure of the graphs. This brings forth the challenge of building systematic approaches for supporting users’ exploration taking into account the knowledge utility of the exploration paths. To address this challenge, we adopt the subsumption theory for meaningful learning [9] where new knowledge is subsumed under familiar and highly inclusive entities. A core algorithmic component for adopting this theory is the automatic identification of knowledge anchors in a data graph.

The work in this paper adapts Cognitive Science experimental approaches for deriving the BLO, and presents an algorithm to capture the BLO that correspond to human cognitive structures over a data graph. Our work contributes to improving the usability of data graph exploration by presenting a methodology for aligning BLO in human cognitive structures and the corresponding knowledge anchors in a data graph. The obtained sets of BLO and KA_{DG} can have two broad implications: (i) to improve users’ exploration of large data graphs; and (ii) to reengineer the ontology to better align with human cognitive structures. We are focusing on the former, and are devising navigation strategies to expand users’ knowledge while exploring a data graph.

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