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Structure from Motion Photogrammetry in Physical Geography

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Abstract

Accurate, precise and rapid acquisition of topographic data is fundamental to many sub-disciplines of physical geography. Technological developments over the past few decades have made fully distributed data sets of centimetric resolution and accuracy commonplace; yet the emergence of Structure from Motion (SfM) with Multi-View Stereo (MVS) in recent years has revolutionised three-dimensional topographic surveys in physical geography by democratising data collection and processing. SfM-MVS originates from the fields of computer vision and photogrammetry, requires minimal expensive equipment or specialist expertise, and under certain conditions can produce point clouds of comparable quality to existing survey methods (e.g. Terrestrial Laser Scanning). Consequently, applications of SfM-MVS in physical geography have multiplied rapidly. There are many practical options available to physical geographers when planning a SfM-MVS survey (e.g. platforms, cameras, software); yet, many focused SfM-MVS end-users are uncertain as to the errors associated with each choice and, perhaps most fundamentally, the processes actually taking place as part of the SfM-MVS workflow. This paper details the typical workflow applied by SfM-MVS software packages, reviews practical details of implementing SfM-MVS, combines existing validation studies to assess practically achievable data quality and reviews the range of applications of SfM-MVS in physical geography. The flexibility of the SfM-MVS approach complicates attempts to validate SfM-MVS robustly as each individual

24 validation study will use a different approach (e.g. platform, camera, georeferencing
25 method, etc.). We highlight the need for greater transparency in SfM-MVS processing
26 and enhanced ability to adjust parameters that determine survey quality. Looking
27 forwards, future prospects of SfM-MVS in physical geography are identified through
28 discussion of more recent developments in the fields of image analysis and computer
29 vision.

30

31 **Keywords**

32 Structure from Motion, Multi View Stereo, topographic survey, point cloud

33

34 **I Introduction**

35

36 Over the past few decades advances in surveying technology have revolutionised our
37 ability to record and characterise the Earth's surface quantitatively: a fundamental
38 requirement of physical geography. Differential Global Positioning Systems (dGPS) and
39 Total Stations (TS) have enabled 3D positioning of observations to millimetre-scale
40 accuracy. More recently, Airborne Laser Scanning (ALS) and Terrestrial Laser Scanning
41 (TLS) have increased the spatial coverage and density of available datasets through
42 non-selective sampling of millions or even billions of survey points to produce 3D point
43 clouds. The impact on the study of physical geography and geomorphology in
44 particular is well documented (Tarolli, 2014). Yet, a limitation to the more widespread
45 uptake of ALS and TLS is the capital outlay and expertise required to acquire and
46 operate these complex instruments.

47

48 In the past few years, Structure from Motion (SfM) has been demonstrated to have the
49 potential to democratise 3D topographic survey by offering rapid 3D point cloud
50 acquisition for minimal expense. Geomorphologists, and physical geographers more
51 generally, have been quick to adopt SfM as seen by the recent and increasing
52 proliferation of studies utilising and testing SfM (e.g. James and Robson, 2012;
53 Westoby et al., 2012). SfM has been applied to a wide range of environmental
54 problems, including monitoring glacier movement (Immerzeel et al., 2014; Ryan et al.,
55 2015), quantifying soil loss and gully erosion (Eltner et al., 2014; Frankl et al., 2015),
56 observing and tracking lava movement (Tuffen et al., 2013) and landslide displacement
57 (Lucieer et al., 2013), monitoring coastal recession (James and Robson, 2012),
58 surveying fluvial morphology (Javernick et al., 2014) including submerged surfaces
59 (Woodget et al., 2014), characterising rock outcrops (Favalli et al., 2012) and
60 quantifying aboveground forest biomass (Dandois and Ellis, 2013).

61

62 At this point, it is instructive to define what is meant by 'SfM'. Strictly speaking,
63 Structure from Motion refers to only one element of the SfM workflow. Although
64 there are cases where a SfM-derived point cloud is seen as the end-product (Dandois
65 and Ellis, 2010; Fonstad et al., 2013) the majority of studies then implement Multi-
66 View Stereo (MVS) photogrammetry algorithms to increase the point density by
67 several orders of magnitude. As a result, the combined workflow is more correctly
68 referred to as 'SfM-MVS'.

69

70 To date there is no comprehensive synthesis of the practical options available to
71 physical geographers when planning an SfM survey, errors to be expected from each
72 choice and, perhaps most fundamentally, the underlying processes actually taking
73 place as part of the SfM workflow. In this paper we provide a qualitative comparison of
74 SfM-MVS with other field topographic survey techniques. We detail the origin of SfM-
75 MVS and the workflow applied by many SfM-MVS software packages (Section III) and
76 review the practical details of implementing SfM-MVS by outlining a number of choices
77 (e.g. camera, survey platform, SfM software) to be made by the user (Section IV). Here
78 we provide specific guidance on data acquisition for SfM-MVs users in physical
79 geography. Existing validation approaches are synthesised (Section V) to provide an
80 overview of the achievable quality of the resulting point clouds. We summarise a range
81 of applications of SfM-MVS in physical geography (Section VI) and consider briefly
82 potential future directions and opportunities for SfM-MVS to make important
83 contributions to the discipline (Section VII).

84

85 **II The place of SfM in topographic survey**

86

87 In recent decades there has been a gradual increase in our ability to collect
88 topographic survey data, from 10^1 - 10^2 measurements per day with a traditional optical
89 level, increasing to 10^3 - 10^4 with dGPS and to $\gg 10^6$ measurements per day with laser
90 scanning technology. Improvements in precision and accuracy have been notable, but
91 more modest. Each new development has required new technology that is typically
92 very costly (often $>£10,000$); conversely, SfM-MVS can offer similar data quality to high

93 resolution survey techniques at minimal expense. A broad comparison of SfM-MVS
94 with existing survey techniques is summarised in Figure 1.

95

96 Total Station (TS) or Electronic Distance Measurement (EDM) surveys offer high-
97 accuracy point data (~mm 3D accuracy) of the ground surface (Milne and Sear, 1997;
98 Fuller et al., 2003). Where local benchmarks or ground control is available, real-world
99 co-ordinates can be provided, even in conditions where sky-view is limited as no
100 communication with satellites is required. They are typically used in conjunction with a
101 pole-mounted prism or can be used without a reflector. TS points are sampled
102 selectively by the operator(s) and can be strategically positioned to identify notable
103 breaks of slope, providing a high-quality Digital Elevation Model (DEM) for relatively
104 small file sizes. The main disadvantage of TS surveys is the point density achievable
105 within a survey campaign which is limited by the time required to sample points
106 individually. Moreover, the expert judgment of where to locate each survey point may
107 introduce bias towards accessible locations and variability between operators (Bangen
108 et al., 2014a). Such bias is significant because the interpolation that is required to
109 produce a topographic model is affected by the specific survey point geometry.

110

111 Data provided by dGPS surveys can be of similar accuracy to that of TS surveys (Bangen
112 et al., 2014b), depending on the length of time a point is occupied and survey mode.
113 Real-time kinetic (RTK) surveys are commonplace in physical geography where a direct
114 radio or GSM (mobile network) link between a surveyor and a base station can provide
115 the surveyor with information on the final accuracy of the solution relative to the base

116 station coordinates (Brasington et al., 2000; 2003; Wheaton et al., 2010). As such,
117 dGPS surveys are subject to many of the same advantages (accuracy, precision,
118 selectivity) and disadvantages (low point density) as TS surveys (Bangen et al., 2014b).
119 The accuracy of RTK-dGPS surveys is ~cm scale (higher accuracies can be achieved on
120 continuously logging static mode) and is dependent on the number and geometry of
121 satellites used to compute a point, therefore a clear sky-view is also required.
122 However, unlike TS surveys, a direct line-of-sight between the instrument and the
123 survey pole is not required.

124

125 Airborne laser scanning (ALS), also known as airborne Light Detection And Ranging
126 (LiDAR), has become a well-established survey tool in physical geography over the last
127 two decades (e.g. Charlton et al., 2003; Evans and Lindsay, 2010; Thommeret et al.,
128 2010). The remote platform and consequent large survey range (typically 100 – 4000 m
129 between the sensor and object of interest; Gallay, 2013) means that ALS is naturally
130 suited to landscape scale surveys, resulting in decimetre scale point resolution and
131 accuracy (Gallay, 2013; Bangen et al., 2014b). Terrestrial laser scanners (TLS) comprise
132 essentially the same technology mounted statically on a conventional survey tripod
133 (Hetherington et al., 2005; Brasington et al., 2012) (though mobile systems are also in
134 use; Alho et al., 2009). The shorter range and static setup of TLS means that mm-scale
135 precision and accuracy can be achieved. The main advantage of LiDAR systems is the
136 acquisition rate, which can be up to hundreds of thousands of points per second.
137 While TLS offers much higher survey accuracy and point density than ALS, this comes
138 at the expense of reduced survey area. Moreover, both ALS and TLS are expensive

139 survey solutions (>£30,000 for a TLS) that produce large quantities of data which must
140 then be decimated to produce useful terrain products. Another disadvantage of TLS is
141 portability; while the TLS instruments themselves typically weigh 5-10 kg, they require
142 much ancillary equipment (e.g. tripods, batteries, cases, targets) and the total weight
143 of many systems restricts their application to areas with good access. Where targets
144 are used to register multiple scans together, surveys must be planned carefully such
145 that they can be viewed from multiple scan locations. Time-limitations determine the
146 number of tripod setups possible meaning that gaps or shadows may be present in the
147 final point cloud owing to occlusion effects. Hand-held mobile laser scanners have
148 been recently used to overcome the limited portability of tripod-mounted TLS (James
149 and Quinton, 2014), though reported errors are centimetre-scale.

150

151 Conventional photogrammetry is the closest existing technique to SfM-MVS, and has
152 contributed much to the workflow of SfM-MVS (Micheletti et al., 2015). Conventional
153 photogrammetry uses precise knowledge of the 3D location and pose of cameras, or
154 the 3D location of a set of control points located in the scene of interest, to
155 reconstruct scene geometry. Achievable spatial resolution is a function of the pixel size
156 but digital photogrammetry has been applied across a range of scales from plots of
157 $\sim 10^1 \text{ m}^2$ (Butler et al. 2002; Carbonneau et al., 2003) to landscapes or river reaches of
158 $>10^6 \text{ m}^2$ (Lane, 2000; Westaway et al., 2000). For photogrammetry, once equipment
159 has been set-up, data collection requires only several minutes. While vertical
160 (overhead) photographs are required in conventional approaches, oblique images can
161 be used either through the implementation of rotation matrices (Chandler, 1999) or by

162 using more recent photogrammetric software capable of processing oblique images
163 (James et al., 2006). Fine resolution and accurate (mm-scale) topography can be
164 obtained at ranges of several metres; the achievable accuracy is reduced with
165 increasing distance between the camera and object of interest. However, the main
166 disadvantages of conventional photogrammetry are the degree of expertise required,
167 the difficulty and expense of obtaining the large amount of *a-priori* information
168 required and the relative inflexibility of the image geometry (e.g. degree of overlap)
169 which may render it unsuitable for some applications.

170

171 SfM-MVS is a non-selective survey method (like ALS, TLS, and conventional
172 photogrammetry where each data point is not selected for inclusion in the survey
173 individually by the surveyor) and the resulting data are most similar to those of TLS.
174 Similar (or greater) point densities can be achieved and while point precision and
175 accuracy is mostly determined by survey range, sub-cm scale errors are achievable
176 (Smith and Vericat, 2015). Perhaps the biggest disadvantage of SfM-MVS is the fact
177 that the quality of the resulting surface model depends on many different factors
178 related to an individual survey. SfM-MVS data are typically not as precise as TLS-
179 derived point clouds; however, SfM-MVS is flexible enough to be applied at a wide
180 range of scales. Specifically, to date, it has been used over survey areas from $10^{-2} - 10^6$
181 m^2 (Smith and Vericat, 2015) and was even used by Dietrich (2015) to survey
182 downstream morphological patterns in a 32 km river reach. The equipment needed for
183 SfM-MVS is often portable and while scale can be provided using only non-specialist
184 technology (e.g. standard laser rangefinders), accurate scaling and georeferencing

185 requires the use of a TS or dGPS. Occlusion and shadowing remain an issue with SfM-
186 MVS, but it is minimised relative to TLS surveys owing to the greater number of
187 viewpoints that can be integrated into a single SfM-MVS survey.

188

189 It is clear that each of the techniques outlined above has different strengths and
190 weaknesses and is better suited to different tasks. Certainly, SfM-MVS is not a
191 complete substitute for these other methods (for example, accurate fluvial bathymetry
192 over small areas is better obtained by total station or dGPS survey than SfM-MVS;
193 Bangen et al., 2014b; Woodget et al., 2014). However, in some circumstances,
194 particularly where plot scale ($\sim 10^1 \text{ m}^2$) data is required (Smith and Vericat, 2015) or
195 where decimetre scale accuracy is acceptable over $\sim 1 \text{ km}^2$ of bare ground (Javernick et
196 al., 2014) SfM-MVS is an efficient and cost-effective survey method.

197

198 **III Principles underlying SfM-MVS**

199

200 The clear similarities between conventional photogrammetry and SfM-MVS may lead
201 to the assumption that SfM-MVS is simply an incremental development in
202 photogrammetry. However, several aspects of SfM-MVS have a different origin
203 entirely, stemming instead from advances in 3D computer vision algorithms.
204 Nonetheless, photogrammetric principles and techniques are embedded in the SfM-
205 MVS workflow (see Michelletti et al., 2015). The typical workflow implemented by
206 many SfM-MVS software packages is presented and summarised in Figure 2. The
207 specifics of this workflow will vary from one software package to another but there

208 exists a clear commonality. The description here is predominantly qualitative to best
209 communicate a technical workflow to a broad audience. Interested readers are
210 directed to other sources (Triggs et al., 2000; Hartley and Zisserman, 2003; Lowe,
211 2004; Snavely, 2008; Szeliski, 2011) for specific details of the mathematical operations
212 applied.

213

214 *1 Feature Detection*

215

216 With a set of images of a scene taken from multiple viewpoints, the first step is to
217 identify features (or ‘keypoints’) in each image and assign a unique identifier to these
218 regardless of the image perspective or scale. To be most useful for SfM-MVS this
219 keypoint identification should be valid for images taken at relatively wide baselines
220 (i.e. different perspectives). Identification of sets of pixels that are invariant to changes
221 in scale and orientation and suitable for wide-baseline matching has been a
222 longstanding question in computer vision (Szeliski, 2011). Popular feature detection
223 algorithms improve on traditional correlation-based approaches as they geometrically
224 normalize the region containing the feature and correct for photometric distortions
225 (e.g. illumination) to ensure rotational and photometric invariance (Mikolajczyk *et al.*,
226 2005). While there are several alternative methods for identifying features (including
227 SURF (Bay et al., 2008), ASIFT (Morel and Yu, 2009), BRIEF (Calonder et al., 2010) and
228 LDAHash (Strecha et al., 2012), the Scale Invariant Feature Transform (SIFT) object
229 recognition system is used most widely in SfM (Lowe, 1999; 2001; 2004) and has been
230 shown by Lowe (2004) to perform well for changes in viewpoint of $<40^\circ$.

231

232 *2 Keypoint Correspondence*

233

234 The next step requires the identification of correspondences between keypoints in
235 multiple images. Of course, there is no guarantee that each keypoint will be
236 represented in each image, so a threshold to identify matches is applied. Descriptors
237 are typically complex (for example, the SIFT descriptor uses 128-vectors to describe
238 each point). The ratio of the Euclidean distance of the nearest neighbour with that of
239 the second nearest is termed the 'distance ratio' and a minimum value (typically 0.6-
240 0.8; Snavely et al., 2008) is specified to increase the chance of all remaining matches
241 being correctly identified. In such high-dimensional space a brute-force Euclidean
242 nearest-neighbour search is computationally demanding (Arya et al., 1998). k -
243 dimensional trees (or k - d trees) modified for approximate matching (Muja and Lowe,
244 2009) are applied as an efficient and approximate solution to this problem. These
245 binary trees partition multidimensional data to quickly eliminate large search spaces
246 (Bentley, 1975; Friedman et al., 1977). The Approximate Nearest Neighbour (ANN)
247 solution permits relative error in the identification of the nearest neighbour (Arya et
248 al., 1998) and by searching only the top ranked candidates can make substantial time
249 savings.

250

251 *3 Identifying Geometrically Consistent Matches*

252

253 A further filter of keypoint correspondences is then applied to try and identify and
254 remove any remaining erroneous matches. Taking any image pair with multiple
255 common keypoints, the fundamental matrix (F-matrix) can be calculated using the
256 Eight-point algorithm (Longuet-Higgins, 1979). The F-matrix specifies the relationship
257 between the two images and reconstructs the scene up to a projective transformation
258 where all points lying on a single line will remain aligned in this way (i.e. 'collinearity' is
259 preserved). Candidate F-matrices are evaluated using the RANdom SAMple Consensus
260 (RANSAC) method (Fischer and Bolles, 1981) in which keypoints used in the
261 construction of the F-matrix are randomly sampled and the difference between the
262 returned F-matrix and that returned by other sampled keypoints is computed. Beyond
263 a threshold the keypoint is considered an 'outlier' and not part of the model fit.
264 Sampling is repeated on different subsets until there is a 95% chance that the subset
265 contains only 'inliers' for which the F-matrix is returned. After further refinement, all
266 'outlier' matches are removed. Other similar 'hypothesise-and-test' frameworks may
267 be implemented at this stage such as the Maximum Likelihood Estimation Sample
268 Consensus (Torr and Zisserman, 2000) or the Hough transform (Ballard and Brown,
269 1982).

270

271 *4 Structure from Motion*

272

273 From the geometrically correct feature correspondences, Structure from Motion uses
274 bundle adjustment algorithms to simultaneously estimate the 3D geometry (or
275 structure) of a scene, the different camera poses (extrinsic calibration) and the camera

276 intrinsic parameters (intrinsic calibration) (Ullman, 1979). Whereas conventional
277 photogrammetric techniques share this step, they often require separate camera
278 calibration. Where such camera calibration is unavailable, SfM uses both EXIF tags in
279 the images and the redundancy provided by the large number of images and keypoint
280 correspondences to estimate the intrinsic camera parameters that define the camera
281 calibration matrix (e.g. skew, focal length, principal point and often radial distortion
282 parameters). By minimizing a cost function, bundle adjustment results in *jointly*
283 *optimal* 3D structure and camera parameters (see Granshaw (1980) and Triggs et al.
284 (2000) for detailed reviews). Here, ‘bundle’ refers to the bundles of light rays
285 connecting camera centres to 3D points, and ‘adjustment’ refers to the minimisation of
286 a non-linear cost function that reflects the measurement error (Szeliski, 2011). This
287 error term can incorporate many sources of information including errors in the
288 projection of individual image features in the object space (re-projection errors).

289

290 Parameter values must be assigned initial values before a non-linear parameter
291 optimisation of the bundle adjustment is calculated. Sequential methods take an initial
292 pair of images which typically exhibit many common keypoints and a wide baseline
293 and initialize the camera intrinsic parameters from EXIF tags and use the Five-point
294 algorithm (Nistér, 2004) to estimate the F-matrix. Incorrectly specified initial
295 parameters for an image can yield an optimisation to a local minima instead of the
296 ‘correct’ solution and cause that image to be rejected from the project. Tracks
297 between keypoints are then triangulated to give initial estimates of feature positions
298 (see Hartley and Sturm, 1997). Errors between the projections of each track and the

299 corresponding keypoints are minimized as part of a two-frame bundle adjustment. The
300 camera containing the largest number of tracks whose 3D locations are already known
301 is then selected and added into the optimization. Using these known 3D locations the
302 2D co-ordinates of the new image are mapped into the 3D object space and the
303 intrinsic camera parameters estimated. In many SfM implementations, a further
304 bundle adjustment is run with only the new parameters permitted to change. At each
305 stage keypoints with a high re-projection error are removed. With each image added
306 sequentially, a global bundle adjustment is then performed to refine the entire model.

307

308 *5 Scale and Georeferencing*

309

310 The output of the SfM stage is a sparse unscaled 3D point cloud in arbitrary units along
311 with camera models and poses. A minimum of three Ground Control Points (GCPs)
312 with XYZ coordinates are required to scale and georeference the SfM-derived point
313 cloud using a seven parameter linear similarity transformation; i.e. three global
314 translation parameters, three rotation parameters and one scaling parameter (Dandois
315 and Ellis, 2010; James and Robson, 2012). Unlike conventional photogrammetry, each
316 photograph does not need to contain visible GCPs. dGPS or TS surveys can provide the
317 co-ordinates of targets clearly visible in the imagery. A much larger number of targets
318 than three is recommended; the minimum absolute number depends on the size of
319 the survey area, but they should cover the whole extent of this area (Javernick et al.,
320 2014; Smith et al., 2014) and be well distributed throughout the area (James and
321 Robson, 2012). Alternatively, 'direct' georeferencing and scaling can be performed

322 from known camera positions derived from RTK-GPS measurements and an Inertial
323 Measurement Unit (Tsai et al., 2010; Turner et al., 2014). A common hybrid of the two
324 georeferencing approaches uses direct georeferencing to provide approximate camera
325 locations to initialize the bundle adjustment and then uses external GCPs to better
326 constrain the solution (e.g. Ryan et al., 2015; Rippin et al., 2015).

327

328 *6 Refinement of Parameter Values*

329

330 The identification of GCPs and input of their co-ordinates in the preceding step
331 provides additional information of the 3D geometry that can be used to further refine
332 intrinsic camera parameter estimates and reconstructed scene geometry. The known
333 co-ordinates (and estimates of point error) provide an additional source of error in the
334 minimization of the non-linear cost function during the bundle adjustment step. With
335 this external information included in the model, the bundle adjustment can be re-run
336 to optimize the image alignment in light of this new information, by minimizing the
337 sum of the reprojection error and the georeferencing error. The spatial distribution of
338 GCPs throughout the survey area is critical for this process to be effective.

339

340 *7 Multi-View Stereo Image Matching Algorithms*

341

342 The final step in the workflow is the application of Multi-View Stereo (MVS) algorithms
343 to the already scaled and georeferenced sparse point cloud and camera parameters.
344 MVS usually increases the density of the point cloud by at least two orders of

345 magnitude. As detailed by Seitz et al. (2006), there are a wide variety of MVS
346 algorithms which can be classified into: (i) Voxel-based methods which are 3D grids
347 that are occupied to define the scene; e.g. Seitz and Dyer (1999); (ii) Surface evolution-
348 based methods that use iteratively evolved polygonal meshes; e.g. Furukawa and
349 Ponce (2009); (iii) Depth-map merging methods where individual depth maps (showing
350 the distance between the camera viewpoint to the 3D scene objects) are combined
351 into a single model; e.g. Li et al. (2010a); and (iv) Patch-based methods where
352 collections of small patches or surfels represent the scene; e.g. Lhuillier and Quan
353 (2005). A commonly applied method in physical geography applications is the patch-
354 based MVS (PMVS) algorithm of Furukawa and Ponce (2010); in comparisons against
355 other MVS algorithms (Ahmadabadian et al., 2013) this MVS method performs well. In
356 general, PMVS matching of features requires reliable texture information, the lack of
357 which may result in gaps in the final model. Once matched, patches are then grown
358 around identified matches. By accounting for occlusion in the model, visibility
359 constraints are then used to filter out outlier patches.

360

361 As the final step of MVS is computationally burdensome when a global reconstruction
362 is specified (Pons et al., 2007), there is the option to split a project into overlapping
363 clusters of images to reduce RAM (Random-Access Memory) requirements. Each
364 cluster is then run through the dense MVS reconstruction separately. Furukawa et al.
365 (2010) detail such an image clustering method known as Clustering Views for Multi-
366 View Stereo (CMVS). As demonstrated for a physical geography application of SfM-
367 MVS by Dietrich (2015), the addition of an image clustering step improves the

368 scalability of MVS, permitting much larger numbers of images to be processed within
369 any given run time.

370

371 Throughout Steps 1-7 above, thresholds and parameters are used to distinguish
372 correct matches from incorrect matches and prevent the excessive computational
373 burden that would be required for exhaustive Nearest Neighbour searches in the
374 matching of keypoints in each image. The specific values will be variable between
375 different SfM-MVS packages. A typical SfM-user may not be able to adjust these
376 values, may be unaware of this, or may simply adjust a qualitative global accuracy
377 setting implemented within particular SfM software packages, or use default values.
378 Moving beyond such a 'black box' approach, an understanding of the full SfM-MVS
379 workflow implemented is useful for physical geographers to identify and minimize
380 potential sources of error in the resulting topographic data.

381

382 **IV SfM in practice**

383

384 The flexibility of the SfM-approach is advantageous considering the range of problems
385 in physical geography to which it can be applied. However, one consequence of this
386 flexibility is that practitioners are faced with many choices in the design and
387 implementation of a SfM-MVS survey.

388

389 *1 Platforms*

390

391 Most imagery can be used for SfM-MVS; indeed the SfM package outlined in Snavely et
392 al. (2008) was designed to use collections of independent images extracted from image
393 searches on the internet. A range of options are available, from ground-based imagery
394 to fully airborne solutions (Figure 3). In general, there are trade-offs between: (i) pixel
395 resolution; (ii) spatial coverage; (iii) image quality; and (iv) cost-effectiveness.

396

397 Hand-held ground-based solutions are the most inexpensive option (only a camera and
398 georeferencing method is needed), can provide excellent pixel resolution and image
399 quality and are easy to implement. The key disadvantage of hand-held solutions is that
400 they are typically limited to the plot-scale ($\sim 10^1 \text{ m}^2$). However, with high relief (e.g. an
401 incised valley or cliffs) areas approaching one hectare can be surveyed from the
402 ground (James and Quinton, 2014; Smith et al., 2014; Micheletti et al., 2014). Matching
403 of oblique ground-based images over large areas can be unreliable on relatively flat
404 terrain; isolated mismatched areas are apparent in the final point clouds which must
405 be inspected carefully (Smith and Vericat, 2015). Extendable masts, booms (Figure 3d)
406 or mobile inspection poles can be used to raise a camera up to 20 m above ground to
407 reduce the likelihood of such mismatches by gaining a more advantageous viewpoint.
408 However, on-the-ground image swaths are still limited in spatial extent and retaining
409 stability of a pole or mast in adverse weather can be challenging.

410

411 Lighter-than-air blimps (Figure 3a) can raise a camera higher still, up to 500 m, though
412 they can become difficult to position if the wind speed exceeds $\sim 15 \text{ km h}^{-1}$ (Verhoeven
413 et al., 2009). Mobile blimp systems are a low-cost solution (Vericat et al., 2009) but are

414 limited in their payload capability, constrained to operating loads of between 0.25-0.5
415 kg per 1 m³ of lighter-than-air gas. They also cannot be deployed in high winds and
416 may require a local source of suitable gas. Conversely, kites (Figure 3b) can carry a
417 payload of several kilograms. Irregular or light winds can make controlling kite-based
418 systems challenging; thus, some systems integrate blimp and kite components to
419 improve the range of suitable weather conditions.

420

421 There has been a proliferation in low-cost airborne platforms in recent years;
422 Unmanned Aerial Vehicles (UAVs) have been used extensively for acquisition of SfM-
423 MVS imagery (e.g. Woodget et al., 2014; Lucieer et al., 2014; Tonkin et al., 2014).
424 There exists a wide range of UAVs (see Colomina and Molina, 2014) from self-
425 propelled fixed-wing aircraft to airships. The most popular UAVs have been so-called
426 'multicopters' (including quadcopters, hexacopters, or octocopters; Figure 3c) because
427 of their ease of operation, stability in most weather conditions and recent decline in
428 financial cost. Most multicopters can take a payload of several kilograms, though larger
429 systems may take up to 10 kg (Lejot et al., 2007). Flight control software and units can
430 allow pre-programmed routes to be followed (Oúedraogo et al., 2014). On smaller
431 UAVs, image quality can be compromised by blurring from vibrations (Dunford et al.,
432 2009), although use of a gimbaled-camera mount can minimise this problem. In many
433 countries legislation limits the range and ground-type over which UAVs can be flown.
434 In general, UAVs have a lower maximum altitude than blimps or kites. In each case, the
435 flying altitude chosen will determine the final pixel resolution for a specific camera.

436

437 The broadest spatial coverage can be achieved with a commissioned, piloted overflight
438 in an aircraft, often a helicopter (Javernick et al., 2014; Dietrich, 2015). This removes
439 maximum altitude restrictions (though minimum altitude restrictions apply) and
440 permits a greater flexibility and responsiveness in the survey to ensure full coverage.
441 As with UAVs, higher altitude surveys will improve spatial coverage at the expense of
442 pixel resolution. Issues with vibrations and blurring are circumvented when images are
443 taken manually, though this is not always possible. Cost is a disadvantage of the
444 piloted helicopter approach. Much smaller light aircraft (James and Varley, 2012),
445 microlites (James and Robson (2012) with images from Cecchi et al. (2003)) or piloted
446 gyrocopters (Smith and Vericat, 2015; Figure 3e) offer a more cost-effective solution
447 and can be hired for <£200 per hour.

448

449 *2 Sensors*

450

451 Images for SfM-MVS can be acquired from almost any camera system; and
452 consequently there is a spectrum of image quality. At the lower quality end are still
453 frames extracted from video. Lower pixel counts, blurring, camera lens and image
454 stability issues mean that still frames captured from video produce poor quality 3D
455 data (Thoenig et al., 2014). Where sensors employ a rolling shutter (e.g. GoPro
456 cameras), not all parts of the resulting images are recorded at the same instant which
457 is a problem for SfM-MVS analysis when the sensor is mounted on a moving platform.

458

459 However, comparisons between simple low-cost cameras (such as those embedded in
460 Smart Phones or compact cameras) and expensive digital SLRs, do not show significant
461 differences in point cloud quality at short ranges (Thoeni et al., 2014; Micheletti et al.,
462 2014). Intrinsic camera parameters are most easily defined for wide-angle lenses
463 (equating to around 35 mm on a traditional SLR) whereas those with longer lenses
464 (>55 mm) or fish-eye lenses require bespoke calibration models (Micusik and Pajdla,
465 2006). Image resolution and sharpness becomes more important at longer survey
466 ranges, i.e. >100 m. Cameras with larger imaging sensors are advantageous for high-
467 altitude aerial imagery, providing a better dynamic range, finer detail and less noise
468 (Cramer, 2004). Moreover, larger sensors (e.g. Full Frame 35 mm format) capture
469 larger image areas at a given focal length, increasing on-the-ground image swaths. The
470 camera platform must be considered as camera size and weight will be of importance
471 for some aerial platforms. Where the operator is not physically present to capture the
472 images manually, a triggering mechanism is required which can be achieved with
473 remote shutter releases (wired/wireless) or intervalometers (internal/external) (e.g.
474 Vericat et al., 2009). For longer-term deployment, arrays of inexpensive trail cameras
475 can be installed to obtain regular synchronised images of a scene (James and Robson,
476 2014) (Figure 3f).

477

478 *3 Data Acquisition*

479

480 When acquiring images for SfM-MVS, the main goal is to capture the scene of interest
481 from as many different viewpoints as possible. Advice on SfM-MVS image acquisition

482 for specific applications is given in several papers, including Favalli et al. (2012); James
483 and Robson (2012); Westoby et al. (2012); Bemis et al. (2014); Micheletti et al. (2014);
484 Smith et al., (2014) and Stumpf et al. (2015). In summary, the following practical
485 guidance should assist the planning of SfM-MVS data acquisition:

- 486 • Full 360° coverage is ideal (Westoby et al., 2012), though not always necessary
487 so long as all surfaces of interest are visible in multiple photographs.
- 488 • While SfM can sometimes work with 2 input images (James and Robson,
489 2014b), a much larger number of images is recommended. While the exact
490 number will depend on the scene size and complexity, tens to hundreds of
491 pictures are often used (Favalli et al., 2012).
- 492 • Higher quality input images can result in higher quality model output (Bemis et
493 al., 2014); however, large images may need to be re-sized to reduce processing
494 times (Westoby et al., 2012).
- 495 • Overlap between images is best considered in terms of both coverage and
496 angular change as multiple images taken of a surface from the same camera
497 location do not aid the reconstruction (Favalli et al., 2012).
- 498 • Angular changes of >25-30° between adjacent camera locations should be
499 avoided because identification of correct keypoint correspondence is limited
500 for larger changes of perspective (Moreels and Perona, 2007). Maximum
501 angular changes of 10-20° are advisable (Bemis et al., 2014).
- 502 • Each point on the surface must be visible in at least two images, but again,
503 more is clearly preferable to ensure that all locations are reconstructed
504 successfully.

- 505 • Large jumps in image scale are best avoided (i.e. avoid mixing close up imagery
506 with that taken from a large range without also including intermediate scale
507 imagery) as image textures will appear differently at different scales and
508 prevent accurate matching (Bemis et al., 2014).
- 509 • Avoid using zoom lenses and changing focal lengths; while not essential,
510 keeping camera parameters constant can aid the bundle adjustment in some
511 SfM-MVS packages.
- 512 • The interval between images should be minimised as changes to lighting
513 conditions and shadow locations will interfere with keypoint matching (James
514 and Robson, 2012).
- 515 • Mobile elements in a scene should be avoided as keypoint matching algorithms
516 rely on a static scene. Where flexible vegetation or other dynamic elements are
517 present, this may be challenging, especially in shifting winds (Bemis et al.,
518 2014). Components of the mobile camera platform (e.g. helicopter skids, kite
519 tethers) or the camera operator (i.e. feet) should be avoided for the same
520 reason.
- 521 • Scenes devoid of distinct features (e.g. smooth ice surfaces) will be challenging
522 and often produce fewer keypoint correspondences and lower point densities
523 (Westoby et al., 2012).
- 524 • Shiny or reflective surfaces are similarly unsuitable for SfM-MVS as their
525 apparent features change with camera position.
- 526 • Where exclusively vertical imagery is collected, a doming effect can be
527 observed (Rosnell and Honkavaara, 2012; Oúedraogo et al., 2014) as a result of

528 incorrect specification or determination of the camera intrinsic parameters.
529 Taking slightly off-vertical convergent imagery and designing a distributed
530 network of ground control points can partially correct this doming (James and
531 Robson, 2014a; Smith and Vericat, 2015).

532 • The maximum number of images for SfM-MVS analysis will be determined by
533 logistical and computational capabilities. With increasing image numbers, gains
534 from adding further imagery are reduced substantially as the percentage of
535 surface points that are already visible in three or more images increases,
536 though this depends on the geometric arrangement of the image set as a
537 whole.

538

539 For scaling and georeferencing, clearly visible targets (GCPs) are required that can be
540 identified in the images. The bigger the target, the better it will be seen from a
541 distance, but also the greater the error in defining the exact reference point, which
542 may be located at the centre of such a target. Targets should be placed on stable
543 features, be visible in as many images as possible (certainly a minimum of three
544 images) and be easily distinguishable from the surrounding landscape. There is no
545 requirement for GCPs to be visible in every image used. Distribution of GCPs through
546 the area of interest determines the quality of the final model (James and Robson,
547 2012) and can help to mitigate doming (James and Robson, 2014a); these should
548 ideally cover both the margins and the centre of the scene, covering a good range of
549 values in each spatial dimension. Linear configurations of GCPs should also be avoided.
550 High-quality 3D co-ordinates of these GCP points (from dGPS or TS surveys) are

551 preferable. Alternatively, co-ordinates of camera positions derived from RTK-GPS
552 measurements and an Inertial Measurement Unit can be used to directly georeference
553 SfM-MVS point clouds (Turner et al., 2014).

554

555 *4 Software*

556

557 A number of SfM-MVS packages exist, ranging from web-based services to open-
558 source and commercial software.

559

560 Freely-available web-based services include Autodesk 123DCatch/ReCap
561 (<http://www.123dapp.com/catch>), Microsoft Photosynth (<https://photosynth.net/>)
562 and ARC3D (<http://www.arc3d.be>). Both Photosynth and 123DCatch are available as
563 either mobile application or desktop versions. In all cases, post-processing options are
564 limited and require export to other software for processing, cleaning or editing (e.g.
565 Meshlab, <http://meshlab.sourceforge.net/>). In the case of Photosynth, the generation
566 of dense point clouds requires additional software (e.g. PMVS2, see below). ARC3D is
567 typically used for cultural heritage projects, while both Photosynth (Fonstad et al.,
568 2013; James and Varley, 2012) and 123DCatch (Gómez-Gutiérrez et al., 2014;
569 Micheletti et al., 2014) have been used for physical geography applications.

570

571 Open-source code packages are used regularly for SfM. The combination of Bundler
572 (<http://www.cs.cornell.edu/~snaveley/bundler/>) (Snavely, 2008; Snavely et al., 2008)
573 for sparse cloud generation and Patch-based Multi-View Stereo (PMVS2)

574 (<http://www.di.ens.fr/pmvs/>) (Furukawa and Ponce, 2010) for dense cloud production
575 is a common workflow (James and Robson, 2012). As Bundler does not exploit modern
576 Graphics Processing Units (GPUs) it can be slower than commercially available
577 alternatives. Moreover, designed for web-based photo tourism, it assumes that each
578 image was taken from a different camera and uses a pin-hole camera model which can
579 produce lower accuracy results than with other models (Snavely et al., 2008).
580 VisualSfM (<http://ccwu.me/vsfm/>) combines an SfM algorithm and PMVS (with
581 associated image clustering software CMVS) into a single interface and is
582 computationally faster. MicMac (www.micmac.ign.fr/) also comprises a full SfM-MVS
583 workflow, offering complex models of camera intrinsic parameters. MicMac can
584 include GCP information in the bundle adjustment step and has yielded accurate
585 results (Oúedraogo et al., 2014; Stumpf et al., 2015). Ecosynth (<http://ecosynth.org/>) is
586 another freely-available SfM software used for vegetation mapping (Zahawi et al.,
587 2015).

588

589 The most frequently applied commercially available software package is Agisoft
590 Photoscan (<http://www.agisoft.com/>) which offers a user-friendly solution to SfM-
591 MVS. Educational licenses can be purchased for ~£360. Although post-processing
592 options are currently limited, this has seen widespread application in physical
593 geography (e.g. Javernick et al., 2014; Smith et al., 2014; Leon et al., 2015).
594 Pix4DMapper (<http://pix4d.com/>) is an emerging software used in several soil erosion
595 applications (Eltner et al., 2014; Castillo et al., 2014) and has been shown to perform
596 well on bundle adjustment, but less well on dense matching and orthophoto

597 generation (Unger et al., 2014). Educational licenses can be purchased for ~£1250. Eos
598 PhotoModeler Scanner <http://www.photomodeler.co.uk/> (~£1600) has also been used
599 in physical geography (Irvine-Fynn et al., 2014; Micheletti et al., 2014). Other available
600 commercial software, including Autodesk ImageModeler (supplied free with other
601 Autodesk software purchases) www.autodesk.com/imagemodeler and D-Sculptor
602 (£500) <http://www.d-vw.com/> require some manual feature matching and
603 photogrammetric expertise.

604

605 While many open-source point cloud viewers are available, Meshlab (above) and
606 CloudCompare (<http://www.danielgm.net/cc/>) are used commonly and provide
607 substantial editing and post-processing functionality. Alternatively, SfM-MVS data can
608 be imported into TLS-focused software (e.g. Leica Cyclone; RiSCAN PRO).

609

610 *5 Filtering and Digital Elevation Model (DEM) Generation*

611

612 Distinguishing between ground surface and non-surface points and normalizing the
613 point density is often required for point clouds (Brasington et al., 2012). Extensive
614 software libraries of point filters are available (e.g. the Point Cloud Library
615 www.pointclouds.org); however, the way in which particularly ground-based SfM-MVS
616 data is captured limits the applicability of existing tools developed for ALS data as point
617 densities are much higher and vegetation is captured from a different perspective.
618 Radius-based methods of outlier detection are commonplace (Hodge et al., 2009).
619 Geomorphologists and many other users typically wish to filter out vegetation from

620 the point cloud and focus on the bare ground surface topography (Javernick et al.,
621 2014); conversely, ecologists may wish to focus on the vegetation points alone, to
622 estimate biomass, for example (Zahawi et al., 2015). Classification of vegetation and
623 ground points is more challenging as they may be less easily distinguished. Brodu and
624 Lague (2012) identify such points based on multi-scale dimensionality criteria. Use of
625 colour filters is also possible, as SfM-MVS returns true-coloured points. Intelligent
626 decimation algorithms (e.g. ToPCAT; Brasington et al., 2012; Rychkov et al., 2012)
627 create gridded terrain products at a user-specified grid-scale, also returning sub-grid
628 roughness statistics for each cell. Normalization of point density is a necessary step for
629 the creation of raster-based topographic data products and reduces file sizes markedly
630 as only summary statistics for each grid cell are required and details of individual
631 points are discarded.

632

633 Finally, interpolation algorithms such as Inverse Distance Weighting, Radial Basis
634 Functions or Ordinary Kriging (see Bell, 2012 for a review) are required to fill any gaps
635 in the SfM-MVS-derived model for DEM creation. Commercially-available SfM-MVS
636 software (e.g. Agisoft Photoscan) also offer DEM-creation tools. Development of
637 efficient processing methods to extract the maximum useful data from 3D point clouds
638 remains a research priority, as much essential information of the 3D scene (e.g.
639 multiple elevation values at a single raster cell as seen with overhanging surfaces) is
640 lost in the conversion into rasterised DEMs. In addition, orthophotos can be generated
641 from point cloud data, often by running surfacing algorithms to generate a textured
642 mesh, reprojecting the photographs onto the mesh and viewing the mesh from an

643 orthographic projection. Such orthophotos yield additional information of use to
644 physical geographers in many applications.

645

646 **V Validation of SfM-MVS**

647

648 As with any emerging technology, quantitative validation of SfM-MVS-derived
649 topographic data against those derived from more conventional methods (e.g. TS,
650 dGPS, ALS, TLS) is prerequisite to confident application to a real-world problem. Only
651 TLS and ALS provides directly comparable topographic data, but concurrent data
652 derived using laser scanning is rarely available. Moreover, issues of beam divergence
653 and 'mixed pixels' in laser scan data mean that in some cases there is no *a priori*
654 reason to treat TLS data as the more correct data set, especially where SfM-MVS
655 survey ranges (i.e. object-camera baselines) are short (Smith and Vericat, 2015).

656

657 Numerous studies have validated SfM-MVS-derived data against other methods; we
658 have synthesised them herein to provide a broad overview of the capabilities of SfM-
659 MVS. The dataset is compiled from the findings of Favalli et al. (2012), Harwin and
660 Lucieer (2012), James and Robson (2012), Mancini et al. (2013), James and Quinton
661 (2014), Javernick et al. (2014), Lucieer et al. (2014), Micheletti et al. (2014), Ouédraogo
662 et al. (2014), Ruzic et al. (2014), Smith et al. (2014), Thoeni et al. (2014), Tonkin et al.
663 (2014), Stumpf et al. (2015), Smith and Vericat (2015), subaerial data from Woodget et
664 al. (2014) and an unpublished result by the authors on ice surface plots. The aggregate
665 dataset consisted of 50 data points covering a wide range of survey scales. Most

666 studies reported the vertical Root Mean Squared Error (RMSE), Mean Error (ME) or
667 Mean Absolute Error (MAE). Mean Error values should be treated with caution as
668 positive and negative errors will compensate for each other.

669

670 Three general validation methods have been identified (see Smith and Vericat, 2015):

671 (i) Point-to-Raster (PR), where a SfM-MVS-derived DEM is validated against point data
672 from TS or dGPS (Lucieer et al., 2013; Javernick et al., 2014) and results depend on

673 both the DEM grid-size and location of the validation point relative to the mean
674 elevation within any cell; (ii) Raster-to-Raster (RR), where two separately derived DEMs

675 are compared (Favalli et al., 2012; James and Robson, 2012) and the method of
676 validation-DEM generation must be considered carefully to ensure comparability; and

677 (iii) Point-to-Point (PP), where two point clouds are compared directly (James and
678 Quinton, 2014) and a limiting assumption is that two points would be exactly

679 concordant under error-free conditions. Analysis of the compiled dataset reveals that
680 PP- and RR-type validation typically results in smaller errors than PR-type validation.

681 Smith and Vericat (2015) showed that even at 0.1 m grid sizes, PR-type validation can
682 yield RMSE values ~20% higher than RR-type validation of the same data. This

683 discrepancy is to be expected since RR-type validation compares two rasters that both
684 summarise the topographic variability within a single grid cell statistically, while PR-

685 type validation compares the SfM-MVS-derived raster with a single point
686 measurement taken within that grid cell which will exhibit sub-grid topographic

687 variability. Other validation methods have been described: Favalli et al. (2012) use a
688 mesh-comparison tool (Cignoni et al., 1998) instead of generating raster-based

689 topographic models while Lague et al. (2013) compute surface normals for each point
690 based on all data points within a pre-specified radius to inform the comparison of
691 points (as applied by Stumpf et al., 2015).

692

693 Over half of validation data points (56%) used ground based imagery while the
694 remainder are based on imagery from airborne platforms (including manned and
695 unmanned systems). The reported Root Mean Squared Error (RMSE) is an order of
696 magnitude greater for aerial surveys (0.277 m) than ground-based surveys (0.043 m),
697 but aerial surveys typically cover larger areas with the camera positioned at a greater
698 distance from the object of interest (i.e. a longer survey range). Indeed, the main
699 observable effect on SfM-MVS data quality is a result of survey range (Figure 4). A
700 linear degradation of precision with survey range might be expected from the
701 increased pixel size; James and Robson (2012) observed such a linear relationship
702 between the standard deviation of errors and survey range for three validation studies,
703 estimating a ratio between these values as 1:1000. Yet RMSE is reported more
704 commonly, it integrates all sources of error, and absolute accuracy is often required for
705 monitoring studies. Considering RMSE and survey range, Micheletti et al. (2014)
706 observed a ratio of 1:625. Combining the 43 validation data points that report RMSE
707 our data show a similar median ratio (1:639). A power law better describes the
708 relationship between RMSE and range. The exponent of this relationship (0.88 ; $R^2 =$
709 0.80) is reasonably close to linear (Smith and Vericat, 2015).

710

711 Figure 4 provides a useful indication of errors expected for SfM-MVS surveys at a given
712 range. However, the effect of validation method can be seen with point-to-raster
713 methods exhibiting the highest errors for a given survey range. When survey range is
714 taken into account, there are minimal differences between the accuracy of ground-
715 based and aerial SfM-MVS surveys. Overall, considering the RMSE : range ratio, ~10-15
716 mm errors are achievable at ~10 m survey range suitable for detailed studies, while
717 ~100-200 mm errors are observed from 100 m range which could be applied over
718 much larger areas. Such errors are similar to those expected from ALS surveys (Gallay
719 et al., 2012).

720

721 Several studies included in the above analysis report results using multiple SfM-MVS
722 workflows (e.g. varying cameras or software) on the same image set or area of interest
723 (James and Robson, 2012; Javernick et al., 2014; Micheletti et al., 2014; Ouédraogo et
724 al., 2014; Smith et al., 2014; Thoeni et al. 2014; Smith and Vericat 2015; Stumpf et al.,
725 2015). In each case, the best-performing SfM-MVS-workflow on each image set or area
726 of interest was selected for inclusion in Figure 4. Through comparison of the best-
727 performing workflow with other workflows, these studies yield further insight into the
728 effects of GCP distribution, processing software used and camera used for image
729 acquisition.

730

731 Clearly, the GCP quality will determine overall SfM-MVS survey accuracy. In addition, it
732 is well established that poor GCP distribution has a detrimental effect on survey
733 quality. Javernick et al. (2014) reported an increase in RMSE from 0.23 m to 0.27 m

734 when the study reach was extended beyond the area covered with GCPs. Smith et al.
735 (2014) observed a more pronounced increase (from 0.14 m to 0.47 m). James and
736 Robson (2012) also reported increased survey errors when GCPs were not distributed
737 throughout the survey area.

738

739 In a comparison of SfM-MVS processing software, Micheletti et al. (2014) noted a near-
740 doubling of RMSE when the web-based 123DCatch was used instead of Eos
741 PhotoModeler, though this effect was removed when the point clouds were aligned
742 using an iterative closest point algorithm (Besl and McKay, 1992). Ouédraogo et al.
743 (2014) observed that MicMac performed better than Agisoft in a ploughed agricultural
744 catchment as the more sophisticated camera model reduced the observed doming
745 effect and Stumpf et al. (2015) found that MicMac outperformed VisualSfM for similar
746 reasons. In a comparison of sensors, Thoeni et al. (2014) observed that consumer-
747 grade digital cameras performed similarly to professional grade cameras, though
748 GoPro devices performed less well. Micheletti et al. (2014) found that DSLR imagery
749 and that from a camera phone produced models of a similar quality with errors of the
750 same order of magnitude; indeed camera phone imagery even out-performed DSLR
751 imagery in one test. Moreover, Smith and Vericat (2015) found convergent gyrocopter-
752 based images produced a higher quality model than standard vertical UAV-based
753 images at similar survey ranges as the doming effect was removed (James and Robson,
754 2014a), image blurring from vibrations was reduced and greater user-control over the
755 images from manual camera operation enabled image overlap to be better specified.

756

757 Using aerial imagery and applying a basic refraction correction, Woodget et al. (2014)
758 assessed the ability of SfM-MVS to obtain topography through water. Accuracy of
759 exposed and submerged surface reconstructions was compared in 4 separate surveys.
760 Average water depths were ~ 0.15 m, though maximum depths of > 0.5 m were
761 reported. Results were promising: once refraction correction had been applied mean
762 errors increased in only 2 of the 4 of the surveys (0.005 m to 0.053 m and 0.004 m to -
763 0.008 m) and were lower than exposed areas in the remaining 2 surveys (0.044 m to
764 0.023 m and 0.111 m to -0.029 m) (Woodget et al., 2014).

765

766 Overall, the lack of a consistent validation methodology or a systematic campaign to
767 validate SfM-MVS-derived models inhibits precise determination of expected errors.
768 The flexibility of SfM-MVS as a survey tool means that many confounding variables will
769 combine to determine the accuracy of a SfM-MVS terrain model thereby making
770 isolation of individual error sources extremely challenging. There exists insufficient
771 validation data to isolate and quantify the effect of each component. This is in contrast
772 to the standardised validation strategies for Multi-View Stereo algorithms where the
773 performance of each algorithm is compared for a range of freely available high quality
774 validation data sets (available at <http://vision.middlebury.edu/mview/>; Seitz et al.,
775 2006). However, establishing such objective reference data to benchmark approaches
776 is more challenging for the entire SfM-MVS workflow as applied to natural
777 environments. It is encouraging to see images and data being made available by
778 individual studies (James and Robson, 2012); a co-ordinated attempt to host such
779 image sets for which concurrent TLS data is available would provide a useful starting

780 point. The recent proliferation of SfM-MVS validation studies in physical geography-
781 facing publications is testament to the need to improve co-ordination and
782 standardisation of such efforts.

783

784 **VI Applications of SfM-MVS in physical geography**

785

786 At present, published applications of SfM-MVS in physical geography are often proof-
787 of-concept studies. As seen in Section V, there are many papers where quantitative
788 validation of SfM-MVS is the primary (or secondary) aim. In general, other aims can be
789 classified into studies that either: (i) extract spatial patterns or planimetric
790 measurements from SfM-MVS-derived orthomosaic photographs; (ii) extract three-
791 dimensional information (volumes or topography) from SfM-MVS point-clouds; or (iii)
792 use SfM-MVS to quantify surface change. Each aim is demonstrated in a wide variety of
793 environmental settings and applied to address a range of problems. A brief summary is
794 provided herein.

795

796 The ability of SfM-MVS to generate orthophotographs of the scene of interest presents
797 a substantial advantage over TLS as they hold a wealth of information of use to
798 physical geographers. Indeed, orthomosaic photographs created using SfM-MVS have
799 been used to calculate the area of wildlife sampling strips (Lisein et al., 2013), to map
800 active and relict supraglacial drainage pathways and their association with glacier
801 structure (Rippin et al., 2015), to delineate geological faults, joints and fractures
802 (Vasuki et al., 2014; Figure 5a) and outcrops (see Bemis et al., 2014) (Figure 5f) and

803 have been used in combination with correlations between image texture and particle
804 grain sizes (Carbonneau et al., 2004) to derive maps of grain size distribution on an
805 alluvial fan (de Haas et al., 2014). Certainly, there is the potential to interrogate these
806 orthophotographs in greater detail, for example, by applying gravelometric analysis in
807 object detection software (e.g. BASEGRAIN; Detert and Weitbrecht, 2012, 2013).

808

809 Most commonly, SfM-MVS is applied in the production of fine-resolution terrain data.
810 A large number of studies apply SfM-MVS to coastal environments (Harwin and
811 Lucieer, 2012; Mancini et al., 2013; James and Quinton, 2014; Ruzic et al., 2014) to
812 extract the topography of beaches, dunes or cliffs. Implementation of SfM-MVS on
813 cliffs surfaces is particularly straightforward since their near-vertical surfaces offer
814 advantageous viewpoints for ground-based imagery. Beyond the shore, subaqueous
815 topography of coral reefs has been derived by Nicosevici and Garcia (2008) and Leon et
816 al. (2015; Figure 5b). Again, advantageous viewpoints can be achieved with relative
817 ease underwater (images were taken by a snorkeler in Leon et al., 2015); however
818 obtaining accurate georeferencing data underwater is more problematic, with a basic
819 hand-held GPS device used by Leon et al. (2015). SfM-MVS has also been used to
820 quantify properties of rock outcrops (Favalli et al., 2012) and geological hand samples
821 (James and Robson, 2012) where a range of viewpoints can be easily acquired.

822

823 The geometry and environmental setting of fluvial surfaces presents a more
824 challenging test of SfM. Fonstad et al. (2013) used SfM on aerial imagery to produce
825 models of exposed topography and Dietrich (2015) used a SfM-derived

826 orthophorograph and DEM from a helicopter-based survey to describe morphological
827 features of a 32 km river reach. In a braided system, Javernick et al. (2014, 2015)
828 extended this by fusing the SfM-MVS topographic model of exposed surfaces with
829 optical bathymetric mapping also using imagery taken from a helicopter, while
830 Woodget et al. (2014) corrected for refraction effects to extract bathymetry from SfM-
831 MVS data directly. This method relies on the visibility of the river bed and cannot be
832 applied where light does not penetrate to the bed. An ephemeral river setting
833 permitted Smith et al. (2014) to extract bed topography using SfM-MVS once a flood
834 wave had passed. This study coupled a SfM-MVS DEM with flood marks extracted from
835 the imagery used for the SfM-MVS model and both were input into a depth-averaged
836 2D hydraulic model to evaluate peak flash-flood flood magnitude. Used in this way,
837 SfM-MVS has potential to be used as part of post-flood surveys by increasing the data-
838 acquisition rate of teams in the field and thus enabling greater spatial coverage of
839 flood reconstructions shortly after a flood event.

840

841 Other applications of SfM-MVS are increasingly using SfM-MVS data as input into
842 models of surface processes in this way. Javernick et al. (2015) also used SfM
843 topographic data as input to depth-averaged 2D hydraulic model; while Westoby et al.
844 (2015) used SfM-MVS terrain data and a 2D hydraulic model to model numerically the
845 propagation of different glacial outburst flood scenarios as part of a hazard
846 assessment. Meesuk et al. (2015) fuse SfM-MVS data with ALS data, which was shown
847 to improve the performance of urban flood models in predicting flood depth and
848 extents. In a coastal setting Casella et al. (2014) merged SfM-MVS topography with

849 multibeam bathymetry for input to a wave runup model. Predicted maximum wave
850 runup was compared with that observed in SfM-MVS orthophotographs to evaluate
851 the model. Such coupling of the topographic data created from SfM-MVS surveys with
852 data extracted from orthophotographs has the potential expand SfM into more novel
853 physical geography applications. For example, Lucieer et al. (2014) also combined SfM-
854 MVS-derived topographic models and orthophotos to relate the spatial distribution
855 and health of moss beds in East Antarctica to snowmelt drainage pathways.

856

857 Topographic data sets are often interrogated further to extract sub-grid roughness
858 metrics (Rippin et al., 2015; Leon et al., 2015; Smith and Vericat, 2015) which are a
859 common requirement in physical geography and related disciplines (see Smith, 2014).
860 The large increase of data density in TLS and SfM-MVS datasets (orders of magnitude
861 above more conventional survey techniques) permits the calculation of roughness at a
862 greater range of scales than before. Such roughness may influence surface processes
863 directly (e.g. ice surface melting; Irvine-Fynn et al., 2014), reflect spatial or temporal
864 differences in process operation (e.g. subglacial erosion and deposition; Li et al.,
865 2010b) or be used as a surrogate for less measurable processes (e.g. flow resistance;
866 Aberle and Smart, 2003). The increased availability of dense topographic datasets
867 resulting from widespread application of SfM-MVS opens up the possibility of more
868 extensive application of roughness metrics to address physical geography problems,
869 particularly in the use of multi-scale roughness metrics (Smith, 2014).

870

871 SfM-MVS data are also used for volumetric measurement of features (Figure 5c),
872 including the size of coastal boulders (Gienko and Terry, 2014), eroded gully volumes
873 (Castillo et al., 2012; d'Oleire-Oltmanns et al., 2012; Gómez-Gutiérrez et al., 2014;
874 Frankl et al., 2015) and aboveground forest biomass (Dandois and Ellis, 2013).

875

876 Repeat SfM-MVS surveys are used to monitor topographic or positional changes.
877 Changes are quantified through: (i) interrogation of orthophotographs with image
878 correlation software to observe displacements, as applied by Lucieer et al. (2013) to
879 landslide displacement monitoring (Figure 5e) and Immerzeel et al. (2014) and Ryan et
880 al. (2015) to glacier movement (Figure 5d); (ii) differencing resulting topographic
881 models, as applied extensively in physical geography to monitor cliff retreat (James
882 and Robson, 2012), change in periglacial sorted circles (Kääb et al., 2013), braided
883 rivers (Tamminga et al., 2015), erosion rates of badlands (Smith and Vericat, 2015),
884 gully volume change (Kaiser et al., 2014), rill and interrill erosion (Eltner et al., 2014),
885 landslide activity (Turner et al., 2015; Stumpf et al., 2015), glacier thinning (Immerzel
886 et al., 2014), calving dynamics (Ryan et al., 2015) and lava dome subsidence (James
887 and Varley, 2012); or (iii) by identifying 3D displacement vectors of features observed
888 on two point clouds, as applied to study the mobility of advancing rhyolitic lava flows
889 (Tuffen et al., 2013).

890

891 While not comprehensive, this brief overview demonstrates the range of applications
892 for SfM-MVS in the field of physical geography and the high demand for the data
893 provided. Physical geography is not unique in this regard. In related fields, SfM-MVS is

894 used regularly; for example SfM-MVS is now used in archaeology (De Reu et al., 2014;
895 McCarthy, 2014) and as part of efforts to preserve cultural heritage digitally (Gallo, et
896 al., 2013; Koutsoudis et al., 2014).

897

898 **VII Looking forward: the potential of SfM-MVS**

899

900 There is little doubt that SfM-MVS surveys will play an important role in the study of
901 physical geography into the future. It is unlikely that SfM-MVS has achieved its full
902 potential; recent developments in computer vision and related fields indicate that SfM-
903 MVS can address an even wider range of problems in physical geography.

904

905 Aerial platforms suitable for SfM-MVS have developed markedly in the last few years.
906 Previous issues of image stability (Hardin and Hardin, 2010) have largely been resolved
907 in more sophisticated UAVs on the market today. The increasing popularity of UAVs for
908 a range of applications will likely drive down the cost of such systems. Increased
909 battery life is improving the range and performance of UAVs. Developments in pilot-
910 assistance and navigation systems will increase the reliability of UAVs, especially
911 during critical take-off and landing phases. Improvement in on-board GPS systems
912 could increase the accuracy of methods to determine camera position co-ordinates
913 directly and avoid the need for target-based georeferencing. This development would
914 permit SfM-MVS reconstructions of large scale geomorphological features (e.g. alluvial
915 fans, whole valleys) as no physical access to the study site is required. While technical
916 issues remain relating to timing errors and the weight of on-board components

917 required for direct georeferencing (Whitehead and Hugenholtz, 2014), these are
918 largely being resolved. Such developments will enable SfM-MVS data acquisition over
919 much larger areas useful for capturing topography beyond the hillslope or feature
920 scale and towards the landscape scale. Even routine monitoring of topographic
921 changes over broad areas could be achieved this way. Perhaps the biggest challenge
922 facing UAV-based SfM-MVS surveys is future legislation restricting both flight ranges
923 and the degree of automation of such systems. With such legislation in mind, the
924 deployment of autonomous vehicles for SfM-MVS is likely to be restricted to the
925 ground or underwater settings. Indeed, the development of compact and cheap
926 underwater platforms (e.g. 'OpenROV') will likely stimulate underwater applications of
927 SfM-MVS in relatively inaccessible locations.

928

929 While the above developments enable larger areas to be incorporated into SfM-MVS
930 surveys, static arrays of cameras can be used to monitor topographic changes over
931 time and improve the temporal resolution of data sets. Discreet trail cameras are
932 available for such networks and could permit truly event-scale monitoring of
933 topographic change, useful to accurately constrain the driving forces of observed
934 change and understand the relevant controls. Images can be transferred over the
935 mobile network and could even be automatically input into SfM-MVS software to
936 produce automated models of topographic change. Using such a network, image
937 capture can be triggered by an external sensor, such as a rain or river stage gauge.
938 Video footage could also be used in this way to ensure individual events are detected
939 automatically thereby avoiding the need to pre-define survey intervals. Developing

940 techniques to create models of dynamic scenes that move *during* a survey (so-called
941 ‘non-rigid’ SfM; Wang et al., 2014) requires dynamic keypoint correspondences and is
942 currently an active area of research that would have applications in studies of mass
943 movement dynamics, for example. For field deployment, power consumption and data
944 memory storage are both issues that need resolving. Generating topographic models
945 ‘on the fly’ is computationally demanding but could potentially be used to track the
946 movement of objects through a scene. Video stabilisation algorithms such as those
947 underlying the ‘hyper-lapse’ videos of Kopf et al. (2014) could improve the quality of
948 video footage taken on-board mobile platforms.

949

950 Crowd-sourcing of images for SfM has been already implemented outside of physical
951 geography (Snavely et al., 2008; Irschara et al., 2012) and offers exciting opportunities
952 to develop participatory science projects. In particular, hazard assessment would lend
953 itself to such participatory methods (e.g. post-flood analysis), though issues with
954 georeferencing, reliability, accuracy and precision remain (Boulos et al., 2011). In
955 general, as our ability to acquire input data improves, managing data volumes and
956 identifying efficient methods of generating and intelligently decimating point clouds
957 (Morales et al., 2011; Lai et al., 2014) represents the main bottleneck for the future
958 development of SfM-MVS.

959

960 **VIII Summary**

961

962 By removing the necessity for either technical expertise or expensive surveying
963 equipment, Structure from Motion has effectively democratised the acquisition of high
964 resolution topographic data (Javernick et al., 2014). The main technical and financial
965 limitation is the need for TS or dGPS equipment for accurate georeferencing of point
966 clouds. The point densities and spatial resolution that are achievable with SfM-MVS
967 are significantly greater than those of TS, dGPS, ALS and comparable to TLS; however,
968 SfM-MVS data are typically less precise at longer ranges (James and Robson, 2012).
969 Reflecting this increased capacity for data capture, there has been an explosion of
970 applications of SfM-MVS in physical geography in recent years. Survey time required in
971 the field is minimal and the technique is sufficiently flexible to be applied over a variety
972 of scales.

973

974 Yet, the flexibility of SfM-MVS, in terms of available platforms, sensors, data
975 acquisition protocols, software packages and DEM generation methods, confounds
976 attempts to robustly validate the practically achievable data quality using SfM-MVS. A
977 general relationship between RMSE-error and survey range has been established from
978 a synthesis of all available quantitative validation data (Smith and Vericat, 2015), but
979 the absence of a standardised or systematic validation strategy complicates further
980 quantification. Indeed, the limited ability to pre-determine data quality in SfM-MVS
981 surveys and the variable success of surveys (which can only be evaluated after field
982 campaigns are complete) is perhaps the biggest weakness in the approach.

983

984 From a detailed description of the workflow underlying SfM-MVS, it is clear that the
985 success of SfM-MVS is determined by the specific combination of the properties of the
986 scene and the images captured. There are a large number of complicating factors (e.g.
987 blurring, motion, shadows, angular separation of images) that interact to determine
988 model quality. As the workflow is often not apparent to a typical end-user, reasons for
989 success or failure may be unclear.

990

991 Moreover, the workflow demonstrates a large number of quality thresholds that must
992 be specified to implement SfM-MVS. For example, at the keypoint correspondence
993 stage a 'distance ratio' criterion is used to ensure the Euclidean distance of the nearest
994 neighbour is sufficiently distinct from the second nearest neighbour; the value
995 specified is variable between implementations of SfM. Other thresholds relate to
996 approximate matching of nearest neighbours for computational efficiency and the
997 identification of geometrically inconsistent matches. At present, these are neither
998 routinely reported nor adjusted individually by SfM-MVS-users in physical geography;
999 rather a qualitative global quality setting is often specified in individual software
1000 packages, further encouraging a 'black box' approach to SfM-MVS. The specific
1001 implementation of SfM-MVS is often more transparent in open source software; such
1002 transparency and ability to adjust specific parameters implemented in the workflow
1003 should be encouraged. Critical perspectives of SfM-MVS implementation in physical
1004 geography often focus on the stages that are common to conventional
1005 photogrammetry (e.g. lens model specification; James and Robson, 2014a). Greater

1006 engagement with each step of the SfM-MVS workflow will be of benefit to the physical
1007 geography community.

1008

1009 Nevertheless, SfM-MVS has revolutionized topographic data capture in physical
1010 geography; it has been applied in a range of environmental settings to address a
1011 number of problems. The advent of TLS in the previous decade perhaps primed the
1012 physical geography community to be especially receptive to SfM-MVS. Indeed, in
1013 common with TLS, greater interrogation and quantification of the rich data sets that
1014 arise, combined with further technological advances in sensor design, platforms and
1015 real-time topographic monitoring indicate that the full potential of SfM-MVS in
1016 physical geography has yet to be realised.

1017

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1026

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1574

1575 **Figure 1.** Comparison of digital survey methods with regards to financial cost, data
1576 acquisition rate, spatial coverage, resolution and accuracy. Note that photogrammetry
1577 and SfM values are dependent on survey range. Colour bars for photogrammetry
1578 represent 'conventional' aerial photogrammetry, though the range values for
1579 alternative implementations of photogrammetry are indicated. Bars derived from
1580 information in Brasington et al. (2000); Young (2012); Gallay (2013) and Bangen et al.
1581 (2014b).

1582

1583 **Figure 2.** Typical workflow in the production of georeferenced dense point clouds from
1584 image sets and Ground Control Points. Inputs and outputs are shown in dark red. In
1585 the top right, as a demonstration, matches determined to be valid are shown in red,
1586 while matches determined to be invalid are given in blue.

1587

1588 **Figure 3.** Examples of platform-types from which SfM-MVS imagery can be applied: (a)
1589 lighter-than-air blimp; (b) kite; (c) multicopter-type UAV; (d) camera boom; (e)
1590 gyrocopter; (f) trail camera.

1591

1592 **Figure 4.** Variability of SfM-MVS Root Mean Squared Error (RMSE, m) with survey
1593 range (m) for different validation-types. Fitted power law described in the text. Data
1594 extracted from: Favalli et al. (2012); Harwin and Lucieer (2012); James and Robson

1595 (2012); Mancini et al. (2013); James and Quinton (2014); Javernick et al. (2014); Lucieer
1596 et al. (2014); Micheletti et al. (2014); Oúedraogo et al. (2014); Ružić et al. (2014); Smith
1597 et al. (2014); Thoeni et al. (2014); Tonkin et al. (2014); Stumpf et al. (2015); subaerial
1598 data from Woodget et al. (2014) and an unpublished result by the authors on ice
1599 surface plots. Adapted from Smith and Vericat (sub).

1600

1601 **Figure 5.** Example SfM-MVS-derived data products: (a) Faults on a rock surface
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