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# Green Spending Reforms, Growth and Welfare with Endogenous Subjective Discounting

August 9, 2013

## Abstract

This paper studies optimal fiscal policy, in the form of taxation and the allocation of tax revenues between infrastructure and environmental investment, in a general-equilibrium growth model with endogenous subjective discounting. A green spending reform, defined as a reallocation of government expenditures towards the environment, can procure a double dividend by raising growth and improving environmental conditions, although the environment does not impact the production technology. Also, endogenous Ramsey fiscal policy eliminates the possibility of an ‘environmental and economic poverty trap’. Contrary to the case of exogenous discounting, green spending reforms are the optimal response of the Ramsey government to a rise in the agents’ environmental concerns.

**JEL classification:** D90, E21, E62, H31, O44, Q28.

**Keywords:** endogenous time preference, growth, environmental quality, second-best fiscal policy.

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# 1 Introduction

The economic growth - environmental quality nexus has received considerable attention both in academic research and policy debates.<sup>1</sup> Economic activity contributes to environmental degradation by generating pollution and thus understanding why richer economies may be more environmentally deteriorated is straightforward. Yet, there is evidence that many advanced economies perform better in terms of environmental quality than poorer countries.<sup>2</sup>

From a positive aspect, in an attempt to explain this stylized fact a strand of the literature has derived, through various mechanisms, multiple equilibria in which environmental quality and income or growth are positively related (e.g. Ikefuji and Horii, 2007; Prieur, 2009; Mariani et al., 2010; Varvarigos, 2010a). Multiple equilibria in these studies may imply the existence of an ‘environmental and economic poverty trap’ characterized by economic stagnation and bad environmental conditions. In this context, the implications of endogenous government intervention when there are multiple paths over which income and environmental quality evolve, become important.

From a normative aspect, under unique equilibrium regimes, a large body of the literature has analyzed the impact of environmental policy reforms on growth and welfare by concentrating on the tax instruments (see e.g. Goulder, 1995; Bovenberg and Smulders, 1996; Bovenberg and Mooij, 1997). The main conclusion is that a rise in pollution taxes may provide a double dividend consisting in a simultaneous increase in the growth rate and environmental quality, provided the latter has a positive impact on the production technology. However, given the presence of binding fiscal constraints in the economy, alternative policy reforms on the expenditures side can be considered, which may yield positive effects on growth and environmental quality in a fiscally neutral way.

The present paper (i) studies the role of optimal fiscal policy in eliminating an ‘environmental

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<sup>1</sup>For a survey, see e.g. Xepapadeas (2005).

<sup>2</sup>For instance, using the Environmental Performance Index (YCELP, 2010) as a proxy for environmental quality, higher values in the range of 0-100 can be observed for a number of relatively rich nations, like Switzerland (89.1), Norway (81.1), France (78.2), compared to countries with lower per capita GDP, such as Russia (61.2), Egypt (62.0), and Thailand (62.2). The traditional explanation based on the environmental Kuznets curve (e.g. Grossman and Krueger, 1995) has been questioned on the empirical front (Kijima et al., 2010).

and economic poverty trap’ and (ii) focuses on green spending reforms, implying a shift in public spending from ‘productive’ towards environmental outlays, as a means to achieve a double dividend without the assumption of environmental production externalities.<sup>3</sup>

Our main tool is a continuous-time growth model with renewable resources, in which the generating mechanism of multiple equilibria is the assumption of endogenous subjective discounting (time preference). Specifically, we incorporate an environmental externality into individuals’ impatience by assuming that agents who experience a higher environmental quality are less myopic and tend to value the future more. Our approach captures the standard ‘life expectancy effect’ of environmental quality or pollution, through the impact exerted on human health.<sup>4</sup> In a similar spirit, Agénor (2010) has captured the ‘life expectancy effect’ of health services by endogenizing the degree of impatience to this variable. Recently, Yanase (2011) also incorporates an environmental externality by modeling the rate of time preference (RTP) as a negative function of total pollution and finds, in an exogenous policy setup, that multiple steady states may exist and that the dynamic equilibrium may display indeterminacy.<sup>5</sup>

Starting the analysis at the Decentralized Competitive Equilibrium (DCE) level, we show that global indeterminacy, in the form of multiple equilibria, may arise in the market economy. Intuitively, economies with the same fundamentals can end up in a ‘bad’ equilibrium, characterized by high impatience, poor environmental conditions and low growth, or in a ‘good’ equilibrium, with lower impatience, better environmental conditions and higher growth. These equilibrium regimes are associated with different policy prescriptions. Contrary to the case of the ‘bad’ equilibrium, in which a growth-enhancing strategy is to engage in pure ‘productive’

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<sup>3</sup>Public expenditures on environmental care may be thought of as ‘cleanup’ expenditures on pollution abatement or, more generally, as total spending on all environmental programs. Throughout the paper, we use interchangeably the terms ‘public environmental maintenance/investment’ and ‘pollution abatement policies’.

<sup>4</sup>See e.g. Balestra and Dottori (2012), Mariani et al. (2010), Pautrel (2008), Jouvet et al. (2010), and Varvarigos (2010a,b). This strand of the literature is typically developed in an overlapping generations (OLG) setup, which offers the advantage of measurable mortality rates. We note that our positive results would hold in such a framework, but the normative aspects of second-best Ramsey policy would be intractable, with issues of intergenerational equity raised.

<sup>5</sup>Behavioral evidence shows that people who are familiar to natural resources have low rates of discount (see e.g. Viscusi et al., 2008). For theoretical models see Pittel (2002, Chapter 5) and Lines (2005). In Ayong Le Kama and Schubert (2007) the social planner’s discount rate is an increasing function of environmental quality to reflect *social* motive of sustainability and intergenerational altruism.

expenditures, in the ‘good’ equilibrium the more tax revenues the government allocates to environmental care vis-à-vis infrastructure above a critical value, the higher is the long-run growth rate. Only below this critical value the above-mentioned traditional recipe is obtained. We therefore emphasize that in the ‘good’ equilibrium the economy can enjoy a double dividend in terms of higher growth and better environmental conditions though a fiscally neutral shift in the spending mix, such as a green spending reform, although the environment does not impact the production technology. This alters the typical finding in related setups with exogenous RTP that tax revenues should be devoted to ‘productive’ expenditures from a growth perspective and that public environmental investment is only justified by social welfare considerations due to the amenity value of the environment in the utility function (Ligthart and van der Ploeg, 1994; Pérez and Ruiz, 2007; Economides and Philippopoulos, 2008). Intuitively, this occurs because, in addition to the standard growth-promoting role of infrastructure investment, there is now a similar indirect role played by environmental spending by means of promoting patience and inducing higher savings, which in turn support capital accumulation. In the case of a ‘good’ equilibrium, in which the tax base is large enough for this effect to be relatively strong, a trade-off exists between the two types of public expenditures and hence the relationship between long-run growth and the resource allocation to infrastructure vis-à-vis the environment becomes inverse-U shaped.

Next, we take the analysis one step further by examining optimal Ramsey policy aiming at maximizing welfare. By endogenizing government policy we can analyze the feedback effect of economic structure on the fiscal instruments. This becomes more interesting in the present setup, characterized by multiple equilibrium regimes, as it allows us to demonstrate how the government can eliminate the possibility of an ‘environmental and economic poverty trap’ by setting the policy instruments as a function of the long-run state of the economy. Although there has been some investigation of the role of public policy in eliminating a poverty trap and selecting the ‘good’ equilibrium in models with multiple growth paths (but no environmental externalities), the focus has been on how government intervention can affect the set of equilibria that exist under *laisser-faire*, without explicitly specifying the government’s objec-

tive (see Matsuyama, 1991; Boldrin, 1992; Rodrik, 1996), or how an exogenous reallocation of government spending from unproductive to productive expenditure can facilitate the shift from a low- to a high-growth equilibrium (Agénor, 2010). The only study in which the ‘good’ equilibrium is implemented through endogenous choice of taxation is Diokitopoulos and Kalyvitis (2013). The present paper adds to these recent findings by showing how the endogenous choices of tax-spending policies under environmental externalities eliminate the possibility of an ‘environmental and economic poverty trap’.

Further, we show that under endogenous subjective discounting the Ramsey planner has to pursue green spending reforms following an increase in agents’ environmental concern. The opposite response of more growth-enhancing policies has been obtained by Economides and Philippopoulos (2008) for an economy with exogenous RTP and ‘productive’ spending solely as the source of endogenous growth. In such an economy, the reallocation of revenues towards ‘productive’ spending promotes growth and yields larger tax bases and extra revenues for cleanup policy, while in our model it raises the RTP and can lead the economy to a vicious cycle of low growth, high impatience and poor environmental conditions. Instead, by increasing the share of environmental maintenance, the Ramsey government achieves a direct increase in welfare given the presence of environmental quality in the utility function and additionally a reduction in subjective discounting, which impacts the growth dynamics positively.

A central policy implication of the paper is therefore that, even without considering a direct positive environmental externality in production, green spending reforms can yield a double dividend in fast-growing economies. Further, the stronger the agents’ environmental concerns, the more a Ramsey government should engage in green spending reforms. The paper thus suggests a channel for the impact of public environmental spending on long-run growth and welfare that has been left unnoticed in existing studies and adds to recent findings on the potentially favourable effect of environmental taxation on economic activity in the absence of environmental externalities in the production function (see Pautrel, 2012).

The rest of the paper is organized as follows. The model is described in Section 2. We then solve for a DCE for given policy in Section 3. Section 4 considers the long-run growth impact of

a change in resource allocation between ‘productive’ spending and abatement. Section 5 solves the Ramsey problem of the government. Finally, Section 6 concludes.

## 2 The model

This section presents the setup of our model. Note that we focus on public abatement policies here and abstract from private abatement, as well as environmental policies devoted to incentivize the latter (e.g. Pigouvian taxation), for two reasons. First, the proportion of public expenditure in total abatement expenditure is high in most countries (see e.g. Hatzipanayotou et al., 2003; Haibara, 2009) and, accordingly, many studies have assumed publicly provided abatement (see e.g. Ligthart and van der Ploeg, 1994; Pérez and Ruiz, 2007; Gupta and Barman, 2010; Pautrel, 2012). Second, our goal is to examine whether green spending reforms can procure a double dividend in the absence of environmental externalities from the production function rather than focus on tax instruments, which have been widely explored so far.<sup>6</sup>

### 2.1 Households

The economy is made up of a large number of identical, infinitely lived households, normalized to unity, seeking to maximize the present discounted value of the lifetime utility:

$$\int_0^{\infty} u(c_t, N_t) \exp \left[ - \int_0^t \rho(N_v, C_v) dv \right] dt \quad (1a)$$

where  $u(c, N) = (c^\nu N^{1-\nu})^{1-\sigma} / (1 - \sigma)$  is the instantaneous utility function, which depends on individual consumption,  $c$ , and the stock of economy-wide natural resources,  $N$ , interpreted as an index for environmental quality,  $0 < \nu \leq 1$  measures how much agents value  $c$  vis-à-vis  $N$  and  $\sigma > 0$  represents a degree of intertemporal substitution. In turn,  $\rho(N, C)$  denotes the endogenous RTP, which is assumed to depend on environmental quality and aggregate

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<sup>6</sup>An interesting direction for further research would be to allow for the simultaneous presence of private and public abatement in the model.

consumption,  $C$ :

$$\rho(N, C) = \rho\left(1, \frac{C}{N}\right) \equiv \rho\left(\frac{C}{N}\right) \quad (1b)$$

with  $\frac{\partial \rho(\cdot)}{\partial (C/N)} \equiv \rho'(\cdot) \geq 0$  and  $\rho''(\cdot) \geq 0$ .<sup>7</sup> We also assume that there exists a lower bound for the RTP,  $\lim_{(C/N) \rightarrow 0} \rho(C/N) = \check{\rho} > 0$ . The assumption that a higher level of environmental quality lowers individual impatience has been motivated in the Introduction. The assumption that a higher level of the economy-wide average consumption raises impatience follows a large strand of the literature that has linked the RTP to social factors taken as external by agents (see e.g. Shi, 1999; Schmitt-Grohé and Uribe, 2003; Meng, 2006; Choi et al., 2008; Dioikitopoulos and Kalyvitis, 2010, 2013; Enders et al., 2013). Intuitively, as the economy gets richer and consumes more in the aggregate, each individual wanting to ‘keep up with the Joneses’ becomes more impatient to consume.<sup>8</sup>

Households save in the form of capital and receive dividends,  $\pi$ . The budget constraint is given by:

$$\dot{\Xi} + c = r\Xi + \pi \quad (2a)$$

where a dot over a variable denotes a derivative with respect to time,  $r$  is the capital rental rate and  $\Xi$  denotes financial assets. The household acts competitively by taking prices, policy and environmental quality as given. The latter is justified by the open-access and public-good features of the environment. The control variables are the paths of  $c$  and  $\Xi$ , so that the first-order conditions include the constraint (2a) and the Euler equation below:

$$\frac{\dot{c}}{c} = \frac{1}{1 - \nu(1 - \sigma)} \left[ (1 - \nu)(1 - \sigma) \frac{\dot{N}}{N} + r - \rho\left(\frac{C}{N}\right) \right] \quad (2b)$$

Notice that environmental quality affects positively consumption growth through the RTP and

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<sup>7</sup>The homogeneity of degree zero assumption is required for the RTP to be bounded at the steady-state (see e.g. Palivos et al., 1997) and for the utility function to be consistent with balanced growth (Dolmas, 1996). We retain the equality sign in the derivative for comparability with the case of constant RTP. Throughout the rest of the paper, the time subscript  $t$  is omitted for simplicity of notation and the terms ‘average’ and ‘aggregate’ are used interchangeably given the population of unit mass.

<sup>8</sup>Earlier literature has thoroughly investigated the connections between time preference and individual consumption (see e.g. Uzawa, 1968; Epstein, 1987; Obstfeld, 1990; Palivos et al., 1997).



thus plays an implicit ‘productive’ role in the economy.

## 2.2 Firms

The production function of the single good in this economy is given by:

$$Y = AK^a K_g^{1-a} \quad (3)$$

where  $Y$  denotes output,  $A > 0$  is a total factor productivity parameter,  $0 < a < 1$  denotes the share of physical capital,  $K$ , in the production function, and  $K_g$  refers to the public capital stock (e.g. infrastructure). Labour endowment is normalized to unity as we assume population growth away. The law of motion for the public capital stock is given by:

$$\dot{K}_g = G - \delta_{K_g} K_g \quad (4)$$

where  $G$  is government investment in public capital and  $\delta_{K_g}$  denotes the depreciation rate. The firm maximizes profits,  $\pi$ :

$$\pi = (1 - \tau)Y - (r + \delta_K)K \quad (5)$$

where  $0 < \tau < 1$  is a tax rate on output,  $\delta_K$  is the depreciation rate of private capital, and its summation with  $r$  forms the rental cost of capital. The firm acts competitively by taking prices and policy as given. The first-order condition is given by:

$$r + \delta_k = a(1 - \tau)A \left( \frac{K}{K_g} \right)^{a-1} \quad (6)$$

## 2.3 Motion of environmental quality

Following Economides and Philippopoulos (2008), the law of motion for environmental quality is given by:

$$\dot{N} = \theta E + \delta_N N - P \quad (7a)$$

where  $E$  is public environmental investment,  $\delta_N > 0$  and  $0 < \theta \leq 1$  measure respectively the regeneration rate of natural resources and how public spending is translated into actual units of renewable natural resources, and  $P$  is the pollution flow. Natural resources can be renewed by regeneration, at a constant rate (see e.g. Harrington et al., 2005; Valente, 2005; Acemoglu et al., 2012), and through publicly financed abatement (see e.g. Ligthart and van der Ploeg, 1994; Pérez and Ruiz, 2007; Gupta and Barman, 2010; Pautrel, 2012). We assume that  $P$  occurs as a by-product of output:

$$P = sY \tag{7b}$$

where  $0 < s < 1$  quantifies the detrimental effect of economic activity on the environment.<sup>9</sup>

## 2.4 Government budget constraint

The government spends  $G$  on infrastructure and  $E$  on environmental policy, and collects revenues through a tax on the polluting firm's output,  $0 < \tau < 1$ , running a balanced budget:

$$G + E = \tau Y \tag{8a}$$

Equivalently, we can write (8a) as:

$$G = b\tau Y \tag{8b}$$

$$E = (1 - b)\tau Y \tag{8c}$$

where  $0 < b \leq 1$  is the fraction of tax revenue used to finance infrastructure. Thus, the two policy instruments are  $\tau$  and  $b$ .<sup>10</sup>

## 3 Decentralized competitive equilibrium

In this section we solve for a DCE, which holds for any feasible policy and analyze its properties.

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<sup>9</sup>We consider a linear relationship between pollution flows and production for simplicity. Our results do not change if pollution occurs as a by-product of consumption.

<sup>10</sup>Given the setup of the model, a tax levied on output boils down to taxing pollution.

**Definition 1** *The DCE of the economy is defined for the exogenous policy instruments  $\tau$  and  $b$ , the factor price  $r$ , and the aggregate allocations  $K, K_g, N, G, E, C$  such that: i) Individuals solve their intertemporal utility maximization problem by choosing  $c$  and  $\Xi$ , given the policy instruments and the factor price; ii) Firms choose  $K$  in order to maximize their profits, given the factor price and aggregate allocations; iii) All markets clear, which implies for the capital market  $\Xi = K$  (assets held by agents equal the private capital stock); iv) The government budget constraint holds.*

Combining (1)-(8) and assuming that  $\delta_K = \delta_{K_g} = \delta$ , the DCE is given by:

$$\frac{\dot{C}}{C} = \frac{(1-\nu)(1-\sigma)}{1-\nu(1-\sigma)} \frac{\dot{N}}{N} + \frac{1}{1-\nu(1-\sigma)} \left[ a(1-\tau)A \left( \frac{K}{K_g} \right)^{a-1} - \delta - \rho \left( \frac{C}{N} \right) \right] \quad (9a)$$

$$\frac{\dot{K}}{K} = (1-\tau)A \left( \frac{K}{K_g} \right)^{a-1} - \frac{C}{K} - \delta \quad (9b)$$

$$\frac{\dot{K}_g}{K_g} = b\tau A \left( \frac{K}{K_g} \right)^a - \delta \quad (9c)$$

$$\frac{\dot{N}}{N} = [\theta(1-b)\tau - s] A \frac{K^a K_g^{1-a}}{N} + \delta_N \quad (9d)$$

Notice that equations (9a)-(9c) cannot be solved independently of the environmental stock accumulation equation, (9d). In line with Economides and Philippopoulos (2008), we assume that economic activity has a net damaging effect on the dynamics of environmental quality in (9d), i.e.  $\Theta(\tau, b) \equiv \theta(1-b)\tau - s < 0$ . This implies that the environmental damage caused by one unit of production,  $s$ , is higher than the environmental benefit arising from one unit of production (through providing a tax base for financing environmental investment),  $\theta(1-b)\tau$ , and is meant to describe a real world economy. Finally, the transversality condition is given by:

$$\lim_{t \rightarrow \infty} \frac{K_t}{C_t^\sigma} \exp \left[ - \int_0^t \rho \left( \frac{C_v}{N_v} \right) dv \right] = 0 \quad (10)$$

The balanced growth path (BGP) is defined here as a state where all variables grow at a constant rate,  $g$ . As noted by Economides and Philippopoulos (2008), the concept of a growing environmental quality can apply to renewable resources characterized by biological regeneration, including living organisms like fish, forests, cattle and to some extent water and atmospheric systems. Also, environmental policy and innovation can even help fossil fuels and non-energy minerals not to become extinct, for instance, through discovery of new sources, improved efficiency of extraction, more economic use of existing supplies, and invention of new substitutes.<sup>11</sup> To proceed we define the following auxiliary stationary variables,  $\omega \equiv \frac{C}{K}$ ,  $z \equiv \frac{K}{K_g}$ , and  $x \equiv \frac{K_g}{N}$ , so that the dynamics of (9a)-(9d) are equivalent to:

$$\frac{\dot{\omega}}{\omega} = [1 - \nu(1 - \sigma)]^{-1} \{ (1 - \nu)(1 - \sigma)(\Theta(\tau, b)Az^a x + \delta_N) - [1 - \nu(1 - \sigma) - a](1 - \tau)Az^{a-1} - \rho(\omega z x) - \nu(1 - \sigma)\delta \} + \omega \quad (11a)$$

$$\frac{\dot{z}}{z} = (1 - \tau)Az^{a-1} - b\tau Az^a - \omega \quad (11b)$$

$$\frac{\dot{x}}{x} = b\tau Az^a - \Theta(\tau, b)Az^a x - \delta - \delta_N \quad (11c)$$

It follows that at the BGP  $\frac{\dot{\omega}}{\omega} = \frac{\dot{z}}{z} = \frac{\dot{x}}{x} = 0$ . Then (11b)-(11c) imply that the long-run ratios,  $\hat{\omega}$  and  $\hat{x}$ , are expressed as functions of  $\hat{z}$  by:

$$\hat{\omega}(\hat{z}) = (1 - \tau)A\hat{z}^{a-1} - b\tau A\hat{z}^a \quad (12a)$$

$$\hat{x}(\hat{z}) = (b\tau A\hat{z}^a - \delta - \delta_N) [\Theta(\tau, b)A\hat{z}^a]^{-1} \quad (12b)$$

Finally, substituting (12a)-(12b) in (11a) we get that  $\hat{z}$  is determined by:

$$\Phi(\hat{z}) \equiv -\sigma b\tau A\hat{z}^a + a(1 - \tau)A\hat{z}^{a-1} - (1 - \sigma)\delta - \rho(\hat{\omega}(\hat{z}) \cdot \hat{z} \cdot \hat{x}(\hat{z})) = 0 \quad (12c)$$

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<sup>11</sup>The balanced growth rate for environmental quality and consumption here also ensures a constant long-run RTP.

Provided that there exists a solution  $\hat{z} > 0$  in (12c), the balanced growth rate,  $g$ , can then be determined by (9c). Assuming equilibrium existence, equations (12a)-(12c) imply the following:

**Proposition 1** *Under the assumptions of Section 2, the long-run equilibrium can be unique or multiple.*

**Proof.** See the Companion Online Appendix. ■

Proposition 1 states that endogenous impatience, determined by aggregate consumption and environmental quality, can lead to multiple solutions for  $\hat{z}$ , and, in turn, multiple Pareto-ranked DCE allocations. Inspection of (9c), (12a), and (12b) reveals that an equilibrium with high  $\hat{z}$  may be referred to as the ‘good’ equilibrium, since it is associated with a higher balanced growth rate, better environmental quality (relative to public goods and private consumption), and lower impatience compared to an equilibrium with low  $\hat{z}$  (‘bad’ equilibrium).<sup>12</sup> The latter can be characterized as an ‘ecological and economic poverty trap’. Hence, although the instantaneous utility and production technology functions satisfy the standard concavity assumptions, the existence of a unique positive balanced growth rate is not guaranteed here. The multiplicity result occurs because the endogenous discount rate becomes nonlinearly related to the stock of private capital (relative to public capital) in the long run and alters the behavior of the Euler equation. To understand the emergence of multiplicity driven by self-fulfilling saving rates suppose that a long-run ratio of private to public capital,  $\hat{z}$ , exists and we want to investigate whether a second one, say higher, is also feasible. Under exogenous RTP, a second BGP would not be possible as a higher  $\hat{z}$  would imply a higher growth rate for public capital, given by (9c), but a lower one for consumption, given at the BGP by  $\frac{\dot{C}}{C} = \frac{1}{\sigma}[r(z) - \rho]$ , because of the lower return to private capital, i.e.  $r'(z) < 0$ . Under the discounting externalities, there is an *additional* opposite impact of  $z$  in the Euler equation, which becomes  $\frac{\dot{C}}{C} = \frac{1}{\sigma}[r(z) - \rho(z)]$  with  $\rho'(z) < 0$ . Hence for sufficiently large values of  $\hat{z}$ , the term  $\rho(\cdot)$  can dominate so that the difference between the marginal product of capital and the discount rate can be increasing in  $z$ , enabling the existence of a second BGP. Hence, both outcomes are feasible in this economy.

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<sup>12</sup>It can be easily verified that  $\frac{\partial \hat{\omega}(\hat{z})}{\partial \hat{z}} < 0$ ,  $\frac{\partial \hat{x}(\hat{z})}{\partial \hat{z}} < 0$ , and  $\frac{\partial [\hat{\omega}(\hat{z}) \cdot \hat{z} \cdot \hat{x}(\hat{z})]}{\partial \hat{z}} < 0$ .

Intuitively, in the presence of the environmental externality in subjective discounting, future utility will be discounted at a lower rate relative to an economy with exogenous RTP, so that the marginal utility of future consumption will be higher. This will trigger further capital accumulation leading to a high-growth BGP. Given the prospect of higher income, the agent may decide to increase consumption. In the presence of the consumption externality in subjective discounting, if everyone’s consumption is higher, future utility will be discounted at a higher rate and, therefore, the marginal utility of future consumption will be lower. If the second channel dominates the over-accumulation of capital, the economy will result in a low-growth BGP. Hence, for the same fundamentals both outcomes are feasible in this economy.

The nature of the theoretical result of Proposition 1 may be further clarified numerically using the parameterization reported in Table 1. The values of the economic parameters are as in most dynamic general equilibrium calibration and estimation studies. Thus, the values used for the productivity of private capital in the production function,  $\alpha$ , and the capital depreciation rate,  $\delta$ , come from Economides and Philippopoulos (2008) and Dioikitopoulos and Kalyvitis (2010). Following common practice, we use the total factor productivity,  $A$ , as a scale parameter to help us get plausible values for the growth rates. Regarding the degree of intertemporal substitution,  $\sigma$ , much of the literature on real business cycle models cites the econometric estimates of Hansen and Singleton (1983), which place the coefficient of risk aversion ‘somewhere between 0 and 2’, and quite often choose a value greater than unity. In line with Bennett and Farmer (2000) and Meng (2006) we choose the curvature of the utility function to be on the linear side of logarithmic preferences ( $\sigma < 1$ ), but we also confirm below that the multiplicity result of Proposition 1 can hold for  $\sigma > 1$ . Further, note that estimates like the Hansen and Singleton ones are not directly relevant to our utility function, which is non-separable both in consumption and environmental quality. There is of course less empirical evidence and consensus on the value of the environmental and impatience parameters. We set the values for the detrimental effect of economic activity on the environment,  $s$ , and the effectiveness of environmental policy,  $\theta$ , following Economides and Philippopoulos (2008), while for the regeneration rate of natural resources,  $\delta_N$ , we use a value that is sufficiently high

to ensure a non-negative growth rate for the environmental stock. We employ a linear time preference function,  $\rho(\frac{C}{N}) = \gamma \times (\frac{C}{N}) + \check{\rho}$ , for computational tractability (see e.g. Pittel, 2002; Meng, 2006; Dioikitopoulos and Kalyvitis, 2010,2013), which is rich enough to obtain our main results. The chosen values for the low bound,  $\check{\rho}$ , and slope,  $\gamma$ , help us calibrate values for  $\rho$  in line with the literature. In particular, the highest RTP values reported for the low-growth regime are close to that in Elbasha and Roe (1996), while those reported for the high-growth regime are in the range commonly employed in the growth literature.

The following numerical example illustrates the possibility for some countries to be caught in a high-impatience, poor-environment, low-growth trap.

**Example 1** *Consider the parameter values displayed in Table 1 and the following values for the policy instruments:  $\tau = 0.45$  and  $b = 0.70$ . We find that equations (12a)-(12c) and (9c) yield two long-run equilibria in the market economy:  $\{z_1 = 0.120, g_1 = 0.018, \rho_1 = 0.286, x_1 = 2.589, \omega_1 = 0.589\}$  and  $\{z_2 = 1.055, g_2 = 0.104, \rho_2 = 0.050, x_2 = 0.303, \omega_2 = 0.084\}$ , where the former corresponds to a high-impatience, poor-environment, low-growth trap.*

In order to assess the robustness of our findings with respect to the specifications for the RTP and the utility function we provide below a second example with a higher degree of intertemporal substitution and discounting externality.<sup>13</sup> Note that the long-run outcome in the market economy does not depend on the preference weight attached to consumption,  $\nu$ , while we investigate the impact of this parameter when endogenizing policy in Section 5.

**Example 2** *Consider the following parameters  $\sigma = 1.3, \gamma = 2.8, A = 0.8$  and  $b = 0.55$ , while for the rest we maintain those reported in Example 1. We find that equations (12a)-(12c) and (9c) yield two long-run equilibria in the market economy:  $\{z_1 = 0.139, g_1 = 0.048, \rho_1 = 0.499, x_1 = 1.135, \omega_1 = 1.103\}$  and  $\{z_2 = 0.596, g_2 = 0.127, \rho_2 = 0.090, x_2 = 0.119, \omega_2 = 0.416\}$ , where the former corresponds to a high-impatience, poor-environment, low-growth trap.*

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<sup>13</sup>We also adjust slightly the parameters for the TFP and the share of environmental spending to help us get plausible values.

In contrast to other studies of multiple equilibria with negative association between environmental quality and growth/income (e.g. Ikefuji and Horii, 2007; Prieur, 2009; Mariani et al., 2010; Varvarigos, 2010a), multiplicity here emerges in the presence of government policy.<sup>14</sup> More importantly, the comparative statics exercises we perform in the next section demonstrate the existence of thresholds in the spending instrument,  $b$ , that affect the properties of the DCE.

## 4 ‘Productive’ versus environmental spending and long-run growth

Conventional wisdom argues that, in the absence of environmental externalities in the production function, public environmental maintenance will have an adverse effect on growth by diverting resources from the ‘productive’ sectors. A strand of the literature has formalized this notion by showing that public environmental investment has an unfavourable effect on long-run growth and is only justified by social welfare considerations due to the amenity value of environmental quality in the utility function (Ligthart and van der Ploeg, 1994; Pérez and Ruiz, 2007; Economides and Philippopoulos, 2008). In this section we demonstrate how such a shift towards environmental expenditures can promote long-run growth without the assumption of environmental externalities in production.

In order to provide exogenous policy prescriptions for each regime type, we investigate how the balanced growth rate,  $g$ , in (9c) reacts to exogenous changes in the spending share of infrastructure versus abatement,  $b$ :

$$\frac{\partial g}{\partial b} = \tau A \hat{z}^{a-1} (\hat{z} + ab \hat{z}_b) \quad (13)$$

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<sup>14</sup>The analysis of local stability is performed in the Companion Appendix of the paper.



where  $\hat{z}_b \equiv \frac{\partial \hat{z}}{\partial b} = -\frac{\partial \Phi(\hat{z})/\partial b}{\partial \Phi(\hat{z})/\partial \hat{z}}$  is derived from total differentiation of (12c), with:

$$\frac{\partial \Phi(\hat{z})}{\partial \hat{z}} = -a\sigma b\tau A\hat{z}^{a-1} - a(1-\tau)(1-a)A\hat{z}^{a-2} - \underbrace{\rho'(\cdot)b\tau \frac{a\hat{\omega}(\hat{z}) - \Psi(\hat{z}, \tau, b)}{\Theta(\tau, b)}}_{>0} \quad (14a)$$

$$\frac{\partial \Phi(\hat{z})}{\partial b} = -\sigma\tau A\hat{z}^a - \underbrace{\rho'(\cdot)\tau\hat{z} \frac{[\theta\hat{x}(\hat{z}) + 1]\hat{\omega}(\hat{z}) - \Psi(\hat{z}, \tau, b)}{\Theta(\tau, b)}}_{>0} \quad (14b)$$

where  $\Psi(\hat{z}, \tau, b) \equiv b\tau A\hat{z}^a - \delta - \delta_N < 0$ .

When the RTP is exogenous ( $\rho'(\cdot) = 0$ ), the standard result that the growth rate,  $g$ , increases monotonically with the revenue share allocated to infrastructure,  $b$ , can be easily verified. In this case, because public expenditures for the environment contribute neither to production nor to the savings rate, expenditures for infrastructure solely affect growth through the positive externality of the infrastructure stock in the production function. Hence, although there is a negative effect on  $g$  from the induced fall in the physical-to-public-capital ratio ( $\hat{z}_b < 0$ ) when more tax revenues are allocated to infrastructure, this is outweighed by the direct positive effect from the increase in  $b$ , i.e.  $\hat{z} + ab\hat{z}_b > 0$  in (13).

In the case of endogenous discounting ( $\rho'(\cdot) > 0$ ), not only the infrastructure stock but also the stock of environmental quality affects growth through the time preference which, in turn, affects positively the savings rate, and hence the sign of (13) becomes ambiguous. Due to analytical intractability we resort to numerical simulations using the parameter values of Table 1. The response of the DCE allocation is reported in Table 2 for the range of  $b$  in which a well-defined solution exists.<sup>15</sup> As can be seen, there are threshold values of  $b$  that play a crucial role in the emergence of multiplicity, thus verifying that policy choices matter for the nature of the final outcome (uniqueness or multiplicity) in the economy. In particular, for sufficiently low shares of infrastructure investment ( $b = 0.5 - 0.55$ ) the resulting equilibrium is unique, while for high levels ( $0.6 \leq b \leq 0.8$ ) two equilibria arise. In addition, these regimes exhibit different comparative statics properties. The standard monotonic effect of  $b$  on growth holds in the ‘bad’

<sup>15</sup>For  $b < 0.5$  or  $b > 0.8$  at least one of the following:  $\hat{\omega} > 0$ ,  $\hat{x} > 0$ ,  $\hat{\rho} > 0$ ,  $g > 0$  is not satisfied.

equilibrium, but is altered in the ‘good’ regime, because now  $\hat{z}$  is sufficiently high so that the positive direct effect from the increase in  $b$  does not always dominate the negative indirect one (i.e.  $z_b < 0$ ), and a trade-off is in place. Specifically, for  $b < 0.55$  we have  $\frac{\partial g_2}{\partial b} > 0$ , while for  $b \geq 0.55$  we have  $\frac{\partial g_2}{\partial b} < 0$ . Consequently, the relationship between  $g$  and  $b$  appears inverse-U shaped in the ‘good’ equilibrium, as depicted in Figure 1, showing the different responses of the two growth rates.

Our findings thus imply that the two regimes are associated with different policy recipes. When the economy is trapped in a ‘bad’ equilibrium, a growth-enhancing strategy is to engage in pure ‘productive’ expenditures by financing public infrastructure. However, when the economy is in the high-growth regime this conventional policy recipe holds if the government allocates relatively little resources to infrastructure investment vis-à-vis public abatement (low values of  $b$ ). Instead, for relatively high levels of  $b$ , the more revenues the government allocates to environmental investment, the higher is the balanced growth rate. Intuitively, in addition to the standard growth-promoting role of infrastructure investment, there is also an indirect positive growth impact of environmental spending; by enhancing environmental quality, abatement expenditures promote patience and induces higher savings, which support capital accumulation and fuel long-run growth. As a result, a trade-off exists between the two spending components in the case of a ‘good’ equilibrium, in which the tax base is large enough for the effect of environmental expenditures to be relatively strong. Hence, in fast-growing economies, reallocating government spending towards the environment can procure a double dividend by raising growth and improving environmental conditions, even though no environmental externalities are postulated in production.<sup>16</sup> The above can be summarized as follows.

**Result 1** *Under the assumptions of Section 2, in the DCE there is a critical value of  $b$ , denoted as  $b^\dagger$ , for which  $b < b^\dagger$  implies a unique BGP and  $b > b^\dagger$  implies two BGPs.*

**Result 2** *Under the assumptions of Section 2, along the BGP of the ‘good’ regime in the DCE, there can be a critical value of  $b$ , denoted as  $b^*$ , for which  $b > b^*$  implies  $\frac{\partial g}{\partial b} < 0$  and*

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<sup>16</sup>In the Companion Appendix, we present the different responses of the two market economy equilibria displayed in Example 2.

$b < b^*$  implies  $\frac{\partial g}{\partial b} > 0$ . Along the BGP of the ‘bad’ regime,  $\frac{\partial g}{\partial b} > 0$  always holds.

## 5 Ramsey fiscal policy and green preferences

Previous studies of fiscal policies have assumed that the government is endowed with nondistortionary instruments (e.g. lump-sum taxes or transfers). In turn, the public finance literature has assumed that the government has a comprehensive mechanism (e.g. Pigouvian taxation) for fully internalizing any market failures from externalities. As shown in the Companion Appendix, the policy instruments considered here do not allow the government to decentralize the Pareto optimal allocation. This result depends crucially on the set of instruments considered, which is not sufficient to correct all the market failures and reproduce the first-best outcome. When, for some reason, the first-best allocation is unattainable, the government has to design a second-best optimal policy. In this section, we endogenize policy by solving the Ramsey problem of a benevolent government, which acts as a Stackelberg leader vis-à-vis private agents, when maximizing her objective function. In doing so, the government tries to correct the market imperfections (arising from externalities), raise tax revenue to finance public expenditures, and minimize the distorting effects of policy intervention on the economy.

**Definition 2** *A Ramsey Allocation is given under Definition 1 when (i) the government chooses the tax rate,  $\tau$ , and the levels of infrastructure and environmental investments,  $G$  and  $E$ , in order to maximize the welfare of the economy by taking into account the aggregate optimality conditions of the competitive equilibrium; (ii) the government budget constraints and the feasibility and technological conditions are met.*

Due to the variable RTP, Pontryagin’s maximum principle cannot be applied directly. We thus follow Obstfeld (1990) and introduce an additional ‘artificial’ variable that accounts for the development of the accumulated discount rate,  $\Delta(t) \equiv \int_0^t \rho(N_v, C_v) dv$ . Then, the objective of the government is given by:

$$\max U^R = \int_0^\infty \frac{(C^\nu N^{1-\nu})^{1-\sigma}}{1-\sigma} \exp[-\Delta(t)] dt$$

constrained by the DCE ((8a), (9b), (9c), (9d)) and the derivative of  $\Delta(t)$  with respect to time,  $\dot{\Delta} = \rho(\cdot)$ . The first-order conditions include the Euler equation, the growth rates of private capital, public capital and environmental quality, the resource and the government budget constraints and the optimality conditions with respect to  $C, K_g, N, \tau, G, E, \Delta$ :

$$\nu C^{\nu(1-\sigma)-1} N^{(1-\nu)(1-\sigma)} e^{-\Delta} - \tilde{\lambda}_1 + \frac{1}{N} \tilde{\lambda}_5 \rho' \left( \frac{C}{N} \right) = 0 \quad (15a)$$

$$\tilde{\lambda}_1(1-a)(1-\tau)AK^aK_g^{-a} - \tilde{\lambda}_2\delta - \tilde{\lambda}_3(1-a)sAK^aK_g^{-a} + \tilde{\lambda}_4(1-a)\tau AK^aK_g^{-a} = -\dot{\tilde{\lambda}}_2 \quad (15b)$$

$$(1-\nu)C^{\nu(1-\sigma)}N^{(1-\nu)(1-\sigma)-1}e^{-\Delta} + \tilde{\lambda}_3\delta_N - \tilde{\lambda}_5\frac{C}{N^2}\rho' \left( \frac{C}{N} \right) = -\dot{\tilde{\lambda}}_3 \quad (15c)$$

$$\tilde{\lambda}_1 = \tilde{\lambda}_4 \quad (15d)$$

$$\tilde{\lambda}_2 = \tilde{\lambda}_4 \quad (15e)$$

$$\tilde{\lambda}_3 = \frac{1}{\theta} \tilde{\lambda}_4 \quad (15f)$$

$$\frac{(C^\nu N^{1-\nu})^{1-\sigma}}{1-\sigma} e^{-\Delta} = \dot{\tilde{\lambda}}_5 \quad (15g)$$

where  $\tilde{\lambda}_1, \tilde{\lambda}_2, \tilde{\lambda}_3, \tilde{\lambda}_4, \tilde{\lambda}_5$  are the dynamic multipliers associated with (8a), (9b), (9c), (9d), and the condition  $\dot{\Delta} = \rho(\cdot)$ , respectively. Equations (9a)-(9d), (15a)-(15g), and the optimality condition for the Hamiltonian  $\lim_{t \rightarrow \infty} H^R = 0$  as given by:

$$\frac{C^{\nu(1-\sigma)}N^{(1-\nu)(1-\sigma)}}{1-\sigma}e^{-\Delta} + \tilde{\lambda}_1\dot{K} + \tilde{\lambda}_2\dot{K}_g + \tilde{\lambda}_3\dot{N} + \tilde{\lambda}_5\rho(\cdot) = 0 \quad (15h)$$

characterize the solution of the Ramsey problem. To derive the stationary Ramsey allocation we define as before  $\omega \equiv \frac{C}{K}$ ,  $z \equiv \frac{K}{K_g}$ ,  $x \equiv \frac{K_g}{N}$ ,  $\chi \equiv \lambda_4 K_g$ , and  $\lambda_j \equiv \tilde{\lambda}_j e^{\Delta(t)}$  for  $j = 1, 2, 3, 4, 5$ . Then, as shown in detail in the Companion Appendix, we can obtain:

$$\frac{\dot{\chi}}{\chi} = Az^a \left[ b\tau - \left( 1 - \frac{s}{\theta} \right) (1-a) \right] + \rho(\cdot) \quad (16a)$$

$$\frac{1}{\theta x} [\delta_N - \delta + (1 - s)(1 - a)Az^a + \theta x \omega z] [\nu(1 - \sigma)\rho(\cdot) - x \omega z \rho'(\cdot)] - (1 - \sigma)\rho(\cdot) \omega z = 0 \quad (16b)$$

where  $\rho(\cdot)$  here denotes  $\rho(\omega z x)$ . In the long run we have that all stationary variables should grow at a zero rate. After some algebra, the long-run Ramsey allocation is given by (12a)-(12c) and the following equations:

$$b\tau = \left(1 - \frac{s}{\theta}\right) (1 - a) - \frac{1}{A\hat{z}^a} \rho(\cdot) \quad (17)$$

$$\frac{1}{\theta \hat{x}} [\delta_N - \delta + (1 - s)(1 - a)A\hat{z}^a + \theta \hat{x} \hat{\omega} \hat{z}] [\nu(1 - \sigma)\rho(\cdot) - \hat{x} \hat{\omega} \hat{z} \rho'(\cdot)] - (1 - \sigma)\hat{\omega} \hat{z} \rho(\cdot) = 0 \quad (18)$$

where the five unknowns are  $\omega$ ,  $z$ ,  $x$ ,  $\tau$ ,  $b$ .

As this system is analytically intractable, we present numerical solutions in Table 3 by using the parameter values in Table 1 and experimenting with different values of  $1 - \nu$ , which measures how much agents value environmental quality vis-à-vis consumption, following the exercise in Economides and Philippopoulos (2008). First, it should be pointed out that the Ramsey allocation is unique and implements the ‘good’ equilibrium.<sup>17</sup> This outcome is feasible because the Ramsey planner has two policy instruments,  $\tau$  and  $b$ , to impact the dynamics of the economy, thus eliminating the possibility of a trap, and to attain welfare maximization. This is reflected in the additional equations in comparison to the DCE, (17) and (18), which give the values of the policy instruments as implicit functions of the long-run value of  $z$ , i.e.  $0 < \tau^*(\hat{z}) < 1$  and  $0 < b^*(\hat{z}) \leq 1$ . The Ramsey government therefore chooses a policy schedule that depends on the long-run equilibrium level of the private-to-public-capital ratio and manages to resolve indeterminacy in the region of multiple DCE by affecting the market allocation rule in (12c).<sup>18</sup>

The results reveal that when agents care more about the environment ( $1 - \nu$  increases), it is optimal to allocate more tax revenues to abatement vis-à-vis infrastructure ( $b$  falls) and to tax more ( $\tau$  rises), in contrast with the findings in Economides and Philippopoulos (2008). Intu-

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<sup>17</sup>For example, we find that for the Ramsey optimal values of the policy instruments,  $\tau = 0.386$  and  $b = 0.578$ , equations (12a)-(12c) yield two long-run equilibria in the market economy:  $\{z_1 = 0.080, g_1 = 0.0004, \rho_1 = 0.406, x_1 = 3.902, \omega_1 = 0.939\}$  and  $\{z_2 = 8.079, g_2 = 0.117, \rho_2 = 0.016, x_2 = 0.046, \omega_2 = 0.011\}$ .

<sup>18</sup>Boldrin (1992) discusses how fiscal policy may be used to eliminate the multiplicity of equilibria through a nonlinear tax scheme dependent on the capital stock.

itively, a rise in environmental concern implies a stronger welfare effect of environmental quality and thus agents can directly benefit if the government increases environmental investment by raising taxation and shifting the allocation of revenues towards abatement (*‘Static Amenity Channel’*). When only pure ‘productive’ expenditures impact the growth process, the opposite policy mix (lower taxes and shift in the allocation of revenues towards ‘productive’ spending) forms an optimal government response to greener preferences through dynamically creating a higher tax base that finances both types of expenditures (*‘Dynamic Supply-Side Channel’*). In this case, the ‘static’ effect on utility is negative because of a lower environmental quality resulting from the spending reallocation towards infrastructure, but this outweighed by the induced higher growth, resulting in higher intertemporal utility. In our model, the initial decline in environmental quality from such a spending shift impacts also the RTP, making agents more impatient, and can lead the economy to a vicious cycle of low growth and poor environmental quality, as shown in Section 4. Hence, when environmental quality exerts a positive externality on impatience, greener preferences lead the Ramsey planner to engage in green spending reforms by directing resources towards the environment. This raises directly welfare via the ‘static’ channel and additionally impacts the growth dynamics positively, given the implicit productive role of the environment through the RTP (*‘Dynamic Patience Channel’*).<sup>19</sup> The main findings of this section are summarized as follows.

**Result 3** *The long-run Ramsey allocation is unique. In this allocation, green spending reforms form the optimal government response to a rise in agents’ environmental concerns.*

Finally, it is worth noting that an alternative objective for the government when choosing fiscal policy may be to maximize the long-run growth rate of the economy. In this case, the optimal share of infrastructure spending in the region of multiple DCE is less than one, i.e.  $b^* < 1$ , which implies that public abatement is required for growth-maximization, even though environmental externalities are absent from production.<sup>20</sup> This result directly follows from the comparative statics of Section 4 with regard to the ‘good’ equilibrium. Also, the growth-

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<sup>19</sup>The response of the growth rate depends on which of the two dynamic channels dominates. For low levels of environmental concern in Table 3, the growth rate increases, while it falls for higher levels.

<sup>20</sup>Results are available from the authors upon request.

maximizing tax rate differs from the Barro (1990) tax rule,  $\tau^* = (1 - a)$ , by depending also on demand-driven parameters, like the degree of intertemporal substitution,  $\sigma$ . Intuitively, the endogeneity of the RTP changes the marginal cost of public funds: an increase in  $\tau$  not only affects growth by increasing public capital expenditures and decreasing private capital, but also impacts on the steady-state RTP, which through the Euler equation affects balanced growth.

## 6 Concluding remarks

This paper studied optimal fiscal policy in a general equilibrium model of growth and natural resources, in which the endogeneity of time preference to environmental quality and aggregate consumption gives rise to multiple equilibria in the market economy. Analyzing the different policy prescriptions for each regime type, we showed that green spending reforms can yield a double dividend in fast-growing economies in the absence of an environmental externality in production. Further, the stronger the agents' environmental concerns, the more a Ramsey government should engage in green spending reforms.

Given that countries with similar structural characteristics often seem to display divergent economic behavior and environmental performance, our results suggest an additional generating mechanism of multiple equilibria corresponding to this observed divergence. This stems from the linkage between subjective discounting and environmental quality, with the latter now operating through the demand, rather than the supply, side of the economy. Moreover, to the extent that environmental quality affects patience, our findings suggest a channel for the impact of public abatement on long-run growth that has been left unnoticed in existing studies.

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**Table 1.** Values for parameters and exogenous policy instruments

Parameters	Description	Value
$\alpha$	share of private capital in the production function	0.5
$A$	total factor productivity	0.4
$\sigma$	degree of intertemporal substitution	0.3
$\delta$	capital depreciation rate	0.025
$\delta_N$	regeneration rate of natural resources	0.15
$\theta$	transformation of environmental spending in natural stock	1.0
$s$	polluting effect of economic activity	0.5
$\gamma$	slope in the impatience function	1.5
$\check{\rho}$	low bound for the impatience function	0.01

**Table 2.** Green spending reforms in the DCE

$b$	$\hat{z}_1$	$\hat{z}_2$	$\hat{\omega}_1$	$\hat{\omega}_2$	$\hat{x}_1$	$\hat{x}_2$	$\hat{\rho}_1$	$\hat{\rho}_2$	$g_1$	$g_2$
<i>0.5</i>	-	2.412	-	0.002	-	0.206	-	0.011	-	0.114
<i>0.55</i>	-	2.067	-	0.010	-	0.190	-	0.016	-	0.117
<i>0.6</i>	0.077	1.698	0.762	0.028	4.080	0.205	0.369	0.024	0.004	0.115
<i>0.65</i>	0.095	1.354	0.675	0.052	3.276	0.243	0.327	0.036	0.011	0.111
<i>0.7</i>	0.120	1.055	0.589	0.084	2.589	0.303	0.286	0.050	0.018	0.104
<i>0.75</i>	0.157	0.791	0.500	0.127	1.972	0.398	0.243	0.070	0.028	0.095
<i>0.8</i>	0.230	0.531	0.389	0.196	1.344	0.585	0.190	0.101	0.044	0.079

Note:  $\tau = 0.45$ . See Table 1 for the rest of the parameter values.

**Table 3.** Ramsey allocation and green preferences

$1 - \nu$	$\tau$	$b$	$z$	$\omega$	$x$	$\rho$	$g$
<i>0.1</i>	0.296	0.715	2.745	0.029	0.126	0.025	0.1152
<i>0.2</i>	0.332	0.650	2.664	0.022	0.134	0.021	0.1164
<i>0.3</i>	0.362	0.608	2.595	0.016	0.142	0.019	0.1170
<i>0.4</i>	0.386	0.578	2.533	0.011	0.152	0.016	0.1172
<i>0.5</i>	0.407	0.554	2.475	0.008	0.164	0.015	0.1171
<i>0.6</i>	0.426	0.534	2.417	0.005	0.177	0.013	0.1167
<i>0.7</i>	0.444	0.516	2.359	0.003	0.193	0.012	0.1160
<i>0.8</i>	0.460	0.501	2.299	0.002	0.213	0.011	0.1150
<i>0.9</i>	0.477	0.486	2.238	0.001	0.236	0.010	0.1138

Note: See Table 1 for the parameter values used.

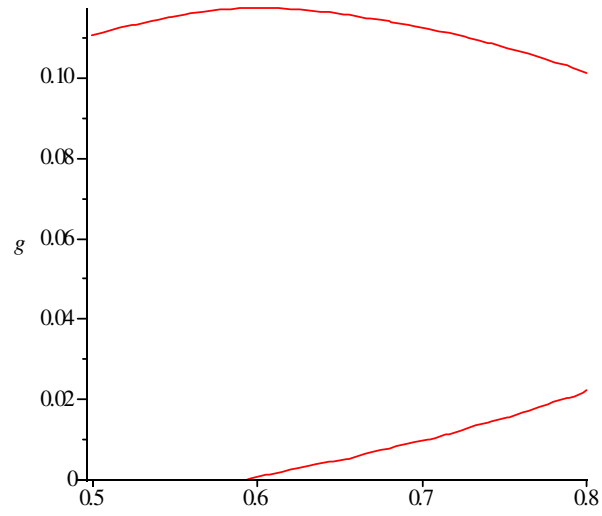


Figure 1. Long-run growth and share of infrastructure vs. environmental investment,  $b$ .

Notes: See also Table 2.