Emerging Pattern Mining To Aid Toxicological Knowledge Discovery

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ABSTRACT: Knowledge-based systems for toxicity prediction are typically based on rules, known as structural alerts, that describe relationships between structural features and different toxic effects. The identification of structural features associated with toxicological activity can be a time-consuming process and often requires significant input from domain experts. Here, we describe an emerging pattern mining method for the automated identification of activating structural features in toxicity data sets that is designed to help expedite the process of alert development. We apply the contrast pattern tree mining algorithm to generate a set of emerging patterns of structural fragment descriptors. Using the emerging patterns it is possible to form hierarchical clusters of compounds that are defined by the presence of common structural features and represent distinct chemical classes. The method has been tested on a large public in vitro mutagenicity data set and a public hERG channel inhibition data set and is shown to be effective at identifying common toxic features and recognizable classes of toxicants. We also describe how knowledge developers can use emerging patterns to improve the specificity and sensitivity of an existing expert system.

INTRODUCTION

The development of accurate methods for the prediction of toxic hazard and environmental effects of chemical compounds is a topic of great importance to all chemical industries1,2 both from the economic stand point of reducing the need for expensive in vivo or in vitro experiments and from the ethical stand point of reducing testing in animals. However, predicting toxic effects is a significant challenge for a number of reasons: multiple different toxic effects exist; the same toxic effect can arise through multiple biological mechanisms; and for many toxic effects the mechanisms of action are poorly understood. Furthermore, it is difficult to obtain large high-quality data sets from which to form reliable computational models.

Expert systems are a class of computational tools that have shown success in predicting toxic hazard by applying established knowledge of toxicology. For example, the Derek Nexus,3 HazardExpert,4 and CASEUltra5 systems encode structural features that have been associated with particular toxicological effects, known as structural alerts, alongside other parameters such as physicochemical properties. These systems apply different rule-based or reasoning-based decision making algorithms to the stored knowledge in order to make predictions of toxicity. For instance, Derek Nexus uses a reasoning model to construct and weigh up arguments for and against toxicity. A disadvantage of expert systems is that developing new structural alerts to expand the knowledge bases requires considerable time and effort from domain experts and involves detailed analysis of relevant literature.

Our aim in this work is to develop a data mining method to assist knowledge base developers in identifying substructural features associated with toxic effects which can be used to expedite the process of forming new structural alerts. Several methods have been reported in the literature aimed at identifying structural features or motifs that are associated with biological activity. For example, Nicolaou et al.6 describe an automated approach to identifying structural motifs associated with active compounds in high throughput screening (HTS) data. Their approach is iterative, with each iteration involving a clustering step followed by the identification of a maximum common substructure within a cluster which is then used to define a new compound set for further clustering. Harper et al.7 also describe a data driven clustering method aimed at identifying motifs that are common to active compounds in HTS data. The motifs are based on reduced graphs which are generated for all compounds and are then ranked based on the activity values of the compounds that exhibit them. Frequent subgraph mining techniques have also been applied to identify subgraphs that are associated with biological activity and toxicity.8 These approaches are essentially based on enumerating all possible subgraphs within a data set and then identifying those which are more prevalent in one class of compounds compared to another. Graph mining methods are computationally expensive, and various algorithms have been developed to improve the efficiency of the process. For example,
Kazius et al. apply the Gaston subgraph mining algorithm to identifying features associated with mutagenicity.\textsuperscript{9} Lozano et al. describe a similar approach that involves enumerating connected subgraphs directly from the toxic compounds and searching for each independently in the toxic and nontoxic compounds, retaining those that occur only in the toxic compounds.\textsuperscript{10} Poezevara et al. have since extended this method to identify combinations of connected subgraphs that are associated with toxicity, which are then represented in a condensed form using closed graphs.\textsuperscript{11} More recently, Ferrari et al. have described a substructure mining approach that is based on fragmenting molecules via their SMILES representations with the fragments selected according to their predictive ability on a training set.\textsuperscript{12} Julian and Afshar have developed Knowledge Extraction and Management (KEM) software\textsuperscript{13} that is based on association rule mining, also known as formal concept analysis\textsuperscript{14} or Galois lattice theory.\textsuperscript{15} The compounds are first fragmented into substructures of various sizes, and each compound is encoded as binary properties indicating the presence or absence of the substructural fragments together with its activity, which is also encoded as a binary property. KEM can be used to find association rules that relate substructural fragments to activity by limiting the extracted rules to those containing the presence of activity as the consequent. They describe an application of KEM to a data set of reproductive toxicants and innocuous compounds.

In our previous work, we applied jumping emerging pattern (JEP) mining to data sets consisting of toxic and nontoxic compounds to identify structural features associated with toxicity.\textsuperscript{16} Emerging pattern (EP) mining is a data mining technique first developed within the engineering communities to identify combinations of descriptors that are able to distinguish between classes of objects based on binary descriptors.\textsuperscript{17} JEPs are sets of one or more combined descriptors that are present in one class and absent from the other; for instance, collections of molecular descriptors that are only found together in active compounds. In the first application of emerging pattern mining to chemical data sets, Auer and Bajorath\textsuperscript{18} used emerging pattern mining to develop predictive models of biological activity based on physicochemical and molecular properties. Continuous value descriptors were discretized into bits representing, for example, discrete ranges of molecular weight and log P values. JEP mining was then used to identify combinations of bits that are more prevalent in active compounds than in inactives and which represent sets of property ranges that are characteristic of the actives. More recently, Bajorath’s group has applied JEP mining to multigetarget classification,\textsuperscript{19} and Garcia-Borroto et al.\textsuperscript{20} have described a method for extracting emerging patterns from a decision tree which avoids the need to discretise continuous property descriptors and have demonstrated its application to classification modeling.

A limitation of JEPs is that they are inherently intolerant of noisy data. As a consequence, the presence of even a small number of misclassified compounds can lead to the generation of several detailed JEPs which are necessary to describe the active compounds while at the same time excluding the misclassified compounds. For example, aromatic nitro compounds are well-known to be associated with mutagenicity, and the presence of a single aromatic nitro compound in the set of nontoxic compounds causes the creation of many, overly detailed descriptions of active compounds in order to exclude the inactive one. Emerging patterns, on the other hand, are noise tolerant since they represent patterns that are more common to one class than the other; however, they can be less discriminating. Since the aim of our work is the extraction of characteristic features of toxic compounds for expert analysis, rather than direct prediction of toxicity, greater noise tolerance and improved interpretability of results are more important than the predictivity of individual patterns.

In this paper, we describe the contrast pattern tree (CP-tree) algorithm\textsuperscript{21} for mining EPs and apply it to mine structural features in toxicity data sets. The emerging pattern mining enables toxic compounds to be organized into hierarchies in which the patterns of features become more detailed as a hierarchy is descended. This allows knowledge-base developers to browse through a set of compounds in a highly organized way and to choose an appropriate level of detail. We evaluate the performance of the EP mining on a large Ames mutagenicity data set and compare the results with those found using JEP mining. Finally, we apply the EP mining to a hERG channel inhibition data set to demonstrate its applicability to more complex toxicity end points.

\section*{Methodology}

The concept of an emerging pattern is illustrated by a hypothetical data set in Table 1. The data set consists of data entries in two classes, $D_1$ and $D_2$, with each class consisting of five entries. Each data entry is represented by a set of up to four binary properties or items ($a, b, c, d$). If an item is present in a data entry, then its label is shown in the corresponding row, otherwise the label is absent. A set of properties of any length (cardinality) is called an itemset or pattern. Any pattern that is a proper subset (a subset of fewer items) or is equal to the itemset of one or more of the data entries and occurs more frequently in one of the two classes is said to be “emerging” in that class. In Table 1, the two items that are both italic and bold, $a$ and $c$, represent an itemset that occurs more frequently in the entries in the class $D_1$ relative to $D_2$ so that the pattern \{$a, c\}$ is emerging in $D_1$. Thus, an EP can be considered to be a characteristic of the entries in one class that distinguishes them from those in the other class, regardless of the discriminatory ability of any individual item in the pattern.

The data entries that contain a pattern are referred to as its support set, i.e., they support the pattern. For example, the pattern \{$a, c\}$ is found in the entries \{1, 2, 3, 6\} which form its support set. The proportion of data entries in one class that support a pattern is referred to as its support; the support for pattern, $pat$, in class $D$ is

\[
\text{Supp}_{D}(pat) = \frac{\text{count}_{D}(pat)}{|D|}
\]
where $\text{count}_D(pat)$ is the number of entries in class $D$ that contain the pattern, and $|D|$ is the total number of entries in $D$. An EP is a pattern which has higher support in one class compared to another. The EP $\{a, c\}$ in Table 1 has a support of 0.6 in $D_1$, since it is present in three of the five data entries in that class, whereas it has support of only 0.2 in $D_2$, since it occurs in only one of five data entries.

The ratio of support in two classes indicates how emerging a pattern is. This ratio is often referred to as growth rate; the growth rate, $G$, of pattern, $pat$, in class $D_1$ compared to $D_2$ is

$$G(pat) = \frac{\text{Supp}_{D_1}(pat)}{\text{Supp}_{D_2}(pat)}$$

The growth rate of an EP must be between 1 and infinity, with an infinite growth rate indicating a JEP, i.e., the support in one class is zero. The growth rate of EP $\{a, c\}$ in Table 1 is 3 (support value of 0.6 in $D_1$ and 0.2 in $D_2$).

The simplest method of identifying the EPs in one class compared to another is to enumerate all possible itemsets in the class of interest and then obtain their support sets by searching for instances of each itemset in the data entries of each class. However, the number of combinations of properties can be prohibitive, even for low dimensional data sets. The contrast pattern tree (CP-tree) mining algorithm, developed by Fan et al. allows EPs to be identified within a reasonable time.

**Contrast Pattern Tree Mining.** A contrast pattern tree (CP-tree) is an ordered multiway tree representation of the itemsets in a data set. The CP-tree for the hypothetical data set in Table 1 is shown in Figure 1. Each node in the tree contains one or more items which are ordered on descending support rate (and then lexicographically for equal support rates). Each item within a node can be connected by a branch to a node below it in the tree, i.e., as a child node of the item. Itemsets can be extracted from a CP-tree by tracing paths depth-first starting at the root node and considering one item at a time in order. Where a node contains multiple items, paths are traced through the left-most item considering one item at a time in order. Where a node contains a single item, paths are traced through that item. Itemsets can be extracted from a CP-tree by tracing paths depth-first starting at the root node and considering one item at a time in order. Where a node contains multiple items, paths are traced through the left-most item considering one item at a time in order. Where a node contains a single item, paths are traced through that item.

From the CP-tree, the highest support item, $a$, is taken as the root node and itemset $\{a\}$ is registered in the left-most path. Thus, data entry 1 which has the correct support rate (3, 0) has the correct support rate (3, 0); $\{b, c, a\}$ has the correct support rate (2, 0); and $\{b, a, c, d\}$ has the correct support rate (1, 0) even though there are two occurrences of $\{b, a, d\}$ within the data entries. This arises because each data entry is registered in only one path in the tree, and this is the left most path. Thus, data entry 1 with itemset $\{b, a, c, d\}$ is registered in the left most path only and not in any paths that occur to the right in the CP-tree where some of the items are missing, for example, paths $\{b, a, d\}$, $\{b, c, d\}$, and $\{b, d\}$. The first step in creating a CP-tree is to sort the items within each data entry on decreasing support rate. The data entries themselves are then sorted on their itemsets. For example, the items in the hypothetical data set are ordered in the sequence $b < a < c < d \not< null$, where $b < a$ indicates that $b$ is before $a$; the data entries are then ordered $1 < 2 < 4 < 5 < 8 < 6 < 3 < 10 < 7 < 9$, as shown in Table 2. The data entries are then processed in turn.

**Table 2. Items in Each Data Entries Shown in Table 1 Are Ordered on Support Rate and the Data Entries Are Ordered by Itemset**

<table>
<thead>
<tr>
<th>data entry</th>
<th>properties</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>b a c d</td>
</tr>
<tr>
<td>2</td>
<td>b a c</td>
</tr>
<tr>
<td>4</td>
<td>b a d</td>
</tr>
<tr>
<td>5</td>
<td>b c d</td>
</tr>
<tr>
<td>8</td>
<td>b d</td>
</tr>
<tr>
<td>6</td>
<td>a c d</td>
</tr>
<tr>
<td>3</td>
<td>a c</td>
</tr>
<tr>
<td>10</td>
<td>a</td>
</tr>
<tr>
<td>7</td>
<td>c d</td>
</tr>
<tr>
<td>9</td>
<td>c</td>
</tr>
</tbody>
</table>

Figure 2 illustrates the process of generating the initial CP-tree from a single pass over the hypothetical data set in Table 2. Entry 1, as the highest priority data entry, is taken first, and the item with highest support is inserted into the root node of the tree with counts set as (1, 0), since the data entry is a member of $D_1$. The rest of the items form new nodes at progressively lower levels of the tree. After processing data entry 1 the tree is as shown at Step 1 of Figure 2 with each item having the values (1, 0). The next data entry is then processed. If its highest supported item already exists in the root node, then the appropriate counts are incremented; otherwise a new item is added to the root node. The itemset $\{b, a, c\}$ of the second data entry already exists, and the appropriate counts are incremented. Having inserted all data entries containing the most supported item $\{b\}$ (Steps 1–4) data entry 6 is inserted. The highest supported item for data entry 6 is $\{a\}$ which does not exist in the root node, and so a new item is inserted with counts set as (0, 1). A new node is created below the root and item set inserted with counts also set as (0, 1). This process continues until all data entries have been inserted into the CP-tree, resulting in the CP-tree shown at Step 6 of Figure 2.

At this stage, the leftmost path through the tree in Step 6 has correct support counts. However, counts for itemsets which are subsets of larger itemsets that are present in the data are not correctly registered, and some itemsets are missing from the tree. Thus, itemset $\{b, a\}$ has the correct support rate (3, 0); $\{b, a, c\}$ has the correct support rate (2, 0); and $\{b, a, c, d\}$ has the correct support rate (1, 0) even though there are two occurrences of $\{b, a, d\}$ within the data entries. This arises because each data entry is registered in only one path in the tree, and this is the left most path. Thus, data entry 1 with itemset $\{b, a, c, d\}$ is registered in the left most path only and not in any paths that occur to the right in the CP-tree where some of the items are missing, for example, paths $\{b, a, d\}$, $\{b, c, d\}$, and $\{b, d\}$. Generation of the complete CP-tree together with correct support counts requires additional processing which involves
recursively merging subtrees in a depth-first, left-to-right trace through the initial tree. The depth-first trace begins with leftmost item \( b \) in the root node. The child node of \( b \) is shown shaded in Figure 3 and is merged into the root node. If the child node contains items that are already present in the root (\( a \) and \( c \), in this example), then the counts associated with the corresponding items are summed, and any children of these nodes are merged with children of the item in the parent, and so on. If the child contains an item that is not already present in the parent (\( d \)), a new item is created and counts set according to the child. This process effectively adjusts the counts for itemsets that are subsets of \( \{b, a, c, d\} \) but that do not contain \( b \). The depth-first trace then shifts to node \( \{a, c, d\} \) and merges its subtrees into the node. This process continues until the leaf nodes are reached at which point the trace back-tracks and processes the next item in the parent node, and so on. When all the items in the root node have been processed, this will result in the complete CP-tree being generated, as shown in Figure 3.

Storing a complete CP-tree in memory in order to mine EPs is impractical for large high dimensional data sets. However, the construction of the complete CP-tree can be avoided by combining the procedure for merging subtrees with the procedure for extracting EPs. The CP-tree is created and traversed, and the branches already visited are pruned in one continuous process. The algorithm follows a depth-first trace and uses heuristics to terminate a branch if various continuation criteria are not met. The heuristics are used to prevent the generation of EPs that are unlikely to be of interest, for example, they are of too low support to be considered useful. As each item is processed, if it has a child node, the subtree is merged prior to adding the item into the current EP and processing then passes to the child node. Processing continues if all of the conditions given
below are met, otherwise the item together with its child nodes are pruned from the tree and the algorithm backtracks.

1. Descending to the next node does not exceed a threshold on path length (that is, number of items in the EP).

2. There has been a change in support for the pattern in either \( D_1 \) or \( D_2 \), or the number of steps for which there has been no increase in growth rate is below a user-defined threshold.

3. Support in \( D_1 \) is greater than support in \( D_2 \).

4. Support in \( D_1 \) is above a user-defined minimum support \( \delta_1 \).

5. The following statement is true

\[
G(\text{pat}) \geq \frac{\delta_1}{\delta_2} \times \left( \frac{\text{Supp}_{D_1}(\text{pat})}{\text{Supp}_{D_2}(\text{pat})} \right)^{\alpha-1}
\]

Figure 3. Merging of subtrees to create a complete CP-tree.
where $\delta_2$ is a user-defined support threshold in $D_2$, that must satisfy $0 \leq \delta_2 \leq \delta_1$, and $\rho$ is a noise tolerance parameter greater than 1.

Alternatively, the algorithm may be configured to identify the shortest valid EP in a path. The algorithm will stop traversing down a branch as soon as condition 5 is met, and the resulting pattern will be returned as an EP. The branch will then be pruned, and the algorithm will continue to the next branch.

The growth function, $G(\text{pat})$, results in a curved frontier (solid black line) as shown in Figure 4 which plots support in $D_1$ against support in $D_2$ and defines the growth rate threshold at different support values. An EP with high support in $D_1$ must have a higher growth rate than one with lower support. The shaded area indicates the space in which EPs may be found. The red and blue lines represent the parameters $\delta_1$ and $\delta_2$, respectively, which define the starting point and initial gradient (dashed line) of the curve. In this case, $\delta_1$ is 0.1, $\delta_2$ is 0.075, and $\rho$ is 1.5. The green diagonal line shows where support for an itemset is equal in both classes.

Altering $\delta_1$ and $\delta_2$ allows the initial gradient of the curved frontier to be increased or decreased to include or exclude weaker EPs, respectively. These parameters determine how strongly discriminating an EP must be for it to be identified by the algorithm; a shallow gradient will shift the frontier toward support in $D_1$ and significantly reduce the space in which EPs can be found. The noise tolerance parameter $\rho$ can be used to alter the growth rate as support in $D_1$ increases so that the growth rates of EPs with larger support in $D_1$ are greater than the growth rates of EPs with smaller support in $D_1$. Thus, highly supported but weakly discriminating EPs are excluded. Such patterns may represent inconsequential features that are common within the data but are arbitrarily found in more entries in $D_1$ than in $D_2$. If $\rho$ is equal to 1.0, then the frontier defined by $G(\text{pat})$ is linear and follows the dashed line. If $\rho$ is increased, then the curve becomes more pronounced, and the deviation from the dashed line becomes greater. Increasing $\rho$ can dramatically limit the space in which EPs are found, such that only JEPs can be identified. This may significantly increase the number of resulting patterns and computation time while increasing pattern length and reducing their support.

**Support Set Hierarchies.** Once the EPs have been mined from the CP-tree, they can be organized into hierarchies, in a similar way to the JEPs described in our previous work. Many of the support sets for EPs exhibit subset-superset relationships, which permit the sorting of EPs, and their support sets, into hierarchical families with the most supported EP forming the root node of a tree. The remaining EPs are arranged below the root node in order of decreasing support. As a tree is descended, the EPs become more specific and less supported. Figure 5 illustrates a hierarchy based on data entries in the hypothetical data set that contain items \{a, c\} where the tree is composed of four EPs arranged as a tree of five nodes. Within the tree, each node represents an EP, in braces, and its support set in square brackets.

The resulting hierarchies represent a form of supervised clustering, i.e., the clustering is based on features that are characteristic of one class. Where EPs are associated with a toxic end point, the hierarchies of clusters are considered to be potential classes of toxicants that share a common mode of action, and individual clusters may represent potential subclasses. The clusters found using EPs overlap since a supporting data entry can be present in more than one node of a hierarchical tree and in more than one hierarchy. This is distinct from conventional hierarchical clustering methods, which do not typically result in overlapping clusters or multiple hierarchies.

![Figure 4. Support space of EPs.](image)

![Figure 5. An example support hierarchy for four EPs and their support sets extracted from the hypothetical example in Table 1.](image)

### EXPERIMENTAL SECTION

**Data Sets.** The EP mining method has been applied to an internally curated version of the Hansen et al. Ames mutagenicity data set and to a hERG channel inhibition data set available through PubChem.

The Hansen data set is a publicly available benchmark in vitro mutagenicity data set which is a compilation of data from a number of sources. The data set was curated to ensure the validity of molecular structures using a combination of ChemAxon software and KNIME nodes. Where possible, structures were matched by their CAS registry number to structures present in Lhasa Limited’s Vitic database, where the structures have previously undergone thorough validation and curation. Where matches in Vitic were found and there were differences in the structures, the structures in the benchmark data set were replaced with those from Vitic. Where a match could not be found, the structures were compared against their source data set, as referenced by Hansen et al., where a common identifier was available and the data was provided in a readily accessible format. Where structures differed, those in the benchmark data set were replaced by those from the source material.

Structures with valency violations and charge violations were repaired, for example aromatic nitro compounds frequently contained pentavalent nitrogen atoms, which were standardized as positively charged tetravalent nitrogen. Molecules containing R or X pseudo atoms were removed, as they could not be resolved to complete structures. Multicomponent structures containing significantly smaller components, such as H-X or sodium ions, were processed to retain only the largest component. Where multiple large components were found, the entire entry was removed from the data set, as it was not clear which component is most significant or if the activity is a result of both components combined. Finally, ChemAxon’s Standardizer software, and a number of small purpose-built software tools were used to generate standardized representations of structures.

Following this curation and validation, our version of the benchmark data set contained 6338 compounds: 2311 from the original benchmark data set, 1107 structures from the data set published by Kazius et al.,9 172 from the NISS data set, and 2748 from the Viti database. 3432 of the compounds are classed as mutagenic and represent the active class (D_a), and 2906 are classed as nonmutagenic and represent the inactive class (D_i). In 

### RESULTS

#### In Vitro Mutagenicity

EPs and support hierarchies were mined from the mutagenicity data set using a minimum threshold on support in actives of 0.01, i.e., 1% the active class or at least 35 molecules. The parameter for support in inactives was also 0.01, resulting in an initial gradient of the curved growth frontier of 1.0. The curve of the frontier was defined by a noise tolerance parameter (ρ) of 1.3, which provided sufficient noise tolerance without overly reducing the support space available for EP mining. To reduce run time and limit the potential generation of redundant EPs, the CP-tree mining algorithm applied the EP mining heuristics, described previously, such that only the first EP in any branch of the CP-tree was retained.

The results of EP mining are compared to those found by JEP mining in Table 3. The JEPs were mined using the method described in our previous work for the same data set and fragment descriptors, and a minimum value for support in actives of 0.01. The first two columns give the number of unique patterns and hierarchies generated by each method. The columns headed “coverage of actives” show the number and percentage of active compounds included in the support for at least one of each type of pattern. The columns headed “coverage of inactives” give the number and percentage of inactive compounds included in the support.

<table>
<thead>
<tr>
<th>patterns</th>
<th>hierarchies</th>
<th>coverage of actives</th>
<th>coverage of inactives</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>count</td>
<td>%</td>
</tr>
<tr>
<td></td>
<td></td>
<td>count</td>
<td>%</td>
</tr>
<tr>
<td>EP</td>
<td>116</td>
<td>53</td>
<td>2959</td>
</tr>
<tr>
<td>JEP</td>
<td>1191</td>
<td>478</td>
<td>1329</td>
</tr>
</tbody>
</table>

"The columns headed “coverage of actives” give the number and percentage of active compounds included in the support for at least one of each type of pattern. The columns headed “coverage of inactives” give the number and percentage of inactive compounds included in the support."
the highest growth rate is only supported by 83 active compounds (support value of \(~0.02\)) and no supporting inactives and is therefore a JEP with an infinite growth rate. The EP with the second highest growth rate is supported by 43 actives (support value of \(~0.01\)) and only one inactive (support value of \(~0.0003\)), resulting in a very high growth rate of approximately 36.4. Conversely, the most supported EP is supported by 784 actives (support value of \(~0.23\)) and 143 inactives (support value of \(~0.05\)) and has a relatively low growth rate of approximately 4.5. For knowledge discovery, the EPs can be sorted on the growth rate so that a knowledge base developer examines those with the highest growth rate first. If the coverage of inactives is considered too high, it could be reduced by altering the support and noise tolerance parameters and regenerating the EPs. Both the EP and JEP mining methods required a run time of approximately 1 min.

To put the coverage of these methods into context, Table 4 shows the number of structural alerts for in vitro mutagenicity from Lhasa Limited’s Derek Nexus that was found in the active class. The columns headed “coverage of actives” show the number of active molecules that exhibit at least one of the Derek Nexus alerts where it can be seen that Derek Nexus covered approximately 77% of the active compounds. The columns headed “coverage of inactives” show the number of inactive molecules that exhibit at least one of the Derek Nexus alerts; Derek Nexus covered approximately 23% of the inactive compounds. Table 5 shows the exclusive and shared coverage of the EP method and Derek Nexus. The columns headed “exclusive coverage” show the number of active and inactive molecules found exclusively in the support for at least one EP or exhibit at least one of the Derek Nexus alerts. The columns headed “shared coverage” show the number of active and inactive molecules found in both the support for at least one EP and exhibit at least one Derek Nexus alert.

Table 4. Number of Alerts Found in the Actives in the Mutagenicity Data Set

<table>
<thead>
<tr>
<th></th>
<th>found alerts</th>
<th>coverage of actives</th>
<th>coverage of inactives</th>
</tr>
</thead>
<tbody>
<tr>
<td>Derek Nexus</td>
<td>73</td>
<td>2632</td>
<td>659</td>
</tr>
</tbody>
</table>

“The columns headed “coverage of actives” give the number and percentage of active compounds that exhibit at least one of the alerts. The columns headed “coverage of inactives” give the number and percentage of inactive compounds that exhibit at least one of the alerts.

Table 5. Comparison of the Coverage of EPs and Derek Nexus

<table>
<thead>
<tr>
<th></th>
<th>exclusive coverage</th>
<th>shared coverage</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>actives</td>
<td>inactives</td>
</tr>
<tr>
<td>EP</td>
<td>561</td>
<td>830</td>
</tr>
<tr>
<td>Derek Nexus</td>
<td>234</td>
<td>78</td>
</tr>
</tbody>
</table>

“The columns headed “exclusive coverage” give the number of active and inactive compounds that are exclusively found in the support for at least one EP or exhibit at least one Derek Nexus alert. The columns headed “shared coverage” give the number of active and inactive compounds that are found in both the support for at least one EP and exhibit at least one Derek Nexus alert.

Figure 6. Number of supporting active and inactive compounds for each EP and their resulting growth rate.

Figure 7 shows the root nodes of three trees, one generated by EP mining and two by JEP mining, all of which represent structural variations of aromatic nitro compounds: examples of the molecules that support each pattern are shown together with the fragment(s) that comprise them. The EP is composed of a single fragment that describes a nitro group bonded to an aromatic carbon atom: a well-known activating substructure for
in vitro mutagenicity. The EP is supported by all the aromatic nitro compounds in the data set (784), including 143 compounds classified as inactive. The EP hierarchy contains 11 child nodes below the root shown. JEPs, on the other hand, are restricted to patterns that occur only in active compounds, and so numerous JEPs are formed that describe variations in the structural features surrounding the nitro group in the active molecules that are not present in the inactives. JEP 1 is a combination of the aromatic nitro group fragment and a subfragment of a furan ring that includes two aromatic carbon atoms and an aromatic oxygen atom. JEP 1 is supported by only 96 of the actives, and the JEP 1 hierarchy contains 32 child nodes. JEP 2 is a combination of the aromatic nitro group fragment, a thiophene ring, and a subfragment of thiophene that includes an aromatic sulfur atom and two aromatic carbon atoms. JEP 2 is supported by 37 actives, and the JEP 2 hierarchy contains 24 child nodes. The structural features represented by JEP 1 and JEP 2 are also found among the 11 nodes below the root node in the

Figure 7. Patterns and support for the root nodes of one EP and two JEP hierarchies that describe aromatic nitro compounds. Examples of supporting molecules are shown for each pattern; separate sets of examples are shown for actives and inactives supporting the EP. The fragments that the patterns are composed of are shown above the supporting molecules — see text for further details.
EP hierarchy; despite the smaller number of patterns and hierarchies, these two potentially activating structural features have still been identified.

Figure 8 shows the root nodes of an EP and one JEP tree that represent variations of azide compounds: examples of the molecules that support each pattern are shown together with the fragment(s) the pattern is composed of. The EP is composed of a single fragment that describes an azide group bonded to an aliphatic carbon atom: another well-known mutagenic substructure. The EP hierarchy includes only the EP shown, which is supported by all aliphatic azides in the data set including a single compound classified as inactive. This single inactive azide is responsible for there being no single JEP that can represent all azides in the data set. Thus, JEPs are formed that describe variations in the structural features surrounding the azide group in the active molecules that are not present in the inactives. The JEP shown in the figure is a combination of the azide group fragment and a hydroxyl group. The JEP is supported by 24 actives, and the JEP hierarchy contains 16 further nodes.

For the mutagenicity data set, both EP and JEP mining have been successful in producing clusters of compounds that are representative of known activating substructures for in vitro mutagenicity. However, significantly fewer patterns and hierarchies are produced by the EP method, and the hierarchies typically contain fewer nodes. Browsing of the results of EP mining to identify potentially activating features is, therefore, far easier than is the case for JEP mining. Moreover, the patterns produced by EP mining are typically more representative of
known mutagenic structures.\textsuperscript{30} The presence of the activating substructures in the inactives results in longer JEPs that include additional, sometimes unrelated structural features. This additional detail is often difficult to interpret making it hard to identify combinations of features that represent variations of the activating substructures that genuinely increase activity.

**Alert Substructure Development.** A number of the EPs mined from the \textit{in vitro} mutagenicity data set represent good candidates for forming the basis of new alert substructures and for refining existing alerts. New alerts would result in an increase in the coverage of actives and thus an increase in the sensitivity of an expert system, and refining of existing alerts to reduce the coverage of inactives would improve the specificity of an expert system. A subset of the EPs that represent potential gaps within the Derek Nexus knowledge base was selected for detailed analysis. These are EPs that are supported by a proportionally high number of compounds that Derek Nexus incorrectly predicted as negative (false negatives) and a proportionally low number of compounds correctly predicted to be negative (true negatives). This subset was evaluated by one of Lhasa Limited’s knowledge base developers by analyzing relevant literature and validated using in-house data sets. One such EP and the fragment it represents is shown in Figure 9 together with example molecules that support the pattern and a confusion matrix, shown in Table 6, that compares the true activity classifications with the Derek Nexus predictions for the compounds supported by the pattern. The EP is composed of a single fragment that describes a xanthene ring system and is supported by a range of xanthene derivatives, which have been used to define two new alerts for the Derek Nexus knowledge base.

**hERG Channel Inhibition.** EPs were mined from the hERG channel inhibition data using both types of fingerprint and a minimum threshold for support in actives of 0.02, i.e., 2\% the active class or at least 5 molecules. The parameter for support in inactives was 0.001. The hERG data set is strongly biased toward inactives (252 actives and 1708 inactives). The support values were chosen to ensure that EPs occur in more actives than inactives as an absolute number. This resulted in a very limited support space from which to find EPs and necessitated a noise tolerance parameter of 1.0 and a linear frontier; increasing the noise tolerance parameter above 1.0 would have limited the support space even further and may have precluded the identification of any EPs. The minimum growth rate and gradient of the emerging frontier was therefore 20.0. Unlike for mutagenicity, the EP mining heuristics were applied such that branches that produced an EP were not immediately pruned, so that a branch may produce multiple EPs. The numbers of unique EPs generated using each set of descriptors are shown in Table 7. The columns headed “coverage of actives” show the number and percentage of the active class found considering all EPs. A much smaller number of EPs were produced than for \textit{in vitro} mutagenicity and the coverage of the active class was very low; however, the EPs have very high growth rates and are therefore very strongly emerging.

Detailed inspection of the 12 EPs generated using the fragment descriptors indicated that they may represent only three distinct classes of hERG channel inhibitors: one class is represented by 10 of the 12 EPs. Figure 10 shows the 10 EPs that have been combined to represent a single class: examples of the molecules in the class are shown together with the fragment(s) that the EPs are composed of and the observed combinations of those fragments. If interpreted as a single pattern, the combined EPs loosely describe a tertiary amine with aliphatic neighbors and two aromatic rings that are often joined by another tertiary amine: key components of known pharmacophores for hERG inhibition.

**Table 6. Confusion Matrix of the Predictions Made by Derek Nexus for Xanthene Derivatives Supporting an EP**

<table>
<thead>
<tr>
<th></th>
<th>true activity</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>positive</td>
<td>negative</td>
<td></td>
</tr>
<tr>
<td>predicted activity</td>
<td>10 6</td>
<td>13 2</td>
<td></td>
</tr>
</tbody>
</table>

**Table 7. Number of EPs Mined from the hERG Channel Inhibition Data Set Using Different Descriptors**

<table>
<thead>
<tr>
<th>descriptors</th>
<th>coverage of actives</th>
<th>coverage of inactives</th>
</tr>
</thead>
<tbody>
<tr>
<td>fragments</td>
<td>count</td>
<td>%</td>
</tr>
<tr>
<td>pharmacophores</td>
<td>2 21</td>
<td>8.33%</td>
</tr>
</tbody>
</table>

\textsuperscript{30}The columns headed “coverage of actives” give the number and percentage of active compounds included in the support for at least one of each set of EPs — see text for further details.

Figure 9. Pattern and support for the root node of one hierarchy that describe xanthenes that resulted in poor Derek Nexus performance. The fragment that the pattern comprises is shown with examples of supporting active compounds that Derek Nexus incorrectly predicted to be inactive — see text for further details.

Figure 10. Pattern and support for the root node of one hierarchy that describe xanthenes that resulted in poor Derek Nexus performance. The fragment that the pattern comprises is shown with examples of supporting active compounds that Derek Nexus incorrectly predicted to be inactive — see text for further details.
channel inhibition. The pattern also gives an indication of the distance from the twin aromatic system to the aliphatic tertiary amine; there is often a chain of three aliphatic carbon atoms present, which inspection of the supporting compounds shows is frequently between the aromatic system and the tertiary amine. This distance is in accordance with known pharmacophores for hERG channel inhibition.

Figure 11 shows the two remaining EPs from the set of 12: examples of the molecules that support each pattern are shown together with the fragments that compose them. Both EPs are in fact JEPs, as they are only supported by the actives shown. EP 1 describes a hydroxyl group bonded to an aromatic carbon atom and a positively charged nitrogen atom that forms part of an aromatic system with one aliphatic neighbor. Inspection of the compounds supporting EP 1 shows that three do not include the aliphatic tertiary amine that is commonly associated with hERG channel inhibition but do have a common quinolinol group that may be of significance. The remaining two supporting compounds do contain an aliphatic tertiary amine and clearly conform to known pharmacophores. EP 2 describes an aliphatic tertiary amine and an oxygen atom between two aromatic carbon atoms. The EP is supported by four complex ring molecules and a structurally simpler compound that clearly conforms to known pharmacophores for hERG channel inhibition.

Figure 12 shows the two EPs mined from the hERG inhibition data using pharmacophore pairs: examples of the molecules that support each pattern are shown together with the pharmacophore pairs that compose them and a supporting example in both its reduced graph and molecular form. EP 1 is composed of four pharmacophore pairs describing the following: an aromatic system two bonds away from another aromatic system; an aromatic system two bonds from an aliphatic chain; an aromatic system two bonds from a hydrogen bond acceptor; and an aromatic system three bonds from a hydrogen bond acceptor. These sets of features correspond to a known pharmacophore comprising two aromatic groups, at least one chain of two atoms or greater, suggesting a distance of at least three bonds, and at least one hydrogen bond acceptor. EP 2 is composed of three pharmacophore pairs describing the following: an aromatic system neighboring a hydrogen bond acceptor; an aromatic system seven bonds from a hydrogen bond acceptor; and an aliphatic chain six bonds from a hydrogen bond acceptor. These features correspond to a pharmacophore comprising a single aromatic group and a more distant hydrogen bond acceptor; inspection of the compounds supporting EP 2 suggests the
The distance between the hydrogen bond acceptor and the aromatic system is more varied but typically further than observed in the support for EP 1.

Mining EPs from hERG channel inhibition data using both types of descriptors has resulted in quite well-defined clusters of compounds. This has demonstrated the capability of the CP-tree mining method and the EP selection heuristics to tolerate highly biased data sets. However, the fragment descriptors are too specific to describe the various structural features capable of interacting with the hERG channel and are thus poorly suited to this toxicity end point. The pharmacophore pairs are more generalized; mining EPs using this type of descriptor has resulted in the formation of two descriptions of structural features that closely resemble known pharmacophores for hERG channel inhibition. A direct comparison between EPs and JEPs has not been attempted for the hERG inhibition data set and these descriptors. In the next section we demonstrate that the JEP mining method can be considerably less efficient than mining EPs.

**Performance.** To demonstrate the improved efficiency and thus reduced run time of the EP mining method compared to JEP mining, EPs and JEPs were mined from data sets for three different toxicity end points using three different types of descriptors. For EP and JEP mining, the minimum threshold value for support in actives was 0.05, i.e. 5% the active class. For EP mining, the parameter for support in inactives was also 0.05, resulting in an initial gradient of the curved growth frontier of 1.0. The curve of the frontier was defined by a noise tolerance parameter of 1.5; quite a strict definition of EPs.

EPs and JEPs were mined from the *in vitro* mutagenicity, hERG channel inhibition, and oestrogenicity data sets described in detail in our previous publication. In brief, the mutagenicity data set consists of 195 Ames active compounds (comprising alkylating agents; \(\alpha,\beta\)-unsaturated aldehydes; epoxides; and aromatic nitro compounds) and 424 inactive compounds extracted from the Lhasa Limited Vitis 4 database. The hERG inhibition data set was also extracted from the same version of Vitis and consists of 148 compounds (114 active and 34 inactive classified using an IC\(_{50}\) threshold of 20 \(\mu\)M). The oestrogenicity data set was obtained from the Distributed Structure-Searchable Toxicity (DSSTox) network, hosted by the US EPA,\(^{33}\) and is composed of 232 compounds with 131 classified as active (ER_RBA+) and 101 classified as inactive (ER_RBA-) based on estrogen receptor binding affinity data, obtained through in vitro assay experiments. The following descriptors were generated using a KNIME workflow including an RDKit\(^{19}\) fingerprinting node: atom-pairs, again described in our previous work; Morgan\(^{34}\) circular fingerprints; and Morgan-feature fingerprints, which encode pharmacophoric features as pseudo atoms. Two ranges of lengths were used for each type of descriptor. For atom-pairs, length represents the number of bonds between the encoded atoms, while for Morgan circular fingerprints length is the radius, in bonds, from a central atom. The length ranges for atom-pairs were 1–4 bonds and 1–8 bonds. The length ranges for the Morgan fingerprints were 1–2 bonds and 1–4 bonds:

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**Figure 11.** Patterns and support for two EPs that describe different classes of hERG channel inhibitors. Examples of supporting molecules are shown for each pattern. The fragments the patterns are composed of are shown above their supporting molecules – see text for further details.
Figure 12. Patterns and support for two EPs that describe different classes of hERG channel inhibitors. The pharmacophore pairs comprising the patterns are shown above their support. Examples of supporting molecules are shown for each pattern; an example active is also shown for each pattern in a reduced graph representation and its original structural form — see text for further details.
equivalent to Extended-Connectivity Fingerprints (ECFP) with diameters of 2–4 and 2–8. The run times observed when mining EPs and JEPs from the three data sets using the different descriptors and length ranges is shown in Table 8. The columns headed “run time (min)” show the number of minutes required to complete the EP and JEP mining process; “N/A” indicates that the mining process failed to complete within 8640 min, i.e. 6 days.

The run times observed when mining EPs are consistently below 1 min with the variation between the shortest and longest time only 30 s. Conversely, the JEP mining run times varied greatly from between approximately 6 s to 6 days. The longest run times were observed when mining JEPs using atom-pairs with a broader length range and thus more descriptors. In such cases the JEP method failed to complete the mining process in two of three experiments, while the EP mining method completed the process within 1 min. EP mining is therefore scalable to a wider range of fingerprint types, lengths, and densities, making it a more broadly applicable and reliable knowledge discovery technique.

### Table 8. Run Times Observed When Mining EPs and JEPs Using Different Descriptors

<table>
<thead>
<tr>
<th>end point</th>
<th>descriptor</th>
<th>length (bonds)</th>
<th>descriptor count</th>
<th>run time (min)</th>
</tr>
</thead>
<tbody>
<tr>
<td>mutagenicity</td>
<td>atom-pair</td>
<td>1–4</td>
<td>1058</td>
<td>0.5 81.5</td>
</tr>
<tr>
<td></td>
<td>atom-pair</td>
<td>1–8</td>
<td>1956</td>
<td>0.7 N/A</td>
</tr>
<tr>
<td></td>
<td>Morgan</td>
<td>1–2</td>
<td>0.3 0.1</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Morgan</td>
<td>1–4</td>
<td>0.3 0.2</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Feature-Morgan</td>
<td>1–2</td>
<td>0.2 0.2</td>
<td></td>
</tr>
<tr>
<td></td>
<td>feature-Morgan</td>
<td>1–4</td>
<td>0.3 0.8</td>
<td></td>
</tr>
<tr>
<td>hERG inhibition</td>
<td>atom-pair</td>
<td>1–4</td>
<td>663</td>
<td>0.2 4.6</td>
</tr>
<tr>
<td></td>
<td>atom-pair</td>
<td>1–8</td>
<td>1426</td>
<td>0.5 N/A</td>
</tr>
<tr>
<td></td>
<td>Morgan</td>
<td>1–2</td>
<td>0.2 0.1</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Morgan</td>
<td>1–4</td>
<td>0.3 0.2</td>
<td></td>
</tr>
<tr>
<td></td>
<td>feature-Morgan</td>
<td>1–2</td>
<td>0.2 0.1</td>
<td></td>
</tr>
<tr>
<td></td>
<td>feature-Morgan</td>
<td>1–4</td>
<td>0.2 0.5</td>
<td></td>
</tr>
<tr>
<td>oestrogenicity</td>
<td>atom-pair</td>
<td>1–4</td>
<td>337</td>
<td>0.3 76.4</td>
</tr>
<tr>
<td></td>
<td>atom-pair</td>
<td>1–8</td>
<td>658</td>
<td>0.4 8595.0</td>
</tr>
<tr>
<td></td>
<td>Morgan</td>
<td>1–2</td>
<td>0.3 1.1</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Morgan</td>
<td>1–4</td>
<td>0.4 0.2</td>
<td></td>
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<tr>
<td></td>
<td>feature-Morgan</td>
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<tr>
<td></td>
<td>feature-Morgan</td>
<td>1–4</td>
<td>0.3 5.0</td>
<td></td>
</tr>
</tbody>
</table>

The practical application of the emerging pattern mining to incorporate the resulting alerts into an existing expert system. We have validated the approach on data sets in which features giving rise to toxic effects are well understood and demonstrated its tolerance of biased data sets for more complex end points. The method has also been applied to identify toxicophores and incorporate the resulting alerts into an existing expert system. The practical application of the emerging pattern mining to develop alerts will be described in greater detail in a forthcoming paper.

### CONCLUSIONS

We have developed an emerging pattern mining method that can assist knowledge base developers in compiling structural alerts to improve the performance of expert systems for toxicity prediction. Emerging patterns have the significant advantage over the jumping emerging patterns described in our earlier work of being tolerant to noise in the data. This is achieved through allowing some inactives to be covered by an emerging pattern which can compensate for misclassified data. This characteristic typically leads to a much smaller number of patterns being generated which makes the output more manageable for browsing by knowledge developers. Furthermore, the time required to generate emerging patterns for the data sets described here was consistently less than 1 min for a variety of descriptor types, whereas the corresponding times for jumping emerging pattern mining were much more variable, and, in some cases, the jumping emerging pattern mining was still running after 6 days. Our implementation of emerging pattern mining is based on the CP-tree algorithm which uses various heuristics to restrict the patterns to those that are most likely to be of interest. The method is not intended to generate definitive toxicological alerts wholly automatically but to provide a tool for experts to enable them to explore data in order to develop alerts. We have validated the approach on data sets in which features giving rise to toxic effects are well understood and demonstrated its tolerance of biased data sets for more complex end points. The method has also been applied to identify toxicophores and incorporate the resulting alerts into an existing expert system. The practical application of the emerging pattern mining to develop alerts will be described in greater detail in a forthcoming paper.

### ASSOCIATED CONTENT

Supporting Information

Our curated version of the Hansen mutagenicity data set with Derek Nexus prediction and the hERG channel inhibition data set extracted from PubChem. This material is available free of charge via the Internet at http://pubs.acs.org.

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#### Notes
The authors declare no competing financial interest.

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