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# Behavioural Models for FMI Co-simulations

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Abstract. Simulation is a favoured technique for analysis of cyber-physical systems. With their increase in complexity, co-simulation, which involves the coordinated use of heterogeneous models and tools, has become widespread. An industry standard, FMI, has been developed to support orchestration; we provide the first behavioural semantics of FMI. We use the state-rich process algebra, *Circus*, to present our modelling approach, and indicate how models can be automatically generated from a description of the individual simulations and their dependencies. We illustrate the work using three algorithms for orchestration. A stateless version of the models can be verified using model checking via translation to CSP. With that, we can prove important properties of these algorithms, like termination and determinism, for example. We also show that the example provided in the FMI standard is not a valid algorithm.

Keywords: verification, modelling, Circus, CSP

## 1 Introduction

The Functional Mock-up Interface (FMI) [12] is an industry standard for cosimulation: collaborative simulation of separately developed models. It has been applied across a variety of domains, including automotive, energy, aerospace, and real-time systems integration; dozens of tools support the standard.

An FMI co-simulation [4] is organised around black-box slave FMUs (Functional Mockup Units): effectively, wrappings of models that are interconnected through their inputs and outputs. FMUs are passive entities whose simulation is triggered and orchestrated by a master algorithm. A simulation is divided into steps that serve as synchronisation and data exchange points; between these steps, the FMUs are simulated independently. The master algorithm communicates with the FMUs via a number of functions that compose the FMI API.

Here, we present the first behavioural formal semantics for FMI-based co-simulations. We use *Circus* [21], a state-rich process algebra that combines Z [26] for data modelling and CSP [23] for behavioural specification. We characterise formally master algorithms and FMUs that make appropriate use of the FMI API. These abstract models of a co-simulation can be automatically generated from the number of FMUs, their inputs and outputs and dependencies.

The general models can be used to verify specific master algorithms and the adequacy of simulation models for FMUs. We have verified a classic algorithm from the FMI standard for Simulink [19], and a more robust algorithm that caters for FMU failures [4]. This revealed that the example in the standard implicitly assumes that FMUs do not raise fatal errors; it is not a valid algorithm.

Circus models, with abstracted state, can be translated to CSP and verified using the FDR3 model checker [16]. We prove important properties discussed in the FMI literature, like termination and determinism using the FDR3 model checker. Richer models can be verified using a Circus theorem prover [14]. Given a choice of master algorithm and formal models of the FMUs, our work can also be used to prove properties of an overall system described by the separate simulations. Circus can currently cater only for discrete-time models. On the other hand, a continuous time extension of Circus that can be used to give semantics to continuous-systems simulations [13] is under development.

Broman [4] has presented the most influential formalisation of FMI to date: a state-based model of the three main API functions that set and get FMU variables and trigger a simulation step with two master algorithms and a proof of core properties. Our model of a co-simulation also has its interface defined by the interactions corresponding to the simulation steps and the exchange of data associated with them. Our behavioural model covers a large portion of the FMI API, defining valid patterns for its usage and error treatment.

Sects 2 and 3 describe FMI for co-simulation and *Circus*. Sect. 4 describes the *Circus* semantics of FMI. The specification and verification of master algorithms and co-simulations is discussed in Sect. 5. Sect. 6 presents our conclusions.

### 2 FMI

Modelling and simulating cyber-physical systems (CPSs) [10] involves different engineering fields: a global system with components tackled by domain engineers using specialised tools. Co-simulation [18] involves tool interoperability for modelling and simulating heterogeneous components. FMI avoids the need for tool-specific integration, by exchanging dynamic models, co-simulating heterogeneous models, and protecting intellectual property. We deal with co-simulation, but we can also reason about simulations with model exchange.

A master algorithm orchestrates a collection of FMUs that may be standalone, containing runnable code, or be coupled, in which case it contains a wrapper to a simulation tool. Like FMI, our model is agnostic to the particular realisation of an FMU, and does not cover any communication infrastructure that may be in place to support distributed co-simulation. We assume that communication between the master algorithm and the various FMUs is reliable.

When the co-simulation is started, the models of the FMUs are solved independently between two discrete communication points defined by a step. For that, the master algorithm reads the outputs of the FMUs, sets their inputs, and then waits for all FMUs to simulate up to the defined communication point, before advancing the simulation time. Master algorithms differ in their approach to handling the definition of the step sizes and any simulation errors.

Although the FMI standard does not specify any particular master algorithms, or the technology for development of FMUs, it specifies an API that can be used to orchestrate the various simulations. Restrictions on the use of the API functions specify, indirectly and informally, how a master algorithm can be

```
\begin{array}{l} \textbf{channel}: setT: TIME; \ updateSS: NZTIME; \ step: TIME \times NZTIME; \ end \\ \textbf{process} \ \ Timer \ \widehat{=} \ ct, hc, tN: TIME \bullet \textbf{begin} \\ \textbf{state} \ State = = [currentTime, stepSize: TIME] \\ Step = \\ setT?t: t \leq tN \longrightarrow currentTime := t; \ Step \\ \square \ updateSS?ss \longrightarrow stepSize := ss; \ Step \\ \square \ step!currentTime!stepSize \longrightarrow currentTime := currentTime + stepSize; \ Step \\ \square \ currentTime = tN \ \& \ end \longrightarrow \textbf{Stop} \\ \bullet \ currentTime, stepSize := ct, hc; \ Step \\ \textbf{end} \end{array}
```

Fig. 1. Circus specification of a Timer process

defined and how an FMU may respond. Our model captures a significant subset of the FMI API, and defines formally validity for algorithms and FMUs.

### 3 Circus

The main construct of *Circus* is a process, used to specify a system and its components. Processes communicate with each other via channels. Communications are instantaneous and synchronous events. A process can have a state, defined using a Z schema, and a behaviour, defined using an action.

To illustrate Circus, Fig. 1 presents the model of a Timer from a valid master algorithm. Timer takes as parameters the current time ct, the step size hc, and the end time tN of the simulation. Although it is possible to set up experiments without an end time, we restrict ourselves to experiments that are time bounded.

Timer's state contains two components: currentTime and stepSize. Its behaviour is defined by the action at the end. After initialising currentTime and stepSize using ct and hc, it calls the local action Step. It takes inputs on channels setT and updateSS to update the current time and step size. The channel declarations define the type of the values that can be communicated through them: TIME is the set of natural numbers, and NZTIME excludes 0. Step sizes cannot be 0. It uses a channel step to output the current time and step size. After a communication on step, the current time is advanced to the next simulation step; at the end of the experiment (currentTime = tN), it synchronises on end.

The action Step offers communications on the above channels in external choice ( $\square$ ). The time t input through setT cannot exceed the end time tN of the simulation. The offer of synchronisation on end is guarded by currentTime = tN and only becomes available if this condition holds. After the event end, the timer deadlocks: behaves like the action **Stop**.

Processes can also be defined by combination of other processes. For example, the specification of the process *TimedInteractions* below combines three processes *Timer*, *endSimulation* and *Interaction*.

```
TimedInteractions \triangleq t0, tN : TIME \bullet \\ \begin{pmatrix} (Timer(t0, 1, tN) \triangle endSimulation) \\ \llbracket \{ step, end, setT, updateSS, endsimulation \} \rrbracket \end{pmatrix} \setminus \{ step, end, setT, updateSS \} \\ Interaction \end{pmatrix}
```

fmi2Get	FMI2COMP.VAR.VAL.FMI2ST
fmi2Set	FMI2COMP.VAR.VAL.FMI2STF
fmi2DoStep	FMI2COMP.TIME.NZTIME.FMI2STF
fmi2Instantiate	FMI2COMP.Bool
fmi2SetUpExperiment	FMI2COMP.TIME.Bool.TIME.FMI2ST
fmi2EnterInitializationMode	FMI2COMP.FMI2ST
fmi2ExitInitializationMode	FMI2COMP.FMI2ST
fmi2GetBooleanStatusfmi2Terminated	FMI2COMP.Bool.FMI2ST
fmi2GetMaxStepSize	FMI2COMP.TIME.FMI2ST
fmi2Terminate	FMI2COMP.FMI2ST
fmi2FreeInstance	FMI2COMP.FMI2ST
fmi2GetFMUState	FMI2COMP.FMUSTATE.FMI2ST
fmi2SetFMUState	FMI2COMP.FMUSTATE.FMI2ST

Table 1. Channels that model FMI API functions

TimedInteractions has two parameters: a start and an end time t0 and tN. It uses Timer defined above with arguments t0, 1, and tN. Timer can be interrupted ( $\Delta$ ) by the process endSimulation. It, however, runs in parallel ([]) with the process Interaction. They synchronise on communications on step, end, setT, updateSS, and endsimulation, but otherwise proceed independently. The process that results from the parallelism hides ( $\backslash$ ) communications on step, end, setT, and updateSS, which are used just internally by Timer and Interaction.

A complete account of *Circus* can be found in [8]. We explain any extra notation not explained here as needed.

#### 4 A model of FMI

The FMI API consists of functions used by the master algorithm to orchestrate the FMUs. In our model, these functions are defined as channels whose types correspond to the input and output types of the functions; see Table 1.

We use the given type FMI2COMP to represent an instance of an FMU. In FMI, these are pointers to an FMU-specific structure that contains the information needed to simulate it. Here, we use identifiers for such components.

Valid variable names and values are represented by the sets *VAR* and *VAL*. We do not model the FMI type system, which includes reals, integers, booleans, characters, strings, and bytes; however, it is not difficult to cater for this type system. Extensions to the type system are expected in future versions of FMI.

The type FMI2ST contains flags of the FMI type fmi2Status that are returned by the API functions. We include fmi2OK, fmi2Error, and fmi2Fatal, which indicate, respectively, that all is well, the FMU encountered an error, and the computations are irreparable for all FMUs. The extra flag fmi2Discard is also included in the superset FMI2STF; it can only be returned by fmi2Set and fmi2DoStep. fmi2Set indicates that a status cannot be returned, and in the case of fmi2DoStep that a smaller step size is required or the requested information cannot be returned. We do not include fmi2Warning, used for logging, and fmi2Pending, used for asynchronous simulation steps.

FMUSTATE contains values that represent an internal state of an FMU. It comprises all values (of parameters, inputs, buffers, and so on) needed to continue a simulation. It can be recorded by a master algorithm to support rollback.

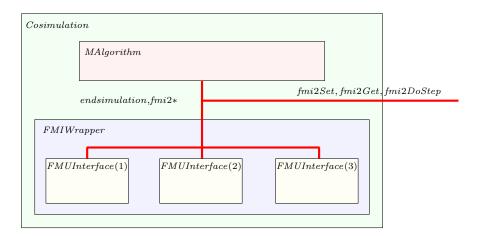


Fig. 2. Structure of a co-simulation model

The signature of the channels impose restrictions on the use of the API. It is not possible to call fmi2DoStep with a non-positive step size. Given a particular configuration of FMUs, we can define the types of the fmi2Get and fmi2Set channels so that setting or getting a variable that is not in the given FMU is undefined. Without this fine tuning, such attempts lead to deadlocks in our model: a check for deadlock freedom ensures the absence of such problems. The API actually includes specialised fmi2Get and fmi2Set functions for each data type available. As already said, we do not cater for the FMI type system.

The function fmi2Instantiate returns a pointer to a component, and null if the instantiation fails. Since we do not model pointers, we use a boolean to cater for the possibility of failure. The function fmi2GetMaxStepSize is not part of the standard; we use it to implement the rollback algorithm in [4].

The overall structure of our models of a co-simulation is shown in Fig. 2. The visible channels are fmi2Get, fmi2Set, and fmi2DoStep. So, we can use our model to verify properties of co-simulations that can be described in terms of these interactions, and involving variables from any of the FMUs involved.

The other channels enforce the expected control flow of a master algorithm. They are used for communication between the process MAlgorithm that models a master algorithm and each process FMUInterface(i) that models the FMU identified by i. We call FMIWrapper the collection of FMU interfaces: they execute independently in parallel, that is, in interleaving.

The control channel *endsimulation* is used to shutdown the simulation. Since an FMU may fail, its termination may not be carried out gracefully (with fmi2Terminate and fmi2FreeInstance). So, *endsimulation* is used to indicate the end of the experiment in all cases and shutdown the model processes.

In what follows, we describe our specifications of *MAlgorithm* (Sect. 4.1) and *FMUInterface* (Sect. 4.2), which provide a correctness criterion for these components. In Sect. 4.3, we describe how to construct models of specific FMUs. Applications of our models are described in Sect. 5.

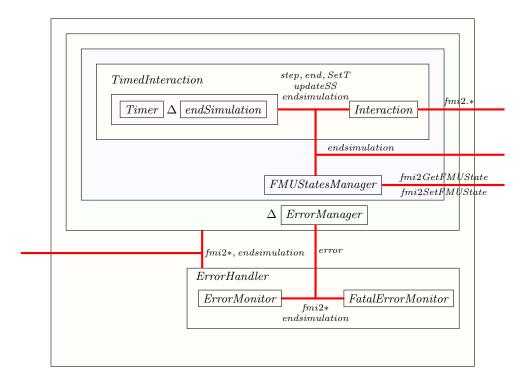


Fig. 3. Structure of a model of a master algorithm

## 4.1 Master algorithms

A master algorithm is a monolithic program that defines the connections between the FMUs and the time of the simulation steps, and handles any errors raised by an FMU. In our model, we consider each of these aspects of a master algorithm separately. The overall structure of the *MAlgorithm* process is described in Fig. 3. It provides a general characterisation of the valid history of interactions of a master algorithm. It does not commit to specific policies to define step sizes and error handling in case an API function returns fmi2Discard. The treatment of fmi2Error and fmi2Fatal is restricted by the standard.

MAlgorithm has three main components described next. TimedInteractions specifies the co-simulation steps and orchestration of the FMUs. FMUStates-Manager controls access to the internal state of the FMUs. ErrorHandler monitors the occurrence of an fmi2Error or fmi2Fatal from the API functions.

TimedInteractions has two components. Timer is presented in Sect. 3. It uses step and end to drive the Interaction process, which defines the orchestration of the FMUs. This is the core process that restricts the order in which the API functions can be used. Timer also exposes channels setT and updateSS to allow Interaction to define algorithms will rollback or a variable step size. The timer can be terminated by the signal endsimulation raised by Interaction.

Interaction is the sequential composition of Instantiation, InstantiationMode, InitializationMode, and slaveInitialized, which correspond to states that define

the stages of a co-simulation [12, p.103]. The definitions of these processes depend on the configuration of the FMUs. Given such a configuration, they can be automatically generated as indicated below. A configuration is characterised by a sequence of FMU identifiers (FMUs: seq FMI2COMP), and sequences that define the parameters and their values (parameters: seq( $FMI2COMP \times VAR \times VAL$ )), inputs and their initial values (inputs: seq( $FMI2COMP \times VAR \times VAL$ )), outputs (outputs: seq( $FMI2COMP \times VAR$ )), and an input/output port dependency graph [4] pdg. Some of this information is also needed to generate automatically a sketch of the models of the FMUs (see Sect. 4.3).

The port dependency graph pdg is a relation between outputs and inputs defined by a pair of type  $FMI2COMP \times VAR$ . The graph establishes how the inputs of each of the FMUs depend on the outputs of the others. It must be acyclic, and this can be automatically checked using the CSP model checker. Using the port dependency graph, once we retrieve the outputs, via the fmi2Get function, we know how to provide the inputs, via the fmi2Set function.

Instantiation, defined below, instantiates the FMUs. It is an iterated sequential composition (;) of actions  $fmi2Instantiate.i?sc \longrightarrow \mathbf{Skip}$ , where i comes from FMUs and  $\mathbf{Skip}$  is the action that terminates immediately.

InstantiationMode and InitializationMode allow the setting up of parameters and initial values of inputs before calling the API function that signals the start of the next phase. We show below InitializationMode. For an element inp of inputs, we use projection functions FMU, name and val to get its components.

```
(; inp: inputs \bullet fmi2Set!(FMU\ inp)!(name\ inp)!(val\ inp)?st \longrightarrow \mathbf{Skip});
(; i: FMUs \bullet fmi2ExitInitializationMode!i?st \longrightarrow \mathbf{Skip})
```

We can easily generalise the model to allow an interleaving of the events involved. The value of such a generalisation, however, is unclear (and it harms the possibility of automated verification via model checking).

The process slaveInitialized is sketched in Fig. 4; it is driven by the Timer. Its state contains a component rinps: a function that records, for each FMU identifier a function from the names of its inputs to values. This function is defined by taking the value of each output from the FMUs, and updating rinps to record that value for the inputs associated with the output in the port dependency graph. If the Timer signals the end, slaveInitialized finishes. Otherwise, it collects the outputs, distributes the inputs, and carries out a step.

Similarly to that of InitializationMode, the definition of TakeOutputs uses an iterated sequence, now over outputs: the sequence of pairs that identify an FMU and an output name. Once the value v of an output out is obtained, it is assigned to each input inp in the sequence pdf(out) associated with out in the port dependency graph pdg. We use  $\oplus$  to denote function overriding.

DistributeInputs uses inp to set the inputs of the FMUs using fmi2Set. Step proceeds with the calls to fmi2DoStep and if all goes well, recurses back to the Main action of slaveInitialized. Their definitions are omitted for brevity.

FMUStatesManager controls the use of the functions fmi2GetFMUState and fmi2SetFMUState for each of the FMUs. It is an interleaving of instances of the

```
process slaveInitialized \widehat{=} state State == [rinps : FMI2COMP \leftrightarrow (VAR \leftrightarrow VAL)] ...

TakeOutputs \, \widehat{=} ; out : outputs • fmi2Get.(FMU \ out).(name \ out)?v \longrightarrow ; inp : pdg(out) \bullet  rinps := rinps \oplus \{(FMU \ inp) \mapsto ((rinps \ (FMU \ inp))) \oplus \{(name \ inp) \mapsto v\})\}

Main \, \widehat{=} \ end \, \longrightarrow \mathbf{Skip}  \square \ step?t?hc \longrightarrow TakeOutputs; \ DistributeInputs; \ Step

• Main end
```

Fig. 4. Sketch of slaveInitialized

```
process FMUStatesManager = i : FMI2COMP \bullet begin
AllowAGet = fmi2GetFMUState.i?s?st \longrightarrow AllowsGetsAndSets(s)
AllowsGetsAndSets = s : FMUSTATE \bullet
fmi2GetFMUState.i?t?st \longrightarrow AllowsGetsAndSets(t)
fmi2SetFMUState.i!s?st \longrightarrow AllowsGetsAndSets(s)
\bullet fmi2Instantiate.i?b \longrightarrow AllowAGet
end
```

Fig. 5. Model of FMUStateManager

process FMUStateManager(i) in Fig. 5 for each of the FMUs. Once an FMU is instantiated, then it is possible to retrieve its state. After that, both gets and sets are allowed. The actual values of the state are defined in the FMUs, but recorded in the master algorithm via fmi2GetFMUState for later use with fmi2SetFMUState as defined in FMUStateManager(i).

For complex internal states, model checking can become infeasible (although we have managed it for simple examples). To carry out verifications that are independent of the values of the internal state of the FMUs, we need to adjust only this component. Some examples, explored in the next section, are properties of algorithms that do not support retrieval and resetting of the FMU states, determinism and termination of algorithms, and so on.

The ErrorHandler process contains two components: monitors for fmi2Error and fmi2Fatal. If any of the API functions returns an error, they signal that to the ErrorManager via a channel error. Upon an error, the ErrorManager interrupts the main flow of execution. In the case of an fmi2Fatal error, the simulation is stopped via endsimulation. In the case of an fmi2Error, a call to fmi2FreeInstance is allowed, before the simulation is ended.

#### 4.2 FMU interfaces

The model of a valid FMU is simpler. It captures the control flow of an FMU, specifying, at each stage, the API functions to which it can respond. Unsurpris-

ingly, it has some of the restrictions of a master algorithm, but it is much more lax, in that it captures just the expected capabilities of an FMU.

At first, the only API function that is available is fmi2Instantiate. The simple action below specifies this behaviour.

```
Instantiation = \\ fmi2Instantiate.i?b \longrightarrow \begin{pmatrix} b \otimes status := fmi2OK; \ Instantiated \\ \Box \\ \neg \ b \otimes status := fmi2Fatal; \ RUN(FMUAPI(i)) \end{pmatrix}
```

A state component status records the result of the last call to an API function. In this case, it is updated based on the boolean b returned by fmi2Instantiate. If the instantiation is successful, the behaviour is described by Instantiated, sketched below; otherwise, it is unrestricted: specified by RUN(FMUAPI(i)), which allows the occurrence of any API functions, in any order.

```
Instantiated = status = fmi2Fatal \& RUN(FMUAPI(i))
\Box status \notin \{fmi2Error, fmi2Fatal\} \&
\left(fmi2Get.i?n?v?st \longrightarrow status := st; Instantiated\right)
\Box fmi2DoStep.i?t?hc?st \longrightarrow status := st; Instantiated
\Box \cdots
\Box st \neq fmi2Fatal \& fmi2FreeInstance!i?st \longrightarrow \cdots
```

Again, if there is a fatal error, the behaviour is unrestricted. If there is no error, all functions except fmi2Instantiate are available. Finally, if there is a non-fatal error, only fmi2FreeInstance is possible.

While a pattern of calls is defined by a master algorithm, so that, for example, all outputs are obtained before the inputs are distributed, the FMU is passive and does not impose such a policy on its use. So, the various actions enforce only the restrictions in the standard [12, p.105].

Although it is possible to specify a more restricted behaviour for FMUs, such a specification rules out robust FMU implementations that handle calls to the API functions that do not necessarily follow the strict pattern of a co-simulation. Next, we describe how to generate FMU models that follow a more restricted pattern that is adequate for use with valid master algorithms.

### 4.3 Specific FMU models

In the previous section, we have presented a general model for an FMU. The particular model of an FMU depends, of course, on its functionality, and must conform to (trace refine) our general model. This can be proved via model checking for stateless models of FMUs that do not offer the facility to retrieve and set its internal state. In this case, the models do not offer the choices of communications fmi2GetFMUState.i?st and fmi2SetFMUState.i?st. The availability of such facilities is defined by capability flags of the FMU.

We can, however, generate a sketch of the model of an FMU using information about its structure: lists of parameters  $p_i$ , inputs  $inp_i$ , and outputs  $out_i$ .

```
process FMUSketch = i : FMI2COMP \bullet begin
state\ State = [current\ Time,\ end\ Time:\ TIME;\ cp_i,\ cinp_i,\ cev_i,\ cout_i]
Instantiation = fmi2Instantiate.i!true \longrightarrow Skip
InstantiationMode =
   fmi2Set.i.p_i?v!fmi2OK \longrightarrow cp_i := v; InstantiationMode
   \Box fmi2SetUpExperiment.i?t0!true?tN!fmi2OK\longrightarrow
      currentTime, endTime := t0, tN;
      fmi2EnterInitializationMode.i!fmi2OK \longrightarrow \mathbf{Skip}
InitializationMode =
   fmi2Set.i.inp_i?v!fmi2OK \longrightarrow cinp_i := v; InitializationMode
   \Box fmi2ExitInitializationMode.i!fmi2OK \longrightarrow UpdateState
slaveInitialized =
   fmi2Get.i.out_i!cout_i!fmi2OK \longrightarrow slaveInitialized
   \Box fmi2Set.i.inp<sub>i</sub>?v.fmi2OK \longrightarrow cinp<sub>i</sub> := v; slaveInitialized
   \Box fmi2DoStep.i?t?ss!fmi2OK \longrightarrow (UpdateState; slaveInitialized)
• Instantiation; InstantiationMode; InitializationMode;
   (slaveInitialized \ \Delta)
     fmi2Terminate.i!fmi2OK \longrightarrow fmi2FreeInstance.i!fmi2OK \longrightarrow Stop)
end
```

**Fig. 6.** Sketch of a model for a specific FMU

This information is used to construct a master algorithm (see Sect. 4.1). Fig. 6 shows the sketch of a *Circus* process with the FMU behaviour. Its state includes components  $cp_i$ ,  $cinp_i$ , and  $cout_i$ , besides the current and end simulation time.

Its structure is similar to that of the *Interaction* process used to model a master algorithm. In all cases, the interactions flag success (fmi2OK). If an FMU makes assumptions about its inputs, the possibility of error can be modelled. For example, *Instantiation* indicates success, but to explore the possibility of failure, we can define it as  $fmi2Instantiate.i?b \longrightarrow \mathbf{Skip}$ . The action UpdateState is left unspecified. It is this action that specifies the functionality of the FMU. It can be automatically generated if there is a more complete model of the FMU. For example, [7] shows the case if a discrete-time Simulink model is available.

If the FMU supports retrieval and update of its state, we need to add the following choices to *InstantiationMode*, *InitializationMode*, and *slaveInitialized*.

Via fmi2GetFMUState, it outputs the whole state record, that is,  $\theta$  State, and via fmi2SetFMUState, we can update it.

If the state, either via setting of parameters and input or via an update, may become invalid, we can flag fmi2Fatal and deadlock. For example, we consider the test case shown in Fig. 7 taken from [5]. It has been designed to show that

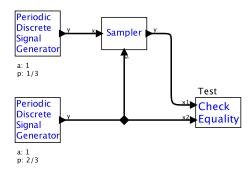


Fig. 7. Test case for sampling of discrete event signals [5]

components with discrete timed behaviour coordinate their representation of time. There are three main components: two periodic discrete signal generators, both generating the same signal, one with period one time unit and the other two time units; and a discrete sampler. The test criterion is that the output of the Sampler should equal the output of the second periodic discrete signal generator at all superdense times. There is an implicit constraint that the period p should not be 0; therefore, we specify its InstantiationMode action as follows.

```
\begin{split} InstantiationMode = \\ fmi2Set.i.a?v!fmi2OK &\longrightarrow a := v \longrightarrow InstantiationMode \\ &\square fmi2Set.i.p?v!fmi2OK \longrightarrow p := v \longrightarrow InstantiationMode \\ &\square p \neq 0 \& fmi2SetUpExperiment.i?t0!true?tN!fmi2OK \longrightarrow \\ currentTime, endTime := t0, tN; \\ fmi2EnterInitializationMode.i!fmi2OK \longrightarrow \mathbf{Skip} \\ &\square p = 0 \& fmi2SetUpExperiment.i?t0!true?tN!fmi2Fatal \longrightarrow \mathbf{Stop} \end{split}
```

In this case, if the experiment is set up when p is 0, we have a fatal error.

An FMU model generated as just explained trace refines FMUInterface(i). This means that all possible histories of interactions of the FMU are possible for FMUInterface(i) and, therefore, valid according to that criterion. We have proofs of refinement for all FMUs in Fig. 7 and for a data-flow network.

# 5 Evaluation: verification applications

In this section, we show how we can use our formal semantics for FMI to verify master algorithms and to study system properties via their co-simulations. For automation, our semantics can be translated from *Circus* to CSPM (the input language for the model checker FDR3), using a strategy similar to that of [20], so that it can be both model checked in FDR3 and executed in ProBe (FDR's process behaviour explorer), for suitably chosen model parameters.

## 5.1 Master algorithms

As well as giving a correctness criterion for a master algorithm, the model presented in Sect. 4 gives an indication of how to construct models for particular algorithms. We consider here three examples.

Classic brute-force The simplest algorithm uses a fixed step size, has no access to the state of the FMUs, and queries them for termination if fmi2Discard is flagged. To model this algorithm, we define a process ClassicMAlgorithm with the same structure shown in Fig. 3, but more specific components.

ClassicMAlgorithm uses a simple timer that does not use setT or updateSS. For the FMUStatesManager, we use a simple process that just terminates immediately. Finally, for Interaction, we use the parallel composition of Interaction itself with a process DiscardMonitor, whose main action is Monitor defined below, followed by an action Terminated that shuts down the FMUs.

```
\begin{array}{l} \mathit{Monitor} \cong \\ \mathit{fmi2DoStep?i?t?hc?st} : \mathit{st} \neq \mathit{fmi2Discard} \longrightarrow \mathit{Monitor} \\ \square \mathit{fmi2DoStep?i?t?hc.fmi2Discard} \longrightarrow \\ & \left( \mathit{fmi2GetBooleanStatusfmi2Terminated.i.true?st} \longrightarrow \mathit{ToDiscard} \right) \\ & \left( \square \mathit{fmi2GetBooleanStatusfmi2Terminated.i.false?st} \longrightarrow \mathit{Monitor} \right) \\ \square \mathit{stepAnalysed} \longrightarrow \mathit{Monitor} \ \square \mathit{step?t?hc} \longrightarrow \mathit{Monitor} \\ \square \mathit{end} \longrightarrow \mathbf{Skip} \end{array} \right) \end{array}
```

Monitor ignores all flags st returned by fmi2DoStep except fmi2Discard. If this flag is returned, it queries the FMU using fmi2GetBooleanStatusfmi2Terminated. If the FMU requests termination, Monitor behaves like ToDiscard whose simple definition we omit. In ToDiscard, when completion of the step is indicated via either a stepAnalysed or a step?t?hc event, the co-simulation is terminated. The signal stepAnalysed is not part of the Interaction interface, but is used to indicate that fmi2DoStep has been carried out for all FMUs, and we are now in a position to decide how to continue with the co-simulation.

Since ClassicMAlgorithm has the same structure as MAlgorithm, we can prove refinement by considering each of the components in isolation. While proof of refinement by model checking for the whole model is not feasible, it is feasible for the individual components. In the sequel, we use the same approach to analyse more complex algorithms. It is also feasible to prove that ClassicMAlgorithm terminates, but otherwise does not deadlock, and is deterministic.

The example in the FMI standard is a classic algorithm with a fixed step and handling of fmi2Discard, but does not include error management. So, its specification does not include the *ErrorHander* and the *ErrorManager*. Model checking can show that this is not a valid algorithm. A simple counterexample shows that it continues and calls fmi2Instantiate a second time even after the first call returns an fmi2Fatal flag. This is explicitly ruled out in the standard.

**Simulink** This is a widely used tool for simulation based on control law diagrams [19]. A popular solver uses a variable-step policy based on change rate

```
process\ VaryStep \stackrel{\frown}{=} threshold: VAL;\ initialSS: NZTIME \bullet begin
state
  State = [oldOuts, newOuts: (FMI2COMP \times VAR) \rightarrow VAL; currentSS: NZTIME]
   Init
    State'
    dom \ oldOuts' = ran \ outputs \land ran \ oldOuts = \epsilon \land newOuts' = \varnothing
    currentSS' = initialSS
Monitor \stackrel{\frown}{=}; out : outputs \bullet
  fmi2Get.(FMU\ out).(name\ out)?nv?st \longrightarrow newOuts := newOuts \oplus \{out \mapsto nv\}
Adjust \stackrel{\frown}{=} if \ delta(oldOuts, newOuts) > threshold \longrightarrow
                currentSS := newstep(delta(oldOuts, newOuts), currentSS);
                updateSS!currentSS \longrightarrow \mathbf{Skip}
            \parallel delta(oldOuts, newOuts) > threshold \longrightarrow \mathbf{Skip}
Step = Monitor; Adjust; Step
• Init: (Step \ \Delta \ endSimulation)
end
```

of the state. To model this algorithm, we use a process SimulinkMAlgorithm, which is similar to ClassicMAlgorithm, but has another monitor VaryStep, spec-

ified in Fig. 8. It is composed in parallel with *Interaction* to define a process *VariableStepInteraction* used in *SimulinkMAlgorithm*.

VaryStep takes as parameters a threshold for change and the initial value of the step size initialSS. Taking a simple approach, we define a state that records the old (oldOuts) and new (newOuts) values of the outputs, besides the current step size currentSS. After the state is initialised (using the action Init) to record undefined  $(\epsilon)$  old values for the outputs, no new values (empty function  $\varnothing$ ), and the initial step size, the monitor steps by recording the new output values (Monitor) and then changing the step size (Adjust). Adjustment is based just on a comparison between the old and new values defined by an (omitted) function delta. If the threshold is reached, a new step size is defined by another function newstep and informed to the Timer.

Fig. 8. Model of VaryStep

We have established that SimulinkMAlgorithm is valid, that is, it refines MAlgorithm, by proving that the new VariableStepInteraction refines Interaction. We have also proved termination, deadlock freedom, and determinism.

Rollback In the same way as illustrated by VaryStep in Fig. 8, we can model a sophisticated algorithm suggested in [4]. We define a Rollback monitor that has the same structure as VaryStep. Its Monitor (a) saves the state using fmi2GetFMUState before each step of co-simulation, and (b) queries the maximum step size that each FMU is prepared to take. This uses an extra FMI API

function fmi2GetMaxStepSize. In Adjust, if any of the maximum values returned is lower than that originally proposed, the states of the FMUs are reset using fmi2SetFMUState, and the time as well as the step size are adjusted (using setT and updateSS). We have again proved validity, termination, and determinism.

In [4], determinism is also based on the FMU states, which are visible via fmi2Get and fmi2Set. On the other hand, that work considers determinism with respect to the order of retrieval and update of variables and execution of the FMUs. In our models, this order is fixed. To establish determinism in that sense, we need to consider a highly parallel model with all valid execution orders respecting the port dependency graph. This is the approach in [7], where verification uses theorem proving. The approach taken here is more amenable to model checking and sufficient to verify sequential implementations of simulations.

As explained in the previous section, the definition of *Interaction* is determined by structural information about the FMUs configuration. Using that information, and a choice of master algorithm (fixed or variable step, treatment of fmi2Discard, and so on), we can obtain a model. For the FMUs, in the previous section, we have explained how to derive (sketches of) models.

## 5.2 Co-simulations

Our semantics is also useful for analysis using FDR of the FMU compositions in co-simulations for deadlock, livelock, and determinism. We have done this verification, for instance, for the discrete event signal example in Fig. 7.

The semantics can also be used to validate the results of co-simulation runs. For example, Fig 9 describes a short scenario involving two co-simulation steps. We specify it using CSP-M, rather than *Circus*, and write the traces refinement ([T=) assertion we use for verification. The assertion says that this scenario is a possible trace of the model: it is a correct co-simulation run. (We may check this by noting that the final two operations set the same inputs for FMU 4 (Check Equality)—the FMU that checks equality in the simulation model.) To facilitate model checking, we use numbers for the names of the variables. With this approach, we validate our model against an actual co-simulation.

Moreover, we can go further and check behavioural correctness too. The specification of an FMI composition  $\mathcal{C}$  is an assertion over traces of events corresponding to the FMI API, principally doStep, get, and set. A similar technique is used for specification of processes in CSPm based on traces of events [17], and in CCS, using temporal logic over actions [3].

An alternative is to use a more abstract composition of FMUs  $\mathcal{A}$  as a specification.  $\mathcal{A}$  can be used as an oracle in testing the simulation: do a step of  $\mathcal{C}$  and then compare it with a step of  $\mathcal{A}$ .  $\mathcal{A}$  and  $\mathcal{C}$  can be used even more directly in our model by carrying out a refinement check in FDR3.

Consider a dataflow process taken from [17, p.124] and depicted in Fig. 10 that computes the weighted sums of consecutive pairs of inputs. So, if the input is  $x_0, x_1, x_2, x_3, \ldots$ , then the output is  $(a*x_0+b*x_1), (a*x_1+b*x_2), (a*x_2+b*x_3), \ldots$ , for weights a and b. The network has two external channels, left and right, and three internal channels. X2 multiplies an input on channel left1 by a and passes

```
DSynchronousEventsSpec =
  -- Set parameters
 fmi2Set.1.1.1.fmi2OK -> fmi2Set.1.2.1.fmi2OK ->
 fmi2Set.2.1.1.fmi2OK -> fmi2Set.2.2.2.fmi2OK ->
 -- Set initial values of inputs
 fmi2Set.3.1.1.fmi2OK -> fmi2Set.3.2.1.fmi2OK ->
 fmi2Set.4.1.1.fmi2OK -> fmi2Set.4.2.1.fmi2OK ->
  -- Steps
 fmi2Get.1.1.1.fmi2OK -> fmi2Get.2.1.1.fmi2OK -> fmi2Get.3.3.1.fmi2OK ->
 fmi2Set.3.1.1.fmi2OK -> fmi2Set.3.2.1.fmi2OK ->
 fmi2Set.4.2.1.fmi2OK -> fmi2Set.4.1.1.fmi2OK ->
 fmi2DoStep.1.0.2.fmi2OK -> fmi2DoStep.2.0.2.fmi2OK ->
 fmi2DoStep.3.0.2.fmi2OK -> fmi2DoStep.4.0.2.fmi2OK ->
 fmi2Get.1.1.1.fmi2OK -> fmi2Get.2.1.1.fmi2OK -> fmi2Get.3.3.1.fmi2OK ->
 fmi2Set.3.1.1.fmi2OK -> fmi2Set.3.2.1.fmi2OK ->
 fmi2Set.4.2.1.fmi2OK -> fmi2Set.4.1.1.fmi2OK ->
 fmi2DoStep.1.2.2.fmi2OK -> fmi2DoStep.2.2.2.fmi2OK ->
 fmi2DoStep.3.2.2.fmi2OK -> fmi2DoStep.4.2.2.fmi2OK -> SKIP
```

assert Cosimulation(0,2) [T= SynchronousEventsSpec

Fig. 9. Scenarios for Fig 7: sampling of discrete event signals

the result to X3 on mid. X3 multiplies an input on the left2 channel by b and adds the result to the corresponding value from the mid channel. X1 duplicates its inputs and passes them to the other two processes (since all values except the first and last are used twice), where the multiplications can be performed in parallel. A little care needs to be taken to get the order of communications on the left1 and left2 channels right, otherwise a deadlock soon ensues.

The CSP specification of this network remembers the previous input.

```
DFProc(a, b) = left?x \longrightarrow P(x)
 P(x) = left?y \longrightarrow right!(a * x + b * y) \longrightarrow P(y)
```

The key part of the main FMU in this specification is shown in Fig 11.

Once the slave FMU has been initialised, the master algorithm can instruct it to perform a simulation step (fmi2DoStep). The FMU fetches the state item, gets the next input, fetches the parameters a and b, performs the necessary computation, and stores it as the current output.

We have been able to encode both the specification and implementation of the data flow network, with small values for maxint, and check behavioural refinement. We have identified the problem alluded to above, in getting the communications on left1 and left2 in the wrong order; issues to do with determinism concerning hidden state in our model; and termination issues to do with the end of the experiment and closing down resources. We have also been able to demonstrate in a small way the consistency of the semantics model.

The transformation from *Circus* to CSPM corresponding to the FMI API requires the identification of barrier synchronisations that correspond to the doStep commands. An appropriate strategy is outlined in [6].

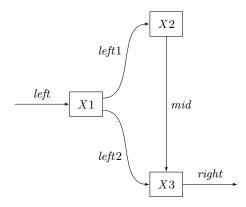


Fig. 10. A data-flow example

```
DFSPECFMUProc(i) =
let
    slaveInitialized(hc) =
    ...
    []
    fmi2DoStep.i?t?ss!fmi2OK -> (UpdateState; slaveInitialized(ss))
UpdateState =
    get.i.1?x:INPUTVALP ->
        getinput.i.1?y:INPUTVALP ->
        getparam.i.1?a:PARAMVAL -> getparam.i.2?b:PARAMVAL ->
        setoutput.i.1!(a*x+b*y) -> SKIP
within
Instantiation; InstantiationMode(eps,eps);
InitializationMode; slaveInitialized(0)
```

Fig. 11. Data flow specification

## 6 Conclusions

We have provided a comprehensive model of the FMI API, characterising formally valid master algorithms and FMUs. We can use our models to prove validity of master algorithms and FMU models. For stateless models, model checking is feasible, and we can use that to establish properties of interest of algorithms and FMU models. For state-rich models, we need theorem proving.

Given information about the network of FMUs and a choice of master algorithm, it is possible to construct a model of their co-simulation automatically for reasoning about the whole system. This is indicated by how our models are defined in terms of information about parameters, inputs, and so on, for each FMU, and about the FMU connections. A detailed account of the generation process and its mechanisation are, however, left as future work.

We have discussed a few example master algorithms. This includes a sophisticated rollback algorithm presented in [4] using a proposed extension of the FMI. It uses API functions to get and set the state of an FMU. In [4], this algorithm uses a doStep function that returns an alternative step size, in case the input

step size is not possible. Here, instead, we use an extra function that can get the alternative step size. This means that our standard algorithms respect the existing signature of the fmi2DoStep function. As part of our future work, we plan to model one additional master algorithm proposed in [4].

There has been very practical work on new master algorithms, generation of FMUs and simulations, and hybrid models [2, 22, 11, 9]. Tripakis [25] shows how components with different underlying models (state machines, synchronous data flow, and so on) can be encoded as FMUs. Savicks [24] presents a framework for co-simulation of Event-B and continuous models based on FMI, using a fixed-step master algorithm and a characterisation of simulation components as a class specialised by Event-B models or FMUs. This work has no semantics for the FMI API, but supplements reasoning in Event-B with simulation of FMUs.

Pre-dating FMI, the work in [15] presents models of co-simulations using timed automata, with validation and verification carried out using UPPAAL, and support for code generation. It concentrates on the combination of one continuous and one discrete component using a particular orchestration approach. The work in [5] discusses the difficulties for treatment of hybrid models in FMI.

There are several ways in which our models can be enriched: definition of the type system, consideration of asynchronous FMUs, sophisticated error handling policies that allow resetting of the FMU states, and increased coverage of the API. FMI includes capability flags that define the services supported by FMUs, like asynchronous steps, and retrieval and update of state, for example. We need a family of models to consider all combinations of values of the capability flags. We have explained here how a typical combination can be modelled.

Our long-term goal is to use our semantics to reason about the overall system composed of the various simulation models. In particular, we are interested in hybrid models, involving FMUs defined by languages for discrete and for continuous modelling. To cater for models involving continuous FMUs, we plan to use a *Circus* extension [13]. Using current support for *Circus* in Isabelle [14], we may also be able to explore code generation from the models. We envisage fully automated support for generation and verification of models and programs.

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