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Stochastic modelling of muscle recruitment during activity

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ABSTRACT

1 Muscle forces can be selected from a space of muscle recruitment strategies that produce
2 stable motion and variable muscle and joint forces. However, current optimization methods
3 provide only a single muscle recruitment strategy. We modelled the spectrum of muscle
4 recruitment strategies while walking. The equilibrium equations at the joints, muscle
5 constraints, static optimization solutions, and 15-channel electromyography recordings for
6 seven walking cycles were taken from earlier studies. The spectrum of muscle forces was
7 calculated using Bayesian statistics and MCMC while EMG-driven muscle forces were
8 calculated using EMG-driven modelling. We calculated the differences between the spectrum
9 and EMG-driven muscle force for 1 to 15 input EMGs and we identified the muscle strategy
10 that best matched the recorded electromyography pattern. The best-fit strategy, static
11 optimization solution, and EMG-driven force data were compared using correlation analysis.
12 Possible and plausible muscle forces were defined as within physiological boundaries and
13 within EMG boundaries. Possible muscle and joint forces were calculated by constraining the
14 muscle forces between zero and the peak muscle force. Plausible muscle forces were
15 constrained within six selected EMG boundaries. The spectrum to EMG-driven force difference
16 increased from 40 N to 108 N for 1 to 15 EMG inputs. The best-fit muscle strategy better
17 described the EMG-driven pattern ($R^2 = 0.94$; RMSE = 19 N) than the static optimization
18 solution ($R^2 = 0.38$; RMSE = 61 N). Possible forces for 27 of 34 muscles varied between zero
19 and the peak muscle force, inducing a peak hip force of 11.3 body-weights. Plausible muscle
20 forces closely matched the selected EMG patterns; no effect of the EMG constraint was
21 observed on the remaining muscle force ranges. The model can be used to study alternative
22 muscle recruitment strategies in both physiological and pathophysiological neuromotor
23 conditions.

24

25

KEYWORDS

26 Subject-specific musculoskeletal models; Bayesian muscle force simulator; statistical
27 muscle recruitment; personalized lower-limb loads; level walking; human locomotion; muscle
28 synergy; muscle load sharing; muscle recruitment.

29

30

INTRODUCTION

31 Internal forces that physical activity engender on our skeleton through muscles and joints
32 are important for studying human motion [1] and skeletal mechanics [2]. However, the
33 biomechanical assessment of muscle forces is difficult because the musculoskeletal system is
34 highly redundant [3] and the sensorimotor control system is intrinsically variable [4]. Muscles
35 recruitment targets multiple and competing goals, and depends on the task being executed,
36 subjective healthy condition and noise that plague the sensory inputs and muscles output in
37 determining the appropriate motor command [5]. A better understanding of the repertoire of
38 alternative sensorimotor control strategies may reveal important in studying human motion and
39 skeletal mechanics [5].

40 According to the uncontrolled manifold hypothesis, our central nervous system uses all the
41 redundant degrees of freedom to ensure flexible and stable motion [6]. Possible muscle
42 synergies can therefore be defined as organizations of muscle forces that stabilize joint torques
43 and motion; or, in other words, alternative solutions to the muscle load sharing problem.
44 Körding and Wolpert showed that our central nervous system (CNS) likely interprets the
45 problem of optimal performance in a statistical fashion by weighting knowledge gathered from
46 previous experiences and information gathered from multiple sensory modalities [4]. By
47 considering both types of information in the form of prior and likelihood, Bayesian statistics
48 have been shown to properly describe the mechanism behind the generation of movement
49 trajectories [7], forces [8] and judgment timing [9]. Likewise, our CNS may solve the muscle
50 load sharing problem [4] by recruiting muscles from a space of alternative solutions, ensuring
51 stable motion [6]. However, the large majority of current methods used for calculating muscle
52 forces target, among the infinite possible solutions, the single muscle synergy that minimizes a
53 chosen cost function [10].

54 By using different energy- and stress-based cost functions, static optimization methods have
55 been shown to provide muscle force patterns that are in qualitative agreement with the recorded
56 electromyography (EMG) [11]. However, static optimization methods are known to
57 underestimate the contribution of balanced agonist-antagonist muscle contractions [12], the so-
58 called muscle co-contractions, which are essential in a number of circumstances. For example,
59 muscle co-contractions are important in (a) controlling the joint impedance and stability during
60 daily activities [13] and (b) for executing motions characterized by rapid changes of joint
61 torque, such as those occurring while landing [14] and running [15]. Muscle co-contractions
62 have also been found to determine the hip force during activity in terms of magnitude,
63 distribution and timing [13,16]. In cats, the static optimizations solution has been shown a poor
64 predictor of the soleus and gastrocnemius force pattern [17].

65 EMG-driven methods have been developed to calculate muscle force patterns that follow the
66 muscle electrical activity recorded using electromyography (EMG). EMG-driven muscle forces
67 are calculated by inputting the EMG signal to muscle excitation- and contraction-dynamic
68 models, which are then used to solve the dynamic problem of the motion [18–20]. However,
69 model simplifications and measurement errors cause inconsistencies between the motion being
70 studied and the calculated EMG-driven muscle forces. Inverse EMG-driven models solve the
71 muscle load sharing problem by forcing the static optimization solution within an arbitrarily
72 defined interval around the calculated EMG-driven muscle force to ensure that a solution to the
73 problem exists [19]. Forward EMG-driven models use optimization-based procedures to tune
74 the model so that the calculated EMG-driven muscle forces generate the desired motion of the
75 model [18,20]. Lloyd and Besier [18] used an EMG-driven model of the knee-spanning muscles
76 to estimate the knee torque. Sartori et al. [20] used a lower-limb model to calculate muscle
77 forces during walking, running, sidestepping and crossover cutting manoeuvres. However, the
78 single representative muscle synergy calculated using both EMG-driven and static optimization

79 methods cannot provide information about the spectrum of muscle synergies driving motion
80 [18–20].

81 Another possibility is to explore the entire solution space of the muscle load-sharing problem
82 [21]. The space of physiologically possible muscle synergies can be described as the solution
83 space of the inverse, highly indeterminate, linear problem of muscle equilibrium at the joints,
84 which can be geometrically represented by a bounded portion of a hyper-plane in the muscle
85 force domain [11]; its orientation, offset and boundaries are respectively determined by the
86 muscle lever arms, joint torques and physiological constraints of muscle force. Heino *et al.* [22]
87 combined Bayesian statistics and Markov Chain Monte Carlo (MCMC) methods for exploring
88 the solution space of highly indeterminate inverse linear problems in a software called
89 METABOLICA, which uses Bayesian statistics to estimate the posterior probability density
90 function (PDF) for the unknowns and the MCMC algorithm to sample the estimated PDF. By
91 constraining muscle forces between zero and the muscle peak force, this approach has been
92 used to explore the muscle potential to generate force during a single walking frame [21]. No
93 study has investigated the natural unpredictable variability of muscle forces during activity.
94 Combining musculoskeletal models, Bayesian statistics, MCMC sampling methods and EMG-
95 driven muscle force modelling is a viable solution for calculating the spectrum of either
96 potential or physiologically plausible musculoskeletal forces during activity.

97 The aim of this study was to investigate the repertoire of muscle synergies during walking.
98 The lower-limb joint torques, muscle lever arms, muscle force constraints and the EMG signals
99 for seven walking trials were taken from earlier studies [23,24]. The spectrum of muscle
100 recruitment strategies was calculated using Bayesian statistics and MCMC sampling methods,
101 while EMG-driven muscle forces were calculated using the available EMGs and a Hill-type
102 muscle excitation- and contraction-model. The model was characterised by studying the
103 consistency between EMG-driven forces and the model of the motion, and comparing the

104 proposed method with a commonly used static optimization procedure. Finally, the muscle
105 potential to generate force and the spectrum of physiologically plausible muscle forces were
106 calculated and analysed.

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110 MATERIALS AND METHODS

111 *Model development*

112 The model, developed for studying possible muscle recruitment strategies during motion,
113 was based on an earlier lower-limb model of a complete stride [23]. The complete motion
114 capture is available for download at www.physiomespace.com (key-word:
115 LHDL_1stMatchedVolunteer_MOCAP). EMGs were recorded for 15 lower-limb muscles (i.e.,
116 gluteus maximus, gluteus medius, rectus femoris, vastus lateralis, vastus medialis,
117 semitendinosus, biceps femoris long head, tibialis anterior, extensor digitorum, extensor
118 hallucis, peroneus longus, soleus, gastrocnemius lateralis, gastrocnemius medialis, flexor
119 digitorum) using a TelEMG[®] system (BTS, Milan, Italy, 2000 Hz). The model, implemented
120 in Matlab (The MathWorks, Natick, MA, USA), is generic in that it can be used to study the
121 muscle load sharing problem of any musculoskeletal model and task of motion. The analysis is
122 described in four parts: (1) the gait model; (2) the calculation of the muscle force potential,
123 hereinafter referred to as physiologically possible muscle forces; (3) the calculation of the
124 spectrum of muscle forces that represent the unpredictable variability of the muscle recruitment
125 process, hereinafter referred to as physiologically plausible muscle forces; and, (4) data
126 analysis.

127 *The gait model*

128 The musculoskeletal model, including the joint angles and torques while walking was
129 obtained from earlier studies [23,25,26] (Fig. 1). In summary, the lower-limb musculoskeletal
130 model was a muscle-actuated articulated system based on the work of Delp et al. [27], whose
131 anatomy was taken from the computed-tomography images and dissection of an 81 year-old
132 female donor (63 kg weight, 167 cm height). The articulated system was a 13-segment, 15
133 degree-of-freedom system, actuated by 84 Hill-type muscle-tendon units. The inertial

134 properties were calculated assuming homogenous bone (1.42 g/cm³) and soft-tissue (1.03
 135 g/cm³) density [28]. The physiological cross section area (PCSA) was calculated from the
 136 muscle volume and length. The peak isometric muscle stress was assumed equal to 1.37 MPa,
 137 the upper bound of published values [29]. The remaining muscle parameters were based on the
 138 work of Delp et al. (1990). The gait simulation used skin-mounted marker trajectories (Vicon
 139 Motion Capture, Oxford UK, 100 Hz) and ground reaction forces at both feet (Kistler
 140 Instrument AG, Switzerland, 2000 Hz), recorded following the protocol proposed by Leardini
 141 et al. (2007) [30]. Joint angles and torques were calculated using the inverse kinematic, dynamic
 142 and static optimization algorithms implemented in Opensim [31]. The model yielded joint
 143 torques within published values, hip contact forces in agreement with in vivo measurements
 144 and muscle force patterns in good qualitative agreement with corresponding EMG recordings
 145 [23,25,26].

146 *Physiologically possible muscle and joint forces*

147 Physiologically possible muscle forces are defined as muscle forces within physiological
 148 boundaries, generating the joint torque from inverse dynamics and assuming that muscle
 149 activation can range from zero to full activation. Therefore, the muscle's force generating
 150 potential is represented by the boundaries of physiologically possible muscle forces. For each
 151 walking frame, the instantaneous equilibrium equation at the joints (Eq. 1), representing the
 152 muscle load sharing problem, was determined by extracting the muscle lever arm, the muscle
 153 constraints and the net joint torques from an earlier simulation of walking [23]. The equation
 154 takes the form

$$155 \quad \begin{cases} \bar{B} \times \bar{F} = \bar{M}; \bar{B} \in \mathfrak{R}^{m \times n}; \bar{F} \in \mathfrak{R}^n; \bar{M} \in \mathfrak{R}^m \\ \bar{F}_l < \bar{F} < \bar{F}_u \end{cases} \quad \text{Eq. 1}$$

156 where \bar{B} is the matrix of muscle lever arms, \bar{F} is the muscle force vector, \bar{M} is the joint torque
 157 vector, \bar{F}_l and \bar{F}_u are respectively the lower and the upper muscles force boundaries, m is the

158 number of degree-of-freedom of the articulated system and n is the number of muscles in the
 159 model. The peak muscle force was calculated using a Hill-type muscle model. The active and
 160 passive force-length relationships were taken from the work of Thelen [32], while the force-
 161 velocity relationship was taken from the work of Delp et al. [27]. Muscle force vectors within
 162 the spectrum were categorised using a single parameter, or muscle co-contraction, defined as
 163 the difference between the actual muscle force and the minimal force required to generate a
 164 given joint torque. Each muscle force vector, solution of the muscle recruitment problem, was
 165 thus composed by a first minimal co-contraction component, represented by the static
 166 optimization solution, and a second component or muscle co-contraction force component. The
 167 muscle co-contraction level was assumed the fraction between the actual muscle co-contraction
 168 force component and the difference between the peak muscle force and the static optimization
 169 solution. The lower bound of muscles force \bar{F}_l was set to zero, mimicking the muscle inability
 170 to sustain compressive forces. The upper bound of muscle forces \bar{F}_u was defined by studying
 171 five uniformly distributed co-contraction levels from zero (i.e., the optimization solution) to
 172 full co-contraction (i.e., the peak muscle force vector). Samples of physiologically possible
 173 muscle forces, solutions of Eq. 1, were calculated using METABOLICA [22]. The software
 174 interprets the vector of muscle forces \bar{F} as a multivariate random variable characterized by its
 175 probability density function (PDF) and it samples the calculated PDF using a Markov Chain
 176 Monte Carlo (MCMC) algorithm. The vector of muscle force \bar{F} was assumed uniformly
 177 distributed [21]. Thus, the prior probability density function of muscle forces takes the form

$$178 \quad \pi_{pr}(\bar{F}) \propto \Theta(\bar{F}) \Theta(\bar{F}_u - \bar{F}) \quad \text{Eq. 2}$$

179 where $\Theta(\bar{F})$ takes on the value of one if all components of the argument are positive and
 180 vanishes otherwise. The posterior PDF describing how \bar{F} is distributed is

$$181 \quad \pi(\bar{F}|\bar{M}) \propto \pi_{pr}(\bar{F})\pi(\bar{M}|\bar{F}) \quad \text{Eq. 3}$$

182 meaning that the posterior probability density function of muscle forces $\pi(\bar{F}|\bar{M})$ is
 183 proportional to the prior PDF, $\pi_{pr}(\bar{F})$, and the sensory information about the system states
 184 $\pi(\bar{M}|\bar{F})$, or likelihood. The stability of motion was defined by assuming the joint torque vector
 185 \bar{M} the deterministic value calculated using inverse dynamics. For each walking frame, Markov
 186 Chain Monte Carlo (MCMC) algorithm was used to generate the ensemble $\{\bar{F}^0, \bar{F}^1, \dots, \bar{F}^n\}$ of
 187 200,000 samples whose entries are random realizations drawn from Eq. 3. The null space of the
 188 matrix \bar{B} , containing the muscle lever arm extracted from the model [23], is calculated using
 189 Singular Value Decomposition. The vector \bar{F} is decomposed into a component \bar{F}_1 lying on the
 190 null space and a component \bar{F}_2 orthogonal to \bar{F}_1 . Samples are drawn from the solution space
 191 using an MCMC algorithm by separately sampling the component \bar{F}_1 using a hit-and-run
 192 algorithm and the component \bar{F}_2 using a Gibbs algorithm [22].

193 The hip, knee and ankle reaction forces were calculated using the equation

$$194 \quad \bar{J}R = \bar{J}R_d + \sum_{i=1}^n \bar{F}_i \quad \text{Eq. 5}$$

195 where $\bar{J}R_d$ is the joint reaction force vector calculated using inverse dynamics, and \bar{F}_i is the
 196 i^{th} joint-spanning muscle force vector.

197 *Physiologically plausible muscle forces*

198 Physiologically plausible muscle forces are defined as forces most likely to occur during
 199 normal gait and can be seen as a sub-group of the physiologically possible muscle forces.
 200 Therefore, physiologically plausible muscle forces were calculated by combining
 201 physiologically possible muscle forces and the variability of the muscle electrical activity from
 202 repeated EMGs.

203 Muscle forces were calculated using EMGs and Hill-type excitation- and contraction-
 204 dynamic models according to the guidelines proposed by Zajac [33]. The raw EMG signal was
 205 band-pass filtered (zero-pole-gain design, 8th order, Butterworth filter) with cut-off frequencies

206 of 10 and 400 Hz to minimize noise due to motion artifacts and the EMG amplifier [34]. The
207 filtered EMG signal was rectified and low-pass filtered (zero-pole-gain design, 2nd order,
208 Butterworth filter) with cut-off frequency of 6 Hz [33] and a 22 ms electromechanical delay,
209 representing the muscle time response to stimuli, applied to synchronize the processed signal
210 with the muscle response [35]. Normalisation of the processed EMG signal was then necessary
211 to obtain a signal between zero and one representing muscle activation [33]. We scaled the
212 processed EMG signal to match the peak muscle activation calculated using static optimization
213 [23]. The EMG-driven muscle force was calculated using the calculated muscle activation, the
214 active and passive force-length relationships from the work of Thelen [32] and the force-
215 velocity relationship from the work of Delp et al. [27] for all seven gait repetitions. The force
216 range, that is, the upper (\bar{F}_u) to the lower (\bar{F}_l) bound of muscle forces of physiologically
217 plausible muscle forces, was assumed at the 0.68 quantile (i.e. mean \pm SD) of the EMG-driven
218 muscle force distribution projected onto the solution space of Eq. 1. Samples of physiologically
219 plausible muscle forces were generated using METABOLICA by constraining muscle forces
220 within the calculated force range for selected muscles and between zero and the peak
221 physiological force for the remaining muscles.

222 *Data analysis*

223 Simulations were run on a desktop PC (Window 7, 64 bit, Intel Xenon E5-2630 v2, 2.60
224 GHz, 64 GB of memory). The gait cycle was divided into clusters of time frames and processed
225 by 12 different CPUs using parallel computing. The speed in generating muscle force samples
226 was output by the code.

227 The gait model was assessed by comparing the donor's PCSAs to corresponding
228 measurements from donors of 83 \pm 9 year of age [36]. The muscle lever arm and the joint torques
229 in the model were compared to corresponding published values [36–40]. Calculation of muscle
230 forces were verified by comparing the joint torque generated by the muscles with that calculated

231 using inverse dynamics. The consistency between the EMG-driven muscle forces and the
232 motion was assessed by using the distance between the EMG-driven muscle forces and the
233 solution space of Eq. 1 as the metric; the average force distance over gait and muscles, and the
234 muscle-by-muscle average distance during gait were calculated. The nearest muscle force
235 vector to the EMG-driven force vector, henceforth referred to as the best-fit solution, was used
236 for comparing the ability of the present method with that of a commonly used static
237 optimization procedure in describing the recorded EMG pattern. To this purpose, we calculated
238 (a) the linear regression between the EMG-driven muscle force and the best-fit muscle force,
239 and (b) the linear regression between the EMG-driven muscle force and the static optimization
240 solution obtained by minimizing the squared sum of muscle stress [27,31].

241 Alternative muscle recruitment strategies were studied in terms of physiologically possible
242 and plausible muscle and joint forces. Physiologically possible forces were assessed by plotting
243 the boundaries of muscle and joint forces for a progressive increase of the muscle co-contraction
244 level. Physiologically plausible muscle forces were calculated by inputting to the model a sub-
245 set of EMGs [19]; for this study we used six of the principal lower-limb muscles spanning the
246 hip, the knee and the ankle (gluteus maximus, rectus femoris, vastus lateralis, biceps femoris
247 long head, tibialis anterior and gastrocnemius medialis). The available EMGs not input to the
248 model were compared with the respective force spectrum from the model.

249

250

RESULTS

251 The process resulted in 103 M and 20.6 M of different muscle forces respectively
252 representing potential and plausible muscle forces driving walking. The algorithm generated
253 909 muscle force vectors, solution of Eq. 1, per second per processor.

254 The model anatomy and motion were in agreement with earlier studies. The muscle lever
255 arms were consistent with those reported in earlier theoretical and experimental studies [37–
256 39,41–44] (Table 1). The average donor's muscle PCSA was 6.15 cm^2 , which represent the 25th
257 lower percentile of the elderly population reported by Ward et al. [36] (Table 2). The joint
258 torques pattern was in agreement with that reported by Benedetti and co-workers [40] (Fig. 2).
259 The highest unbalance between the joint torque driving walking and the net joint torque
260 produced by the muscles was $3 \times 10^{-11} \text{ Nm}$. The distance between the model and the EMG-driven
261 force, averaged over gait and muscles, was below 40 N, while the peak muscle-by-muscle
262 average distance over gait increased up to 108 N for 15 EMGs input to the model (Fig. 3). The
263 best-fit solution better represented the EMG pattern than it did the static optimization solution
264 (Fig. 4). The coefficient of determination between the best-fit solution and EMG-driven muscle
265 forces was $R^2 = 0.94$, and the average error was $\text{RMS} = 19 \text{ N}$ (Fig. 5). The static optimization
266 solution showed major discrepancies in the muscle force pattern during (a) the early stance
267 phase of walking for the rectus femoris, (b) the stance-to-swing phase for the rectus femoris
268 and the biceps femoris long head, and (c) the late swing phase for the gluteus maximus and the
269 tibialis anterior. The coefficient of determination between the static optimization solution and
270 EMG-driven muscle forces was $R^2 = 0.38$, and the average error was $\text{RMSE} = 61 \text{ N}$.

271 Physiologically possible muscle synergies comprised muscle forces ranging from zero to the
272 peak muscle force for most muscles. Twenty-seven out of the 34 lower-limb muscles ranged
273 from zero to their peak force whereas seven muscles (gluteus maximus, adductor magnus,
274 semimembranosus, vastus medialis, vastus lateralis, vastus medialis and soleus) couldn't reach

275 their peak force. The resulting upper and lower boundaries of the hip, knee and ankle force
276 spectrums showed typical double-peak patterns; the upper force boundary reached 11.3 BW,
277 6.2 BW, 7.6 BW, and the lower boundary reached 4.4 BW, 2.5 BW and 3.5 BW at the hip, the
278 knee and the ankle, respectively. Increasing the upper boundary of the muscle force up to 60%
279 muscle co-contraction caused a proportional shift upward of the upper force boundary of
280 possible muscle and joint forces. Further increasing the upper bound of muscle forces caused a
281 complex non-linear response of muscle and joint forces. Negligible changes of the lower force
282 boundary were observed by allowing different muscle co-contraction levels (Fig. 6 and 7).
283 Physiologically plausible muscle forces well represented the pattern of the muscle electrical
284 activity (Fig. 8 and 9). The gluteus maximus showed a consistent double-peak activity, reaching
285 its peak values during the early stance (5% gait) and mid-swing (65% gait) phases of walking.
286 The biceps femoris long head peaked at 10%, 50% and 90% gait. The rectus femoris peaked at
287 heel strike (7% gait) and prior to toe-off (50% gait). The vastus lateralis peaked at heel-strike
288 (5% gait) and prior to toe-off (43% gait). The medial gastrocnemius peaked at 40% gait and
289 showed a smaller second peak at mid-swing (70% gait). The tibialis anterior showed a double-
290 peak activity, reaching its peak at early stance (5% gait) and mid-swing (75% gait). The EMG-
291 driven force range for the gluteus medius, vastus medialis, semitendinosus, extensor hallucis,
292 extensor digitorum, peroneus longus, soleus, gastrocnemius lateralis and flexor digitorum,
293 which were not input to the model, was smaller than the calculated force range (Fig. 9).

294 **DISCUSSION**

295 The aim of this study was to investigate possible muscle synergies during walking. We used
296 a human gait model in conjunction with Bayesian statistics, MCMC sampling method and
297 EMG-driven muscle force modelling to calculate muscle forces in full respect of physiological
298 and dynamical constraints. The gait model provided reliable information about all the relevant
299 musculoskeletal parameters during walking, including muscle lever arm, muscle size and joint

300 torques [36–40]. Muscle forces were calculated in an efficient manner, providing information
301 about (a) the potential muscle and joint forces, and (b) the spectrum of muscle forces consistent
302 with the muscle electrical activity input to the model.

303 The algorithm generated 909 muscle force samples per second per processor. Therefore, the
304 present method can be used to calculate the spectrum of muscle forces during motion on
305 standard desktop machines and can take advantage from using parallel computing on
306 multiprocessor systems. The model could well represent, on average, EMG-driven muscle
307 forces. However, the muscle-by-muscle distance between the model solutions and the EMG-
308 driven muscle forces increased for an increasing number of EMG signals input into the model.
309 This inconsistency may explain why EMG-driven models may not offer a solution when several
310 EMGs are input to the model [19]. Other authors optimized the model parameters within
311 physiological boundaries, solving the model consistency problem and ensuring that a solution
312 to the motion problem exists [18,20,45]. However, the optimized model likely provides little
313 information about how the calculated solution represents the subject under study because of the
314 typically large variability of physiological parameters. More work is necessary to understand
315 how model simplifications and input errors influence model calculations. To this purpose, the
316 proposed method is well suited to take in input the variability of joint torques and EMGs, either
317 caused by the natural unpredictable variability of motion or by uncertainties on measurements.
318 The best-fit solution in the model more closely represented ($R^2 = 0.94$) the muscle electrical
319 activity than a static optimization procedure ($R^2 = 0.38$) largely accepted for simulating normal
320 walking [11,31], without requiring any assumptions about the adopted sensorimotor behaviour.
321 Therefore, the proposed method can be used to calculate muscle forces when the objective of
322 the sensorimotor behaviour is variable or not known, including in the instances of either
323 physiological or pathophysiological neuromotor conditions.

324 Physiologically possible muscle synergies comprehend muscle forces ranging from zero to
325 the peak muscle force (Fig. 6) and joint contact force of up to 11.3 BW at the hip (Fig. 7). Up
326 to 60% muscle co-contraction caused a linear increase of muscle and joint forces, whereas
327 higher muscle co-contraction caused a non-linear increase of the same quantities (Fig. 6 and 7).
328 While the probability for these extreme loading conditions to occur has to be determined, these
329 findings may have implications in studying muscle ability to control joint impedance and
330 stability [13], the yet unresolved fracture mechanism for low-energy osteoporotic fractures [46],
331 and may reveal important information for the development of exercise therapies for bone health
332 [47]. Physiologically plausible muscle force patterns well represented the muscle electrical
333 activity input to the model (Fig. 9). Therefore, the proposed approach can be used to study deep
334 aspects of human motion. For example, the calculated spectrum can be used for exploring how
335 different muscles can combine their action in response to the same motor demand.

336 To the best of the authors' knowledge this is the first numerical study exploring the spectrum
337 of muscle synergies during motion. The model has been shown capable of yielding kinematic,
338 kinetics, hip contact forces and muscle firing patterns in agreement with published patterns for
339 multiple activities [23,25], providing confidence in the reliability of the studied muscle load
340 sharing problem. The large variability of physiologically possible and physiologically plausible
341 muscle forces is consistent with the known ability of the CNS for adopting very different muscle
342 recruitment strategies [16,48]. Although no measurements of the joint contact force under full
343 muscle co-contractions are available, the range of the calculated hip contact force (3.7-11.4
344 BW) compares well with the hip contact force of 8.7 BW measured by Bergmann and co-
345 workers during stumbling, a value that has been largely attributed to muscle co-contraction
346 rather than to motion dynamics [16]. This provides confidence in the calculated spectrum of
347 muscle forces.

348 The main limitation of the present study is that the majority of the muscle forces that were
349 not constrained between EMG-driven muscle force boundaries (e.g., the semitendinosus)
350 showed a much higher variability (Fig. 9) than that obtained from repeated EMG recordings,
351 indicating that the calculated spectrum of physiologically plausible muscle forces is larger than
352 that observed in vivo. While it is possible that a reduced number of EMGs input to the model
353 [19] explain the majority of the muscle force variability, the optimal number and type of EMG
354 signals has to be determined. Second, the processed EMG signal was normalised using the peak
355 muscle activation calculated using static optimization, whereas others normalized the processed
356 EMGs to a maximum voluntary contraction task [18,19]. However, a standardized EMG
357 normalization process has yet to be defined [19]. Third, the present results cannot be generalized
358 due to the single anatomy used. More research is necessary to solve this limitation. Fourth, the
359 joint torque was set to the deterministic values calculated using inverse dynamics, thus
360 neglecting the joint torque uncertainties attributable to model assumption and measurement
361 errors [49]. However, this allowed studying the isolated effect of alternative muscle recruitment
362 strategies on calculated muscle and joint forces. Last, the peak isometric muscle stress was the
363 upper boundary of published values (1.37 MPa, [29]), possibly causing an overestimation of
364 calculated forces. However, the upper boundary of muscle forces is a linear function of the peak
365 isometric muscle stress while the lower boundary is almost invariant [23]. Therefore, the
366 boundaries of muscle and joint forces for every intermediate value of the peak isometric stress
367 can be easily extrapolated.

368 Despite the study limitations, present findings are important for the biomechanics
369 community in that they provide a viable numerical approach for modelling the stochastic nature
370 of the muscle recruitment process. The present results strengthen the notion that muscle co-
371 contraction is important in studying human motion, and provide a viable numerical approach
372 for studying physiological and pathophysiological conditions characterized by complex

373 sensorimotor behaviours. Moreover, because the proposed approach makes no assumptions on
 374 the “normality” of neuromotor control, we expect it to be equally effective in subjects affected
 375 by severe neuromuscular pathologies.

376

377

AKNOWLEDGMENTS

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380

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- 532
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534

TABLES

535 Table 1 – The range of the muscle lever arm (cm).

Muscle bundles	The model	Scheys et al., [37]	Arnold et al., [38]	Bonnefoy et al., [39]	White et al. [41]	Kepple et al. [42]	Pierrynowski et al. [43,44]
<i>Hip abduction moment arm</i>							
Gluteus medius anterior	4.7 : 5.7	1.0 : 4.0					
Gluteus medius medial	5.1 : 5.7	1.8 : 4.5					
Gluteus medius posterior	4.1 : 4.9	0.7 : 4.8					
Gluteus minimus anterior	4.1 : 4.7	0.2 : 3.8					
Gluteus minimus medial	4.2 : 5.3	1.0 : 4.0					
Gluteus minimus posterior	4.3 : 5.7	0.0 : 4.2					
Tensor fascia latae	4.7 : 6.8	2.0 : 6.5		6.0 : 7.4	12.4 : 13.2	11.6 : 12.4	3.7 : 5.3
<i>Hip adduction moment arm</i>							
Adductor brevis	5.4 : 7.5	1.0 : 6.0					
Adductor longus	5.3 : 7.0	2.2 : 7.7					
Adductor magnus superior	6.5 : 8.2	3.0 : 6.0					
Adductor magnus medial	6.7 : 7.7	3.0 : 6.0					
Adductor magnus inferior	3.2 : 6.2	2.2 : 6.1					
Gracilis	8.4 : 9.4	1.0 : 7.8		5.6 : 6.2	2.4 : 3.1	2.8 : 4.4	1.5 : 4.5
<i>Hip flexion moment arm</i>							
Ileo-psoas	3.5 : 4.1						
Rectus femoris	2.1 : 4.2	1.9 : 5	2.3 : 3.5	5.3 : 6.1	8.8 : 10.2	9.2 : 11.2	2.4 : 5.0
Sartorius	2.0 : 7.3	1.8 : 7					
<i>Hip extension moment arm</i>							
Biceps femoris long head	2.5 : 6.0	0.2 : 6.0					
Gluteus maximus anterior	4.6 : 5.3	0.0 : 4.0					
Gluteus maximus medial	5.3 : 6.9	0.0 : 4.5					
Gluteus maximus posterior	4.8 : 9.0	0.0 : 6.2					
Semimembranosus	1.4 : 5.4	0.0 : 5.9	3.1 : 4.1				
Semitendinosus	2.2 : 6.3	0.0 : 6.0	3.3 : 5.2				
<i>Knee flexion moment arm</i>							
Biceps femoris long head	4.1 : 5.5			5.7 : 7.1	2.1 : 3.5	3.5 : 4.9	6.1 : 7.1
Biceps femoris short head	3.0 : 4.2						
Semimembranosus	2.9 : 4.1			6.2 : 6.6	2.2 : 5.2	2.7 : 5.3	3.3 : 5.5
Semitendinosus	2.7 : 4.4						
<i>Knee extension moment arm</i>							
Rectus femoris	2.5 : 5.2			3.7 : 4.3	2.1 : 2.7	2.8 : 3.4	4.3 : 5.1
Vastus intermedius	2.6 : 5.3						
Vastus lateralis	2.5 : 5.0						
Vastus medialis	2.4 : 4.9						
<i>Ankle dorsi-flexor moment arm</i>							
Tibialis anterior	3.1 : 3.6			2.5 : 2.9	6.3 : 7.7	3.6 : 4.1	2.3 : 2.5
Extensor digitorum	2.7 : 3.1						
<i>Ankle plantar-flexor moment arm</i>							
Triceps surae	3.4 : 5.0			4.4 : 5.6	4.9 : 6.5	5.3 : 6.5	6.3 : 7.1
Peroneus	1.7 : 2.3			2.8 : 3.0	5.7 : 7.3	2.9 : 4.0	1.7 : 1.9
Tibialis posterior	1.4 : 1.8			2.3 : 2.5	2.9 : 4.3	1.7 : 2.1	1.7 : 1.8
Flexor hallucis	2.1 : 2.2						

536

537

538 Table 2 – Physiological cross section areas (PCSAs) in the model and corresponding published
 539 values (cm²).
 540

Muscles	Ward et al. [36] [^] Mean (STD)	The donor*	
		Left	Right
Psoas major	7.7 (2.3)	3.8	2.9
Iliacus	9.9 (3.4)	4.0	2.7
Gluteus maximus	33.4 (8.8)	27.6	24.1
Gluteus medius	33.8 (14.4)	14.9	15.4
Gluteus minimus	N/A	2.5	N/A
Sartorius	1.9 (0.7)	1.2	1.1
Tensor Fascia Lata	N/A	2.6	2.4
Rectus femoris	13.5 (5.0)	2.1	2.7
Vastus lateralis	35.1 (16.1)	9.3	9.3
Vastus intermedius	16.7 (6.9)	6.4	7.0
Vastus medialis	20.6 (7.2)	11.7	12.0
Gracilis	2.2 (0.8)	1.6	1.3
Adductor longus	6.5 (2.2)	5.1	4.1
Adductor brevis	5 (2.1)	5.4	6.0
Adductor magnus	20.5 (7.8)	12.7	8.5
Biceps femoris long head	11.3 (4.8)	3.3	3.4
Biceps femoris short head	5.1 (1.7)	4.6	4.0
Semitendinosus	4.8 (2.0)	2.9	3.0
Semimembranosus	18.4 (7.5)	12.8	16.1
Tibialis anterior	10.9 (3)	4.3	4.0
Extensor hallucis longus	2.7 (1.5)	1.7	2.7
Extensor digitorum longus	5.6 (1.7)	1.4	3.7
Peroneus longus	10.4 (3.8)	4.5	5.9
Peroneus brevis	4.9 (2.0)	3.4	4.4
Gastrocnemius medial head	21.1 (5.7)	N/A	N/A
Gastrocnemius lateral head	9.7 (3.3)	6.3	6.1
Soleus	51.8 (14.9)	10.5	11.2
Flexor hallucis longus	6.9 (2.7)	N/A	N/A
Flexor digitorum longus	4.4 (2)	2.5	2.6
Tibialis posterior	14.4 (4.9)	1.1	1.4
Mean	13.9 (5.0)	6.1	6.2

541 * The physiological cross section area was calculated by measuring the muscle volume and length and using published estimates of the
 542 pennation angle [50].

543 [^] PCSA values represent the mean and the standard deviation of measurements taken from 21 elderly donors (83 ± 9 years; male:female ratio,
 544 9:12) [36].
 545

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FIGURES

551 **Fig. 1:** The musculoskeletal model (a), the motion capture scheme (b) and the model during
552 an intermediate frame of walking (c).

553 **Fig. 2:** Comparison between the calculated joint torque (solid black) at the hip, the knee and
554 the ankle and the joint torque bands (grey bands) reported by Benedetti et al. [40] for
555 healthy subjects.

556 **Fig. 3:** Distance between EMG-driven muscle forces and the solution space of the muscle
557 load sharing problem for an increasing number of EMGs input to the model. In blue,
558 the muscle distance averaged over gait and muscles. In green, the muscle-by-muscle
559 distance averaged over gait.

560 **Fig. 4:** Force patterns for the EMG-driven, the static optimization and the best-fit muscle
561 synergy extracted from the solution space of the muscle recruitment problem.

562 **Fig. 5:** Linear regression analysis between the EMG-driven muscle forces, the static
563 optimization solution (right) and the best-fit muscle synergy (left).

564 **Fig. 6:** Physiologically possible muscle forces. The dashed-black line represents the peak
565 muscle force. The solid-red and solid-blue lines represent the upper and the lower
566 muscle force boundary (low-band passed at 6 Hz, zero-pole design, sixth-order
567 Butterworth filter). Each level represents an admissible muscle co-contraction of 0.2,
568 0.4, 0.6, 0.8 and 1.

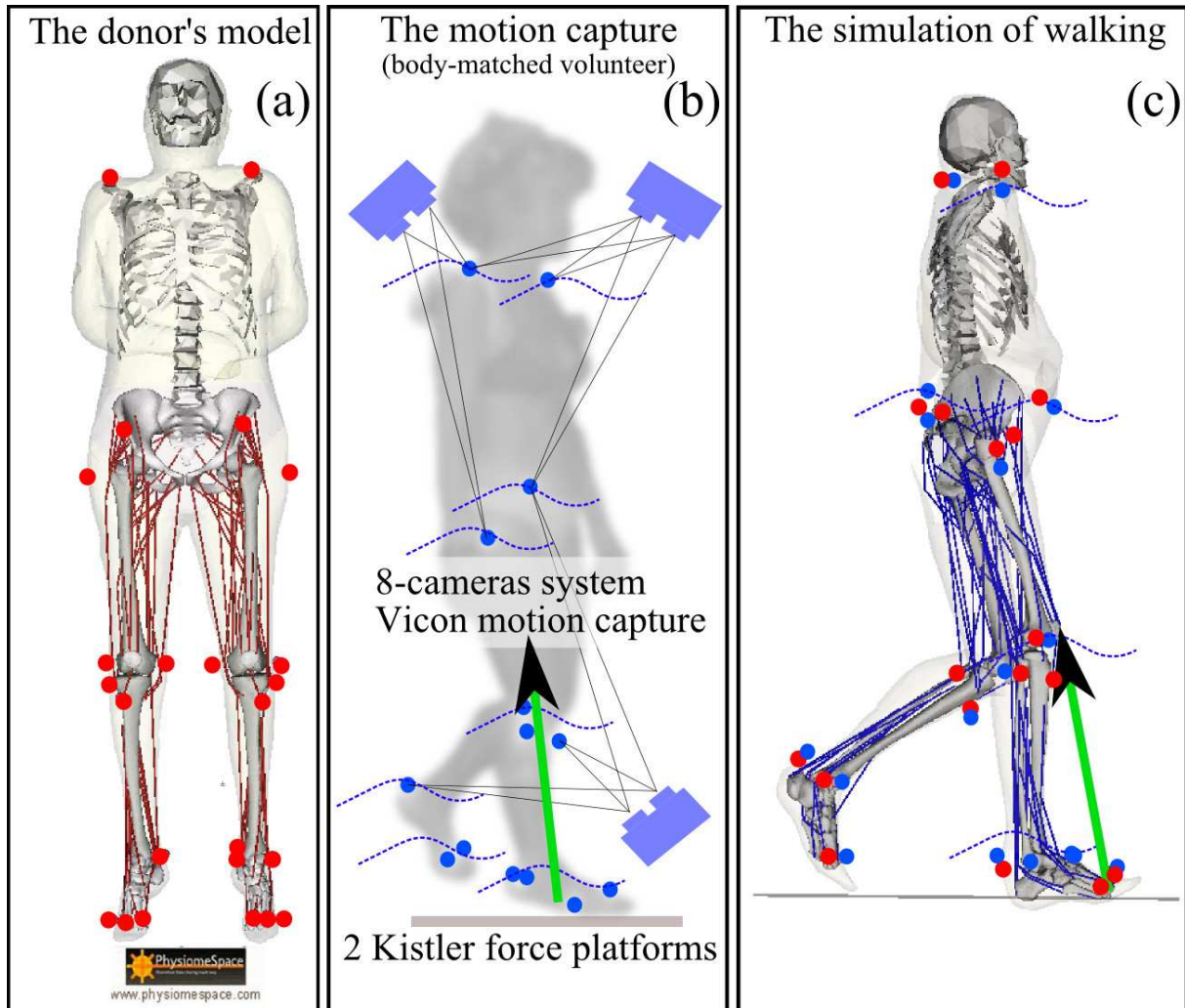
569 **Fig. 7:** Physiologically possible hip, knee and ankle contact forces. The shaded grey area
570 represents possible joint forces calculated constraining muscle forces between zero
571 and the peak muscle force. The solid-black lines represent the joint contact force
572 boundary for an admissible muscle co-contraction of 0.2, 0.4, 0.6, 0.8 and 1 (low-
573 band passed at 6 Hz, zero-pole design, sixth-order Butterworth filter).

574 **Fig. 8:** The 15-channel EMG signals for the seven gait trials. The shaded areas represent the
575 0.68 quantile (i.e. mean \pm SD) of the EMG distribution. The EMGs sub-set used to
576 calculate the spectrum of physiologically plausible muscle forces is shaded in red.

577 **Fig. 9:** Physiologically plausible muscle forces. The selected muscle force spectrums
578 constrained between EMG-driven force boundaries are shaded in red whereas the
579 remaining muscle force spectrums are shaded in grey. For these latter, the dashed-
580 black line represents the peak muscle force.

581

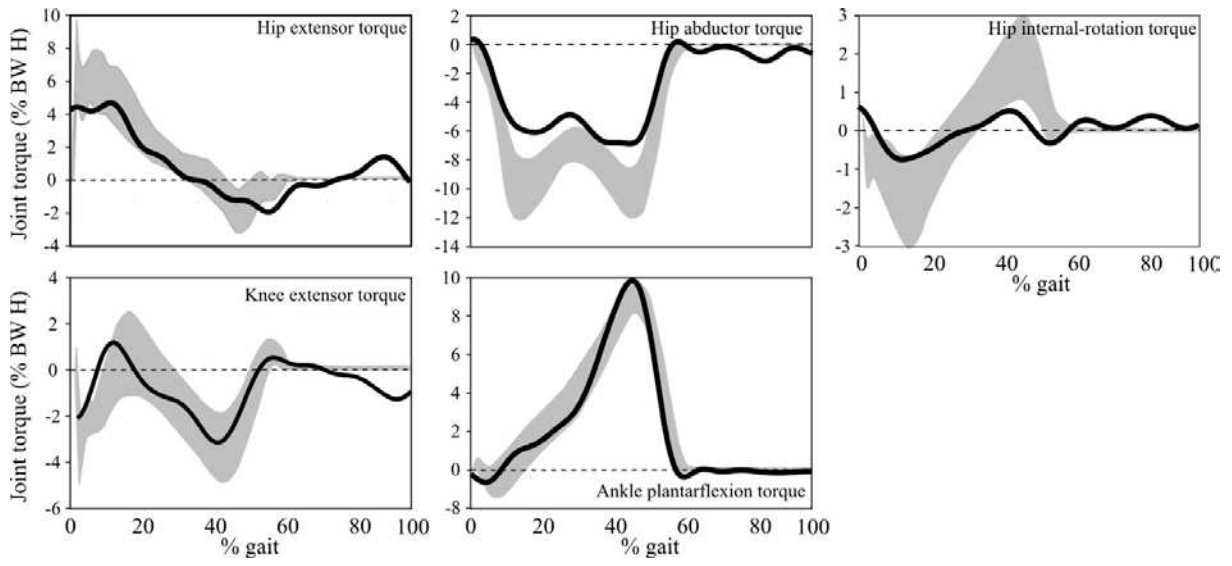
582 **Figure 1**



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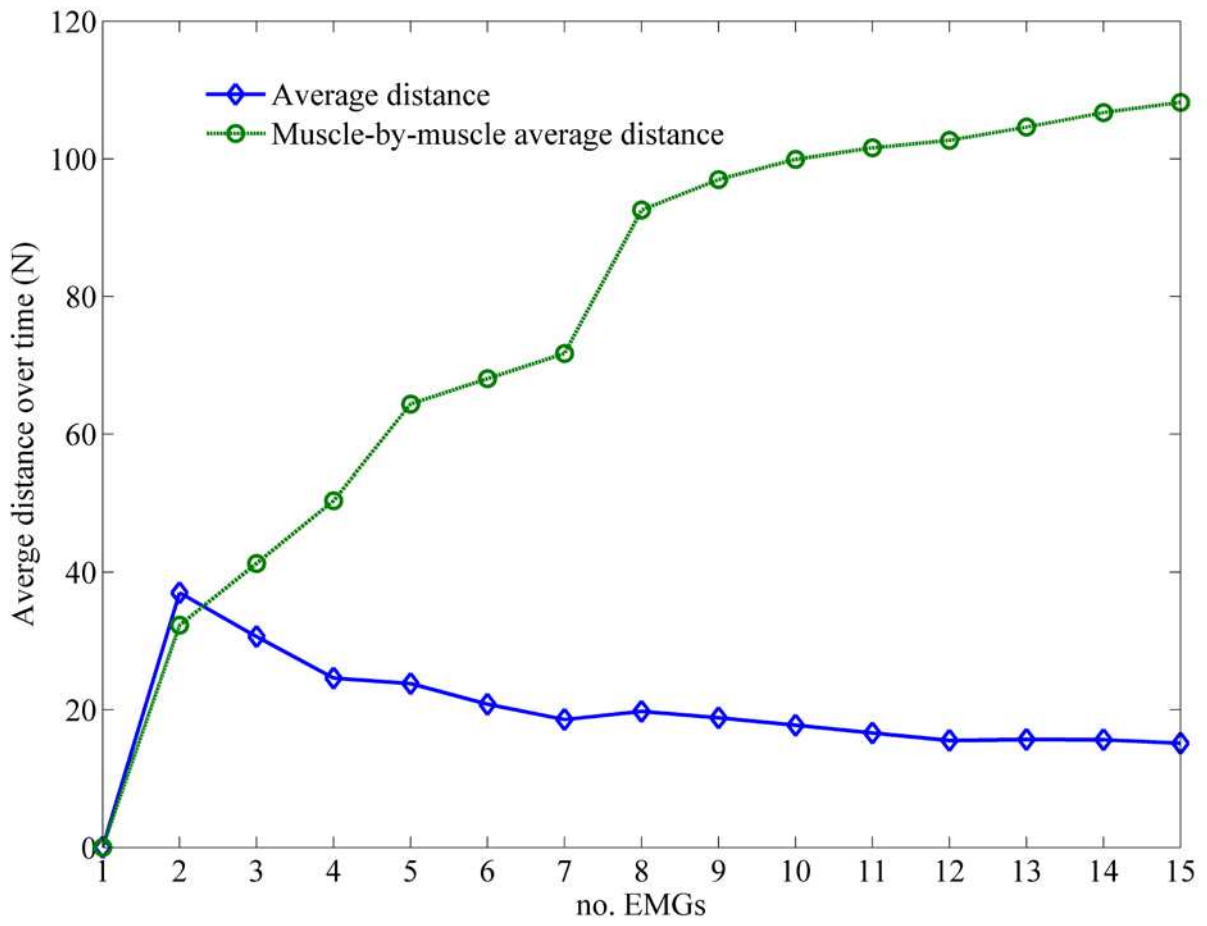
585 Figure2



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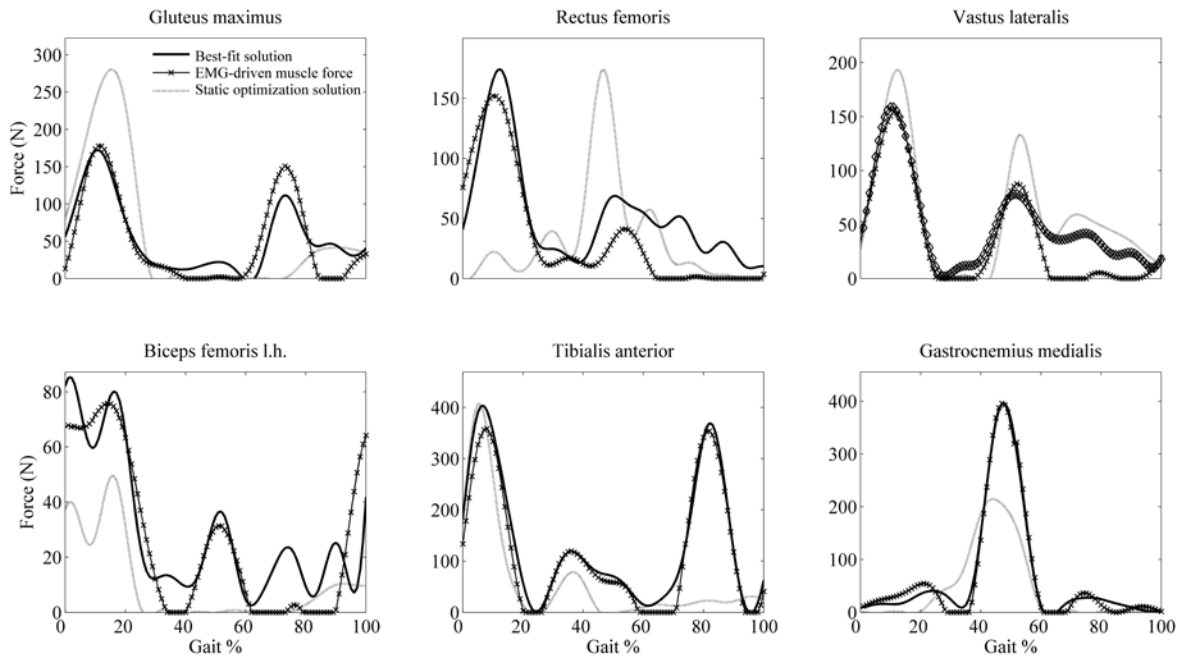
588 Figure 3



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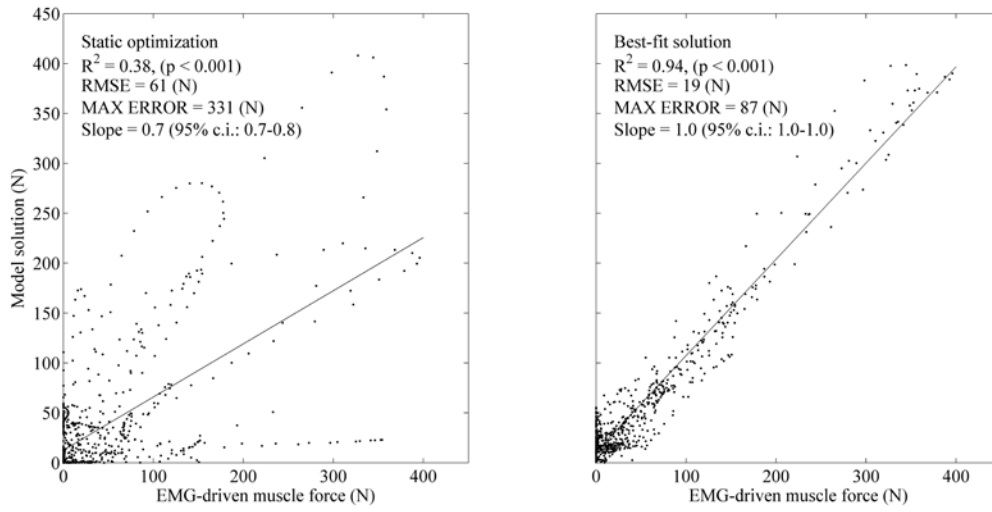
591 Figure 4



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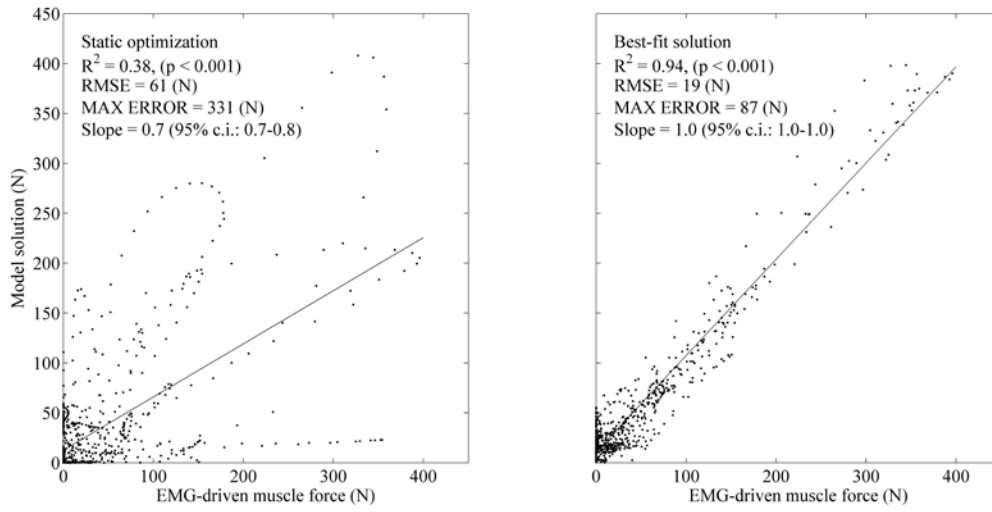
594 Figure 4



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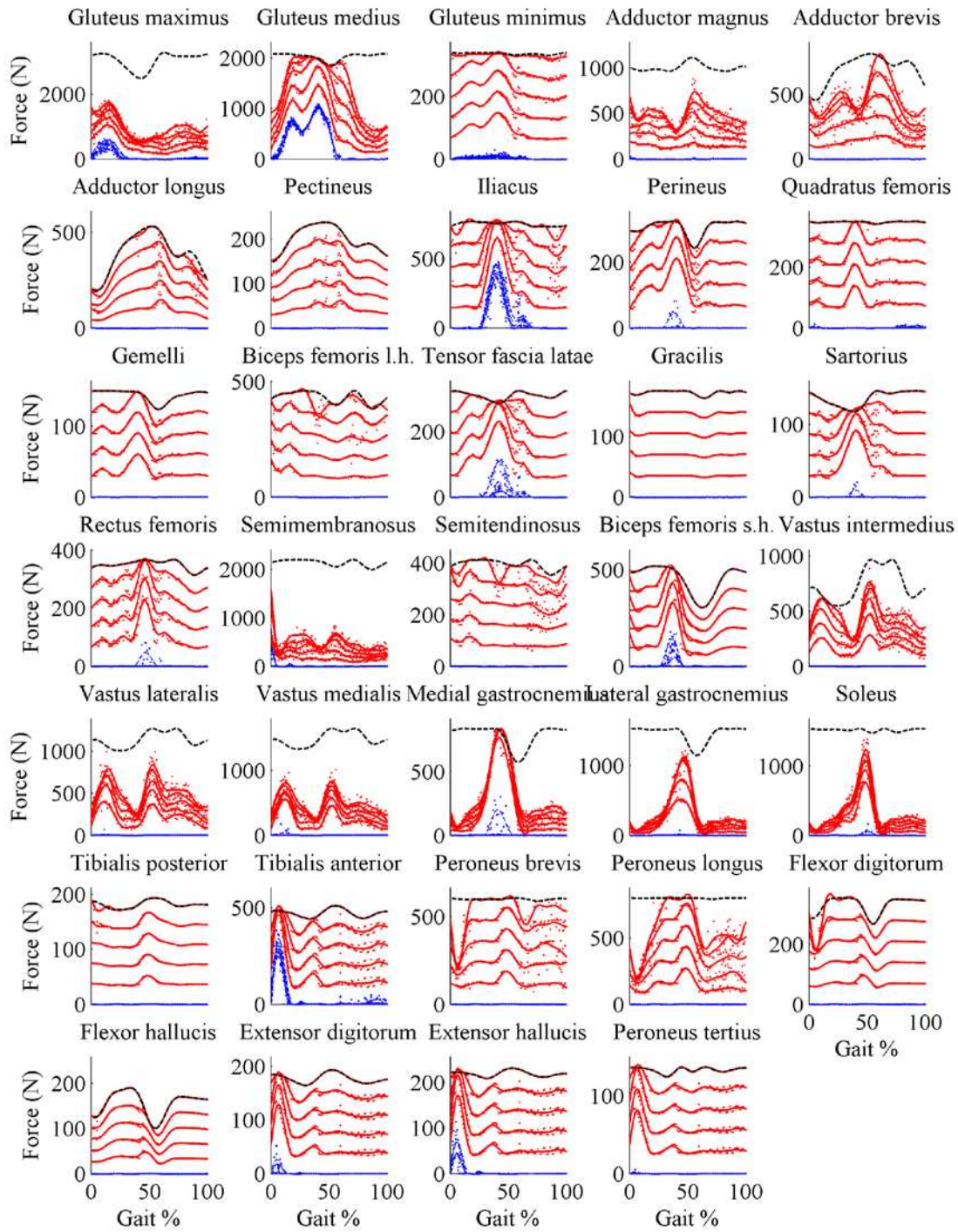
597 Figure 5



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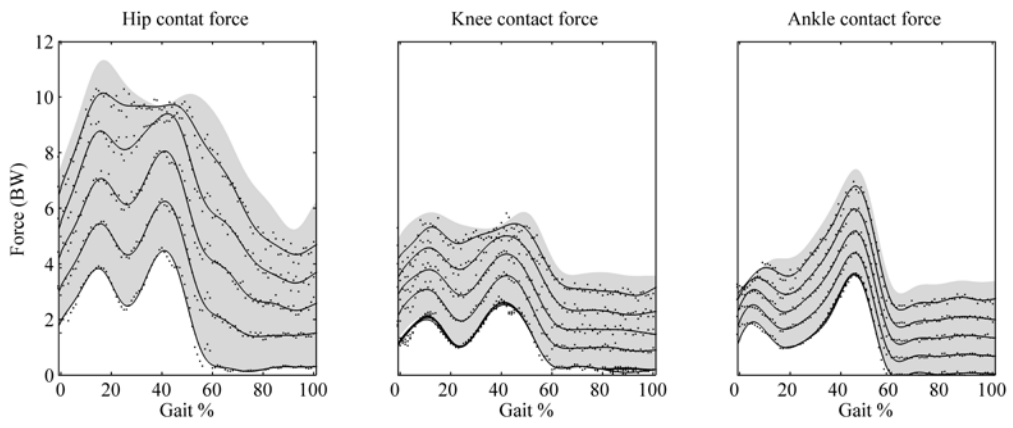
600 Figure 6



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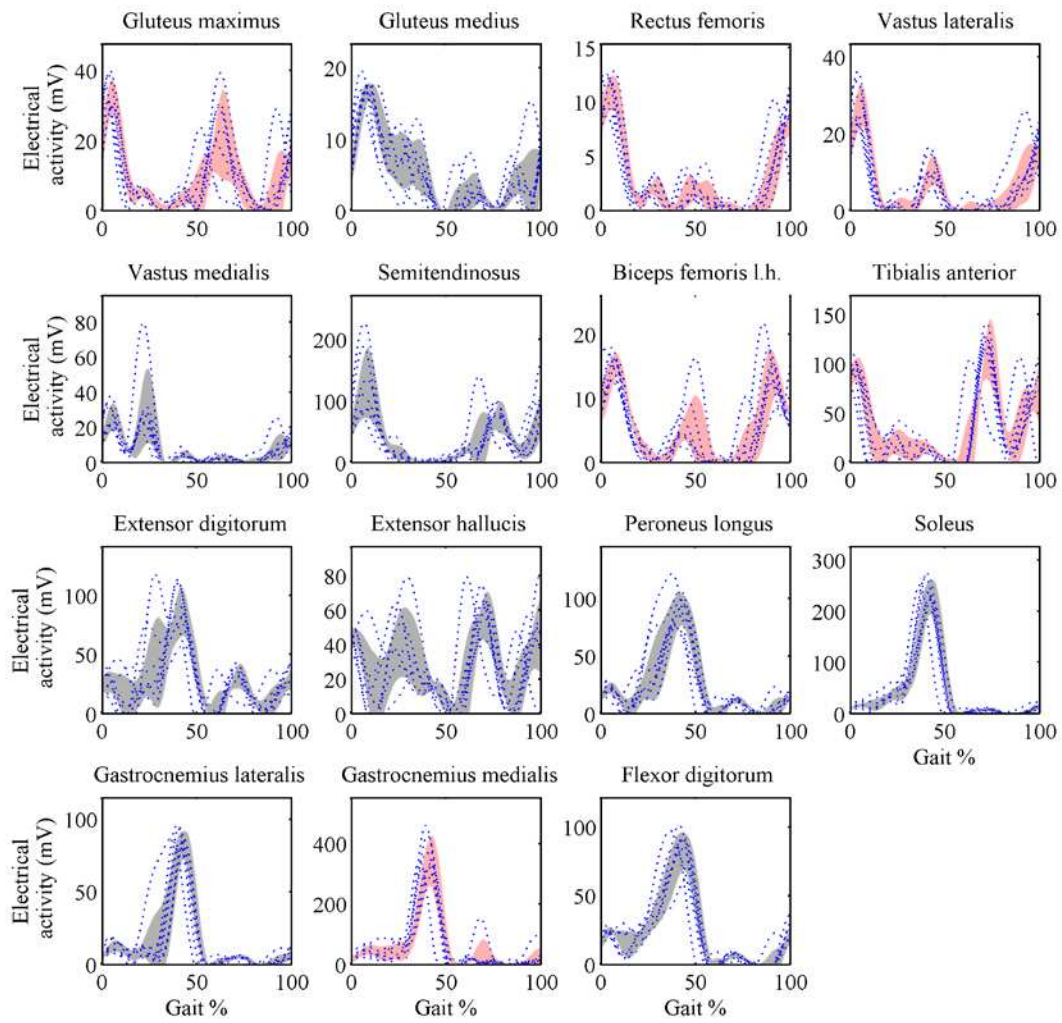
603 Figure 7



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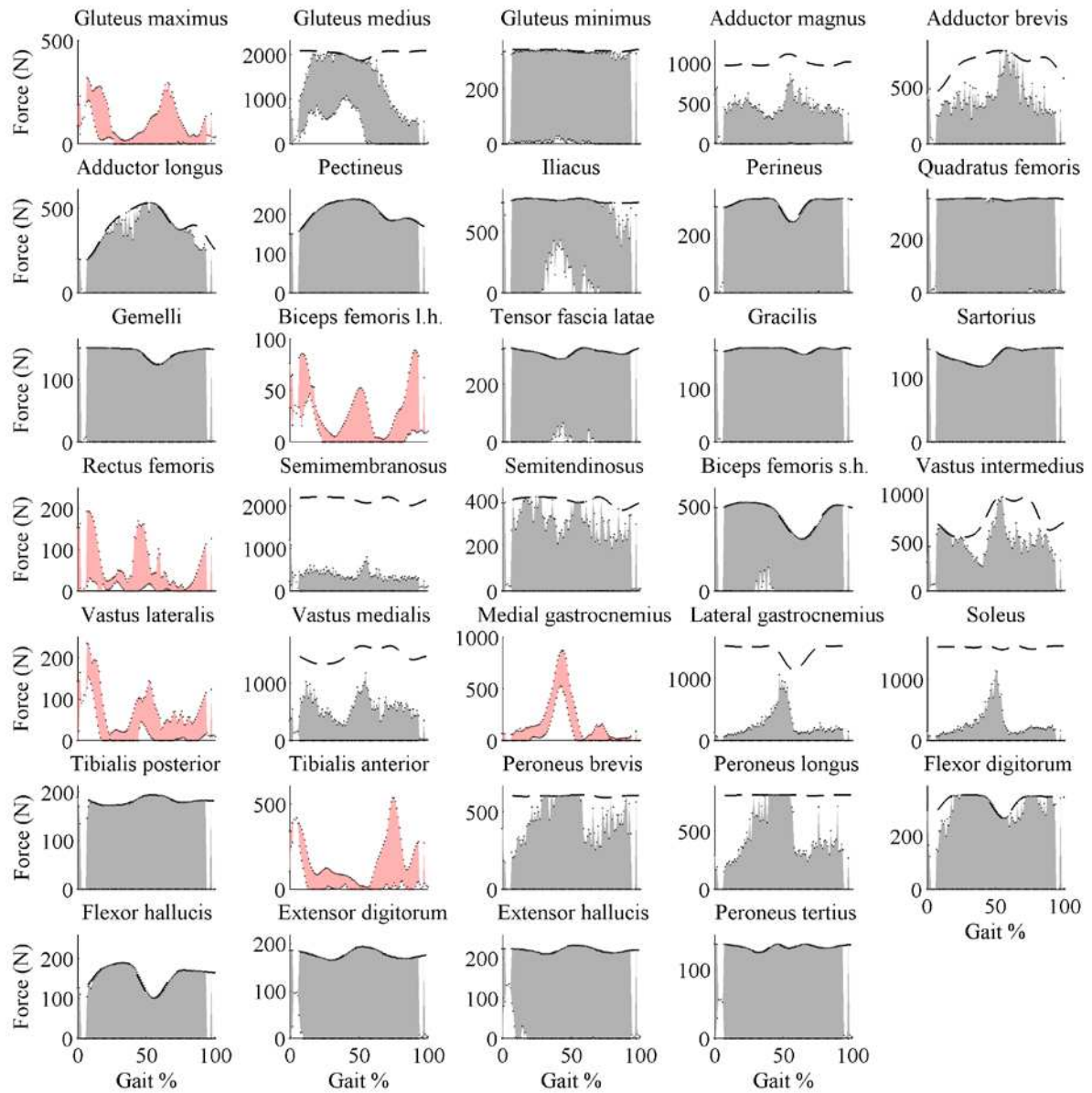
606 Figure 8



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609 Figure 9



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