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Active phase-nulling of the self-mixing phase in a terahertz frequency quantum cascade laser


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We demonstrate an active phase-nulling scheme for terahertz (THz) frequency quantum cascade lasers (QCLs) under optical feedback, by active electronic feedback control of the emission frequency. Using this scheme the frequency tuning rate of a THz QCL is characterised, with significantly reduced experimental complexity compared to alternative approaches. Furthermore, we demonstrate real-time displacement sensing of targets, overcoming the resolution limits imposed by quantisation in previously-implemented fringe counting methods. Our approach is readily applicable to high-frequency vibrometry and surface profiling of targets, as well as frequency-stabilisation schemes for THz QCLs.

Self-mixing (SM) interferometry [1] using quantum cascade lasers (QCLs) [2] has recently emerged as a powerful sensing technique in the terahertz (THz) frequency range. The SM scheme is based on the optical feedback (OF) of radiation coupled back into the laser cavity, where it mixes with the intracavity field causing measurable perturbations to the laser operating parameters [3]. Amongst the principal benefits of the SM scheme is the ability to probe the electric field reflected from remote targets coherently through the laser compliance voltage, thereby removing the need for an external detector and enabling the development of compact sensing systems. This is particularly beneficial at THz frequencies owing to a lack of mature technologies that provide fast, sensitive, and compact coherent detection capability. These benefits, in addition to the non-invasive nature of the SM scheme, have recently stimulated its application to displacement sensing [4], velocimetry [5], two- and three-dimensional imaging [6, 7, 8, 9], and materials analysis [10] at THz frequencies. In addition, SM has been applied to study the fundamental properties of THz QCLs, including measurement of the linewidth enhancement factor [4, 11] and investigation of the intrinsic stability of QCLs under optical reinjection [12]. In all SM studies to date, however, the QCL has been operated under free-running conditions without any electronic feedback control. In contrast, feedback control schemes for near-infrared lasers under OF have been demonstrated as powerful tools for applications including sub-wavelength displacement sensing of targets [13], and non-contact vibrometry of vehicles [14].

In this work we develop an active phase-nulling scheme for THz QCLs under OF, through electronic feedback control of the emission frequency. We first apply this method to measurement of the frequency tuning of a laser as a function of drive current. Such characterisation is essential for many applications, including gas spectroscopy, and frequency-modulated approaches to imaging and materials analysis using THz QCLs. In addition to offering real-time capability, our measurement approach provides a greatly reduced experimental complexity compared to previously reported schemes for characterising frequency tuning in QCLs – these typically require detection of the high-frequency beat note generated by mixing the QCL field with that derived from a local oscillator source (either a second QCL [15, 16] or an optically-pumped gas laser [17, 18]) on a diode mixer. In contrast to these approaches, which are restricted to the operating frequency range of the mixer, our technique can be applied across the full 1.2−5.2 THz spectral coverage range of THz QCLs. We also demonstrate that our phase-nulling scheme can be applied to real-time displacement sensing of targets. This scheme achieves all of the advantages of previous SM-based displacement sensors whilst overcoming the resolution limits imposed by the quantisation associated with fringe counting methods [19, 20] and simultaneously avoiding the need for parametric fitting to an OF model in post-processing [4].

A schematic diagram of our system is shown in Fig 1. The THz QCL consisted of a 10 µm-thick bound-to-continuum active region [21], which was processed into a semi-insulating surface-plasmon ridge waveguide with dimensions 3 mm × 140 µm. Measurements of the emission spectrum of the isolated laser, performed using a Fourier-transform infrared spectrometer with a spectral resolution of 7.5 GHz, revealed emission in a single longitudinal mode at a frequency, ν₀~2.62 THz (λ ~ 114 µm) for all driving currents, at a heat sink temperature of 25 K. Radiation from the laser was focused onto a gold planar mirror using a pair of axis parabolic reflectors and coupled back into the QCL facet along the same optical path as the emitted beam. The planar mirror was mounted on a computer-controlled translation stage to enable mechanical modulation of the external cavity length around its mean value L₀ = 0.41 m.
The mirror position was recorded in real-time at a sampling rate of 10 kS/s through the analogue output of the stage encoder. An externally modulated current source was used to drive the laser with an electronically conditioned dynamic feedback current $\Delta i$ superimposed on a quiescent current of $i_0 = 1080 \text{ mA} (=1.08 i_0)$. The SM signal ($V_{SM}$) was monitored using the QCL terminal voltage, which was amplified using a 15 dB dc-coupled voltage amplifier following subtraction of a dc voltage offset.

$$\Delta V = k \Delta i = kGV_{out}$$

where $k$ is the frequency tuning rate of the QCL. In addition to this frequency tuning effect, the applied current perturbation also causes a direct modulation of the QCL terminal voltage through the differential resistance of the device, $R$. For small perturbations around the operating point of the laser, $R$ can be approximated as being constant. This unwanted component of voltage modulation can therefore be subtracted from the input to the loop filter by use of an adjustable inverting amplifier stage acting on the filter output $V_{out}$, as shown by the dashed box in Fig. 1. This compensation loop was tuned to provide the necessary amplification, $A = RG \approx 0.7$, by applying a 30 mA ramp modulation to the driving current of the laser without OF, and adjusting the amplifier such that its output matched the resulting modulation of the QCL voltage.

Figure 2(b) shows the error signal $V_{error}$ obtained in response to a modulation of the external cavity length, without feedback control of the QCL. In this example the cavity length was increased at a rate of $-60 \mu\text{m/s}$ with a peak mirror displacement $\Delta L = 25 \mu\text{m}$ (corresponding to approximately half a fringe), as shown in Fig. 2(a). As expected, under open-loop operation the SM signal $V_{SM}$ (and hence $V_{error}$) varies according to the external round-trip phase $\phi$, as described above. By contrast Fig. 2(b) also shows $V_{error}$ obtained in the closed-loop condition, along with the corresponding control signal $V_{out}$ (Fig. 2(c)). In this case the SM voltage is maintained at a constant value as the feedback loop acts to compensate for the varying round-trip phase by dynamic control of the laser emission frequency. The resulting time-dependent frequency excursion of the laser can be deduced from the recorded mirror trajectory $\Delta L$ by use of Eq. 1. By correlating this with the measured control signal, the frequency tuning can be mapped as a function of current perturbation $\Delta i$, enabling the tuning rate $k$ to be determined using Eq. 2. The relationship between $\Delta i$ and $\Delta v$ obtained in this way is shown in Fig. 3. From a linear fit to this data a value $k = -8.2 \text{ MHz/mA}$ is found, consistent with the range of values reported for other THz QCLs [23].
Fig. 4(b). We attribute this displacement error primarily to the voltage-dependent differential resistance of the device causing incomplete subtraction of the laser voltage modulation by the compensation loop. This same effect also determines the practical current modulation amplitude to be ~30 mA in our system, which corresponds to a measurable displacement amplitude of ~40 μm. It is worth emphasizing, though, that with correct non-linear compensation of the QCL voltage modulation (using a digital synthesizer, for example), the useful current modulation range could be extended up to the mode-hop free tuning range of the laser under OF, which is ~100 mA in our case. Furthermore, the operating range of the electronic feedback loop in our system is expected to be ~A_{OL}λ/2 = 3.6 cm [13] for an open-loop gain A_{OL} = 4πf_bkG_{A_e}/c = 630, suggesting much greater displacement amplitudes could, in principle, be measured using our technique.

As a second demonstration of our scheme we have applied it to the reciprocal modality, namely the real-time displacement sensing of targets. In this case the filter output \( V_{\text{out}} \) generated in response to a moving target represents a replica of the target displacement, scaled by the responsivity factor \( R = -v_0/kG_L \) = 3.9 V/mm according to Eq. 1 and 2, and using the value \( k = -8.2 \text{ MHz/mA} \). Figure 4(a) shows the displacement measured over two oscillation cycles of a mirror vibrating at 2 Hz with a peak-to-peak displacement, \( D = 22.5 \text{ μm} \). This SM measurement yields a value of \( D = 23.1 \text{ μm} \), representing an error of only -2.5%. From Fourier analysis of the filter output signal, the noise equivalent displacement was found to be -0.2 μm for a 1 Hz measurement bandwidth centered around the oscillation frequency of 2 Hz. In addition, the maximum displacement error recorded over the full range of displacement was determined to be ~2.5 μm (see Fig. 4(b)). We attribute this displacement error primarily

Fig. 3. Frequency tuning \( \Delta v \) of the QCL arising from a current perturbation \( \Delta i \), as determined from the feedback control signal \( V_{\text{out}} \) measured in response to a modulation of the external cavity length. A linear fit to the data (red, dashed line) yields a tuning rate \( k = -8.2 \text{ MHz/mA} \). Inset: Relationship between driving current and \( \Delta v \) determined using a swept-frequency interferometric measurement (blue circles). A linear fit to this data (red, solid line) yields a tuning rate \( k = -8.5 \text{ MHz/mA} \).

In summary, we have demonstrated an active phase-nulling scheme for THz QCLs under OF, through electronic feedback control of the emission frequency. This scheme has been applied successfully to real-time measurement of the frequency tuning rate of a QCL, and offers significantly reduced experimental complexity compared to alternative measurement approaches. In addition, we have demonstrated an alternative modality in which the position of a moving target is replicated on the output voltage of our instrument in real-time and with a noise equivalent displacement of ~0.2 μm (~λ/570). In this regard it is worth noting that the speed of response to OF is fundamentally determined by elastic and inelastic scattering mechanisms that occur on picosecond time scales in THz QCLs, thereby enabling response bandwidths on the order of ~10–100 GHz, in principle. As such, this scheme could be extended readily to high-frequency vibrometry applications, with the maximum frequency response being determined, in practice, by the
Fig. 4. (a) Displacement (blue, solid line) determined from the feedback control signal $V_{out}$, in response to two oscillation cycles of a target vibrating at 2 Hz with a peak-to-peak displacement of 22.5 μm (actual displacement shown by the red, dashed line). (b) Displacement error determined from the difference between the measured and actual displacements.

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