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## Performance of the cut-cell method of representing orography in idealized simulations<sup>†</sup>

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Abstract

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<sup>†</sup>The creative commons license for this article was changed on 20 November 2013 after original online publication. Several tests of a model with a cut-cell representation of orography are presented: a resting atmosphere test, advection across a hill and a warm rising bubble over hills with different gradients. The tests are compared with results from terrain-following models. Results indicate that errors associated with terrain-following coordinates are reduced, in some cases greatly reduced, with the cut-cell approach. In a resting atmosphere, the cut-cell approach does not generate flow around an isolated hill however steep the terrain. Relative errors in a rising bubble test are an order of magnitude smaller than terrain-following simulations.

Keywords: cut-cell; orography; numerical methods; idealized simulations; high resolution; finite volume

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#### I. Introduction

The underlying surface topography has a significant effect on the local and in some cases synoptic weather patterns. Mountain ranges can cause severe downslope winds and impact local rain patterns (McIlveen, 1992). Terrain also exerts low-level and gravity wave drag on the atmosphere that influences the global circulations. Correctly representing this drag is essential for getting the large scale circulations right (McFarlane, 1987). To enable accurate forecasts, it is important for numerical weather prediction (NWP) models to accurately represent the terrain and lower boundary.

The majority of NWP models use terrain-following coordinates, where the vertical levels follow the shape of the underlying terrain near the model-bottom, smoothly reverting to horizontal surfaces by the model-top. The traditional, and most commonly used, methods reduce the influence of the terrain linearly with height (or pressure), removing it completely only by the uppermost level [basic terrain-following, BTF, of Gal-Chen and Somerville (1975)] or some level below the model-top [hybrid terrain-following, HTF, of Simmons and Burridge (1981)]. As the coordinate surfaces are not horizontal, errors occur in the calculation of the discrete horizontal pressure gradient giving rise to spurious winds in the vicinity of orography (Janjic, 1989). Horizontal diffusion errors also occur in mountainous regions (Zängl, 2002). Recent work has demonstrated that such errors can be reduced by using more sophisticated methods to reduce the terrain influence more rapidly with height [SLEVE of Schär et al. (2002) and Leuenberger et al. (2010); and STF of Klemp (2011)] and by modifying the computation of the horizontal pressure gradient term itself (Klemp,

2011; Zängl, 2012). Terrain-following coordinates have the advantage of easy implementation because there is a one-to-one transformation between grid cells in the regular computational grid for the cases with and without orography. Moreover, it is also easy to implement a variable vertical resolution that is fine close to the surface, where small-scale physical processes are important, and coarser further aloft.

As computing power continues to increase, models move towards higher and higher resolutions. Consequently, steeper and more complex features in the terrain can be resolved by the model grid, placing greater demands on the terrain-following methods. The alternative approach of representing terrain within a Cartesian grid is being explored. These methods retain horizontal vertical grid levels throughout the depth of the model, enabling a more accurate calculation of the horizontal pressure gradient term. The step-coordinate model (Mesinger et al., 1988) approximates the presence of terrain by removing entire grid cells from the computational domain producing a block-shaped mountain. However, Gallus and Klemp (2000) showed that this method fails to accurately simulate flows, generating spurious vorticity at the step corners.

The 'cut-cell' (or 'shaved cell') method extends the step-coordinate approach by using piecewise continuous sections that lie within the regular grid, thereby permitting some grid cells to be cut by the terrain surface. Accuracy and stability have been demonstrated for moderate and very steep gradients for two-dimensional (2D) and 3D hills (Adcroft *et al.*, 1997; Bonaventura, 2000; Steppeler *et al.*, 2002; Yamazaki and Satomura, 2008, 2010; Lock et al., 2012).

The cut-cells vary in size depending on the orography and approaches have been proposed to handle

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the severe stability constraints that are possible due to the presence of very small cut-cells. The thin-wall approximation (Steppeler *et al.*, 2002, 2006) artificially inflates the volumes of the cut-cells to match those of the uncut-cells, enabling the use of a timestep similar to that of the equivalent terrain-following model. Their results exhibited no indication of the spurious vorticity of the step-coordinate and showed improved skill scores for precipitation and temperature in 39 1-day forecasts from real data. Subsequent analysis of a 5-day hindcast over the Himalaya region exhibited improvements in the temperature field and precipitation field (Steppeler *et al.*, 2011, 2013).

Klein *et al.* (2009) developed a 2D cut-cell model using directional operator splitting and the wellbalancing strategy described in Botta *et al.* (2004) to reduce the stability constraints from small cells, showing simulations of flow over hills and bubbles interacting with a zeppelin.

Yamazaki and Satomura (2010) implemented a cellcombining technique whereby small cells near the surface are combined either horizontally or vertically with neighbouring cells to reduce the restriction on the time-step. They demonstrated that the length of timestep permitted by combining cells could increase by as much as a factor of 10, and that the method produced more accurate results than a terrain-following model for flow over a semi-circular hill. Yamazaki and Satomura (2012) also successfully implemented the cut-cell technique in a block structured grid which enabled a higher resolution near the surface.

Jebens *et al.* (2011) demonstrated a partially implicit method to avoid the time-step constraints by solving all computations in the cut-cells with a fully implicit solver and reverting to a more common semi-implicit approach in the regular grid cells.

This paper presents further examples and discussions of the reduction in errors that are achieved in simulations of flows near orography by use of the cutcell method from Lock *et al.* (2012) relative to terrainfollowing models. These simulations demonstrate the ability of the cut-cell technique in a wider variety of test cases than previously seen and allow a comparison with a terrain-following approach. The models used are outlined in Section 2. Section 3 describes the set-up and results from simulations of a resting atmosphere, advection and rising bubble tests and Section 4 summarizes the conclusions of these tests.

#### 2. Model

The model (Cut-cell) used for the cut-cell tests, described in detail in Lock *et al.* (2012), is a non-hydrostatic 3D model that was designed for high-resolution microscale studies. The dry equations are in advective form and they predict potential temperature, velocity and the Exner function of pressure. The time-stepping scheme is a split-explicit scheme with Robert-Asselin filtered leapfrog used on the longer

time-step and a forward-backward scheme used on the short step (Klemp and Wilhelmson, 1978). For the spatial differencing, a centred Piacsek-Williams scheme that is second-order accurate is combined with a Charney-Phillips and Arakawa C grid. The orography is represented by piecewise continuous bilinear sections that intersect the grid. This produces three different types of cells: those cells completely below the boundary which are ignored, those completely above the boundary which are treated as normal and those cut by the boundary which are treated using a finite volume approach. For more details see Lock (2008) and Lock *et al.* (2012).

#### 3. Tests

A number of 2D idealized tests commonly used for atmospheric dynamics have been conducted to further demonstrate the benefits of the cut-cell method relative to the terrain-following approach. The Cut-cell model is run in 2D by reducing the number of cells in the y direction to 10 and setting up the test cases so that there is no variation in the y direction.

#### 3.1. Resting atmosphere

In Klemp (2011), model simulations of a resting atmosphere demonstrated the relative errors associated with various terrain-following coordinates, which arise from grid-induced errors in the calculation of the horizontal pressure gradient and diffusion terms. The terrain-following coordinates considered by Klemp (2011) include the BTF of Gal-Chen and Somerville (1975), the HTF of Simmons and Burridge (1981), the SLEVE of Schär et al. (2002) and the STF of Klemp (2011). Each coordinate distorts the vertical grid differently for the coordinate surfaces, see Figure 1 in Klemp (2011). By retaining a Cartesian grid in the cut-cell model, these errors should not occur and the model should be able to accurately simulate an atmosphere at rest. To test the accuracy of the Cutcell model, it was initialized to simulate the resting atmosphere of Klemp, 2011.

The periodic domain was set at 200 km wide and 20 km high with a uniform grid spacing of 500 m. At the bottom of the domain in the centre there is a range of hills with height

 $h(x) = h^*(x) \cos\left(\frac{\pi x}{\lambda}\right)$ 

where

$$h^*(x) = \begin{pmatrix} h_0 \cos^2\left(\frac{\pi x}{2a}\right) & |x| \le a\\ 0 & |x| > a \end{cases}$$

and  $h_0 = 1000$  m is the maximum height, a = 5000 m is the half width and  $\lambda = 4000$  m is the wavelength of small perturbations. As highlighted in Klemp (2011), errors in simulating a resting atmosphere occur for terrain-following coordinates due to the horizontal

(1)

**Figure 1.** Results from the Cut-cell model for the advection test. Contours indicate the tracer bubble concentration according to the colour bar with intervals of 0.1 and ranging from -0.2 to 1. The position of the bubble is indicated at three times 0, 5000 and 10 000 s after the introduction of the bubble on the left. The domain shown is 150 km wide and 15 km high centred on the orography which is indicated by the blue line at the base. The vectors down the left show the wind profile, large vectors have a magnitude of  $10 \text{ m s}^{-1}$ .

pressure gradient calculation. The errors can be vanishingly small for nearly linear vertical pressure gradients. By introducing an inversion layer, the nearby vertical pressure gradients become very non-linear, causing small errors in the horizontal pressure gradient calculation which induce spurious motion. To highlight these errors, an inversion is included in this test. The background potential temperature profile is a constant 300 K. The potential temperature perturbations are non-zero such that the full potential temperature profile varies with the Brunt–Väisäla frequency (*N*) and has an inversion between 2 and 3 km. Below 2 km and above 3 km  $N = 0.1 \text{ s}^{-1}$  whereas between 2 and 3 km  $N = 0.2 \text{ s}^{-1}$ . The initial wind field is set to zero and the simulation is run out to 5 h with a time-step of 1.01 s.

After 5 h the maximum vertical velocity in the cutcell experiment is  $10^{-12} \text{ m s}^{-1} \approx 0 \text{ m s}^{-1}$  to machine accuracy and the horizontal velocities are identically zero. By comparison, for terrain-following models Klemp (2011) reports a maximum velocity of 1 m s<sup>-1</sup> for the basic terrain-following methods (BTF/HTF) and 0.1 m s<sup>-1</sup> for the more sophisticated methods (STF/SLEVE).

Increasing the height of the hill up to at least 4000 m does not change this result for the Cut-cell model. This confirms that a correctly implemented cut-cell model does not suffer the spuriously generated winds associated with terrain-following models.

#### 3.2. Advection test

Schär *et al.* (2002) demonstrated errors due to terrainfollowing coordinates with a simple advection test. This test is reproduced here with the cut-cell model.

A bubble of tracer is blown across a mountain range with a wind profile that is zero below the mountain tops and constant above 5 km is described by

$$u(z) = \begin{pmatrix} u_0 & z_2 \le z \\ u_0 \sin^2\left(\frac{\pi}{2} \frac{z - z_1}{z_2 - z_1}\right) & z_1 \le z \le z_2 \\ 0 & z \le z_1 \end{cases}$$

where  $u_0 = 10 \text{ m s}^{-1}$ ,  $z_1 = 4 \text{ km}$  and  $z_2 = 5 \text{ km}$ , see Figure 1. The initial tracer concentration is described by

$$q(x,z) = \begin{pmatrix} \cos^2\left(\frac{\pi r}{2}\right) & r \le 1\\ 0 & \text{otherwise} \end{cases}$$
(2)

where

$$r = \left[ \left( \frac{x - x_0}{A_x} \right)^2 + \left( \frac{z - z_0}{A_z} \right)^2 \right]^{\frac{1}{2}}$$

and  $A_z = 3 \text{ km}$  is the vertical radius,  $A_x = 25 \text{ km}$  is the horizontal radius and the bubble is centred at  $x_0 = 100 \text{ km}$ ,  $z_0 = 9 \text{ km}$ . The domain is 300 km wide and 25 km high with a horizontal grid spacing of 1000 m and a vertical grid spacing of 500 m. In the centre of the bottom boundary is a sinusoidal mountain range described by Equation 1 from the resting atmosphere test with  $h_0 = 3 \text{ km}$ , a = 25 km and  $\gamma = 8 \text{ km}$ . The atmosphere is neutrally stratified with a constant potential temperature of 300 K and the model is run for 10 000 s so that the bubble passes once across the mountain range.

The results from the cut-cell model are shown in Figure 1. Results have been compared (though not shown) to the same run with no orography. The differences between the two simulated bubbles were exactly zero confirming that any observed differences along the trajectory are due to the advection scheme and not the representation of terrain. Furthermore, moving the bubble closer to the top of the mountains does not change the results suggesting there is no undue influence from the terrain on the flow aloft.

Schär *et al.* (2002, Figure 6) demonstrate that the basic terrain-following coordinates induce disturbances which visibly distort the bubble downstream of the mountain range. By removing the terrain influence more rapidly with height, the SLEVE coordinate exhibits much improved results (Schaer *et al.* (2002) Figure 6c,d), similar to those described here. Regayre *et al.* (2013) shows that bringing the tracer bubble closer to the hill affects the evolution of the bubble downstream of the mountain range when terrainfollowing methods are used.

#### 3.3. Rising bubble

The resting atmosphere and advection tests demonstrate errors in the flow aloft from the terrain-following models. A commonly used test for numerics is the rising bubble test of, for example, Bryan and Fritsch (2002). This test is repeated here with the Cut-cell model. Hills with varying gradients are placed beneath the bubbles to examine the effect of the surface gradients on the evolution aloft. In addition, the experiments are repeated with the UK Met Office terrain-following research model, BLASIUS (Wood., 1992; Wood and Mason, 1993). BLASIUS has been used extensively for idealised studies of 2D and 3D boundary-layer

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flows over small hills. The model solves the timedependent Boussinesq equations in a BTF (Gal-Chen and Somerville, 1975) terrain-following coordinate system and utilises a finite-difference discretisation and an explicit time integration scheme. For these simulations a centred-difference advection scheme was used and the turbulence closure scheme was turned off to keep the numerics as similar to the Cut-cell model as possible.

The Cut-cell model and BLASIUS were both set up with a no-slip condition imposed at the lower boundary, periodic lateral boundary conditions and a rigid-lid upper boundary condition. A round, warm potential temperature perturbation with a Gaussian profile is initialized in the centre of a domain 20 km wide and 20 km high, with a uniform grid spacing of 100 m. The bubble is described by

$$\theta'(x,z) = \begin{pmatrix} \cos^2\left(\frac{\pi r}{2}\right) & r \le 1\\ 0 & \text{otherwise} \end{cases}$$
(3)

where

$$r = \left[ \left( \frac{x - x_0}{A_x} \right)^2 + \left( \frac{z - z_0}{A_z} \right)^2 \right]^{\frac{1}{2}}$$

and  $A_z = 2 \text{ km}$  is the vertical radius,  $A_x = 2 \text{ km}$  is the horizontal radius and the bubble is centred at  $x_0 = 10 \text{ km}, z_0 = 4.5 \text{ km}.$ 

The atmosphere is neutrally stable with a background potential temperature of 300 K and the model is run out to 1000 s. Several runs are completed with the cut-cell model with different terrain at the lower boundary and repeated with the terrain-following model BLASIUS. Figure 2 shows the evolution of the bubble in the no-hill case with a flat lower boundary for both the Cut-cell model and BLASIUS. These are similar to the bubble produced by Bryan and Fritsch (2002) and are used as a reference in the discussion below.

Three different runs are made each with a bellshaped hill described by

$$h(x) = \frac{h_0}{\left(1 + \frac{x^2}{a^2}\right)}$$
(4)

with a maximum height (h0) of 1,000 m and three different half widths (a) of 3,000 m, 2,000 m and 1,000 m. The key difference between these hills is the gradient of their slopes which increases as the width decreases indicated by the aspect ratio (h0/a) increasing from 1/3 to 1/2 to 1. As indicated by the wind vectors in Figure 2, the winds are not strong below 1,100 m: for both models, the maximum wind speed below 1,100 m remains more than an order of magnitude smaller than the maximum further aloft, at all times throughout the simulation, and for all hills. Therefore, as the hill is far beneath the bubble, where the winds are not strong, the different hills should not significantly impact the evolution of the bubble.

The Cut-cell model uses a time-step of  $10^{-3}$  s due to the restrictions on the CFL condition because of the small cut-cells at the boundary. BLASIUS uses a variable time-step dependent on the CFL condition of about 1.3 s. Tests have been run with BLASIUS for smaller fixed time-steps of 0.1 s and 0.01 s for the steepest hill (not shown) and no significant differences in the results were observed. Therefore we are confident that the results for the terrain-following model are not strongly dependent on the time-step.

For both models the result from each hill is subtracted from the respective no hill case and the differences are plotted in Figure 3. For the Cut-cell



**Figure 2.** Potential temperature perturbations for the warm bubble after 1000 s from the Cut-cell model (a) and BLASIUS (b). The contour interval is 0.1 K. The vectors indicate the wind velocity. The maximum vertical velocity in (a) is 15.61 m s<sup>-1</sup> and in (b) is 17.17 m s<sup>-1</sup>



**Figure 3.** Potential temperature difference plots at time t = 1000 s. Differences are between the warm rising bubble with no hill and 1000 m high hills of different half-widths. For (a) and (d) a = 3 km, for (b) and (e) a = 2 km and for (c) and (f) a = 1 km wide. Panels (a-c) are from the cut-cell model and panels (d-f) are from the terrain-following model, BLASIUS. Differences are in K the contour interval is 0.1 K ranging from -1.2 to 1.7 K. The maximum absolute potential difference is given beneath each subfigure, along with the maximum vertical velocity.

model the difference is a straightforward subtraction. However as the computational grid is different for each hill with BLASIUS the results are first interpolated linearly onto a regular grid before subtracting. The errors of this interpolation are of the order  $10^{-3}$  K, 3 orders of magnitude smaller than the differences plotted in Figure 3 and therefore do not significantly contribute to the results.

The differences with the cut-cell model are an order of magnitude smaller than the differences with the terrain-following model and do not increase as  $h_0/a$  increases from 1/3 to 1. The differences in the BLASIUS plots on the other hand increase as the aspect ratio increases, from a max of 0.70 K when the ratio is 1/3 to a max of 1.67 K when it is 1. The increase in differences from BLASIUS as  $h_0/a$ increases indicates a worsening in the solution as the computational grid becomes increasingly deformed and for steeper hills, with aspect ratios greater than 1, BLASIUS no longer converges to a solution. This problem is not encountered with the Cut-cell model, whose computational grid away from the lower boundary is not affected by the presence of orography. The Cut-cell model has been successfully run with hills having aspect ratios up to 10. Though not shown,

the results remain consistent with those presented here, showing little change in the magnitude of the differences from the no-hill case.

#### 4. Conclusions

A number of numerical experiments from the literature have been repeated with a model using cut-cells to represent orography, in order to demonstrate its performance relative to terrain-following methods. The tests demonstrate that the Cut-cell model can accurately simulate a resting atmosphere, not exhibiting gridinduced winds commonly seen with terrain-following methods. A simulation of a tracer bubble advected above the top of the mountains demonstrates that, unlike for terrain-following models, solutions from the cut-cell model do not exhibit errors aloft induced by the underlying terrain. The rising bubble tests demonstrate that the Cut-cell model is better at handling steep gradients than the basic terrain-following method. Differences due to the effect of the underlying terrain do not erroneously increase as the aspect ratio increases in contrast to a terrain-following model. All these tests demonstrate that by avoiding any distortion of the

computational grid away from the terrain, the cut-cell method reduces errors in the flow aloft compared to terrain-following methods. Furthermore, results from the rising bubble test with very steep orography (aspect ratio of 10) demonstrate that the Cut-cell model is stable, without compromising accuracy. This is important for large scale models and in representing features such as wave propagation.

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