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Abstract 9

10 The 1999 jökulhlaup at Sólheimajökull was the first major flood to be routed through the proglacial system in over 600 years. This study reconstructed the flood using hydrodynamic, sediment transport and morphodynamic 11 numerical modelling informed by field surveys, aerial photograph and digital elevation model analysis. Total 12 modelled sediment transport was 469,800 m³ (+/- 20 %). Maximum erosion of 8.2 m occurred along the ice 13 margin. Modelled net landscape change was -86,400 m³ (+/- 40 %) resulting from -275,400 m³ (+/- 20 %) 14 proglacial erosion and 194,400 m³ (+/- 20 %) proglacial deposition. Peak erosion rate and peak deposition rate 15 were 650 m^3s^{-1} (+/- 20 %) and 595 m^3s^{-1} (+/- 20 %), respectively, and coincided with peak discharge of water at 16 17 1.5 hours after flood initiation. The pattern of bed elevation change during the rising limb suggested widespread 18 activation of the bed, whereas more organisation; perhaps primitive bedform development, occurred during the 19 falling limb. Contrary to simplistic conceptual models, deposition occurred on the rising stage and erosion 20 occurred on the falling limb. Comparison of the morphodynamic results to a hydrodynamic simulation illustrated 21 effects of sediment transport and bed elevation change on flow conveyance. The morphodynamic model 22 advanced flood arrival and peak discharge timings by 100 % and 19 %, respectively. However, peak flow depth 23 and peak flow velocity were not significantly affected. We suggest that morphodynamic processes not only 24 increase flow mass and momentum but that they also introduce a feedback process whereby flood conveyance 25 becomes more efficient via erosion of minor bed protrusions and deposition that infills or subdues minor bed hollows. A major implication of this study is that reconstructions of outburst floods that ignore sediment 26 transport, such as those used in interpretation of long term hydrological record and flood risk assessments, may 27 need considerable refinement. 28

Keywords: GLOF; outburst flood; glacier flood; erosion; deposition; proglacial; 29

30 Introduction

Jökulhlaups (glacier outburst floods) are a sudden outburst of water from a glacial source. These high-magnitude 31 yet relatively infrequent floods can be effective agents of subglacial and proglacial erosion and deposition, 32 causing intense and widespread geomorphological change (Baker, 1996; Björnsson, 2009; Carrivick, 2009). The 33 frequency and potentially the magnitude of jökulhlaups is predicted to increase with climate change and glacier 34 retreat (Pagli and Sigmundsson, 2008; Richardson and Reynolds, 2000; McGuire, 2013; Carrivick and Tweed, 35 36 2013) thereby placing more persons and infrastructure at risk from outburst floods. Understanding when, how 37 and why proglacial erosion and deposition occurs during jökulhlaups is therefore crucial for hazard mitigation 38 and landscape management.

39 The rapid onset of flooding and the short length of time to peak discharge are both characteristics of jökulhlaups 40 and are key reasons why they are poorly understood (Rushmer et al. 2002; Carrivick and Rushmer, 2006; 41 Rushmer, 2007). Direct measurement of flow conditions during jökulhlaups is exceptionally difficult, due to 42 high flow velocities, high flow energy and the sheer volume of water and sediment transported. Furthermore, 43 jökulhlaups tend to occur in remote regions where monitoring and access are limited. Current understanding of jökulhlaup processes and products is therefore largely based on (i) qualitative conceptual models developed from 44 45 sedimentary studies (e.g. Maizels, 1989a, 1989b, 1991), (ii) geomorphological evidence either from field measurements (Russell et al., 2006) or from remote sensing (e.g. Smith et al., 2006), or (iii) from application of 46 numerical models. 47

48 Numerical models applied at the field (landscape) scale to the routing, propagation and proglacial hydraulics of 49 jökulhlaups and other types of outburst flood can be categorised between 1D and 2D types (Table 1). A limitation of 1D models is that hydraulic parameters are calculated based on prescribed channel cross-section 50 positions. In contrast, 2D models can accommodate the complexity of time-transgressive flow typical of outburst 51 52 floods; flow splitting around islands; transcritical flow, and they can parameterise secondary flow circulation 53 such as is common within major topographical embayments, for example (Carrivick, 2007). However, both 1D 54 and 2D models are capable of accommodating vertical channel changes; i.e. morphodynamics, i.e. erosion and 55 deposition of sediment. Inclusion in numerical modelling of sediment transport and particularly of 56 morphodynamics for real world field-scale outburst floods is very rare but include Carrivick et al., (2011), Worni et al. (2012) and Huang et al. (2014), for example. At the experimental scale, numerical fluid dynamics-57 based models of sediment transport in outburst floods (e.g. Xia et al., 2010) and morphodynamics (e.g. 58

Swartenbroekx et al., 2013) are rare and underdeveloped; spatio-temporally variable rheology, bank and bedrock
erosion for example have yet to be mechanistically included.

Previous studies on other types of outburst floods unequivocally demonstrate that inclusion of sediment transport 61 and morphodynamics in modelling of the flow is important because: (i) outburst floods often undergo 'bulking' 62 and 'dilution' due to rapid sediment entrainment and deposition, respectively (e.g. Lube et al., 2012), (ii) 63 entrained sediment affects the mass and momentum energy of a flow (e.g. Fraccarollo and Capart, 2002; Zech et 64 65 al., 2008; Carrivick, 2010; Carrivick et al., 2011; Iverson et al., 2011; Guan et al. 2014, 2015) (iii) erosion and 66 deposition changes channel geometry, on occasion by over 100 % in a few minutes (e.g. Carrivick et al., 2011), 67 and crucially these three individually and in combination feedback to perturb hydraulics (e.g. Guan et al., 2014, 68 2015). Furthermore, (iv) sediment transported in a flow can constitute the major hazard associated with outburst floods, impacting structures and burying property, for example. 69

70 Flume experiments of outburst floods with mobile sediment (e.g. Capart and Young, 1998; Fraccarollo and 71 Capart, 2002; Pritchard and Hogg, 2002; Cao et al., 2004; Rushmer, 2007; Wu and Wang, 2007; Zech et al., 72 2008; Emmett and Moodie, 2008; Xia et al., 2010) have emphasised grain-scale erosion and deposition by 73 outburst floods. Whilst several of these experimental studies have informed development of numerical 74 morphodynamic outburst flood models the experiments have been idealised, for example very simple channel 75 geometry, regular-shaped (spherical) particles. Furthermore, with the exception of the work by Guan (2013), they have not been tested at the field scale, which is typically hundreds of metres channel width and many 76 77 kilometres long. This means that it is unknown whether the grain-scale understanding represented in present 78 theoretical morphodynamic outburst flood models is applicable at the field (landscape) world (Table 1). The only 79 'real-world' applications of fluid sediment transport models to glacial outburst floods, has been that of a multi-80 phase model; which includes both fluid and granular phases and interactions between them, for the 1994 flood 81 from Lugge Lake in Bhutan by Pitman et al. (2013), and a parallelised 2D hydrodynamic model with coupled 82 sediment transport for the Altai megaflood, by Huang et al. (2014). Overall, numerical computations of (glacial 83 and other) outburst floods are challenging because they must accommodate: (i) highly transient hydraulics, (ii) extreme wetting and drying, (iii) highly irregular topography, and (iv) time-transgressive topography due to 84 85 erosion and deposition. We note that morphodynamic models have been applied elsewhere in fluvial geomorphology studies. 86

The aim of this study is to apply a morphodynamic model to a real-world glacial outburst flood or 'jökulhlaup',
to quantify in unprecedented detail spatiotemporal sediment transport and geomorphological change.
3

Specifically, we compare 'real' surface changes, as measured by digital elevation models of difference, against numerical morphodynamic model results. Our research question is 'what difference does inclusion of morphodynamics have on outburst flood model output hydraulics, sediment transport and geomorphological work?' Our working hypothesis is that it is crucial to include sediment transport and morphodynamics in field (landscape) scale applications of models for: (i) improved understanding of outburst flood processes and; (ii) for realistic simulations.

95 Study site

96 Sólheimajökull is an 8 km long non-surging outlet glacier of Mýrdalsjökull in southern Iceland (Fig. 1). 97 Mýrdalsjökull is located at the south-east end of the 'neovolcanic' zone (Jaenicke et al., 2006) and overlays the 98 Katla central volcano. Of the 16 volcanic systems active in Iceland since 870 AD (Gudmundsson et al., 2008), the Katla system is the second most active and one of the most hazardous (Jónsdottir et al., 2007; Scharrer et al., 99 100 2007). Sólheimajökull was selected as the study site for two main reasons. Firstly, this site, like many of the Icelandic glaciers and sandar has been repeatedly photographed since the mid-20th Century. Aerial photographs 101 therefore exist both pre- and post-jökulhlaup, enabling the construction of high-resolution and high-precision 102 103 digital elevation models (DEMs). Secondly, the proglacial channel system has been exposed to high-magnitude 104 low-frequency glacier outburst floods throughout the Holocene (Maizels, 1991); the 1999 jökulhlaup was the 105 first major flood to route through Sólheimajökull in over 600 years (Russell et al., 2010).

106 Volcanically-triggered jökulhlaups have occurred at least 17 times since 900 AD (Maizels, 1992; Jónsdottir et 107 al., 2007). The route taken by these jökulhlaups draining from Katla has been determined by the location of the eruption centre, which has migrated over time (Mountney and Russell, 2006; Smith and Dugmore, 2006). 108 Consequently, volcano-glacial jökulhlaups have drained from Mýrdalsjökull along a number of different routes. 109 Eight major jökulhlaups occurred at Sólheimajökull between 4.5 ka BP and the mid-14th Century; after this, the 110 eruption centre of Katla migrated and jökulhlaups were routed through Kötlujökull and across Mýrdalssandur 111 112 towards the east (Fig. 1). The river flowing from Sólheimajökull, the Jökulsá á Sólheimasandi (abbreviated to 'Jökulsá') flows southwards from the glacier terminus to the North Atlantic Ocean, a distance of ~ 9 km. For 113 114 most of its length, the Jökulsá is confined to an incised channel that cuts through the extensive outwash deposits of Sólheimasandur and Skógasandur. The sandur deposits are arranged in terraces and fans extending 115 116 southwards from Mýrdalsjökull.

117

118 The 1999 jökulhlaup

119 The July 1999 was triggered by subglacial volcanic activity within the Katla caldera, which underlies 120 Mýrdalsjökull (Russell et al., 2010) and included drainage of an ice-dammed lake as predicted by Tweed (1998). The 1999 jökulhlaup presents an opportunity for improving understanding of the impact of high-magnitude 121 122 outburst floods and associated geomorphological impacts in proglacial environments because: (i) inundation extent was directly observed, (ii) peak-discharge estimates were made at the Jökulsá bridge (Sigurðsson et al., 123 124 2000; Fig. 1) and (iii) immediate geomorphological impacts were recorded (Russell et al., 2002b; Russell et al., 125 2000; Russell et al., 2010). These field measurements and observations constrain some of the palaeohydraulic reconstructions presented in this study. 126

127 Renewed volcanic activity was apparent in the days prior to the 1999 flood when the water flowing through the 128 Jökulsá á Sólheimasandi changed turbidity (Sigurðsson et al., 2000) and 15 supraglacial cauldrons developed indicating subglacial melting (Russell et al., 2000). Seismic tremors were recorded up to five hours before the 129 130 release of the jökulhlaup with the peak in seismic activity coinciding with the onset of flooding around 02:00 on the 18th July (Roberts et al., 2003). Water travelled beneath the glacier as a subglacial wave (Russell et al., 2006) 131 and exited from Sólheimajökull at several locations. Four kilometres up-glacier from the glacier terminus, water 132 133 burst out at the western margin and flowed along the glacier edge where two temporary ice-dammed lakes 134 formed (Russell et al., 2002); one 3.7 km from the terminus and the other in Jökulsárgil (Tweed, 1998). Water 135 also burst through the ice-surface 2 km up-glacier from the terminus, draining supraglacially (Russell et al., 2000). Meltwater exited onto the proglacial zone through a 150 m wide conduit at the western margin of the 136 terminus and also through a conduit at the centre of the terminus. Proglacially, the jökulhlaup was predominantly 137 confined to the main river channel although over-bank flow led to the reactivation of some ice-proximal palaeo-138 139 channels (Russell et al., 2002a, b).

The rise to peak discharge was rapid with 1,700 m³s⁻¹ reported by Sigurðsson et al. (2000) as recorded 4 km downstream at the bridge (Figure 1) just one hour after jökulhlaup initiation (Sigurðsson et al., 2000). Peak discharge at the glacier terminus has been estimated at 4,780 m³s⁻¹ from the size of boulders and the velocity required to transport them (Russell et al., 2010) but there must be uncertainty of at least \pm 250 m³s⁻¹ on this value due to the range of results from the different methods used by Russell et al. (2010). The jökulhlaup was relatively short-lived; flow levels at the bridge had returned to base-level after approximately 6 hours (Sigurðsson et al., 2000; Roberts et al., 2003).

Present understanding of the geomorphological impact of the 1999 flood can be summarised to be that 147 deposition occurred in supraglacial, ice-marginal and proglacial locations (Russell et al., 2000), with the greatest 148 impact in the ice-proximal zone. A small delta formed in an upper lake basin with sediment depths around 0.1 -149 0.5 m thick (Russell et al., 2002a, b). These sediments showed evidence of scouring by ice blocks, indicating 150 strong circulation of shallow flows (Russell, et al., 2002a). In the proglacial area, up to 6 m of sediment were 151 deposited, the source of which was predominantly subglacial excavation (Russell et al., 2000). A 1,200 m² 152 boulder fan was deposited in front of the western side of the glacier terminus with boulders > 10 m in diameter 153 154 (Russell et al., 2010).

155 Methods

Each palaeohydraulic modelling technique has its own assumptions and limitations, so several were used in this study in combination with field-based surveys, aerial photograph analysis and terrain analysis to reconstruct sediment transport and geomorphological impact.

159 Palaeocompetence measurements

160 Clast measurements focussing on the largest clasts only were made at the ice-proximal boulder fan for the 161 purpose of reconstructing flow velocity using the palaeocompetence method. This method is based on 162 relationships between incipient clast motion, clast entrainment and flow velocity (Costa, 1983). However, whilst such techniques enable estimates to be made on flow velocity, shear strength and viscosity (Maizels, 1989b), 163 they are based on flume experiments with gravel < 35 mm, assume an unlimited sediment supply (calibre and 164 volume), are assumed to pertain to peak discharge, and are restricted to at-a-point in space, so must be used with 165 extreme caution (e.g. Carrivick et al., 2013b). With these limitations and assumptions in mind, the 166 palaeocompetence method was used in this study only to give independent comparison with the hydrodynamic 167 and morphodynamic modelling. The a, b and c axes lengths of 395 boulder clasts were measured on the ice-168 proximal boulder fan; these clasts were selected subjectively but with an aim to cover the whole fan area and to 169 preferentially sample the largest clasts to provide a minimum estimate of spatially-distributed flow competence. 170 The length of the intermediate axis of each boulder clast was used to reconstruct flow velocity (v), shear stress 171 (τ) and stream power (ω) using the equations of Costa (1983). The channel slope near the boulder fan was 172 173 0.0275 m/m (Russell et al., 2010). Proglacial hydraulic roughness was estimated at Manning's n = 0.05 during field surveys and this agrees with that in Fig. 9 of Russell et al. (2010). To maintain consistency and to permit 174

inter-model comparisons, the same value of Manning's n was used for palaeocompetence reconstructions and for

176 hydrodynamic and morphodynamic modelling.

177 Morphodynamic modelling

178 Morphodynamic modelling was used to reconstruct spatiotemporal flow hydraulics, sediment transport and geomorphological impact and specifically utilised depth-averaged modelling within (the now open source) 179 Delft3D (Delft Hydraulics) model software. This model is a multi-dimensional hydrodynamic and 180 181 morphodynamic simulation programme that is numerically stable for unsteady flow conditions. It solves the Navier–Stokes equations for an incompressible fluid under the shallow water and the Boussinesq assumptions. 182 The former of these assumptions reduces the vertical momentum equation to a hydrostatic pressure equation and 183 the latter assumes that momentum transfer caused by turbulent eddies can be represented with a user-specified 184 eddy viscosity value. The key model equations are given elsewhere; by Lesser et al. (2004) and by Carrivick et 185 al. (2009) for example but here it is important to note that this is a fluid model not a multi-phase model. 186 Furthermore, there is no bank erosion in terms of 'mass failure', only grain by grain entrainment and deposition. 187 188 Depth-averaged simulations were preferred over 3D modelling because horizontal flow conditions were 189 expected to predominate over vertical motion and were of greater interest in this study.

190 Computational domain and mesh formation

191 Model equations were formulated on an orthogonal curvilinear mesh, which was defined in spatial extent, shape 192 and spatial resolution by the same properties of terrain elevation points extracted from panchromatic black-and-193 white stereo-pair aerial photographs in digital format (having been photogrammetrically scanned at 15 microns 194 or 1800 dpi) with a ground pixel size of < 1 m. Pre-flood aerial photographs were taken in August 1996 and post-flood aerial photographs date from August 2001. Both sets were sourced from Landmaelingar Islands 195 196 (LMI) and orthorectified in Leica Photogrammetry Suite (LPS) with ground control points (GCPs) generated using a Leica GPS500 dual phase differential Global Positioning System (dGPS). Although it is acknowledged 197 198 that some parts of the landscape could have changed slightly in the 3 years between the pre-flood aerial photograph survey and the 1999 jökulhlaup it was considered preferable to use a pre-flood terrain model rather 199 200 than a post-flood landscape, as is often the case in jökulhlaup reconstructions. Indeed, other studies should note that quantifying sediment transport and geomorphological impact of jökulhlaups and of other outburst floods 201 202 will be very difficult if only a post-flood landscape terrain model is available.

The pre- and post-flood Digital Elevation Models (DEMs) had regular grid cells of size ~ 2m. DEM errors and 203 204 uncertainty was assessed by comparing grid cell values to dGPS-derived spot elevations and to a DEM constructed from a summer 2010 airborne LiDAR survey, which for our purposes we assumed had no error. 205 Uncertainty in our photogrammetrically-derived 1996 and 2001 DEMs was assessed by automatically defining 206 207 400 random points sampled across each DEM, the dGPS and the LiDAR datasets and only in areas suspected not 208 to have changed in elevation; i.e. excluding the glacier and the proglacial braidplain. Comparisons of the elevations of these 400 points revealed a heterogeneous error, and were used with inverse distance weighting 209 interpolation to generate an error surface, which was then used to correct the two DEMs (Staines et al., 2014). 210 Errors were greatest in steeper and more rugged areas, as expected (e.g. Hopkinson, Hayashi and Peddle 2009; 211 212 Huggel et al. 2002), although we think that a proportion of these 'errors' could indeed have been real landscape change in the form of hillslope activity. Final 1996 DEM error was quantified with mean elevation difference of 213 214 -0.03 m and RMSE of 0.89 m, and final 2001 DEM error was quantified with mean elevation difference of 0.002 m and RMSE of 1.24 m (Staines et al., 2014). Assessment of uncertainty in our volume calculations follows the 215 216 method of Lane et al. (2003) whereby we use 'unthresholded' DEMs of difference, because differences below 217 the level of detection are uncertain, and where volumetric uncertainty, σ volume, as considered when producing DEMs of difference (DoDs) is calculated as follows: 218

σ volume = $d^2 \sqrt{n} \sigma DoD$

219 where d is raster cell size, n is number of raster cells for which the DEM of difference is calculated, and σDoD is the error of the DEM of difference as given by $\sqrt{\sigma_D EM \# 1^2 + \sigma_D EM \# 2^2}$, where σ is the standard deviation of 220 residuals. This method indicates that when we differenced the 1996 and 2001 DEMs uncertainty in our elevation 221 values was 1.53 m and in our volume changes was 0.009 km³ (Staines et al. 2014). However, we consider these 222 223 uncertainty values to be a 'worst case scenario' because: (i) the quality of photogrammetry-derived DEMs is best 224 in areas of low relief and high-contrast, such as proglacial areas, and; (ii) as Staines et al. (2014) show in their 225 Table 2 whilst absolute elevation error in the proglacial area cannot be assessed, because it cannot be certain that 226 those points are static, volumetric uncertainty over the valley floor is approximately half that of the DEM in its 227 entirety.

228 Spikes and sinks were removed and the terrain 'inverted' in ArcGIS to produce a bathymetric xyz file (i.e. 229 positive elevations beneath 0 m) for the model. The x and y coordinates in this file demarked an extent and shape 230 around which user-specified splines crudely defined the mesh shape (Fig. 2) and were then refined automatically to give an orthogonal curvilinear mesh (Fig. 2) with each mesh cell resolution ~ 2 m in the lateral direction and \sim

10 m (at most ~ 15 m) in the longitudinal direction. To reduce file sizes and hence computation times, the mesh

233 was clipped to the extent of the main river channel (Fig. 2), as observations during the jökulhlaup established

that flow was confined to this channel (Sigurðsson et al., 2000). The bathymetry xyz points were mapped onto
the mesh (Fig. 2) using the Delft3D QUICKIN module using grid-cell averaging.

236 Input data to numerical model

The model proglacial channel was 'pre-wetted' by running base flow (without sediment transport or morphological updating) up to 90 m³ s⁻¹ which is the bankfull discharge under 'normal' flow conditions at the bridge (Lawler, 1994; Lawler and Brown, 1992). Hydraulic conditions at the last time-step of the baseflow model were used as the input ('restart') file for the jökulhlaup model.

241 Water discharge was introduced to the jökulhlaup model at both the western side of the glacier terminus and at 242 the terminus centre. These positions were chosen on the basis of field observations of the main glacial drainage 243 conduits at the time of the flood (Russell et al., 2002b; Russell et al., 2000; Russell et al., 2010). Field observations (Matthew Roberts, pers. comm.; Russell et al., 2010) indicated that the western conduit was the 244 245 main drainage channel both before and during the 1999 jökulhlaup and therefore we defined 40 % of the total 246 discharge exited from at the central conduit and 60 % from the western conduit (Fig. 3). The jökulhlaup model initial hydrograph (Fig. 3) was best-fit to the magnitude (1,700 m³s⁻¹) and timing (one hour after initiation) of 247 peak discharge, and flood volume, as recorded 4 km downstream at the bridge (Sigurðsson et al., 2000; Roberts 248 et al., 2003). In more detail, the jökulhlaup model input hydrograph peak discharge, duration and shape (Fig. 3) 249 was based on: measurements of river stage and discharge of 1700 m³ s⁻¹ made at the bridge by Sigurðsson et al. 250 251 (2000); the peak discharge estimates of Russell et al. (2010) and; knowledge of the flood trigger. Russell et al. (2010) suggested that downstream flow attenuation was considerable but we regard that the input discharge of 252 $4,000 \text{ m}^3\text{s}^{-1}$ as reconstructed by Russell et al. (2010) is rather high for our usage because we had to run the model 253 with no sediment input at the discharge point. Russell et al.'s (2010) boulder fan evidences that boulder-sized 254 clasts were moved, implying rapid deposition because very few boulders occur farther downstream. However, 255 256 neither the total volume nor the temporal flux of this subglacially-derived sediment transport is known and cannot even be reasonably estimated. Therefore, our jökulhlaup model was necessarily run with no subglacially-257 derived sediment. Thus to be clear, our modelled flow was initially 100 % water because any sediment in the 258 259 model is that from the proglacial area only.

The model time-step was set at 0.005 minutes to accommodate rapidly varying hydraulics and rapidly varying channel bathymetry. Horizontal eddy viscosity was defined at 0.01 m²s⁻¹ and the horizontal eddy diffusivity at 10 m²s⁻¹; both of these parameters affect advection of mass and momentum and concern momentum transfer caused by turbulent eddies but scale depending on mesh cell size. Whilst there is little advice on setting eddy viscosity and eddy diffusivity values, over a braided gravel bed river reach Williams et al. (2013) found that an eddy viscosity of 0.01 m²s⁻¹ produced model errors in terms of depth and velocity that agreed well with independently-measured field data.

267 Model sensitivity was assessed against peak discharge magnitude and timing (at the bridge), which are the only 268 measured and thus relatively certain properties of the 1999 jökulhlaup. However, modelled peak discharge 269 magnitude and timing was sensitive to roughness, which we defined with Manning's n (Fig. 4). Figure 4, which 270 illustrates a cross-section near the downstream model boundary, demonstrates that varying Manning's n does not 271 produce a linear response in discharge, and this is because of the morphodynamic part of the model and 272 feedbacks between sediment entrainment and flow hydraulics, as partly suggested by the response of bed elevation change to varying Manning's n (Fig. 4). Therefore, bed roughness was defined as a uniform value of 273 274 0.05 across the whole mesh, with respect to the channel substrate that we have observed in the field and as has 275 been reported by Russell et al. (2010). We note that Manning's n values used for other proglacial areas 276 comprising sand to cobble sized materials has varied from 0.04 to 0.06 (Alho and Aaltonen, 2008). For interest, 277 the model was not sensitive to other user-specified parameters including mesh resolution and grain size 278 distribution, in agreement with the findings of model (in)sensitivity by Guan, (2013) and Huang et al. (2014).

279 For the purposes of modelling sediment transport, three sediment fractions were defined on the basis of the sedimentological observations reported by Russell et al. (2010) and our own sedimentological analysis (Staines 280 et al. 2014). These sediment fractions were: boulders ($D_{50} = 400 \text{ mm}$); cobbles ($D_{50} = 100 \text{ mm}$) and; granules 281 $(D_{50} = 3 \text{ mm})$, all with specific density of 2680 kg.m⁻³, which is typical for the basalt-dominated geology. Non-282 283 cohesive suspended sediment transport was computed by solving the 3D advection-diffusion (mass-balance) 284 equation and by imposing a reference concentration at a reference height following the method of van Rijn (1993). Bedload was computed in two stages: (i) calculating transport magnitude and direction at mesh cell 285 centres using the Meyer-Peter-Müller (1948) 'MPM' equation for bedload, and; (ii) computing bedload transport 286 rates at cell interfaces. We note that the MPM formulae was developed via flume experiments and thus its 287 288 applicability for the range of sediment sizes observed in the field is questionable, but there is no alternative equation suitable for coarse sediment transport. The MPM formulae was implemented in Delft3d using the mean 289

290 grain size from the fraction being considered. An option in Delft3d for considering 'hiding and exposure' effects 291 by adjusting the effective critical shear stress for fine-grained sediments whilst lowering it for coarse sediments 292 was not used in this study because of the lack of information on a suitable multiplicative factor to use.

293 Suspended sediment transport included consideration of suspended sediment on fluid density, settling velocity, interaction of bed sediment fractions and inclusion of a fixed layer. In overview, the transport of suspended 294 sediment was calculated by solving the three-dimensional advection-diffusion (mass-balance) equation for the 295 296 suspended sediment. Density effects of suspended sediment fractions in the fluid mixture were recognised by 297 adding (per unit volume) the mass of all sediment fractions, and by subtracting the mass of displaced water. The 298 settling velocity of the (non-cohesive) sediment fractions were computed depending on the diameter of the 299 sediment in suspension. Sediment transfer between the bed and the flow was modelled using sink and source 300 terms acting on the near-bottom layer. The mathematical form of these sediment transport calculations are given 301 by Carrivick et al. (2010) and so are not repeated here for brevity.

302 An initial bed thickness of 5 m was defined for each sediment fraction, set as uniform across the computational 303 mesh, and based on (i) representative GPR surveys in the vicinity of the river channel of sediment thickness and (ii) sediment exposures in river banks (Staines et al., 2014). Note that there was no consideration in the model of 304 305 the stratigraphy of these sediments; all fractions were available in all three layers and all grains were available 306 for entrainment simultaneously. The total of 15 m sediment depth was not exhausted by the model, which seems sensible given that there are no bedrock sections of the river. The downstream boundary of the model at the 307 308 Jökulsá estuary is tidal (Mountney and Russell, 2006) and so was defined as 'open' with 'uniform water level' 309 set as 0 m.asl. Downstream boundary tide water level changes were assumed to be negligible due to the short 310 time-frame of modelling.

Morphodynamics were modelled by considering that if there was sediment deposition of y (m) within a grid cell of z m.asl. at timestep 'x', then that grid cell was updated accordingly to give a sediment thickness of z + y (m). Sediment erosion was modelled correspondingly, to cause a reduction in sediment thickness. Updated sediment thickness then informed updated bathymetry and this bed elevation then perturbed flow hydraulics at time step x+1. There was no inclusion of stratigraphy, i.e. no calculation of the order in which sediments were deposited, and thereby we assume that vertical sorting was not a major control on rates or volumes of deposition. Erosion and deposition volumes were computed from the difference in elevation grids output at 10 min intervals. 318 Ouantifying uncertainty in our model calculations is difficult because it is due to a combination of factors. For the hydrodynamic model, the factors affecting model uncertainty are the: input 1996 DEM (± 0.03 m); input 319 hvdrograph ($\pm 250 \text{ m}^3 \text{s}^{-1}$); specified roughness (field-measured), and; hydrodynamic model formulations. For the 320 morphodynamic model, and in addition to the factors mentioned for the hydrodynamic model, the factors 321 322 affecting model uncertainty are the: sediment grain size distribution (field-measured), and; sediment transport 323 model formulations. Since the hydrodynamic model was best-fit to the peak discharge timing and flood volume as recorded at the bridge, 4 km downstream, model uncertainty cannot be constrained from a comparison of 324 325 modelled versus measured hydrographs. Morphodynamic model uncertainty cannot be constrained from a 326 comparison of the simulated and observed net change in sediment storage because as will be discussed there are 327 different time scales involved in these two calculations. Therefore both hydrodynamic and morphodynamic model uncertainty estimates must recognise that: (i) there are components of the model that cannot be quantified 328 329 for uncertainty; (ii) that these uncertainties propagate through the model work flow and act in combination, and 330 (iii) that there are some facets of model behaviour that might not be so well simulated. Overall, given the factors 331 in the model for which we can quantify uncertainty, given our field knowledge and measurements, and given our 332 previous experience of applying the model to outburst floods (e.g. Carrivick, 2006, 2007; Carrivick et al., 2009, 2010, 2013a) we estimate uncertainty in hydrodynamics to be within +/- 10 %, uncertainty in erosion and 333 334 deposition (morphodynamics) to be within +/- 20 %, and summative/net landscape change to be within +/- 40 %.

335 **Results**

336 **Palaeocompetence reconstructions**

337 The ice-proximal boulder fan clasts have a bimodal size distribution, with the greatest frequency of clasts 338 measured in the 'small cobble' and 'large boulder' categories (Fig. 5). Palaeocompetence reconstructions, using just the 5 largest boulders to suggest maximum values, suggest that peak flow velocity was $\sim 13 \text{ m.s}^{-1}$ and peak 339 flow depth was 7.6 m (Table 2). Boulder size decreased rapidly downstream (Fig. 6A) and therefore flow 340 parameters were also calculated for each individual boulder (clasts > 256 mm in diameter) and visualised in 341 ArcGIS (Fig. 6B). Flow velocity ranged from 14 m.s⁻¹ at the ice proximal end of the fan to 2.4 m.s⁻¹ at the ice-342 distal end. Stream power varied from approximately 75 to 35,400 W.m⁻² and boundary shear stress from 36 to 343 3,000 N.m⁻². Flow depths varied from just under 10 m ice-proximally to 0.6 m at the ice-distal end of the fan. A 344 comparison of the palaeocompetence reconstructions with the slope area and numerical modelling methods are 345 given in Table 3. 346

347

348 Morphodynamic modelling

This study ran morphodynamic models lasting ~ 24 hours in computational time on a desktop PC with a 3 Ghz processor, 8 Gb RAM and a 1 Tb hard disk.

351

352 Flood inundation

Flow was largely constrained within the post-LIA incised Jökulsá channel, although some palaeo-channels were 353 354 re-activated (Fig. 7). The dominant area of channel reactivation was approximately 500 m south of the glacier, where flow was routed through palaeo-channels on the older moraine surface (Fig. 7). These channels were 355 located 2 to 3 m above the pre-jökulhlaup active river channel. Beyond this point, modelled flow was confined to 356 the steeply-incised channel for 1 km between the moraine. At the downstream opening of this confinement, the 357 358 older (dry) sandur surface was reactivated between this point and the Jökulsá road bridge (Fig. 7). Simulated flow built up behind the Jökulsá road-bridge embankment, approximately 5 km downstream, eventually flowing 359 over the road south of the Jökulsá bridge at 60 minutes We do not know if this happened in reality, but as 360 361 outlined in the methods section, the road bridge had been removed from the pre-flood DEM, leaving a 160 m 362 wide opening between the road embankments on either side of the river. Previously dry, vegetated channels were 363 inundated along much of the channel (circled area on Fig. 6). By the end of the simulated jökulhlaup, these 364 channels were dry. At the Jökulsá estuary, flow ponded behind the low-relief sand-dune ridge to the west of the river (Fig. 7). 365

366 Spatiotemporal variations in modelled hydraulics

The overall spatial pattern of modelled flow depth and flow velocity are mapped in Figure 8 at time 01:30 after 367 flood initiation, i.e. near peak flow conditions. The pattern distinguishes channelled flow, overbank flow and 368 braided flow (Fig. 7). In detail, the pattern of flow velocity and flow depth is 'smoother' or more spatially 369 coherent, in the morphodynamic simulation compared to the hydrodynamic simulation. Bed elevation changed 370 371 as a result of erosion and deposition and showed considerable variability along the channel. In ice-proximal zone 372 progressive erosion occurred, in channelized areas (cross-section 3) rising stage erosion occurred and falling 373 stage deposition, in distal reaches rising stage deposition and falling stage erosion occurred (Fig. 8). Figure 8 374 also plots the temporal model output of flow velocity, water depth and bed elevation change at selected points on 375 each of the cross-sections. These temporal comparisons between the hydrodynamic and morphodynamic model 376 output illustrate the effects of including sediment transport and iterative (per model time step) bed elevation 377 change on flow conveyance and are summarised in Table 4, namely: no effect on total inundation area; nearly 13

double frontal wave speed; timing of peak stage advanced by about 19 %; no significant effect on peak flow
depths or peak flow velocities; a strong effect on the rate of change of flow depth and flow velocity.

380 The detail of the morphodynamic simulation was further examined at seven cross-sections as indicated in the last 381 panel of Figure 7 and were chosen in location to permit (i) analysis of the longitudinal evolution of the flood, (ii) comparisons with those considered by Russell et al. (2010) and (ii) comparison against the bridge record of 382 383 Sigurðsson et al. (2000). Spatiotemporal quantification of depth-averaged velocity, average bed shear stress, 384 total sediment transport (sum of all fractions) and flow discharge are provided as suppl, material video and for 385 brevity and ease of reporting in this paper were recorded at each cross-section (Fig. 9). Flow discharge exhibited a steep rise to peak values and a shallower falling limb. Peak discharge at cross-section 1 was reached after 30 386 387 minutes and after 60 minutes at each other cross-section (which is not surprising because the input hydrograph was best-fitted to the peak discharge magnitude and flood volume at the bridge). The magnitude of peak 388 discharge ranged from 1,600 m³s⁻¹ at cross-section 1, to 2,500 m³s⁻¹ at cross-section 3, and 2,000 m³s⁻¹ at cross-389 390 section 6 (Fig. 9).

Depth-averaged velocity at peak discharge (one hour after flood initiation) was highest at the glacier terminus, 391 reaching 12 m.s⁻¹ at the northern conduit (Fig. 9). Flow velocity decreased rapidly to $\sim 4 \text{ m s}^{-1}$ in the immediate 392 393 proglacial channel, but increased in the constricted section of the channel cut through moraine (Fig. 9). Cross-394 sectional averaged velocities showed a similar downstream pattern to discharge, with average velocities lower in 395 cross-section 1 (Fig. 9). The time at which peak velocity was reached varied with distance downstream. Peak flow velocity was reached after 30 minutes at cross-section 1 and after 60 minutes at cross-sections 2 to 5 (Fig. 396 397 9). At cross-sections 6 and 7, velocity remained near constant between 60 and 90 minutes Bed shear stress ranged from 60 to 580 N.m⁻² at peak discharge, 30 minutes after flood initiation. Bed shear stress was highest 398 where velocities were highest except at cross-section 2, where bed shear stress was greatest at 180 minutes after 399 400 flood initiation (Fig. 9).

401

402 Patterns, volumes and rates of geomorphological change

The modelled volume of total sediment transport (the sum of the three sediment fractions) was 469,800 m³ (\pm 20%) (Table 4). The rate of modelled total sediment transport at cross-section 1 peaked at 0.25 m³s⁻¹m⁻¹ 30 minutes after flood initiation (Fig. 9). With progression of time, modelled total sediment transport became more 'flashy', that is, the peak of curve was steeper. This is in contrast to modelled discharge, which became less

flashy through time and with distance downstream (Fig. 9). Total sediment transport generally decreased with distance downstream (Fig. 9). Maximum erosion of 8.2 m occurred along the ice margin (Fig. 10) and 5.9 m of erosion occurred at 2.4 km down valley. This latter site was also the site of maximum deposition at up to 3.2 m.

410

The total change in the differenced DEMs = $-415,200 \text{ m}^3 (\pm 9,000 \text{ m}^3)$ which is ~ 55,000 m³ less than suggested 411 by the morphodynamic model. This difference in volume between what we have modelled and what we have 412 measured could be an indication of: (i) the amount of subglacially-sourced material; (ii) geomorphological 413 activity that has occurred during the flood; i.e. incision and infill, (iii) geomorphological activity between the 414 flood and the DEM survey dates; (iv) a reflection of measurement error. The modelled landscape change was 415 416 compared on a grid cell by grid cell basis to the DEM of difference (DoD) and whilst visually the agreement is generally good spatially (Figure 11A), and to a lesser extent along a long profile (Figure 11B), there was no 417 statistical correlation for either. Four zones highlighted by white circles in Figure 11A indicate discrepancy 418 between the DoDs, as highlighted in the 3rd panel difference measured minus modelled map. These 419 420 differences in the white ellipse zones suggest: (i) incision of bar forms probably after the 1999 flood but before 421 the re-survey in 2001, and; (ii) lateral bank (mass collapse) erosion, which is not accounted for in the 422 morphodynamic model. The ice-marginal difference (red zone) in the difference map is the boulder fan; 423 demonstrating the subglacial provenance of this material during the 1999 flood and the ignorance of this in the 424 morphodynamic model. The long profile depicted in Figure 11B could be interpreted to indicate underprediction of erosion and deposition by the model, but with consideration of the results of Staines et al. (2014) 425 may actually just reflect subsequent landscape response to the jökulhlaup (between the flood date and the 2001 426 427 aerial photograph survey) as over-steepened unconsolidated banks collapsed and ablation-fed meltwater incised 428 jökulhlaup deposits, for example.

429 The net landscape change during the modelled jökulhlaup as measured by the total modelled elevation change was -86,400 m³ (\pm 40%), resulting from -275,400 m³ (\pm 20%) proglacial erosion and 194,400 m³ (\pm 20%) 430 proglacial deposition. These quantities are interesting because they are measures of geomorphological work and 431 432 will permit comparison to other geomorphological processes that mobilise a relatively large volume moved over a relatively short time period. The modelled net loss of -86,400 m^3 (± 40%) indicates the volume of sediment 433 434 that was transported into the sea in just 7 hours. Total erosion and deposition per grid cell and were 435 discriminated for both the rising and falling limbs of the modelled jökulhlaup (Fig. 12). The pattern of elevation 436 change was 'smoother' or most 'spatially coherent' during the falling limb (Fig. 12). The rising limb pattern 437 suggests widespread activation of the bed, whereas the falling limb pattern suggests more organisation, perhaps pseudo bedforms. In ice-proximal positions, the morphodynamic model produced substantial channel incision with a 10 m vertical decrease in bed level measured at cross-section 1 (Fig. 10). Just north of the Jökulsá bridge at cross-section 4, deposition was observed to the west of the main channel, which corresponds well with postjökulhlaup observations made in the field (Russell et al., 2010). In ice-distal positions at cross-section 7, largescale bars and channels formed: two main channels formed at 350 m and 420 m along the cross-section transect and deposition occurred at the channel margins (Fig. 10).

Both peak erosion rate and peak deposition rate coincided with peak discharge and were 650 m³s⁻¹ and 595 m³s⁻¹. 444 445 respectively. Qualitatively, erosion proceeded rapidly as a result of intense bed shear stress on the rising stage of the flood (Fig. 9; suppl. material video). However, there was some re-deposition on the rising stage of the flood 446 (suppl. material video). Peak erosion rate was ~ 650 m^3s^{-1} and the peak deposition rate was ~ 580 m^3s^{-1} , both 447 448 occurring at the peak stage at 1.5 hours after flood initiation. During the falling limb, bed shear stress diminished 449 and we also note that the total erosion volume and deposition volume did not significantly change. However, there was some waning stage incision of sediments as evidenced by the decline in bed elevation in the later part 450 of the event (Fig. 8). We note that more sophisticated analyses of the patterns of erosion and sedimentation 451 452 should consider the spatial stress divergences/convergences as the fundamental control on channel 453 morphological response, but we have not done that here because of the lack of a statistical correlation between our modelled elevation changes and measured elevation changes. 454

455 **Discussion**

456 **Comparison of reconstruction methods**

457 Palaeocompetence calculations were performed to provide an independent comparison to the numerical modelling, but there is a big discrepancy in the hydraulic reconstructions by the palaeocompetence and 458 numerical modelling methods. Palaeocompetence-derived hydraulic values are higher than those obtained from 459 the numerical modelling (Table 3) but only pertain to the boulder fan whereas the numerical modelling included 460 the entire proglacial channel (Fig. 8). For example, maximum flow depths reconstructed by each method ranged 461 from 4.8 m using the slope-area technique (Russell et al., 2010) to 9.7 m using the palaeocompetence method 462 (Table 2) to 12 m using distributed numerical modelling. We interpret the discrepancy in reconstructed 463 464 hydraulics to highlight the assumptions (and thus limitations) inherent within each method. Firstly, palaeocompetence techniques rely on 'scaled-up' relationships between gravel-sized clasts and hydraulic 465

parameters and therefore erroneous results are likely for large boulders (Cook, 1987; Jarrett, 1987). Indeed Costa (1983) stated that palaeocompetence reconstructions for clast greater than 2 m in diameter are less reliable than those generated from smaller clasts. Secondly, the palaeocompetence technique assumed that sediment supply to a flood was unlimited (Carrivick 2007, 2009) and therefore provides a minimum estimate of flow parameters. It is possible that clasts larger than those measured could have been transported if they were available. Thirdly, in highly turbulent floods, lifting forces can encourage the entrainment of clasts larger than those transported by flow-velocity and tractive forces alone (Costa, 1983).

Regarding the discrepancy between Russell et al.'s (2010) slope area results and our morphodynamic modelling, Russell et al.'s slope area reconstructions were applied only at discrete cross-sections and necessarily assumed gradually-varied flow conditions. They estimated flow velocity in part via grain roughness; i.e. boulder measurements, so with the same limitations as outlined for the palaeocompetence methods above. Perhaps most crucially, they were applied on the post-flood terrain. In contrast, our morphodynamic modelling input a preflood DEM, specified an input hydrograph and pre-existing sediment across the model domain, and modelled fully spatiotemporal hydraulics, sediment transport and subsequent geomorphological change.

480 Comparing the hydrodynamic model with the morphodynamic model, inclusion of sediment transport and 481 morphological updating did not affect the total inundation area. However, it did cause the frontal wave speed to 482 nearly double (Table 4). This is due to loss of energy in sediment entrainment and flow resistance and at the leading wave front edge, c.f. experiments by Carrivick et al. (2011). It suggests that usage of numerical models 483 of outburst floods in a hazard analysis should include morphodynamics if the time to inundation is important. 484 485 The same suggestion can be made again because the timing of peak stage was advanced by about 19 % by including morphodynamics (Table 4). Generally, morphodynamics did not alter absolute values of peak flow 486 487 depths or peak flow velocities very much, in general agreement with the findings of Huang et al. (2014), but did 488 affect the rate of rise and fall of these parameters (Figs. 7 and 8). Attributing these differences to sediment 489 transport and morphodynamic processes demands more work to (i) define the spatiotemporal mass and momentum of the fluid, and (ii) examine spatiotemporal channel geometry changes in greater detail, for example 490 491 vertical versus lateral changes and the relationship (feedback?) between changing channel cross-section and 492 hydraulics.

493 Proglacial jökulhlaup character and impact

494 A key advantage of morphodynamic over hydrodynamic modelling that it provides quantification of erosion and deposition patterns, volumes and rates that would otherwise be unobtainable. Whilst parameterising a 495 496 morphodynamic model requires good knowledge of the flood event and of the flood channel before the event, that effort is rewarded with improved process and product understanding. Whilst it must be remembered that 497 498 there are errors in the DEMs (Staines et al., 2014) and assumptions in the morphodynamic modelling, the main 499 differences between the two (Fig. 12) are likely to be due to the different time-scales considered: 5 years 500 between the DEMs versus a few hours for the model. That said, the remarkable similarity in pattern (Fig. 11) gives confidence in both the DEMs and the model and demonstrates that the 1999 jökulhlaup had an important 501 502 geomorphological impact on the proglacial area.

503 Overall, erosion and deposition both occurred in the main channel, and both were greater in narrower reaches 504 (Fig. 11). Erosion was greater in narrower reaches because the water depth was deepened and velocity was higher, which induced more sediment movement. The erosion maps, and the more coherent flow structures in the 505 morphodynamic model (Fig. 8), together suggest that morphodynamic processes make flow conveyance more 506 efficient via smoothing of the bed and straightening of the channel sides in combination subduing form 507 508 roughness. We suggest that deposition was greater in narrower reaches because the (finite) amount of sediment 509 being transported was redistributed over a relatively small area, in comparison to wider reaches. The slight increase in peak discharge observed at cross-section 2 (Fig. 9) is likely a response to changing channel geometry 510 511 because flow was constricted to a single channel between the moraine belt 2 km downstream of the glacier 512 terminus. Beyond this constriction the flood routeway becomes wider with increased distance from the glacier and shallower in gradient. Correspondingly net deposition was observed as a result of reduced velocities and 513 514 reduced bed shear stress, which is similar to expansion fans and valley-fill sediment documented by Alho et al., (2005), for example. 515

The evidence in the morphodynamic model results of rising-stage deposition and waning stage incision has considerable promise for quantitatively assessing the conceptual models that have been developed from sedimentary (e.g. Maizels, 1989a, 1989b, 1991) and geomorphological observations and measurements (Russell et al., 2006). During the rising limb of the jökulhlaup ice-proximal deposition was modelled at the glacier terminus (Fig. 11). This is interesting because ice-proximal deposition was observed during the jökulhlaup, the boulder fan being the key depositional impact of the flood (Russell et al, 2010). Falling stage coherence of elevation changes (Fig. 11) is potentially indicative of bedform development (c.f. Rushmer 2007). Volcanoglacial jökulhlaups frequently exhibit a rapid rising stage, during which proximal aggradation rates are high and
 downstream transport is limited (Rushmer, 2007).

525 A note on the post-jökulhlaup landscape response

The post-jökulhlaup period at Sólheimajökull has been characterised by glacier retreat (Staines et al, 2014). 526 Sólheimajökull retreated on average 40 m yr⁻¹ between 1996 and 2010. Owing to a subglacial overdeepening, 527 channel incision occurred ice-proximally, leading to the abandonment of the boulder fan altitudinally above the 528 529 present-day channel. As a result, the boulder fan has only been subject to minor re-working post-jökulhlaup. Landscape change in the lower channel reaches in the decade following the jökulhlaup was characterised by net 530 channel aggradation. Between 2001 and 2010 there was a progressive increase in downstream channel braiding, 531 suggesting that sediment deposited by the jökulhlaup is moving through the proglacial channel system, being re-532 533 distributed by non-jökulhlaup flow.

534 A note on modelling approaches

535 Outburst flood modelling inevitably involves a series of uncertainties associated with the difficulties in estimating the 536 values of key parameters. Notwithstanding the excellent pre- and post-flood data we have used in this study, it has 537 been necessary to consider uncertainty propagation through the investigation. We could not define sediment input 538 from a subglacial source and whilst we could have an insight to the volume of this subglacial sediment (as the 539 difference between our model and the DoD), the subglacial sediment flux remains unknown. Considering subglacially-sourced sediment will of course not be a problem for studies of glacial outburst floods from ice-marginal 540 541 lakes. For studies of any sort of outburst flood, it could be considered that studies who have very limited field data 542 could find that the parameterisation of roughness could be as important as the model structure employed. Indeed the 543 wider challenge of how to use limited observational data to support high-resolution predictions is certainly unresolved. In contrast to the mechanistic approach, such as the 'natural test case' of this study, an alternative 544 545 approach is to acknowledge that actually none of the model inputs are known, except within reasonable bounds, and then to conduct Monte Carlo scenario-based modelling where each variable and combination of variables is 546 547 systematically varied to define 'most likely' outputs.

548 **Conclusions**

549 The key contribution of this study is a demonstration that the morphological adjustments induced by the passage of a 550 glacial outburst flood (GLOF), or 'jökulhlaup', are significant enough to significantly and dynamically affect the

551 conveyance characteristics of the flow. A major potential implication of this work, therefore, is that if reconstructions 552 of outburst flood hydraulics for interpretation of the long term hydrological record and flood risk assessment could be 553 with significant error. Assessment of differences in flow velocity and flow depth simulated in cases where the model 554 had either a fixed bed or a moveable bed was opportunistically employed for the 1999 Sólheimajökull jökulhlaup, 555 which acted as a 'natural laboratory', because modelled sediment transport and geomorphological change was 556 able to be compared to the difference between pre- and post-flood topography as measured using 557 photogrammetrically-derived DEMs.

Firstly, this analysis has revealed new insights into the proglacial character and behaviour of the 1999 jökulhlaup 558 event. Total sediment transport was 469,800 m³ (\pm 20 %) (Table 4). Maximum erosion of 8.2 m occurred along 559 the ice margin (Fig. 10) and 5.9 m of erosion occurred at 2.4 km down valley. This latter site was also the site of 560 561 maximum deposition at up to 3.2 m. The net landscape change during the modelled jökulhlaup was $-86,400 \text{ m}^3$ $(\pm 40 \%)$, resulting from -275,400 m³ $(\pm 20 \%)$ proglacial erosion and 194,400 m³ $(\pm 20 \%)$ proglacial 562 deposition. The rising limb pattern of bed elevation change suggested widespread activation of the bed, whereas 563 the falling limb pattern suggested more organisation, perhaps primitive bedform development. Peak erosion rate 564 and peak deposition rate were 650 m^3s^{-1} and 595 m^3s^{-1} , respectively, and coincided with peak discharge at 1.5 565 hours after flood initiation. Deposition occurred on the rising stage and erosion occurred on the falling limb, 566 567 which is contrary to prevailing simple conceptual models.

568 Secondly, this study has several important implications for reconstructions of outburst floods at other sites. At its simplest, numerical modelling permits interpolation between (often sparse) field measurements. It permits 569 570 discrimination of how an 'end-product' is obtained, in this case production of the post-flood landscape. However, analysing this spatiotemporal model output is challenging and needs development of automated grid-571 based programs (c.f. Carrivick et al., 2013a). Whether or not it is crucial to include sediment transport and 572 morphodynamics in field (landscape) scale applications of numerical models of jökulhlaups or of other types of 573 574 outburst floods depends on the intended application. This study has shown that inclusion of morphodynamics beyond a simpler hydrodynamic simulation accelerated the arrival time of the flow front and brought forwards 575 the time of peak discharge. This is due to increased mass and momentum with sediment transport but also due to 576 a feedback process whereby flow conveyance becomes more efficient due to (i) erosion of minor bed protrusions 577 and (ii) deposition that infills or subdues minor bed hollows. Therefore hazard analyses focussed on inundation 578 area need not go beyond hydrodynamic simulations, but those focussed on frontal wave arrival time and peak 579 580 arrival time should note that the morphodynamic simulations of this study advanced those arrival timings by 100 % and 19 %, respectively. The peak magnitude of flow depth and flow velocity was not significantly affected by
including morphodynamic processes.

583 Morphodynamic simulations can be extremely instructive for understanding rapid (minute-scale) landform construction and deposition process and products, but present challenges in parameterisation and validation. 584 Most events will not have a pre-flood terrain model, especially at a high resolution, available and spatially 585 distributed sediment characteristics can be hard to ascertain. This study found that over the course of the 586 587 jökulhlaup, the pattern of erosion and deposition became more coherent, potentially indicative of bedform development. Total sediment transport became more 'flashy' over time, in contrast to discharge. Downstream 588 589 variations in sediment transport, flow velocity, shear stress and flow discharge were largely a reflection of 590 channel geometry: velocities and sediment transport were highest in constricted reaches and lower in unconfined 591 reaches.

With regards to the opportunity presented by this modelling for process-product studies, future work should aim to target specific sediment-landform assemblages and examine energy exchanges between bed and flow, thereby beginning to bridge the gap in knowledge between grain-scale experiments and field-scale measurements. Refinements of the model presented here might include discrimination between vertical and lateral sediment via a slope failure operator for bank collapse, for example.

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	(landscape) scale outburst floods
	1D
I	Magilligan et al., (2002), Skeiðarársandur, Iceland.
	Alho <i>et al</i> ., (2005), Jökulsá á Fjöllum, Iceland.
	Herget (2005), Altai floods, Siberia, Russia.
	1D-2D
	Kamrath <i>et al</i> . (2006), dike breach on River Rhine.
	2D
	Begnudelli and Sanders (2007), St Francis,
	California.
	Fuamba <i>et al</i> . (2007), Quebec.
	Carrivick, (2006, 2007); Kverkfjöll, Iceland.
	Carrivick et al. (2009, 2011*), Ruapehu, NZ.
	Carrivick et al. (2013a); Russell Glacier, w.
	Greenland.
	Bohorquez and Darby (2008). Mont Miné, Switz.
	Miyamoto <i>et al</i> . (2006, 2007), Denlinger and
	O'Connell, (2010), Alho et al. (2010); Missoula
	flooding, NW USA.
	Carling et al. (2010), Altai floods, Siberia, Russia.
	Worni <i>et al</i> . (2012)*, Ventisquero Negro,
	Patagonia.
k	Coike and Takenaka (2012), Mangde Chhu, Bhutan.
	Pitman <i>et al</i> . (2013), Lugge Lake, Bhutan.
	Westoby <i>et al.</i> (2014), Chukhung Glacier. Nepal.

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Table 1. Selected examples of application of numerical models of outburst floods, mostly to jökulhlaups, at the field
(landscape) scale, for both palaeo and modern studies. *Only the models applied by Carrivick *et al.* (2011), Worni *et al.*(2012) and Pitman *et al.* (2013) include sediment transport.

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Axis	Axis Length (mm)		Velocity (v)	Shear Stress ($ au$)	Stream Power (ω)	Flow Depth (D)
а	b	С	$m s^{-1}$	N m ⁻²	W m ⁻²	m
10750	8410	3720	15	3,200	37,200	9.7
10250	6370	750	13	2,300	23,300	7.9
9900	5900	4400	12	2,100	20,500	7.5
8450	6180	5070	13	2,200	22,200	7.7
8200	3550	2270	10	1,100	8,700	5.2
	Mean		13	2,200	21,600	7.6

Table 2: Palaeocompetence reconstructions using the five largest clasts of 395 boulders measured on the boulder fanand via the equations of Costa (1983).

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Palaeohydraulic Method	Velocity (m.s ⁻¹)	Shear Stress (N m ⁻²)	Stream Power (ω)	Flow Depth (m)
Palaeocompetence (point) measurements	13 (mean)	2200	21,600	7.6
Slope-area reconstructions (Russell <i>et al.</i> 2010)	~5 – 7	930 to 1,280	~5,200 to 8,200	3.3 to 4.8
Hydrodynamic modelling	0.9 (average) 8.6 (max)	110 (average) 3,430 (max)	n/a	12 (cross-section 1)

828	Table 3: Com	parison of I	oalaeohv	draulic re	constructior	ns at the s	glacier	terminus

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Parameter	Hydrodynamic	Morphodynamic simulation		
	Ear whole model d	omain		
	TOT WHOLE MODEL U	emam		
(m.s ⁻¹)	1.06	2.14		
Inundation area (m ²)	3,668,490	3,681,220		
Sediment moved (m ³)	-	469,800		
By way of examp	ole, for cross-section 7	, 7.05 km from ice margin		
Flow depth max. (m)	3.75	3.4		
Time of peak flow	01:20 after start	01:05 after start		
Cumulative bed		0.00		
elevation change (m)	-	0.88		
Time of max. bed level	-	06:15		
Velocity max. (m.s ⁻¹)	3.95	4.21		
Max. bedload transport				
rate: all fractions	-	0.0116		
(m ³ .s ⁻¹ .m ⁻¹)				
Max. bed shear stress		208 75		
(N.m⁻²)	-	308.75		

Table 4. Summary of results of hydrodynamic and morphoynamic simulations

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Figure 1: Location of Solheimajokul and Solheimasandur on the southern margin of Myrdalsjokull in southern Iceland. The
 numerical model domain used in this study is indicated.

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Figure 2: Steps involved in the creation of the curvilinear grid. [A] Splines are defined using sample points as a guide; [B]
 Splines interpolated to grid; [C] Grid refined; [D] Grid refined and orthogonalised; [E] Grid clipped to desired extent of
 model; [F] Bathymetry points mapped onto mesh.

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Figure 3: Input hydrograph to Delft3d as defined by: field measurements of river stage and discharge of 1700 m³s⁻¹ made at the bridge by Sigurðsson et al. (2000); the peak discharge estimates of Russell et al. (2010); and knowledge of the flood trigger. The first 6 hours of the hydrograph are the input values for the 'baseflow model' and the following 6 ½ hours are the 'jökulhlaup model'.

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905 **Figure 4.** Sensitivity of cross-sectional discharge and mean cross-sectional bed elevation change to Manning's n roughness.

906 Cross-section is 50 m upstream from the downstream boundary.

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Figure 5. Clast size analysis of the ice-proximal boulder fan.

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925 **Figure 6:** [A] Size of clasts measured at the ice-proximal boulder fan. [B] Flow parameters reconstructed using the

926 palaeocompetence technique. Note that there are some minor interpolation effects along the periphery of each map in B.



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Figure 7: Modelled flow depth for duration of simulated jökulhlaup. Note the wetting and drying effect at the edges of the flood, highlighted in red. Yellow arrow highlights area of palaeo-channel reactivation near the ice-margin. Time in minutes since flood initiation are shown in the top left corner of each image.

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Figure 8. Comparison of spatiotemporal hydrodynamic and morphodynamic simulations. Maps pertain to time 01:30 after flood initation. Note that deeper and faster flow occurred than legend suggests, but colour scale is optimised to show variability. Note only bed elevation is plotted for cross-sections 1, 3, 5 and 7, and flow velocity and flow depth are only plotted for cross-section 7, for brevity and clarity. Note changing y-scale for bed elevation. More temporal information on hydraulics at each cross-section is given in Figure 7 and for cross-sections in Figure 9.



955 **Figure 9:** Downstream variation in modelled hydraulic parameters for the morphodynamic model run.

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Figure 10: Bed elevations at three cross-sections at the start of the modelled jökulhlaup (0 minutes) and at the end (330 minutes). The spike in elevation gained at cross-section 1 remains unexplained. Cross-sectional distance x-axis is measured

- 963 from the true left bank. For location of cross-sections, see Figure 8.

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Α

Modelled: morphodynamic simulation Measured: 2001 minus 1996 DEM Measured - modelled difference elevation elevation change (m) difference (m) < -1.0 < -5.0 -0.99 to -0.50 -0.49 to -0.30 -0.49 to -0.25 -0.29 to -0.20 -0.24 to -0.10 -0.19 to -0.10 -0.09 to 0.10 -0.09 to 0.10 0.11 to 0.25 0.11 to 0.20 0.26 to 0.50 0.21 to 0.30 0.51 to 1.00 0.31 to 0.50 > 1 > 5



972

973 Figure 11. Comparison of DEM of difference between 1996 and 2001, and the net cumulative elevation changes as a result 974 of the morphodynamic model, in part [A] both overlayed on the 2010 LiDAR-derived hillshaded DEM. Note colour scale in 975 part A is to emphasise detail and values < -1.0 and > 0.5 did occur. Black line in part [A] is the long profile along which 976 elevation differences are plotted in part [B]. White ellipses in A delimit zones mentioned in the text. 977

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Figure 12. Pattern of cumulative bed elevation change discriminated by rising and falling hydrograph limbs, overlayed on
 aerial photograph mosaic.

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994 **Supplementary material**: video (.avi) files of spatiotemporal flow depth, velocity, bed shear stress, froude 995 number, total sediment transport and cumulative bed elevation change.