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Article:

Gooding, JD, Crook, R and Tomlin, AS orcid.org/0000-0001-6621-9492 (2015) Modelling of roof geometries from low-resolution LiDAR data for city-scale solar energy applications using a neighbouring buildings method. *Applied Energy*, 148. pp. 93-104. ISSN 0306-2619

<https://doi.org/10.1016/j.apenergy.2015.03.013>

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1 Modelling of Roof Geometries from Low-resolution LiDAR Data for City-Scale 2 Solar Energy Applications using a Neighbouring Buildings Method

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6 Abstract

7 This article describes a method to model roof geometries from widely available low-resolution (2 m
8 horizontal) Light Detection and Ranging (LiDAR) datasets for application on a city wide scale. The
9 model provides roof area, orientation, and slope, appropriate for predictions of solar technology
10 performance, being of value to national and regional policy makers in addition to investors and
11 individuals appraising the viability of specific sites. Where present, similar buildings are grouped
12 together based on proximity and building footprint dimensions. LiDAR data from all the buildings in a
13 group is combined to construct a shared high-resolution LiDAR dataset. The best-fit roof shape is
14 then selected from a catalogue of common roof shapes and assigned to all buildings in that group.
15 Method validation was completed by comparing the model output to a ground-based survey of 169
16 buildings and aerial photographs of 536 buildings, all located in Leeds, UK. The method correctly
17 identifies roof shape in 87% of cases and the modelled roof slope has a mean absolute error of 3.76°.
18 These performance figures are only possible when segmentation, similar building grouping and ridge
19 repositioning algorithms are used.

20 Highlights

- 21 • Automated modelling of roof geometries from low-resolution LiDAR data
- 22 • 87% success rate in recognition of roof shape
- 23 • Roof slope estimated with 3.76° mean absolute error
- 24 • City-scale applicability
- 25 • Improves accuracy of solar photovoltaic installation performance predictions

26 Keywords

27 Solar; LiDAR; Urban landscape; City; Microgeneration

28 1 Introduction

29 Photovoltaics (PV) and solar water heating are two climate change mitigation technologies that can
30 be installed on the rooftops of individual properties and offer substantial emission savings [1, 2]. The
31 sector has experienced tremendous growth in recent years [3-5] but its expansion remains mostly
32 dependent on a very large number of decisions to invest in separate projects [6]. The absence of
33 reliable performance projections has been identified as a major barrier to the uptake of low carbon
34 technologies among individuals [7], landlords and local governments [8]. The roll-out of solar
35 technologies on a city wide scale could be supported by mapping the feasibility of solar installations
36 [7] to influence not only individual property owners but also those responsible for entire portfolios.

37 This process must be supported by accurate installation performance projections [9, 10] not on a
38 case-by-case basis, but at the city scale where many thousands of potential investment decisions
39 require information.

40 The city wide approach has further advantages beyond influencing small-scale investment as policy
41 makers would have access to estimations of the regional and national potential of the technologies
42 underpinned by locally accurate appraisals from the city-scale. This could move decision making
43 away from top-down studies based on generalised socio-economic trends that, by their nature,
44 cannot be inspected to the individual property level.

45 The accurate appraisal of a proposed solar installation's performance requires detailed knowledge of
46 the property's geometry and positioning [11]. Height above sea level LiDAR data aggregated into a
47 digital surface model (DSM) is a data source that can be used to estimate this information for
48 buildings across an entire city as various sources demonstrate [12-15]. Resolution is critically
49 important when attempting to model the slope, orientation and available area of roofs as it controls
50 the amount of height data available for the appraisal of each building. Currently in the UK, the
51 availability of DSMs with a horizontal resolution finer than 2 m is limited to small areas of cities at
52 prohibitively high costs. We previously reported that more widely available low-resolution 2 m data
53 is too coarse to provide an accurate reflection of the number of roof planes and their angles when
54 the plan area of a building is less than approximately 200 m² [16]. This is particularly problematic for
55 city-scale roof shape modelling given that building footprint data for Sheffield, a typical UK city,
56 shows that over 70% of properties fall below this threshold [17]. This is a fundamental problem
57 because it is at these properties where the greatest interest in microgeneration investment lies.

58 DSM data collection processes detect overhanging trees, chimneys and dormer windows which lead
59 to inaccuracy in the assessment of building height and is exacerbated by the incumbent vertical error
60 of the measurements that can be as great as 0.15 m [18]. This is significant as small property roofs
61 are typically less than 3.5 m in height from eave to ridge. In addition, the datasets are also prone to
62 noise and poor geospatial referencing. These issues mean that small property roof shapes and the
63 angles of their facets are inaccurately appraised using low-resolution DSM data and basic
64 interpolation. Due to these problems the most suitable approaches to roof reconstruction from low-
65 resolution DSM data are model-driven methodologies as opposed to data-driven ones. The two
66 types of methodology have been defined by Maas and Vosselman [19]. Data-driven methodologies
67 establish planes directly from the DSM or following a small degree of alteration. By contrast, model-
68 driven approaches compare DSM data to a series of common roof shapes, or 'templates', with the
69 quality of fit quantified, and the best performing template accepted as the modelled roof shape.
70 Tarsha-Kurdi et al. [20] provide analysis and comparison of both approaches to further aid
71 distinction between the two, stating that data-driven methods have a fundamental assumption that
72 buildings are an aggregation of several segmented roof planes. Model-driven methodologies
73 however, test the quality of fit when matching raw data to the most similar roof shape from a library
74 of pre-defined shapes. This means that a model-driven methodology will always return a logical roof
75 shape whereas data-driven methods have been found to misinterpret low-resolution data and
76 suggest a large number of nonsensical roof facets on each property [21].

77 **2 Method**

78 Here we describe a methodology that builds on previous model-driven approaches by incorporating
79 a number of novel elements. We first apply segmentation processes to building footprint data in
80 order to remove peripheral building components, thus disregarding small building protrusions (<20
81 m²) that are unsuitable for solar technologies. The resulting segmented building footprints are
82 assumed to define locations within the DSM containing roof-space potentially suitable for solar
83 technologies. They are also used to estimate orientation and to provide a basis for identifying
84 similarities in the roof shapes of neighbouring properties. Buildings within the same 250 m x 250 m
85 areas are then grouped together if their segmented building footprint dimensions are similar. There
86 is then a process to combine the DSM data from properties of the same group, thus creating a pool
87 of DSM data of a finer resolution than from the original individual properties. The combined data is
88 then compared to a series of common roof shapes in a model-driven approach, with the best fit
89 selected as the modelled roof shape in a similar method to that of Huang et al. [22], Lafarge et al.
90 [23] and Henn et al. [24]. Where there are no similar buildings to a particular property, outliers from
91 the segmented individual building's data are removed before the ridge repositioning and template
92 comparison proceed.

93 The outputs of the methodology are the shape, slope, orientation and plan and sloped area of roofs
94 in a study area. As such, the methodology can also better inform three-dimensional city models
95 which have a wide variety of applications including solar resource estimation. The modelled data are
96 validated against measured data from a large number of buildings within the city of Leeds, UK. The
97 method has been designed for application on a city wide scale meaning it can be implemented for a
98 large number of buildings using only moderate computing power. Furthermore, its use of commonly
99 available low-resolution DSM and building footprint data mean its application may be viable in more
100 locations than those requiring finer resolution data.

101 **2.1 Footprint Segmentation**

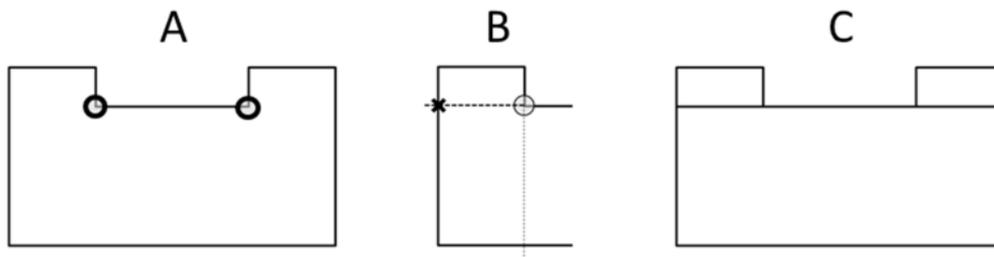
102 This process aims to establish the largest rectangle that can be inscribed in the original building
103 footprint. Since the DSM only provides height above sea-level information, the boundaries of each
104 property are established using building footprint data sourced from Digimap [25]. The footprint data
105 is of sufficient detail to include conservatories, porches and other protrusions on small properties
106 which are unlikely to be suitable for solar installations. In addition, such building features can
107 confuse template matching processes as they lead to a wide variety of height measurements across
108 a building which are not representative of the main roof shape.

109 Segmenting polygons into simple shapes is a basic problem in computational geometry with a body
110 of literature describing potential solutions for specific conditions. A first level of complexity was
111 explored by Fischer and Höffgen [26] who examined inscribing axis-parallel polygons to convex
112 polygons. Daniels et al. [27] and Boland and Urrutia [28] presented methodologies of greater
113 complexity that consider polygons containing both concave and convex angles but still only accept
114 axis-parallel inscribed rectangles which may not define the largest possible rectangle. Conversely,
115 Knauer et al. [29] and Molano et al. [30] have recently explored the problem of computing the
116 largest rectangle of any orientation but only with regard to convex polygons. Hence despite the
117 range of approaches, no single methodology provides a definitive solution to the particular problem
118 faced in this work. However, the building footprint data consists of polygons with characteristics that
119 can be exploited to create a relatively simple and computationally efficient solution. For instance,

120 the small property polygons never feature internal holes, a large (>16) number of vertices or more
121 curved than straight lines which all increase computational time [30]. There also tends to be a right-
122 angled vertex of the original building footprint that forms part of the largest rectangle that could be
123 inscribed. Utilising these traits, the processes described in the following sections were developed for
124 polygon types of differing complexity.

125 2.1.1 Polygon Type 1

126 Polygons with internal angles that are all approximately 90 or 270° are segmented by proposing
127 locations for a fourth vertex of a protrusion in the original building footprint outline. Concave angles
128 in the footprint outline are identified (Figure 1A) as starting points for two intersection lines (Figure
129 1B), the first of which runs from the vertex preceding the concave angle, through the concave angle
130 itself and on to its intersection with the polygon outline (Figure 1B grey line). The second line
131 proceeds from the vertex following the concave angle through the concave angle and on to its
132 intersection with the polygon outline (Figure 1B black line). The intersection point of the shorter line
133 defines the fourth vertex of a smaller shape within the building footprint (marked with a cross in
134 Figure 1B).

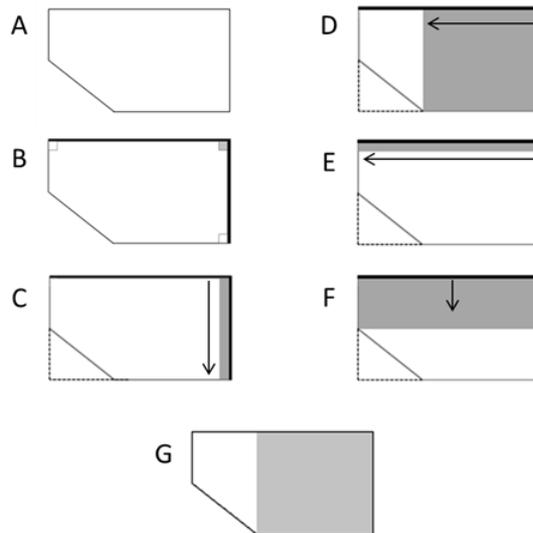


135
136 **Figure 1 Segmentation process from concave angles. A: Two concave angles circled. B: Creation of intersection lines from**
137 **a concave angle and identification of an intersection point (denoted by cross) on the shortest. C: Final segmented shape**
138 **after intersection process repeated for the second concave angle**

139 Figure 1C shows a polygon with two segmented protrusions and a large rectangle that is assumed to
140 define the location of the building's main roof part in the DSM.

141 2.1.2 Polygon Type 2

142 The process described above fails on polygons with internal angles that are not 90 or 270° (Figure
143 2A). For such polygons a second process is presented in which a rectangle is expanded from an
144 internal right-angle of the footprint outline. First, the longest pair of lines to form a right angle in the
145 original building footprint (Figure 2B bold line) are identified and used to project a fourth vertex of a
146 new rectangle (Figure 2C dotted lines) that will be referred to as the 'large rectangle'.



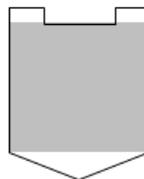
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151

Figure 2 A: Original footprint. B: Longest pair of lines to form a right angle (bold line). C: Large rectangle (dotted lines) formed from the longest right-angled lines. Also shows iterative expansion of a new, inner rectangle along width of large rectangle. D: Second expansion along length of large rectangle. E & F: Repetition of expansion process (length first). G: Larger shape created by the two expansions (in grey) accepted as main roof part of original footprint.

152 A 0.5 by 0.5 m rectangle is constructed at the intersection of the two longest lines to intersect at a
153 right-angle (Figure 2B, grey square) that will be referred to hereafter as the ‘new rectangle’. The new
154 rectangle is expanded in increments of 0.1 m along the width of the large rectangle until it no longer
155 fits inside the original building footprint (Figure 2C). The enlarged new rectangle is then expanded in
156 increments of 0.1 m along the length of the large rectangle again until it no longer fits inside the
157 original building footprint (Figure 2D) which defines a first inscribed rectangle. The double expansion
158 process is then repeated but with extension by length preceding the enlargement in width (Figure 2E
159 & F) to create a second inscribed rectangle. The larger of the two inscribed rectangles is selected as
160 the best approximation for the location of the property’s main roof structure from within the
161 original building footprint (Figure 2G, grey rectangle).

162 2.1.3 Polygon Type 3

163 A small proportion of polygons fail the criteria of the processes described above, an example of
164 which has been provided in Figure 3.



165
166
167

Figure 3 Polygon (black outline) containing interior angles not approximately 90 or 270° and without right-angled vertices in common with the final desired segmented polygon (grey rectangle)

168 Here the interior angles are not all approximately 90 or 270° and do not share right angles in
169 common with the final segmented polygon. A brute force method is implemented for these polygons
170 whereby a small rectangle is expanded and rotated incrementally from the centre of the original
171 building footprint until it occupies the largest space of the original building footprint. There is no
172 prior information to deduce if a building footprint shares any vertices in common with its final
173 segmented building footprint so if the polygon is not type 1, the processes for polygon types 2 and 3

174 must both be executed. The larger inscribed polygon resulting from the two processes is accepted as
175 the segmented building footprint.

176 The solutions for polygon types 2 and 3 are iterative procedures that reflect the lack of an elegant
177 mathematical solution for this problem. The resulting modified building footprints are more suitable
178 for identifying the location of roof shapes suitable for solar technologies within the DSM for
179 extraction. Figure 4 shows an example of the outcome of the segmentation process when applied
180 across a neighbourhood.



181
182 **Figure 4 Segmentation of building footprint data (left) across a neighbourhood to extract major roof parts (right) in**
183 **neighbourhood 690**

184 The segmented polygons also provide a way to assess the size and orientation of roof structures,
185 saving significant computational time compared to Huang et al. [22] who use only DSM data and find
186 building locations by 'blob detection' and size and orientation by localised iteration.

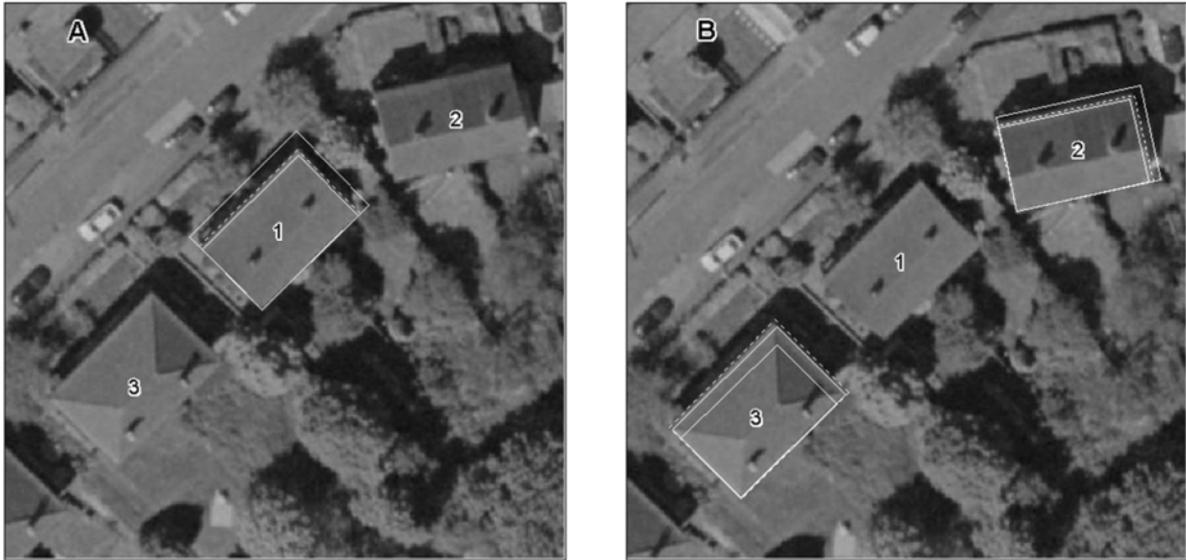
187 **2.2 Data Combination Procedures**

188 It is important to note here that the combination of data is limited to neighbourhoods where there
189 are similar buildings. The DSM data from buildings that do not share a similar neighbour still undergo
190 the processing steps outlined below and are then compared to a series of roof templates without
191 any combination of data and thus remain at low resolution.

192 **2.2.1 Similarity Identification**

193 The dimensions of the segmented building footprints are used to identify similar shapes within
194 62,500 m² neighbourhoods. The buildings are categorised using bins of 1.1 m for length and 1.2 m
195 for width which were empirically found to be robust thresholds to group similar buildings together.
196 Buildings within the same bins for both dimensions are assigned to the same similarity group to have
197 their DSM data combined following further processing.

198 The following paragraphs describe how the tightly constrained plan dimensional thresholds enable
199 the grouping of buildings with identical roof shape. For example buildings 1, 2 and 3 in Figure 5 are
200 within the same 62,500 m² neighbourhood and have plan dimensions that are alike, but building 3
201 has a different roof type (hipped) to 1 and 2 (both gabled).



202
 203 **Figure 5 Similarity thresholds.** The small, solid white rectangles have the shortest length and width of the bin to which
 204 the building footprint (dotted white line) is a member. The larger, solid white-lined rectangle has the longest length and
 205 width of this bin.

206 The bin sizes used to assign similarity grouping are based on increments of 1.1 m for width and 1.2 m
 207 for length. For example, building 1 has a length of 13.05 m and width of 8.28 m and falls in to a bin
 208 of 12.58 m to 13.78 m for length and a 7.98 m to 9.08 m bin for width. Figure 5A shows two
 209 rectangles constructed around the segmented footprint of building 1 (dotted outline). The smaller
 210 white outline has the dimensions of a rectangle with the smallest width and length of their
 211 respective bins creating a rectangle 12.58 m in length and 7.98 m in width. The larger white
 212 rectangle has dimensions equal to the longest edges of each bin, meaning a length of 13.78 m and a
 213 width of 9.08 m. For buildings 2 or 3 to be considered similar to building 1 they must have a
 214 segmented footprint that fits between the solid white lines.

215 Figure 5B shows that the footprint of building 2 fits between the solid white lines meaning it would
 216 be considered a similar building. The footprint for building 3 extends out of the two solid lines and so
 217 would not be grouped as similar to buildings 1 and 2. The method detects small differences in plan
 218 dimensions that reflect differences in building construction and roof shape.

219 **2.2.2 Outlier Identification and Height Normalisation**

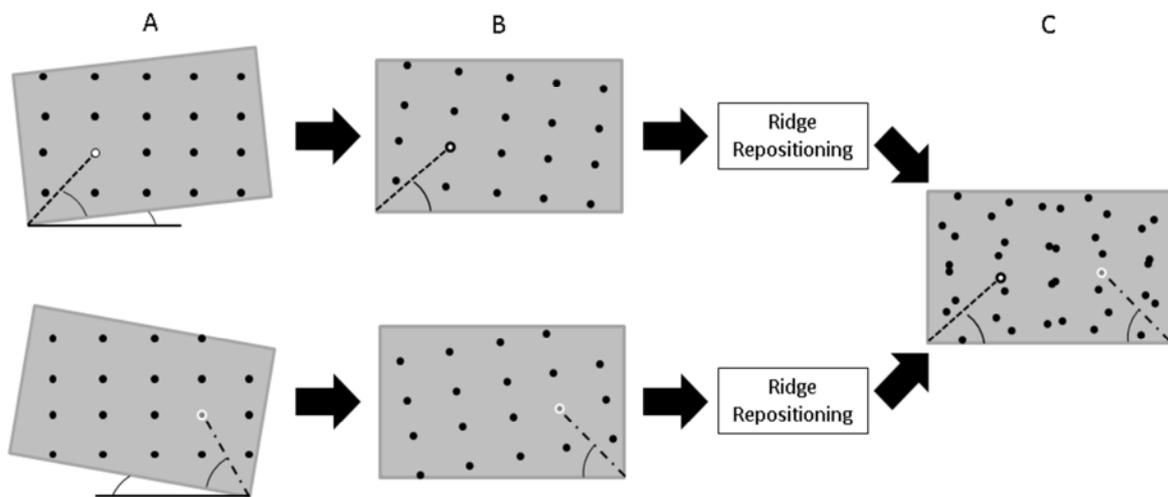
220 Building footprint and DSM data are often misaligned which can result in ground height data
 221 appearing inside a building footprint or conversely, roof data falling outside and being mistakenly
 222 disregarded. DSM data also tends to contain many outliers that must be identified and removed.
 223 Therefore, data points with an absolute height difference greater than 1.5 m compared to the
 224 average of their neighbours were removed.

225 DSMs provide height above sea-level measurements which means that data from two buildings
 226 cannot be directly combined without first normalising the heights such that they are made relative
 227 to ground or eave level. Therefore, the lowest height measurement of each property following the
 228 removal of outliers is used to define the roof's minimum height. The relative heights of the building's
 229 data points are then established by subtracting this minimum height from each DSM data point
 230 contained by the relevant segmented building footprint.

231 **2.2.3 Rotation, Ridge Repositioning and Combination**

232 To enable the combination of similar buildings' data, each segmented building footprint and the
233 DSM data it contains are rotated until the lengths of the footprint are made axis-parallel. The
234 processed DSM data of similar buildings from a neighbourhood are then combined and in doing so a
235 dataset of far higher resolution than the original individual buildings is obtained. The following
236 paragraphs explain how this and the outlier identification algorithm are executed using a gable roof
237 shape template as an example because it is the clearest to visualise. The same approach is applied to
238 the hipped, long hipped and pyramidal templates.

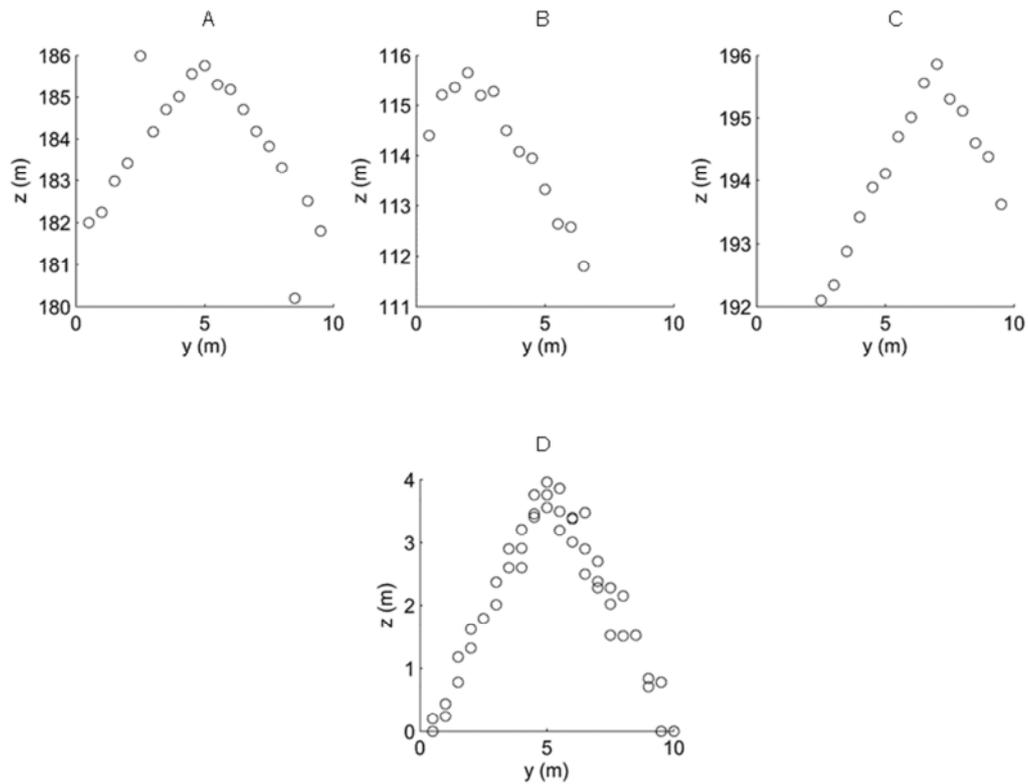
239 The angle between the horizontal and the most southerly line in the building footprint outline is
240 calculated as are the angle and distance of each DSM data point from the most southerly vertex of
241 the building footprint (Figure 6A). This information is used to re-project the DSM data points into
242 position when the building footprint is rotated to make its length axis-parallel (Figure 6B).



243
244

Figure 6 Data rotation and combination procedure

245 The rotated data is used to assess the true position of roof ridges in the data extracted from the
246 DSM using each building footprint. Due to misalignment between the building footprint data and the
247 DSM, the geometric centre of a segmented building footprint is often not the location of the tallest
248 DSM data as would be expected for a symmetrical roof with accurate positioning. This problem is
249 addressed to ensure that data from similar buildings are overlaid correctly. The data is split into 0.7
250 m bins along the y-axis of rotated data from individual buildings with ridge location identified by the
251 bin containing the highest average DSM data.



252
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Figure 7 A-C: Rotated DSM data for three similar gable buildings prior to combination viewed from the y, z perspective.
D: Combined data following height normalisation, outlier identification and ridge repositioning processes

255 Figure 7A-C show datasets with issues that must be addressed prior to data combination. Figure 7A
256 has two outlier data points whilst B and C show the outcome of particularly poor alignments
257 between building footprint and DSM data as two aligned datasets would lead to a peak near 5m on
258 the y -axis. Consequently B contains little data for the left hand side of its roof whilst the data in C
259 has no information regarding its lower right hand side. All three datasets must also have their
260 heights normalised prior to combination. The result of the combination procedures is demonstrated
261 in Figure 7D where there is a complete roof profile free of outliers at a far higher resolution than
262 data for individual roofs could provide.

263 2.3 Template Construction and Selection

264 The combined data is then compared to the set of common roof shapes shown in Figure 8 with the
265 best fitting selected as the most appropriate model of the similar buildings' roofs.

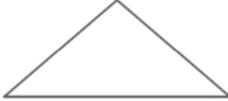
Plan	Width Elevation	Plan	Width Elevation
Flat 	Flat 	Shed 	Shed 
Gabled 	Gabled 	Hipped 	Hipped 
Pyramidal 	Pyramidal 	Long Hipped 	Long Hipped 

Figure 8 The roof template library

266
267

268 2.3.1 Construction

269 For a fair comparison the templates are constructed to achieve the best possible fit whilst
270 maintaining the integrity of their shape. Therefore, templates are constructed using the combined
271 data itself to establish eave and ridge heights from which the rest of the model shape is formed.

272 The data is first divided between the facets of the particular template depending on its x, y position.
273 Facet dimensions are defined by empirical evidence from aerial photography such that, for example,
274 the ridge length is 35% of the footprint length for the hipped template and 68% for the long hipped
275 template. Figure 9 shows a hipped template with four numbered facets.

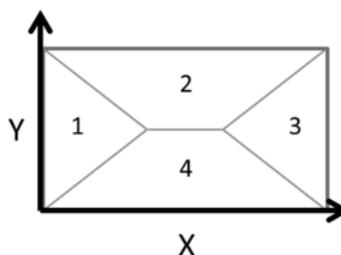


Figure 9 The four regions of a hipped template. 1 and 3: hip sections. 2 and 4: gable sections

276
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278 Owing to the directions of the template's slopes, the y-axis information is disregarded for sections 1
279 and 3 of Figure 9 and regression is applied to the x, z data. By contrast, only the y, z data of sections
280 2 and 4 is analysed. The MATLAB® robustfit function [31] is used to execute an iteratively reweighted
281 least squares fit that reduces the effect of any remaining outliers that were not identified by the
282 outlier identification criterion described in section 2.2.3. However, regression lines alone do not
283 constitute a satisfactorily modelled roof shape because they fail to meet at the same ridge height
284 and do not share a common eave height, which are two essential properties of a logical roof shape.
285 Hence the regression lines are used to establish average eave and ridge heights. Returning to the
286 hipped template example, the lowest and highest points of the four regression lines within the

287 facets are averaged by weight of the number of data points in their respective facets, thus
288 calculating the average minimum (eave) and maximum (ridge) heights of the prospective template.
289 The eave and ridge heights are then used to define the template's final shape by constructing facets
290 between them appropriate to the template type of plan dimensions relative to the average plan area
291 of all segmented building footprints in the relevant similarity group. At this stage, if the difference in
292 height from eave to ridge is less than 2 m, all templates except flat and shed are rejected.

293 **2.3.2 Selection**

294 The constructed templates are then compared to the combined data using a z-error (Δ_z) metric
295 similar to Huang et al. [22] such that,

$$296 \quad \Delta_z = \frac{\sum |Z_m - Z_d|}{K} \quad (1)$$

297 where Z_m is height above eave level suggested by the model, Z_d is the height above eave level of
298 the combined data and K the total number of data points in the combined data. The template with
299 the smallest Δ_z value defines the best fit and provides the modelled angles of facet slopes. The data
300 is compared to each template unless its length is less than 15.9 m, in which case the long hipped
301 template is not tested as in early investigations it was found to bare close similarity to the gable
302 template when scaled for building lengths shorter than this threshold.

303 **3 Validation and Applications**

304 **3.1 Data Sources and Test Area**

305 Building footprint data was sourced from EDINA [17], a centre that provides spatial data for UK
306 research institutions [32]. It provides the location and two-dimensional plan view shape of buildings
307 which were used in this study to establish areas of the DSM containing roof height information. The
308 2 m resolution DSM and aerial photography used in the validation were sourced from Landmap [18],
309 a service that provided UK academia with spatial data until December 2013 [33]. The methodology
310 was applied to seven randomly selected 62,500 m² suburban neighbourhood zones in North West
311 Leeds, UK containing a total of 536 buildings. Figure 10 shows four of the neighbourhoods selected.



312
313
314 **Figure 10 Four of the neighbourhoods tested using the methodology where the white lines represent the building footprint data prior to segmentation**

315 The accuracy of roof shape and orientation modelling was validated by comparison to aerial
316 photography. Slope estimation accuracy was appraised from site surveys for which a tripod-
317 mounted laser distance measuring device with an accuracy of +/- 20 mm over 150 m was used.

318 Across the seven tested neighbourhoods, the number of buildings within each grouping ranged from
319 2 to 68 and averaged 3.9. Typically 35% of buildings had to be regarded as individual for the tested
320 neighbourhoods. It should be noted that this is highly specific to the test locations and that regional
321 variations are to be expected. However, when the segmentation and similarity identification
322 processes were applied to all neighbourhoods across the city of Leeds, a similar figure of 29.2% of
323 buildings were defined as individual.

324 The similarity grouping criteria proved to be robust as comparison to geo-referenced aerial
325 photography showed only three buildings (0.6%) erroneously grouped with others that did not share
326 the same roof shape despite having similar plan dimensions.

327 **3.2 Model Outputs**

328 An example of the model's outputs is shown for neighbourhood 364 in Figure 11 where the buildings
329 are labelled by their similarity grouping before the modelled shape, angle and areas of each group
330 are described in Table 1. Facet 1 refers to the modelled slope of the gable section of each roof.
331 Where appropriate, facet 2 refers to the angle modelled for a hip roof section.



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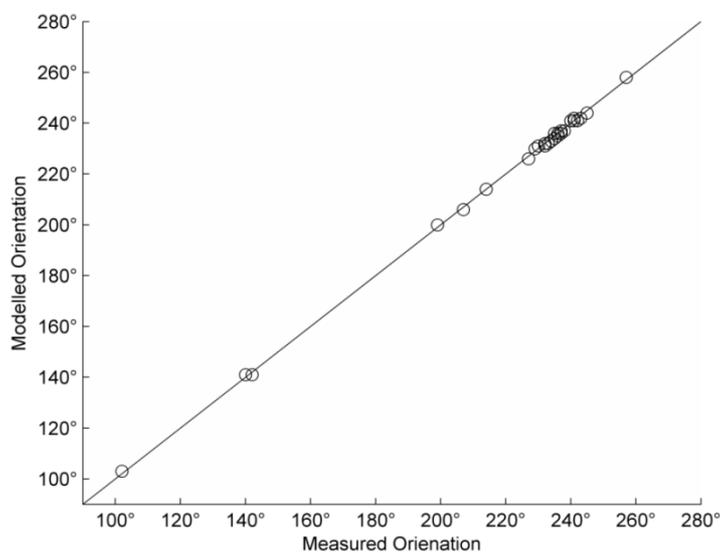
Figure 11 Neighbourhood 364 labelled by similarity grouping identification numbers

Group	Buildings (no.)	Modelled Shape	Actual Shape	Mean Segmented footprint Plan Area (m ²)	Mean Measured Plan Area (m ²)	Difference (% of Measured Area)	Facet 1 Modelled Slope (°)	Facet 1 Measured Slope (°)	Facet 1 Slope % Error	Facet 2 Modelled Slope (°)	Facet 2 Measured Slope (°)	Facet 2 Slope % Error
1	2	Flat	Flat	40.56	41.54	-2.37	n/a	n/a	n/a	n/a	n/a	n/a
2	1	Flat	Flat	68.98	72.17	-4.42	n/a	n/a	n/a	n/a	n/a	n/a
3	8	Hipped	Hipped	78.60	89.74	-12.42	29.12	29.62	-1.69	26.69	29.82	-10.50
4	1	Flat	Hipped	73.34	87.98	-16.64	n/a	32.5	n/a	n/a	31.29	n/a
5	1	Flat	Flat	46.07	43.59	5.69	n/a	n/a	n/a	n/a	n/a	n/a
6	1	Flat	Flat	199.00	186.5	6.70	n/a	n/a	n/a	n/a	n/a	n/a
7	5	Long Hipped	Long Hipped	158.92	183.78	-13.53	27.76	28.90	-3.94	31.97	29.68	7.72
8	1	Gabled	Long Hipped	152.00	184.09	-17.43	33.49	28.90	-15.88	n/a	29.68	n/a
9	18	Long Hipped	Long Hipped	164.31	184.58	-10.98	28.13	28.90	-2.66	33.45	29.68	12.70
10	2	Long Hipped	Long Hipped	176.50	187.67	-5.95	31.15	30.00	3.83	36.84	32.00	15.13
11	1	Gabled	Gabled	440.30	453.44	-2.90	11.71	11.40	2.72	n/a	n/a	n/a

Table 1 Model output for similarity groups of neighbourhood 364

335 For neighbourhood 364, the method successfully modelled roof shape in 39/41 (95.1%) cases. In the
336 two erroneous results, the buildings concerned were regarded as individual buildings and so could
337 only be modelled using the resolution of the input DSM.

338 The average error in the modelling of plan area for neighbourhood 364 was -6.75% and Table 1
339 shows that there was a slight underestimation in the majority of cases. This is due to both the
340 inherent inaccuracy of building footprint sizes and the adjustments made to polygons that were not
341 completely rectangular during the segmentation process. Slope was modelled with an average error
342 of 2.36% for facet 1 slopes in neighbourhood 364 whilst facet 2 slopes were modelled with an
343 average error of 6.26%. The greater error in the modelling of facet 2 slopes arises from the reduced
344 amount of data available because of the smaller size of facet 2 compared to facet 1 for the long
345 hipped template.



346 **Figure 12 Modelled and observed**
347 **orientation for neighbourhood 364. Line denotes a 1:1 relationship**

348 Figure 12 shows that for neighbourhood 364, there was an average absolute error of 0.82° (0.39%) in
349 orientation modelling which may result from slight inaccuracies in the positioning of the input
350 building footprint data or slight changes that result from the segmentation process.

351 **3.3 Shape Accuracy**

352 Across all seven tested neighbourhoods, the methodology found the correct shape for 87% of roofs,
353 as shown in Table 2.

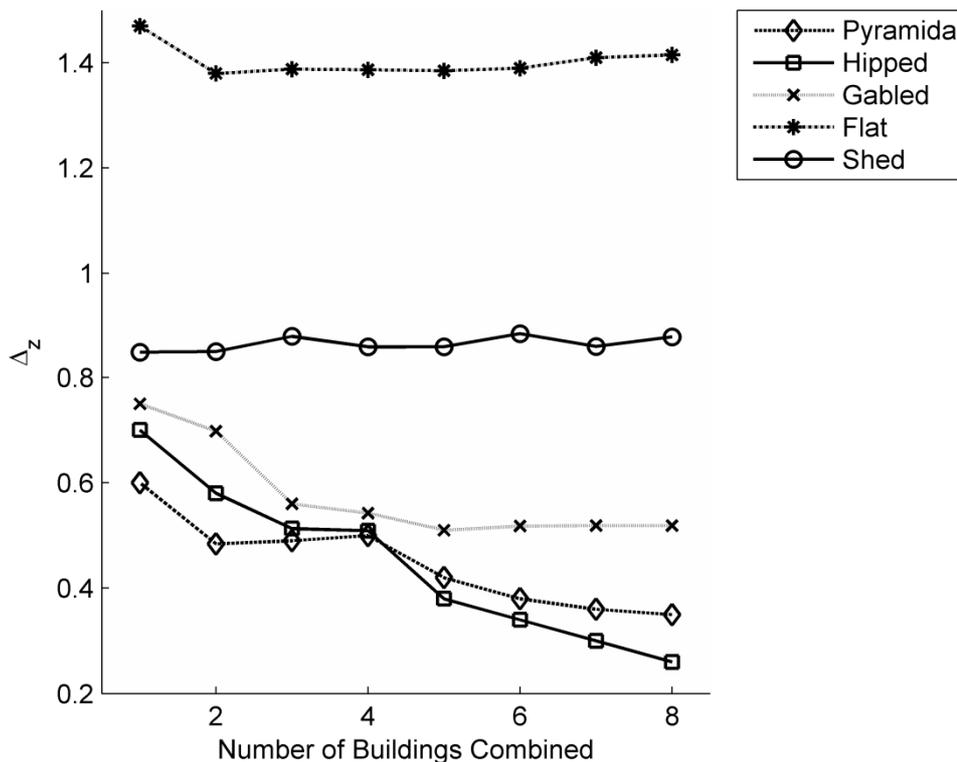
Neighbourhood	Total Buildings	Success (No.)	Success (%)
406	83	76	92
759	64	47	73
209	128	110	86
690	84	82	98
867	49	40	80
364	40	38	95
447	88	75	85
Total	536	468	
Average			87

Table 2 Shape matching success in seven tested neighbourhoods

354

355 This compares favourably with the one other existing methodology to use low-resolution DSM data
 356 by Jacques et al. [21] who achieved a shape matching success rate of 81% based on a study of 242
 357 buildings using a more limited roof template library.

358 Δ_z was found to decrease when the correct template was compared to data from an increasing
 359 number of buildings. Figure 13 provides Δ_z values for five templates as data from an increasing
 360 number of hipped roof buildings of a similarity group with eight buildings were combined and
 361 compared.



362

363 Figure 13 Changes in Δ_z when data from an increasing number of buildings is combined. The correct template is hipped.

364 The initial trend for pyramidal, hipped and gabled templates is for Δ_z to decrease as data from more
 365 buildings are considered in the comparison which signifies an improving fit. It is interesting to note
 366 that the correct template (hipped) only scored the lowest Δ_z (and therefore best fit) after the DSM
 367 data of more than four buildings were combined. With fewer than five buildings' data, a pyramidal

368 roof shape would have been incorrectly modelled, demonstrating the key advantage of using
 369 multiple similar buildings.

370 **3.4 Slope Accuracy**

371 The facet 1 slopes of the modelled buildings were compared to the angles observed when 169
 372 building roofs were surveyed. The mean absolute error (MAE) of each similarity group between the
 373 modelled and surveyed roofs has been calculated using the equation:

$$374 \quad MAE = \frac{1}{n} \sum_{i=1}^n |f_i - y_i| \quad (2)$$

375 where n represents the number of slope estimations in each neighbourhood, f_i the modelled slope
 376 and y_i the observed slope. Table 3 shows that the MAE when averaged across all of the similarity
 377 groups in all of the neighbourhoods was 3.76°.

Neighbourhood	Surveyed Angle (°)	Total Buildings	MAE (°)
406	42.0	19	11.07
209	29.5	49	9.50
690	27.6	68	2.29
867	27.5	5	2.22
364	28.9	18	2.66
364	27.5	5	3.94
364	29.62	8	1.69
364	30.10	2	3.83
447	27.04	5	0.09
447	21.65	3	0.26
Total		182	
Average			3.76

378 **Table 3 MAE in slope prediction of 169 buildings from a range of test neighbourhoods**

379 The worst performing group of buildings (neighbourhood 406) had steep roofs of 42°. This could
 380 result in an increased probability of outlier identification failure due to the greater difference in
 381 height from one data point to the next on a steeper roof. For this reason the outlier identification
 382 process may have incorrectly removed data relating to the ridge of the steep roofs leading to a
 383 shallower modelled angle than that surveyed.

384 **3.4.1 Comparison to Footprint-Defined Regression**

385 The simplest method to estimate roof slope would be to fit a regression line to the data points
 386 provided by each facet of a single building using, for example, the MATLAB® [31] robustfit tool. The
 387 expected geometry of the roof would be defined purely from the building footprint such that, for
 388 example, the ridge of a gable roof would occur exactly halfway along the width of the building. In
 389 this section we compare the slopes predicted for similar individual gabled facets under this more
 390 basic method ($\hat{\beta}_{g-RB}$, where g refers to gable facets and RB signifies the use of robustfit) and the
 391 angle modelled when the multiple buildings methodology described in the present paper was
 392 applied ($\hat{\beta}_{g-MB}$, where MB denotes the use of multiple buildings). A further comparison is made by
 393 applying $\hat{\beta}_{g-RB}$ to the combined data of the buildings to assess the importance of the features in
 394 $\hat{\beta}_{g-MB}$ other than the combination of DSM data from similar buildings, such as the ridge

395 repositioning process. The buildings below were from a randomly selected similarity group of gable-
 396 roofed buildings and had a slope (β_g) of 37° when surveyed, 3.06° greater than $\hat{\beta}_{g-MB}$.

Building ID	$\hat{\beta}_{g-RB}$ ($^\circ$)	$ \hat{\beta}_{g-RB} - \beta_g $ ($^\circ$)
2	25.51	11.49
34	8.44	28.56
41	29.07	7.93
44	33.44	3.56
48	35.40	1.60
49	31.03	5.97
Average	27.15	9.85
$\hat{\beta}_{g-RB}$ Combined	28.50	8.50

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	$\hat{\beta}_{g-MB}$ ($^\circ$)	$ \hat{\beta}_{g-MB} - \beta_g $ ($^\circ$)
$\hat{\beta}_{g-MB}$ Combined	33.94	3.06

398 **Table 4 Comparison of modelling gabled roof slopes using building footprint defined MATLAB® robustfit regression on**
 399 **individual and combined data (top) against $\hat{\beta}_{g-MB}$ (bottom)**

400 From table 4, the average $|\hat{\beta}_{g-RB} - \beta_g|$ value for individual buildings was 9.85° which is greater
 401 than the value for using combined data (8.5°) and substantially larger than the 3.06° value
 402 for $|\hat{\beta}_{g-MB} - \beta_g|$. This shows that the application of the robustfit MATLAB® tool in evaluating
 403 geometry derived from building footprints is a less accurate than the methodology presented here,
 404 even when the buildings are combined. Whilst a possible cause of the disparity between the two
 405 methods is the approach to identifying outliers, the main reason for the improved performance of
 406 $\hat{\beta}_{g-MB}$ is the correction to the misalignment of the two datasets. $\hat{\beta}_{g-MB}$ compensates for this
 407 misalignment by repositioning individual building DSM data prior to combination, enabling a fairer
 408 calculation of template suitability.

409 3.4.2 Benefits of Considering Multiple Buildings When Modelling Slope

410 Table 5 shows the modelled angles for the gabled ($\hat{\beta}_{g-IND}$) and hipped ($\hat{\beta}_{h-IND}$) facets from a
 411 randomly selected group of similar buildings with long hipped roof shapes when processed through
 412 the methodology individually (IND denotes the use of individual buildings). This means the
 413 segmented buildings' DSM data were each passed through the ridge centring, height normalisation
 414 and outlier removal processes, but not the rotation and combination procedures. When surveyed,
 415 the buildings were found to have gable (β_g) and hip (β_h) section facets of 27.5° . The final row shows
 416 the angles modelled when the data for the five similar buildings was combined and the complete
 417 methodology presented here ($\hat{\beta}_{g-MB}$) was applied.

Building ID	$\hat{\beta}_g$ (°)	$ \hat{\beta}_{g-IND} - \beta_g $ (°)	$\hat{\beta}_h$ (°)	$ \hat{\beta}_{h-IND} - \beta_h $ (°)
6	22.63	4.87	*	*
13	29.5	2.00	21.99	5.51
18	32.24	4.74	42.07	14.57
19	34.85	7.35	41.27	13.77
28	15.46	12.04	*	*
Average	N/A	6.20	N/A	11.28

418

	$\hat{\beta}_g$ (°)	$ \hat{\beta}_{g-MB} - \beta_g $ (°)	$\hat{\beta}_h$ (°)	$ \hat{\beta}_{h-MB} - \beta_h $ (°)
$\hat{\beta}_{g-MB}$	29.72	2.22	33.53	6.03

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Table 5 Comparison of slope modelling when buildings were considered individually and when combined. * denotes instances where building shape was incorrectly modelled and did not return an angle for the hipped section of the long-hipped roof template

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The average $|\hat{\beta}_g - \beta_g|$ error in slope estimation is 6.2° which is significantly greater than the 2.22° achieved using $\hat{\beta}_{g-MB}$. Buildings 6 and 28 of Table 5 are instances in which roof shape was incorrectly modelled as gabled when treated as individual buildings, meaning that no $\hat{\beta}_{h-IND}$ value was returned, re-illustrating the benefit of using multiple buildings to model shape. Due to their size, the hip sections contain less data than gabled so it is unsurprising that the error in slope estimation is greatest for these parts.

428

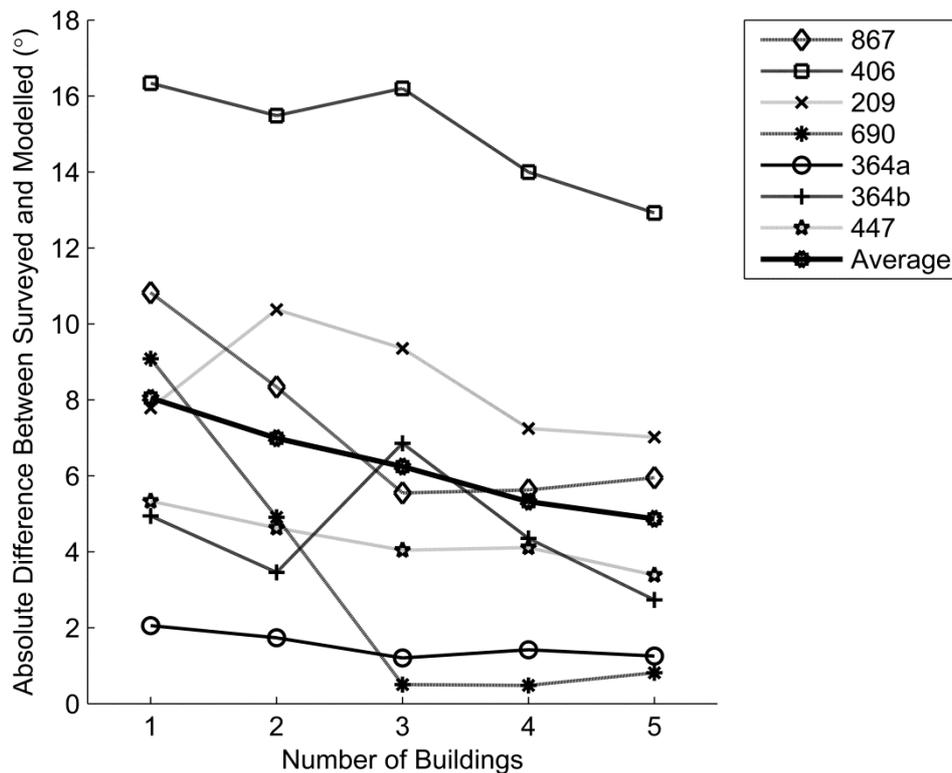
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As with roof shape modelling, considering an increasing number of buildings' data for the appraisal of roof slope led to more accurate results. In the following example, the roof slope angle predicted by the model was compared to the angles surveyed on 35 buildings from a range of neighbourhoods with a variety of roof shapes. The key result illustrated by Figure 14 is the general pattern of decreasing errors in modelled slope as data from an increasing number of buildings are combined.



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Figure 14 Slope accuracy improvement when using combined DSM data from increasing numbers of buildings. Legend items refer to neighbourhood IDs.

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The largest error shown in Figure 14 relates to data from neighbourhood 406 which was characterized by steeper angled roofs. Although requiring further investigation on a larger sample of steep roofs, the results suggest that the method is less accurate on roofs with a slope greater than 40°. Data from such properties have a greater difference in height between neighbouring points and the effect of alterations to the outlier identification criterion should be investigated in future work.

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3.5 Suitability to City-Scale Application and Implications for Installation Performance Projections

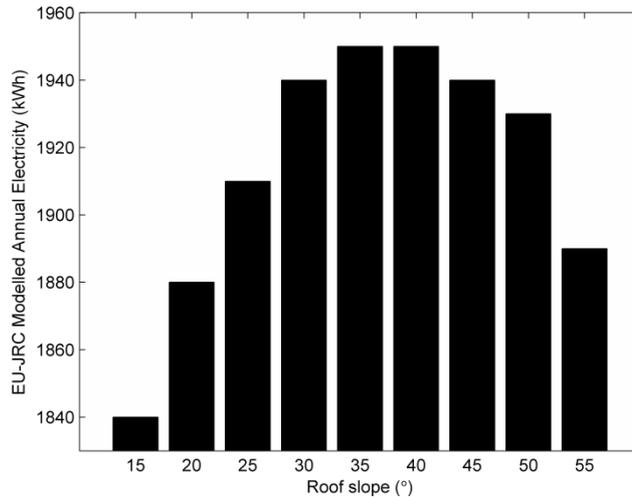
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Using only moderate computing resources, an Intel® Xeon® 3.1GHz processor and 4GB of RAM, the method executed in under three and a half minutes on each neighbourhood including one particularly dense area containing 128 buildings. This suggests it would be suitable for the estimation of potential PV capacity on a city scale. It would however be important to take account of errors in modelled shape and slope in such estimations and this section discusses the potential impact of such errors on the projection of PV installation performance. It is acknowledged that there will be many other factors that influence the performance of solar technologies including shading from surrounding objects and terrain that are beyond the scope of this article which is focused on increasing the accuracy with which area, orientation and slope of roof-spaces are determined from low resolution data.

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3.5.1 Slope Errors and Performance Projections

On average over the test areas, the methodology modelled buildings to within 5° of the surveyed slope. Figure 15 shows annual electricity predicted by the EU-JRC PVGIS webtool [34] for a 2.2 kWp system with optimized azimuth for increasing slope, demonstrating a non-linear relationship between the two.



458
459 **Figure 15 EU JRC PVGIS estimated annual PV power output for a 2.2kWp installation with optimized azimuth under a**
460 **range of slope conditions**

461 Table 6 shows the range of power output predictions at a range of slope angles for a slope error of
462 $\pm 5^\circ$ and $\pm 10^\circ$.

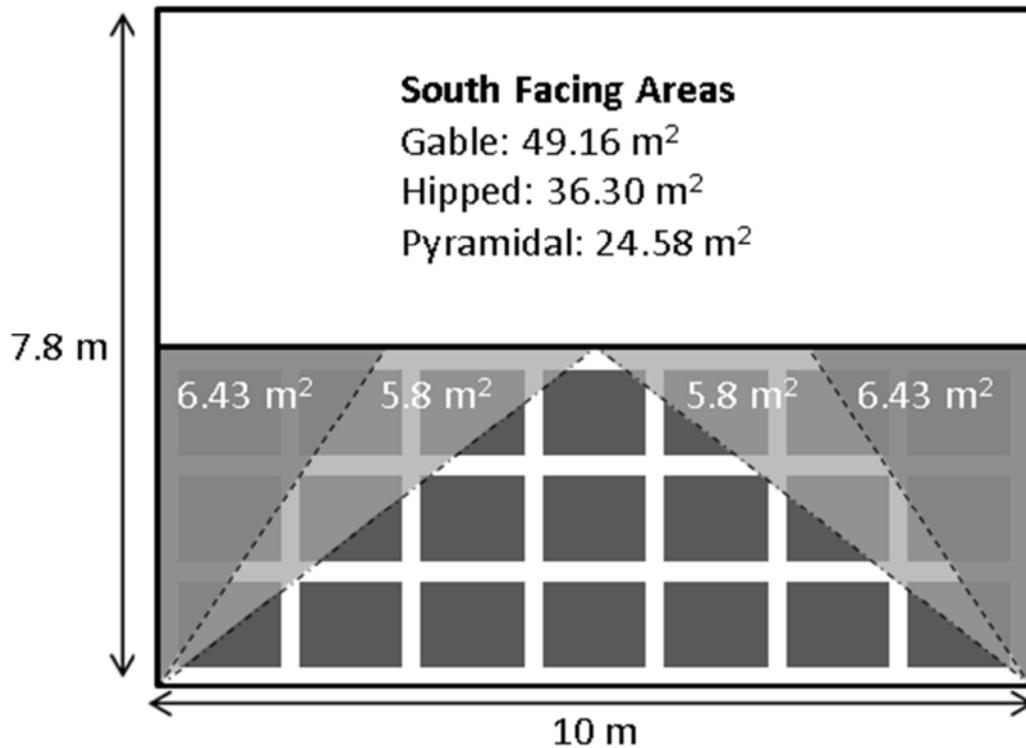
Roof Slope (°)	% change in predicted annual power output for slope error of $\pm 5^\circ$ (%)	% change in predicted annual power output for slope error of $\pm 10^\circ$ (%)
25	3.14	4.71
30	2.06	3.61
35	0.51	2.05
40	0.51	1.03
45	1.03	3.09

463 **Table 6 Difference in EU JRC annual PV power output estimations with changing slope**

464 This shows how sensitive annual power predictions are to errors in slope and in particular, how the
465 sensitivity is greater for the extremes of slope compared to slopes close to the optimum value
466 (approximately 39° for Leeds, UK). As discussed above, the MAE for the tested neighbourhoods using
467 the current method is less than 5° and hence is sufficiently accurate to provide predictions of annual
468 power output even for shallow roof slopes.

469 **3.5.2 Shape Errors and Performance Projections**

470 Available roof area is a function of modelled roof shape and orientation as PV panels are deployed
471 on the most southerly facing roof facets of buildings. This emphasizes the importance of modelling
472 the correct shape of roofs to estimate the performance of PV installations. Figure 16 takes a
473 hypothetical building with a plan area typical of suburban properties (78 m^2) and roof slope of 37.5°
474 and investigates the impact on available area if it were modelled as gabled, hipped or pyramidal.
475 The figure is a scaled drawing in which the solar panels are 1 m by 1.6 m and rated at 0.25 kWp to
476 reflect a common PV panel on the market. The darker grey regions on the periphery of the south
477 facing slope represent the area that would be lost if the building were modelled as hipped instead of
478 gabled. The lighter grey regions are the additional south facing area that would be lost if the building
479 was modelled as pyramidal instead of hipped. The inset text states the south facing roof area under
480 each of the templates.



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Figure 16 Effect of modelled roof shape on area available for solar technologies

483 From the available area calculations of Figure 16, the impact of roof shape on annual power output
 484 predictions could be investigated. The predicted power outputs shown in Table 7 were again taken
 485 from the EU JRC PVGIS tool [34] for a south-facing, 37.5° sloped crystalline silicon panel type without
 486 any shading objects in the vicinity.

Modelled shape	Available area (m ²)	System size (kWp)	Predicted Output (kWh a ⁻¹)
Gable	49.16	5.25	4,560
Hipped	36.30	3.25	2,820
Pyramidal	24.58	2.25	1,950

487

Table 7 Effect of roof shape modelling on annual power output predictions

488 Table 7 shows the importance of finding the correct roof shape as it defines the south-facing area
 489 available for a PV installation and therefore system size. Power output is clearly far more sensitive to
 490 system size than to slope. In the example provided, the reduction in predicted annual power output
 491 from a gabled to a hipped property is 37.35%. The reduction if a hipped property were to be
 492 modelled as pyramidal is 50.23%, whilst if a property was gabled but incorrectly modelled as
 493 pyramidal, there would be a 68.82% loss in predicted output. Hence, achieving 87% success in shape
 494 recognition and 3.76° error in slope estimation has been shown to be especially important when
 495 seeking to model the potential for PV at every property in a city or for estimating a maximum yield
 496 from PV technologies across an entire region.

497 **4 Conclusions**

498 A methodology is presented to model roof shapes using building footprint and low-resolution DSM
499 data. With moderate computing resources the method executes rapidly and so demonstrates high
500 suitability for application across a whole city region.

501 In 87% of cases tested, the method identified the correct shape of the main roof part of buildings.
502 This was validated using a total of 536 small buildings from different areas of the city of Leeds, UK.
503 The MAE in roof slope was found to be $\pm 3.76^\circ$ when validated against 182 buildings. Both roof shape
504 and slope were more accurately appraised as greater numbers of similar buildings were
505 incorporated into the combined data set.

506 Roof slope was defined with greater accuracy than by the application of regression techniques to
507 areas of roofs defined by building footprint data alone. In the example provided, the error of roof
508 slope calculation from the current method was 3.06° whereas using regression on areas of the DSM
509 identified by building footprints led to an average error of 9.85° .

510 The importance of increased accuracy in modelling roof slope and shape has been discussed in terms
511 of predicted annual PV installation power output with the caveat that there are additional local
512 factors, such as shading, that may affect the performance of solar installations beyond the factors
513 modelled in this methodology. The discussion shows that outputs from the method could be used to
514 calculate payback periods for PV installations on typical residential properties with greater accuracy
515 than previous methodologies.

516 **5 Acknowledgements**

517 This work was financially supported by the Engineering and Physical Sciences Research Council
518 through the University of Leeds Doctoral Training Centre in Low Carbon Technologies. We would
519 also like to thank EDINA and Landmap for the provision of data.

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