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The Impact of Road Grade on Carbon Dioxide (CO₂) Emission of a Passenger Vehicle in Real-World Driving

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Abstract

To accurately estimate real-world vehicle emission at 1Hz the road grade for each second of data must be quantified. Failure to incorporate road grade can result in over or underestimation of a vehicle's power output and hence cause inaccuracy in the instantaneous emission estimate. This study proposes a simple LiDAR (Light Detection And Ranging) – GIS (Geographic Information System) road grade estimation methodology, using GIS software to interpolate the elevation for each second of data from a Digital Terrain Map (DTM). On-road carbon dioxide (CO₂) emissions from a passenger car were recorded by Portable Emission Measurement System (PEMS) over 48 test laps through an urban-traffic network. The test lap was divided into 8 sections for micro-scale analysis. The PHEM instantaneous emission model (Hausberger, 2003) was employed to estimate the total CO₂ emission through each lap and section. The addition of the LiDAR-GIS road grade to the PHEM modelling improved the accuracy of the CO₂ emission predictions. The average PHEM estimate (with road grade) of the PEMS measured section total CO₂ emission (n=288) was 93%, with 90% of the PHEM estimates between 80% and 110% of the PEMS recorded value. The research suggests that instantaneous emission modelling with LiDAR-GIS calculated road grade is a viable method for generating accurate real-world micro-scale CO₂ emission estimates. The sensitivity of the CO₂ emission predictions to road grade was also tested by lessening and exaggerating the gradient profiles, and demonstrates that assuming a flat profile could cause considerable error in real-world CO₂ emission estimation.

35 **Keywords**

36

37 Vehicle Emissions; Carbon Dioxide; Vehicle Specific Power; Road Grade; Portable Emission
38 Measurement System (PEMS); LiDAR.

39

40

41 **1. Introduction**

42

43 Research has demonstrated that on-board vehicle Portable Emission Measurement Systems (PEMS)
44 can be utilised to provide accurate measurement of vehicle exhaust emissions in real-world driving
45 (Frey et al., 2003; Liu et al., 2010; Ropkins et al., 2007). PEMS instrumentation in such studies are
46 deployed to record the motion, geographical position and exhaust emission of a vehicle driven over a
47 real-world test route, most commonly measured on a second-by-second basis. Utilising the 1Hz
48 PEMS data and values from the test vehicle specification, the engine power output of the vehicle for
49 each second of data can be computed and used as an explanatory variable in predicting fuel
50 consumption and exhaust emission at that instant.

51

52 Exploiting the relationship between engine power and exhaust emission, the latest generation of
53 emissions models such as the US Environmental Protection Agency's (EPA) MOtor Vehicle Emission
54 Simulator (MOVES) (Koupal et al., 2004), the Netherlands Organisation for Applied Scientific
55 Research's (TNO) VERSIT+ model (Smit et al., 2007) and the Technical University of Graz's (TUG)
56 Passenger car and Heavy duty Emission Model (PHEM) (Hausberger, 2003) predict vehicle exhaust
57 emission by referencing the calculated engine power output for each second of data to a calibrated
58 mass of exhaust emission at that power, for each emission species.

59

60 Derivation of instantaneous engine power output requires a second-by-second measure of vehicle
61 speed, acceleration and road gradient. PEMS can reliably capture vehicle speed, and hence
62 acceleration, during real-world driving, but road grade is very difficult to measure accurately from an
63 instrumented vehicle (Zhang and Frey, 2006).

64

65 A number of studies have highlighted the significant influence road grade can have on real-world fuel
66 consumption and exhaust emission (Boriboonsomsin and Barth, 2009; Boroujeni and Frey, 2014;
67 Zhang and Frey, 2006). For test sections with positive road grade, as the gradient increases so must
68 the engine power output to keep the vehicle at a constant speed, due to the increasing force of gravity
69 opposing the motion of the vehicle. This increase in power requires greater fuel consumption
70 resulting in increased CO₂ exhaust emission. Likewise where a vehicle is travelling on a road with
71 negative grade, gravity acts to accelerate the vehicle, reducing the power demand on the engine,

72 which lowers fuel consumption and hence CO₂ emission. Zhang and Frey (2006) recorded an
73 increase in CO₂ emission of 40-90% for three light duty gasoline vehicles over sections of road with
74 gradient $\geq 5\%$ when compared to sections with gradient $\leq 0\%$, whilst Boriboonsomsin and Barth
75 (2009) measured a 15-20% rise in fuel consumption for a gasoline passenger car between a flat route
76 and a hilly route.

77

78 Given the effect of road grade on engine power output and therefore vehicle emission, it is vital for
79 micro-scale emission modelling that instantaneous engine power output is calculated accurately,
80 which necessitates a representative road grade value for each second of test data. There are a number
81 of methods for quantifying road grade proposed in the literature, including; calculation from design
82 drawings; direct land survey measurement; on-board measurement by GPS, accelerometers,
83 barometric altimeters and inclinometers; and mathematical derivation from DTM or DEM (digital
84 elevation maps), each with different characteristics relating to accuracy, precision, scale and price
85 (Boroujeni et al., 2013; Sahlholm and Johansson, 2010; Zhang and Frey, 2006). Zhang and Frey
86 (2006) proposed a LiDAR based methodology concluding that the LiDAR method is advantageous;
87 having relatively few practical and logistical limitations compared with other methods, and can be
88 considered sufficiently accurate for emission estimation.

89

90 LiDAR is a mapping technique which quantifies terrain elevation using laser measurement from
91 aircraft. These measurements can be processed to construct highly accurate Digital Terrain Models
92 (DTM) which render a three dimensional representation of the surface topography, describing
93 elevation and position. The availability and cost of LiDAR data have been a cited as a main
94 limitation in its use for road grade estimation (Boroujeni et al., 2013), however, a comprehensive
95 LiDAR 5-metre resolution DTM dataset for the U.K. is available free of charge to academics and
96 students at U.K. institutions through the Landmap Kaia Service hosted at MIMAS based at the
97 University of Manchester (Millin-Chalabi et al., 2011). The advantage of the simple LiDAR-GIS
98 method proposed in this study is that by referencing the measured GPS position to a DTM elevation, a
99 representative 1Hz road grade profile can be quickly generated for a test area without the multiple
100 runs required by GPS measured altitude methodologies (Boroujeni et al., 2013; Sahlholm and
101 Johansson, 2010) and without the detailed roadway analysis and segmentation required in the LiDAR
102 methodology described by Zhang and Frey (2006).

103

104 In combination with reducing the fossil fuel dependence of the vehicle fleet through engine efficiency
105 improvements and new vehicle technologies, road traffic management schemes may also deliver CO₂
106 emission reductions. Mechanisms such as better traffic control systems, which reduce the number of
107 aggressive braking and acceleration events through a network; eco-driver training, which promotes
108 efficient driving; policies which reward multiple-occupancy of cars or the use of public transport to

109 reduce both the number of vehicle trips and traffic congestion; and improved road geometry design to
110 reduce the impact of road grade can all be used to reduce CO₂ emission from the road transport sector.
111 In order to provide detailed micro-scale assessment of the impact of such strategies, emission
112 estimation models are required that can predict emissions of vehicles in real-world driving conditions
113 with sufficient accuracy and resolution to quantify their environmental benefit and inform the policy
114 decision making process.

115

116 The purpose of this paper is to develop and demonstrate a simple LiDAR-GIS methodology for
117 calculating a representative 1Hz road grade for use in instantaneous vehicle emission modelling. The
118 sensitivity of CO₂ emission predictions to road grade, in a range of traffic conditions will also tested.

119

120

121 2. Methodology

122

123 2.1. Study Design

124

125 A fixed lap through Headingley, Leeds was used as a test route for the research. This test lap, shown
126 in Figure 1, comprises a 4.6 km route on mainly single lane urban commuter roads, with a speed limit
127 of 30 mph (48 km/h). The route encompasses one of the main arterial roads into and out of Leeds and
128 is frequently congested.

129

130

Figure 1. Headingley Test Lap and Sections (GPSVisualizer, 2013)



131

132

133 The test lap was covered by the same driver in an instrumented vehicle a total of 48 times during a
134 week-long testing period between the 26th February 2007 and the 5th March 2007, with runs conducted
135 between the hours of 07:30 and 21:00 to capture the full range of traffic conditions for this road
136 network. The laps were completed in variety of weather conditions, with sunny, dry, overcast and
137 rainy test laps, in temperatures ranging from 1°C to 15°C.

138

139 In order to facilitate analysis at a micro-scale level the Headingley lap was divided into 8 test sections
140 (see Figure 1). These sections were determined by classifying points of latitude and longitude to mark
141 the beginning and end of each section, after which the closest measured GPS points from each run to
142 those selected start and end points were identified. Sections 1 and 8 are the same segment of road but
143 with opposite directions of traffic flow, likewise sections 2 and 4, and sections 5 and 7. Section 3 and
144 section 6 are separate short ‘turning’ sections.

145

146 2.2. Test Vehicle

147

148 The instrumented vehicle used in this study was a EURO 4 emission compliant petrol Ford Mondeo
149 with a 5-speed manual gearbox and a port fuel injected 1.8 litre, 4 cylinder, 16 valve spark ignition
150 engine with a maximum power of 92 kW (125 PS) at 6000 rpm. The vehicle was equipped with a
151 Three Way Catalyst (TWC).

152

153 The vehicle specifications used for modelling in this study are a kerbweight (with 90% fuel levels, full
154 fluid levels and a 75kg driver) of 1374 kg (Li et al., 2008), a rolling resistance coefficient of 0.013
155 (Ehsani et al., 2009), an aerodynamic drag coefficient of 0.32, a frontal area of 2.3 m² (Doucette and
156 McCulloch, 2011), and an idle engine speed of 850 rpm.

157

158 2.3. Test Vehicle Instrumentation

159

160 A Horiba On Board emission measurement System (OBS-1300) was used to measure the exhaust
161 flow rate and air/fuel ratio, enabling calculation of CO₂ mass emission from the volumetric
162 measurements. Speed, acceleration and geographical position data were measured and recorded by a
163 RaceLogic VBOX II GPS engine and data logger. All data was recorded at 1 Hz. The OBS set up and
164 its validation over a wide range of engine operating conditions and drive cycles is described by
165 Ropkins et al. (2008).

166

167 The OBS and VBOX were time aligned using the vehicle velocity data measured by each instrument.
168 Exhaust flow measurement drift was corrected, where required, using the standard ‘on-road’
169 correction method used in other University of Leeds studies, measuring ‘zero flow’ values before and

170 after each test run and re-calibrating the zero-points, assuming a linear drift over the test (Ropkins et
171 al., 2007). The documented OBS-1300 ‘pulse effect’ overestimation of idle exhaust flow (Daham et
172 al., 2005; Nakamura et al., 2002; Ropkins et al., 2008) was corrected based on the work of Ropkins et
173 al. (2008), which demonstrated an OBS overestimation of idle exhaust flow rate in the order of 40 to
174 60 percent. A correction factor was applied to the OBS measured exhaust flow rate at all points of
175 vehicle engine idle recorded during the testing.

176

177 2.4. Mass Emission Calculation

178

179 The exhaust CO₂ emissions as measured by use of the OBS-1300 are captured on a volumetric basis.
180 The CO₂ mass emission rate is calculated from the measured exhaust gas volumetric flow rate, the
181 density of CO₂ and the wet gas concentration of CO₂, using Equation 1.

182

$$183 \text{CO}_{2\text{ MASS}} = [\text{CO}_2]_{t=t+\text{DT}} \times \text{MWT}_{\text{CO}_2} \times [\text{Q}_{\text{EX}}]_{t=t} \times (273.15/293.15) \times \text{UCF} \quad (1)$$

184

185 Where, CO_{2 MASS} is the CO₂ mass emission rate in g/s, standardised to 20°C and 1 atm (293.15K and
186 101.3 kPa); [Q_{EX}]_{t=t} is the exhaust flow rate in m³/min at time t; [CO₂]_{t=t+DT} is the percentage
187 concentration of CO₂ associated with [Q_{EX}]_{t=t}, which is read after a measurement Delay Time (DT);
188 MWT_{CO₂} is the molecular weight of CO₂, 44.01 g/mol; and UCF are the required Unit Conversion
189 Factors. The Unit Conversion Factors are a multiplication by 1/100 to correct the units of [CO₂]_{t=t+DT}
190 from a percentage volume to volume; a multiplication of 1/60 to change the units of [Q_{EX}]_{t=t} from
191 m³/min to m³/s; a multiplication of 1/22.415 to convert MWT_{CO₂} from g/mol to CO₂ density using the
192 ideal gas volume of 1 mole at Standard Temperature and Pressure (STP), with 273.15/293.15
193 amending the density of CO₂ to that at 20°C and 1 bar

194

195 2.5. LiDAR-GIS Methodology for Elevation Profile and 1Hz Road Grade Estimation

196

197 The possible error range resulting from instrument imprecision (the VBOX II has a 95% Circular
198 Error Probability (CEP) of 10 metres, meaning that the measured height is within 10 metres of the
199 true position 95% of the time (Racelogic, 2008)) and measurement errors during vehicle transit,
200 caused by GPS signal interference from buildings in urban streets for example, made the raw GPS
201 height measurements recorded by the instrumented vehicle too unreliable to use to generate an
202 accurate elevation profile for the test lap, and insufficiently precise to calculate road grade for each
203 second of data. The test lap elevation profile in this research was instead calculated using a 5m DTM,
204 generated from the LiDAR elevation data, provided through Landmap Kaia (Millin-Chalabi et al.,

205 2011) . The DTM and the VBOX measured GPS positions for each test run were imported into the
206 GIS software ArcGIS enabling the height at each recorded GPS point to be extracted from the DTM.
207

208 The road grade for each second of recorded data was calculated by applying an algorithm to reduce
209 the effect of errors associated with inaccuracies in the measured GPS latitude and longitude position
210 (95% CEP of 3m (Racelogic, 2008)). The errors resulting from GPS absolute position measurement
211 accuracy are especially apparent at points where the vehicle was moving slowly or stationary, as the
212 GPS position appears to shift whilst the vehicle is not moving. As the GPS position changes, so does
213 the elevation estimate extracted from the 5-metre DTM and relatively small changes in GPS position
214 can result in changes in the elevation estimate. Unfeasible erroneous gradients may therefore be
215 calculated where the vehicle travels only a short distance along the test route but due to GPS
216 measurement error there is a significant change in the DTM extracted elevation.

217
218 In order to determine a representative gradient on a second-by-second basis an algorithm was
219 therefore applied to smooth out the errors resulting from GPS absolute position measurement
220 imprecision. For each second of data, when the vehicle was travelling at greater than 10m/s then the
221 gradient was calculated by dividing the distance travelled in the measured second by the change in
222 height in that measured second. Where the vehicle was travelling at less than 10m/s, rather than
223 calculating the gradient over 1 second, the gradient is calculated over the period from where the
224 vehicle was at least 5 metres before the start of that measured second to the point where the vehicle
225 was at least 5 metres past the end of the measured second. This ensures that the minimum length of
226 road section over which the gradient is calculated is 10 metres.

227
228 The Bluesky LiDAR height data utilised in this study have an accuracy of up to $\pm 10\text{cm}$ (Bluesky,
229 2013), however the resolution of the DTM does have an influence on the accuracy of LIDAR based
230 elevation estimates. In this study, the 5-metre resolution DTM presents a map of LiDAR calculated
231 elevations at the intersection points on a horizontal 5 metre grid covering the test area. The height of
232 any GPS point within that grid is calculated by linearly interpolating between the nearest grid
233 intersection points, by the GIS software. However as a result of interpolation, surface features such as
234 bridges, underpasses and steep road side banking, where there is an abrupt non-linear change in
235 surface elevation within a 5-metre grid square, can produce errors in the height estimation. In these
236 cases the modelled linear change in surface height does not reflect the abrupt real-world change.
237 Manual correction of physically unfeasible road grade estimates could be undertaken utilising geo-
238 referenced photographic images. In this study no manual adjustments of the estimate road grade were
239 necessary, as the Headingly test lap contained no surface features that required correction.

240

241 2.6. Vehicle Specific Power

242

243 Vehicle Specific Power (VSP) is employed in this research to estimate the power per unit mass for the
244 vehicle for each second of recorded data. The VSP of the test vehicle was calculated for each second
245 of test data, from the 1Hz vehicle speed data, recorded by PEMS measurement, and the 1Hz road
246 grade estimate generated by the LiDAR-GIS methodology. The general form of the VSP equation
247 (Jimenez-Palacios, 1999) is described in Equation 2.

248

$$249 \text{VSP} = v \cdot (a \cdot (1 + \varepsilon_i) + (g \cdot \text{grade}) + (g \cdot C_R)) + (0.5\rho_a ((C_D \cdot A)/m) (v + v_w)^2 \cdot v) \quad (2)$$

250

251 Where VSP is vehicle specific power (kW/tonne); v is vehicle speed (m/s); a is vehicle acceleration
252 (m/s^2); ε_i is the gear-dependent “Mass factor” (tonne), which is the equivalent translational mass of
253 the rotating components of the powertrain; g is the acceleration of gravity ; grade is road grade
254 (dimensionless); C_R is the coefficient of rolling resistance (dimensionless); ρ_a is the ambient air
255 density (kg/m^3); C_D is the drag coefficient (dimensionless); A is the frontal area of the vehicle (m^2); m
256 is the mass of the vehicle and v_w is the velocity of the headwind into the vehicle.

257

258 For this study the simplified VSP equation for a typical light duty vehicle (Jimenez-Palacios, 1999)
259 was employed, with the rolling resistance term coefficient ($g \cdot C_R$) of 0.128 and aerodynamic drag
260 term coefficient ($0.5\rho_a (C_D \cdot A)/m$) of 0.000318 calculated to correspond to the test vehicle used in
261 the research.

262

$$263 \text{VSP}_{\text{EURO4}} = v \times [(1.1 \times a) + (9.81 \times (\sin(\text{atan}(\text{grade}))) + 0.128] + (0.000318 \times v^3) \quad (3)$$

264

265 2.7. Modelling in PHEM

266

267 Vehicle emission estimation in this research was conducted using the power-instantaneous emission
268 model PHEM (Hausberger, 2003). The PHEM model enables micro-scale calculation of vehicle
269 second-by-second fuel consumption and exhaust emission in any reasonable driving conditions.

270 PHEM requires a 1Hz speed profile with associated road grade measurements and data describing the
271 test vehicle to calculate, for each second of test data, the engine speed and power output of the vehicle.
272 These speed and power values are then referenced to an engine emission map, specific to the test
273 vehicle’s fuel type and certified EU emission standard, to estimate the second-by-second vehicle fuel
274 consumption and emission values (Hausberger et al., 2010).

275

276 For this study the 1Hz speed profile from the PEMS was used with LiDAR-GIS calculated road
277 grades. The specification data (as described in Section 2.2) for the EURO 4 Mondeo test vehicle were
278 used to parameterise PHEM, with an estimated loading of 150 kg for the PEMS system. The PHEM
279 engine-emission map used during the modelling was that for a comparable EURO 4 petrol vehicle.
280
281

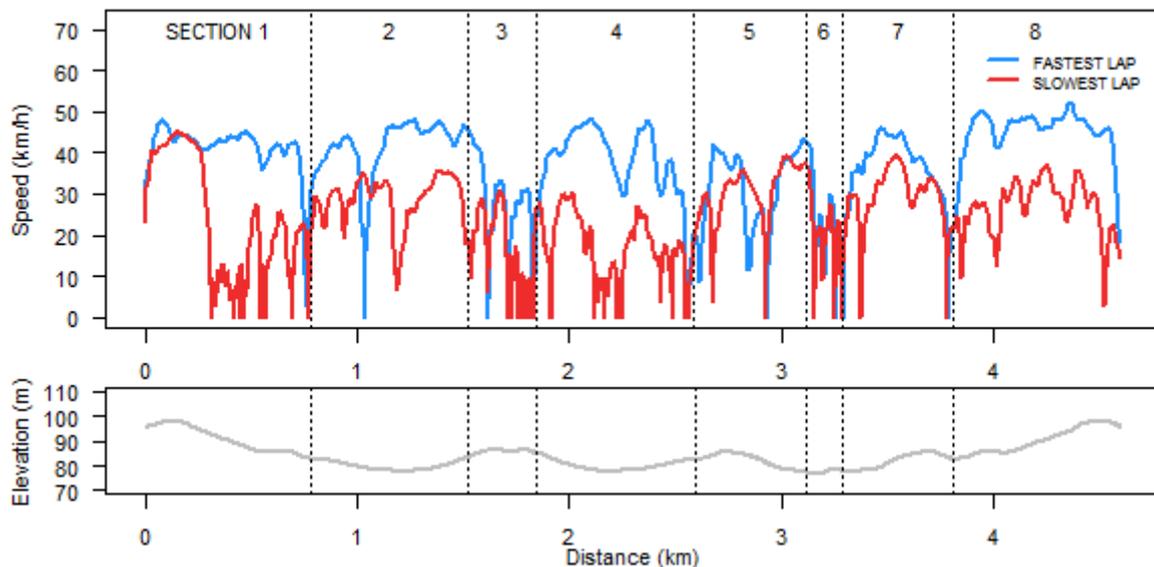
282 3. Analysis of PEMS Measurements over the Headingley Test Lap

283

284 The median time to complete the test route over the 48 test laps was 19 minutes 50 seconds, however
285 the lap times ranged from 10 minutes 14 seconds in free flowing conditions to 28 minutes 37 seconds
286 in congested traffic. The average lap speed was 14.2 km/h (range 9.6 km/h to 27 km/h). Plotting the
287 distance - speed profile for the slowest lap, recorded at 8.20am in peak morning rush hour traffic
288 against the fastest lap, recorded at 8:36pm in free flowing traffic conditions, highlights the variation in
289 vehicle operation which can occur over the same lap and road segments. The speed profile for the
290 congested lap, marked in red in Figure 2, displays recurrent periods of very low speed, where the
291 vehicle frequently stops and starts. Even outside of these periods, congestion hinders the vehicle from
292 reaching the 48 km/h speed limit for the road. The distance - speed profile for the fastest lap, marked
293 in blue, shows that whilst there were points where the vehicle was stationary, there were noticeably
294 fewer stationary points than during slowest lap, and upon restarting the vehicle was able to accelerate
295 back up to the speed limit of the road.
296

296

297 Figure 2. (a) Vehicle Distance - Speed Profiles for the Fastest and Slowest Recorded Laps and
298 (b) Elevation Profile



299
300

301 The specific traffic conditions experienced during each of the real-world test runs influenced both the
302 driver input (and as a result engine load) and the total time to complete the lap. The variability of

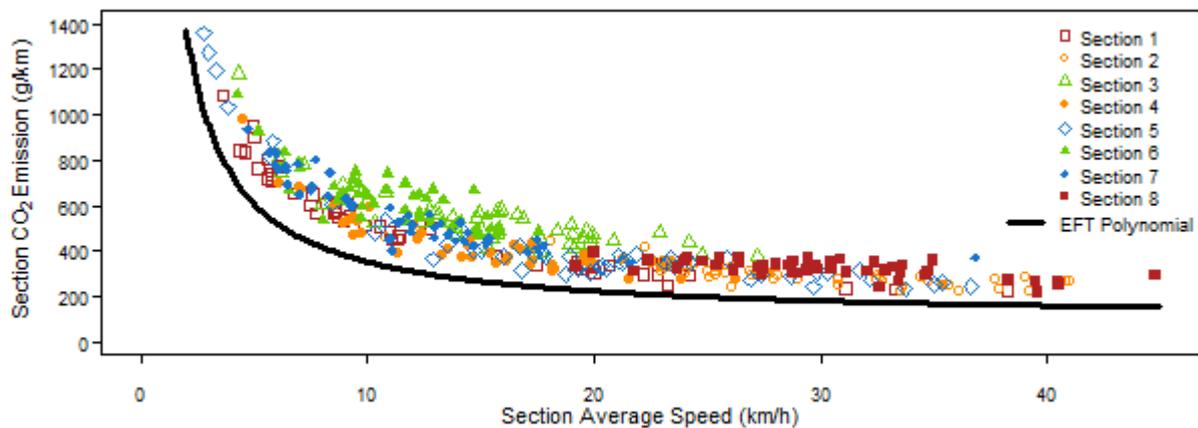
303 these conditions resulted in a wide range of average CO₂ emissions per km for the 48 test laps (313
304 gCO₂/km to 586 gCO₂/km). The median emission over the 48 laps was 438 gCO₂/km, which is more
305 than double the rated CO₂ emission for the vehicle of 182 gCO₂/km (Ford, 2005).

306

307 Figure 3 compares the PEMS measured gCO₂/km for each of the road sections. Although the section
308 emissions roughly follow the curve of the EFT function, for this vehicle the function underestimates
309 the emission generated in every section. It is also clear from the graph that at each speed the real-
310 world measurements show a wide spread of possible emission rates, indicating that CO₂ emission
311 assessment through an average speed function may not provide a reasonable estimate for real-world
312 CO₂ emission in all situations.

313

314 Figure 3. PEMS Measured Section CO₂ Emissions versus Section Average Speed (n=384). EFT
315 Polynomial is the Emission Factor Toolkit (EFT) average speed emission function for the vehicle type
316 (R012, Car <2.5 t, Petrol, 1400-2000 cc, Euro 4) (DEFRA, 2009)

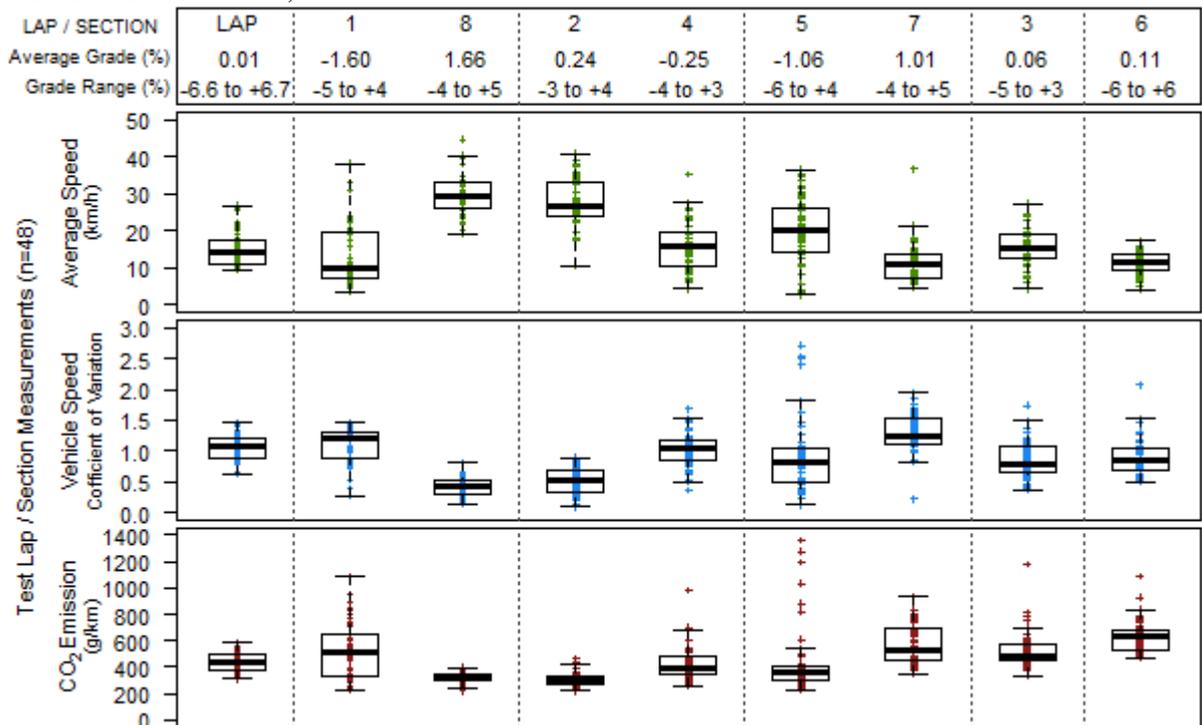


317
318

319 The coefficient of variation (CV) is the ratio of the standard deviation to the mean, is a measure of the
320 relative dispersion of vehicle speeds from the average speed, and describes the consistency of the
321 vehicle speed through a lap or section. A low CV indicates a relatively constant speed and a high CV
322 shows a wide dispersion of vehicle speeds. Sections 2 and 8 had the lowest rate of CO₂ emission and
323 also the narrowest spread of emission values (see Figure 4). These were the sections with consistently
324 high average speeds and relatively consistent vehicle speed. In these sections traffic flow was not
325 greatly hindered by increased traffic density in the network during peak traffic periods. Conversely
326 the data for sections 1 and 7 present a wide spread of CO₂ emission values. During free flowing
327 conditions these sections could be completed relatively quickly, at relatively low gCO₂/km emission
328 rates. However, during rush hour periods, the queuing times over these sections increased, raising the
329 vehicles gCO₂/km emission rate because the stationary vehicle's idle CO₂ emissions increase the total
330 CO₂ emission whilst the vehicle is not moving.

331
332

333 Figure 4. Box Plots of the Test Sections gCO₂/km, Average Speed and Vehicle Speed Coefficient of
 334 Variation measurements, over the 48 Test Runs



335
 336

337

338 **4. Evaluation of the LiDAR-GIS method for Road Grade Estimation.**

339

340 As demonstrated in other studies (Coelho et al., 2009; Song and Yu, 2009; Zhai et al., 2008), CO₂
 341 emission increases approximately monotonically with positive VSP and has a consistently low CO₂
 342 emission rate with negative VSP. To evaluate whether the LiDAR-GIS road grade values enhanced
 343 the calculation of VSP, the Pearson Correlation Coefficient (r) between VSP and CO₂ emission was
 344 calculated for each of the 48 test laps, for VSP calculated both with (VSP_G) and without (VSP₀) the
 345 LiDAR-GIS 1Hz road grade.

346

347 Table 1. Summary of the Pearson Correlation Coefficient (r) values between VSP and PEMS
 348 measured CO₂ emission for each of the 48 test laps. VSP calculated both with (VSP_G) and without
 349 (VSP₀) road grade.

Test Route	Number of Runs	VSP ₀		VSP _G	
		Ave r	r Range	Ave r	r Range
Headingley	48	0.76	0.72 - 0.80	0.79	0.74 - 0.84

350

351 To assess if there was a significant increase in the strength of the linear association between VSP and
 352 CO₂ emission with the addition of road grade the Williams' t-test for comparing two non-independent
 353 correlations was used (Howell, 2013; Williams, 1959). Both VSP calculation methods show a
 354 relatively strong linear correlation between VSP and CO₂ emission (see Table 1), however the

355 strength of the linear relationship between VSP and CO₂ emission increased for each of the 48 test
356 laps with the addition of the LiDAR-GIS road grade. In each instance, at a significance level of α
357 =.05 (two-tailed), the correlation using VSP_G proved significantly greater than the correlation
358 calculated with VSP₀, which suggests that the LiDAR-GIS method provides a reliable representative
359 1Hz gradient.

360

361

362 **5. Instantaneous CO₂ Modelling with and without LiDAR-GIS generated Road Grade.**

363

364 The PHEM instantaneous emission model was used to calculate the second-by-second CO₂ emission
365 estimates for the EURO 4 test vehicle on the Headingley test laps. In order to test the LiDAR-GIS
366 road grade methodology, CO₂ emission estimates from PHEM were calculated for each test run with
367 the test area modelled as flat with all road grade values set as zero (PHEM₀), and modelled with the
368 calculated LiDAR-GIS road grade values (PHEM_G).

369

370 PHEM was configured for the specific EURO 4 test vehicle (as described in Section 2.2) with a 150kg
371 loading and emission estimates determined from the recorded (PEMS) speed profile for each test run
372 under the two road grade conditions specified in PHEM₀ and PHEM_G. For each of the 48 test laps and
373 sections the PHEM₀ and PHEM_G modelled CO₂ aggregate emissions were compared with the
374 corresponding PEMS measurements (illustrated in the Figure 5 boxplots). Modelling each of the 48
375 test laps, the average PHEM_G estimate of the lap total CO₂ emission was 91% of the real-world PEMS
376 measured CO₂ emission, with a range from 81% to 110% (with 50% of the PHEM_G estimates between
377 87.4% and 96.1%).

378

379 Although PHEM_G modelling appears to underestimate the real-world vehicle CO₂ emission, which
380 may result from the PHEM EURO 4 petrol average engine emission map not being specific to the test
381 vehicle and/or possible disparity in the timing of the modelled and real-world gear changes, much of
382 this discrepancy is likely to be caused by factors not included in the modelling such as day-to-day
383 variation in ambient temperature, starter battery state of charge and use of the vehicles air
384 conditioning and heating systems, each of which can have a significant effect on vehicle fuel
385 consumption (Mock et al., 2012). Inaccuracy of the simulated vehicle weight may also have had an
386 influence on the modelled rate of CO₂. Although the test vehicle's kerbweight is recorded in the
387 vehicle's specification, and the vehicle loading was estimated, the actual weight of the test vehicle
388 was not directly measured. Future modelling would be improved by an accurate measure of the test
389 vehicle weight, since an underestimation may result in lower modelled than measured CO₂ emission.

390

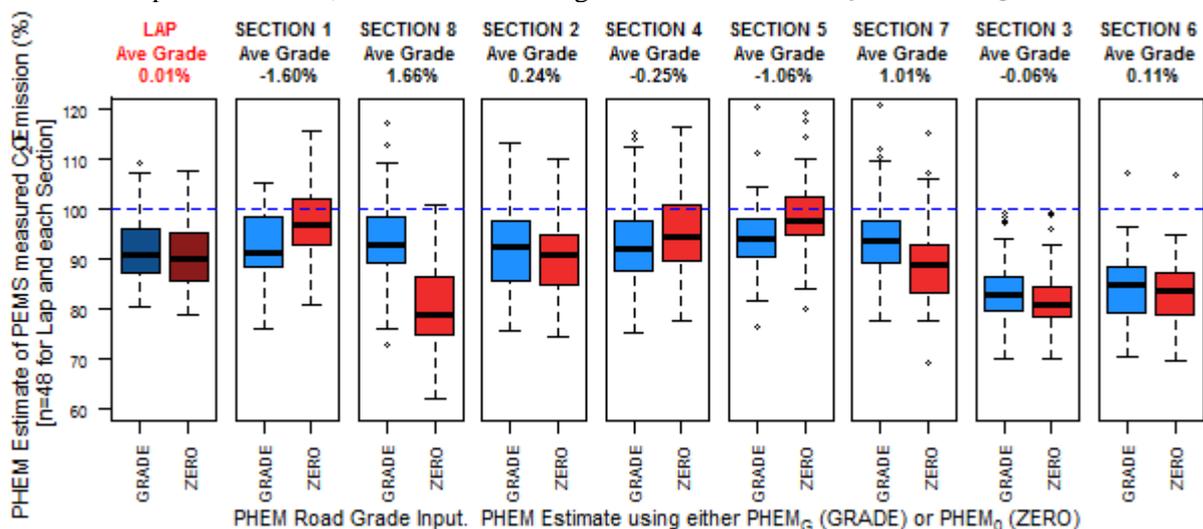
391 The average PHEM₀ estimate (without road grade) of the lap total CO₂ emission was 90% of the
 392 PEMS recorded value, with a range from 79% to 108% (with 50% of the values between 85.8% and
 393 95.3%). The results for the test lap are similar to those attained with PHEM_G, with only a slight
 394 improvement in PHEM CO₂ emission estimation over the test lap using the LiDAR-GIS road grade.
 395 The Headingley test lap starts and ends at the same point, therefore the average road grade over the
 396 lap is approximately zero. As a result, PHEM₀ overestimates of CO₂ emission on downhill road
 397 segments are partially offset underestimation on uphill road segment. The overestimation /
 398 underestimation by PHEM₀ can be seen in the Figure 5 test section box plots. Whilst the average
 399 PHEM_G estimate of the PEMS CO₂ emission in Sections 1, 2, 4, 5, 7 and 8 (excluding the turning
 400 sections) range between 91% and 94%, the PHEM₀ estimates of PEMS CO₂ emission are greatly
 401 influenced by the road grade in the section and vary from 79% to 98%.

402

403 For example over Section 1, a primarily downhill section with an average road grade of -1.6%, the
 404 average PHEM_G and PHEM₀ estimates of the section total CO₂ emission were 91% and 97% PEMS
 405 measured emission respectively. In this instance the PHEM₀ appears to provide the most accurate
 406 estimate of the real-world CO₂ emission. However over Section 8, the corresponding uphill section
 407 (the opposite traffic flow to Section 1) the average total section CO₂ emission estimate from PHEM₀
 408 is 79% of the PEMS measured value, whereas for PHEM_G it is 93%. Whilst the calculated PHEM₀
 409 CO₂ emissions for the downhill sections (1, 4 and 5) are closer to the PEMS measured emission, the
 410 stability of the PHEM_G estimates over all sections irrespective of average road grade demonstrates the
 411 addition of the LiDAR-GIS data in PHEM delivers consistently more reliable micro-simulation CO₂
 412 emission estimates.

413

414 Figure 5. PHEM modelled CO₂ emission as a percentage of the PEMS measured emission for each of
 415 the 48 test laps and sections, under the two road grade scenarios PHEM₀ and PHEM_G.



416

417

418 The PHEM CO₂ emission estimates of the real-world emission through the short ‘turning’ sections 3
419 and 6 are perceptibly less accurate than for the longer test sections. The decrease in the accuracy of
420 PHEM in these sections is likely to be due to the driver gear selections in these short stop start
421 sections not being characteristic of the gear shift patterns under normal driving conditions and hence
422 not being adequately represented in the model.

423

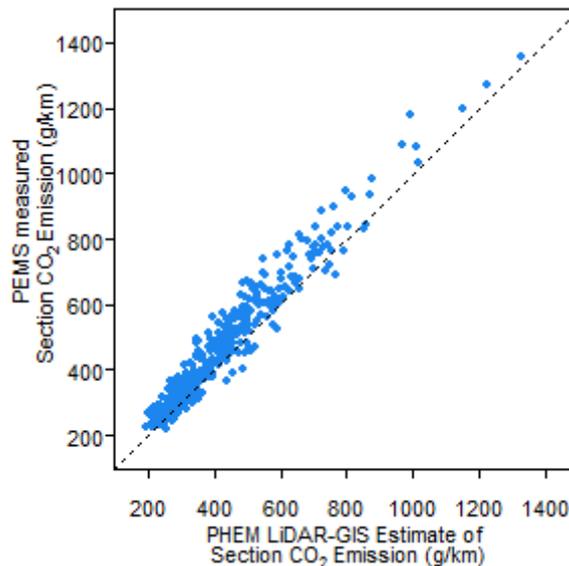
424 The stability and accuracy of the PHEM_G estimates when compared to the measured PEMS CO₂
425 emission at this micro-scale section level suggests that both the LiDAR-GIS method for generating
426 road grade provides a representative 1Hz gradient profile and that reliable micro-scale simulation of
427 CO₂ emission over real-world networks is possible utilising the PHEM power-instantaneous emission
428 model.

429

430 The scatter plot of PHEM_G CO₂ emission estimate versus the PEMS measured CO₂ emission for each
431 section (n=348) (see Figure 6) demonstrates the strength of the PHEM_G model in estimating the real-
432 world vehicle CO₂ emission over the Headingley test sections.

433

434 Figure 6. PHEM_G Calculated gCO₂/km Emission versus PEMS Recorded gCO₂/km Measurements
435 for the Headingley Test Sections.



436

437

438

439 6. Sensitivity of CO₂ Emission Estimates to Road Grade

440

441 The sensitivity of the CO₂ emission predictions to road grade was tested by lessening and
442 exaggerating the gradient profiles. PHEM CO₂ emission estimates for the test vehicle were calculated
443 using the real-world PEMS measured speed profiles under five road grade scenarios, where
444 coefficients of 0, 0.5, 1, 2 and 3 were applied respectively to each second of LiDAR-GIS calculated
445 road grade. The zero road grade coefficient (PHEM₀) models the test area as totally flat. With the 0.5

446 coefficient (PHEM_{0.5G}), the model uses half of the calculated LiDAR-GIS value at each second. For
447 PHEM_{0.5G} 96.79% of the 1Hz road grade estimates were between $\pm 2\%$ with 99.61% between $\pm 3\%$.
448 For PHEM_G 99.46% of the 1Hz road grade estimates were between $\pm 6\%$ and 94.4% were within the
449 range of $\pm 4\%$. Doubling the road grade at each section with the road grade coefficient of 2 (PHEM_{2G}),
450 76.24% of the 1Hz road grade estimates were between $\pm 6\%$ and 97.46% were within the range of
451 $\pm 10\%$. With a road grade coefficient set to 3 (PHEM_{3G}) 80.93% of the 1Hz road grade estimates were
452 between $\pm 10\%$ and 96.26% were within the range of $\pm 14\%$ Whilst it is likely that in real-world
453 driving the steeper road grades would have an impact on the speed profile of the vehicle, to enable
454 comparison, the modelling in this section of the study assumes the same speed profiles (as measured
455 by the PEMS system) for the vehicle at every road grade coefficient.

456

457 Table 2 details the PHEM modelled CO₂ emission results for the 48 test runs over each lap and
458 section for the 5 road grade scenarios. The average lap CO₂ emission under PHEM₀ is 400 gCO₂/km
459 with a range over the 48 test runs from 276 – 513 gCO₂/km. The average lap CO₂ emission increase
460 by 1.4% when the LiDAR-GIS road grade (PHEM_G) is considered. For PHEM_{2G} the average CO₂
461 emission change over the lap compared to PHEM₀ is 4.0% higher, rising to +7.6% for the PHEM_{3G}
462 scenario. As this test lap starts and ends at approximately the same point, the average lap road grade is
463 zero. This modelling suggests that it is incorrect to assume that over a test route with an average flat
464 road grade but which experiences change in elevation over the length of its profile, that the increase in
465 CO₂ emission in uphill sections will be offset by the decrease in CO₂ emission in downhill sections.
466 The PHEM modelling indicates that for such test routes CO₂ emission increases with increasing
467 steepness of road grade.

468

469 Analysing the PHEM calculations at the section micro-scale suggests that road grade is a very
470 important factor in establishing CO₂ emission over short road sections. Over Section 8, a relatively
471 fast free flowing uphill section (with an average road grade of +1.66% from the LiDAR-GIS elevation
472 profile), the average increase in CO₂ emission from PHEM₀ to PHEM_G is 17.2% with a range in CO₂
473 emission increase for the section of between 8.5% and 43.2%. Over the same section under PHEM_{3G},
474 with a hypothetical tripling of 1Hz road grade, the CO₂ emission increase range is from 32.3% to
475 102.1%. This suggests conducting micro-scale modelling without establishing accurate road grade
476 would cause the CO₂ emission estimates to vary considerably from the real-world CO₂ emission.

477

478 Table 2. PHEM CO₂ Emission Calculation under five road grade scenarios.

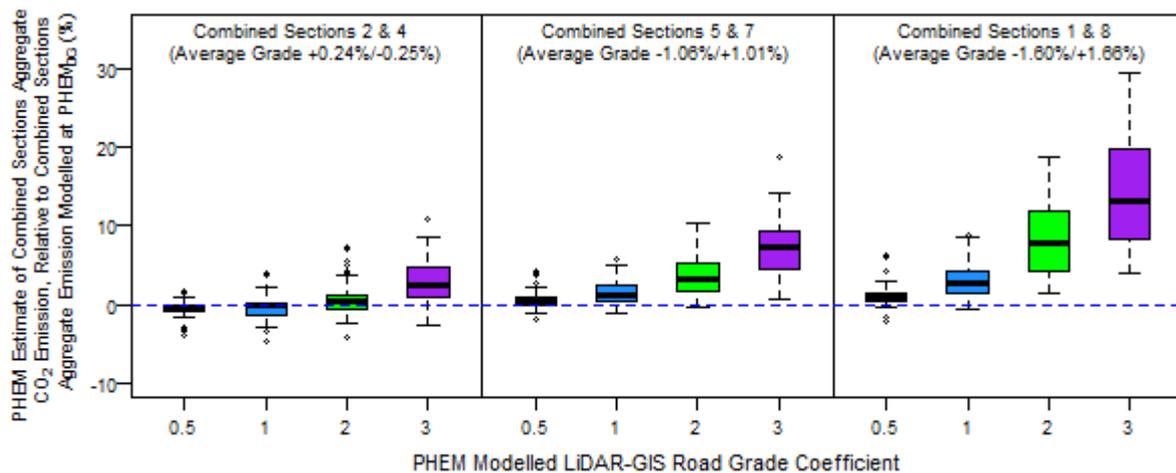
CO ₂ Emission Comparison at Modelled Road Grade Coefficients											
Section #	Ave. Grade (%)	PHEM ₀		PHEM _{0.5G}		PHEM _G		PHEM _{2G}		PHEM _{3G}	
		Ave. (g/km)	Range (g/km)	Ave. (% Change from PHEM ₀)	Range (% Change from PHEM ₀)	Ave. (% Change from PHEM ₀)	Range (% Change from PHEM ₀)	Ave. (% Change from PHEM ₀)	Range (% Change from PHEM ₀)	Ave. (% Change from PHEM ₀)	Range (% Change from PHEM ₀)
1	-1.60	509	210 - 1037	-2.7	-9.3 - 0.3	-4.8	-11.7 - -3.9	-8.0	-17.5 - -3.9	-9.9	-22.2 - -4.5
8	1.66	258	170 - 336	8.5	4.0 - 32.0	17.2	8.5 - 43.2	37.1	18.5 - 67.7	57.1	32.3 - 102.1
2	0.24	274	203 - 503	0.5	-4.7 - 3.7	2.0	-3.8 - 11.0	4.8	-1.7 - 13.9	8.7	1.0 - 17.5
4	-0.25	409	236 - 876	-1.4	-6.3 - 2.7	-2.0	-6.7 - 5.3	-2.3	-7.1 - 7.6	-1.5	-6.7 - 8.3
5	-1.06	434	246 - 1322	-2.4	-7.5 - 1.1	-4.1	-9.7 - 2.3	-7.4	-17.8 - 0.7	-9.1	-20.7 - 3.3
7	1.01	515	257 - 856	3.2	0.9 - 12.9	6.0	2.0 - 17.2	12.1	5.1 - 28.2	20.1	8.3 - 41.0
3	0.06	436	273 - 986	0.7	-1.1 - 2.6	1.7	-0.5 - 6.3	3.9	0.0 - 8.9	7.0	0.5 - 14.3
6	0.11	524	344 - 957	0.4	-3.5 - 3.9	0.9	-3.3 - 2.0	2.4	-2.3 - 6.5	4.4	-0.4 - 9.4
LAP	0.01	400	276 - 513	0.5	-0.8 - 2.3	1.4	-0.3 - 3.9	4.0	1.4 - 8.9	7.6	3.2 - 15.8

479

480 In order to assess how the magnitude of CO₂ emission varies with road grade over a road segment
 481 with two-way traffic flow, the total CO₂ emission over paired sections 1 and 8, 5 and 7, 2 and 4 were
 482 calculated. The total CO₂ emission was calculated over each combined section for each of the 48 test
 483 runs under the five road grade scenarios. As these section pairs cover the same road segment there is
 484 no net change in elevation, so the average grade of each of the combined sections is zero. In Figure 7,
 485 the combined sections aggregate CO₂ emissions for each of the road grade coefficients (0.5, 1, 2 and 3)
 486 are referenced against the aggregate CO₂ emission over the same combined section with PHEM_{0G}. The
 487 results indicate that the higher CO₂ emissions on uphill sections are not offset by the lower emission
 488 rates on downhill sections. The discrepancy over the combined sections tends to rise as the road
 489 grade coefficient applied in the PHEM modelling increases. The magnitude of the increase in
 490 emission is greatest where the average road grades of the two sections of opposing traffic flow are
 491 steepest.

492

493 Figure 7. Percentage Change in the PHEM Aggregate Total CO₂ Emission between PHEM_{0G} and
 494 PHEM_G modelled with each Road Grade Coefficient, over the Combined Sections.



495

496

497 It should be noted that the traffic conditions in the road sections that make up the combined pairs can
498 be quite different for each direction of traffic flow, as traffic control measures and traffic volume can
499 cause different levels of congestion, resulting in a wide range of CO₂ emission values in each section
500 (as illustrated in Figure 4). However the results in Figure 7 present the calculated emission from real-
501 world speed profiles recorded throughout the day, and thus these combined emissions should reflect
502 the likely range of CO₂ emission for the test vehicle on these real-world road segments.

503

504

505 **7. Summary and Conclusions**

506

507 Analysis of the PEMS data revealed a wide spectrum of traffic flow conditions captured by the
508 instrumented vehicle repeatedly driving through the urban traffic network, with measurements taken
509 both during peak rush hour congestion and in free flowing traffic conditions. A wide range of CO₂
510 emission values were recorded (PEMS) over the test lap, ranging from 313 gCO₂/km to 586 gCO₂/km.
511 The measured CO₂ emission values were consistently higher than those predicted by the UK EFT
512 average speed emission curve. The spread of the CO₂ emission values at each speed demonstrates why
513 average speed based emission models may not reliably predict CO₂ emission estimates for short road
514 segments/ sections as they fail to correctly account for acceleration, road grade, drag, rolling
515 resistance and engine speed.

516

517 This study has shown that in order to accurately estimate vehicle CO₂ exhaust emissions at a micro-
518 scale in real-world conditions, a representative road grade profile for each second of the test data is
519 needed. The straightforward and quick LiDAR-GIS method proposed in this study provides a
520 methodology for determining road grade for each second of a vehicle journey, and improved the
521 modelling of CO₂ emission for this PEMS data set. The research demonstrates that using the PHEM
522 instantaneous emission model with LiDAR-GIS calculated road grade is a viable method for
523 generating accurate real-world micro-scale CO₂ emission estimates. The results also show that it is
524 incorrect to assume that the increase in emission on uphill sections will be offset by the decrease in
525 emission on paired downhill sections.

526

527 The research shows that failing to account for even a relatively modest road grade, when modelling
528 micro-scale vehicle emission, could potentially result in highly inaccurate estimates of real-world
529 emission. Transport management and urban planning projects should be incorporating road grade into
530 their analysis where prediction of vehicle emissions is required.

531

532 With the proposal for a PEMS element in Euro 6c type approval from September 2017 (Delphi, 2013)
533 the development of a robust yet practical road grade estimation methodology for PEMS analysis will
534 be very important to assist the analysis of on-road test data and quantify the relationship between
535 power output and exhaust emission. Whilst this research focused on CO₂ emission, it is expected that
536 road grade will have an even greater influence on the emission of other exhaust pollutant such as NO_x
537 where a higher proportion of emissions are related to high power events (Carslaw et al, 2013).

538

539

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541

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546 Measurement and Modelling) Project.

547

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