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Mesh Management Methods in Finite Element Simulations of Orthodontic Tooth Movement

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Abstract

In finite element simulations of orthodontic tooth movement, one of the challenges is to represent long term tooth movement. Large deformation of the periodontal ligament and large tooth displacement due to bone remodelling lead to large distortions of the finite element mesh when a Lagrangian formalism is used. We propose in this work to use an Arbitrary Lagrangian Eulerian (ALE) formalism to delay remeshing operations. A large tooth displacement is obtained including effect of remodelling without the need of remeshing steps but keeping a good-quality mesh. Very large deformations in soft tissues such as the periodontal ligament is obtained using a combination of the ALE formalism used continuously and a remeshing algorithm used when needed. This work demonstrates that the ALE formalism is a very efficient way to delay remeshing operations.

Keywords: Orthodontic Tooth Movement, Arbitrary Lagrangian Eulerian formalism, Remeshing, Finite Element Method

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1. Introduction

The Finite Element (FE) Method is a numerical procedure to approximate problems modelled by partial differential equations using a discrete representation of the problem to be solved on a grid of nodes and elements. In mechanical models, it involves procedures to calculate in each element stresses and strains resulting from external factors such as forces and displacements. The FE method is extremely useful for estimating mechanical response of biomaterials and tissues that can hardly be measured in vivo. It has been used in dentistry-related problems since the 1970's, as reviewed in [1, 2, 3], with the interest of determining stresses in dental structures and materials used for clinical treatment and repair, and to improve the strength and response of these treatments, procedures and associated adaptive behaviour of the tissues. In particular, for orthodontic tooth movement problems, the FE method can deliver not only the global mechanical behaviour of the involved structures, i.e. the tooth mobility, but also it gives access to local stresses and strains of each tissue. That local behaviour is essential to couple mechanics and biology and to model the adaptive response of tissues.

One of the main principles of orthodontic treatment is to impose external loads to a tooth, leading to an altered mechanical environment in the periodontal ligament (PDL) surrounding the tooth and bone tissues supporting it. This altered environment induces remodelling and leads the tooth into a new position. The driving force of remodelling is the biological interaction between bone tissues and the PDL. Remodelling models in orthodontics FE analysis usually involve an update of the purely mechanical displacement of the tooth due to applied forces by a displacement due to the remodelling

26 stimulus [4, 5]. The stimulus for remodelling is either the strain energy den-
27 sity [6], based on the strain field [7, 8, 9], or based on the stress field [10].
28 However, other approaches can also be found: Soncini and Pietrabissa [11]
29 or van Schepdael et al. [12] proposed remodelling models considering a vis-
30 cious behaviour of the bone (viscoelastic Maxwell models) ; Cronau et al. [13]
31 proposed a remodelling model considering a viscous behaviour of the PDL
32 (viscoelastic Maxwell model) ; finally, Field et al. [14], Lin et al. [15], Men-
33 goni and Ponthot [16] proposed remodelling laws involving an explicit local
34 change of the bone elastic properties based on the strain level, similarly to
35 remodelling algorithms used within the orthopaedic biomechanics literature.

36 In any case, due to remodelling and therefore softening of the bone tissue,
37 or when the PDL deformations are physically modelled, large deformations
38 are locally encountered during tooth movement. This leads to deformations
39 of the finite element mesh up to a point where the mesh quality is no longer
40 sufficient enough either to continue the computation, if elements happen
41 to get highly distorted, or simply to blindly trust the solution quality. To
42 overcome this problem, mesh management techniques such as the Arbitrary
43 Lagrangian-Eulerian (ALE) formalism and a remeshing method are proposed
44 in this work. The ALE formalism decouples, at each time step of the simu-
45 lation, the mesh movement from the material displacement. The remeshing
46 method authorises, at given predefined time step, a complete remesh the de-
47 formed geometry. The ALE method has been previously used in biomechan-
48 ical problems, specifically in cardiovascular problems where fluid-structure
49 interactions between blood flow and natural tissues [17, 18, 19, 20, 21, 22, 23]
50 or devices [24, 25, 26] are modelled, or in deformation problems of soft or-

51 gans such as breasts and lungs [27, 28], or in car safety simulation such as
52 airbag deployment [29]. However, to the best of the authors' knowledge, it
53 has not been used with dentistry-related models. Remeshing methods are
54 often used in bone remodelling models when remodelling algorithms involve
55 the computation of a new geometry [5] rather than being embedded into the
56 constitutive behaviour of the tissue. In the present study, the remodelling
57 algorithm for orthodontic tooth movement [16] is embedded into the bone
58 tissue behaviour allowing it to soften as biological activity occurs. The aim
59 of this study was to assess the advantages and drawbacks of using the ALE
60 method and remeshing procedures to model a tooth moving along a finite
61 distance in the alveolar bone due to orthodontic forces. The simulations
62 presented in this work were performed using the non-linear implicit FE code
63 METAFOR (developed at the LTAS/MN²L, University of Liège, Belgium -
64 metafor.ltas.ulg.ac.be). All material models [16, 30] and numerical methods
65 such as ALE [31, 32] and remeshing method [33] used in this work were previ-
66 ously implemented, verified, or validated, in this software in such a way that
67 they are fully compatible. They are here used in the new context of long term
68 orthodontic tooth movement. Similar simulations would have been difficult
69 in traditional commercial software.

70 **2. Methods**

71 *2.1. Theoretical Background*

72 The Arbitrary Lagrangian Eulerian (ALE) formalism [34] consists in de-
73 coupling the movement of the finite element mesh from the deformations
74 of the underlying material. Compared to the classical Lagrangian formal-

75 ism where the nodes follow the same material particles or to the Eulerian
76 formalism where the nodes are fixed in space, the motion of the ALE com-
77 putational grid can be arbitrarily chosen by the user of the FE code. ALE
78 methods are very helpful in large deformation problems, such as the ap-
79 plications presented in this paper, when the quality of the finite elements
80 deteriorates rapidly during the simulation. For these particular models, the
81 quality of the ALE mesh is constantly optimised and costly remeshing op-
82 erations are delayed, and sometimes completely avoided. Another kind of
83 problems targeted by ALE methods is the simulation of complex material
84 flows involving free boundaries which cannot be handled by the traditional
85 Eulerian formalism with a fixed mesh [31].

86 The ALE equilibrium equations contain two sets of unknowns defined at
87 each node [34]: the material velocity and the mesh velocity. This system
88 of equations must be completed with additional relationships describing the
89 motion of the mesh. However, in the case of highly nonlinear problems in-
90 cluding large deformations and possibly contact between boundaries, writing
91 these equations explicitly is very difficult. The common workaround is to
92 solve the two sets of equations sequentially with an operator split procedure.
93 At each time-step, the nonlinear equilibrium equations are iteratively solved
94 as in the Lagrangian case, i.e. with a mesh that follows the material. Once
95 the equilibrium is reached, the nodes are then relocated using appropriate
96 techniques [31] such as smoothing, projections or prescribed displacements.
97 The solution fields (e.g. the stress tensor and the internal variables of the
98 material) are eventually transferred from the old mesh configuration to the
99 new one. Since the topology of both meshes is exactly the same (each ele-

100 ment keeps the same neighbours during the redefinition of the new mesh) and
101 the distance between two corresponding elements is usually small, very fast
102 and efficient transfer algorithms based on projections and the Finite Volume
103 Method can be employed [32, 35, 36].

104 When the deformation of the computational domain becomes so impor-
105 tant that the quality of the mesh cannot be improved without modifying
106 its topology, a new one has to be generated by a remeshing procedure. In
107 METAFOR, this expensive operation consists in several steps. First the
108 boundaries of the deformed domain are extracted and converted to smooth
109 cubic splines which are remeshed one by one using a prescribed mesh density.
110 Secondly the interior of the domain is remeshed thanks to a robust quadran-
111 gular mesher [37]. Then the solution fields are transferred from the old mesh
112 to the new one. The transfer methods used in this work [33] are very similar
113 to the former ones implemented in the ALE context. Nevertheless, they are
114 much slower because the projection requires the determination of all the ele-
115 ments of the old mesh which intersects each element of the new mesh. In the
116 ALE case, this expensive search can be restricted to the element itself and
117 its direct neighbours. At last, when all the fields have been transferred, the
118 time integration procedure is restarted with the new mesh using the ALE
119 formalism until a new remeshing operation is required.

120 In the current state of the code, remeshing operations should be man-
121 ually planned by the user. However, thanks to the ALE formalism which
122 constantly improves the mesh quality despite of large deformations, the num-
123 ber of remeshing is expected to be much lower than in a purely Lagrangian
124 approach.

125 *2.2. Modelling of Orthodontic Tooth Movement*

126 Two types of simulations were developed to illustrate the need for mesh
127 management methods in finite element models of orthodontic tooth move-
128 ments. Both simulations are 2D plane-strain models.

129 The first simulation was an academic case, testing the capacity of a re-
130 modelling model combined with mesh management methods for tooth move-
131 ment applications. A 2D single-rooted tooth was modelled with a root thick-
132 ness of 7 mm at the alveolar margin and a root height of 16 mm, surrounded
133 by alveolar bone (composed solely of trabecular tissue) 49-mm thick on each
134 side of the tooth, and 40-mm high (see Figure 1). This model corresponded
135 to a simulation of a tooth moving along the alveolar arch, with no other teeth
136 present. The size of the considered bone reduced boundary effects to which
137 remodelling algorithms are very sensitive [38, 39]. The tooth was considered
138 as being a rigid tissue and the PDL was represented with a piecewise-linear
139 interface model [16]. The bone was assumed to follow mechanical and remod-
140 elling constitutive models such as described in [16, 30] with an initial uniform
141 bone density of 1.3 gr/cc. These material and remodelling models assumed
142 an anisotropic elastoplastic bone, submitted to remodelling in such a way
143 that bone formation was observed at high strain energy density locations
144 and bone resorption at low strain energy density locations. The coupling
145 between the constitutive model and the remodelling model was expressed
146 in a Continuum Damage Mechanics framework, with a remodelling criterion
147 function of the strain energy density. Bone remodelling followed the concept
148 of the mechanostat theory [40]: the bone density and orientation evolved
149 according to the signed difference between the remodelling criterion and an

150 homeostatic level of that value. All material and remodelling parameters
151 are listed in Table 1. The remodelling rates are the only drivers of time in
152 the remodelling algorithm and the all simulation. All time measures are thus
153 described with respect to arbitrary time units, T. The bone was meshed with
154 linear quadrangular elements using a structured mesh away from the tooth
155 root in the regions delimited by the lateral rectangles $ABHG$ and $EFLK$
156 and using an unstructured mesh matching the root shape in its surround-
157 ing in the region delimited by the central rectangle $BEKH$ (see Figure 1)
158 with a total of 1004 elements. This subdivision of the geometrical domain
159 facilitated the mesh refinement in the area submitted to large strains around
160 the apex of the tooth root. Boundary conditions were applied to represent
161 the outcome of an orthodontic treatment at constant velocity. Boundary
162 conditions representative of a end-of-treatment state, i.e. constant rate of
163 displacement, were applied to the tooth. The tooth root was horizontally
164 translated at a constant velocity to achieve a displacement of 1.5 times its
165 width over 365 units of time. Rigid boundary conditions were applied to the
166 bone basal line while it was restrained vertically on its top line and horizon-
167 tally on its vertical extremities (see Figure 1). The ALE mesh movement was
168 specified following the tooth kinematics to keep a good mesh quality along
169 the displacement. The unstructured central mesh was moved with the same
170 velocity as the tooth, imposing that the displacement of nodes B , H , and I
171 was identical to that of node C in contact with the tooth root. In the same
172 way, the displacement of nodes E , J , and K was identical to that of node D .
173 The mesh nodes along the root surface (green curve in Figure 1) were relo-
174 cated using spline curves [31]. Finally, the nodes of lines BC , DE , EK , KJ ,

Table 1: Material and Remodelling parameters of tissues

Bone remodelling parameters (model 1 only) [16]					
homeostatic stimulus (MPa)	remodelling rate in resorption ($\mu\text{ m}/(\text{MPa T})$)	remodelling rate in formation ($\mu\text{ m}/(\text{MPa T})$)	width of lazy zone (MPa)	degree of anisotropy (-)	
0	10	5	0.1	1	
Elastoplastic parameters					
Material	Young's modulus (GPa)	Poisson's ratio (-)	Yield stress (MPa)	Hardening parameter (MPa)	Apparent density (gr/cc)
Bone	13.75	0.3	200.0	723.7	1.3
Tooth (model 2 only)	19	0.3	-	-	2.7
PDL	piecewise linear	0.49	-	-	0.1

(table 2, Figure 2)

175 JI , IH , and HB were repositioned so that the lines remained straight during
176 the material displacement. All the other inner nodes of the central region
177 were repositioned using Giuliani's smoothing method [41], which is based on
178 an iterative optimisation of the shape of neighbouring elements. The two
179 structured regions (sections $ABHG$ and $EFLK$) were meshed using a trans-
180 finite mesher. After relocation of the nodes, the different internal fields were
181 transferred onto the new mesh with a first order Godunov scheme [36, 32].

182 The second, more realistic, simulation consisted in a 2D lower incisor sub-
183 mitted to loading representative of clinical treatment. A mandible geometry
184 was obtained from the INRIA/GAMMA repository [52], constructed from a

	Engineering Strain	Tangential Modulus
	[-]	[MPa]
Compression	0.0	0.068 (i.e. Young's modulus)
	0.0 \rightarrow -0.25	linear variation up to 0.68
	-0.25 \rightarrow -0.31	linear variation up to 8.5
	-0.31 \rightarrow -0.82	constant value of 8.5
	< -0.82	13.5
Traction	0.0	0.068 (i.e. Young's modulus)
	0.0 \rightarrow 0.14	linear variation up to 1.35
	0.14 \rightarrow 0.63	constant value of 8.5
	> 0.63	0.01

Table 2: Values of the mechanical model for the periodontal ligament

185 surface reconstruction of the mandibular bone and its teeth. The 2D outline
186 in the mesiodistal plane of the left central incisor was extracted. The PDL
187 was created at the interface between the bone and the tooth assuming a con-
188 stant thickness of 0.2 mm (see Figure 3). The three surfaces (PDL, tooth,
189 and alveolar bone) were meshed with linear quadrangular elements. The
190 resulting unstructured mesh was composed of 1000 elements for the PDL,
191 1820 for the alveolar bone, and 2294 for the tooth. The tooth and bone were
192 modelled with a linear elastic constitutive law. The PDL was represented
193 with a piecewise-linear elastic material (see Table 2, Figure 2). Only the
194 initial tooth displacement was modelled and no remodelling algorithm was
195 used. All material parameters are listed in Table 1. Boundary conditions
196 were applied to represent the outcome of a constant-force orthodontic treat-

197 ment. The bone was clamped on its basal line (see Figure 3, red curve). A
198 pressure representative of a total 1.2 N force was gradually applied on the
199 labial side of the tooth crown (see Figure 3). The force used in this model
200 can be classified as a high orthodontic force. The PDL was thus submitted to
201 large strains and the numerical convergence could not be ensured with a clas-
202 sical Lagrangian approach due to excessive mesh distortion. Therefore, two
203 mesh management techniques were used: the Arbitrary Lagrangian-Eulerian
204 (ALE) method and a remeshing technique. The ALE method was applied at
205 each time increment of the simulation while remeshing was applied at four
206 load levels of 0.65 N, 0.85 N , 0.95 N and 1.05 N. Those loads were determined
207 in a pre-analysis as the values for which the ALE formalism could not man-
208 age the large deformations. In the case of the PDL, a spline rezoner [31] was
209 used for the two free boundaries delimiting the surface of the PDL (purple
210 lines in Figure 3). It permitted to relocate the nodes of the PDL boundary
211 with a cubic spline. Guiliani’s iterative smoothing method was subsequently
212 used on the inner nodes of the mesh, homogenizing the elements area [41].
213 After repositioning of the nodes, the different internal fields were transferred
214 onto the new mesh using a first order Godunov scheme [36, 32]. When the
215 ALE rezoning was not sufficient to keep a good mesh quality, a full remeshing
216 of the deformed geometry was considered. In this case, cubic splines were
217 built on the outline of the deformed geometry which was fully remeshed [53].
218 Solution fields were transferred from the old mesh to the new mesh using a
219 projection technique [33].

220 3. Results

221 The benefit of the ALE method in the first model was analysed comparing
222 the remodelling criteria values at 50% of the maximal displacement, i.e. 5.25
223 mm (see Figure 4) with and without ALE. At that level of displacement,
224 both methods showed the same results in the regions where the mesh is of
225 good quality. However, the classical Lagrangian method produced a distorted
226 mesh around the tooth apex to a point where the local numerical solution
227 could not be trusted any more, with a remodelling criterion reaching high
228 values around the tooth apex. Displacement higher than 5.4 mm could not be
229 computed with a Lagrangian mesh due to negative jacobians while the ALE
230 mesh allowed the full tooth displacement to be computed. The force needed
231 for the ALE model (Figure 5 plain line) is the same as the one needed for
232 the Lagrangian model (Figure 5 dash-dot line) where the Lagrangian mesh
233 is of good quality (for the first 2.6 mm of translation). The Lagrangian force
234 however deviates from the ALE one when the mesh becomes too distorted.
235 The remodelling constitutive model facilitated the tooth movement, requiring
236 a force about 40% lower than the force needed to displace the tooth of the
237 same length if no biological remodelling were present (Figure 5). The ALE
238 mesh kinematics is depicted in Figure 6 where the remodelling criterion is
239 plotted at three different time points of the simulation. The unstructured
240 mesh around the tooth in the rectangle $BEKH$ of Figure 1 followed the
241 tooth movement. The structured mesh of the upstream rectangle $ABHG$
242 expanded as the tooth moved away from the fixed left boundary while the
243 structured mesh of the downstream rectangle $EFLK$ shrunk.

244 The forces applied on the second model led to large strains around the

245 tooth collar. The soft PDL thus deformed up to a point where the mesh
246 quality can not be trusted any more (see Figure 7(b)). A better represen-
247 tation of the large strains at the alveolar margin without excessive mesh
248 distortion was allowed by the ALE method (see initial and deformed meshes,
249 with and without ALE in Figure 7(a-d)). A tipping force of 0.65 N was
250 applied while keeping a good mesh quality but a higher force could not be
251 used, with elements too distorted for a higher force, whatever the ALE node
252 relocation algorithm used (Figure 7(e), red element). Indeed in the cervical
253 area, because of the almost incompressible behaviour of the ligament, the free
254 boundaries created convex and concave menisci so that inversion of the finite
255 elements occurred. The first load step defined for remeshing was when the
256 applied load reached 0.65 N. The resulting new mesh (Figure 8(b)) allowed
257 the computation to continue further (still applying the ALE method at each
258 time step) up to a 0.85 N force. At a higher force level the mesh became once
259 more too distorted on the tension side (Figure 8(c)). New remeshing instants
260 were defined similarly at 0.85 N, 0.95 N, and 1.05 N. This fourth and final
261 mesh was used for forces up to 1.2 N. This remeshing technique could be used
262 further, every time defining new time steps at which remeshing takes place.
263 The displacement of the tooth tip was identical for all three models (purely
264 Lagrangian, ALE, ALE with remeshing) as long as the model converged (see
265 Figure 9).

266 4. Discussion

267 This work proposes an assessment of computational tools such as the Ar-
268 bitrary Lagrangian Eulerian formalism and remeshing in the development of

269 orthodontics tooth movement predictive models. Although this work focuses
270 on the computational methods and the presented models are not validated
271 against experimental and clinical data, it demonstrates the advantages and
272 drawbacks of these methods for soft tissues modelling and remodelling mod-
273 els.

274 The first model shows that the ALE formalism makes it possible to reach
275 a large displacement of a tooth within a mandible including the effect of
276 bone remodelling without any remeshing steps. While the model is not rep-
277 resentative of an actual tooth movement, it emphasizes the need to keep a
278 good-quality mesh where remodelling is observed so that the bone formation
279 or resorption is not artificially modified by numerical errors due to exces-
280 sive mesh distortion. It should be emphasized that the aim of the proposed
281 model is not clinically-driven. While the loading conditions have been cho-
282 sen to represent average constant rate of displacement achieved in the third
283 phase of orthodontic treatments [54, 55], the reproduced movement is not
284 a model of an actual treatment. In particular, no physiological homeostatic
285 loads are present, and the constant velocity condition is assumed to be the
286 result of using orthodontic devices which are not modelled. It is unlikely
287 that a constant rate of displacement would be achieved over such a distance
288 without the need to adapt the device used.

289 The second model underlines the possibility of reaching very large defor-
290 mations in soft tissues models. The combination of the ALE formalism used
291 continuously throughout the simulation with a remeshing algorithm used
292 when needed facilitates the development of a reliable model of the menisci
293 creation at the free boundaries of thin soft tissues. Analysing the evolution

294 of the mesh in the periodontal ligament however shows that the number of
295 elements describing those boundaries has to decrease with increasing applied
296 load. The creation of the menisci due to the deformation needs an initial fine
297 mesh. Once the menisci are formed, building a fine mesh without creating
298 badly shaped elements at the extremities is very hard. At the tension side,
299 the angle between the concave meniscus and the tooth boundary increases
300 as the force increases, and become obtuse. At the compression side however,
301 the angle between the convex meniscus and the bone boundary decreases,
302 with a tendency to deform the quadrangles into triangles. Therefore, the
303 description of the geometry of the free boundary is less and less accurate in
304 order to be able to mesh it properly. Using the combination of ALE and
305 remeshing methods in this case allows the simulation to reach force levels
306 that are representative of orthodontic treatment force levels. This is a major
307 improvement with respect to a purely Lagrangian approach that can only
308 reach a force a quarter of the final value achieved here.

309 3D models of a set of adjacent teeth submitted to loading through or-
310 thodontic devices would however better represent an actual clinical outcome.
311 Such models have already shown to perform well in initial tooth movement
312 predictions and in long-term prediction when the remodelling algorithm in-
313 volves full remeshing of a new geometry at each time step. In the case of
314 remodelling algorithm such as used in this work, the presented applications
315 demonstrate that the ALE formalism is a very efficient way to delay remesh-
316 ing operations. The later are usually very expensive in terms of CPU time
317 and user work time, even for 2D problems. In a 3D context, remeshing be-
318 comes a major issue and we think that it could be partially solved by the

319 ALE methods, which are already fully functional in 3D. Applications in 3D
320 will be thus addressed in a near future.

321 This computational work presents a promising approach to model large
322 tooth displacements in orthodontic treatment. This approach is not limited
323 to orthodontic treatment and can be used in combination with any remod-
324 elling algorithm fully embedded within the constitutive law and not needing
325 full computation of a new geometry.

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329 Ethical Approval: Not required

330 **References**

331 [1] Cattaneo PM, Dalstra M, Melsen B. The finite element method : a tool
332 to study orthodontic tooth movement. *J Dent Res* 2005;84(5):428–33.

333 [2] Mackerle J. Finite element modelling and simulations in dentistry:
334 a bibliography 1990-2003. *Comput Methods Biomech Biomed Engin*
335 2004;7(5):277–303.

336 [3] Van Staden RC, Guan H, Loo YC. Application of the finite element
337 method in dental implant research. *Comput Methods Biomech Biomed*
338 *Engin* 2006;9(4):257–70.

- 339 [4] Provatidis CG. A bone-remodelling scheme based on principal strains
340 applied to a tooth during translation. *Comput Methods Biomech*
341 *Biomed Engin* 2003;6(5-6):347–52.
- 342 [5] Chen J, Li W, Swain MV, Ali Darendeliler M, Li Q. A periodontal
343 ligament driven remodeling algorithm for orthodontic tooth movement.
344 *J Biomech* 2014;47(7):1689–95.
- 345 [6] Li J, Li H, Shi L, Fok AS, Ucer C, Devlin H, et al. A mathematical model
346 for simulating the bone remodeling process under mechanical stimulus.
347 *Dent Mater* 2007;23(9):1073–8.
- 348 [7] Bourauel C, Vollmer D, Jäger A. Application of bone remodeling theo-
349 ries in the simulation of orthodontic tooth movements. *J Orofac Orthop*
350 2000;61(4):266–79.
- 351 [8] Marangalou JH, Ghalichi F, Mirzakouchaki B. Numerical simulation of
352 orthodontic bone remodeling. *Orthod Waves* 2009;68(2):64–71.
- 353 [9] Qian Y, Fan Y, Liu Z, Zhang M. Numerical simulation of tooth move-
354 ment in a therapy period. *Clin Biomech* 2008;23(Supplement 1):S48–52.
- 355 [10] Kojima Y, Kawamura J, Fukui H. Finite element analysis of the ef-
356 fect of force directions on tooth movement in extraction space closure
357 with miniscrew sliding mechanics. *Am J Orthod Dentofacial Orthop*
358 2012;142(4):501–8.
- 359 [11] Soncini M, Pietrabissa R. Quantitative approach for the prediction
360 of tooth movement during orthodontic treatment. *Comput Methods*
361 *Biomech Biomed Engin* 2002;5(5):361–8.

- 362 [12] van Schepdael A, De Bondt K, Geris L, Sloten JV. A visco-elastic model
363 for the prediction of orthodontic tooth movement. *Comput Methods*
364 *Biomech Biomed Engin* 2014;17(6):581–90.
- 365 [13] Cronau M, Ihlow D, Kubein-Meesenburg D, Fanghnel J, Dathe H, Ngerl
366 H. Biomechanical features of the periodontium: an experimental pilot
367 study in vivo. *Am J Orthod Dentofacial Orthop* 2006;129(5):599.e13–21.
- 368 [14] Field C, Li Q, Li W, Thompson M, Swain M. A comparative mechanical
369 and bone remodelling study of all-ceramic posterior inlay and onlay fixed
370 partial dentures. *J Dent* 2012;40(1):48–56.
- 371 [15] Lin D, Li Q, Li W, Duckmanton N, Swain M. Mandibular bone remod-
372 eling induced by dental implant. *J Biomech* 2010;43(2):287–93.
- 373 [16] Mengoni M, Ponthot JP. A generic anisotropic continuum damage
374 model integration scheme adaptable to both ductile damage and bio-
375 logical damage-like situations. *Int J Plasticity* 2015;66:46–70.
- 376 [17] Colciago C, Deparis S, Quarteroni A. Comparisons between reduced
377 order models and full 3D models for fluid-structure interaction problems
378 in haemodynamics. *J Comput Appl Math* 2014;265:120–38.
- 379 [18] Martino ED, Guadagni G, Fumero A, Ballerini G, Spirito R, Biglioli
380 P, et al. Fluid-structure interaction within realistic three-dimensional
381 models of the aneurysmatic aorta as a guidance to assess the risk of
382 rupture of the aneurysm. *Med Eng Phys* 2001;23(9):647–55.

- 383 [19] Javadzadegan A, Fakhim B, Behnia M, Behnia M. Fluid-structure in-
384 teraction investigation of spiral flow in a model of abdominal aortic
385 aneurysm. *Eur J Mech B Fluids* 2014;46:109–17.
- 386 [20] Langer U, Yang H. Partitioned solution algorithms for fluid-structure
387 interaction problems with hyperelastic models. *J Comput Appl Math*
388 2015;276:47–61.
- 389 [21] Lee C, Zhang Y, Takao H, Murayama Y, Qian Y. A fluid-structure inter-
390 action study using patient-specific ruptured and unruptured aneurysm:
391 The effect of aneurysm morphology, hypertension and elasticity. *J*
392 *Biomech* 2013;46(14):2402–10.
- 393 [22] Taelman L, Degroote J, Swillens A, Vierendeels J, Segers P. Fluid-
394 structure interaction simulation of pulse propagation in arteries: Nu-
395 merical pitfalls and hemodynamic impact of a local stiffening. *Int J Eng*
396 *Sci* 2014;77:1–13.
- 397 [23] Wolters B, Rutten M, Schurink G, Kose U, de Hart J, van de Vosse F.
398 A patient-specific computational model of fluid-structure interaction in
399 abdominal aortic aneurysms. *Med Eng Phys* 2005;27(10):871–83.
- 400 [24] Chiastra C, Migliavacca F, Martínez MÁ, Malvè M. On the necessity
401 of modelling fluid-structure interaction for stented coronary arteries. *J*
402 *Mech Behav Biomed Mater* 2014;34:217–30.
- 403 [25] Guivier-Curien C, Deplano V, Bertrand E. Validation of a numerical
404 3D fluid-structure interaction model for a prosthetic valve based on ex-
405 perimental PIV measurements. *Med Eng Phys* 2009;31(8):986–93.

- 406 [26] McCormick M, Nordsletten D, Kay D, Smith N. Simulating left ventricu-
407 lar fluid-solid mechanics through the cardiac cycle under LVAD support.
408 J Comput Phys 2013;244:80–96.
- 409 [27] Yin Y, Choi J, Hoffman EA, Tawhai MH, Lin CL. A multiscale MDCT
410 image-based breathing lung model with time-varying regional ventila-
411 tion. J Comput Phys 2013;244:168–92.
- 412 [28] Kuhlmann M, Fear E, Ramirez-Serrano A, Federico S. Mechanical model
413 of the breast for the prediction of deformation during imaging. Med Eng
414 Phys 2013;35(4):470–8.
- 415 [29] Potula S, Solanki K, Oglesby D, Tschopp M, Bhatia M. Investigating
416 occupant safety through simulating the interaction between side curtain
417 airbag deployment and an out-of-position occupant. Accid Anal Prev
418 2012;49:392–403.
- 419 [30] Mengoni M, Ponthot JP. An enhanced version of a bone remodelling
420 model based on the continuum damage mechanics theory. Comput Meth-
421 ods Biomech Biomed Engin 2015;18(12):1367–76.
- 422 [31] Boman R, Ponthot JP. Efficient ALE mesh management for 3D quasi-
423 Eulerian problems. Int J Numer Methods Eng 2012;92(10):857–90.
- 424 [32] Boman R, Ponthot JP. Enhanced ALE data transfer strategy for explicit
425 and implicit thermomechanical simulations of high-speed processes. Int
426 J Impact Eng 2013;53:62–73.
- 427 [33] Bussetta P, Boman R, Ponthot JP. Efficient 3D data transfer operators

- 428 based on numerical integration. *Int J Numer Methods Eng* 2015;102(3-
429 4):892–929.
- 430 [34] Donéa J, Huerta A, Ponthot JP, Rodriguez-Ferran A. *Encyclopedia of*
431 *Computational Mechanics, Volume 1*; chap. 14: Arbitrary Lagrangian-
432 Eulerian Methods. Stein, E. and de Borst, R. and Hughes T. J. R.; 2004,
433 p. 413–37.
- 434 [35] Benson DJ. An efficient, accurate, simple ALE method for non-
435 linear finite element programs. *Comput Methods Appl Mech Eng*
436 1989;72(3):305–50.
- 437 [36] Rodriguez-Ferran A, Casadei F, Huerta A. ALE stress update for tran-
438 sient and quasistatic processes. *Int J Numer Methods Eng* 1998;42:241–
439 62.
- 440 [37] Sarrate J, Huerta A. Efficient unstructured quadrilateral mesh genera-
441 tion. *Int J Numer Methods Eng* 2000;49:1327–50.
- 442 [38] Bitsakos C, Kerner J, Fisher I, Amis AA. The effect of muscle loading
443 on the simulation of bone remodelling in the proximal femur. *J Biomech*
444 2005;38(1):133–9.
- 445 [39] Fernández J, García-Aznar J, Martínez R. Numerical analysis of a
446 diffusive strain-adaptive bone remodelling theory. *Int J Solids Struct*
447 2012;49(15):2085–93.
- 448 [40] Frost H. Skeletal structural adaptations to mechanical usage (SATMU):
449 2. Redefining Wolff’s law: the remodeling problem. *Anat Rec*
450 1990;226(4):414–22.

- 451 [41] Giuliani S. An algorithm for continuous rezoning of the hydrodynamic
452 grid in Arbitrary Lagrangian-Eulerian computer codes. Nucl Eng Des
453 1982;72(2):205–12.
- 454 [42] Dorow C, Krstin N, Sander FG. Determination of the mechanical prop-
455 erties of the periodontal ligament in a uniaxial tensional experiment. J
456 Orofac Orthop 2003;64(2):100–7.
- 457 [43] Natali AN, Carniel EL, Pavan PG, Bourauel C, Ziegler A, Keilig L.
458 Experimental-numerical analysis of minipig’s multi-rooted teeth. J
459 Biomech 2007;40(8):1701–8.
- 460 [44] Natali AN, Pavan PG, Carniel EL, Dorow C. A transversally isotropic
461 elasto-damage constitutive model for the periodontal ligament. Comput
462 Methods Biomech Biomed Engin 2003;6(5-6):pp. 329–336.
- 463 [45] Aversa R, Apicella D, Perillo L, Sorrentino R, Zarone F, Ferrari M,
464 et al. Non-linear elastic three-dimensional finite element analysis on
465 the effect of endocrown material rigidity on alveolar bone remodeling
466 process. Dent Mater 2009;25(5):678–90.
- 467 [46] Pini M, Wiskott HWA, Scherrer SS, Botsis J, Belser UC. Mechani-
468 cal characterization of bovine periodontal ligament. J Periodontal Res
469 2002;37(4):237–44.
- 470 [47] Pini M, Zysset PK, Botsis J, Contro R. Tensile and compressive be-
471 haviour of the bovine periodontal ligament. J Biomech 2004;37(1):111–
472 9.

- 473 [48] Toms SR, Eberhardt AW. A nonlinear finite element analysis of the
474 periodontal ligament under orthodontic tooth loading. *Am J Orthod*
475 *Dentofacial Orthop* 2003;123(6):657–65.
- 476 [49] Komatsu K, Sanctuary C, Shibata T, Shimada A, Botsis J. Stress-
477 relaxation and microscopic dynamics of rabbit periodontal ligament. *J*
478 *Biomech* 2007;40(3):634–44.
- 479 [50] Borák L, Florian Z, Bartáková S, Prachár P, Murakami N, Ona M, et al.
480 Bilinear elastic property of the periodontal ligament for simulation using
481 a finite element mandible model. *Dent Mater J* 2011;30(4):448–54.
- 482 [51] Qian L, Todo M, Morita Y, Matsushita Y, Koyano K. Deformation
483 analysis of the periodontium considering the viscoelasticity of the peri-
484 odontal ligament. *Dent Mater* 2009;25(10):1285–92.
- 485 [52] INRIA . Gamma repository. [https://www.rocq.inria.fr/gamma/gamma/
486 download/affichage.php?dir=ANATOMY&name=mandibule](https://www.rocq.inria.fr/gamma/gamma/download/affichage.php?dir=ANATOMY&name=mandibule); last visit
487 10/2014.
- 488 [53] Bussetta P, Dialami N, Boman R, Chiumenti M, Agelet de Saracibar
489 C, Cervera M, et al. Comparison of a fluid and a solid approach for the
490 numerical simulation of friction stir welding with a non-cylindrical pin.
491 *Steel Res Int* 2014;85(6):968–79.
- 492 [54] Buschang PH, Campbell PM, Ruso S. Accelerating tooth movement
493 with corticotomies: is it possible and desirable? *Semin Orthod*
494 2012;18(4):286–94.

495 [55] Dixon V, Read M, O'Brien K, Worthington H, Mandall N. A randomized
496 clinical trial to compare three methods of orthodontic space closure. J
497 Orthod 2002;29(1):31-6.

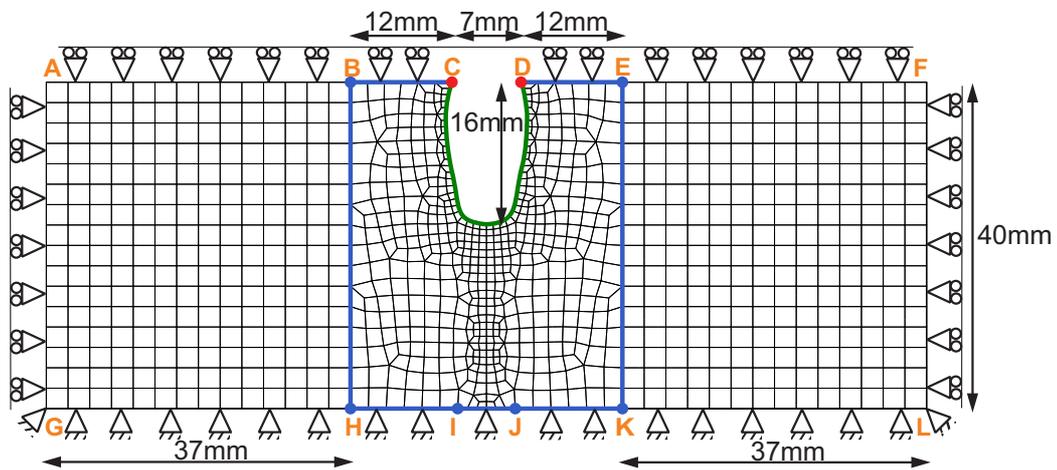


Figure 1: Academic case: geometry, mesh, and ALE mesh management: the nodes on the green curve are relocated using spline curves, the blue points have an horizontal displacement which is set equal to the one of the red points, the blue lines are remeshed (with a constant number of elements) as if they remained straight between their extremities.

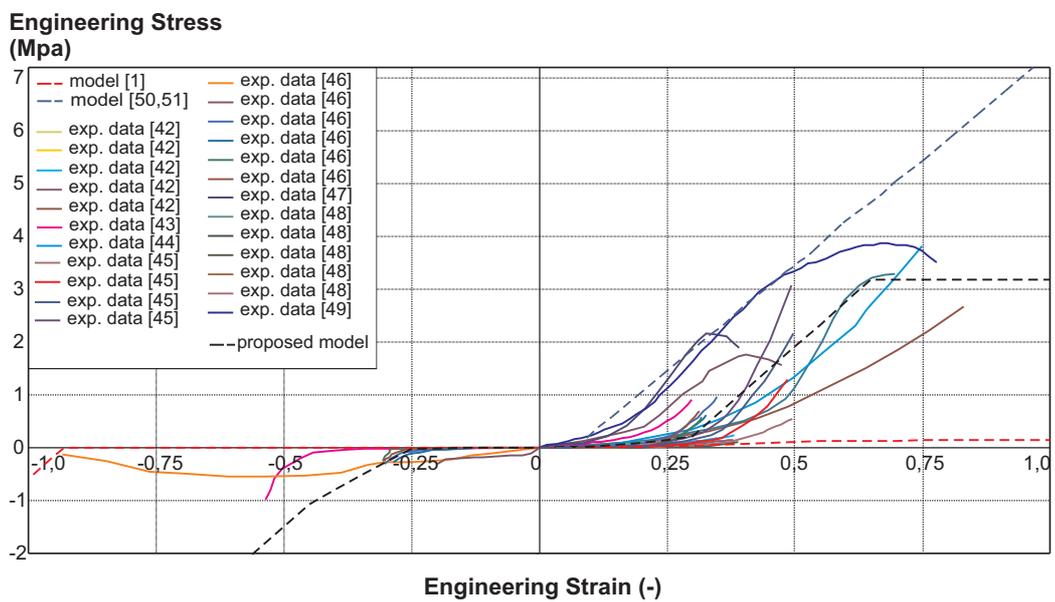


Figure 2: Periodontal Ligament - experimental data [42, 43, 44, 45, 46, 47, 48, 49] : Engineering Strain vs. Engineering Stress for uniaxial tests. The data is labelled after the name of first author of the paper it comes from, followed by the year of publication and the number of the figure in the paper (a letter is added if several curves appear on the same figure). As a comparison, in blue and red dashed line, two multi-linear models [1, 50, 51] that surround this experimental data. In black dashed line, the model used in this work.

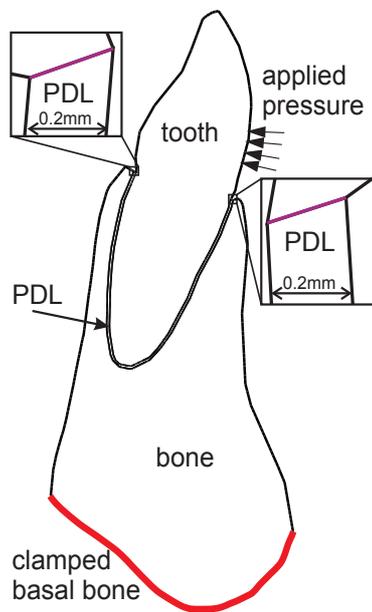


Figure 3: 2D geometry in the mesiodistal plane of the left central incisor.

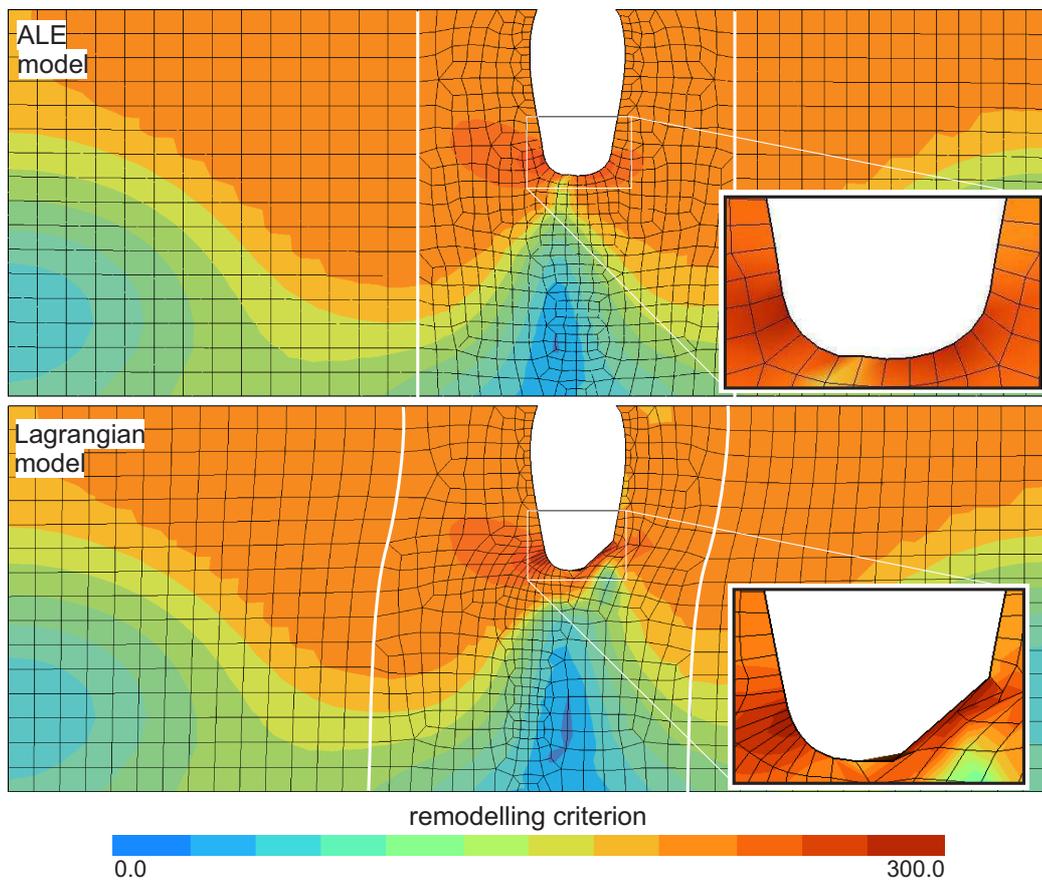


Figure 4: Comparison of the ALE and Lagrangian methods after 180 time units. Top panel: ALE mesh, bottom panel: Lagrangian mesh.

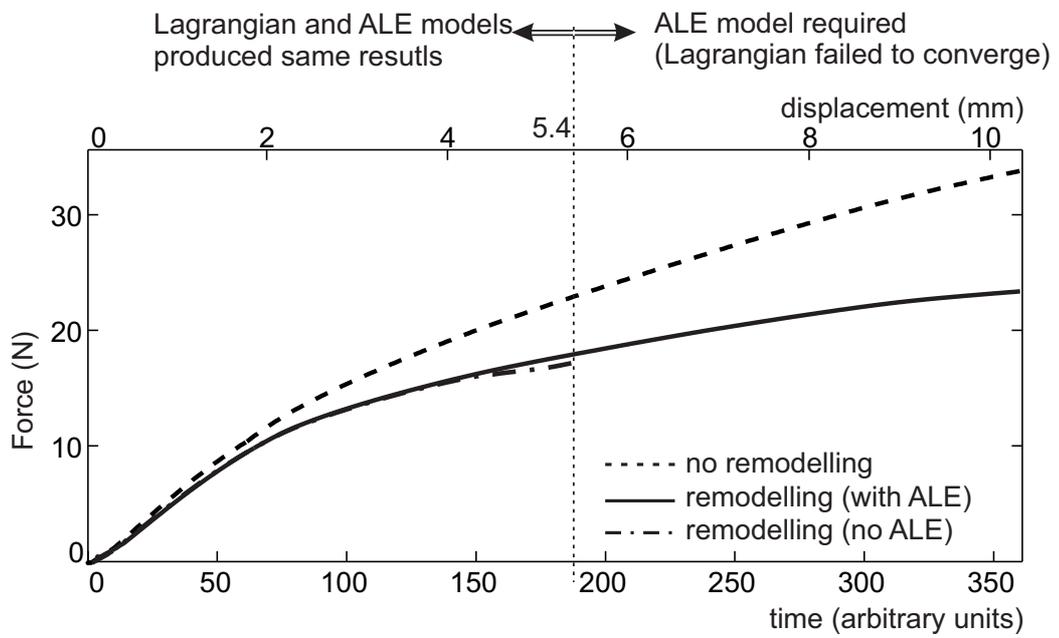


Figure 5: Force vs. time and corresponding displacements for the imposed velocity.

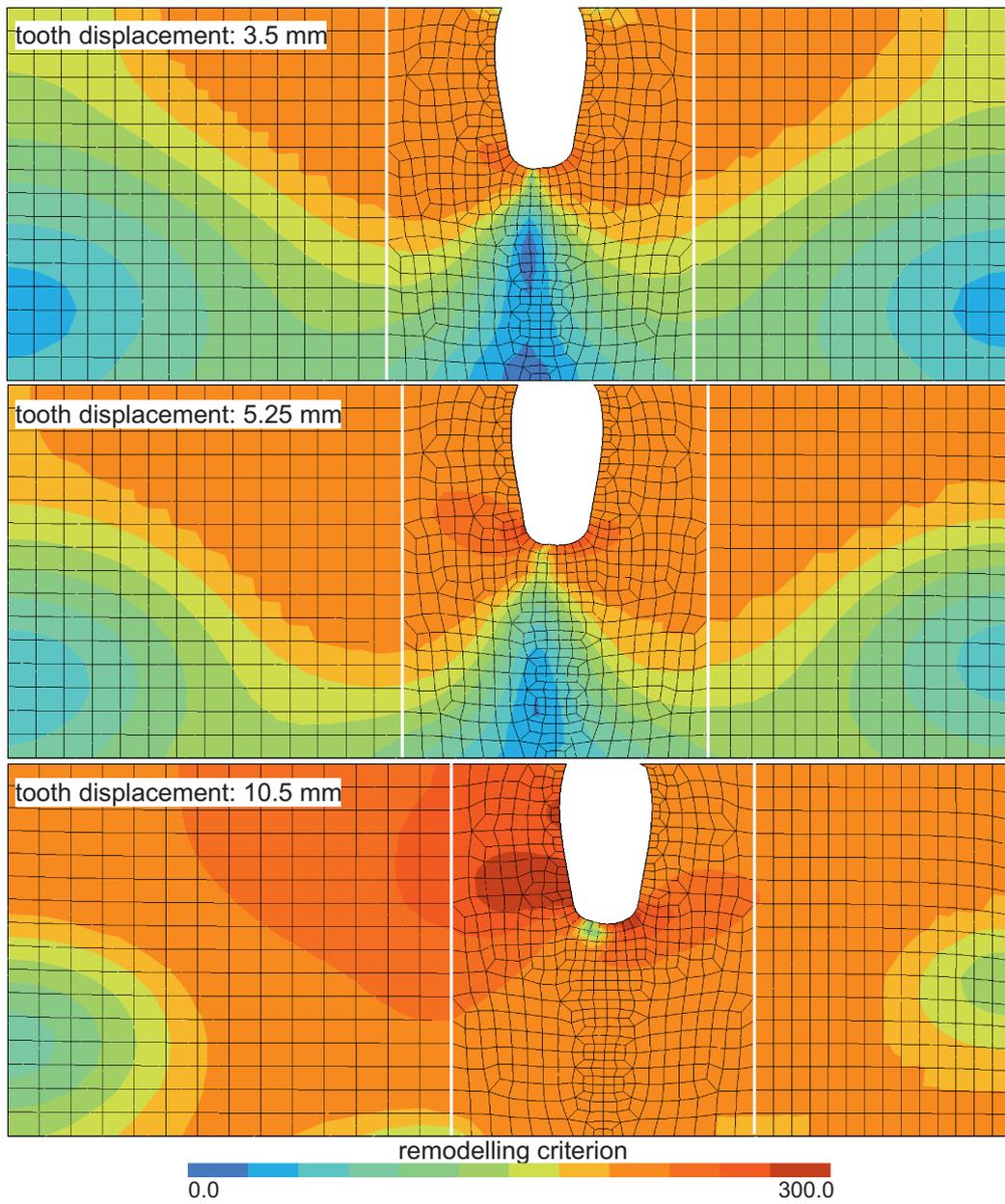


Figure 6: ALE mesh movement: the mesh follows the movement of the tooth.

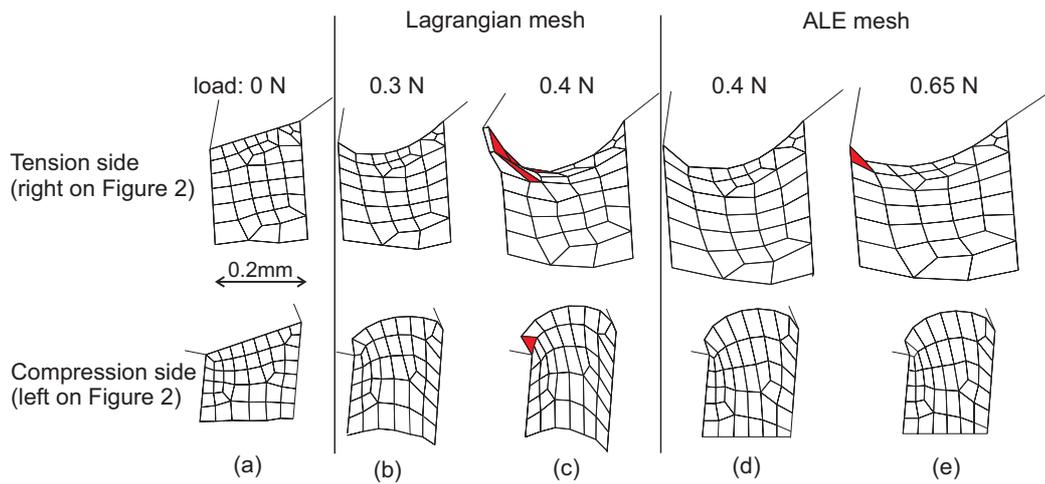


Figure 7: Zoom on the mesh evolution of the periodontal ligament at the alveolar margin. In red, the problematic elements.

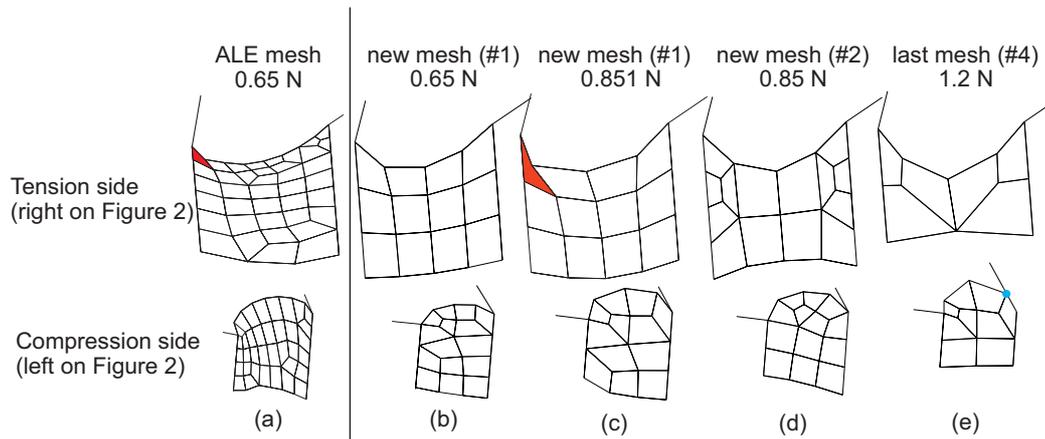


Figure 8: Zoom on the mesh of the periodontal ligament at the alveolar margin. In red, distorted elements (remeshing was required at those load values). In blue, node in contact with the base of the tooth crown.

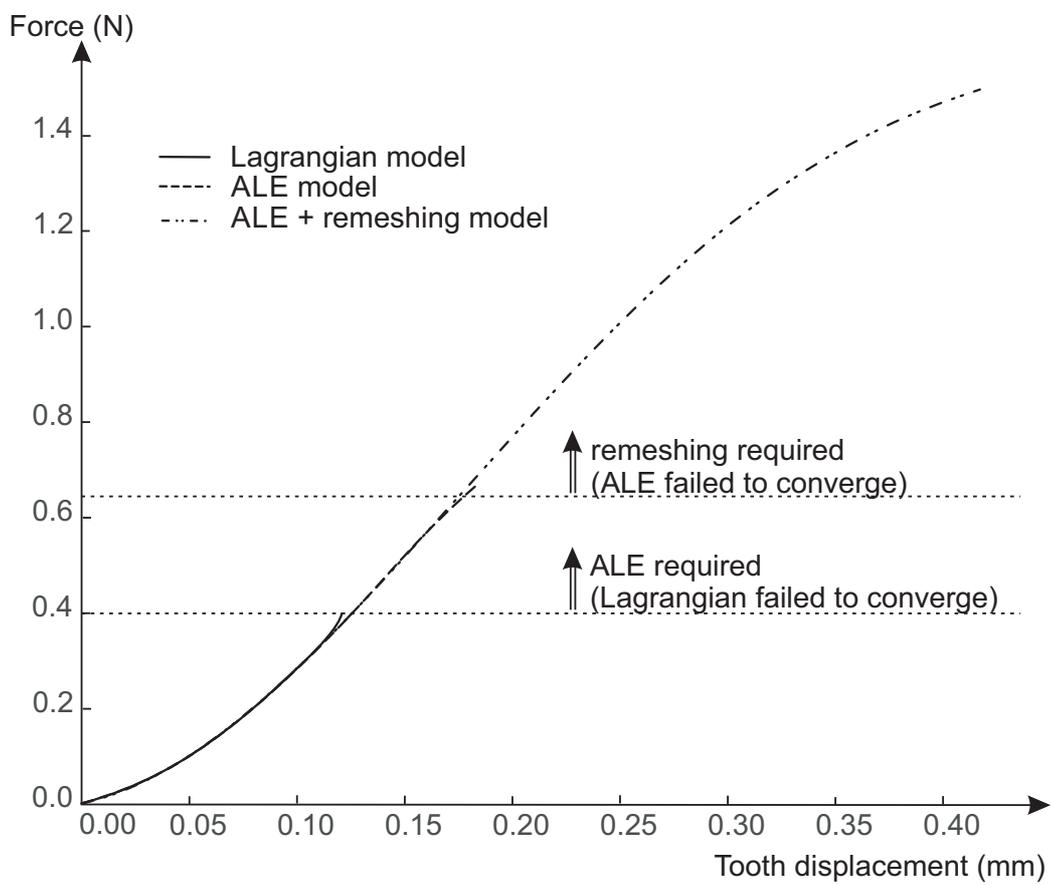


Figure 9: Force vs. tooth tip buccal displacement.