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Editorial

Focus on topological quantum computation

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Abstract

Topological quantum computation started as a niche area of research aimed at employing particles with exotic statistics, called anyons, for performing quantum computation. Soon it evolved to include a wide variety of disciplines. Advances in the understanding of anyon properties inspired new quantum algorithms and helped in the characterization of topological phases of matter and their experimental realization. The conceptual appeal of topological systems as well as their promise for building fault-tolerant quantum technologies fuelled the fascination in this field. This ‘focus on’ collection brings together several of the latest developments in the field and facilitates the synergy between different approaches.

Keywords: topological quantum computation, quantum error correction, topological order, quantum Hall effect, non-Abelian anyons, Jones polynomials

The great promise of quantum computers has to be balanced against the great difficulties of actually building them. Foremost among these is the fundamental challenge of defeating decoherence and errors. Small improvements to current strategies may not be sufficient to overcome this problem; radically new ideas may be required. Topological quantum computation is precisely such a new and different approach [1]. It employs many-body
physical systems with the unique property of encoding and processing quantum information in a naturally fault-tolerant way.

Research on topological quantum computation has become a highly interdisciplinary field, with frontiers in physics, mathematics and computer science. Moreover, advances in the theoretical understanding of abstract topology [2], in physical realizations of topological matter [3] and in computational paradigms [4] have been closely interrelated, with developments in one area strongly influencing the others. In recent years we have witnessed significant theoretical and experimental developments. These include major experimental and theoretical advances in fractional quantum Hall systems that support the existence of non-Abelian anyons—the building blocks of topological quantum computation—as well as the predication and experimental discovery of novel spin—orbit systems such as topological insulators [5].

The aim of this ‘focus on’ collection is to bring together the latest developments in a variety of areas, with the goal of promoting new results to a wider community of scientists and advancing the synergy between different approaches. To a large extent, we believe this has been a success.

One of the dominant directions of the field has been towards better understanding topological matter by investigating the phase transitions between topological phases—how one phase condenses out of another, often in some sort of confinement transition. Loop models, as the simplest of all topological phases, were studied by Monte Carlo methods [6], and semi-analytic high-order perturbation theory methods were applied to study the transitions in $\mathbb{Z}_n$ topological phases [7]. In some cases, powerful purely analytic approaches could be applied to study the phase transitions in detail [8–10]. There was substantial focus on identifying order parameters for such topological phase transitions to try and draw analogies with the conventional Landau theory of phase transitions [11, 12]. Despite this progress, and although some general principles are now established [13], a unified theory of the details of phase transitions between topological phases is still absent and remains an active topic of research.

Another emerging direction in the field has been the study of Majorana fermions and the physical systems that may harbour them. In the past few years, several proposals were made for creating analogs of chiral p-wave superconductors using spin–orbit-coupled superconductors that would host non-Abelian Majoranas as their quasiparticle excitations (see [14] for a review of these ideas). Indeed, this development became such an active field that it called for a separate collection [15]. However, before that issue was created, many groundbreaking works on the topic ended up in the current ‘focus on’ collection. One direction is in determining the parameters necessary for obtaining topological superconductivity in spin–orbit-coupled systems [16]. Another is the proposal of experiments (in this case, Ettingshausen effect experiments [17] or quantum point contact tunnelling experiments [18]) that might establish the existence of Majorana modes in these systems. Yet another direction is in the development of device designs to read out [19, 20] or manipulate [21] such Majoranas qubits. Majoranas, as perhaps the simplest non-Abelian objects, were also studied in several other contexts, including phase transitions [8], the fractional quantum Hall effect [22], the Kitaev honeycomb model [23–26], Hanbury–Brown–Twiss experiments, [27] and the quench dynamics of spin chains [28]. It is certain that the study of Majorana physics will be a main direction of the field in the future.

A perennially dominant direction since the inception of the field has been the study of fractional quantum Hall effects [29, 3]. This is perhaps not surprising as the quantum Hall effect in semiconductors remains the only physical system convincingly established as nontrivial
topological matter. In this issue, quantum Hall physics was also discussed in other physical realizations ranging from mono-layer and bilayer graphene [30] to cold atoms in non-Abelian gauge fields [31, 32]. The presence of extra degrees of freedom, such as spin and valley, over the conventionally studied spinless electrons provides the freedom to have richer physics, including charged spin textures [33]. In another direction, a nice theoretical advance (the extension of a many-year project by some of the same authors and others) was the development of a conformal field theory approach to the quantum Hall hierarchies [34]. As in the broader field of condensed matter, understanding the patterns of entanglement of fractional Hall states has becoming an increasingly important and interesting topic [35, 36].

While several experimental works attempting to demonstrate non-Abelian quasiparticles in the fractional quantum Hall effect have recently been performed [37, 38], the interpretation of these experiments is very controversial, and this remains a forefront of research. Several papers in the current issue were aimed at either providing other methods to make this demonstration, for example by measuring tunnelling spectra [39] or examining the additional physics of these experiments (in this case, the Zeno effect [22], or disorder in quasiparticle lattices [40]) not previously considered in the predictions. In our entire ‘focus on’ collection, disappointingly, only a single submitted manuscript was actually a real experiment [41], and this, although a nice experiment demonstrating Aharonov–Bohm oscillations in quantum Hall samples, remains quite a distance from the desired result that would convincingly show non-Abelian physics.

Back to the theoretical front, we note that perhaps one of the most studied models has been the Kitaev honeycomb model [23]. Unsurprisingly, this continued to provide fertile ground for further thought. Within this framework, the interactions between non-Abelian vortices and the nucleation of new topological phases was studied [24], and the braiding statistics were evaluated explicitly to very high accuracy [25]. A square-octagon variant of the Kitaev honeycomb model was shown to exhibit a rather remarkably rich phase diagram [26].

Another of the most celebrated models of topological matter is the toric code model [1]. In one study, the thermal stability of this model was examined [42]. Another work considered how this model might actually be simulated using trapped ions [43]. Since its inception, the toric code model has since been generalized to $\mathbb{Z}_N$ models [7], non-Abelian discrete gauge theories [9], and finally to their most general form, the Levin–Wen models [8, 10, 44–46]. One work in this issue geometrically reinterpreted the Levin–Wen partition functions as knot invariants [45]. Another explored (at least in one dimension) generalising to theories based on non-unitary conformal field theories [46].

On the more computational side of research, one of the key ideas that launched the field was the realization that the evaluation of the Jones polynomial, a ‘hard’ problem for a classical computer, might not be ‘hard’ for an anyon computer [47]. Indeed, evaluation of Jones polynomials [4, 48] is perhaps one of the most natural algorithms for a topological quantum computer. In this issue, extensions of this line of thought have resulted in advances in determining the precise complexity of this quantum algorithm [49] and in its relationship to Khovanov homology—a natural ‘categorification’ of the Jones polynomial [50].

The quantum gates produced by anyonic braiding are very specific, tightly connected to the statistical properties of the anyons. In this ‘focus on’ collection, it was shown that no computationally universal anyon system can be built where two qubit gates do not have finite leakage errors [51]. This further draws attention towards the necessity of approximating quantum gates to high accuracy (even though they must remain imperfect). One approach
pursued towards designing such high-accuracy gates is to use hashing techniques [52]. Finally, ideas from cluster state quantum computation were applied to the realm of topological models [53, 54].

As witnessed from these contributions, it is clear that the field of topological quantum computing, and topological matter in general, has continued to progress at a remarkable rate. Despite these advances, several fundamental questions still remain open. Arguably, two main directions can be identified: building systems where non-Abelian statistics can be conclusively measured, and finding a topologically inspired quantum memory that can successfully combat physically induced errors. It is the hope and vision of the editors that bringing together methods and techniques from a wide range of fields can eventually enable the construction of topological quantum computation.

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