Statistical prediction of nanoparticle delivery: from culture media to cell

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Abstract

The application of nanoparticles (NPs) within medicine is of great interest; their innate physicochemical characteristics provide the potential to enhance current technology, diagnostics and therapeutics. Recently a number of NP-based diagnostic and therapeutic agents have been developed for treatment of various diseases, where judicious surface functionalization is exploited to increase efficacy of administered therapeutic dose. However, quantification of heterogeneity associated with absolute dose of a nanotherapeutic (NP number), how this is trafficked across biological barriers has proven difficult to achieve. The main issue being the quantitative assessment of NP number at the spatial scale of the individual NP, data which is essential for the continued growth and development of the next generation of nanotherapeutics. Recent advances in sample preparation and the imaging fidelity of transmission electron microscopy (TEM) platforms provide information at the required spatial scale, where individual NPs can be individually identified. High spatial resolution however reduces the sample frequency and as a result dynamic biological features or processes become opaque. However, the combination of TEM data with appropriate probabilistic models provide a means to extract biophysical information that imaging alone cannot. Previously, we demonstrated that limited cell sampling via TEM can be statistically coupled to large population flow cytometry measurements to quantify exact NP dose. Here we extended this concept to link TEM measurements of NP agglomerates in cell culture media to that encapsulated within vesicles in human osteosarcoma cells. By construction and validation of a data-driven transfer function, we are able to investigate the dynamic properties of NP agglomeration through endocytosis. In particular, we statistically predict how NP agglomerates may traverse a biological barrier, detailing inter-agglomerate merging events providing the basis for predictive modelling of nanopharmacology.

Keywords: nanoparticle, nonhomogeneous Poisson process, transmission electron microscopy, nanotherapeutic

(Some figures may appear in colour only in the online journal)

Introduction

The application of nanoparticles (NPs) within medicine is of great interest; their innate physicochemical characteristics provide the potential to enhance current technology, diagnostics and therapeutics. In recent years a number of NP-based diagnostic and therapeutic agents have been developed for treatment of various cancers, where surface functionality has been exploited to provide more effective routes to administration of therapeutic dose [1, 2]. As delivery systems NPs provide an improved means to detect abnormalities at the molecular scale; surface functionality providing increased targeting efficiency and controlled release of therapeutic dose...
over a user-defined period; a thorough review is provided by Zhang et al. [3]. Additionally, NPs have improved the sensitivity and specificity of many imaging platforms. In particular, superparamagnetic NPs now play a key role in magnetic resonance imaging, providing enhanced image contrast and increased resolution to inform and quantify many tissue abnormalities (see Na et al. [4] for examples).

Despite success in these areas, application of NP technology or quantification of NP dose at the individual cellular level is still at an infant stage. Specifically, detailing the influence that the myriad of biophysical processes have on NP agglomeration, transport within biological media, cellular uptake, internalization and redistribution has proven difficult to quantify. This shortcoming is directly related to the inability of high-throughput time-lapse systems to provide rigorous cytomteric measurement and analyses of the evolution path of NPs on an appropriate spatial scale (i.e. the individual NP (nm)). If NP-based medicine is to be truly realized in future years it is an absolute that the community are able to accurately (i) quantify the internalized nanomaterial dose as opposed to that simply applied [5, 6], (ii) determine the biological consequences associated with this actual dose and (iii) predict how the dose evolves over time.

Electron microscopy, in particular transmission electron microscopy (TEM), is a technical platform that can deliver information at the required spatial scale, where individual NPs can be identified, in terms of both number and spatial location [7]. Recent in vitro studies have detailed the impact of gold NP agglomeration on several cell lines [8, 9], where this is important because comparisons of NP agglomerate size measured in water and cell culture media report increases in size for the latter [10]. We have previously demonstrated a method in which NP dispersion can be rapidly frozen and imaged in the TEM, with representative agglomerate dimensions measured [11]. This provides more precise imaging of actual NP agglomerate state in which a NP agglomerate size and distribution is more accurately determined, a fundamental criterion for the continued development of a nanomedicine. TEM has also been applied to study the cellular uptake of NPs to human mammary cells by endocytosis, with outputs suggesting initial sequestration in early endosomes followed by translocation to late endosomes or lysosomes [12]. In addition, Krpetic et al. have previously used TEM to track the intracellular distribution of peptide modified gold NPs at several time points, covering initial membrane bound encapsulation and release, and through to clearing of the particles from the analyzed cells [13].

Application of this technology however comes with an intrinsic compromise that limits temporal sampling when compared to flow cytometry and current optical microscopy platforms. Due to reduced temporal sampling many electron microscopy contributions to research in nanomedicine are purely qualitative, however, there is a growing research community that are developing novel methodologies that provide quantitative biophysical insight of contiguous TEM measurements [14–16]. Specifically, utilizing TEM in conjunction with appropriate stochastic or statistical methods that provide a bridge between measurement points can be exploited to provide unresolvable information of the underlying biophysical processes in this interval.

In this work, we apply the concept of statistical analysis to link distinct spatiotemporal TEM measurements [15] to investigate the transport of NP agglomerates in cell culture media, to that within endosome compartments in human osteosarcoma cells (U2-OS cell-line). The NPs employed were QTracker 705 nm CdTe/ZnS quantum dots at a 10 nM dose; we have significant experience incorporating these NPs within U2-OS cellular systems and have demonstrated that they are toxicologically and pharmacodynamically inert at this dosage [17, 18], and that they may be utilized to extract meaningful biological parameters, see [15, 17, 19–24] for examples. QTracker 705 nm quantum dots are specifically targeted for endocytic uptake; the NPs have an organic coating, composed of arginine-rich targeting peptides conjugated to biotin bonded to streptavidin and the arginine-rich peptides can lead to cellular uptake via micropinocytosis [25].

We image and characterize 500 distinct NP agglomerates/aggregates in culture media and within endosome compartment cells respectively, the latter following the 1 h exposure to the NP rich culture media. For clarity, we refer to NP clusters in culture media as agglomerates and those within endosomes as aggregates. Each of the NP agglomerates/aggregates imaged via TEM is randomly selected, in the latter case we first randomly select 100 distinct cells from a cellular population comprising of >10⁴ cells and subsequently select stochastically 500 endosomes from within this cellular sub-population. In both spatiotemporal cases the number of individual NPs per agglomerateaggregate is determined [11]. Previously, we have shown stochastic sampling of high-resolution low frequency TEM images in this manner is capable of capturing cellular heterogeneity in NP uptake and further redistribution within daughter cells through mitosis. Specifically, we demonstrated that stochastic sampling of probability mass functions (PMFs) that encapsulate NP number per endosome and NP aggregate number per cell can be utilized to provide the total quantum dot fluorescent intensity per cell for 10⁴ in-silico cells. It was established that the in-silico population accurately recreated and predicted corresponding high-throughput flow cytometry measurements [15].

Analyzing the collected TEM images we construct the PMFs that encapsulate system heterogeneity associated with NP agglomerates/aggregates size (i.e. number of constituent NPs) in culture media and in endosome compartments following 1 h NP exposure.

We demonstrate that transition of states between the two PMFs can be achieved by considering the combined biophysical processes of NP transport [26] and cellular uptake as a nonhomogeneous Poisson process (NHPP), where the rate parameter that describes NP agglomerate aggregation at the cellular surface or during endocytosis is driven by actual TEM measurements. Statistical sampling of the NHPP returns the number of NP agglomerates from within the culture media that have attached to an active endocytic domain on the cell surface and have subsequently been encapsulated within an
endosome through one of the many endocytic pathways. The PMF of the number of NPs per in-silico endosome is then deduced and compared with the correspond PMF actually measured via TEM; through difference minimization we are able to recover the average lifetime of an active endocytic event and the mean area of the domain and show these are commensurate with direct measurements of clathrin-coated pits through high-resolution optical microscopy techniques [27, 28], validating the applicability of the methodology. This data-driven methodology provides a means to intrinsically embed internalized nanomaterial dose within the in-silico endosome population [5, 6] and statistically establish how the cell media NP dose has translated across the biological membrane into endosome compartments in so doing addressing important unmet requirements of associated with quantification of nanotherapeutics.

Materials and methods

TEM

TEM was conducted on an FEI Tecnai F20 FEG-TEM operated at 200 kV and equipped with a Gatan Orius SC600A CCD camera. Commercially available targeted nanocrystals, QTracker705 quantum dots dispersed at 10 nM in McCoy’s 5A cell culture media containing 10% fetal calf serum were examined using the plunge-freeze method previously reported [11]. Briefly, this involves rapidly freezing a blotted 3.5 μL droplet of the suspension on a glow discharge treated carbon support film in to liquid ethane. Following this, the sample was warmed to room temperature using a rotary pumped vacuum desiccator. In cell uptake experiments, U2OS cells maintained in McCoy’s 5a media and 10% fetal calf serum at 37 °C in an atmosphere of 5% CO₂ were loaded with the commercially available targeted nanocrystals, QTracker705 at a 10 nM concentration [15, 17]. Samples were prepared for TEM in a standard manner [11, 15] with no additional heavy metal stain added to the resulting 100 nm thick sections.

NP agglomerate—translation from cell culture media to endosome compartment

In the following we present an overview of NP particle traverse from media to endosome compartment. We describe qualitatively the key biophysical states (i) NPs are loaded into culture media (outside the cell) at the start of the experiment, (ii) during the experiment, NPs are transported through the media to the cell surface and may be internalized through an active endocytic pathway and (iii) 1 h post NP load, the cellular population are biologically fixed and no further NP particle internalization by the cells takes place. Time points (i) and (iii) coincide with previously reported TEM measurements of NP agglomerates in media [11] and in cellular vesicles [15]; 500 agglomerates were imaged at random and the number of individual NPs per agglomerate, $x$, was deduced via a bespoke image analysis routine [11]. The data
measured at these distinct time points are embedded within our model, intrinsically incorporating system heterogeneity.

Figure 1(a) is a schematic of the experimental set-up at the beginning of the experiment (0–h) and illustrates a cellular population (grey protuberances) in media subject to a NP dose of 10 nM [11, 15]. Hondow et al [11] previously reported that QTracker 705 NPs agglomerate indiscriminately in culture media, (see results) the high heterogeneity of $x$ is illustrated here by the variance associated with the radii of the black disks. A TEM image of a NP agglomerate captured in media [11] is shown on the right-hand side of the figure (scale bar is 75 nm). During the 1 h interval of the experiment NP agglomerates are transported to the cell surface via diffusion and sedimentation processes. The mean transport rates of the differently sized NP agglomerates, $\gamma (x)$, can be accurately determined through application of the in vitro sedimentation, diffusion and dosimetry (ISDD) model [26] specific to the NP and experimental set-up considered.

At the cell surface NP agglomerates can be captured by one of the many endocytic pathways and subsequently be internalized by the cell into discrete endosome compartments [29]. A simplified view of this complex biophysical process is shown in figure 1(b). The figure displays a plan view of the cellular population; cells are represented by the grey domains, blue circles are corresponding cell nuclei and the red-dashed circles represent areas on the cell surface where an endocytic event is taking place. We define such areas to be endosome active domains (EADs). The red and black disks in the figure represent NP agglomerates inside or outside these domains respectively. For simplicity, we assume (i) that NP agglomerate attachment to receptors within individual EAD are irreversible and all attached agglomerates are subsequently aggregated and internalized by the cell (red) and (ii) over the duration of the experiment EADs appear randomly (spatio-temporally) on the cell surface and persist for a mean lifetime, $\tau$, where $\tau \ll 1$ h [27]. The latter criterion together with the approximation that NP agglomerate transport to the cell is deduced via a mean rate over the duration of the entire experiment, suggests that the number of distinct NP agglomerates that impinge on a given EAD, $N(x)$, is intrinsically variable. We postulate that the variability of $N(x)$ is well described if we consider the combined biophysical processes of NP agglomerate transport and EAD attachment as an arrival event within a NHPP. The number of random arrivals of agglomerate with $x$ constituent NPs is then given by:

$$N(x) = \frac{\lambda(x)e^{\lambda(x)}}{x!},$$

where the magnitude of rate parameter $\lambda(x)$ comprises two principle components:

$$\lambda(x) = \alpha(x)E(x).$$

The first component $\alpha(x)$ is driven by the experimental system under investigation and is further split into the following expression:

$$\alpha(x) = N_{EAD} \gamma(x)\tau,$$

where $N_{EAD}$ is the mean number of NPs that settle on a EAD over the period $\tau$ (see below for calculation of $N_{EAD}$). As outlined above $\gamma(x)$ is the deterministic rate at which a NP agglomerate is transported to the surface of the cell during the course of the experiment (see ISDD model below). The mean lifetime or turnover rate an endocytic event $\tau$, is the implicit fitting parameter of this methodology; the consequences of $\tau$ variability is addressed and discussed in the results section of the manuscript. The second component $E(x)$ is a numerical weighting coefficient, it is the product of the PMF associated with the number of individual NPs per agglomerate measured in media ($P_M(x)$, see results) and the experimentally determined range of $x$ itself:

$$E(x) = P_M(x).$$

This parameter is paramount in our data-driven methodology, its magnitude is prescribed by previously measured data, which both limits and biases the values of $N(x)$ accordingly via application of equation (1) (random sampling of the NHPP). Together equations (1)–(4) provide a data-driven and biophysically viable methodology to estimate the number of NP agglomerates per EAD, $N(x)$, over the course of its lifetime $\tau$. Finally, figure 1(c) is a schematic of the experimental set-up at the end of the experiment (1 h); the diagram indicates that previously distinct NP agglomerates within an individual EAD have been condensed into a single aggregate through the internalization process (red ellipses); where total NP number is conserved. A TEM image of a NP aggregate within an endosome is shown on the right-hand side of the figure (scale bar is 100 nm). The total number of NPs per endosome is simply deduced via the summation:

$$N_E = \sum_x N(x),$$

Using equation (5) we can stochastically generate corresponding data to that measured experimentally. Specifically, we can calculate $N_E$ for 500 simulated endosomes and determine their corresponding probability mass distribution to compare with that deduced experimentally within endosome compartments 1 h post NP load.

**In vitro ISDD model**

The ISDD model was used to calculate the transport rates of QTracker 705 CdTe/ZnS quantum dot agglomerates in the cell culture media in [11]. A comprehensive review of the equations governing particle diffusion and sedimentation are provided by Hinderliter et al [26], furthermore the paper provides a MATLAB script to solve the various equations and numerous applications of the model. We modified the ISDD model parameters to make the solution specific for QTracker 705 (CdTe) quantum dots and the biological assay used; all parameters used are displayed in table 1.

The ISDD model provides an estimation of the diffusion and sedimentation rates as a function of number of NPs per agglomerate for a media depth of 287 $\mu$m over the 1 h period of the experiment; these are displayed in figure 2, blue line with ‘x’ markers and green line with circle markers.
Table 1. Empirical values of experimental and ISDD parameters.

<table>
<thead>
<tr>
<th>NP</th>
<th>CdTe</th>
</tr>
</thead>
<tbody>
<tr>
<td>NP Concentration (nMol), Nfi</td>
<td>10</td>
</tr>
<tr>
<td>Major Axis Length (nm)(a)</td>
<td>10</td>
</tr>
<tr>
<td>Packing fraction (nm(^{-2}))(b)</td>
<td>0.02</td>
</tr>
<tr>
<td>Fractal dimension(b)</td>
<td>2.3</td>
</tr>
<tr>
<td>Area of flask, (A_f) (m(^2))</td>
<td>(75 \times 10^{-4})</td>
</tr>
<tr>
<td>Media volume (mL), (V^M)</td>
<td>2</td>
</tr>
<tr>
<td>Media depth ((\mu)m)</td>
<td>287</td>
</tr>
</tbody>
</table>

\(a\) Hondow \(et al\) [11].

\(b\) Estimated as \(d_f + 1\) (see Falconer [31], chapter 6), where \(d_f\) is the fractal dimension of the 2d projection of the actual 3d NP aggregate, i.e. TEM image.

Figure 2. Simulated transport properties of CdTe NP agglomerate generated by the ISDD model. The solid black line is the mean transport rate of agglomerate to the cell surface, \(\gamma(x)\). The curves associated with the blue ‘x’ and green circle markers indicate the individual diffusion and sedimentation rates respectively. The dominant transport mechanism switches from diffusion to sedimentation for \(x > 100\) NPs. The minimum of \(\gamma(x)\) at \(x \approx 100\) NPs suggests agglomerates around this size are transported least rapidly to the cell surface.

respectively. The solid black curve in figure 3 is the mean agglomerate transport rate as a function of the number of NPs per agglomerate, \(\gamma(x)\), which is an average of these two processes and is employed within equation (3) to estimate the number of NPs per agglomerate dependent, Poisson distributed, integer multiplier in equations (1) and (5). The ISDD calculation predicts that \(\gamma(x)\) is a minimum for \(x \approx 100\) NPs per agglomerate; that is agglomerates of this size are the slowest to reach the cell surface; above and below this value transport is dominated by sedimentation and diffusion respectively.

Calculation of the mean number of NPs per endocytic active domain \(N_{EAD}\)

From the experimental parameters given in table 1 we can estimate \(N_{AER}\) from the following expression:

\[
N_{EAD} = N_f \times \frac{A_{EAD}}{A_f},
\]

here \(N_f\) is the number of NPs in the culture flask, \(A_f\) is the area of the culture flask and \(A_{EAD}\) is the mean area of an EAD. The magnitude of \(N_f\) is calculated via the expression:

\[
N_f = N_A \times N_i \times V_M,\]

where \(N_A\) is Avogadro’s constant [22]. The latter parameter is determined empirically; the major axis length of the 500 endosome sample was quantified through image based analysis, the mean, standard deviation and the lower and higher extremities were determined to be 213, 102, 62 and 497 nm respectively. There magnitudes are congruent with that measured through stochastic optical reconstruction microscopy [30]. We approximate the EAD capture area in our simulations to be circular given by \(A_{EAD} = \pi R_E^2\).

Results

Figure 3(a) plots the PMFs corresponding to the experimentally determined number of NPs per agglomerate, \(x\) [11, 15]. The PMF of \(x\) measured at 0-h in media, \(P^M(x)\), is the black curve with circle markers, the PMF corresponding to the number NPs per endosome measured after 1 h, \(P^E(x)\), is the red curve with square markers. In both experimental cases, 500 randomly selected NP agglomerates/aggregates were selected and imaged via TEM, the number of distinct NPs within each cluster was determined via image analysis routines run on MATLAB [11].

To capture the observed variability associated with \(x\), both curves in figure 3(a) are plotted on a semi-log \(x\)-axis. In media, \(x\) varies over the interval 1 to \(\approx 800\) NPs; TEM images in figures 2(b) and (c), show examples from within the range, where the centroid positions of each individual NP within the agglomerate (red dots) is also shown [11]. Similarly, figures 2(d) and (e) display TEM images of low and high NP aggregate densities (17 and 320 NPs respectively) within endosome compartments, where \(x\) now spans the extended interval 1 to \(\approx 1500\) NPs. Comparing \(P^M(x)\) and \(P^E(x)\), it is evident that the most probable magnitude of \(x\) has increased by two orders of magnitude (from 1 to 546 NPs), suggesting an accumulation of distinct NP agglomerates occurs during the endocytic process. Accumulation of NP agglomerates can take place at the cell surface within the lifetime of the EAD or may occur between early endosomes post internalization. In our methodology the exact biophysical mechanism(s) cannot be identified, but we have confidence that they have occurred due to the observed positive shift shown by the respective PMFs over the duration of the experiment.

The experimental data in figure 3 is recast to the equivalent cumulative distribution function (CDF) form in figure 4; classification of curve colours/markers is preserved, i.e. the CDFs in figure 4(a), \(F^M(x)\) and \(F^E(x)\), correspond to
that generated from experimental measurements of NP agglomerates in cell culture media and within endosome compartments respectively. In alignment with that measured experimentally, we evaluate equation (5) for 500 trials and estimate the number of NPs per endosome \(N_E\) for each trial. From this data we can calculate \(F^E_N(x)\), an in silico predicted CDF via the NHPP. \(F^E_{\text{NHPP}}(x)\) is also displayed in figure 4(a) as the blue curve with ‘x’ markers. A statistical assessment of \(F^E_N(x)\) and \(F^E_{\text{NHPP}}(x)\) through application of a two-sample Kolmogorov–Smirnov test does not reject the null hypothesis at a significance level of 1% (\(p\)-value of 0.999), suggesting that both distributions are equivalent. The accuracy of fit between \(F^E_{\text{NHPP}}(x)\) and \(F^E(x)\) was iteratively achieved through optimization of the magnitude of the mean lifetime of an EAD, \(\tau\), the models only fitting parameter. Throughout the optimization process the mean EAD radii \(R_E\) was fixed at 213 nm (sample mean of the 500 TEM images), this magnitude is comparable to that of clathrin-coated pits.

Figure 3. (a) PMFs of the number of constituent nanoparticles measured per cluster in media and within endosome compartments 1 h post nanoparticle load, black and red curves (circle/square markers) respectively. 500 clusters for each situation were examined to generate the PDFs. (b) and (c) TEM images of two typical NP clusters containing 1 and 51 individual NPs respectively; both images were measured in the media surrounding the cellular population. Figures (d) and (e) display TEM images of two endosomes containing NP clusters, the total NP load in the first is 17 NPs and 320 NPs in the second. Bright field TEM image contrast has been inverted such that NPs give white contrast and their identification by the image analysis script is shown as red dots. The scale bar for image (b) is 60 nm, for image (c) is 75 nm, for image (d) and (e) is 100 nm.

Figure 4. Comparison of the CDFs associated with the number of NPs per agglomerate measured experimentally and that predicted via the NHPP. (a) The black curve with circle markers and the red curve with square markers are the CDFs of the measured data at 0 h in media and 1 h post NP load within endosome compartments respectively (i.e. \(F^M(x)\) and \(F^E(x)\)). The blue curve with ‘x’ markers is the optimized CDF predicted by the NHPP methodology, \(F^E_{\text{NHPP}}(x)\); the mean lifetime of the EAD was determined to be \(\tau = 63\) s when \(R_E = 213\) nm. A two-sample Kolmogorov–Smirnov test on \(F^E(x)\) and \(F^E_{\text{NHPP}}(x)\) does not reject the null hypothesis at a significance level of 1% (\(p\)-value of 0.999). (b) The data points (circle markers) show the PMF associated with the predicted number NP agglomerates per EAD. The PMF is from 500 simulated EADs using the optimized value of \(\tau\) and the sample average endosome radii. The data is fitted by the Poisson distribution (black dashed line) which predicts that a mean number of \(\sim 3\) NP agglomerates in media combine to form larger aggregates measured within the endosome. (c) Here the data points (circle markers) indicate the PMF associated with the number of NPs per agglomerate that will merge across the endosome population.
measured through stochastic optical reconstruction microscopy [30]. Location of the optimized lifetime value $\tau$ was established through numerical minimization of the $L_2$-norm of $F_{\text{NHPP}}^E(x)$ and $F^E(x)$. Thus the optimized mean lifetime of an EAD was found to be 63 s, corresponding favourably to the lifetimes measured directly through high-resolution microscopy techniques [27, 28].

At the optimized value of $\tau$ and $R_E$ fixed at 213 nm, we calculate the PMF associated with the number of constituent NP agglomerates per EAD, $N(x)$, over the 500 trials. The PMF of $N(x)$, $P(N(x))$, is displayed in figure 4(b) (circle markers) also shown by the black dashed line is a Poisson distribution fit to the calculated data ($p$-value $= 0.001$). The mean rate ($\lambda(N(x)) = 3.05$) of the Poisson distribution indicates that 3 distinct NP agglomerates merge within the lifetime of the EAD to form a larger internalized aggregate. The main features of figure 4(c) indicate that the most probable NP agglomerates that undergo a fusion event are those containing 10–20 NPs, and those containing 300–400 NPs, additionally there is a low probability that agglomerates containing $\sim$100 NPs will merge and zero probability of individual agglomerates $>800$ as they have not been detected experimentally, so are not sampled. These features approximately reflect the mean rate of transport of the NP agglomerates to the EADs generated by the ISDD model (see materials and methods—ISDD figure 2). The ISDD predicts high rates of transport to the cell surface for small (10 NPs) and large (300 NPs) agglomerates via diffusion and sedimentation respectively and a relatively slow transport of agglomerates that contain approximately 100 NPs. Thus, on average combinations of such NP agglomerates provides the mechanism that translates $P^M(x)$ to $P^E(x)$. The ISDD model also suggests relatively low numbers of 100 NP agglomerates in the internalized dose, however, even though there is a relative drop in probability at this size (see figure 3(a)) it is not expected to be significant as there is a strong likelihood that agglomerates of this magnitude can be created via the high probabilities associated with agglomerates of size 10–50 NPs combining.

Although the actual biological spatiotemporal location of the amalgamation events cannot be determined, the fact that we can statistically acknowledge their average occurrence and dispersion indicates specific properties of the cell-line/NP system. In particular, the PMF provides unresolved experimental information of how NP agglomerate dosage is transformed through endocytosis, one of the key factors limiting the development of nanomedicine based therapeutics and technologies.

To test the sensitivity of our methodology we investigated how the solution, i.e. $F_{\text{NHPP}}^E(x)$, varied if we (i) fixed the mean lifetime of the EAD at its previously optimized value of 63 s and varied the magnitude of $R_E$ contiguously from 62 to 497 nm (the extremities of the experimentally measured range) and (ii) holding $R_E$ fixed at 213 nm and varying $\tau$ over the interval [30, 300] seconds. For every iteration, 500 trials of equation (5) (reflecting the 500 measured endosomes) and the corresponding CDF ($F_{\text{NHPP}}^E(x)$) is deduced. After each in-silico experiment the mean and standard deviations of the respective CDF series is calculated, additionally the mean number of fusion events that have occurred for all iterations of the CDFs series is calculated and found to be $\sim$3 in both cases. The means (dashed black lines) and standard deviations (grey areas) associated with the variation of $R_E$ and $\tau$ are displayed in figures 5(a) and (b) respectively. For reference both $F^M(x)$ and $F^E(x)$ are also indicated on both figures, black line circles markers and red line square markers respectively.

The variation of $R_E$ corresponds physically to variation of the capture area associated with EADs; reduction of $R_E$ 

Figure 5. Sensitivity analysis of model (a) the magnitude of grey shaded area is $\pm$ one standard deviation the mean value of $F_{\text{NHPP}}^E(x)$ when we let $R_E$ range over the interval [62, 497] nm whilst $\tau$ remains fixed at its optimum value (63 s). (b) The magnitude of grey shaded area is $\pm$ one standard deviation the mean value of $F_{\text{NHPP}}^E(x)$ when $R_E$ is fixed at the sample average (213 nm) and the magnitude of the lifetime associated with an EAD varies over the range [30, 240] seconds.
vastly increases the variability of predicted $F(x)$ especially for aggregates having $x < 100$ corresponding to the diffusion dominated transport regime. For $x > 100$, $F(x)$ does not deviate substantially from the optimum CDF shown in figure 4(a) suggesting that at least one of the three fusion events likely to occur is between relatively large agglomerates. As the magnitude of $R_E$ increases in size past the sample mean the calculated CDFs are shifted positively in $x$. This is unsurprising as (i) equation (6) indicates that the number of agglomerates at the EAD will increase proportionally to the magnitude of $R_E$, and (ii) a large proportion of these agglomerates will be that driven by sedimentation as this on average is the dominant transport mechanism an is associated with the larger NP agglomerates. Figure 5(b) illustrates the variability of $F(x)$ when the lifetime of the EAD is varied from half its optimized value to that five times greater than its optimized value and the capture area of the EAD is fixed at $-0.014 \mu m^2$. The general features of the variability follow that observed for $R_E$ variation, i.e. larger fluctuation in $F(x)$ for $x < 100$ for small EAD lifetimes, and a positive shift in magnitude of $F(x)$ as the lifetime is increased well beyond the optimized value of 63 s. In an analogous manner to that previously described, this shift is not surprising as we are again increasing the possibility of larger agglomerate fusion events as they have the dominant transport mechanism in these simulations. The generally low dispersion observed for $F(x)$ (for $x > 100$ NPs) is interesting and suggests that the net NP aggregation by endosomes is insensitive to both the magnitude of the EAD and its mean lifetime. The former feature reflects TEM measurements that indicate small NP agglomerates are found within much larger endosome compartments and equally many large NP agglomerates are found within similar sized compartments (e.g. figures 3(d) and (e)). Ongoing and future experiments will quantify this feature further. The larger fluctuations of $F(x)$ for small $x$, in both cases, is related to increased sampling variability and will have a major impact on the predictability of dosage when no agglomeration is present, i.e. for monodispersions of NPs.

Discussion

This study directly addresses key factors limiting the development of nanomedicine based therapeutics; we precisely quantify actual NP dosage as opposed to that perceived, in doing so we encapsulate the innate heterogeneity of the nanotherapeutic state. We provide a robust methodology that allows the trafficking of NP dosage across biological barriers to be understood quantitatively which provides the basis for predictive modelling of nanopharmacology. In this study, we have focused on quantifying biological barrier trafficking of Qtracker 705 quantum dots exposed to U-2 OS cells in McCoy’s 5a medium media.

The methodology couples high spatial resolution TEM with pertinent physical models that together are statistically sampled to infer the dynamical properties of a NP dose. Specifically, through TEM measurements [11] we characterize the aggregating properties associated with NP agglomerates at two distinct spatiotemporal biological positions (i) in biological media and (ii) within cellular endosome compartments in human osteosarcoma cells [15, 17, 19–21, 23, 24]. The statistical profile of NP dose at these distinct spatiotemporal positions was captured by PMFs that summarize the properties of 500 quantum dot NP agglomerates, which describe the heterogeneity of particle number within measured agglomerates. We detailed and developed a stochastic transfer function (STF) that permits evolution of states from $P^M(x)$ to $P^E(x)$. The STF has two principal components, firstly the previously reported ISDD model [26] is embedded to provide a mean rate of NP agglomerate transport to the cell surface and (ii) system heterogeneity simulated through application of a nonhomogeneous Poisson distribution, which stochastically determines agglomerate arrival at the cell surface where it may be part of and endocytic event and subsequently internalized by a cell. The STF’s principal fitting parameter reflects the lifetime of an endocytic event, its optimized magnitude was found to be commensurate with direct measurements of clathrin-coated pits through high-resolution microscopy techniques [27, 28]. Further analysis of the STF provides previously unresolved dynamics of the NP agglomerate traverse across the cell membrane, quantifying statistically agglomerates fusion as NP dose is translated from cell-culture media to endosome vesicles. Through optimization and sampling of the statistical methodology we are confident in stating that the heterogeneity of the internalized NP dose (reported previously [15, 24]) is a result of the initial, inhomogeneous dispersion of the NPs in the cell culture media used for particle exposure.

This manuscript has developed a statistical framework for the detection (by TEM), quantification and prediction of quantum dots dispersed in media and following uptake by any cells all at the scale of the individual quantum dot. Future work will examine and assess how specific variables of the system, e.g. cell/NP type, NP surface coating, concentration or applied exposure dose of NPs have on the heterogeneity measured at both temporal locations and how these are statistically translated across the biological membrane. Additionally, we will combine the methods presented here with that previously developed [15] to fundamentally link high-throughput flow cytometry measurements with TEM based statistics to provide accurate assessment of actual NP dosage and its evolution and redistribution across a large cellular population over significant periods.

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