



UNIVERSITY OF LEEDS

This is a repository copy of *Photothermal conversion efficiency of nanofluids: An experimental and numerical study*.

White Rose Research Online URL for this paper:
<http://eprints.whiterose.ac.uk/106756/>

Version: Accepted Version

Article:

Jin, H, Lin, G, Bai, L et al. (3 more authors) (2016) Photothermal conversion efficiency of nanofluids: An experimental and numerical study. *Solar Energy*, 139. pp. 278-289. ISSN 0038-092X

<https://doi.org/10.1016/j.solener.2016.09.021>

© 2016. This manuscript version is made available under the CC-BY-NC-ND 4.0 license
<http://creativecommons.org/licenses/by-nc-nd/4.0/>

Reuse

Unless indicated otherwise, fulltext items are protected by copyright with all rights reserved. The copyright exception in section 29 of the Copyright, Designs and Patents Act 1988 allows the making of a single copy solely for the purpose of non-commercial research or private study within the limits of fair dealing. The publisher or other rights-holder may allow further reproduction and re-use of this version - refer to the White Rose Research Online record for this item. Where records identify the publisher as the copyright holder, users can verify any specific terms of use on the publisher's website.

Takedown

If you consider content in White Rose Research Online to be in breach of UK law, please notify us by emailing eprints@whiterose.ac.uk including the URL of the record and the reason for the withdrawal request.



eprints@whiterose.ac.uk
<https://eprints.whiterose.ac.uk/>

Photothermal Conversion Efficiency of Nanofluids: An Experimental and Numerical study

Haichuan Jin^{1,2} Guiping Lin¹ Lizhan Bai^{1,2} Muhammad Amjad²
Enio Bandarra³ Dongsheng Wen^{2,*}

¹ Laboratory of Fundamental Science on Ergonomics and Environmental Control, School of Aeronautic Science and Engineering,
Beihang University, Beijing 100191, PR China

² School of Chemical and Process Engineering, University of Leeds, Leeds, LS2 9JT, UK

³ Department of Mechanical Engineering, Federal State University of Uberlandia, Uberlandia, Brazil

Abstract: This work investigated experimentally the photothermal conversion efficiency (PTE) of gold nanofluids in a cylindrical tube under natural solar irradiation conditions, and compared with a developed 3-dimensional numerical model. The PTE of gold nanofluids was found to be much higher than that of pure water, and increased non-linearly with particle concentration, reaching 76% at a concentration of 5.8 ppm. Significant non-uniform temperature distribution was identified both experimentally and numerically, and a large uncertainty can be caused in the PTE calculation by using only one temperature measurement. A mathematical model was also developed to calculate the absorption efficiency without knowing the temperature field, which can be used to predict the theoretical PTE for nanofluids based on their optical properties only.

Keywords: nanoparticle; nanofluid; solar energy; photothermal conversion efficiency, direct absorption

30 **Nomenclature**

31	A	surface area exposed to solar radiation (m^2) / absorbance (-)
32	a_n	Mie coefficient to compute the amplitudes of the scattered field (-)
33	b_n	Mie coefficient to compute the amplitudes of the scattered field (-)
34	c	specific heat capacity ($\text{J}/(\text{kg} \cdot \text{K})$)
35	c_p	specific heat capacity ($\text{J}/(\text{kg} \cdot \text{K})$)
36	D	particle diameter (m)
37	E	spectral emissive power (W/m^3)
38	f_v	volume concentration (-)
39	h	convection coefficient ($\text{W}/(\text{m}^2 \cdot \text{K})$)
40	I	radiative intensity (W/m^2)
41	k	thermal conductivity ($\text{W}/(\text{m} \cdot \text{K})$)
42	k_f	imaginary part of the complex refractive index of the based fluid (-)
43	L	optical depth (m)
44	m	mass (kg) / relative refractive index (-)
45	n	complex refractive index (-) / order of accuracy
46	q	heat flux (W/m^2)
47	Q	efficiency factor for Mie scattering (-)
48	Q_r	radiative heat source in heat transfer equation
49	R	radius of cylinder experimental tube (m)
50	r	radius in integrating process (m)
51	\hat{s}	one specific direction which contains infinitesimal pencil of rays
52	T	temperature ($^{\circ}\text{C}$)
53	t	time (s)
54	u	velocity (m/s)

55	x	characteristic size of nanoparticles (-)
56		
57	Greek symbols	
58	β	extinction coefficient (m^{-1})
59	Φ	scattering phase function
60	ε	spectral emissivity
61	η	efficiency (-)
62	κ	absorption coefficient (m^{-1})
63	λ	wavelength of light in vacuum (m)
64	σ	scattering coefficient (m^{-1}) / Stefan-Boltzmann constant = $5.670 \times 10^{-8} (\text{W}/(\text{m}^2 \cdot \text{K}^4))$
65	Ω	solid angle
66	ρ	density
67	ψ_n	spherical Bessel function of order n
68	ξ_n	spherical Bessel function of order n
69		
70	Superscripts	
71	-	average value
72	\rightarrow	vector quantity
73	Subscripts	
74	abs	absorption
75	amb	ambient
76	b	black body
77	ext	extinction
78	f	fluid
79	η	wavelength range
80	i	direction number of light
81	n	nanoparticle
82	out	outlet
83	p	particle

84 sca scattering

85 s scattering

86 w water

87

88

89 **1 Introduction**

90 The concerns over excessive use of fossil energies and increasing environmental problems have accelerated
91 rapid development of solar energy technologies [1]. However, the difficulties in efficiently collecting solar
92 energy and converting it into useful energies (i.e., either electricity or heat) limit the extensive utilization of
93 solar energy [2]. Most of solar thermal collectors have ‘tube-in-plate’ arrangements, which absorb solar energy
94 on their surfaces and transfer heat to a working fluid running inside the tubes. Such an arrangement is
95 surface-limited, i.e., relying on the transfer of heat from a tube surface to the fluid inside. This would produce
96 a large temperature difference between the fluid and the absorber especially for high temperature applications
97 (i.e., solar thermal power plants) [3], and result in a limited solar energy utilization efficiency.

98 The concept of volumetric solar energy absorption, i.e., certain materials are seeded in a working fluid to
99 absorb solar energy directly within the fluid itself, was originated in 1970’s and coined as direct absorption
100 solar collector (DASC) [4]. In the concept, selective tube materials are used to allow most of the solar energy
101 pass through the wall and into the fluid, but prevent the radiation leakage from the fluid, forming a ‘thermal
102 trapping’ phenomenon[5]. In this way, the highest temperature exists in the fluid and the overall conversion
103 efficiency from solar energy to heat can be largely improved due to reduced re-radiation heat loss.

104 The use of nanoparticles as effective absorption media is a recent development. It has been reported that
105 adding very diluted particles into base fluid could enhance the radiative absorbing efficiency and improve the
106 overall heat transfer rate due to their large specific surface areas [6]. A range of nanoparticles including metal
107 (such as Cu, Au, and Ag), metal oxide (such as TiO_2 , Al_2O_3) and carbon materials [7–11] have been
108 investigated under laboratory [3,12–14] and natural sunlight conditions [15–17]. Some results were very
109 encouraging. For instance, the solar conversion efficiency of a 0.01% graphite nanofluid was found to be as
110 high as 122.7% of that of a conventional surface absorbing collector [12]. Some metallic nanoparticles such as
111 gold and silver have also drawn wide attentions because of their Surface Plasmon Resonance effects (SPR)

112 [18,19]. For these kinds of materials, the resonance frequencies of conduction electrons are usually in the
113 visible-light spectrum , which is weakly absorbed by most of the heat transfer fluids but occupies nearly half of
114 the total solar radiation energy [20]. Zhang et al. [14] showed that a very low concentration of gold
115 nanoparticles (i.e., mass concentration of 0.0028%) could increase the photothermal conversion efficiency
116 (PTE) of the base fluid by 20%, reaching an impressive specific absorption rate (SAR) of ~10 kW/g under
117 laboratory conditions. In another study conducted outdoor, up to 144% enhancement in the stored thermal
118 energy was obtained for 6.5 ppm silver nanoparticle-based direct absorption under natural sunlight conditions
119 [15]. However it shall be noted that only one temperature was measured in most of the published work [21–25]
120 and a uniform temperature assumption was used to calculate the energy efficiency, neglecting the temperature
121 distribution within the fluid. Considering a reduced radiative intensity along the path of the absorbing liquid,
122 there shall exist large temperature non-uniformity in the fluid, whose neglect may lead to inaccurate
123 calculations for the PTE and disguise some key parameters (such as the optical depth) in optimizing the
124 collector design.

125 Quite a few studies [3,24,26–28] have built numerical models to simulate the radiative and heat transfer
126 process in nanofluids. Unfortunately, most of these simulative studies were based on the ideal solar spectrum,
127 and ignored that the spectral emissive power distribution is affected by the atmosphere’s absorption, especially
128 in the infrared spectrum. As the radiation properties of nanoparticles are highly spectral dependent, any
129 numerical work should consider the solar spectrum associated with realistic experimental conditions. A
130 theoretical method to predict photothermal efficiency directly based on nanoparticle’s basic physical properties
131 with respect to particle loadings and optical depth has yet to be established.

132 To overcome the issues reviewed above, a detailed investigation of the photothermal conversion
133 characteristics of gold nanoparticle dispersions was conducted both experimentally and numerically. Gold
134 nanoparticles were synthesized via a one-pot reaction, and the experiments were performed under natural

135 sunlight conditions with multiple temperature measurement. A 3-dimensional model was developed to simulate
136 the experimental results, which was followed by a parametric investigation of the influence of particle
137 concentration, solar radiation intensity and receiver geometrical parameters on the solar conversion efficiency.
138 A new method to theoretically predict the photothermal conversion efficiency of nanoparticle dispersions was
139 proposed according to the radiative transfer equation.

140 **2 Experimental investigation**

141 **2.1 Gold nanoparticle dispersions formulation**

142 In this study, a one-step method [29] was used to produce gold nanoparticle dispersions and different
143 concentrations were prepared. A typical procedure is introduced below as an illustration, i.e., CASE 6 in **Table**
144 **1**. Here 2.5×10^{-7} mol HAuCl_4 was dispersed into 50 ml DI water in a three-necked flask under
145 heating. A magnetic blender was used to stir the liquid until boiling. Boiling was continued for 10 min and then
146 50 ml of 1×10^{-5} mol/L sodium citrate was added. The solution turned dark blue within 30 seconds and the
147 final color became wine red after being heated for an additional 20 minutes. The size and shape of CASE 6
148 identified by a transmission electron microscopy are shown in **Fig. 1a**. **Table. 1** represents 6 cases of gold
149 nanoparticle dispersions. The dispersions were maintained good stability for over two months, and were used
150 for the below experiments without further purification and separation.

151 An UV/Vis spectrometer (UV-1800 SHIMADZU UV Spectrophotometer) was applied to measure the
152 absorption spectrum of the nanoparticle dispersions at different concentrations. As shown in **Fig. 1b**, due to the
153 strong surface Plasmon resonance of gold nanoparticles in the visible light spectrum[14], a peak absorption
154 wavelength was found at 526 nm for all the dispersions, which is consistent with the TEM analysis that the
155 size of gold nanofluids was about 20 nm. According to the Beer-Lambert Law (known as Beer's Law) [30],
156 also seen in Eq. 8 below, there is a linear relationship between the absorbance and the concentration of the
157 sample, as shown in the inset.

158 2.2 Experimental settings

159 The experimental setup in this study is showed in **Fig. 2a** and **b**. The tubes used in this experiment were
160 custom-made from high temperature resistant quartz glass. The tube contained a vacuum interlayer to reduce
161 the impact of convection from outside air. The sample fluids were placed in the inside-tube with a diameter of
162 25 mm and length of 300 mm. The outside-tube had a diameter of 60 mm with two small-bore pipes, which
163 were used to fix temperature sensors.

164 As shown in **Fig. 2b**, three T-type thermocouples (Omega TT-T-40-SLE) with a precision of ± 0.5 K were
165 placed evenly in the bottom, middle, top of the sample fluids along the optical depth, and two more
166 thermocouples were applied to measure the air inside and outside the tube (i.e., the ambient), respectively. A
167 data acquisition (Agilent 34970A) system was used to measure the thermocouple voltage signal and then
168 transferred it into digital form, recorded in a PC under LabVIEW environment. A solar radiation intensity
169 sensor was employed to measure the solar intensity, and the data was also recorded in the PC.

170 3 Experimental results analysis

171 3.1 Temperature variation

172 Example temperature curves of gold nanofluids and DI water under varied natural solar intensity are shown
173 in **Fig. 3a**, together with the air temperature inside and outside the tube. A slow increase in DI water
174 temperature is observed and the solar intensity (I) was varied from about 400 W/m^2 to 700 W/m^2 . Clearly the
175 temperature variation of both water and nanofluids lags behind, but gold nanofluids show much more rapid
176 temperature increase under the same intensity than pure water. For example, the bulk temperature is increased
177 by ~ 21 K after 60 minutes' heating for a GNP concentration of 5.8 ppm, more than three times of pure water
178 temperature rise. Here the average temperature from three thermocouples, i.e., $(\bar{T} = (T_{TC1} + T_{TC2} + T_{TC3})/3)$,
179 was used to represent the fluid temperature.

180 To reveal the possible temperature difference inside the fluid, **Fig. 3b** shows the temperature profiles of

181 three thermocouples for 5.8 ppm gold nanofluid and DI water respectively under the same condition as Fig.
 182 3a. . Consistent large temperature difference was found for the nanofluid. A maximum 2.6 K temperature
 183 difference was found for nanofluid after 28 minutes' illumination, but for DI water, the maximum temperature
 184 difference was in a relative small region (i.e., less than 0.5 K). Considering the potential large temperature
 185 difference in the nanofluid, as will be revealed by the numerical model, the location of the thermocouple
 186 would affect the calculated PTE significantly if only one measurement was used.

187 **Fig. 3c** shows an example of the influence of solar intensity variation on the PTE for 0.72 ppm gold
 188 nanofluid. For the constant solar intensity case, the temperature increased smoothly and reached the
 189 equilibrium point after two hours' illumination; but for varied solar intensity (cloudy day), the same nanofluid
 190 exhibits a changing tendency, which follows the pattern of solar intensity variation. Generally, salient
 191 temperature difference among three thermocouples can be observed under both solar intensities, being larger
 192 for a higher solar intensity. Further non-uniform temperature distribution and its effects on the solar efficiency
 193 is discussed in **section 5**.

194 3.2 Efficiency and SAR

195 The average photothermal conversion efficiency (PTE) is defined as the ratio of the internal energy increase
 196 of the fluid to the total incoming radiation input:

$$197 \quad \eta = \frac{(c_w m_w + c_n m_n) \Delta T}{IA \Delta t} \approx \frac{c_w m_w}{IA} \cdot \frac{\Delta \bar{T}}{\Delta t} \quad (1)$$

198 where $\Delta \bar{T}$ is the average temperature difference ($\Delta \bar{T} = (\Delta T_{TC1} + \Delta T_{TC2} + \Delta T_{TC3}) / 3$). Comparing with the
 199 base water, thermal energy stored in gold nanoparticles is negligible owing to extremely low concentration: i.e.,
 200 a maximum of 5.8 ppm in volume (0.01% in mass).

201 To quantify the capability of nanoparticles in absorbing solar energy, the specific absorption rate (SAR) is
 202 employed[15]:

$$SAR = \frac{(c_w m_w + c_n m_n) \Delta \bar{T}_n - c_w m_w \Delta \bar{T}_w}{m_n \Delta t} \quad (2)$$

203 The calculated PTEs within the measurement uncertainty of $\pm 3\%$ under two different solar intensities are
 204 shown in **Fig. 4**, which is in general similar to previous studies [14,15]. The PTE reaches 45.5% even at a
 205 relatively low concentration (0.36 ppm), increased by 163% comparing with the base water (17.3% at
 206 $I = 950 \text{ W/m}^2$). The highest PTE of gold nanofluids is 73.6%, which is more than 4 times of DI water and
 207 more promising than what found in previous studies [12,14,31]. The PTE increases rapidly under low particle
 208 concentrations and approaches asymptotically to a constant value when the concentration reaches a certain
 209 status (i.e., 1 ppm for $I = 600 \text{ W/m}^2$). A lower PTE value (i.e., 10% smaller) is found for the high solar
 210 intensity case, which is assumed to be related to an increased heat loss. **Fig. 4** also shows that SAR rapidly
 211 decreases with the increasing concentration below 1 ppm, and the highest SAR reaches 2.715 kW/g at
 212 nanoparticle concentration of 0.36 ppm for $I = 950 \text{ W/m}^2$ solar intensity, which is in the broad range of
 213 previous studies [14,15]. Further investigation with numerical results will be conducted regarding to PTE and
 214 SAR in **section 5**.

216 **4 Numerical model of direct absorbing solar energy for nanofluids**

217 **4.1 Solar radiation and Mie scattering theory**

218 In order to get better understanding of radiative heat transfer in gold nanofluids, a numerical model was built
 219 in this work. Realistic solar irradiation profile was calculated based on ASTM G173-03 Reference Spectra [32].
 220 As shown in **Fig. 5a**, the solar irradiation on the ground is distinctly different from that at top of atmosphere,
 221 especially for spectral emissive power in infrared, which is due to the intense absorption of H_2O and CO_2 in
 222 atmosphere. The result from integrating the spectral emissive power with wavelength shows that nearly 99% of
 223 solar radiation energy at sea level exists in 0.2~3 μm . As solar emissive power takes part of nearly 43% in
 224 infrared, which can be seen in the inset figure, considering the actual solar spectrum on the ground becomes
 225 essential for solar thermal applications. For the purpose of proper simplification [3], spectral emissive power

226 for sun (T=5762 K) and nanofluid (T=303 K) has been calculated and separated into two bands on wavelength
 227 of 3 μm (see in **Fig. 5b**); Solar irradiation wavelength locates mainly below 3 μm with a peak at 480 nm,
 228 while wavelength for nanofluid of 303 K is beyond 3 μm .

229 In the present modeling, the characteristic size employed in radiative transfer equation is as $x_\lambda = \pi D / \lambda$,
 230 where D represents the diameter of nanoparticles. For our experimental study, the diameter of gold
 231 nanoparticles is 20 nm characterized by TEM as shown in **Fig. 1a**. Although it is appropriate to use simplified
 232 equations, i.e., the Rayleigh scattering approximation [30], to calculate the absorption coefficient, since the
 233 diameter of suspended particles in the experiments are much smaller than the wavelength of irradiation
 234 ($x_\lambda \ll 1$). The original Mie scattering equations [30] is preferred to identify the optical properties for spherical
 235 nanoparticle suspensions in order to obtain detailed scattering parameters, such as the efficiencies for
 236 scattering, absorption, backscattering, averaged absolute-square E-field. The Mie scattering equations can be
 237 described by:

$$238 \quad a_n = \frac{m\psi_n(mx)\psi_n'(x) - \psi_n(x)\psi_n'(mx)}{m\psi_n(mx)\xi_n'(x) - \xi_n(x)\psi_n'(mx)} \quad (2-a)$$

$$239 \quad b_n = \frac{\psi_n(mx)\psi_n'(x) - m\psi_n(x)\psi_n'(mx)}{\psi_n(mx)\xi_n'(x) - m\xi_n(x)\psi_n'(mx)} \quad (2-b)$$

$$240 \quad Q_{\text{sca}}(\lambda) = \frac{2}{x^2} \sum_{n=1}^{\infty} (2n+1) \left[|a_n|^2 + |b_n|^2 \right] \quad (2-c)$$

$$241 \quad Q_{\text{ext}}(\lambda) = \frac{2}{x^2} \sum_{n=1}^{\infty} (2n+1) \text{Re}(a_n + b_n) \quad (2-d)$$

242 where the functions $\psi_n(x)$ and $\xi_n(x)$ are spherical Bessel functions[30] of order n (n= 1, 2,..) and the
 243 primes refer to the derivatives with respect to the argument, and m represents the ratio of refractive indexes,
 244 calculated by:

$$245 \quad m = \frac{n_{\text{particles}}}{n_{\text{fluid}}} \quad (3)$$

246 where $n_{\text{particles}}$ and n_{fluid} are the complex refractive index [33–35] of gold and based fluid relative to the
 247 ambient medium, respectively. In consideration of relative low concentrations of nanofluids developed for
 248 solar thermal applications, particles should absorb and scatter light independently according to the scattering
 249 map [30]. With such a consideration, the absorption coefficient can be calculated from the below equation:

$$250 \quad \kappa(\lambda) = \kappa_p(\lambda) + \kappa_f(\lambda) = \frac{3\pi}{2} \frac{f_v Q_{\text{abs}}(\lambda)}{D} + \frac{4\pi k_f(\lambda)}{\lambda} \quad (4)$$

251 4.2 Radiative transfer equation and heat transfer equation

252 The property of spectral intensity can be described simultaneously by the radiative transfer equation, known
 253 as RTE [30]:

$$254 \quad \hat{s} \cdot \nabla I_\eta = \kappa_\eta I_{\text{b}\eta} - \beta_\eta I_\eta + \frac{\sigma_{s\eta}}{4\pi} \int_{4\pi} I_\eta(\hat{s}_i) \Phi_\eta(\hat{s}_i, \hat{s}) d\Omega_i \quad (5-a)$$

$$255 \quad \nabla \cdot \mathbf{q}_\eta = \kappa_\eta \left(4\pi I_{\text{b}\eta} - \int_{4\pi} I_\eta d\Omega \right) \quad (5-b)$$

$$256 \quad \kappa_\eta = \beta_\eta - \sigma_{s\eta} \quad (5-c)$$

257 where I_η represents the radiative intensity of wavelength range $\lambda_{\eta_1} \rightarrow \lambda_{\eta_2}$ in the direction \hat{s}_i , $I_{\text{b}\eta}$ is the
 258 re-emission of nanofluid, $\Phi_\eta(\hat{s}_i, \hat{s})$ is called the scattering phase function and describes the probability that
 259 a ray from one direction \hat{s}_i , will be scattered into a certain other direction \hat{s} , κ_η , β_η and σ_η are the
 260 absorption, extinction and scattering coefficient, respectively. Spectral radiative heat flux \mathbf{q}_η can be obtained
 261 by integrating the radiative intensity with the solid angle Ω .

262 Transient heat transfer equation is shown as:

$$263 \quad \rho c_p \frac{\partial T}{\partial t} + \rho c_p \bar{\mathbf{u}} \cdot \nabla T + \nabla \cdot \bar{\mathbf{q}} = Q_r \quad (6-a)$$

$$264 \quad \bar{\mathbf{q}} = -k \nabla T \quad (6-b)$$

$$265 \quad Q_r = -\int_0^\infty \mathbf{q}_\eta(\lambda) d\lambda \quad (6-c)$$

266 The boundary condition and initial condition are:

$$267 \quad -\bar{\mathbf{n}} \cdot \bar{\mathbf{q}} = \varepsilon \sigma (T_{\text{amb}}^4 - T^4) + h(T_{\text{amb}} - T) \Big|_{\text{contact_air}} \quad (7-a)$$

268 $T_{t=0} = T_i$ (7-b)

269 where h is the convection coefficient due to convection from one end of the tube contacted with air outside,
 270 whose contribution to the result is small and a typical value of $15 \text{ W}/(\text{m}^2 \cdot \text{K})$ is used in this work.

271 **4.3 Predicted absorption efficiency for nanofluids**

272 For most of our applied particles, scattering contribution can be neglected according to the Mie theory.
 273 Furthermore, the radiative equations can be simplified as a 1-dimensional transfer process. Under these
 274 assumptions, an analytical solution for Eq. (6-a) can be obtained:

275
$$E_\lambda(L) = E_{\lambda,(y=0)} e^{-\beta_\lambda L} + E_{\text{bb},\lambda} (1 - e^{-\beta_\lambda L})$$
 (8)

276 where E represents the spectral emissive power with unit of W/m^3 . In order to investigate the spectrum
 277 behavior at wavelength below $1.1 \mu\text{m}$, which is the upper limit of our spectrophotometer, black body
 278 re-emissive radiation can be neglected due to the small intensity of re-emission, seen in **Fig. 5b**. Coupled with
 279 Eq. 5, Eq. 9 can be further simplified as:

280
$$-\log\left(\frac{E_{\text{out}}(\lambda)}{E_0(\lambda)}\right) = \beta_\lambda \cdot L \cdot \log_{10} e = \left(\frac{3\pi Q_{\text{abs}}(\lambda)}{2D} \cdot \log_{10} e\right) \cdot f_v \cdot L = A(\lambda)$$
 (9)

281 Eq.10 represents the analytic derivation process of the famous Beer-Lambert Law [30]. With these
 282 assumptions, a new method is proposed to evaluate the total absorption efficiency (ABE) for a given
 283 nanoparticle concentration and optical depth, which is the theoretical maximum possible photothermal
 284 conversion efficiency:

285
$$\eta(L, f_v) = \frac{\int_{0.2\mu\text{m}}^{3\mu\text{m}} E_0(\lambda) \left(1 - 10^{-A(\lambda) \frac{L}{L_0}}\right) d\lambda}{\int_{0.2\mu\text{m}}^{3\mu\text{m}} E_0(\lambda) d\lambda} = \frac{\int_{0.2\mu\text{m}}^{3\mu\text{m}} E_0(\lambda) (1 - e^{-\kappa(\lambda, f_v)L}) d\lambda}{\int_{0.2\mu\text{m}}^{3\mu\text{m}} E_0(\lambda) d\lambda}$$
 (10)

286 Further investigation will be discussed in next section with experimental results.

287 **4.4 Solution methodology**

288 A high-order algorithm has been used to solve Eqs. (3) ~ (5) and (11) to calculate coefficients related to

289 optical properties for nanofluids and photothermal conversion efficiency, with functions powered by Matlab
290 associated with COMSOL Multiphysics, similar to the one described by Kluczyk[36]. It should be noticed that
291 obtaining an analytical solution to Eqs. (6) ~ (8) is extremely difficult as the 3-dimensional transient heat
292 transfer equations coupled with transient RTE equations are complicated partial differential equations. A finite
293 element method (FEM) was employed to solve the equations numerically in COMSOL. A predefined Heat
294 Transfer with Radiation in Participating Media equations [30] together with user defined functions (radiative
295 transfer equation) were used to describe thermal and radiative energy transfer process. The discretization of the
296 simulative space was conducted with the appliance of a built-in non-structured meshing COMSOL algorithm.
297 The maximum element size inside nanofluid was chosen as 0.2 cm, and the maximum was chosen as 0.05 cm
298 for the surface with respect to radiative and convective heat loss, which mainly happens at the surface. A direct
299 solver called MULTifrontal Massively Parallel sparse direct Solver (MUMPS) with tolerance of 10^{-5} was
300 adopted to numerically solve the matrices assembled according to the governing equations and boundary
301 conditions described above. The initial and boundary conditions were originated from experimental
302 measurement (such as temperature of inside air and the ambient). With Mie scattering, RTE, transient heat
303 transfer equations coupled with varying boundary conditions, it is very demanding on the computational power.
304 The Advanced Research Computing (ARC) at University of Leeds is used to solve the equations in in parallel.

305 **5. Numerical results and comparison**

306 **5.1 Validation against experimental data**

307 The absorption coefficients for gold nanoparticles and working fluid (water) calculated by Mie scattering
308 theory (Eqs.3-5) can be seen in **Fig. 6a**, where the volume concentration of gold particles is 5.8 ppm. The
309 absorption coefficient which cannot be obtained through experiments is a key parameter for 3D heat transfer
310 and radiative transfer equations. As shown in **Fig. 6a**, gold nanoparticles contribute the absorption in the
311 visible light spectrum and the base fluid (water) is more effective in the infrared range. To examine the

312 reliability of our calculation, the absorbance from numerical results based on Eq.10 is compared with
313 experimental value in **Fig. 6b**. The simulation result is generally in agreement with the experimental value.
314 The experimental deviation in 600~800 nm is due to the existence of some bigger particles in the fluids,
315 which could make the absorbance red shift.

316 Based on experimental boundary and initial conditions, as an example, the comparison of the simulation
317 with experimental results under constant solar intensity (i.e., 950 W/m²) is shown in **Fig. 7**. The temperature
318 rise of 1.45 ppm gold nanofluid is much higher than that of DI water, for example ~25 K for nanofluid and ~12
319 K for water. However, both nanofluid and water exhibit non-uniform temperature distribution during the
320 illumination, as much as 4.4 K and 1.9 K temperature difference can be reached, respectively. The high
321 temperature of the top layer (TC1) shows that solar energy is mostly absorbed in the surface layer. The low
322 temperature at the bottom layer is related to effects of solar intensity decay along the optical path, and the
323 limited heat conduction capacity. After about three hours' heating, nanofluid can maintain approximately an
324 equilibrium temperature (~ 57 °C), but for water the maximum is only ~ 45 °C, indicating that gold nanofluid
325 even with very low concentration can significantly enhance the energy conversion from solar radiation to
326 thermal form.

327 **5.2 Temperature distribution profile inside the tube**

328 Non-uniform temperature distribution can be further demonstrated through T-profile in 3-dimensional fluid
329 (gold nanoparticles with volume concentration of 1.45 ppm, water as based fluid, under constant solar intensity,
330 i.e., 950 W/m²), which can be seen in **Fig. 8a**. The result in this case shows that the temperature at the up
331 middle of the tube along Y direction is higher than the bulk value. Generally, the highest temperature is located
332 inside the nanofluid volume (about 0.8 cm to the illuminated surface), for example 44 °C in this case.
333 Clearly larger temperature difference (i.e., more than 6 K) for the whole considered volume can be seen in **Fig.**
334 **8b**, comparing with the 3 thermocouple measurement in **Fig. 7**, which illustrates the danger of using individual

335 measured values to calculate PTE.

336 **5.3 Efficiency prediction and comparison**

337 Most of the prior studies such as Andrej et al. [3] were based on experimental or simulative temperature
338 field to optimize the efficiency of nanofluid-based DASC. Here we report a mathematical method to predict
339 the absorption efficiency (ABE), which represents the maximum possible efficiency for any nanofluid-based
340 solar system, according to optical properties, seen in Eq. (11).

341 **Fig. 9a** shows the absorption efficient in different wavelength. Clearly comparing to the water case, much
342 higher ABE is observed for gold nanofuids across the whole solar spectrum. The spectrum ABE increases with
343 the particle concentration, and nearly 100% ABE is achieved for 5.8 ppm nanofluids in the visible light
344 spectrum, which is related to the surface plasmon resonance phenomenon of gold nanoparticles. The small
345 depression at ~900 nm is associated with the poor absorbency performance in the near-infrared, which can
346 be explained by the Mie scattering theory.

347 **Fig. 9b** and **c** show the ABE as a function of optical length L and particle concentration f_v . The initial
348 efficiency of the nanofluids receiver increases rapidly with L , then asymptotically reaches 100%. This result is
349 similar to Zhang et al.[14]'s experimental observation, where it showed clearly that the PTE increased
350 nonlinearly with volume concentration but no proper explanation was provided. As shown in radiative transfer
351 equations (Eq. 9), the radiative transport energy is consumed inside nanofluid exponentially, and the PTE
352 should exhibit a nonlinear dependence on the particle concentration.

353 **Fig. 9** also reveals the important parameters that determine the maximum possible solar receiver efficiency.
354 The impact of the optical depth L and particle concentration f_v is embedded in the exponential term as
355 $L \cdot f_v$ in Eq. 9. **Fig. 9b** reveals that both optical concentration and optical depth should be in a relative small
356 values to achieve an optimized effect, as higher volume concentration of nanoparticle (i.e., more than 10 ppm
357 for $L=0.05$ m) increases the efficiency slightly. Comparing to nanofluids, the efficiency depends more on the

358 optical depth to reach a relative high value (i.e., 25 m for 80%). Overall, employing GNPs enhances the ABE
 359 significantly compared with pure water.

360 In order to compare the prediction of ABE against experimental and simulative data (i.e., where the optical
 361 depth is not a constant), a modified equation is proposed by integrating the efficiency with the radius, as:

$$362 \quad \eta(f_v) = \frac{\int_0^R \int_{0.2\mu\text{m}}^{3\mu\text{m}} E_0(\lambda) (1 - e^{-2\kappa(\lambda, f_v)r}) d\lambda dr}{R \int_{0.2\mu\text{m}}^{3\mu\text{m}} E_0(\lambda) d\lambda} \quad (11)$$

363 where R is the radius of cylindrical tube. The ABE becomes an only function of volume concentration. The
 364 ABE is compared with three ways of photothermal conversion efficiencies based on temperature field, i)
 365 from one measured thermocouple, ii) from the average temperature measured by three thermocouples, and iii)
 366 from the simulated temperature field. For the simulated data, the efficiency is obtained by considering
 367 temperature difference in each computational nodes, as:

$$368 \quad \eta = \frac{\sum_{i=1}^n c_w \rho_w V_i \Delta T_i}{IA\Delta t} \quad (12)$$

369 **Fig. 10a** shows reasonably good agreement from four different methods. It can be expected that ABE from
 370 Eq. 12 is the theoretical maximum efficiency, in which the scattering and heat leakage are not considered. It
 371 can be used as an efficient method for nanoparticle selection and solar collector optimization without the need
 372 of measuring the temperature field. Photothermal efficiency based only on one temperature point shows a large
 373 underestimation of the PTE for all samples. For example, the PTE is 12% lower than that from the
 374 experiment-determined average temperature at $f_v=5.8$ ppm.

375 What's more, the temperature used to determine PTE is usually at the beginning when the heat leak is not
 376 significant, the temperature difference (i.e., 4.4 °C for 1.45 ppm under 950 W/m² solar intensity) inside
 377 nanofluid is comparable to this temperature range (10-15 °C). Neglecting of non-uniform temperature
 378 distribution could cause significant inaccuracy (with an uncertainty of 29%-44%) in calculating the energy

379 efficiency. To illustrate such an effect, **Fig. 10b** shows the maximum differences in temperature and PTE based
380 on the simulation result under a solar intensity of 1000 W/m^2 and particle size of 20 nm. Here the temperature
381 elevation employed to determine PTE is 10 K from the beginning of the experiment. Depending on the
382 measurement location, as high as 67% uncertainty could be obtained for the case of 5.8 ppm gold nanofluid.

383 The temperature non-uniformity issue will become more and more serious when the volume concentration
384 of nanofluids increases or the radiation intensity increases (i.e., under focused solar intensities). Quite a few
385 recent studies [13,16,17,37] have shown that under a focused solar light, i.e., via a typical Fresnel lens, rapid
386 steam can be produced from plasmonic nanofluids albeit the bulk solution was still under subcooled conditions.
387 In one study [16], by using very dilute gold nanoparticles (16.7 ppm) under a solar concentration of 1000
388 times, , steam generation efficiency was calculated as high as 80%, and only 20% of the absorbed solar energy
389 was used to increase the bulk fluid temperature. However, there is still a strong debate if the steam can be
390 produced around heated nanoparticles. Considering the potential large temperature difference in the fluids
391 under a focused solar intensity, there is a possibility that steam could be produced on the strongly heated
392 surface layer, where strong evaporation or even boiling can occur. Further exploration of this issue is ongoing,
393 and will be presented in the future.

394 **6 Conclusions**

395 Both outdoor experiments and simulation were conducted in this work to analyses the photothermal
396 conversion characteristics of gold nanofluids, and a new method was proposed to predict the theoretical
397 efficiency based only the optical properties. The main conclusions can be summarized as:

398 (1) The photothermal conversion efficiency of gold nanofluids is much higher than that of pure water, and
399 increased non-linearly with particle concentration, reaching 76% at a concentration of 5.8 ppm.

400 (2) Significant non-uniform temperature distribution was identified inside the fluid, indicating that the
401 consideration of average temperature is needed to obtain a reliable PTE.

402 (3) A new method was developed to predict radiative absorption efficiency based on the optical properties of
403 nanofluid, without the need of knowing the temperature field inside the fluid. The method can be used to
404 identify the performance of nanoparticles and optimize solar absorbers efficiently.

405 (4) A radiative heat transfer model coupled with the Mie scattering theory was developed. This model can
406 predict temperature profile successfully, which confirms the existence of large temperature difference inside
407 nanofluids.

408 (5) The comparison of various efficiencies shows that Eq. (11) can be used to predict the theoretical
409 maximum photothermal conversion efficiency, and using only one-point temperature measurement could cause
410 significant inaccuracy, i.e., uncertainty of 67% for 12.75 ppm gold nanofluid at 1000 W/m² solar intensity.

411 **ACKNOWLEDGEMENT**

412 This work was supported by the EU Marie Curie Actions-International Incoming Fellowships
413 (FP7-PEOPLE-2013-IIF-626576), and the author Haichuan Jin also acknowledges the financial support for his
414 visiting study at the University of Leeds from the China Scholarship Council (CSC) under the Grant
415 No.201506020031.

416

417 **References**

- 418 [1] Sukhatme SP. Solar thermal power generation. *J Chem Sci* 1997;109:521–31.
419 doi:10.1007/BF02869211.
- 420 [2] Gupta HK, Agrawal G Das, Mathur J. An experimental investigation of a low temperature Al₂O₃-H₂O
421 nanofluid based direct absorption solar collector. *Sol Energy* 2015;118:390–6.
422 doi:10.1016/j.solener.2015.04.041.
- 423 [3] Lenert A, Wang EN. Optimization of nanofluid volumetric receivers for solar thermal energy
424 conversion. *Sol Energy* 2012;86:253–65. doi:10.1016/j.solener.2011.09.029.
- 425 [4] Minardi JE, Chuang HN. Performance of a “black” liquid flat-plate solar collector. *Sol Energy*
426 1975;17:179–83. doi:10.1016/0038-092X(75)90057-2.
- 427 [5] Arai N, Itaya Y, Hasatani M. Development of a “volume heat-trap” type solar collector using a
428 fine-particle semitransparent liquid suspension (FPSS) as a heat vehicle and heat storage medium
429 Unsteady, one-dimensional heat transfer in a horizontal FPSS layer heated by thermal radiatio. *Sol*
430 *Energy* 1984;32:49–56. doi:10.1016/0038-092X(84)90048-3.
- 431 [6] Rahman MM, Al-Mazroui W a., Al-Hatmi FS, Al-Lawatia M a., Eltayeb I a. The role of a convective
432 surface in models of the radiative heat transfer in nanofluids. *Nucl Eng Des* 2014;275:382–92.
433 doi:10.1016/j.nucengdes.2014.05.028.
- 434 [7] Gan Y, Qiao L. Radiation-enhanced evaporation of ethanol fuel containing suspended metal
435 nanoparticles. *Int J Heat Mass Transf* 2012;55:5777–82. doi:10.1016/j.ijheatmasstransfer.2012.05.074.
- 436 [8] Hussain I, Graham S, Wang Z, Tan B, Sherrington DC, Rannard SP, et al. Size-controlled synthesis of
437 near-monodisperse gold nanoparticles in the 1–4 nm range using polymeric stabilizers. *J Am Chem Soc*
438 2005;127:16398–9. doi:10.1021/ja055321v.
- 439 [9] Hwang SH, Yun J, Jang J. Multi-Shell Porous TiO₂ Hollow Nanoparticles for

- 440 Enhanced Light Harvesting in Dye-sensitized Solar Cells. *Adv Funct Mater* 2014;24:7619–26.
441 doi:10.1002/adfm.201401915.
- 442 [10] Mock JJ, Barbic M, Smith DR, Schultz D a., Schultz S. Shape effects in plasmon resonance of
443 individual colloidal silver nanoparticles. *J Chem Phys* 2002;116:6755–9. doi:10.1063/1.1462610.
- 444 [11] Otanicar TP, Phelan PE, Prasher RS, Rosengarten G, Taylor R a. Nanofluid-based direct absorption
445 solar collector. *J Renew Sustain Energy* 2010;2. doi:10.1063/1.3429737.
- 446 [12] Luo Z, Wang C, Wei W, Xiao G, Ni M. Performance improvement of a nanofluid solar collector based
447 on direct absorption collection (DAC) concepts. *Int J Heat Mass Transf* 2014;75:262–71.
448 doi:10.1016/j.ijheatmasstransfer.2014.03.072.
- 449 [13] Ni G, Miljkovic N, Ghasemi H, Huang X, Boriskina S V, Lin C. Volumetric solar heating of nano fl
450 uids for direct vapor generation 2015.
- 451 [14] Zhang H, Chen HJ, Du X, Wen D. Photothermal conversion characteristics of gold nanoparticle
452 dispersions. *Sol Energy* 2014;100:141–7. doi:10.1016/j.solener.2013.12.004.
- 453 [15] Bandarra Filho EP, Mendoza OSH, Beicker CLL, Menezes A, Wen D. Experimental investigation of a
454 silver nanoparticle-based direct absorption solar thermal system. *Energy Convers Manag*
455 2014;84:261–7. doi:10.1016/j.enconman.2014.04.009.
- 456 [16] Neumann O, Urban AS, Day J, Lal S, Nordlander P, Halas NJ. Solar vapor generation enabled by
457 nanoparticles. *ACS Nano* 2013;7:42–9. doi:10.1021/nn304948h.
- 458 [17] Neumann O, Feronti C, Neumann AD, Dong A, Schell K, Lu B, et al. Compact solar autoclave based
459 on steam generation using broadband light-harvesting nanoparticles. *Proc Natl Acad Sci U S A*
460 2013;110:11677–81. doi:10.1073/pnas.1310131110.
- 461 [18] Pérez-Juste J, Pastoriza-Santos I, Liz-Marzán LM, Mulvaney P. Gold nanorods: Synthesis,
462 characterization and applications. *Coord Chem Rev* 2005;249:1870–901.

- 463 doi:10.1016/j.ccr.2005.01.030.
- 464 [19] Eustis S, el-Sayed M a. Why gold nanoparticles are more precious than pretty gold: noble metal surface
465 plasmon resonance and its enhancement of the radiative and nonradiative properties of nanocrystals of
466 different shapes. *Chem Soc Rev* 2006;35:209–17. doi:10.1039/b514191e.
- 467 [20] Thuillier G, Hersé M, Labs D, Foujols T, Peetermans W, Gillotay D, et al. The solar spectral irradiance
468 from 200 to 2400 nm as measured by the SOLSPEC spectrometer from the ATLAS and EURECA
469 missions. *Sol Phys* 2003;214:1–22. doi:10.1023/A:1024048429145.
- 470 [21] He Q, Wang S, Zeng S, Zheng Z. Experimental investigation on photothermal properties of nanofluids
471 for direct absorption solar thermal energy systems. *Energy Convers Manag* 2013;73:150–7.
472 doi:10.1016/j.enconman.2013.04.019.
- 473 [22] Kasaeian A, Daviran S, Azarian RD, Rashidi A. Performance evaluation and nanofluid using capability
474 study of a solar parabolic trough collector. *Energy Convers Manag* 2015;89:368–75.
475 doi:10.1016/j.enconman.2014.09.056.
- 476 [23] Ladjevardi SM, Asnaghi A, Izadkhast PS, Kashani AH. Applicability of graphite nanofluids in direct
477 solar energy absorption. *Sol Energy* 2013;94:327–34. doi:10.1016/j.solener.2013.05.012.
- 478 [24] Tyagi H, Phelan P, Prasher R. Predicted Efficiency of a Low-Temperature Nanofluid-Based Direct
479 Absorption Solar Collector. *J Sol Energy Eng* 2009;131:041004. doi:10.1115/1.3197562.
- 480 [25] Yousefi T, Veysi F, Shojaeizadeh E, Zinadini S. An experimental investigation on the effect of
481 Al₂O₃–H₂O nanofluid on the efficiency of flat-plate solar collectors. *Renew Energy* 2012;39:293–8.
482 doi:10.1016/j.renene.2011.08.056.
- 483 [26] Hordy N, Rabilloud D, Meunier J-L, Coulombe S. High temperature and long-term stability of carbon
484 nanotube nanofluids for direct absorption solar thermal collectors. *Sol Energy* 2014;105:82–90.
485 doi:10.1016/j.solener.2014.03.013.

- 486 [27] Kabeel a. E, El-Said EMS. Applicability of flashing desalination technique for small scale needs
487 using a novel integrated system coupled with nanofluid-based solar collector. *Desalination*
488 2014;333:10–22. doi:10.1016/j.desal.2013.11.021.
- 489 [28] Khullar V, Tyagi H, Hordy N, Otanicar TP, Hewakuruppu Y, Modi P, et al. Harvesting solar thermal
490 energy through nanofluid-based volumetric absorption systems. *Int J Heat Mass Transf*
491 2014;77:377–84. doi:10.1016/j.ijheatmasstransfer.2014.05.023.
- 492 [29] Chen H-J, Wen D. Ultrasonic-aided fabrication of gold nanofluids. *Nanoscale Res Lett* 2011;6:198.
493 doi:10.1186/1556-276X-6-198.
- 494 [30] Modest MF. *Radiative Heat Transfer*. vol. 1. Academic Press; 2003.
495 doi:http://dx.doi.org/10.1016/B978-012503163-9/50021-7.
- 496 [31] Parvin S, Nasrin R, Alim M a. Heat transfer and entropy generation through nanofluid filled direct
497 absorption solar collector. *Int J Heat Mass Transf* 2014;71:386–95.
498 doi:10.1016/j.ijheatmasstransfer.2013.12.043.
- 499 [32] Gueymard CA. The sun’s total and spectral irradiance for solar energy applications and solar radiation
500 models. *Sol Energy* 2004;76:423–53. doi:10.1016/j.solener.2003.08.039.
- 501 [33] McPeak KM, Jayanti S V, Kress SJP, Meyer S, Iotti S, Rossinelli A, et al. Plasmonic Films Can Easily
502 Be Better: Rules and Recipes. *ACS Photonics* 2015;2:326–33. doi:10.1021/ph5004237.
- 503 [34] Babar S, Weaver JH. Optical constants of Cu, Ag, and Au revisited. *Appl Opt* 2015;54:477.
504 doi:10.1364/AO.54.000477.
- 505 [35] Hale GM, Querry MR. Optical Constants of Water in the 200-nm to 200-microm Wavelength Region.
506 *Appl Opt* 1973;12:555–63. doi:10.1364/AO.12.000555.
- 507 [36] Kluczyk K, Jacak W. Damping-induced size effect in surface plasmon resonance in metallic
508 nano-particles: Comparison of RPA microscopic model with numerical finite element simulation

509 (COMSOL) and Mie approach. *J Quant Spectrosc Radiat Transf* 2016;168:78–88.
510 doi:10.1016/j.jqsrt.2015.08.021.

511 [37] Hogan NJ, Urban AS, Ayala-Orozco C, Pimpinelli A, Nordlander P, Halas NJ. Nanoparticles heat
512 through light localization. *Nano Lett* 2014;14:4640–5. doi:10.1021/nl5016975.

513

514 **Table captions:**

515 Table 1 Different cases of gold nanoparticles dispersions.

516

517 **Figure captions:**

518 **Fig. 1.** Nanoparticle characterization: (a) TEM image of gold nanoparticles (CASE 6); (b) **A:** absorbance of gold nanoparticle
519 dispersions under different volume fraction; **B:** peak absorbance variation with concentrations in volume.

520 **Fig. 2.** Experimental setup: (a) Soar thermal illumination experiment under nature sunlight conditions (located on the roof of
521 Human Machine and Environment Engineering Building in Beihang University in Beijing, 39° 59' 5.49" North, 116° 21' 18.70"
522 East.); (c) A schematic illustration of experimental setup.

523 **Fig. 3.** (a) Temperature profile of differently diluted nanofluids under varied solar intensity (cloudy, solar intensity from about
524 400 W/m² to 700 W/m²); (b) Experimentally obtained increasing temperature profile of TC1-TC3 located inside the tube,
525 concentration of nanofluids is 5.8 ppm and solar intensity is varied. (c) Comparison of three thermocouple signals for 0.72 ppm
526 gold nanofluid under different solar intensities: constant solar intensity (i.e., about 950 W/m²) and varied solar intensity (i.e.,
527 from 400 W/m² to 700 W/m²).

528 **Fig. 4.** Variation of photothermal conversion efficiency (η) and specific absorption rate (SAR) with volume concentration for
529 gold nanofluids under different solar intensities.

530 **Fig. 5.** (a) ASTM G173-03 Reference Spectra from literature, inset shows the solar energy distribution along with wavelength in
531 percentage (integrating spectral emissive power with wavelength divided by irradiation intensity). (b) Calculation of spectral
532 emissive power for sun (T=5762 K) and nanofluid (T=303 K), where spectral distribution is separated into two bands, A
533 ($\lambda < 3000$ nm) and B ($\lambda > 3000$ nm).

534 **Fig.6.** (a) Real and imaginary parts of \mathbf{m} (Eq. (2)) and calculated absorption coefficients for gold nanoparticles (\mathcal{K}_p), working
535 fluid (\mathcal{K}_f) and total (\mathcal{K}) according to Mie scattering theory; (b) Absorbance from Eq. (10) in comparison with results from
536 spectrophotometer.

537 **Fig. 7.** Experimentally obtained increasing temperature profile of TC1-TC3 located inside the tube, compared with numerical
538 results from 3D model concentration of nanofluids is 1.45 ppm and solar intensity is constantly about 950 W/m².

539 **Fig. 8.** (a) Schematic for numerical simulation of a 3-D volumetric solar receiver based on gold nanofluid of concentration 1.45

540 ppm with normal nature solar radiation $I=900 \text{ W/m}^2$, where the geometry parameters can be seen in (b), solar radiation is in -y
541 direction; (b) Temperature profiles in cross-section for nanofluid after 30 minutes' illumination (Global Tilt) at $x=0 \text{ cm}$.

542 **Fig. 9.** (a) Spectral efficiency which is defined as below in this paper:

543
$$\eta_{\lambda}(\lambda_c) = \left[\int_{0.2\mu\text{m}}^{\lambda_c} E_0(\lambda) (1 - e^{-\kappa(\lambda)L}) d\lambda \right] / \left[\int_{0.2\mu\text{m}}^{\lambda_c} E_0(\lambda) d\lambda \right];$$
 (b) Absorption efficiency (ABE) as a function of optical length L for 5

544 different volume concentrations (inset: DI water); (c) ABE as a function of volume concentration f_v for 5 different optical lengths.

545 **Fig. 10.** (a) Comparison of the experimentally obtained photothermal conversion efficiency, efficiency calculated from 3D model
546 and predicted absorption efficiency, result based on only one thermocouple; (b) Maximum efficiency uncertainty caused by
547 non-uniform temperature distribution in nanofluids.

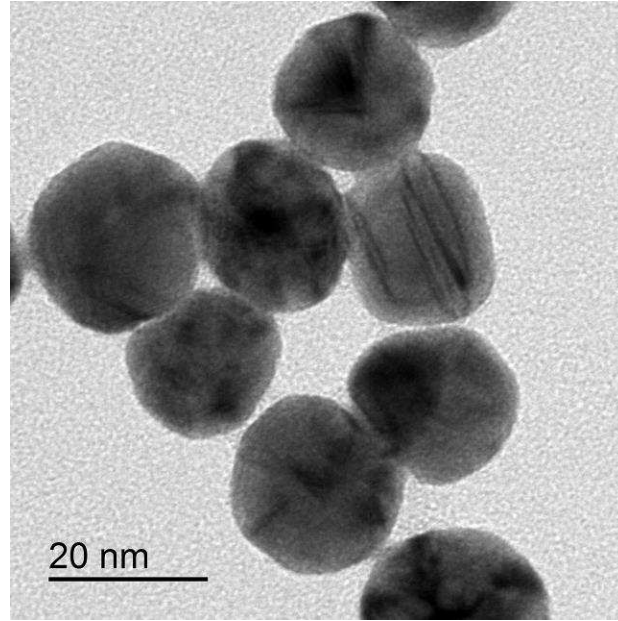
548

Table 1 Different cases of gold nanoparticles dispersions

Case No.	Reagents	Reaction time	Color	Peak size
1	HAuCl ₄ : 100ml 2.4×10 ⁻⁶ mol/L Sodium Citrate: 10ml 0.034mol/L	30 min	Wine red	9nm
2	HAuCl ₄ : 100ml 2.4×10 ⁻⁶ mol/L Sodium Citrate: 5ml 0.034mol/L	30 min	Orange	15nm
3	HAuCl ₄ : 100ml 2.4×10 ⁻⁶ mol/L Sodium Citrate: 2ml 0.034mol/L	40 min	Pink	25nm
4	HAuCl ₄ : 100ml 2.4×10 ⁻⁶ mol/L Sodium Citrate: 0.7ml 0.034mol/L	60 min	Crystal violet	65nm
5	HAuCl ₄ : 100ml 2.4×10 ⁻⁶ mol/L Sodium Citrate: 0.3ml 0.034mol/L	90 min	Ash black	120nm
6	HAuCl ₄ : 50ml 5×10 ⁻⁶ mol/L Sodium Citrate: 50ml 1×10 ⁻⁵ mol/L	20 min	Amaranth	19nm

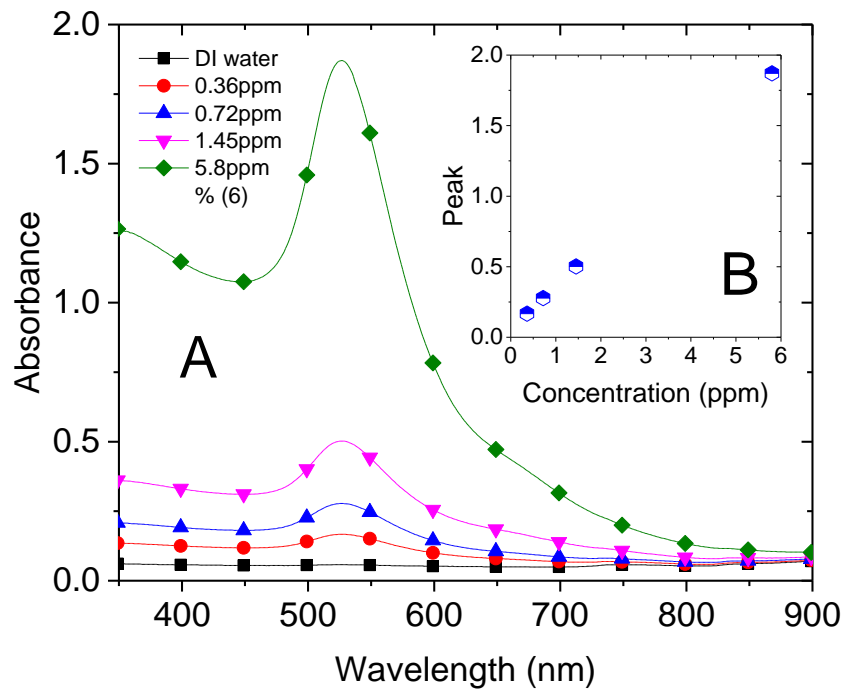
551

(a)



552

(b)

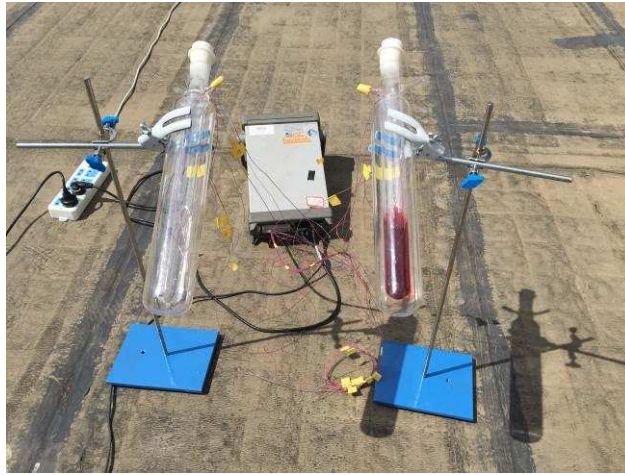


553

554 **Fig. 1.** Nanoparticle characterization: (a) TEM image of gold nanoparticles (CASE 6); (b) **A:** spectral-dependent absorbance of

555 gold nanofluid under different volume fractions; **B:** peak absorbance variation with nanoparticle concentrations.

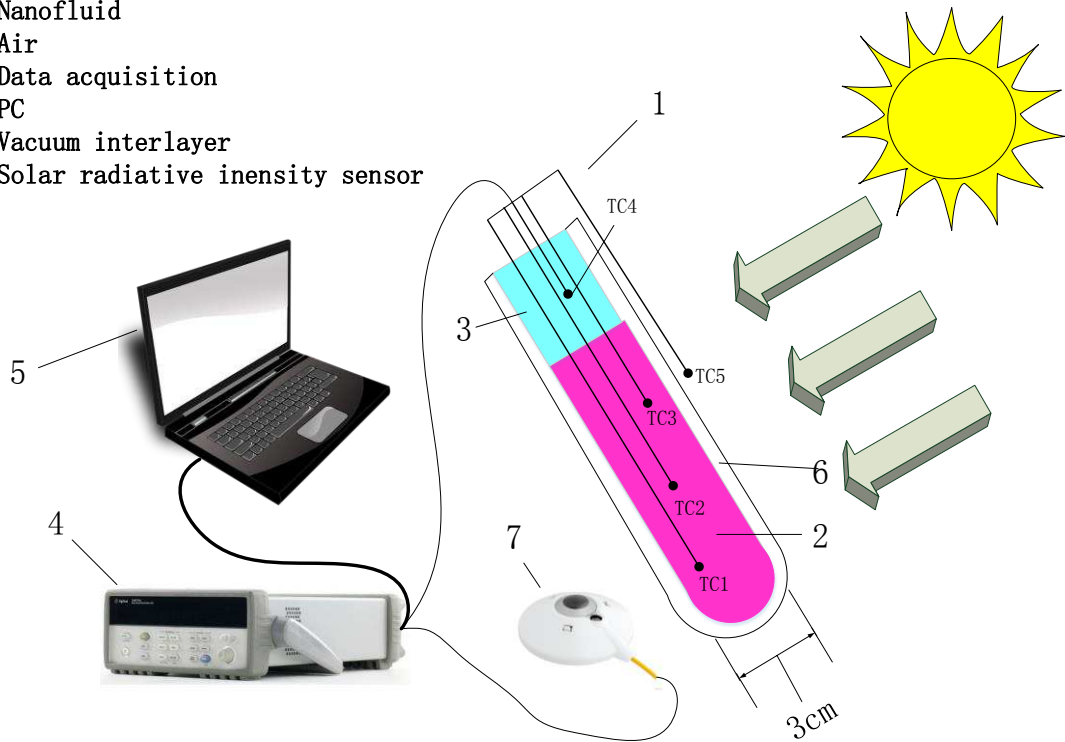
(a)



556

(b)

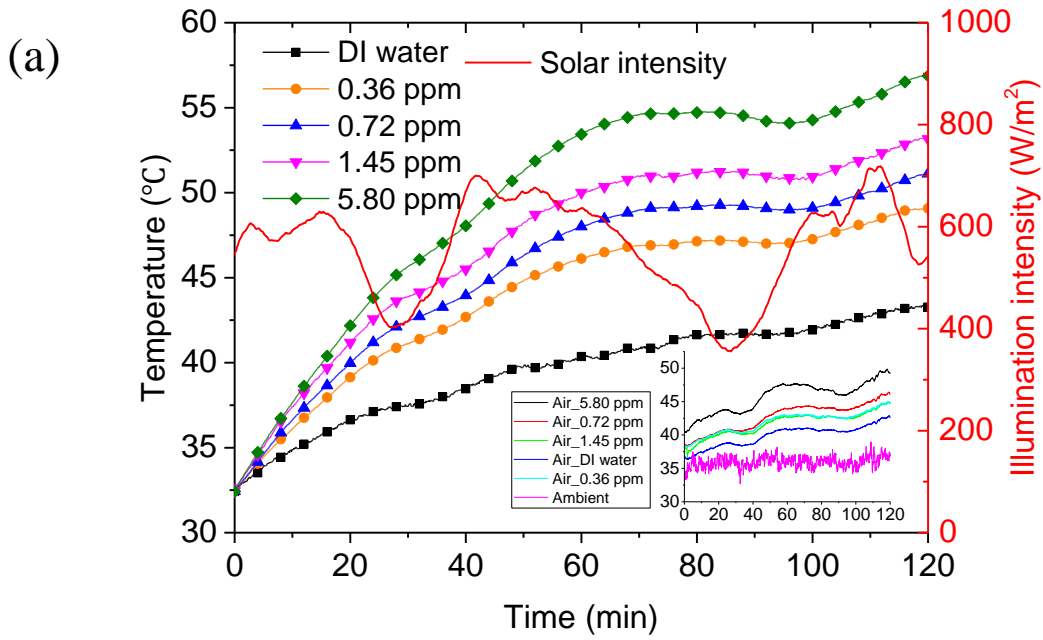
1. Thermocouples
2. Nanofluid
3. Air
4. Data acquisition
5. PC
6. Vacuum interlayer
7. Solar radiative intensity sensor



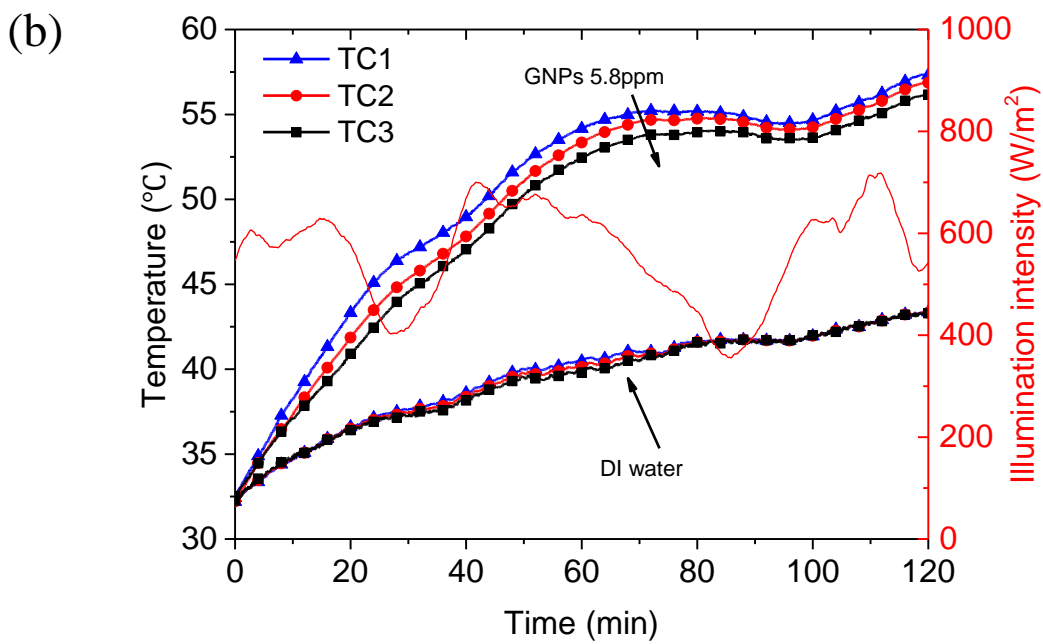
557

558 **Fig. 2.** Experimental setup: (a) Soar thermal illumination experiment under natural sunlight conditions (location $39^{\circ} 59' 5.49''$

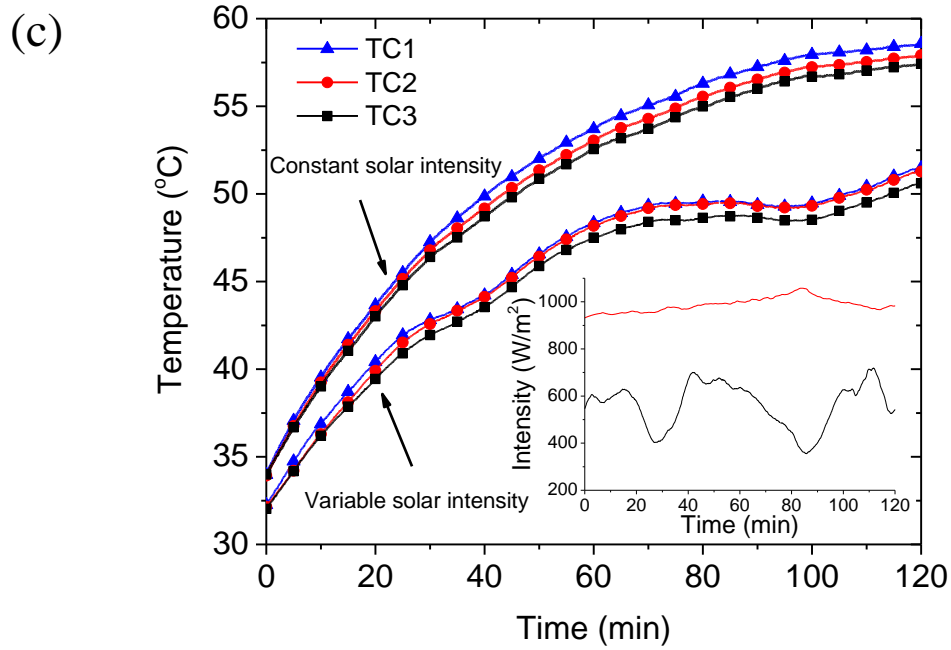
559 North, $116^{\circ} 21' 18.70''$ East.) and (b) A schematic illustration of the experimental setup.



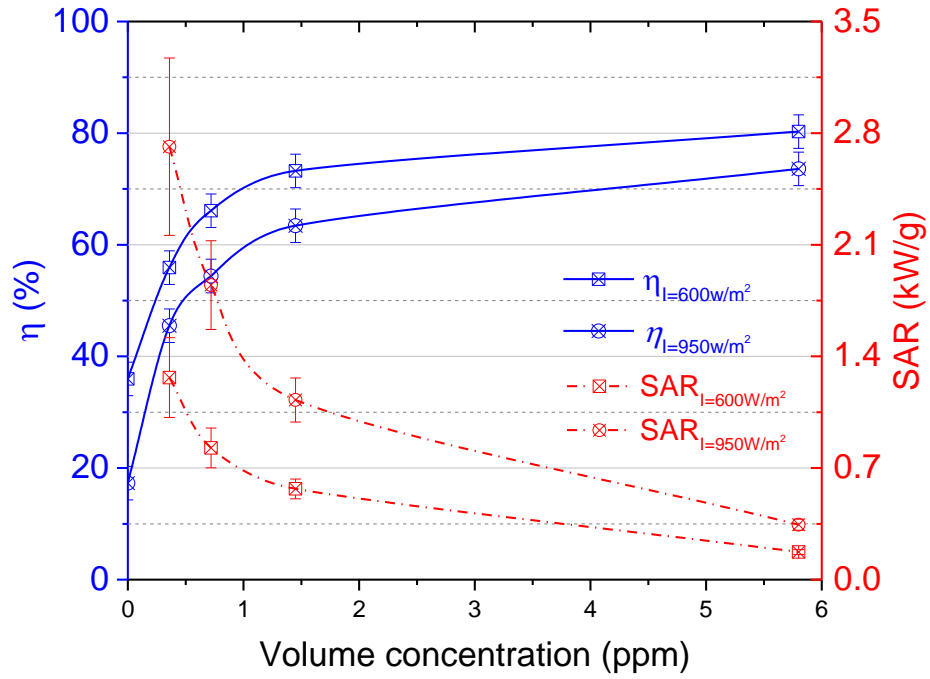
560



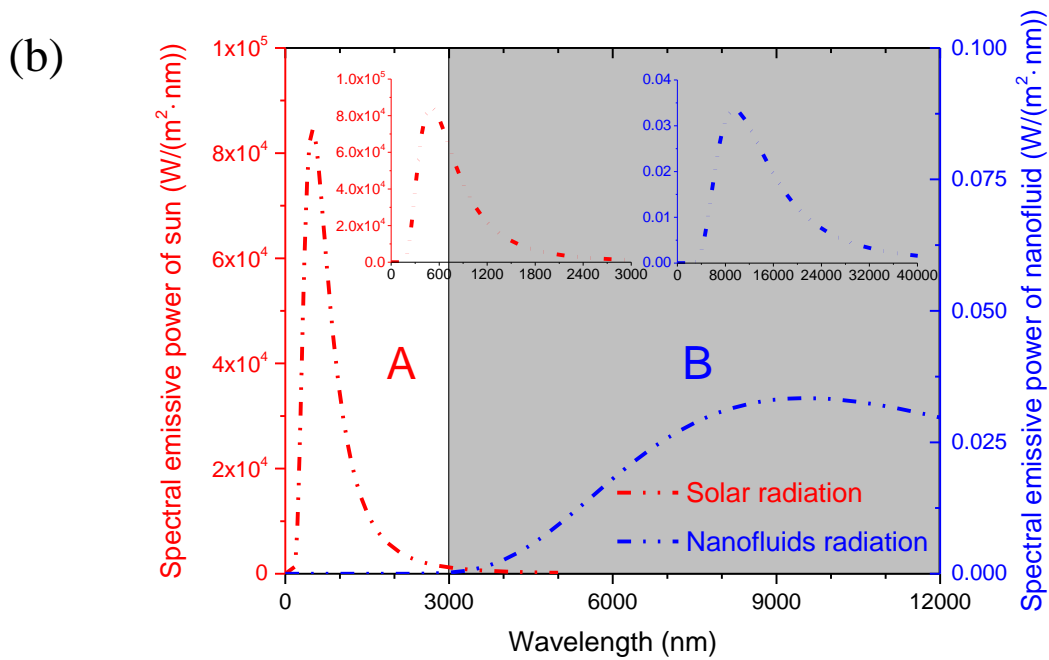
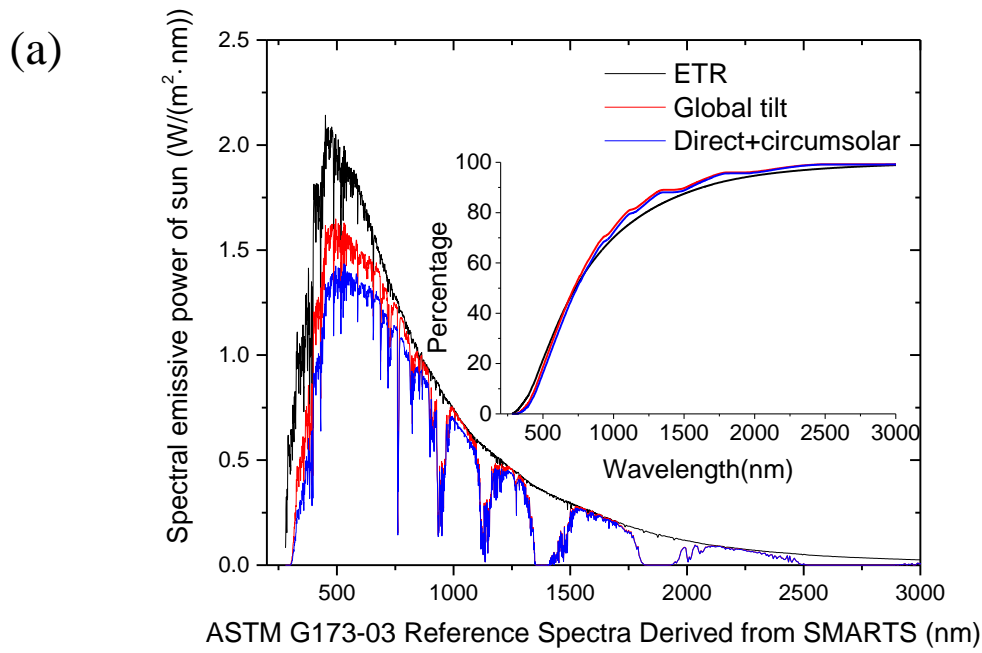
561



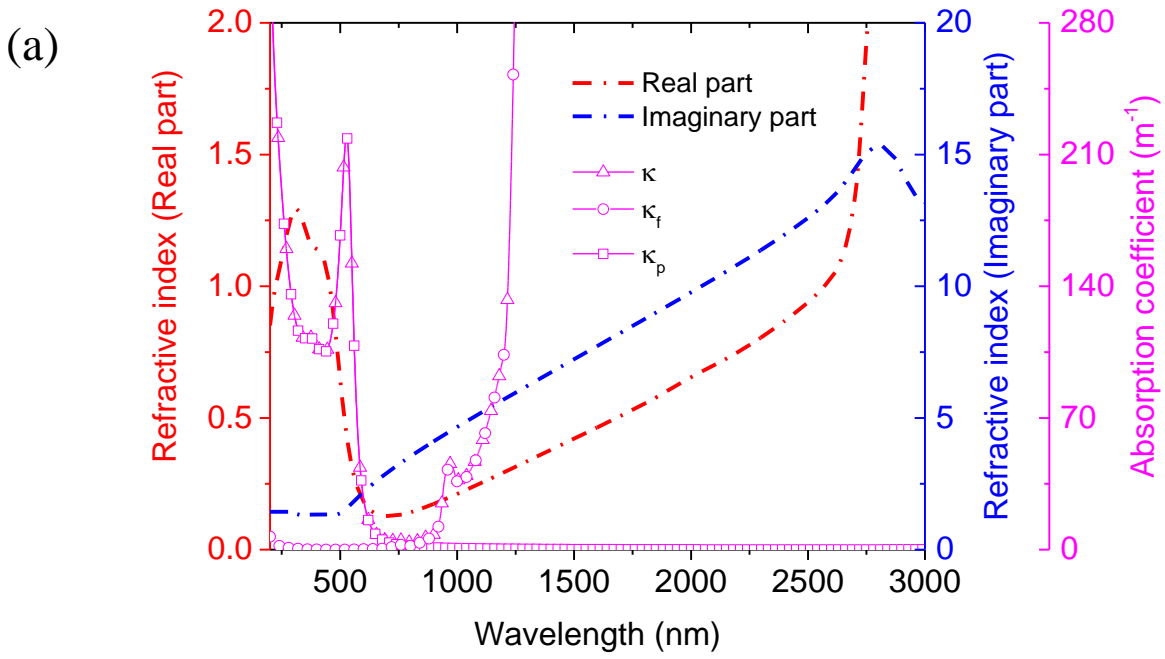
562
 563
 564 **Fig. 3.** (a) Example temperature profile of differentnanofluids under a cloudy day (solar intensity varied from about 400 W/m² to
 565 700 W/m²); (b) Temperature profile of TC1-TC3 located inside the fluid for 5.8 ppm nanofluids in the cloudy day. (c)
 566 Comparison of three thermocouple profiles for 0.72 ppm gold nanofluid under different solar intensities: constant solar
 567 intensity (i.e., about 950 W/m²) and varied solar intensity (i.e., from 400 W/m² to 700 W/m²).



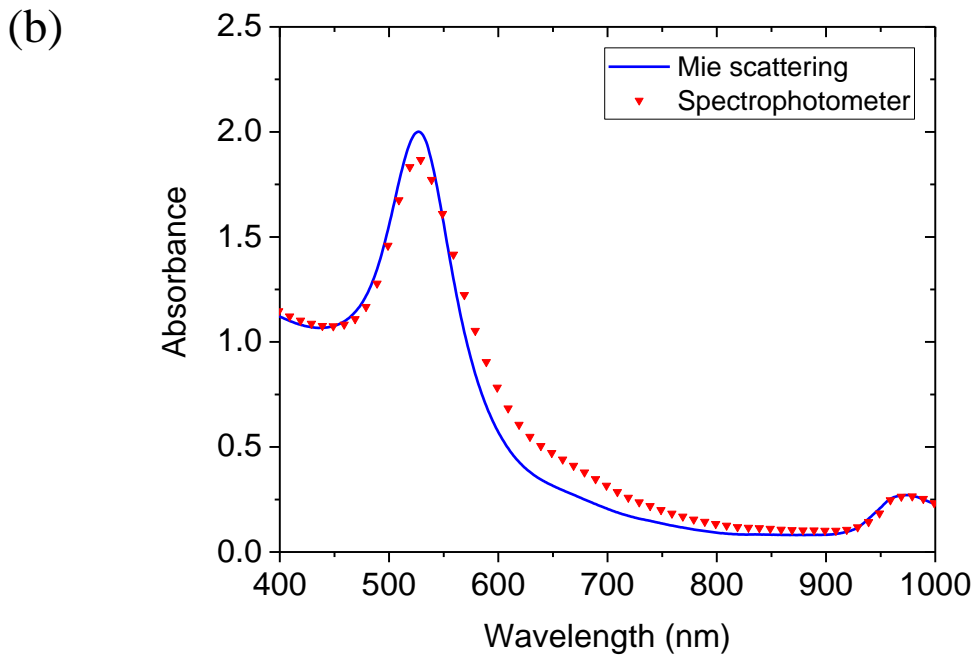
568
 569 **Fig. 4.** Variation of photothermal conversion efficiency (η) and specific absorption rate (SAR) with volume concentration of
 570 gold nanofluids under different solar intensities.
 571



575 **Fig. 5.** (a) ASTM G173-03 Reference Spectra from literature, inset shows the solar energy distribution along with wavelength in
 576 percentage (integrating spectral emissive power with wavelength divided by irradiation intensity). (b) Calculation of spectral
 577 emissive power for sun ($T=5762$ K) and nanofluid ($T=303$ K), where spectral distribution is separated into two bands, **A**
 578 ($\lambda < 3000$ nm) and **B** ($\lambda > 3000$ nm).



579

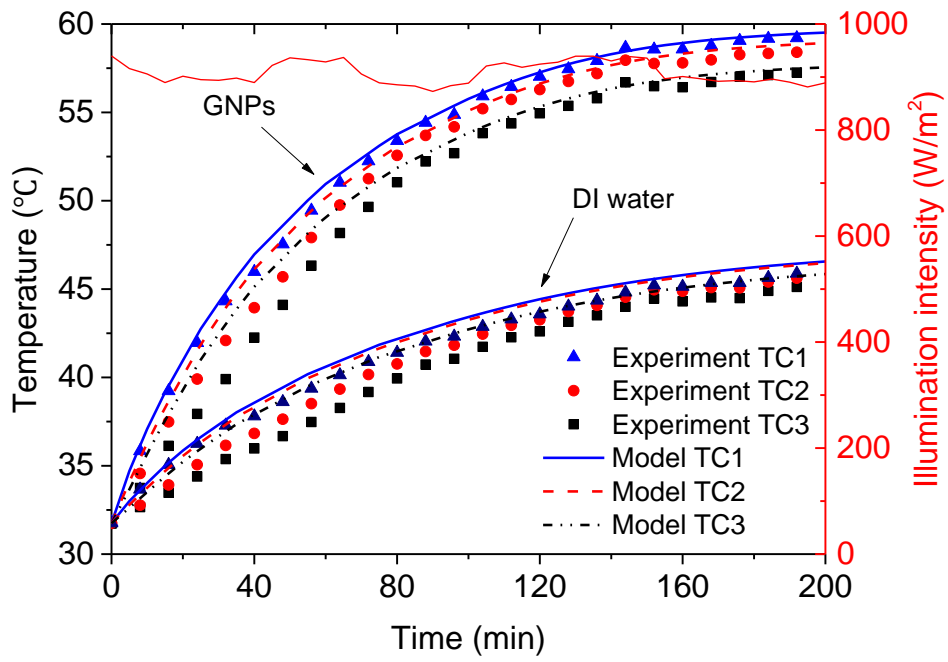


580

581 **Fig.6.** (a) Real and imaginary parts of m (Eq. (2)) and calculated absorption coefficients for gold nanoparticles (κ_p), working

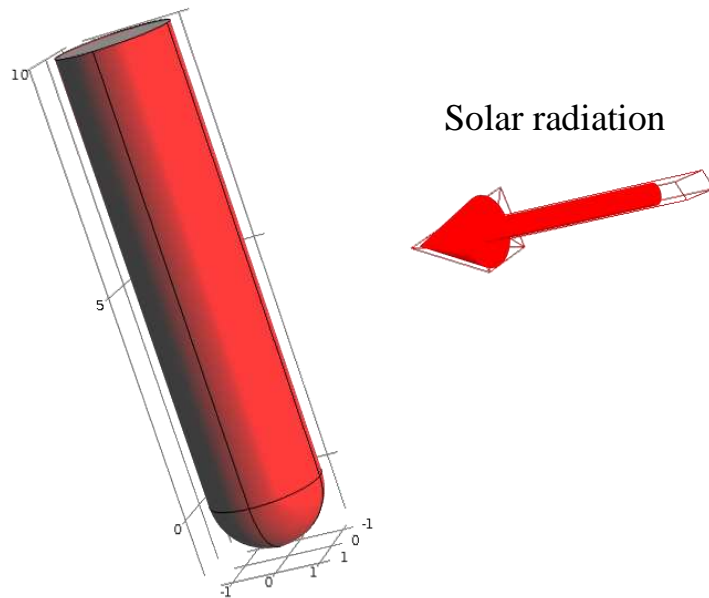
582 fluid (κ_f) and total (κ) according to Mie scattering theory; (b) Absorbance from Eq. (10) in comparison with the results from

583 the UV spectrophotometer.

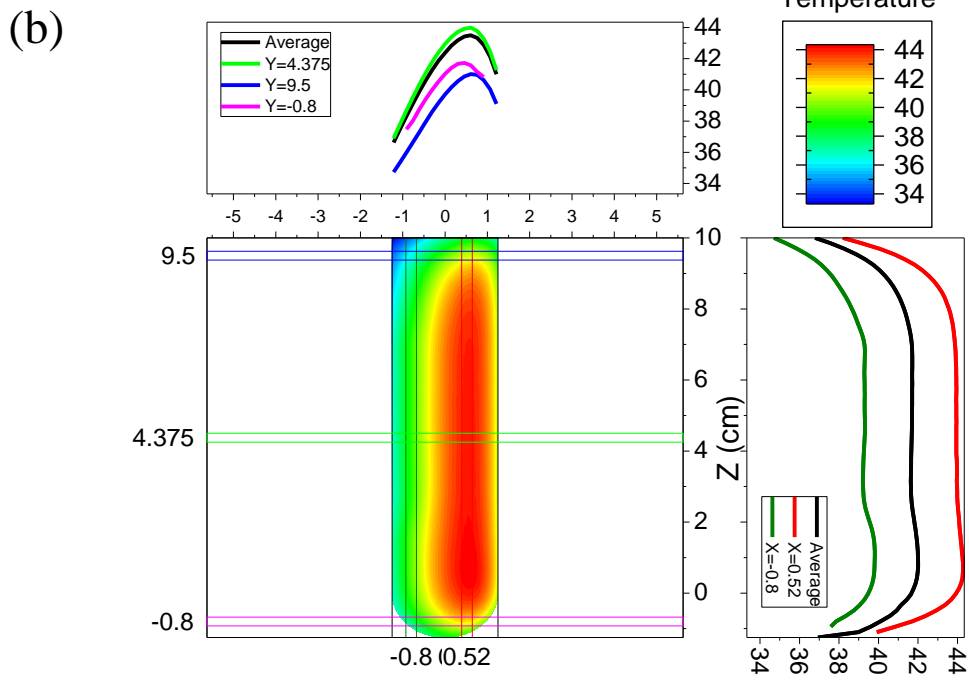


584
 585 **Fig. 7.** Comparisons between experimentally obtained increasing temperature profile of TC1-TC3 with numerical results from 3D
 586 model (nanofluids concentration is 1.45 ppm and solar intensity is constantly ~ 950 W/m²)

(a)



587



588

589

590

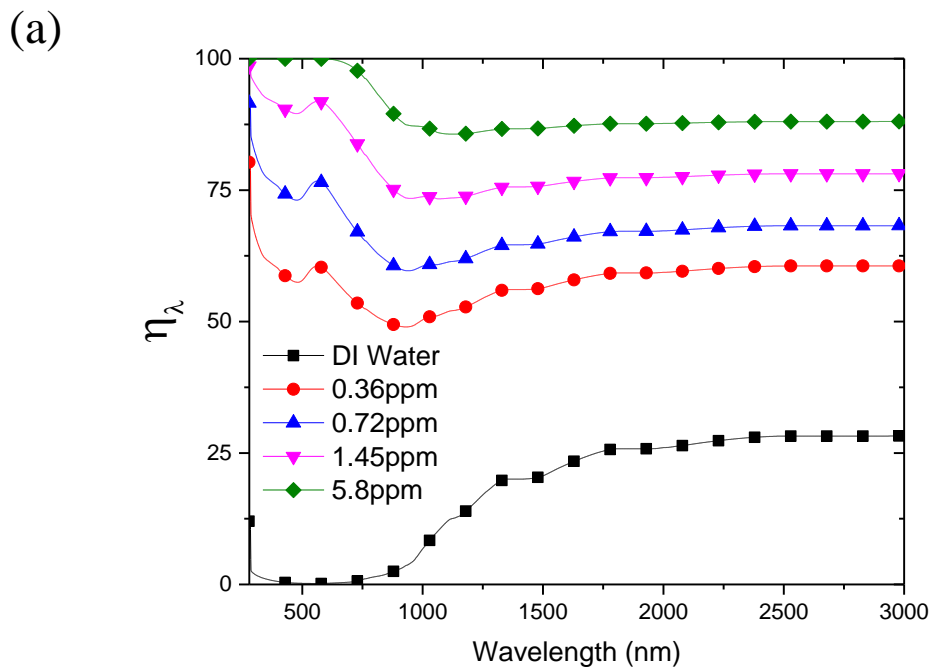
Fig. 8. (a) Schematic illustration of numerical simulation of a 3-D volumetric solar receiver where the geometry parameters is

591

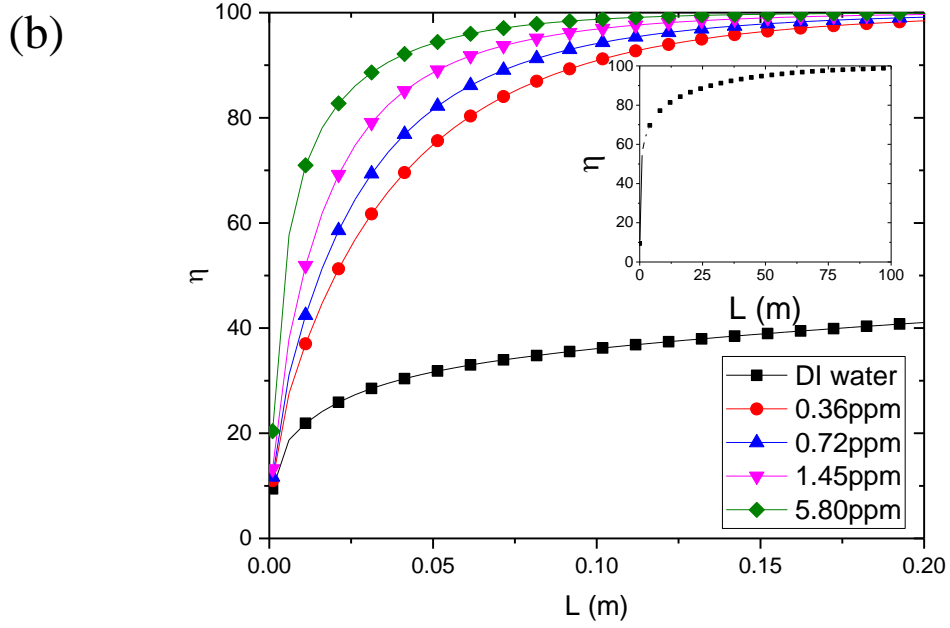
shown in (b) and solar radiation is in -y direction; (b) Temperature contour and cross-sectional profiles for nanofluid after 30

592

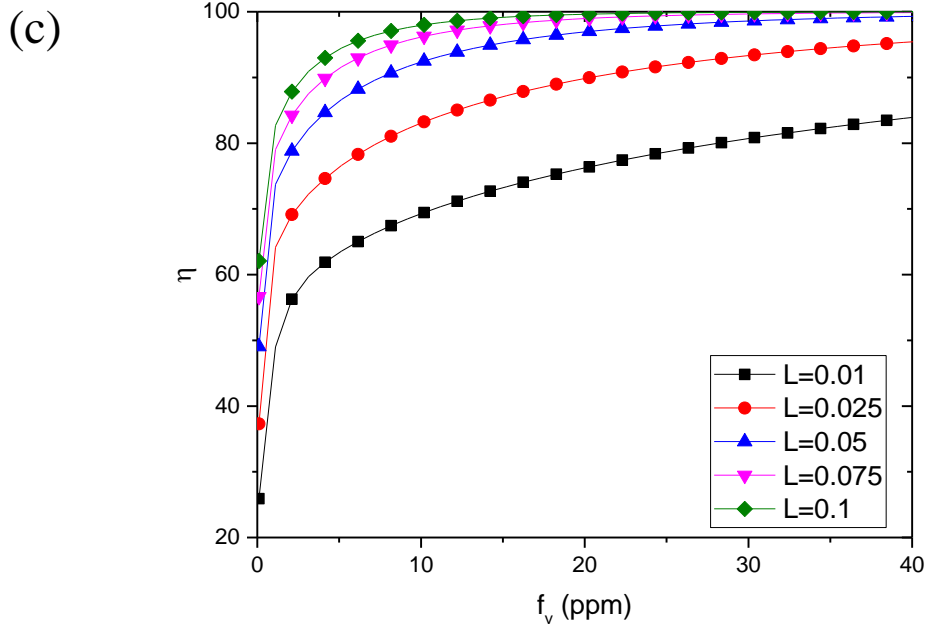
minutes' illumination (Global Tilt, $x=0$ cm, gold nanofluid concentration =1.45 ppm, and solar intensity $I=900$ W/m²,



593



594

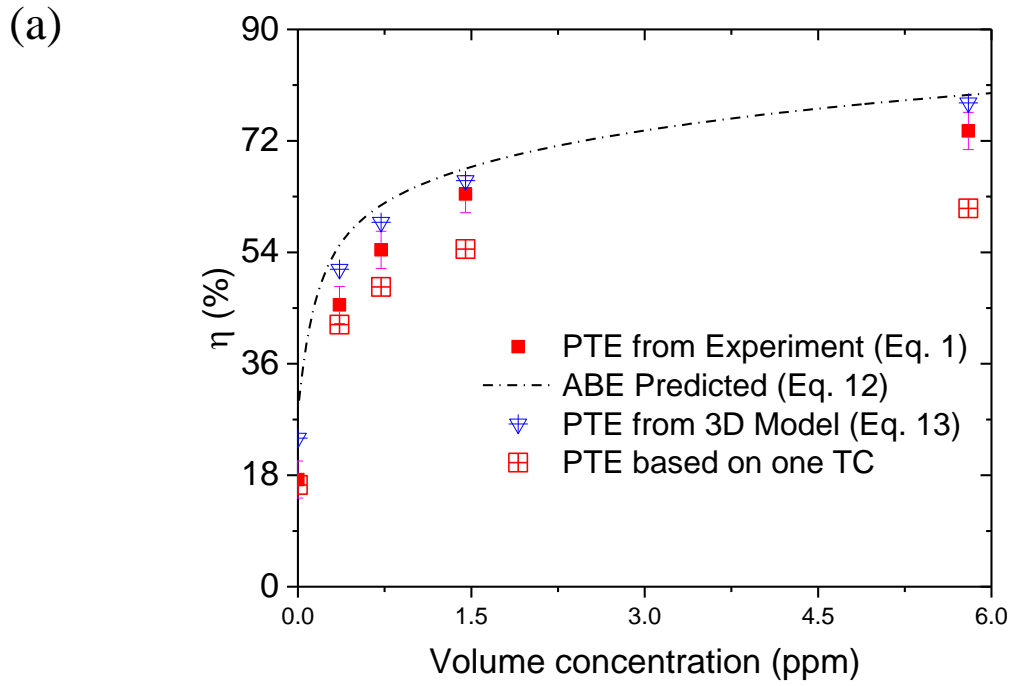


595

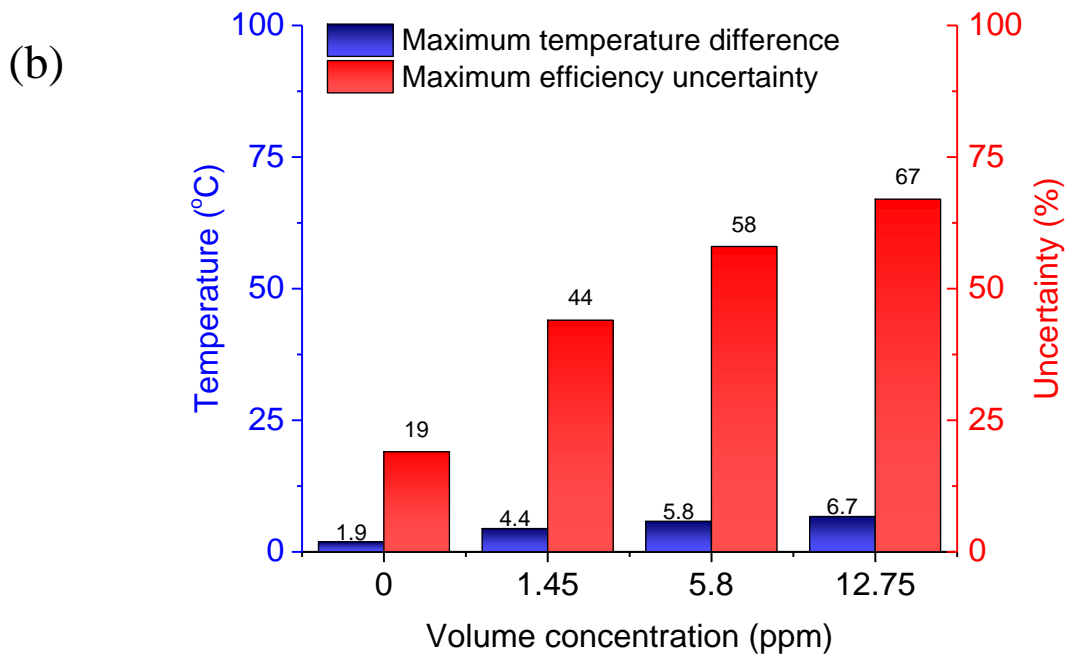
596 **Fig. 9.** (a) Spectral absorption efficiency at different wavelength as below in this paper:

597 $\eta_{\lambda}(\lambda_c) = \left[\int_{0.2\mu\text{m}}^{\lambda_c} E_0(\lambda) (1 - e^{-\kappa(\lambda)L}) d\lambda \right] / \left[\int_{0.2\mu\text{m}}^{\lambda_c} E_0(\lambda) d\lambda \right]$; (b) Absorption efficiency (ABE) as a function of optical length L for 5

598 different volume concentrations (inset: DI water); (c) ABE as a function of volume concentration f_v for 5 different optical lengths.



599



600

601

602

603

Fig. 10. (a) Comparison of the experimentally obtained photothermal conversion efficiency, efficiency calculated from 3D model and predicted absorption efficiency; (b) Maximum efficiency uncertainty caused by non-uniform temperature distribution in nanofluids.