Integrated Terahertz Graphene Modulator with 100% Modulation Depth

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ABSTRACT: Terahertz (THz) frequency technology has many potential applications in nondestructive imaging, spectroscopic sensing, and high-bit-rate free-space communication, with an optical modulator being a key component. However, it has proved challenging to achieve high-speed modulation with a high modulation depth across a broad bandwidth of THz frequencies. Here, we demonstrate that a monolithically integrated graphene modulator can efficiently modulate the light intensity of the THz radiation from a THz quantum cascade laser with a 100% modulation depth for certain region of the pumping current, as a result of the strongly enhanced interaction between the laser field and the graphene enabled by this integration scheme. Moreover, the small area of the resulting device in comparison to existing THz modulators enables a faster modulation speed, greater than 100 MHz, which can be further improved through optimized designs of the laser cavity and modulator architectures. Furthermore, as the graphene absorption spectrum is broadband in nature, our integration scheme can be readily scaled to other wavelength regions, such as the mid-infrared, and applied to a broad range of other optoelectronic devices.

KEYWORDS: terahertz modulator, graphene, integrated photonics, quantum cascade laser, 100 percent modulation depth

Lying between the microwave and mid-infrared, the terahertz (THz) frequency region of the electromagnetic spectrum (∼0.3 to 10 THz) has potential for a number of diverse applications ranging from nondestructive imaging and spectroscopic sensing through to ultrahigh-bit-rate wireless communication. Various research in this region of the spectrum has undergone significant development over the last two decades, and the introduction and application of new materials such as graphene and metamaterials, together with the development of devices such as the quantum cascade laser (QCL) and the THz quantum well infrared photodetector (THz QWIP), are bringing THz technologies closer to more widespread application.

An optical modulator is a key component widely used for beam manipulation, imaging, optical communication, and active mode locking in other parts of the electromagnetic spectrum. However, the development of fast and efficient THz modulators is in its infancy, compared with the significant advances made in THz frequency lasers and detectors. Attempts to fabricate THz amplitude modulators have so far focused on semiconductor heterostructures containing a two-dimensional electron gas (2DEG) in which electrons can be accumulated or depleted by an applied gate voltage. However, the modulation depth of such devices is ultimately limited by the achievable tunability in electron density, which is up to \( \sim 1 \times 10^{12} \text{ cm}^{-2} \) for a 2DEG in a conventional semiconductor heterostructure. These devices were, therefore, initially found to modulate the THz amplitude by only a few percent, although through the incorporation of metamaterials or plasmonic structures that enhance the interaction between the THz radiation and the 2DEG, a modulation depth of 30% was achieved more recently. A more promising material for efficient THz modulation is graphene. Its carrier concentration can be electrically tuned to be as high as \( 1 \times 10^{14} \text{ cm}^{-2} \), and its natural bidimensionality and flexibility allow easy incorporation with other materials and structures. Recently a modulation depth of \( \sim 15\% \) was achieved in the 570–630 GHz frequency band through electrical gating of a graphene sheet, and this was increased to \( \sim 64\% \) through use of plasmonic or cavity structures, albeit with a narrow bandwidth. However, further increase of the modulation depth has proved difficult.

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unless by stacking multiple graphene layers. In addition, all the graphene modulators to date were studied as isolated components, with typically large active areas (tens of mm²) required to facilitate optical alignment. The consequent large time constant of the effective RC circuit of the device limited the modulation speed of such graphene modulators to only ∼13 MHz. Although this is similar to that found in semiconductor modulators, a much higher modulation speed ought to be possible in graphene-based modulators owing to the material’s ultrahigh intrinsic carrier mobility (>20 000 cm² V⁻¹ s⁻¹ for graphene on SiO₂ at room temperature).32

To explore the full potential of graphene, the monolithic integration of a graphene modulator with a THz radiation source is a promising solution. The benefits are threefold: first, miniaturization will increase the modulation speed owing to reduced parasitic capacitance and resistance of the device; second, a larger modulation depth may be achieved as a stronger interaction of the THz radiation with the graphene layer is possible; and, finally, the integration eliminates one stage of optical alignment and the associated bulky mirrors or lenses.

Here, we report, for the first time, the realization of graphene modulators integrated with surface-emitting concentric-circular-grating (CCG) THz quantum cascade lasers for achieving a 100% modulation depth with a fast modulation speed. By employing the CCG as a feedback element, steady single-mode THz QCL operation can be obtained with relatively high output power. We demonstrate that a 100% modulation depth can be achieved as a consequence of a strong interaction of the graphene with the laser field, which is greatly enhanced at the output apertures of the laser cavity. Moreover, the small device area of the device allows fast modulation that could be further improved through optimized design of the laser cavity and the modulator architecture. Furthermore, since graphene has a broadband absorption spectrum, our integration scheme can readily be scaled to other wavelength regions. For example, it can be easily extended to the mid-infrared (mid-IR) regime by monolithically integrating mid-IR QCLs with graphene. In addition, the proposed scheme will enable the realization of mid-IR and THz integrated optical circuits, combined with other photonic components such as detectors, waveguides, and filters, for communication, sensing, and spectroscopy applications.

■ DEVICE OVERVIEW

Figure 1a shows a schematic illustration of the integrated device, which consists of an underlying surface-emitting CCG THz QCL with a graphene modulator, the Fermi level of which can be dynamically tuned by a voltage (Vₓ) applied to the gating electrode. The active region of the QCL, with a peak gain at around 3 THz, is sandwiched between a bottom gold plate and the upper CCG metal grating. The CCG was designed as a second-order grating such that single-mode THz radiation will be emitted vertically through the grating.
apertures, which is then modulated by the electrically gated graphene. To facilitate graphene transfer, the active region of the QCL was not etched to keep the upper surface as flat as possible. Thus, the laser cavity is formed solely by the CCG itself. Additionally, only the central few rings of the CCG (the orange region in Figure 1a) are connected together with spoke-like metal bridges to allow electrical pumping over a small active region beneath. This restricted the otherwise high current in the QCL to only a few amperes. With the correct CCG design, the optical modes are confined in the pumped area so that the QCL maintains a sufficiently low threshold current for lasing action (see Supporting Information). On top of the CCG, a SiO$_2$ layer insulates the QCL electrode from the graphene gate electrode; this is followed by the graphene sheet. The device fabrication is assisted by patterning the graphene gate electrode before the introduction of the graphene sheet. Figure 1b shows optical microscope images of the central part of a fabricated device. The enlarged view in Figure 1c shows the details of the graphene and QCL electrodes, which are insulated by the SiO$_2$ layer. A wrinkle resulting from folding of the transferred chemical-vapor-deposition-grown (CVD) graphene is visible at the lower right corner.

**SEPARATE CHARACTERIZATIONS OF THE THz CCG QCL AND THE GRAPHENE**

We first characterized the THz CCG QCL with the graphene electrode floating. The QCL lased under pulsed operation (500 ns pulse width, 10 kHz repetition rate) up to a 102 K heat sink temperature (Figure 2a), compared with $\sim 135$ K for a typical ridge laser (200 $\mu$m wide and 1.5 mm long) fabricated from the same QCL wafer. Surface-emitting single-mode lasing was obtained at all temperatures and pump currents. Figure 2b shows the laser spectra as a function of pump current $I$, at 20 K. It shows a single-mode operation over the whole dynamic range of THz CCG QCLs.

Figure 2. Separate characterization of the THz QCL and the graphene layer. (a) Light−current−voltage (LIV) characteristics of the THz CCG QCL at different heat sink temperatures. (b) Laser spectra as a function of pump current $I$, at 20 K. It shows a single-mode operation over the whole dynamic range of THz CCG QCLs. (c) Schematic representation of the structure used to characterize the graphene layer. It is noted that the bottom gate metal layer under the graphene area was opened for THz beam transmission. (d) Direct current conductivity, carrier density, and Fermi energy of the graphene as a function of gate voltage, measured at 78 K. (e) Gate voltage dependence of the modulation of the THz transmitted intensity ($\sim 3$ THz) by the graphene, showing a modulation depth of $\sim 11\%$ over the applied bias range from $-40$ to 60 V. The effect of the silicon substrate on the experimentally measured modulation has been removed using a transfer matrix method. Before removing this substrate effect, the modulation depth is 17%.

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substrate, as shown schematically in Figure 2c, using the same CVD graphene sheet (see Methods). The 450 nm thick SiO2 layer was formed by plasma-enhanced CVD (PECVD) and was identical to that used for the QCLs. Raman spectroscopy was used to confirm that the graphene sheet after transfer was both high quality and a monolayer (Figure S2, Supporting Information). In view of the fact that the QCL-integrated devices will be operated under cryogenic conditions, we investigated the electrical and optical absorption properties of the graphene at 78 K (the QCL surface and active region are typically several tens of Kelvin higher than the heat sink temperature). Using a simple model to fit the gate-voltage-dependent sheet resistance of the graphene (see Supporting Information), we obtained the gate-voltage-dependent sheet conductivity, carrier density, and Fermi energy of the graphene, as plotted in Figure 2d. The inherent p-type doping of the CVD graphene sheet is confirmed by the reduction in conductivity with increasing gate bias, up to the Dirac point ($V_G \approx 50$ V). The graphene conductivity and carrier density were found to change from 0.16 mS to 0.65 mS and from $0.1 \times 10^{13}$ cm$^{-2}$ to $0.45 \times 10^{13}$ cm$^{-2}$, respectively, as the gate bias was increased from −40 V to +60 V. Correspondingly, the Fermi energy was tuned from −230 meV to +20 meV. The nonzero conductivity at the Dirac point is due to a residual carrier concentration of $0.1 \times 10^{13}$ cm$^{-2}$, resulting from charged impurities.36

Although the use of a back-gate structure, which features a relatively small capacitance, limits the range of carrier density and Fermi energy tuning possible (a top gating scheme could realize a carrier density as high as $10^{13}$–$10^{14}$ cm$^{-2}$),37 the tunability of the carrier density in graphene is still much larger than that achieved in 2DEGs arising from semiconductor heterostructures. As the optical absorption of graphene in the THz region is dominated by intraband optical transitions (i.e., free carrier absorption), this larger tunability in carrier density, along with the generally high mobility of graphene ($\sim 900$ cm$^2$ V$^{-1}$ s$^{-1}$ at 78 K in our case), makes graphene a much more efficient THz wave modulator than alternative semiconductor devices. Normalized to the maximum light transmission at the Dirac point, $T_{\text{Dir}}$, a modulation depth of $\sim 11\%$ in transmitted power ($T(V_G)/T_{\text{Dir}}$) was observed for our graphene modulator upon sweeping the gate voltage from −26 V to +40 V. (d) $V_G$ dependence of the output power of the CCG QCL with (circles) and without (rectangles) the graphene. The pumping current of the QCL is 2.80 A. (e) Light–current characteristics of the QCL as a function of $V_G$, confirming that a 100% modulation depth is achieved when the pumping current of the THz QCL is less than 2.78 A. For higher pumping current of the QCL (2.78–2.93 A), the THz radiation cannot be totally suppressed, but we can still obtain a modulation depth of 94% in the worst case (when the injection current to the QCL is $\sim 2.85$ A).
Figure 4. Measurement of the modulation speed of the integrated graphene modulator. (a) (i) Device bias scheme. The pulse duration for the QCL was fixed at $T_{\text{QCL}} = 1 \mu$s (corresponding to a frequency of $f_{\text{QCL}} = 1 \text{ MHz}$), while an ac rectangular signal was applied onto the graphene electrode with 50% duty cycle and various periods of $T_G = T_{\text{QCL}}/N$ ($f_G = Nf_{\text{QCL}}$), where $N$ is an integer. (ii) Predicted output optical signal of the device if the graphene modulator is able to follow the variation of the applied voltage. In this case, the average peak power $P_{av} = (P(V_{gr}) + P(V_{g})) / 2$, where $P(V_{gr})$ and $P(V_{g})$ are the output peak powers when a constant $V_{gr}$ or $V_g$ is applied to the graphene electrode, respectively. (iii) Predicted output optical signal of the device if the applied signal to the graphene is faster than the speed of the modulator, in which case $P_{av}$ deviates from $(P(V_{gr}) + P(V_{g})) / 2$. (b) $P_{av}$ as a function of modulation frequency $f_G$. The blue line (star symbols) corresponds to $V_g = 0 \text{ V}$ and $V_{gr} = 10 \text{ V}$, while the red line (circle symbols) corresponds to $V_g = 0 \text{ V}$ and $V_{gr} = 15 \text{ V}$. The gray-, blue-, and red-shaded ribbons indicate the output power when the graphene electrode is dc biased at 0, 10, and 15 V, respectively. The widths of the ribbons reflect the instability of laser power during the measurement period. (c) Frequency response of the graphene modulator.

Here, the effect of the Si substrate on the modulation was removed using a transfer matrix method, and the measured result agrees well with theoretical analysis (Figure 2e, see Supporting Information for details). It is worth noting that the optical absorption of graphene in the THz region of the spectrum differs fundamentally from that at visible and near-infrared frequencies, where interband optical transitions dominate, resulting in only a $\sim 2.3\%$ intensity modulation.

**INTEGRATED GRAPHENE MODULATION OF CCG QCLS**

A larger modulation strength is expected when the graphene is integrated with a THz CCG QCL owing to the electric field enhancement in the graphene near the output aperture of the QCL. Figure 3a plots the cross-sectional view of the calculated electric field distribution of the CCG QCL. As only the horizontally polarized component of the electric field ($E_r$) is responsible for the THz emission into the far field, we investigated the $E_r$ distribution around the CCG apertures, with a representative cross-sectional plot shown in the inset of Figure 3b. The curve in Figure 3b describes the $|E_r|$ field profile along the white dashed line of the inset, indicating a great enhancement of $|E_r|$ in the aperture region. For a SiO$_2$ spacing thickness of 450 nm, it is estimated that $|E_r|$ is enhanced by a factor of 12 in the graphene region, which corresponds to an intensity enhancement factor of $\sim 140$. The resulting enhanced modulating effect of graphene on the CCG QCL is shown in Figure 3c, where the intensity of the lasing peak varies from nearly zero at $V_g = -26 \text{ V}$ to a maximum at $V_g = +40 \text{ V}$. During measurement, the QCL was biased at 14.8 V (corresponding to an injected current of 2.80 A) in pulsed mode operation (500 ns pulse width, 10 kHz repetition rate) at a 20 K heat sink temperature, and the graphene was gated at a series of dc biases $V_G$ defined by $V_G = V_{\text{QCL}} - V_{gr}$, with $V_{\text{QCL}}$ being the voltage applied to the QCL electrode and $V_{gr}$ the voltage applied to the graphene electrode (see Figure 1a). The solid circles in Figure 3d show the average laser output power as a function of $V_G$, which is consistent with the results in Figure 2d and e. As a comparison, a control device without the graphene sheet was fabricated, and the output power is plotted as a function of $V_G$ as rectangles in Figure 3d, with no obvious modulation being observed. Note that in the presence of the graphene the output power decreases significantly; the power of the integrated device at $V_g = +40 \text{ V}$ is around a quarter of that from the control device. To verify the effect of the graphene modulator further, we measured the light–current curves of the laser at a series of graphene gate voltages, as shown in Figure 3e. As it indicates, for the pumping current of the THz QCL below 2.78 A, the integrated device allows a 100% modulation depth ($\Delta T/\Delta T_{\text{max}}$) of the THz radiation amplitude, as the emission vanishes when the graphene is biased with a large enough negative voltage. For higher pumping current of the QCL (2.78–2.93 A), the THz radiation cannot be totally suppressed, but we can still obtain a modulation depth of 94% in the worst case (when the injection current to the QCL is...
~2.85 \,\text{A}). It is worth mentioning that although the graphene was put above the cavity, it actually interacts with the evanescent waves of the cavity mode through the output apertures. Therefore, when gating the graphene at different voltages, its refractive index varies, leading to a slight change of the effective refractive index of the laser cavity and, thus, a slight shift of the lasing peak, as can be seen in Figure 3c.

**Modulation Speed of the Integrated Graphene Modulator**

Owing to the lack of suitable fast THz detectors, we cannot observe the time-varying THz modulated signal directly to determine the operational speed of the modulator. Therefore, the modulation speed is estimated by monitoring the average output power of the device while an ac voltage signal is applied to the graphene electrode, as shown in Figure 4a(i). The pulse duration for the QCL is fixed at $T_{\text{QCL}} = 1 \,\mu\text{s}$ (corresponding to a frequency of $f_{\text{QCL}} = 1 \,\text{MHz}$), while the ac rectangular signal on the graphene has a 50% duty cycle and a period of $T_G = T_{\text{QCL}}/N \,(f_{\text{G}} = N f_{\text{QCL}})$, where $N$ is an integer. If the graphene modulator can follow the variation of the applied voltage, the output optical signal of the device will be as that shown in Figure 4a(ii), and the average power ($P_\text{av}$) detected experimentally should be $(P(V_p) + P(V_0))/2$ regardless of the modulation frequency, where $P(V_p)$ and $P(V_0)$ are the output peak powers when constant gating voltages $V_p$ and $V_0$ are applied to the graphene electrode, respectively. Otherwise, as illustrated in Figure 4a(iii), $P_\text{av}$ will deviate from $(P(V_p) + P(V_0))/2$. Therefore, one could expect a flat $P_\text{av}$ vs $f_{\text{G}}$ curve up to a cutoff point, where the corresponding $f_{\text{G}}$ is approximately the modulation speed of the device. The measured $P_\text{av}$ vs $f_{\text{G}}$ curve is shown in Figure 4b, in which the blue line (star symbols) corresponds to $V_0 = 0 \,\text{V}$ and $V_p = 10 \,\text{V}$, while the red line (circles) corresponds to $V_0 = 0 \,\text{V}$ and $V_p = 15 \,\text{V}$. The gray-, blue-, and red-shaded ribbons indicate the output powers when the graphene electrode is dc biased at 0, 10, and 15 V, respectively. The widths of the ribbons indicate the instability of the laser power during the measurement period. A flat dependency was observed up to 12 MHz, the limit of our experimental facilities, with no cutoff point, which already makes it one of the fastest THz modulators. To extend the measurement range, we investigated the dynamic response ($S_{\text{nn}}$) using a radio frequency (RF) network analyzer. Using this together with an equivalent circuit model, we obtained the frequency response of the integrated modulator (Figure 4c; see Supporting Information for details). The modulation speed can therefore be estimated to be 110 MHz from the 3 dB cutoff point.

The electrical modulation on the graphene sheet is given by (see Supporting Information)

$$\frac{V_G}{V_s} = \frac{1}{1 + i\omega R_G C_p + R_G/(R_G^\prime + 1/i\omega C_G^\prime)} \times \frac{1}{1 + i\omega R_G^\prime C_G^\prime} \approx \frac{1}{1 + i\omega R_G(C_p^\prime + C_g^\prime)} \times \frac{1}{1 + i\omega R_G^\prime C_G^\prime}$$

where $V_G$ and $V_s$ are the amplitude of the voltage on the graphene electrode and that applied to the graphene sheet, respectively, $R_G$ is the internal impedance of the RF source (50 $\Omega$), $R_G^\prime$ is the effective graphene resistance, $C_G$ and $C_p$ are the total capacitance of the graphene sheet and the metal contacts, respectively, and $\omega$ is the angular frequency of the modulation. In eq 1, we assumed $R_G^\prime \ll 1/i\omega C_G^\prime$ for our case. Two time constants, $\tau_1 = R_G(C_p^\prime + C_g^\prime)$ and $\tau_2 = R_G^\prime C_G^\prime$, then determine the cutoff frequency. The first time constant can be decreased by reducing the size of the graphene back gate (i.e., the QCL bias contact), which requires a smaller cavity design. The second time constant can be decreased by reducing the widths of the graphene electrode slits (this makes the effective area of the graphene sheet smaller so that the graphene capacitance is smaller) and by reducing the graphene resistance. The graphene resistance is dominated by the contact resistance at the metal/graphene edges and can be reduced though several techniques reported in the literature.$^{38-40}$

**Discussion**

For QCLs, direct modulation of the laser itself can be very fast by microwave injection (>10 GHz for ridge-waveguide device$^{41}$). However, in this direct modulation case, as the pumped current and voltage keep changing, the gain profile and the refractive index, as well as the temperature, of the active region are varying rapidly, making the laser frequency fluctuate, i.e., the frequency chirping effect. Our scheme could allow the laser to operate more stably because now the modulation is performed by changing the graphene voltage, but not the laser. Although our devices do not totally get rid of the chirping effect—after all, the frequency shift in Figure 3c is perceivable—it could be expected that they have a smaller chirping effect since the effective refractive index change induced by the gating graphene is much smaller than that induced by the modulating gain medium. Therefore, our scheme may be advantageous in applications where the chirping effect is not desired. In addition, our device may also be used as a whole as a THz modulator for free-space light modulation with the active region of the QCL unpumped or pumped below the threshold, so that it is suitable for many other occasions where their own light sources are used.

**Conclusions**

We have reported a THz graphene modulator, monolithically integrated with a surface-emitting CCG QCL, that shows a modulation depth in the range of 94–100% and a response speed of 110 MHz. The high modulation depth is a consequence of a strong interaction of the graphene with the laser field, which was further enhanced at the output apertures of the laser cavity, while the high modulation speed is due to the reduced device area enabled by the integration. Even faster operation frequency could be achieved through further improvements to the device architecture. Our integration scheme can also be applied to the mid-infrared and near-infrared frequency ranges, as the optical absorption of graphene is naturally broadband.

**Methods**

**Preparation of the Graphene Film.** The commercially sourced CVD-grown graphene on copper foil was spin-coated with a poly(methyl methacrylate) (PMMA) film, which was then fully cured in a 110 °C oven for 5 min, resulting in a PMMA thickness of ~1 μm. The copper substrate was etched by floating the PMMA/graphene/copper sheet on an ammonium persulfate (0.1 M, Sigma-Aldrich) solution for >3
h. After rinsing, the PMMA/graphene film was ready for transfer.

Fabrication of the Isolated Graphene Modulator. A 450 nm thick layer of SiO$_2$ was blanket deposited on a lightly doped p-type Si substrate (resistivity 1–20 Ω·cm) using PECVD. The source, drain, and back electrodes were formed by electron-beam evaporation, after which the PMMA/graphene film (1 cm × 1 cm) was transferred and contacted with source and drain electrodes. The sample was dried in air, followed by annealing in nitrogen at 160 °C for 3 h. The PMMA layer was then removed in acetone.

Fabrication of the Integrated Devices with Graphene Modulator and CCG QCL. The active region of the THz QCL was grown by molecular beam epitaxy on an undoped GaAs substrate. Fabrication of the devices commenced with gold–gold thermocompression bonding of the active region to an n+ GaAs receptor wafer. The original QCL substrate was then removed through lapping and selective chemical etching. This was followed by the removal of the highly absorbing contact layer of the active region to prevent attenuation of the THz radiation that couples out of the grating slits. Top metal gratings (Ti/Au/Ti 15/300/10 nm) were defined by standard optical lithography and lift-off; the top 10 nm Ti layer was used as an adhesive between the Au and the subsequent SiO$_2$ insulation layer, which was grown by PECVD. After patterning the SiO$_2$ layer to allow electrical access to the QCL, another optical lithography and lift-off process was carried out to define the graphene electrode on top of the SiO$_2$/CCG rings. A graphene sheet was then transferred onto the graphene electrode, followed by annealing in nitrogen at 160 °C for 3 h to relax the PMMA/graphene film slowly and make full contact with the surface underneath. After removing the PMMA layer with acetone, the graphene was patterned to remove unwanted material area and avoid contacting the other electrodes. The samples were then cut and island-mounted onto Cu submounts, wire-bonded, and finally attached to the coldfinger of a cryostat for measurement.

## ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsphotonics.5b00317.

Detailed structure parameters of the THz CCG QCL and its far-field characterization; Raman spectra of the transferred graphenes; model used to retrieve the graphene parameters (carrier density, Fermi level, etc.) from electrical characterization; comparison of the graphene optical response at 78 and 300 K; high-frequency circuit model of the graphene modulator (PDF)

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G.Z.L. and Q.J.W. wrote the manuscript. A.G.D. and E.H.L. revised the manuscript. H.K.L., Y.Z., and S.F.Y. improved the manuscript presentation. All authors reviewed the manuscript.

Notes

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