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A Modular Multilevel Flying Capacitor Converter-Based STATCOM for Reactive Power Control in Distribution Systems

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Keywords

« Multilevel converters », « Pulse Width Modulation (PWM) », « STATCOM », « Voltage Source Converter (VSC) », «Reactive Power».

Abstract

This paper presents a simulation study for a built prototype of modular multi-level flying capacitor cascade converter as a STATCOM. The converter modulation scheme applied is based on Phase Shifted PWM and the two scenarios which require compensation are investigated to verify this topology. The two scenarios are PCC voltage regulation and unity power factor correction through reactive power compensation. Simulation results verify the performance of the chosen topology.

1. Introduction

The STATCOM, as an established FACTS device for providing reactive power compensation and voltage regulation for power networks, is in increasing demand for distribution systems. Major changes are posing challenges to the stability and power quality of distribution networks, notably the growth in distributed generation, particular in the form of widespread installations of grid connected PV panels and accelerated use of electric vehicles, requiring battery charging stations to provide redundant power supply. Consequently, excessive and often bidirectional current flow in lines and transformers, causes severe voltage fluctuation, and waveform distortion. In combination with these is the presence of predominantly reactive and non-sinusoidal load due to unprecedented widespread use of power electronic based equipment by industrial consumer. The consequent current and voltage harmonics have detrimental effects, including electro-magnetic interference (EMI), overloading the cables and may even result in voltage swell or drop proportional to the load current, interconnected line impedance and frequency. Also, the presence of reactive current on the line results in low power factor and reduced efficiency. STATCOM offers effective solution to some of these problems.

The use of STATCOMs in distribution networks with voltages up to a few kilovolts has spread over the past decades. Most of these installed devices use voltage step-down transformers and two-level voltage source converters with harmonic filters. This combination makes the device bulky and costly, and the converter needs to be switched at high frequencies to achieve low total harmonic distortion, hence generating high stresses and losses in the switches. A different configuration uses classical multilevel inverters such as the 3-level neutral point clamped (NPC) type for generating a waveform with low harmonic levels at the reduced switching frequencies. These, usually combined with a phase shift transformer (PST), form the multi-pulse converter topology and can generate staircase sinusoidal waveforms at high voltages. However the PST is an expensive item and control in this topology is complex.

Recent development in Modular Multi-level Cascaded Converters (MMCC) makes the topology an enabling technology for STATCOM in medium and high voltage network applications [1-4]. The main advantage of the modular structure is in allowing the circuit to be scalable to work at any voltage level, so that a transformer may not be needed. With lower voltage stress across its switches and lower switching frequencies, the topology offers lower power losses and higher converter efficiency whilst generating good quality waveforms. MMCC-STATCOM schemes implemented in practice are based on the Cascaded H-bridge MMCC topology [5-7]

This paper presents a STATCOM built on a variant of the MMCC, the Modular Multilevel Flying Capacitor Converter (MMFCC). In this form, each module is a basic single-phase three-level full-bridge flying capacitor converter which can generate three voltage levels ($0, \pm V_{DC}/2, \pm V_{DC}$) and can be individually controlled [8-11]. For an MMFCC-based STATCOM the main challenge is to achieve flexible and high performance line voltage control and reactive power compensation whilst maintaining module and floating capacitor voltages balanced. In this work a Unipolar Phase Shifting PWM modulation scheme is discussed as the chosen switching control method which can achieve natural floating capacitor voltage balance. Subsequently an MMFCC can be treated as for a cascaded H-bridge converter but having more voltage levels per module. Such a topology may be applied as a STATCOM for reactive power control in a power system. The paper will show that module capacitor voltage can be balanced by controlling the average voltage of phase limbs without concerning about the floating capacitor voltages. Simulation results of this STATCOM for voltage control of a small power network are shown giving desired responses and discussed.

2. MMFCC and Phase Shift PWM Control

The phase limb of an MMFCC comprises a chain of three-level flying capacitor full-bridge converter as the basic module. Each module, as shown in Fig 1a, having two floating capacitors C_a and C_b and an outer DC Bus capacitor C_{DC} , is capable of synthesizing a total of 5 voltage levels, $\pm V_{DC}, \pm V_{DC}/2$, and 0 volt. For three phase applications the three-phase limbs can be in either star or delta connection which may be referred to as Single Star Flying Capacitor Cell (MMC-SSFCC) and Single Delta Flying Capacitor Cell (MMC-SDFCC) following the nomenclature presented by Akagi [5]. For this work an MMCC-SSFCC consisting of six modules is used as shown in Fig 1a. Each phase limb comprising of two modules synthesise a total of 9 voltage levels ($\pm 2V_{DC}, \pm 1.5V_{DC}, \pm V_{DC}, \pm 0.5V_{DC}, 0$ volt). Recent work has investigated using this topology to function as a STATCOM in a medium voltage network [8].

One of the key issues when using a MMCC-SSFCC as a STATCOM relates to the fluctuations of capacitor voltages. With two floating capacitors in each module, an ideal switching scheme should be one which can maintain these voltages balanced, so that the modules can be treated as H-bridges but with the advantage of having more voltage levels. The unipolar phase-shifted PWM (PS-PWM) scheme is considered most suitable as it can ensure natural balance of the floating capacitor voltages. As is known a unipolar scheme uses two reference signals which are anti-phase to each other, and these determine the switching actions of two legs in a two-level H-bridge so that they do not switch simultaneously. When using the unipolar PS-PWM for an MMFCC, each 3-level FC module also has two legs, labelled top and bottom in Fig. 1(a). The top leg is controlled according to the positive reference signal R_+ and comprises two cells: cell 1, consisting of $C_{DC} - C_a - Sa_1 - Sa_4$ and cell 2 containing $C_a - Sa_2 - Sa_3$. Similarly the bottom leg, comprising cell 3 containing $C_{DC} - C_b - Sb_1 - Sb_4$ and cell 4 containing $C_b - Sb_2 - Sb_3$, is switched according to the negative signal R_- .

The two reference signals are compared with four triangular carriers phase shifted by a constant angle $\theta_C = \pi/4$ between each other. The interceptions of each of them with the positive reference R_+ generate four identical but phase shifted pulse trains as shown in Fig. 1(c); these are for driving four complementary switches in cell 1 and cell 2 in the top legs of the two modules. Similarly the interceptions of the same four carriers with R_- are used to control the four cells in the bottom legs. In general the number of carrier waves 'n' is equal to the number of distinct voltage levels between zero

and positive peak phase voltage that an MMFCC can generate. For example for three modules per phase, the number of distinct voltage levels is six, hence six carriers are required.

Applying four switching pulse trains to control the four cell switches of a single module, the natural floating capacitor voltage balances are maintained within a cycle. This can be illustrated using cell 1 in the top leg of module 1 as an example. The PS-PWM waveforms shown in Fig. 1 (b) have reference and carrier frequencies of 50Hz and 250 Hz respectively, giving a frequency modulation index $m_f = 5$. The floating capacitor is set as 5mf and 70V, while the module capacitor C_{DC} is set as a DC supply with 140V.

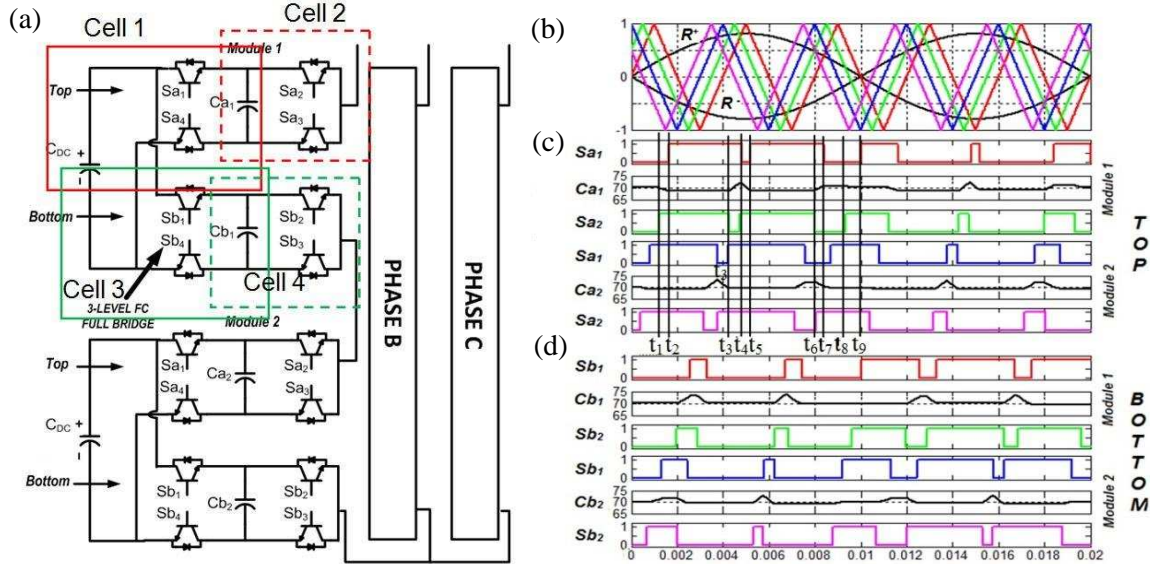


Fig. 1: (a) MMFCC-STATCOM Power Circuit diagram, (b) Reference and Carrier waveforms for PS-PWM Modulation Technique (c) switching pulses for top cells and (d) bottom cells of two modules.

The top two switching pulse trains given in Fig. 1(c) are for control of S_{a1} and S_{a2} in cell 1. At time t_1 a pulse is applied to turn on S_{a2} , setting the module top leg terminal voltage to $+V_{DC}/2$; C_{a1} discharges hence its voltage level falls. This continues until t_2 when S_{a1} is turned on. During t_2 to t_3 the top leg terminal voltage rises to $+V_{DC}$; C_{a1} is neither charging nor discharging, so its voltage stays at the lower discharged level. At t_3 S_{a2} turns off while S_{a1} stays on; this makes the terminal voltage return to $+V_{DC}/2$ as during $t_1 - t_2$, but the switching state is different. In this case the load current path enables C_{a1} to be charged, and hence its voltage rises above the nominal level. In the same way, inspecting the switching states and capacitor voltage changes as shown for the rest of the half cycle from t_3 to t_9 . Likewise for the negative half cycle the switching actions are reverse symmetrical to their positive counterparts. Thus provided the same reference signal is used the voltage for C_{a1} is always balanced. This clearly applies to all the floating capacitors in the other modules.

The above discussion shows that, using PS-PWM control, the MMFCC can be regarded as an H-bridge converter in the steady-state, and hence the consideration of voltage balance control can be mainly focused on the voltages across the module capacitors rather than the floating capacitors. It is also important to note that the unipolar PS-PWM scheme results in equal utilization of the switching states. Thus the voltage stress and switching losses are shared evenly across the switching devices. Clearly when more modules are added in the chain while retaining the same switching frequency per module per cycle, the effective output voltage harmonic frequency increases. This is as a result of the increased number of carrier waves becoming more tightly packed together and thus duty ratio across the unit cells almost identical.

The unipolar switching action on the 4 unit cells in each 3-level FC module results in the harmonics in the output voltage waveform to appear at 4 times the actual cell switching frequency ($f_h = 4 \times f_s$). Each

additional 3-level FC module stacked per-phase pushes this further the spectra by a factor of n , hence the harmonic frequency would be

$$h = j(n \times 4m_f) \pm k \quad (1)$$

where, h = harmonic order, j = harmonic position, m_f = frequency modulation index, k = index of side band. Fourier spectrum analysis of the converters output voltage waveform is shown in Fig. 2

A comparison of total harmonic distortion (THD) at various m_f and m_a is shown. The THD is primarily governed by m_a and varies slightly for various values of m_f . Based on this result, a feasible range in this investigation to maintain good harmonic characteristics would be a modulation frequency index $m_f > 3$ and modulation amplitude index within $0.7 \leq m_f \leq 0.9$.

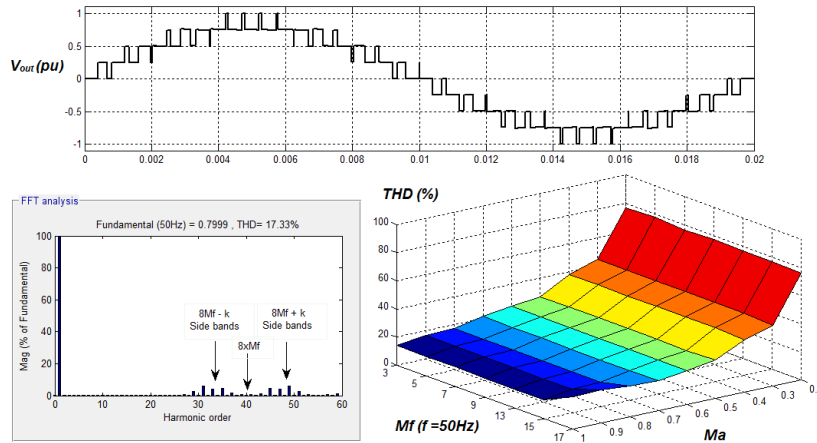


Fig. 2: Fourier Spectrum Analysis of Voltage waveform

3. Control Scheme for an MMFCC-based STATCOM

The power network is rated at 230V, 8.28 KVA, 50Hz. The supply side of the distribution line is modelled as a pi-section equivalent distribution line made of aluminium and of length 2.5km (0.5Ω, 5mH, 10nF per km) corresponding to a reactance of 1.57 Ω. The X/R ratio (short circuit ratio) is greater than 1 showing that the line reactance contributes more to voltage drop across the distribution line. Also connected at the PCC are two loads, a variable load with a power factor of 0.8 drawing a reactive power of 2.07 kVAR, and a static load drawing an active power of 2.07 kW. An R-L filter is used at the converter side to reduce the harmonics due to converter switching. The choice of filtering inductance is based on IEEE 1547 specifications [12-14] which recommends about 30% of the total load impedance. A 20 Ω damping resistor is used to reduce the resonance of the floating capacitors which in this case have no feedback. Each module bus capacitor, C_{DC} , and the module flying capacitors (C_a , C_b) set as 0.26mF and 0.13mF respectively.

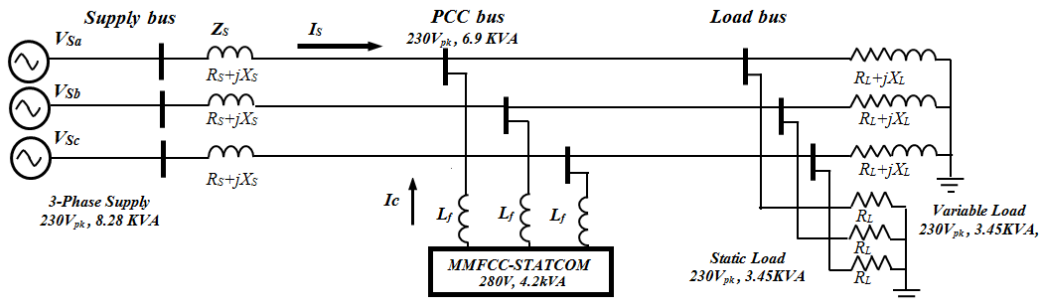


Fig. 3: MMFCC-STATCOM Power System diagram

Crucial requirement for the control scheme is to maintain constant module voltages and ensure that load disturbances/transient changes are maintained within limits. Based on this, the closed loop system comprises the following compensator controllers

- Capacitor DC Bus balancing control,
- PCC voltage regulation control, and
- P+I Current Control

3.1 Capacitor DC Bus Balancing Control

The DC-Bus voltage in each module should ideally be maintained at its required level by its outer module capacitor, but load and switching pattern variations may cause it to fluctuate. A DC-bus voltage controller is, therefore, required to ensure that the DC voltage across every module remains at the specified DC value. The block diagram of the DC bus voltage controller is shown in Fig. 4a. The scheme assumes that the three phase voltages at the PCC-bus are balanced and the STATCOM delivers balanced compensation currents. Hence the controller takes the average value of the three phase limb voltages $V_{dc(avg)}$ as the controlled signal, which is calculated as

$$V_{dc(avg)} = \frac{\sum_{i=1}^6 V_{dc M(i)}}{3} \quad (2)$$

where, i = number of modules and in this study only six modules are used, $V_{dc M(i)}$ represents DC-voltage across each individual module.

The reference DC-bus voltage $V_{dc ref}$ is compared with $V_{dc(avg)}$ and the error is passed onto the P+I regulator in order to generate the d-component of the controlled current vector.

The use of PS-PWM modulation scheme has enabled natural floating capacitor balances, and hence they do not require any feedback control. Using [15], the proportional and integral gain k_p and k_i were chosen as 10, 500 respectively.

3.2 PCC Voltage Regulation Control

The PCC Voltage regulation loop aims to maintain the PCC voltage at the required level given as $V_{AC ref}$. A simple P+I controller is used to generate reactive current element $I_{q ref}$ based on the difference between the PCC voltage and the desired AC voltage set point $V_{AC ref}$. The feedback variable V_{PCC} represents the measured magnitude of the AC voltage at the PCC calculated by resolving the three phase voltage vector into d and q components as shown in (3).

$$|V_{PCC}| = \sqrt{V_{d pcc}^2 + V_{q pcc}^2} \quad (3)$$

The proportional and integral gains were chosen as 9, 500 respectively.

3.1 P+I Current Controller

The compensation current generated by the STATCOM provides a means of regulating the voltages at the two terminals; at the AC side to influence reactive power flow and at the converter DC side to compensate the converter losses. In Fig. 4c, the d and q components $I_{d conv}$, $I_{q conv}$ of STATCOM current vector are measured from converter bus, whilst the $I_{d ref}$, $I_{q ref}$ components are the required d-q current values to be supplied by the converter. They are compared and the error signals are applied to the PI controllers respectively. The d-q output signals from the P+I controllers are combined with the coupling terms, $-\omega L_f$ and ωL_f respectively to form the d-q elements of reference voltage vector required by pulse-width modulation. The pulse signals generated are applied to the converter to achieve compensation. The proportional and integral gain were chosen as 9, 500 respectively.

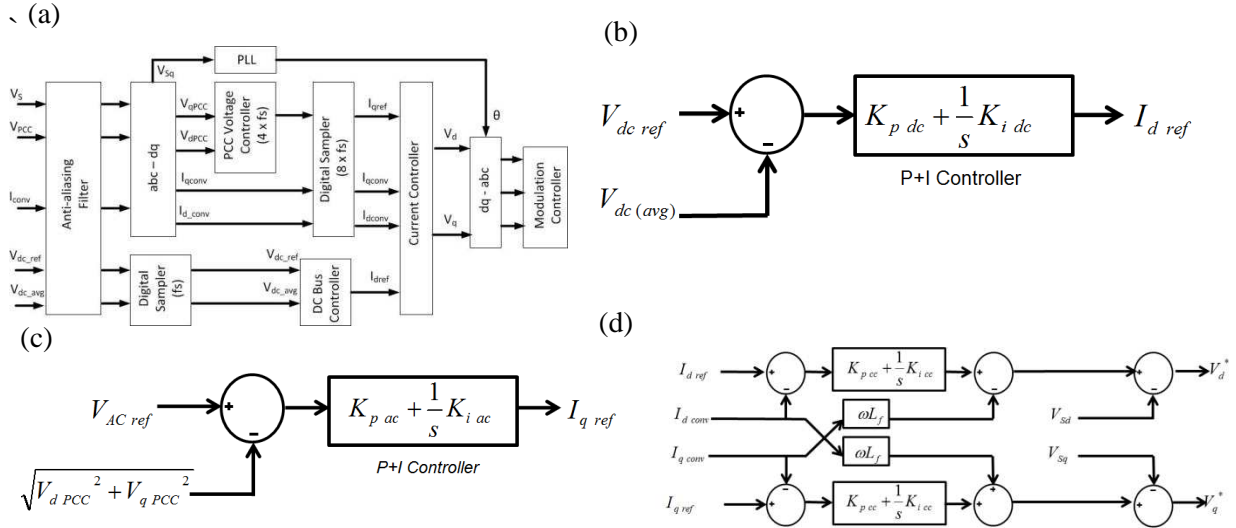


Fig. 4: (a) High level system control diagram, (b) Capacitor DC bus voltage regulator control (c) AC voltage regulator control (d) Compensation current controller

4. Analysis and Simulation Results

Matlab Simulink was used to investigate the systems configuration outlined earlier and two different scenarios were simulated. Firstly, reactive compensation of voltage drop realised at the PCC of the distribution line. Next, unity power factor correction at the PCC when the variable load draws a reactive power of 2.07 KVA. Total simulated time is 3 seconds, converter switching frequency = 750Hz. Converter start/charge-up was completed at approximately 0.04 seconds (2 fundamental cycles) while complete system steady state was achieved at approximately 0.08s (4 Fundamental cycles). All investigations are performed under balanced conditions as such; only single phase representation (Phase A) waveforms are shown for clarity.

4.1 PCC Voltage regulation based on MMFCC-STATCOM

At the start of the simulation ($0 < t < 1$), a small static load is connected and draws an active power of 2.07 KW causing a voltage drop of 1.6 V across the line. At time interval ($1 < t < 2$), a larger static load is switched in addition drawing an active power of 3.45KW corresponding to a voltage drop of 4.3V. At the time interval ($2 < t < 3$), the large static load is switched off and the system returns to back to a voltage drop of 1.6V. The converter compensates by injecting reactive power throughout the whole simulation. The voltages and currents have been normalised to per unit values by dividing by their respective base values.

Fig. 5 (a)-(f) shows the PCC side waveforms. Within the time intervals ($1 < t < 2$) and ($2 < t < 3$) the STATCOM supplies reactive power (capacitive) in order to return the voltage to its nominal value. This operation of the STATCOM converter causes the magnitude of the PCC voltage to remain the same as shown in (c)-(d). The reactive power at PCC hence is -365 VAR and -175 VAR respectively is as shown in (e)-(f). The power factor is no longer unity as expected for PCC voltage regulation and the response of the converter to generate reactive power is fast at 3ms.

Fig. 6 (a)-(f) shows the converter side waveforms. Within the time intervals ($1 < t < 2$) and ($2 < t < 3$) the STATCOM supplies a capacitive current ($+90^\circ$) of 1A and 3.5A respectively in (a)-(b). This operation of the STATCOM converter ($1 < t < 2$) causes a modulation index decrease from 0.81 to 0.78 and increase in the converters angle from -0.11 rads to -0.35 rads as shown in (c)-(d). The reactive power generated from the converter is -685 VAR and -235 VAR respectively is as shown in (e)-(f).

Fig. 7 shows the resulting control signals at the different control blocks and as shown voltage regulation achieved between the time intervals ($1 < t < 2$) and ($2 < t < 3$). The response times are fast seen to 40ms and 30ms respectively.

Fig. 8 shows the DC bus balancing across the capacitors of a single phase. The DC Bus voltage controlled to a nominal value of 140 V across the 0.26 mF capacitor. At the time interval ($1 < t < 2$), the module bus dc capacitors experienced a higher voltage variation of 7 V ($\pm 0.05\%$) while the flying capacitors experienced a deviation of approximately 3.5 V ($\pm 0.05\%$). The ripple are hence maintained within ($\pm 10\%$) its nominal value. As noticed natural balancing occurs using PSWPM and the inner flying capacitor voltages are also balanced.

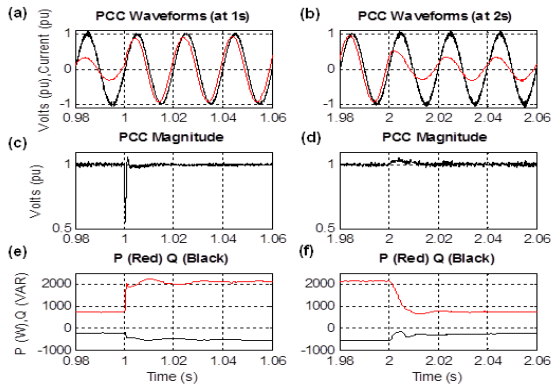


Fig. 5: PCC Side Waveforms

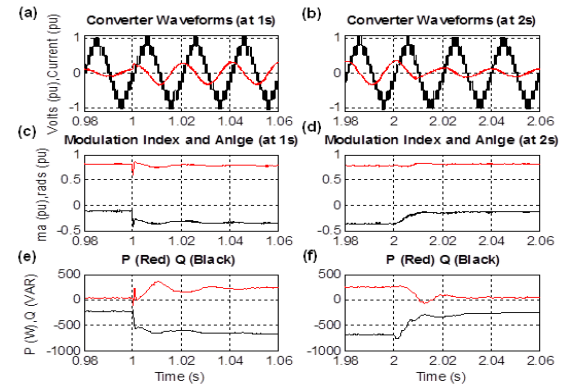


Fig. 6: Converter Side Waveforms

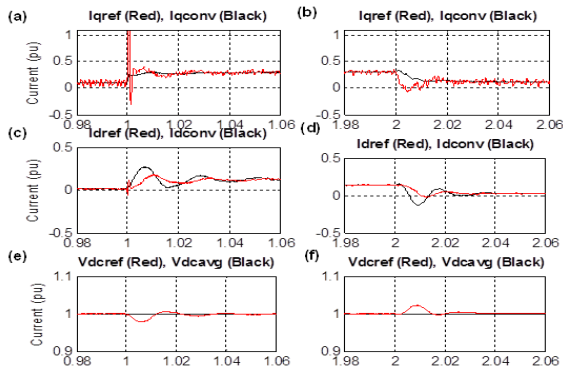


Fig. 7: Power System Control Signals

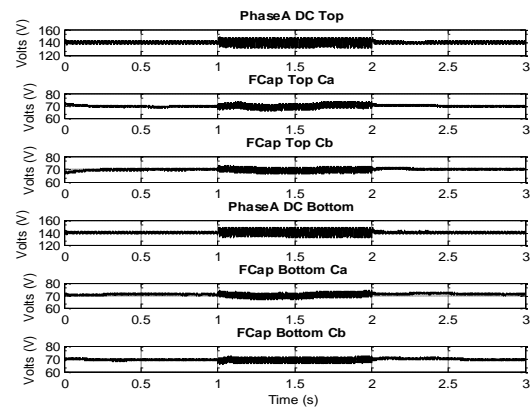


Fig. 8: DC Capacitor Waveforms

3.1 Unity Power Factor Correction based on MMFCC STATCOM

At the start of the simulation ($0 < t < 1$), the static load is connected and draws an active power of 2.07 KW. At time interval ($1 < t < 2$), a variable inductive load in addition is switched in absorbing a reactive power of 690 VAR. At the time interval ($2 < t < 3$), the variable load is switched off and the system returns to normal. The converter compensates by injecting reactive power when the inductive load is switched in.

Fig. 9 (a)-(d) shows the PCC side waveforms. Within the time intervals ($1 < t < 2$) the STATCOM supplies reactive power (capacitive) in eliminate the reactive power absorbed at the PCC. This operation of the STATCOM converter ensures there is no reactive power at the PCC as shown in (c)-(d). The response of the converter takes 0.1s to compensate for reactive power.

Fig. 10 (a)-(f) shows the converter side waveforms. Within the time intervals ($1 < t < 2$) the STATCOM supplies a capacitive current ($+90^\circ$) of 2.6 A in (a)-(b). This operation of the STATCOM converter ($1 < t < 2$) causes a modulation index decrease from 0.81 to 0.78 and increase in the

converters angle from -0.02 rads to -0.28 rads as shown in (c)-(d). The reactive power generated from the converter is -560 VAR as shown in (e)-(f).

Fig. 11 shows the resulting control signals at the different control blocks and as shown unity power factor correction is achieved between the time intervals $(1 < t < 2)$. The response time is seen to be 0.1 s.

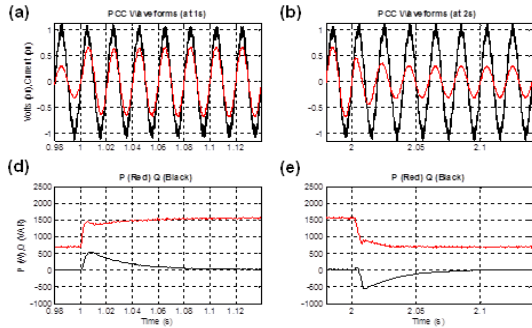


Fig. 5: PCC Side Waveforms

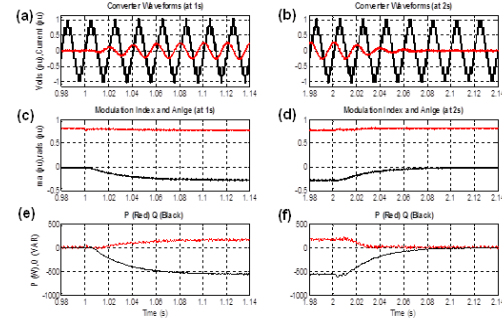


Fig 6: Converter Side Waveforms

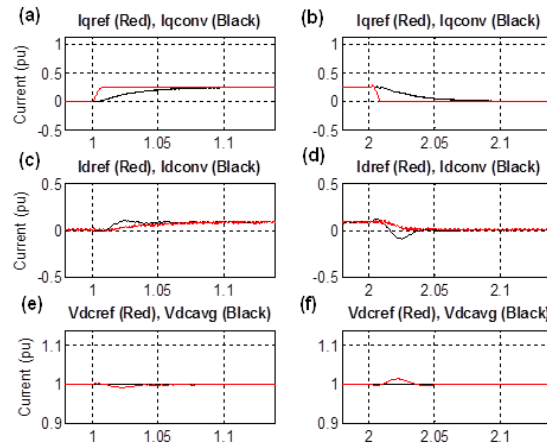


Fig. 7: Power System Control Signals

Conclusion

This paper has achieved the modelling and analysis of modular multilevel cascade converter based on single-star FC cells (MMCC-SSFC) and discussed how Phase Shifted PWM STATCOM scheme effectively maintains the balancing of the floating capacitors with a modular multilevel flying capacitor cascade converter based on single-star FC cells (MMCC-SSFC). Simulation results obtained from a 8.28 KVA rated simulation model verify this topology and its operation for voltage regulation and unity power factor correction. This paves the route for experimental validation of the MMFCC in the laboratory.

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