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# Thermoluminescence measurements of trap depth in alkali feldspars extracted from bedrock samples

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## Abstract

Various measurements of thermal trap depth are evaluated for K-feldspar grains extracted from a bedrock sample. The initial rise method and the various heating rates method yield consistent results for both the natural signal ( $E = 1.23$  and  $1.16$  eV, respectively) and for a regenerative dose of 64 Gy ( $0.83$  and  $0.78$  eV). For the fractional glow curve, apparent  $E$ -values range from  $0.39$  eV to a plateau around  $1.50$  eV. The highest values for the natural and regenerative signals are obtained using the newly-developed post-isothermal TL (pI-TL) method wherein the isothermal loss curves (gotten by subtracting TL curves obtained after different preheat durations) are fitted in the initial rise region on an Arrhenius plot. For a dose of 12.8 Gy, this method measures apparent  $E$ -values ranging from  $0.73$  eV to a plateau near  $1.84 \pm 0.06$  eV. We repeat this analysis on three additional feldspar samples (two perthites and a high albite) to get a mean value of  $E = 1.86 \pm 0.03$  eV. The same analysis of natural aliquots of the K-feldspar sample yields similar results, with the two highest  $E$ -values at  $1.81$  and  $1.86$  eV. The kinetic order does not systematically vary with isothermal holding temperature or duration but remains relatively constant at  $1.6 \pm 0.3$  (regenerative dose) and  $1.5 \pm 0.5$  (natural dose). The apparent frequency factor, measured assuming a single  $E$ -value of  $1.86$  eV, decreases systematically ( $\sim 10^{23} - 10^{12} \text{ s}^{-1}$ ) with hold temperature and duration, a result which is consistent with a thermally-activated, distance-dependent tunneling model for feldspar thermoluminescence (i.e., a single trap depth and a continuum of apparent frequency factors). Frequency factor values measured following identical isothermal treatments are comparable between the natural and regenerative post-isothermal TL curves. By contrast, if different  $E$ -values are assumed, the apparent frequency factor values appear stochastic. Finally, it is speculated that the plateau of pI-TL  $E$ -values may be interpreted as the thermal depth of the main dosimetric trap measured with IRSL protocols.

*Keywords:* feldspar thermoluminescence, fractional glow curve, feldspar trap depth, post-isothermal TL

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## 1. Introduction

One critical parameter in understanding how the feldspar luminescence system will evolve in different thermal scenarios is the thermal activation energy required for recombination ( $E$ -value). A number of measurements can be used to constrain this parameter under first-order kinetics; however, in the case of feldspar luminescence, which exhibits a continuum of thermoluminescence (TL) signals (Grün and Packman, 1994; Visocekas et al., 1996) and is generally considered to exhibit non-first-order recombination kinetics (Ankjaergaard et al., 2006; Jain and Ankjaergaard, 2011), the determination of this parameter is not straightforward, nor is it necessarily a single trap being accessed during a TL measurement (Balescu and Lamothe, 1992; Murray et al., 2009).

The basic obstacle that must be overcome in order to measure the  $E$ -values of a sample, is that TL glow curves (following natural or laboratory irradiations) comprise overlapping emissions of different stability. For potassium-rich feldspars, this is complicated by the presence of a second TL peak at higher temperatures (centered around 330 °C for  $\beta = 5$  °C/s), such that the measured glow curve contains a broad, asymmetric peak at lower temperatures (apex near 100 °C), and a high-temperature peak (or two peaks; e.g., Murray et al., 2009), often embedded within the first (Duller, 1997). This range of stability in the broad, lower-temperature emission has been interpreted as representing multiple, discrete trap depths (Strickertsson, 1985; Kirsh et al., 1987) or a continuum of trap depths (Sanderson, 1988). Alternately, a continuum of recombination distances may produce this behavior (Jain et al., 2012). Pagonis et al. (2014) recently concluded that either mechanism could produce the observed TL data. Regardless, to measure the kinetic properties for a portion of a feldspar TL glow curve (e.g., a single trap depth or a limited range of recombination distances), one must isolate that particular emission, either experimentally or mathematically.

To determine the thermal trap depths of the dosimetric traps producing the TL or IRSL signals, workers have relied chiefly upon: the initial rise method (hereafter, IRM), usually in conjunction with the fractional glow curve method (hereafter, FGC; Strickertsson, 1985; Visocekas et al., 1996; Chruścińska, 2001); isothermal loss measurements (Sanderson, 1988; Guralnik et al., 2015); and curve fitting methods (Pagonis et al., 2014; Jain et al., 2015) (for a full discussion of conventional methods, see pp. 101 - 130 of Chen and McKeever, 1997). The following incomplete list of the resulting  $E$ -values can be broadly categorized as either singular, continuous, or multiple and discrete. The singular estimates for the IRSL source trap include  $>1.5$  (Jain and Ankjaergaard, 2011), 1.66 (Li and Tso, 1997), 1.72 (Li et al., 1997),  $1.71 \pm 0.08$  (Murray et al., 2009), 1.92 - 2.06 (Li and Li, 2013), and  $\sim 2$  (Jain et al., 2015) eV. Pagonis et al. (2014) estimated a continuum of depths from 1.1 to 1.8 eV in plagioclase; Strickertsson (1985) assumed first-order kinetics to fit six TL peaks between 0.76 and 1.80 eV; and Kirsh et al. (1987) estimated five distinct peaks, ranging from 0.70 to 1.39 eV.

In this study, we estimate the apparent thermal activation energies responsible for natural and laboratory TL signals in feldspar crystals extracted from bedrock samples. First, we apply the initial rise method, the various heating rates method, and the fractional glow curve technique. Second, we develop a new  $E$ -value

37 estimation technique based on the isothermal decay of TL curves: the post-isothermal TL (pI-TL) method.  
38 This method quantifies (by glow curve subtraction) the loss between hold times at various temperatures. By  
39 doing so, we quantify not only the magnitude of isothermal decay but also the shape of the TL signal that  
40 would have resulted during thermal stimulation. In other words, those emissions which are of lesser stability  
41 are stripped away, allowing for peak shape analysis of a narrow range of thermal stabilities. Finally, the  
42 pI-TL results are discussed in terms of recombination kinetics, including the variation in kinetic order and  
43 frequency factor.

## 44 **2. Samples and methodology**

### 45 *2.1. Sample collection*

46 Bedrock samples were collected from two locations. Sample J0165 is a granodiorite taken from a vertical  
47 transect of the Yucaipa Ridge block, a fault-bounded, tectonic block within the San Bernardino Mountains  
48 in southern California (Spotila et al., 1998). Samples J0995 (quartzofeldspathic gneiss), J0999 (granite),  
49 and J1001 (granite) were collected from a glacial valley within the Beartooth uplift, a  $60 \times 125$  km block  
50 of Precambrian crystalline basement initially exhumed during the Laramide Orogeny (Wise, 2000). Samples  
51 were collected by detaching chunks of *in situ* bedrock by hammer and chisel.

### 52 *2.2. Sample preparation and luminescence instrumentation*

53 Samples were first spray-painted with a contrasting color. They were then broken into smaller fragments  
54 under dim, amber LED lighting. The light-exposed, outer-surface pieces (as identified by the presence of  
55 spray-paint) were discarded and the unexposed inner pieces were gently ground using a pestle and mortar.

56 The feldspar grains of 175-400  $\mu\text{m}$  were then isolated from the rubble. Subsamples were wet-sieved,  
57 treated with 3% HCl, separated by density using lithium metatungstate ( $\rho < 2.565 \text{ g/cm}^3$ ; Rhodes 2015),  
58 and treated with 10% HF for 10 minutes to remove the outer layer from the grains and thereby enhance the  
59 sample brightness. Grains were mounted on stainless steel discs in a small-diameter (ca. 3-5 mm) monolayer  
60 using silicone oil.

61 Luminescence measurements were carried out using a TL-DA-20 Risø automated reader equipped with a  
62  $^{90}\text{Sr}/^{90}\text{Y}$  beta source (Bøtter-Jensen et al., 2003). TL emissions were detected through a Schott BG3-BG39  
63 filter combination in a nitrogen atmosphere. Unless otherwise noted, TL glow curves were measured at a  
64 heating rate of  $5 \text{ }^\circ\text{C/s}$ .

### 65 *2.3. Sample compositions*

66 Several separated grains of each sample were prepared for electron-probe microanalysis (EPMA) to deter-  
67 mine their chemical compositions. These grains were mounted within epoxy, the surface of which was then  
68 progressively polished to expose the internal surfaces of grains. Prior to analysis, this mount was coated with  
69 a surficial layer of carbon to avoid electrical charging during electron bombardment.

Table 1: Composition of feldspar samples, as determined by electron-probe microanalysis.

Sample	$n$	Endmember composition			Elemental composition		
		An (mol%)	Ab (mol%)	Or (mol%)	Ca (wt%)	Na (wt%)	K (wt%)
J0165	4	0.3	10.5	89.3	0.0	0.9	12.8
J00995	4	0.1	99.6	0.3	0.0	8.9	0.0
J0999							
Na-rich zones	3	18.5	78.5	3.0	2.8	6.8	0.4
K-rich zones	2	0.0	3.6	96.3	0.0	0.3	13.7
J1001							
Na-rich zones	3	8.0	90.3	1.7	1.3	8.1	0.3
K-rich zones	3	0.1	3.8	96.2	0.0	0.3	13.9

70 The mounted and polished grains were then measured with a JEOL JXA-8200 electron-probe microan-  
71 alyzer. First, backscattered electron (BSE) images were acquired to assess the compositional structure of  
72 grains, and then spot analyses with wavelength-dispersive spectroscopy (WDS) were used to quantitatively  
73 determine the K, Na, and Ca abundances of each grain (Huot and Lamothe, 2012). Grains with more hetero-  
74 geneous compositions (i.e., phases of disparate average  $Z$ -values) were measured multiple times to quantify  
75 each phase. Duplicate measurements were performed to assess reproducibility. Spot analyses were performed  
76 using a defocused electron beam of diameter 10  $\mu\text{m}$ , an accelerating voltage of 15 keV, and a beam current  
77 of 15 nA. Immediately prior to measurement, spectrometer calibration was performed with anorthite, albite,  
78 and K-feldspar standards. Spot analyses were rejected when the interpreted total mass was outside the range  
79 of 98 - 102%.

80 The compositions of all samples are listed in Table 1. The analyzed grains of J0165 are K-feldspars, with  
81 an average composition of  $\text{Or}_{89}$ . Sample J0995 is high albite,  $\text{An}_{0.1}$ . Samples J0999 and J1001 both exhibit  
82 perthitic textures. In sample J0999, zones alternate between average compositions of  $\text{An}_{25}$  and  $\text{Or}_{96}$  and  
83 J1001 alternates between  $\text{An}_8$  and  $\text{Or}_{96}$ .

### 84 3. Determining thermal trap depths in K-feldspar

85 The terms used throughout this study are described in Table 2.

#### 86 3.1. Initial rise method

The initial rise method (IRM) plots the natural log of the normalized TL intensity as a function of the inverse temperature, analogous to an Arrhenius plot. If the concentrations of trapped electrons and recombination centers are effectively constant (a reasonable assumption for the low-temperature region of a stimulation curve), then the TL intensity with temperature should go as:

$$I(T) \propto \exp(-E/k_B T), \quad (1)$$

Table 2: Nomenclature used in this study.

Term	Description
$E$	Thermal trap depth
$s$	Frequency factor
$b$	Kinetic order
$k_B$	Boltzmann constant ( $8.617 \times 10^{-5} \text{ eV} \cdot \text{K}^{-1}$ )
$T_m$	Temperature at maximum intensity
$T_{1/2}$	Temperature at half-maximum intensity
$\beta$	Heating rate
IRM	Initial rise method
VHRM	Various heating rates method
FGC	Fractional glow curve
pI-TL	Post-isothermal TL

87 which implies that a straight line fitted to  $\ln(I(T))$  plotted against  $1/T$  should have a slope of  $-E/k_B$  (Chen  
88 and Kirsh, 1981, p.148). The results of the IRM are shown for K-feldspar extract of Yucaipa Ridge bedrock  
89 sample J0165, for the natural luminescence signal (Fig. 1(a)) and following a laboratory beta dose of 64  
90 Gy (Fig. 1(b))(see the Supplementary Materials for the original TL measurements). A heating rate of 0.1  
91  $^\circ\text{C}/\text{s}$  was used to minimize errors associated with thermal lag. Three aliquots were used in both cases and  
92 remarkable inter-aliquot consistency was found. The apparent activation energies of the natural (1.23 eV)  
93 and regenerative (0.83 eV) signals differ substantially, with the  $E$ -value following 64 Gy being far too shallow  
94 to retain electrons for longer than a few days at room temperature.

### 95 3.2. Various heating rates method

The various heating rates method (VHRM) exploits the fact that the temperature of maximum TL  
emission intensity ( $T_m$ ) can be expressed in terms of the heating rate,  $\beta$ :

$$\beta = (sk_B/E)T_m^2 \exp(-E/k_B T_m), \quad (2)$$

96 so that the plot of  $\ln(T_m^2/\beta)$  versus  $(1/T_m)$  can be fitted with a straight line of slope  $-E/k_B$ . To measure  
97 the apparent trap depth of the natural signal, three aliquots were heated for each heating-rate: 0.1, 0.5, 1,  
98 5, and 10  $^\circ\text{C}/\text{s}$ . For the apparent  $E$  value after 64 Gy, the same 3 aliquots were heated at 0.1, 0.3, 1, 3, and  
99 10  $^\circ\text{C}/\text{s}$ . The resulting  $E$  values of 1.16 and 0.78 eV are shown for the natural (Fig. 1(c)) and regenerative  
100 (Fig. 1(d)) signals (see the Supplementary Materials for the original TL measurements).

### 101 3.3. Fractional glow curve analysis

102 To probe multiple traps of similar depths (e.g., a continuum of depths or tunneling distances), researchers  
103 have developed the fractional glow curve (FGC) (Rudlof et al., 1978; Kirsh et al., 1987), which involves a series

104 of preheats to progressively higher temperatures. After holding at a given temperature, the sample is cooled  
105 before heating to a slightly higher hold temperature and so on. In this way, the lowest temperature region  
106 is investigated (and thereby emptied) before the next-highest temperature region is investigated, thereby  
107 minimizing overlap from the lower-temperature region.

108 Although recent feldspar models (Poolton et al., 1995; Jain and Ankjaergaard, 2011) do not require a  
109 distribution of trap depths, the distribution in sub-conduction-band recombination distances should result  
110 in a similar effect of overlapping TL peaks (Jain et al., 2012). Therefore, the FGC for a single aliquot  
111 of J0165 was measured by first administering a dose of 12.8 Gy, then heating the sample at 5 °C/s to a  
112 hold temperature of  $T$  °C for 100 s, with  $T$  ranging from 20 to 500 °C in increments of 20 °C (Fig. 2(a)).  
113 Unfortunately, at  $T > 320$  °C, the signal intensity was similar in magnitude to the thermal background,  
114 precluding analysis beyond this point. The initial rise regions of the individual heating steps following a  
115 single beta dose of 64 Gy (Fig. 2(a)) were then fitted with a straight line having a slope of  $-E/k_B$  (see  
116 Section 3.1). These  $E$ -values are plotted against the corresponding hold temperature (Fig. 2(b); cf. Fig. 3.14  
117 of Chen and McKeever, 1997).

118 Two observations can be made about Fig. 2(b). First, a relationship seems to exist between the final  
119 temperature and the  $E$ -value, representing a gradation in apparent site stability, perhaps due to increasing  
120 recombination distances (if the  $E$ -values are artifacts), or perhaps deeper traps are progressively accessed (if  
121 the  $E$ -values are real). Second, this linear increase in FGC  $E$ -values (0.97 - 1.51 eV) extends past the trap  
122 depth of the natural TL signal as calculated with the IRM and VHRM results (1.23 and 1.16 eV, respectively)  
123 (Fig. 1(a) and (c)).

#### 124 3.4. Post-isothermal TL (*pI-TL*) curve analysis

125 An alternate approach is to monitor how the TL shape changes following isothermal treatments of various  
126 durations. For analysis of the regenerative signal, the same aliquot of sample J0165 was repeatedly given the  
127 same dose of 12.8 Gy and then held at  $T$  °C for  $t$  s, where  $T$  ranged from 100 to 350 °C in increments of  
128 50 °C, and  $t = 0, 3, 10, 30, 100, 300, 1000$  s. Following each isothermal treatment, the aliquot was cooled  
129 to room temperature before a TL measurement at 5 °C/s to 500 °C. These TL curves are shown with linear  
130 and logarithmic y-axes (Fig. 3(a) and inset, respectively). The advantage of this approach is based upon  
131 the ability to isolate the luminescence emitted during hold-times by subtracting one TL curve from another.  
132 In other words, each subtracted curve represents the pseudo-TL curve that would be depleted during that  
133 isothermal treatment. Fig. 3(b) shows the regenerative TL lost during the hold time of  $t = 3-10$  s,  $10-30$  s,  
134 and so on, for all the hold temperatures.

135 For analysis of the post-isothermal TL natural signals, a multi-aliquot approach is necessary, where each  
136 heat treatment is performed on a different unbleached natural aliquot of sample J0165 (Fig.4(a)). The TL  
137 emissions of each aliquot were normalized to a subsequent test dose response (maximum TL intensity following  
138 a dose of 1.3 Gy). Because the natural glow curve is not significantly eroded by the lower temperature  
139 treatments, the isothermal treatments of the natural signals were limited to  $T = 250, 300,$  and  $350$  °C.

#### 140 3.4.1. Trap depth

141 If we consider these subtracted TL curves to be the charge lost during specific hold-time ranges, then the  
142 shape of these curves should contain useful kinetic information. The initial rise portion of these subtracted TL  
143 curves was fitted in the same way as in Section 3.3 to determine the apparent thermal trap depth; hereafter,  
144 this will be called the post-isothermal TL (pI-TL) method. The results for the regenerative and natural  
145 signals are shown in Fig. 5(a) and (e), respectively.

146 Just as with the FGC  $E$ -values following a regenerative dose (Fig. 2(b)), these pI-TL  $E$ -values steadily  
147 increase as deeper thermal regions are probed (Fig. 5(a)). Apparent  $E$ -values increase from about 0.73 eV  
148 to a seeming plateau around 1.86 (K-feldspar sample J0165). It is notable that the lowest value is similar to  
149 the values from the IRM and the VHRM for the 64 Gy irradiation in Sections 3.1 and 3.2. Additionally, this  
150 upper limit is higher than the highest FGC  $E$ -value (1.5 eV) observed for this sample.

151 The pI-TL regenerative  $E$ -values were also measured for samples J0995 (high albite), J0999 (perthite),  
152 and J1001 (perthite). A mean value of  $E = 1.84 \pm 0.06$  eV was calculated from the final three hold intervals  
153 (30 - 100, 100 - 300, and 300 - 1000 s) at 350 °C for the regenerative signals of all four feldspar samples.  
154 While samples J0165 and J0995 may plateau at these durations, samples J0999 and J1001 exhibited a positive  
155 slope, suggesting that the maximum  $E$ -value may be higher for these two samples. (That structurally well-  
156 ordered feldspars like perthites should have greater maximum stability than those which formed at higher  
157 temperatures and exhibit more uniform composition (e.g., Ab and Or) is consistent with the observation of  
158 Visocekas et al. (1994) that athermal fading rates increase with greater structural disorder.) The average  
159 plateau value for J0165 and J0995 is only  $1.86 \pm 0.03$  eV. Whether this plateau is real or apparent requires  
160 further investigation.

161 The trap depths measured for the natural pI-TL signals are generally consistent with the regenerative  
162 signals at the same isothermal conditions. Because of low signal intensity, the final subtracted curve at 350 °C  
163 (300 - 1000 s) was unsuited for analysis. The next two longest durations at 350 °C, however, give  $E$ -values of  
164 1.81 and 1.86 eV and are in good agreement with the plateau found after regenerative doses, lending further  
165 support to the idea of a maximum value near 1.86 eV.

#### 166 3.4.2. Kinetic order

167 The shapes of the pI-TL curves (Figs. 3(b) and 4(b)-(d)) resemble what would be expected under mixed-  
168 order kinetics. This conjecture can be quantified with the TL curve symmetry factor of Halperin and Braner  
169 (1960),  $\mu_g$ , which can be used to assign kinetic order to TL curves based on shape with little dependence on  
170  $E$  or  $s$  values (Chen and Kirsh, 1981, pp. 159 - 167).

171 Calculated symmetry factors for the pI-TL curves (excluding the initial 0 - 3 s measurement) yield an  
172 average kinetic order of  $1.6 \pm 0.3$  for the regenerative signals and  $1.5 \pm 0.5$  for the natural signals (Fig. 5(d)  
173 and (h)). There is no apparent relationship between hold temperature and the kinetic order for most sets  
174 of hold temperatures. This relatively stable kinetic order with greater temperature is consistent with the  
175 interpretation that the pathways are unchanging, whereas the probed lifetimes increase with TL temperature.

176 The high  $b$ -values for the natural signals lost at 250 °C between 3 - 10, 10 - 30, and 30 - 100 s ( $b = 2.2$ ,  
 177 2.3, and 2.1, respectively) may be an exception to this uniformity. That kinetic order is higher as the natural  
 178 signal is initially depleted may be caused by charge transfer to sites of greater thermal stability.

### 179 3.4.3. Frequency factor

Finally, given that each pI-TL curve has an apparent trap depth and kinetic order, we can estimate the  
 corresponding frequency factors. The calculation assumes general-order kinetics, and requires kinetic order  
 ( $b$ ), trap depth ( $E$ ), temperature at maximum intensity ( $T_m$ ), and heating rate ( $\beta$ ) to determine the frequency  
 factor ( $s$ ) (p. 11; Chen and Kirsh, 1981):

$$s(b-1)/\beta \int_{T_0}^{T_m} \exp(-E/k_B T) dT + 1 = (sbk_B T_m^2 / \beta E) \exp(-E/k_B T_m). \quad (3)$$

180 This calculation was performed under two different scenarios. In the first scenario, the  $E$ -value measured  
 181 for each isothermal condition was used to calculate the corresponding frequency factor. In the second, the  
 182 plateau value of 1.86 eV was used to calculate the apparent frequency factor for each pI-TL curve.

183 *Assuming individual  $E$ -values.* If each pI-TL curve derives from different trap depth (or range of depths), the  
 184 frequency factors for the regenerative and natural signals are shown in Fig. 5(b) and (f). The regenerative  
 185 values seem to increase with hold time, especially those at  $T = 100, 300, \text{ and } 350$  °C, but the results from  
 186 the other hold temperatures are less convincing. This result is unexpected if this broad regenerative peak  
 187 represents an increase in recombination-by-tunneling distances; this mechanism should produce the opposite  
 188 effect: a decrease in the apparent frequency factor as sites increase in stability (Jain and Ankjaergaard, 2011;  
 189 Jain et al., 2015).

190 While both natural and regenerative frequency factors span a similar range ( $\sim 10^{11} - 10^{13} \text{ s}^{-1}$ ), the  
 191 former seem less organized. This may represent the lower signal intensities involved, resulting in poor fittings  
 192 of  $E$  or  $b$  values. Alternately, the peak overlap from a higher temperature peak (e.g., Fig. 4 (b) - (d)) may  
 193 sufficiently distort the  $T_m$  value or the position of  $T_2$  ( $T_{1/2} > T_m$ ).

194 *Assuming a shared  $E$ -value of 1.86 eV.* If each pI-TL curve derives from a single trap depth of 1.86 eV  
 195 (see Section 3.4.1), the frequency factors for the regenerative and natural signals are shown in Fig. 5(c)  
 196 and (g). The consistent decrease in apparent frequency factor with increasing hold time and temperature is  
 197 consistent with the interpretation that K-feldspar thermoluminescence derives from a single dosimetric trap  
 198 via tunneling to centers at a variety of distances (Jain and Ankjaergaard, 2011). Such an interpretation would  
 199 result in a range of apparent frequency factors which reflects the range of recombination probabilities (Jain  
 200 et al., 2015). We favor this simple interpretation (i.e., one trap depth of 1.86 eV, many apparent frequency  
 201 factors).

202 Finally, it is remarkable that the frequency factors for the natural and regenerative signals decrease at  
 203 a similar rate and over a similar range. Such similarity supports the conjecture that the natural signal for

204 sample J0165 contains the stable portion of the signal measured after laboratory irradiation and exhibits  
205 similar kinetic properties.

## 206 4. Discussion

### 207 4.1. Comparing the methods for $E$ -value determination

208 To interpret the results from these four methods, it is helpful to consider their critical assumptions. The  
209 initial rise method assumes that detrapping, at least for the first portion of the emitted peak, is related only  
210 to the ratio of  $E/k_B T$  (Eq. 1). In other words, effects like retrapping and changes in recombination efficiency  
211 should be negligible. The method also requires that the entire fitted region derives from the same trap and  
212 does not include overlapping peaks. With the IRM, a single  $E$ -value is produced that, for glow curves without  
213 overlapping emissions, corresponds to the first accessed trap. The various heating rates method also produces  
214 a single  $E$ -value and assumes that neither the trap depth nor the frequency factor change during the TL  
215 measurement. The fractional glow curve method incorporates the assumptions of the IRM but offers the  
216 possibility of measuring multiple trap depths, provided that each initial rise region is sufficiently separated  
217 for the chosen heating rate and stop-temperature increment.

218 The post-isothermal TL method is similar in approach to the FGC method: the TL curve is progressively  
219 measured, allowing for multiple  $E$ -value analyses. Unlike the FGC, however, the pI-TL method is not  
220 inaccurate if there is trap overlap initially, as the next measured curve is subtracted before analysis (in the  
221 case of no overlap, the pI-TL method would reduce to the FGC method for  $E$ -value determination). Another  
222 advantage obtained by considering the emissions between hold times is that peak shape analyses can be  
223 performed, including the evaluation of  $b$  and  $s$  values for each isothermal time range. Because feldspar TL is  
224 known to exhibit overlapping emissions, we consider the pI-TL results least subject to error.

### 225 4.2. Comparing the measured $E$ -values

226 Notable concordance is found between the initial rise method and the various heating rates method. For  
227 the VHRM, the data seem to be sub-linear rather than linear as would normally be expected. This effect  
228 probably reflects the asymmetric nature of the feldspar TL glow curve: the initial rise region of the curve  
229 would be less affected, but in measuring the  $T_m$  value, the influence of overlapping, higher-stability traps  
230 biases the  $E$ -value determination. This effect should vary with heating rate, as lower heating rates will tend  
231 to minimize this trap separation effect. Importantly, the feldspar samples did not receive preheats prior to  
232 the measurement of apparent natural  $E$ -values.

233 The FGC  $E$ -values obtained compare well with experimental results reported elsewhere from sedimentary  
234 K-feldspars. Previous studies have reported values ranging from 0.4 eV at liquid nitrogen temperatures  
235 (Visocekas et al., 1996) to about 1.7 eV at temperatures above 280 °C (Strickertsson, 1985; Chruścińska,  
236 2001). All of these studies also noted the linear increase in  $E$  with FGC hold temperature.

237 Several observations can be made about the regenerative  $E$ -values derived from the post-isothermal TL  
238 method. First, just as with the FGC, a linear relationship exists between the isothermal duration and the  
239 corresponding  $E$ -value. A similar type of analysis on a museum specimen of plagioclase was done by Pagonis  
240 et al. (2014), who performed a general-order kinetics fitting of TL curves gotten by subtraction of post-  
241 isothermal TL curves where hold temperatures were varied but not durations. These authors found a range  
242 of  $E$ -values from 1.1 to 1.8 eV, with a generally decreasing kinetic order, from about 2.0 to 1.5. Measurements  
243 for our albite sample (J0995) are comparable, varying over a slightly broader range, from 0.76 to 1.87 eV  
244 (omitting the 0-3 s measurement, the range becomes 0.97 to 1.87 eV).

245 There exists a plateau in regenerative pI-TL  $E$ -values at  $1.86 \pm 0.03$  eV (J0165 and J0995;  $1.84 \pm 0.06$  eV  
246 for all four samples) for the three highest  $E$ -values observed in our pI-TL method. We tentatively interpret  
247 this as the depth of the ground state for the main dosimetric trap (see also Section 4.4). Whether this is a  
248 maximum within a distribution of depths or the true trap depth (i.e., activation progresses up through the  
249 band-tail states finally into the conduction band) is unclear.

250 Another consideration is the difference between the FGC and pI-TL methods in the final values obtained  
251 for regenerative  $E$ -values. Both techniques yield final values which might be interpreted as plateaus:  $1.49$   
252  $\pm 0.03$  eV (FGC, last four values of J0165) and  $1.84 \pm 0.03$  eV (pI-TL, last three values of J0165). Per-  
253 haps the best explanation for this discrepancy is that the reason for each ‘upper limit’ is different. In the  
254 regenerative fractional glow curve method, the sample receives a single dose before all measurements are  
255 performed. It seems reasonable to assume that above 320 °C the source traps have been emptied and that  
256 further measurements are comprised mostly of thermal background emissions. The FGC upper limit may,  
257 in this interpretation, be understood as methodological, not directly characteristic of trap parameters. By  
258 comparison, the pI-TL method involves irradiation of the sample prior to each isothermal treatment, thereby  
259 replenishing the source traps. The upper limit for this technique is governed also by the low signal intensity  
260 relative to the thermal background, but this is true only after treatments of 350 °C lasting 300 and 1000 s,  
261 which probe higher regions of the glow curve than those reached by the FGC method. Of course, the upper  
262 limit of this technique may also be limited by instrumental resolution and not by the maximum trap depth  
263 that would contribute TL at these measurement conditions.

264 Finally, it is encouraging that both the natural and regenerative doses yield similar  $E$ -values for J0165  
265 when evaluated with the pI-TL method. This is true for both the rising values measured at  $T = 250, 300,$   
266 and 350 °C, and for the uppermost values:  $1.86 \pm 0.03$  eV ( $n = 3$ ) for the regenerative dose, and  $1.84 \pm 0.04$   
267 eV ( $n = 2$ ) for the natural dose.

#### 268 *4.3. Kinetic order and frequency factor values*

269 The pI-TL kinetic order values of  $1.6 \pm 0.3$  for the regenerative signals and  $1.5 \pm 0.5$  for the natural  
270 signals (Fig. 5(d) and (h)) compare well and show no obvious dependence on hold temperature. This may  
271 indicate that similar recombination pathways are utilized during the entirety of the TL measurement.

272 Assuming that a) the application of Eq. 3 to pI-TL curves is valid, and b) the TL emissions share an  
273 actual (i.e., not apparent)  $E$ -value of  $\sim 1.86$  eV, the apparent frequency factor decreases regularly over the  
274 entire range of hold temperatures and durations (Fig. 5(c) and (g)). Even more striking is the correspondence  
275 between the natural and regenerative pI-TL frequency factors. This correspondence lends credence to the  
276 hypothesis that the natural and regenerative TL glow curves may receive contributions from the same trap  
277 population, with the natural signal missing the nearer trap-and-center pairs, i.e., a truncated  $n(r)$  distribution  
278 in Jain et al.'s (2015) model. That a shared  $E$ -value produces expected behavior in apparent frequency  
279 factors may favor the interpretation of a single trap depth responsible for the lower-temperature blue-green  
280 TL emissions (Jain et al., 2015) instead of a continuum of trap depths (Sanderson, 1988).

#### 281 4.4. Relating the pI-TL $E$ -value to IRSL signals

282 A primary concern when evaluating luminescence ages from K-feldspars is the thermal trap depth asso-  
283 ciated with the IRSL signal. Workers have investigated this parameter through the use of pulse-annealing  
284 experiments and the reduction of TL curves by IR stimulation (Li and Aitken, 1989; Duller and Wintle, 1991;  
285 Duller and Bøtter-Jensen, 1993; Duller, 1994; Tso et al., 1996; Murray et al., 2009). The interpretation of  
286 these experiments has not been straightforward, however, for although exposure to IR light depletes a broad  
287 region of the regenerative TL curve at lower temperatures, the majority of the IRSL source trap does not seem  
288 to be depleted significantly until higher temperatures. This reduction in TL intensity at lower measurement  
289 temperatures (i.e., the region populated after irradiation and without preheating) following IR exposure has  
290 been explained as a reduction in recombination efficiency (Murray et al., 2009). (If the loss of efficiency is  
291 related to the depletion of a shared recombination center, this explanation reconciles the similar emission  
292 spectra for K-feldspar TL and IRSL (Huntley et al., 1988, 1991).) More recently, Jain and Ankjaergaard  
293 (2011) have suggested that the lower- and higher-temperature TL peaks commonly found in feldspars may  
294 derive from a) localized recombination via the excited state of the trap, and b) recombination from the band-  
295 tail states (transitioning eventually into the conduction band), respectively. Under this interpretation, and  
296 given that the excited state is thought to lie within the band-tail states (Poolton et al., 2009), the uppermost  
297 pI-TL  $E$ -value should represent the thermal depth of the main dosimetric trap measured in IRSL protocols.

## 298 5. Conclusions

299 The similarity of pI-TL kinetic parameters between natural and artificial TL signals is intriguing and  
300 merits further exploration. The implication that the natural TL signal represents the high-stability region of a  
301 trap continuum may be overly simple, especially given previous studies which demonstrate differential thermo-  
302 optical bleaching properties between the low and high-temperature regions of the TL curve. Nevertheless,  
303 the agreement between the uppermost  $E$ -values of about 1.86 eV offer insight into the maximum thermal  
304 stability that may be expected for alkali feldspars extracted from bedrock samples. Finally, the temperature-  
305 independent kinetic order values combined with the decreasing apparent frequency factor values at higher

306 temperatures and longer hold times both support the recent hypothesis that feldspar TL (in addition to  
307 IRSL) derives from distance-dependent tunneling recombination.

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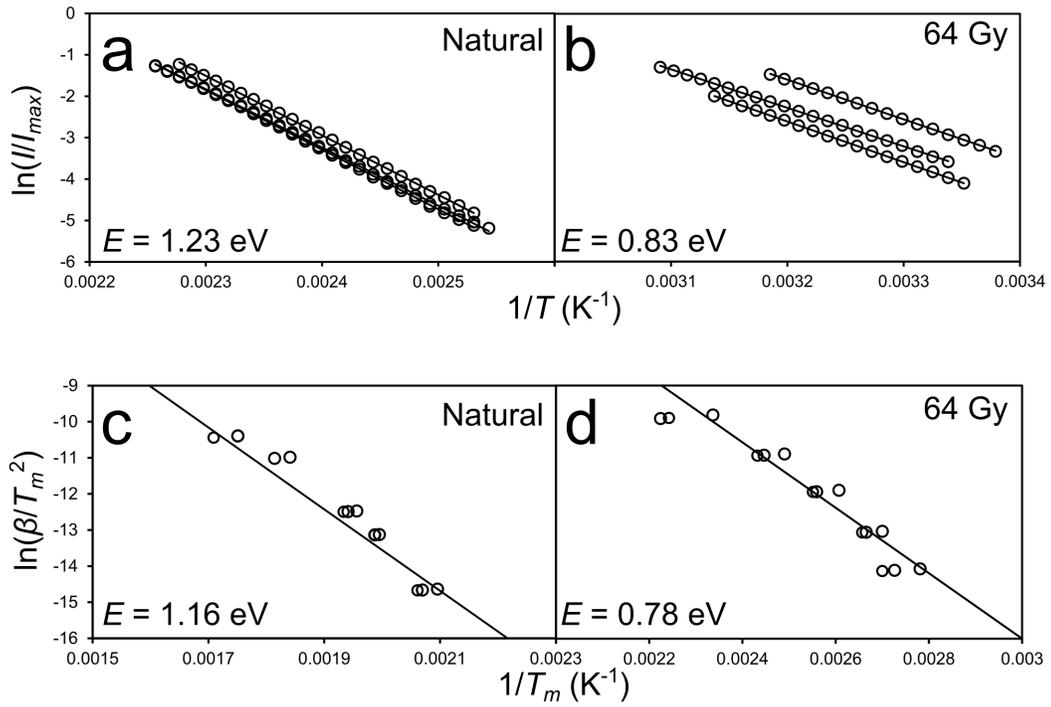


Figure 1: Apparent thermal trap depths for sample J0165 are calculated using the initial rise method (natural signal in (a) and regenerative signal after 64 Gy in (b)) and the various heating rates method (natural in (c) and 64 Gy in (d)). Note that the values calculated with the various heating rates method (1.16 and 0.78 eV) are slightly lower than those from the initial rise method (1.23 and 0.83 eV).

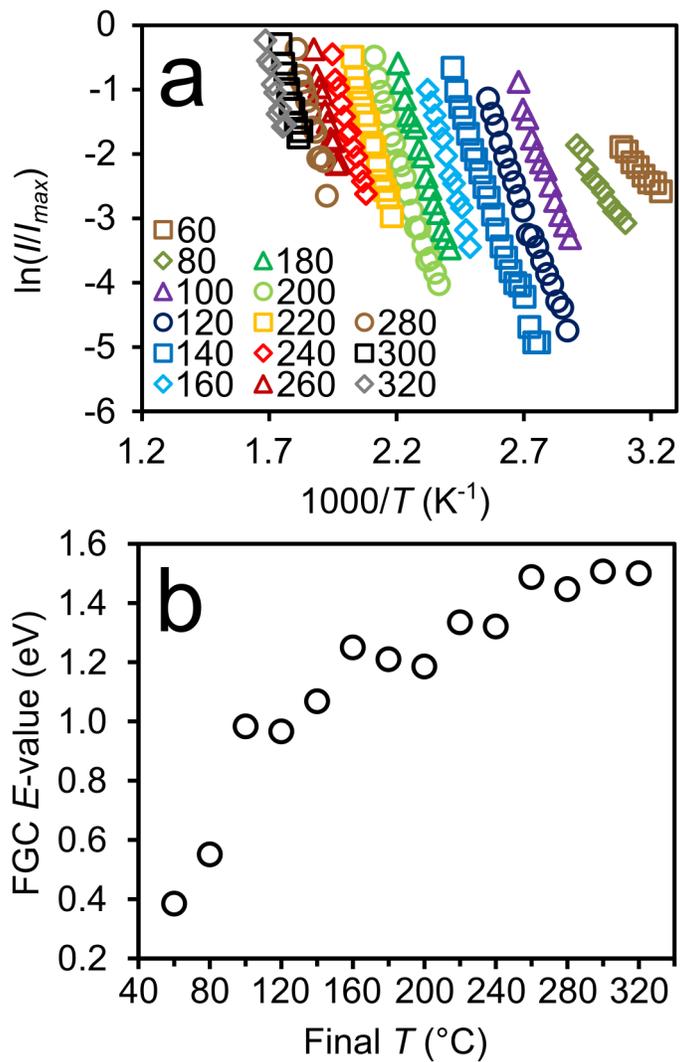


Figure 2: (a) Normalized thermoluminescence intensity plotted against inverse temperature for TL curves measured from  $T = 60$  to  $320$   $^{\circ}C$  in increments of  $20$   $^{\circ}C$  (sample J0165). (b) The data in (a) are fitted to calculate  $E$ -values for each of the TL curves within the fractional glow curve experiment.

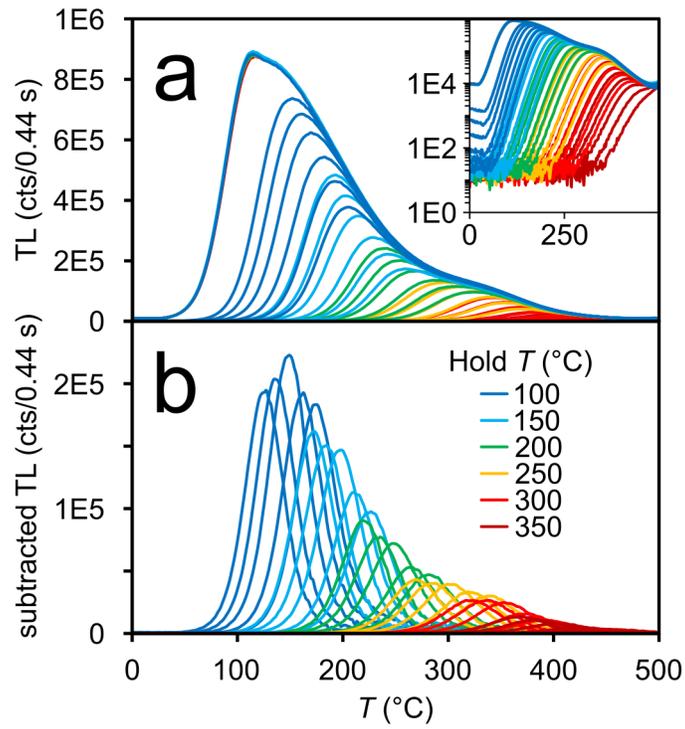


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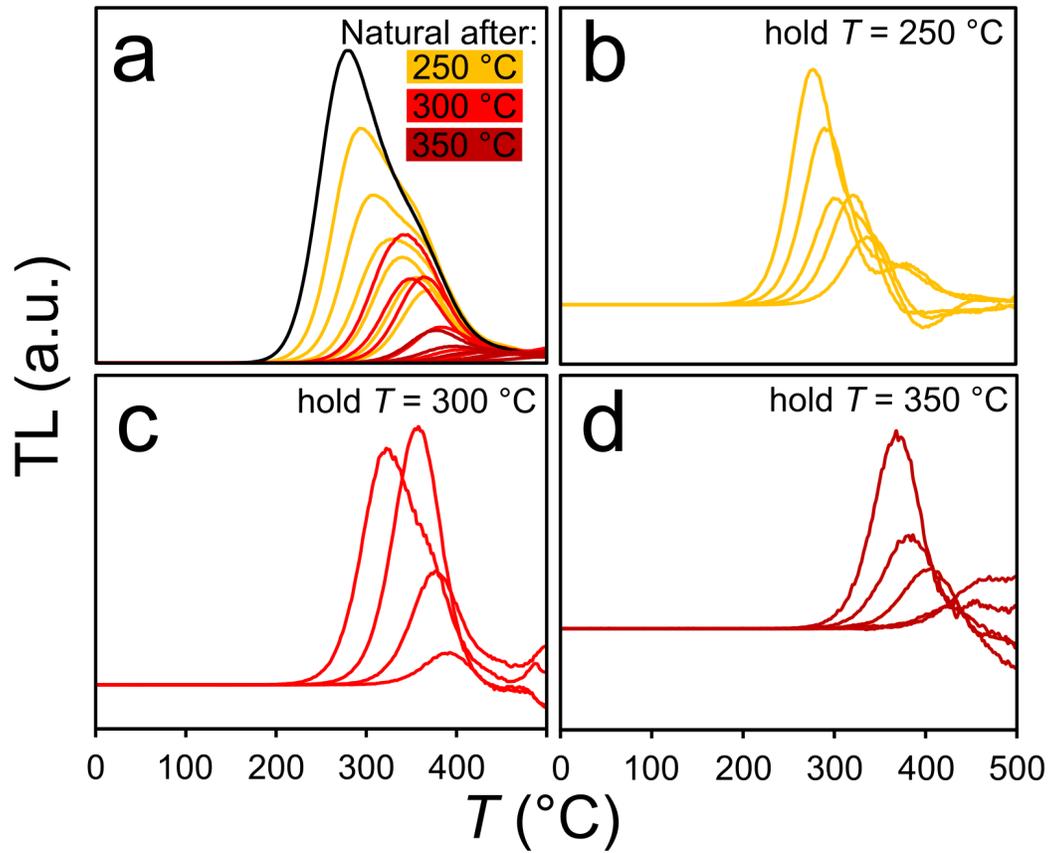


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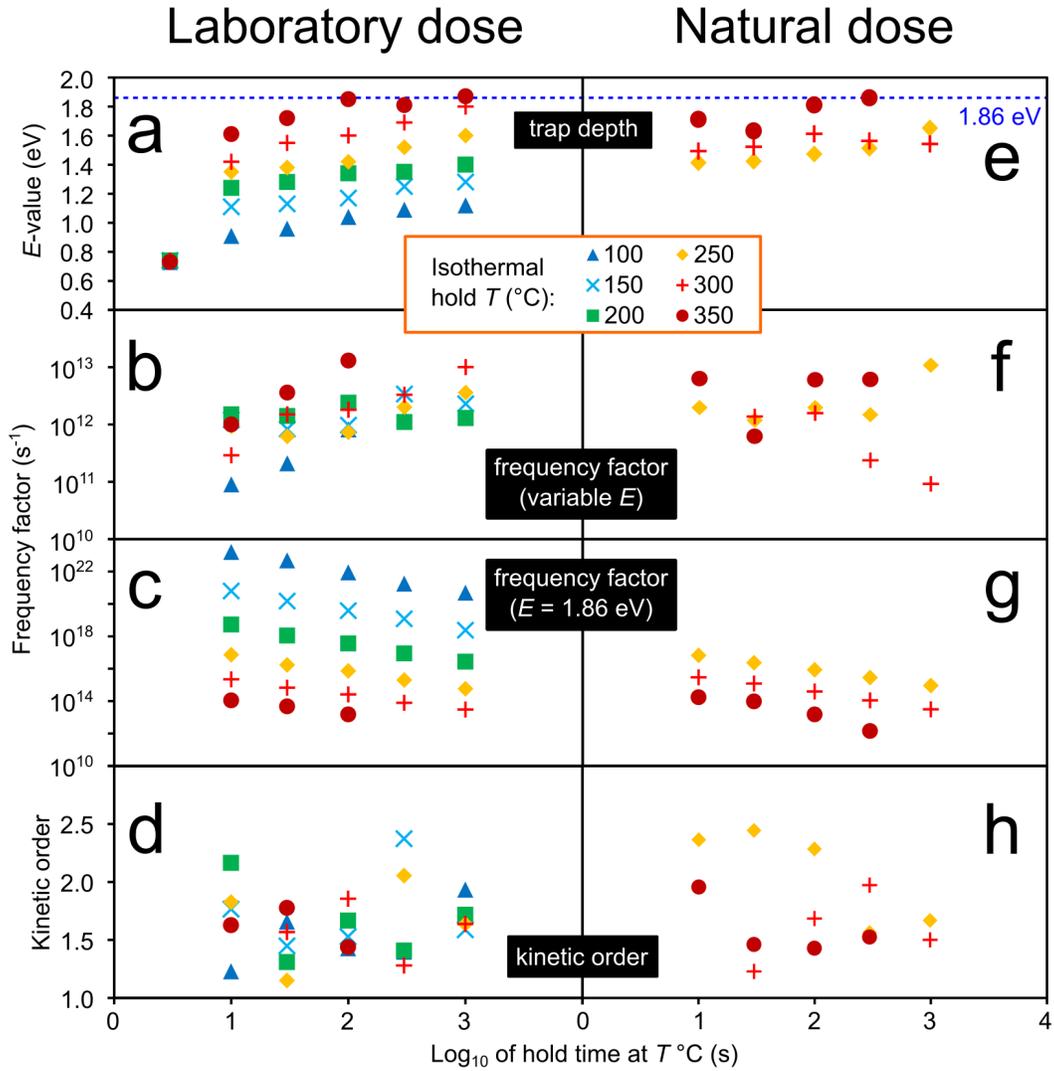


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