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Prediction of the mechanical response of canine humerus to three-point bending using subject-specific finite element modelling

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Abstract

Subject-specific finite element (FE) models could improve decision making in canine long bone fracture repair. However, it preliminary requires that FE models predicting the mechanical response of canine long bone are proposed and validated. We present here a combined experimental-numerical approach to test the ability of subject-specific FE models to predict the bending response of **seven** pairs of canine humeri directly from medical images. Our results show that bending stiffness and yield load are predicted **with a mean absolute error of 10.1% (\pm 5.2%) for the fourteen samples.** This study constitutes a basis for the forthcoming optimization of canine long bone fracture repair.

Keywords

Finite element modelling

Subject-specific

Canine bone material properties

Bending test

Canine humerus

1 Introduction

2 Long bone fracture constitutes a common reason for medical consultation within
3 veterinary orthopaedic services^{1,2}, as emphasized by the substantial recent literature
4 concerning the choice of adapted implants³⁻⁶. Associated surgical interventions are
5 often complex given that each fracture has its own particularities. Canine bone
6 fracture repair differs from the human case in the sense that (1) the physiological
7 characteristics and morphology of the injured bones in animals vary considerably⁷, (2)
8 the animal is not able to limit its activity during the post-operative period, which may
9 lead to premature overloading, and (3) the surgeon is often confronted to cost
10 limitations concerning orthopaedic material. As a result, the treatment of such
11 fractures (implant type, dimension, location ...) depends to some extent on the
12 surgeon's experience, who tries to find a trade-off between a minimum stiffness
13 required for fracture stabilization and a sufficient flexibility essential for bone
14 remodelling. Although available handbooks guide the surgeon in the choice of a suited
15 treatment for each particular fracture, they are still based on empirical knowledge, and
16 there is a lack of studies assessing the effect of different treatment types on the
17 biomechanical properties of the reconstructed bone. This insufficient knowledge may
18 partly explain the complications that are still frequent in the field of canine fracture
19 repair^{8,9}.

20 In order to improve the surgical procedure, ex-vivo experiments^{10,11} as well as
21 numerical biomechanical studies¹²⁻¹⁴ have been reported. Indeed, numerical
22 approaches, such as Finite Element (FE) modelling may enable to evaluate non-
23 invasively the effect of various implants or their combination on the same bone
24 sample. However, these FE studies are often based on simplistic bone models (i.e.
25 elastic, linear, homogeneous cortical and trabecular tissues, etc...). A milestone in
26 delivering relevant data in a subject-specific approach consists of including the bone
27 external geometry and heterogeneous material properties from the information
28 available in CT images. Such subject-specific FE approaches have been developed in
29 human long bone analysis and satisfyingly predicted the failure risk in proximal
30 femur¹⁵⁻¹⁸. However, available studies in human have often led to moderately accurate
31 results as far as the prediction of the global biomechanical response of long bones are
32 concerned, probably due to accumulating inherent approximations throughout the
33 model generation. Particularly, it is not clear if the consideration of density-dependent
34 material properties leads to better results than the modelling of long bone with two
35 materials (trabecular and cortical tissues) separated from a density criterion. The
36 interest of considering anisotropic material properties is also not clear. Moreover, if
37 one wants to extend these subject-specific FE models to canine bone, a supplementary
38 difficulty will come from the variability of bone material properties from one breed to

39 another¹⁹, and from the absence of data concerning relationships between CT
40 information and bone material properties for dogs.

41 Such FE models are usually validated using *ex vivo* mechanical tests such as
42 bending^{20,21}, torsion²² or compression^{17,23}. These combined experimental-numerical
43 approaches require that a particular attention is paid to the application of similar
44 Boundary Conditions (BC), such as load application and displacement restriction, in the
45 experimental and computational setups²⁴.

46 In the present contribution, the hypothesis was that subject-specific FE models are
47 able to predict the global mechanical response of canine long bones to three-point
48 bending tests. The aims of the present work were therefore (1) to provide a direct
49 subject-specific validation of canine long bone FE models including a novel density-
50 elasticity law; and (2) to assess the requirements for the bone material model to
51 replicate measured *ex vivo* behaviour.

52 **Material and Methods**

53 A combined experimental and computational approach was developed to validate the
54 FE models with *ex vivo* three-point bending data, i.e. overall load/deflection behaviour
55 and local fracture patterns. All dynamic FE analyses were performed using the in house
56 non-linear implicit FE code MetaFor (metafor.ltas.ulg.ac.be).

57 *Specimen preparation, imaging, and mechanical testing*

58 Eight pairs of canine humeri were initially harvested from adult dogs euthanized for
59 reasons unrelated to this study. After harvesting, one dog (i.e. one pair of humeri) was
60 excluded from this study due to the observation of severe knee arthrosis. Dog weights
61 finally ranged from 19 to 39kg. Soft tissues were carefully removed and samples were
62 wrapped in saline soaked sponges and stored at -20°C. Samples were prepared for
63 three-point bending mechanical tests at room temperature. In order to accurately
64 control the location of the bones within the custom bending stand and to restrict
65 rotations around the bone diaphysis axis during the bending tests, the epiphyses were
66 embedded into 60×60×60mm³ moulds made of two-component polymeric resin
67 (Motip®, Germany) (Figure 1). A particular attention was paid to define resin moulds
68 orientation with respect to the bone sample position in a reproducible way. Firstly, we
69 used the origin of the medial and lateral collateral ligaments as anatomical landmarks
70 to define a reference axis. Then, the distal resin mould was created in such a way that
71 this anatomical reference axis was parallel to two surfaces of the resin block (namely
72 its cranio-caudal and proximal-distal surfaces). The second mould was perfectly aligned
73 with the first one, using custom-made jig (Figure 1.a).

74 The samples were imaged using a CT-scanner (Siemens SOMATOM at 120 kVp) with a
75 slice thickness of 0.75mm and a spatial resolution of 0.1445mm. A phantom (Siemens

76 BMD calibration phantom²⁵) was used to calibrate the bone densities with respect to
77 the Hounsfield Units (HU) issued from the CT acquisition^{18,26}. Particular attention was
78 paid to keep the samples packed in saline-soaked wraps throughout the procedure in
79 order to avoid tissue dehydration. The following relation was obtained:

$$80 \quad \rho = 4.9332 \cdot 10^{-4} \text{HU} + 0.9839 \text{ (1)}$$

81 Samples were placed on a custom adjustable bending stand (Figure 1.b) made of two
82 steel half-cylinders. The cylinders positions were adjusted so that they were in contact
83 with the middle of each resin mould in the axial direction of the bone. The bending
84 tool consisted in a cylindrical punch located longitudinally at half the distance between
85 the two resin moulds. The stand was mounted in a 100 kN servo-hydraulic testing
86 machine (Zwick/Roell, Ulm, Germany, load cell : XForce HP 5 kN). A medial-lateral
87 displacement was applied to the bending tool at a speed of 0.2 mm.s⁻¹ after a preload
88 of 50 N. The samples were tested until complete fracture. Tool displacement
89 (hereafter called deflection) and vertical force (i.e. shear force) were recorded. Two
90 high speed cameras (Vision Research v7.3) recording 1000 frames/s were used in order
91 to visualize the fracture onset.

92 *Finite Element modelling*

93 Each tested sample was modelled with a subject-specific approach. The geometry of
94 the bone were built from the 3D CT data using 3D-Slicer²⁷ (www.slicer.org) for
95 segmentation and a dedicated in-house algorithm²⁸ for the generation of smooth
96 multi-region surface meshes. The bone volume mesh was obtained using Tetgen
97 (WIAS, Berlin, Germany), generating linear tetrahedra. Final mesh size was issued from
98 a mesh dependency analysis reported hereafter.

99 The resin moulds were not meshed in the FE model but considered as single
100 deformable hexahedrons whose coordinates were automatically computed from the
101 boundaries of resin moulds in the surface mesh (Figure 1.b). Resin was considered
102 linear elastic, with an elastic modulus of 900 MPa characterized from preliminary
103 experiments. Elements were assigned a density issued from the calibration phantom,
104 and equal to $1\text{g}\cdot\text{cm}^{-3}$ for resin. The interaction between the bone and the resin moulds
105 was modelled using springs (arbitrary stiffness of 100 N mm^{-1}) linking the hexahedron
106 nodes with each of the bone surface nodes located within the resin moulds (Figure 1.b)
107 in order to constrain the relative displacement between bone and resin. This numerical
108 representation of the resin blocks is totally equivalent to a penalty formulation in
109 contact algorithms with bilateral restrictions to enforce the continuity of the

110 displacement field at the interface between bone and resin. The proximal resin mould
111 was restrained in the cranio-caudal direction.

112 The bending stand was modelled as two rigid half-cylinders located longitudinally at
113 the middle of each resin moulds. The frictional contact condition between the resin
114 moulds and the bending stand was modelled with a Coulomb's law, with static and
115 dynamic friction coefficients set at 0.7, corresponding to a dry static contact between
116 steel and steel²⁹. This value was chosen due to the lack of published value for resin-
117 steel contact. Each half-cylinders of the bending stand were restrained in their 6
118 degrees of freedom.

119 The bending tool was modelled as a rigid half-cylinder located, as marked
120 experimentally, at half the distance between the two resin moulds. Displacement was
121 applied to the tool in the medial-lateral direction. Contact between the bending tool
122 and the bone surface was modelled as sticking contact.

123 A sensitivity analysis was performed analysing the effect of the resin properties, the
124 stiffness of the springs used to attach bone to resin blocks and the friction coefficient
125 between resin and stand on the predicted bone stiffness and yield load. Load-
126 deflection curves were obtained as the sum of the medial-lateral component of the

127 contact force and the tool displacement at each time step. The experimental preload
128 was mimicked by excluding the initial forces below 50N from the simulation results.

129 For each sample, user interaction was only needed for the image segmentation step.
130 To avoid user variation, all other steps of the model creation and analysis were
131 automated, based on the size of the samples extracted from the segmented data. All
132 FE analyses were performed using local HPC facilities (parallel computation on 144
133 cores).

134 *Bone material models*

135 Three different materials models were considered for the bone: a density-dependent
136 transversely isotropic model, a density-dependent isotropic model, and a two-material
137 isotropic model (one material model for cortical bone and one for trabecular bone).

138 For the density dependent models, material parameters were mapped against the HU
139 values from the CT scans **starting from equation (1)**. The following mapping procedure
140 was applied: (1) for each mesh element, the smallest rectangular box that embraced
141 the tetrahedron was defined, (2) for each voxel included within this box, material
142 properties (see next section) were computed from the density computed from the HU
143 field, and (3) material properties were averaged on this box and assigned to the mesh
144 element. A particular attention was paid to reduce the partial volume artefacts: to this

145 end, we firstly separated the mesh elements that had at least one point belonging to
146 the bone surface (*outer cells*) from the other mesh elements (*inner cells*). Each outer
147 cell was then associated to its closest inner cell, and was assigned the HU value of its
148 associated inner cell when it was higher than its own HU value. This procedure
149 significantly reduced the partial volume artefact, provided that the bone cortical wall
150 was described by a sufficient number of mesh elements, i.e. that the mesh was
151 sufficiently dense.

152 It is known that the properties of canine bone depends on dog mass¹⁹. Therefore a
153 density-elasticity relationship had to be derived for canine bone. It would indeed not
154 be justified to use a unique density-elasticity relationship determined from human
155 bone. Published experimental data¹⁹ reported the elastic moduli of canine cortical
156 bone as a function of dog breed: 13.3GPa (dog mass=5kg), 14.9GPa (dog mass=12kg),
157 16GPa (dog mass=25kg), 16.3GPa (dog mass=50kg). Comparing that data to an
158 average reported elastic modulus of 17.9GPa for human cortical bone³⁰, the following
159 relation between human data and canine data was extrapolated (using a common
160 mean-square method):

161
$$E_{\text{canine}}(\rho) = E_{\text{human}}(\rho) \times (0.3 \exp(-5/m) + 0.64) \quad (2)$$

162 by denoting m the dog mass. This relation is illustrated on Figure 2, and assumes that
163 bone properties depend only on dog mass and not on the breed.

164 This canine-to-human relation was used to weight existing density-elasticity
165 relationships validated for human data:

166 For the density-dependent transversely isotropic model, bone was considered as an
167 elastoplastic material without distinction between cortical and trabecular tissues
168 (except for density). The elastic part of the model was built from relation (2) and using
169 an orthotropic elasticity-density relationship for human bone in tension³¹:

$$\begin{aligned} E_l &= 2065\rho^{3.09} & G_{lt} &= 0.29E_l \\ E_t &= 2314\rho^{1.57} & G_{tt} &= 0.2E_l \end{aligned} \quad (3)$$

171 by denoting E_l and E_t the elastic moduli (MPa) in the longitudinal and transverse
172 directions, G_{lt} and G_{tt} the shear moduli (MPa), and ρ (g cm^{-3}) the apparent density
173 issued from CT calibration. These relations valid for human bone were weighted using
174 relation (2) in order to model canine bone. Asymmetric elastic material properties
175 were assumed by considering that the elastic modulus was 6% higher in compression
176 than in tension³².

177 The global longitudinal direction was automatically computed for each sample, based
178 only on the central third of the bone (representing the diaphysis, see Figure 3). The

179 mesh nodes belonging to the bone surface and included in this part were selected, and
180 used to compute a least-square line defined as the longitudinal direction. The
181 transverse direction was defined perpendicularly to this direction, in a plane
182 containing the tool displacement vector.

183 The yield surface was defined through a Von Mises criterion with linear isotropic
184 hardening. The initial yield stress was obtained from the yield strain of 0.73% reported
185 for human cortical bone³³ and the mean elastic modulus (defined as the average of
186 longitudinal and transverse moduli) following the relation:

$$187 \quad \sigma_y = 0.0073(E_l + E_t) / 2 \quad (4)$$

188 The role of the longitudinal stress was therefore considered predominant in the bone
189 yield. Post-yield hardening was set as 5% of the initial, density-dependent, mean
190 elastic moduli³⁴.

191 The same procedure was applied for the density-dependent isotropic model. The
192 unique Young modulus was defined as the mean of the computed longitudinal and
193 transverse modulus for a given bone density (relation (3)) weighted by the correction
194 coefficients given in relation (2). Yield was modelled identically to the previous model.

195 For the two-material isotropic model, trabecular and cortical canine tissues were
196 respectively modelled with Young's modulus of 750MPa and 15GPa and a Poisson's
197 ratio of 0.3³⁵. Cortical and trabecular tissues were separated using a threshold in
198 terms of HU values. Cortical tissue was assumed for HU values superior to either
199 600HU or 400HU in order to assess the sensitivity to this parameter. Yield was
200 modelled identically to the previous models.

201 *Statistical analysis*

202 For each tested bone, bending stiffness (least-square linear regression of the linear
203 part of force-deflection curve passing through the origin) and yield load (intersection
204 between a parallel to this linear regression with a 0.1 mm offset and the force-
205 deflection curve) were extracted and compared between the experimental and
206 computational data.

207 In order to emphasize the statistical significance of our model, we performed various
208 statistical analyses from our experimental results (14 samples from 7 dogs) and our
209 numerical results (56 models: 14 density-dependant transversely isotropic models, 14
210 density-dependant isotropic models, and 14 two-materials isotropic models with a
211 segmentation threshold of 400 HU or 600 HU). Analysis of variance (ANOVA) was used

212 as the common test to quantify the difference between two sets of data, with a default
213 p-value of 0.01 (when not detailed).

214 **Results**

215 *Experimental results*

216 Experimental results for the seven pairs of humeri are represented in Figure 4. A large
217 intra- and inter-variability was observed: as an example, a mean difference of 14.6% in
218 stiffness between the left and right humerus of the same dog. Left and right humerus
219 of the same dog were however not different (both in terms of stiffness and yield load)
220 in the sense of an ANOVA analysis. The coefficient of variation (ratio between standard
221 deviation and mean) of the stiffness is equal to 20.2%. The data showed a weak
222 correlation between dog mass and mean humerus stiffness (correlation coefficient of
223 0.65). While the failure was sudden for six samples, it was more progressive for the
224 others and no clear fracture pattern was therefore visible.

225 *Computational results*

226 The meshes resulting from the reconstruction of the segmented CT images together
227 with the mapping procedure are represented in Figure 5 for all bone samples. Bone
228 mesh made of approximately 300 000 tetrahedral linear elements (60 000 nodes) led
229 to a relative difference of 2.5% on strain energy density (SED) and 1.4% on stiffness

230 compared to the values obtained for 160 000 nodes. The results of the sensitivity study
231 for one humerus are reported in Table 1. These data emphasize that the simulation
232 results are not sensitive to resin properties, indicating that the resin does not deform
233 substantially during the bending test. Moreover, the simulation results are very slightly
234 sensitive to the stiffness of springs used to attach bone to resin (2% of deviation for a
235 variation of five orders of magnitude). A stiffness of 100N/mm (i.e. of the same order
236 of magnitude than the bone bending stiffness) has been consequently selected for
237 every simulations. However, this sensitivity study emphasizes that the friction
238 coefficient does have an effect on predicted stiffness and yield load. A friction
239 coefficient of 0.7 has been chosen for the simulations due to the lack of existing data,
240 as long as such data are difficult to measure experimentally.

241 For the density-dependent transversely isotropic model on the fourteen samples, the
242 bending stiffness was predicted with a maximum error of 21.7% (absolute value of the
243 mean error = 10.1% \pm 5.2%). The yield load was predicted with an absolute value of the
244 mean error 11% \pm 11.3%, but was unsatisfyingly predicted for one sample over the
245 fourteen samples (maximum error = 43.5%, see Figure 6). Correlation coefficients
246 between predicted and measured values were 0.86 for stiffness and 0.74 for yield load.
247 A Bland-Altman representation of the simulation results obtained with this model has
248 also been provided (Figure 7) : it clearly illustrates the good prediction ability of this

249 model. However, this representation clearly emphasizes that the values of bending
250 stiffness and yield load are badly predicted for one sample (#6 right).

251 Results of the different models were confronted to experimental results in the sense of
252 ANOVA statistical tests, and the *p-values* issued from these tests are gathered in Table
253 2, under the null hypothesis that experimental and simulations results have the same
254 mean (i.e. if the *p-value* is near to zero, experimental and simulation results are
255 significantly different). From this analysis, it is clear that the density-dependant
256 transversely isotropic model is the most predictive model among the four different
257 models tested, and especially compared to the density-dependant isotropic model, as
258 illustrated on Figure 8. Surprisingly, the computational results are better in the case of
259 the two-material isotropic models (no matter the segmentation threshold) than in the
260 case of density-dependant isotropic models.

261 Results of the FE simulations for the two-material isotropic model are represented in
262 Figure 9, with trabecular and cortical tissues being separated either from HU values of
263 400 or 600HU in order to quantify the sensitivity of the bending response to this
264 threshold. There is no statistical difference between the two threshold values used to
265 separate cortical from trabecular tissue in the case of two-material models.

266 **Discussion**

267 *Model accuracy*

268 A finite element mesh of 60 000 nodes showed to be a converged mesh for the bone
269 stiffness and strain energy density (SED). A satisfying prediction of bone stiffness was
270 obtained for every samples, whereas the yield load was satisfyingly predicted for 13
271 over 14 samples. The reported computational results were insensitive to the
272 properties assigned to the resin block holding the bone epiphysis; this indicates that
273 resin blocks do not deform much during the simulations. The computational
274 representation of those blocks is thus a good approximation of the blocks behaviour
275 and interaction with the bone.

276 Using the verified and validated non-linear FE software Metafor³⁶⁻³⁹ to analyse long
277 bone three-point bending tests permits high automation of the model pre- and post-
278 processing steps. This reduces user-variability to the image segmentation step only. All
279 other parameters, especially as far as the definition of model boundary conditions
280 representative of the experimental conditions is concerned, are subject only to the
281 experimental variability.

282 Density-elasticity relationships for canine long bone as a function of dog mass were
283 determined by weighting human relationships from published canine bone properties.

284 Using material parameters from literature only, and not specifically calibrated on the
285 experimental results, the produced models were able to satisfyingly predict bending
286 stiffness and yield load. However, more detailed studies on microstructure or
287 composition of canine bone as a function of mass (or breed) would be required in
288 order to propose a more comprehensive relation.

289 The predictive power of the models for stiffness values and yield loads is here reflected
290 not only by a good correlation but also by a good concordance, which is less often the
291 case in published models^{40,41}. This therefore suggested that the approach used in this
292 work produces valid models to predict bone stiffness and yield loads in three-point
293 bending of canine long bones.

294 *Comparison between models*

295 The benefit of the non-linear density-dependent transversely isotropic model
296 compared to the two other models is demonstrated in terms of its improved
297 prediction capability. However, it is surprising that the two-material isotropic model
298 leads to better predictions than the density-dependent isotropic model. This may be
299 explained by the fact that, during a bending test, the bone is essentially subject to
300 tension and compression, and therefore the longitudinal modulus of the bone plays a
301 crucial role compared to transverse modulus. In the case of the density-dependant

302 isotropic model, the computed average Young modulus is therefore underestimated,
303 for a loading involving mainly the longitudinal direction. Predicted stiffness is thus
304 globally underestimated using the density-dependant isotropic model. On the
305 contrary, the two-material model may widely overestimate the Young modulus by
306 considering constant density for cortical bone, as it is clearly seen that it is not uniform
307 over the cortical bone (Figure 5). Therefore, , it may lead to higher errors in more
308 complex loading modes even without involving a huge overestimation of bone
309 properties in the case of bending loads. For instance, a HU value of 1500HU for cortical
310 bone corresponds to longitudinal and transverse moduli of 9.7GPa and 4.7GPa
311 respectively using the density-dependant transversely isotropic model, whereas it
312 corresponds to a Young modulus equal to 7.2GPa using the density-dependant
313 isotropic model, and equal to 15GPa in the case of the two-material models. One
314 other limitation of the two-material model is the sensitivity of the results to the
315 threshold value chosen to separate trabecular and cortical tissues, which may be user-
316 dependent. This limit obviously disappears when the density-dependent model is used.

317 As far as the ease of implementation is concerned, computation times were equivalent
318 for the three models. However, density-dependant models require to develop and
319 algorithm in order to link HU values to elastic properties, and also require a calibration
320 of the CT-scan. Moreover, using a transversely isotropic model requires the definition

321 of orthotropic axis, which has been approximated in our case for bending tests. More
322 complex algorithms would be required to assign local orthotropic axis for more
323 complex loadings. Except for these pre-processing steps, the calculation of the three
324 types of models is then straightforward.

325 *Limitations and challenges*

326 One of the limitation of bending tests lies in the fact that results depend on the friction
327 coefficient between sample and the bending tools, as illustrated by our sensitivity
328 analysis and by other authors⁴². Bending stand–resin interaction was modelled with
329 friction coefficient of 0.7 due to the lack of existing values. Even if this friction
330 coefficient is realistic for such a soft resin, experiments could be performed in order to
331 confirm these results. However, such measurements are complex to perform, as long
332 as apparent friction coefficients may be affected by local deformation of the resin due
333 to the cylindrical shape of the bending stand and the high loads involved. These local
334 effects are not taken into account in the simulations, as long as resin blocks have been
335 modelled by a single element. This particular point may be subject to further analyses,
336 for instance using an inverse approach from similar bending tests on well-known
337 materials.

338 A simple elastoplastic law with isotropic linear hardening was used as proposed in the
339 literature³³, and associated with a Von Mises yield criterion. Even though the use of
340 such a criterion has been questioned⁴³, no consensus has been clearly found and this
341 criterion is still widely used^{34,38,40}. The simulated post-yield response did not
342 reproduce the plateau observed experimentally for some samples: it may be therefore
343 concluded that the linear hardening set as 5% of the initial mean modulus as proposed
344 in the literature was excessive and should be age and breed dependent, or that a
345 perfectly plastic behaviour might be more representative. Including progressive
346 damage in the model may lead to better results as the physical phenomenon leading
347 to bone non-linear behaviour is most probably related to damage rather than
348 plasticity^{21,34,38,44}.

349 No distinction was made between cortical and trabecular tissues in the bone material
350 properties characterising the non-linear behaviour, although the microstructures of
351 these tissues are clearly different. It is likely that here the trabecular tissue do not
352 participate substantially to the bone bending response. The material axes were
353 defined from the mid-line of the diaphysis, as commonly reported in the literature^{45,46},
354 leading to a global definition of the longitudinal direction. As the segment of interest
355 involved in the bending test was restricted to the bone diaphysis in which the main
356 orthotropic direction does not substantially vary, it is unlikely that this simplification

357 has an effect on the reported results. These two limitations suggest that the validity of
358 the procedure proposed here is thus probably restricted to the bending mode of
359 deformation.

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363 **Conflicts of interest**

364 There is no conflict of interest in this study.

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489

490 **Figure captions**

491 Figure 1. Experimental and simulated bending test on canine humerus. (a) Preparation
492 of bone samples using a custom jig to align resin moulds (b) bone samples embedded
493 in resin moulds were mounted in a custom bending stand (c) the bending tests were
494 simulated by simplifying the resin moulds with single hexahedrons linked to the bone
495 surface (red dots) via artificial springs. A sticking contact condition was considered
496 between the bending tool and the bone surface (green dots), while contact-friction
497 interaction was considered between the resin moulds and the bending stand (blue
498 cylinders).

499 **Figure 2. Determined relation between canine bone properties as a function of mass**
500 **based on existing data¹⁹ and human bone properties.**

501 Figure 3. Calculation of orthotropic axes (longitudinal and transverse for a transversely
502 isotropic model) from the central third of the bone. Longitudinal direction is defined as
503 the computed least-square line of the mesh nodes included in the bone diaphysis
504 surface.

505 Figure 4: Left: bending responses of the **fourteen** humeri. Right: bending stiffness of
506 the **seven** pairs of humeri, emphasizing the large inter- and intra-variability of
507 measured responses.

508 Figure 5. Bone meshes resulting from the reconstruction of segmented CT images
509 together with the mapping procedure. The colour code corresponds to the computed
510 densities (g/mm^3) assigned to each mesh element from HU values.

511 Figure 6. Left: experimental vs. simulated stiffness and yield load for the fourteen bone
512 samples and for the density-dependent transversely isotropic model. The dash line
513 represents a perfect prediction (simulation=experiments), whereas the continuous line
514 represents the linear fitting of the data. Right: Prediction error on stiffness and yield
515 load for the seven pairs of humeri.

516 Figure 7: Bland-Altman representation of the results obtained for the density-
517 dependant transversely isotropic model in terms of bending stiffness (left) and yield
518 load (right). Points are represented with the corresponding sample name (r=right,
519 l=left).

520 Figure 8. Left: experimental vs. simulated stiffness and yield load for the fourteen bone
521 samples and for both a density-dependent transversely isotropic model and a density-
522 dependent isotropic model. Right: Prediction error on stiffness and yield load for these
523 two models.

524 Figure 9. Left: experimental vs. simulated stiffness and yield load for the fourteen bone
525 samples and for a two-material isotropic model. In this model, trabecular and cortical

526 tissues are considered homogeneous and are separated from density thresholds of
527 400HU or 600HU issued the CT-scan. Right: Prediction error on stiffness and yield load
528 for these two models.

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530 **Table captions**

531 Table 1. Sensitivity analysis of the computational results : effect of resin properties,
532 spring stiffness and friction coefficient between bending stand and resin on predicted
533 bone stiffness and yield load. The star indicates a significant difference between a set
534 of parameters and the selected parameters in the presented simulations.

535 Table 2. Confrontation of the computational and experimental results in terms of
536 predicted yield load and bending stiffness. The p-value of ANOVA tests are given for
537 density-dependent transversely isotropic models (trans. iso), density-dependant
538 isotropic models (iso.) and two-materials isotropic models with segmentation
539 threshold of 400HU (400HU) and 600HU (600 HU). Low p-values indicate a significant
540 difference between experimental and simulation results.

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Resin modulus (MPa)	Predicted Stiffness (N/mm)	Predicted yield load (N)	Spring stiffness (N/mm)	Predicted Stiffness (N/mm)	Predicted yield load (N)	Friction coefficient	Predicted Stiffness (N/mm)	Predicted yield load (N)
100	548.3	1500.2	1	532.3	1497.9	0.5	507.3	1425.9
500	548.3	1500.2	10	544.2	1500.1	0.6	527.2	1462.2
900	548.3	1500.2	100	548.8	1500.2	0.7	548.8	1500.2
1300	548.3	1500.2	1000	558.0	1489.4	0.8	572.2	1539.7
1700	548.3	1500.2	10000	544.0	1508.8	0.9	595.1	1590.8

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543 friction coefficient on predicted bone stiffness and yield load.

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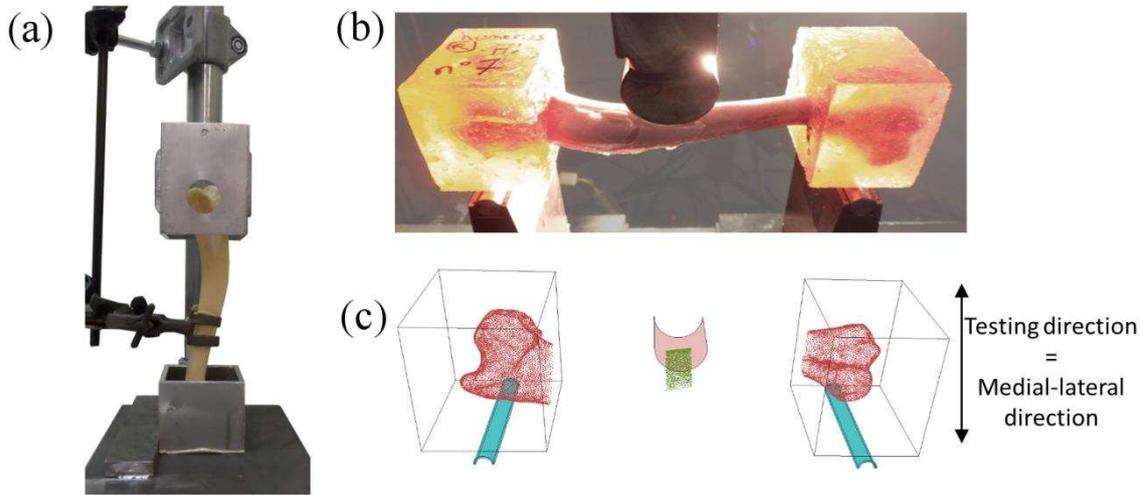
	Stiffness (N/mm)				Yield load (N)			
	Trans. Iso.	Iso.	400HU	600HU	Trans. Iso.	Iso.	400HU	600HU
<i>p-value</i> of the ANOVA test	0,67	2.48 10 ⁻⁴	0,43	0,17	0,74	4.13 10 ⁻⁵	0,18	0,08

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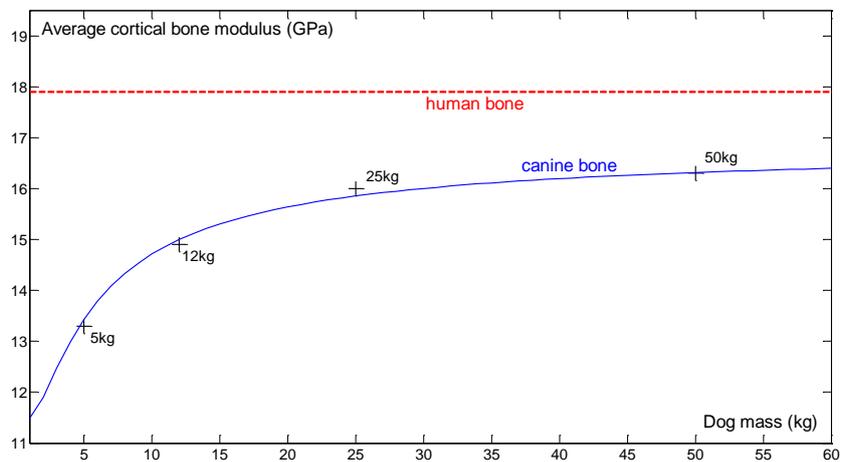
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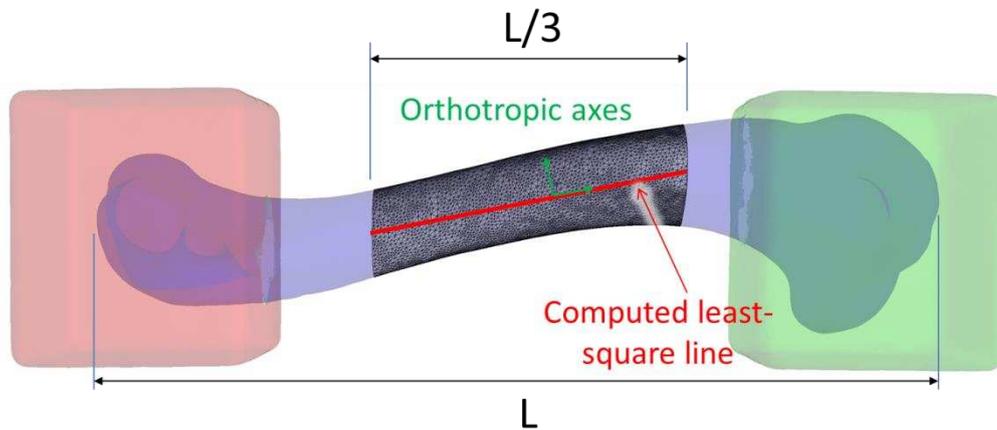
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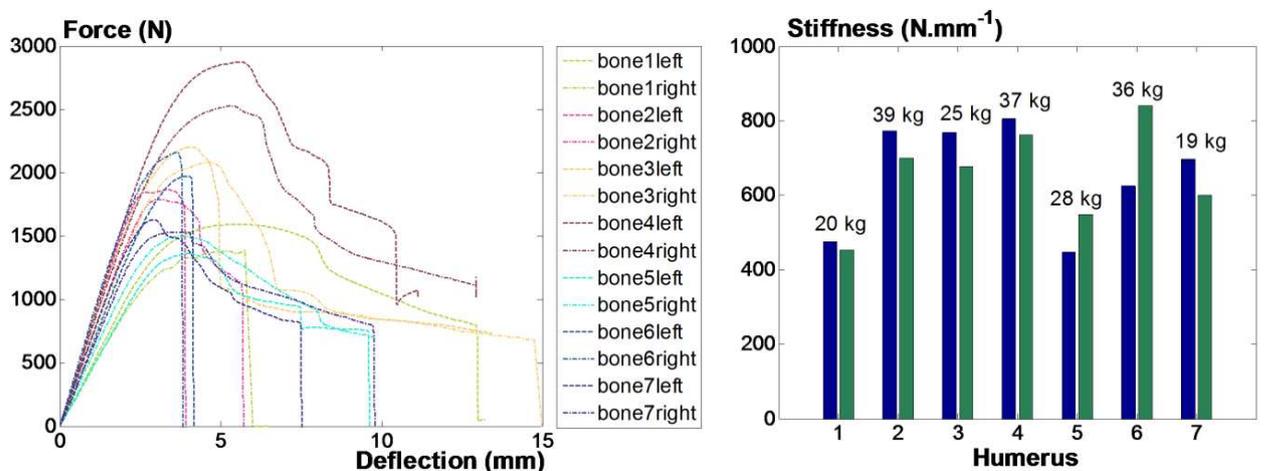
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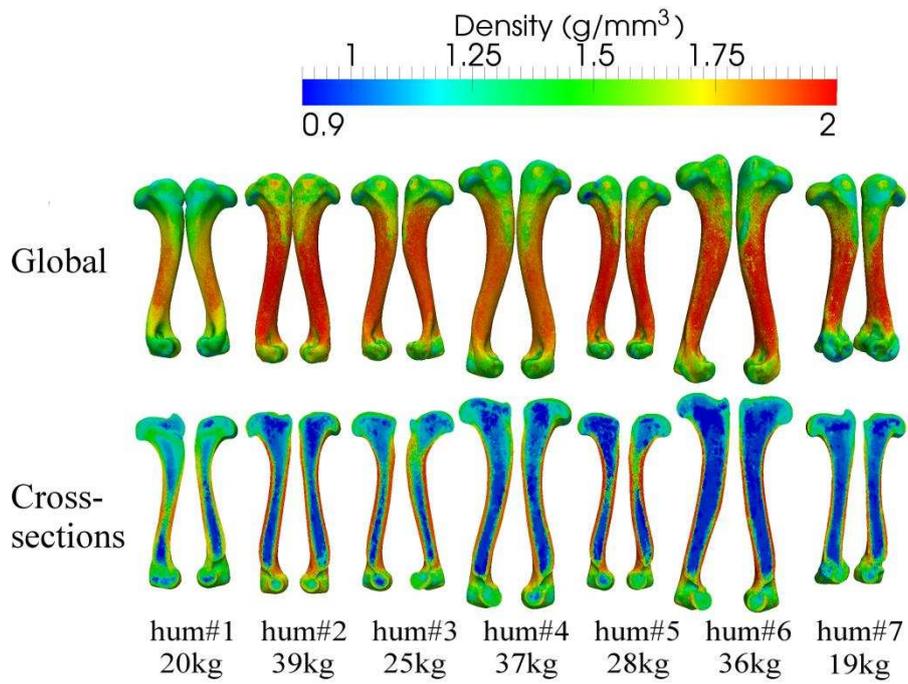
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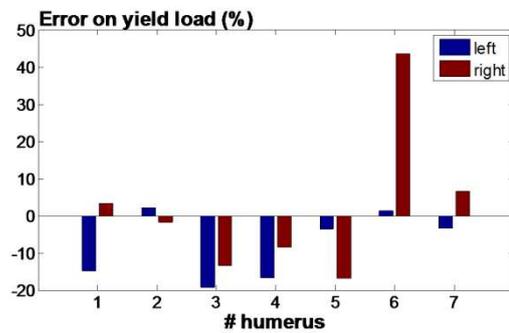
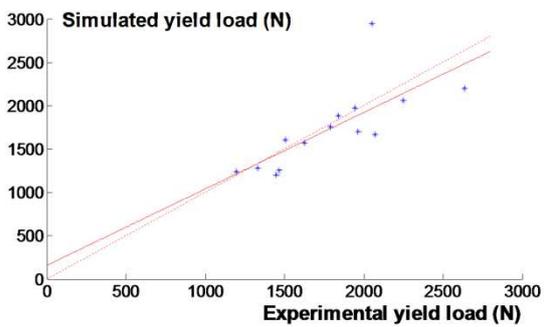
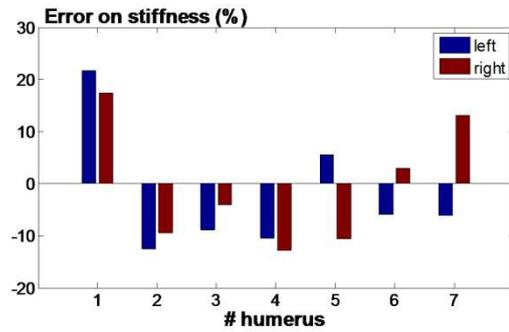
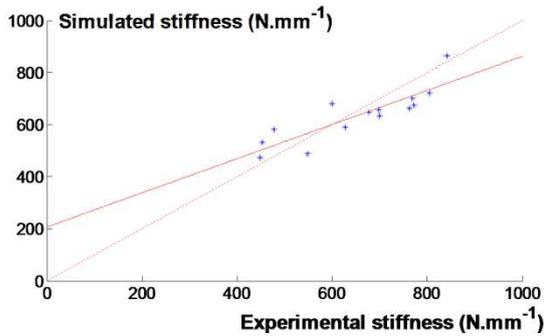
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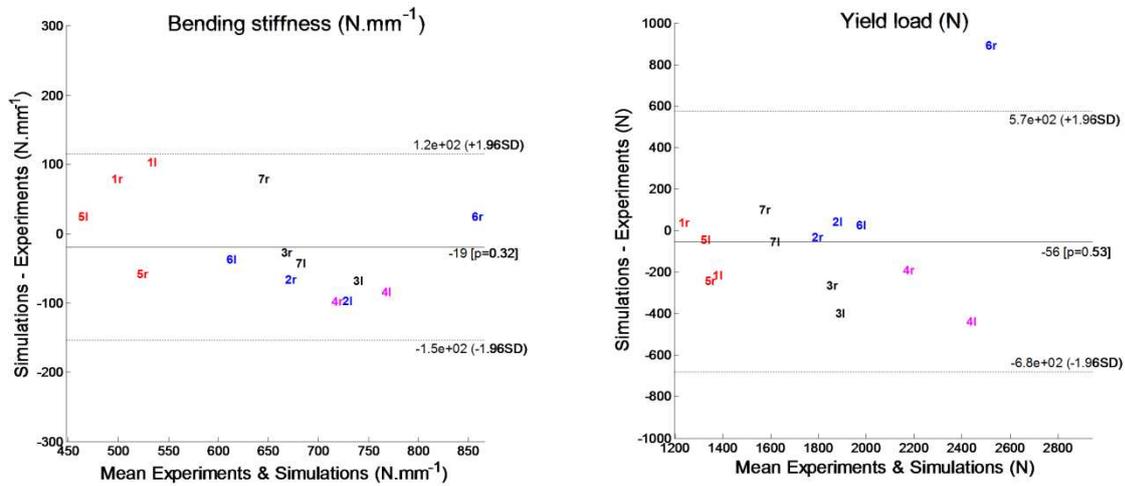
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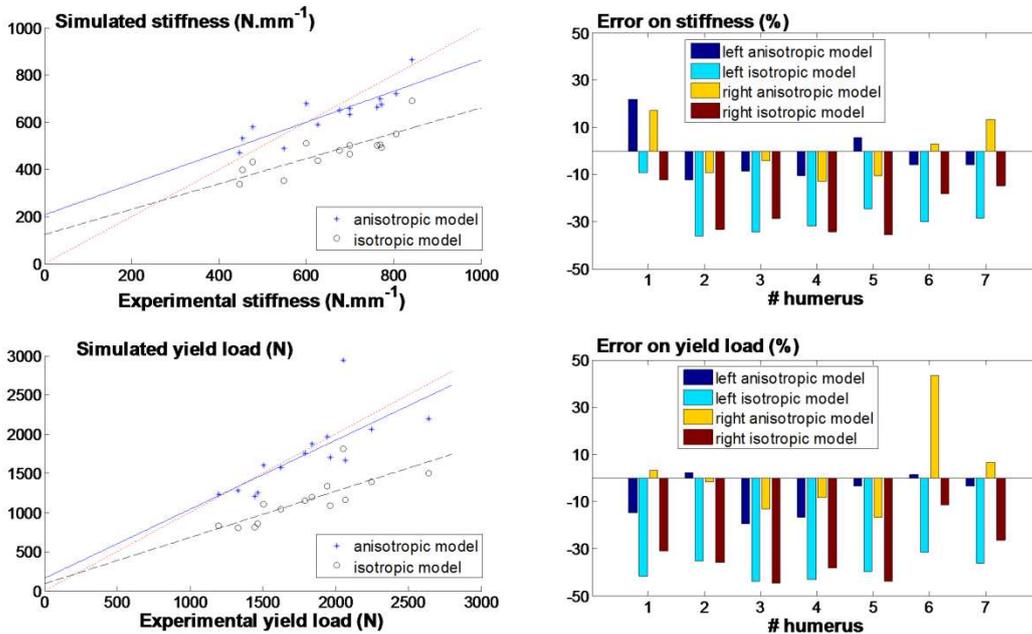
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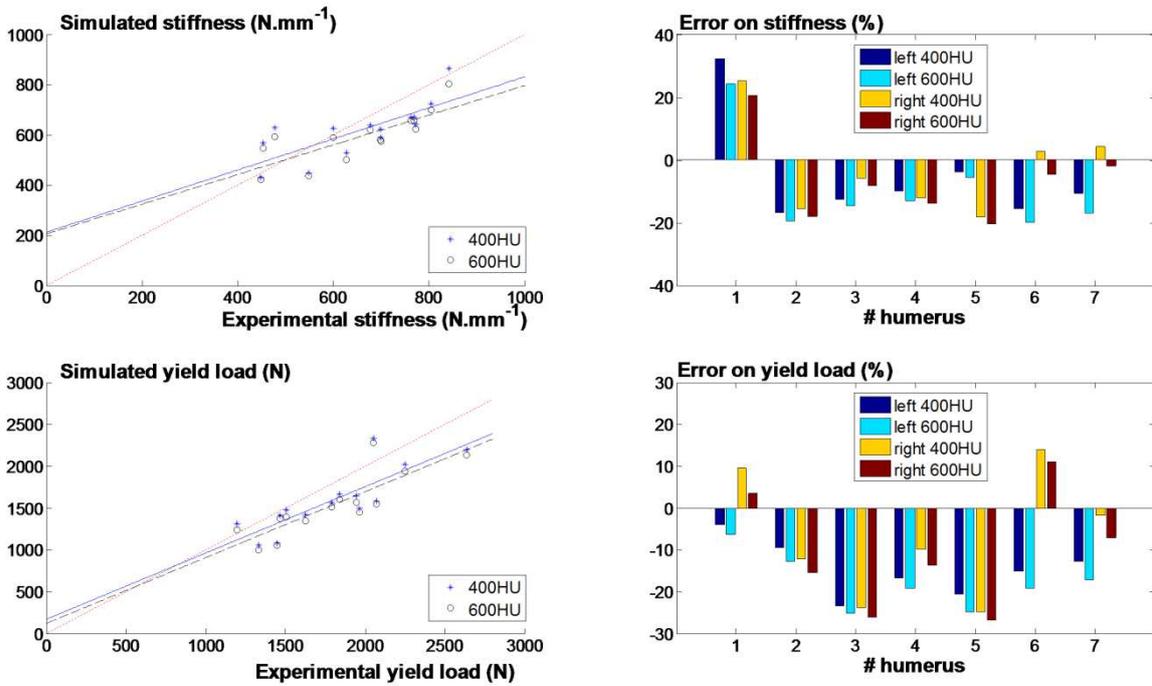
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