UNIVERSITY of York

This is a repository copy of Many-body GW calculations of ground-state properties: Quasi-2D electron systems and van der Waals forces.

White Rose Research Online URL for this paper: <u>https://eprints.whiterose.ac.uk/4014/</u>

Article:

Garcia-Gonzalez, P and Godby, R W orcid.org/0000-0002-1012-4176 (2002) Many-body GW calculations of ground-state properties: Quasi-2D electron systems and van der Waals forces. Physical Review Letters. 056406. -. ISSN 1079-7114

https://doi.org/10.1103/PhysRevLett.88.056406

Reuse

Items deposited in White Rose Research Online are protected by copyright, with all rights reserved unless indicated otherwise. They may be downloaded and/or printed for private study, or other acts as permitted by national copyright laws. The publisher or other rights holders may allow further reproduction and re-use of the full text version. This is indicated by the licence information on the White Rose Research Online record for the item.

Takedown

If you consider content in White Rose Research Online to be in breach of UK law, please notify us by emailing eprints@whiterose.ac.uk including the URL of the record and the reason for the withdrawal request.



eprints@whiterose.ac.uk https://eprints.whiterose.ac.uk/ promoting access to White Rose research papers



Universities of Leeds, Sheffield and York http://eprints.whiterose.ac.uk/

White Rose Research Online URL for this paper: http://eprints.whiterose.ac.uk/4014/

Published paper

Garcia-González, P. and Godby, R.W. (2002) *Many-body GW calculations of ground-state properties: quasi-2D electron systems and van der Waals forces.* Physical Review Letters, 88 (5). Art. No. 056406.

White Rose Research Online eprints@whiterose.ac.uk

Many-body GW Calculations of Ground-State Properties: Quasi-2D Electron Systems and van der Waals Forces

P. García-González¹ and R. W. $Godby^2$

¹Departamento de Física Fundamental, Universidad Nacional de Educación a Distancia,

Apartado 60141, 28080 Madrid, Spain

²Department of Physics, University of York, Heslington, York YO10 5DD, United Kingdom

(February 1, 2008)

We present GW many-body results for ground-state properties of two simple but very distinct families of inhomogenous systems in which traditional implementations of density-functional theory (DFT) fail drastically. The GW approach gives notably better results than the well-known randomphase approximation, at a similar computational cost. These results establish GW as an superior alternative to standard DFT schemes without the expensive numerical effort required by quantum Monte Carlo simulations.

71.15.Nc,71.15.Mb,71.45.Gm

Ab initio many-body-theory (MBT) methods, particularly those based on Hedin's GW approximation [1], have been used extensively during the last decade to calculate excited-state properties of electron systems in solid-state physics [2]. In addition, there is a recent and increasing interest in the application of such methods to obtain ground-state properties [3–10]. In MBT, electronelectron correlations are taken into account directly without resorting to the mean-field density-based approximations used in routine implementations of Density Functional Theory (DFT) [11], thus providing a more microscopic description of the interacting many-electron problem.

Modern MBT calculations use efficient algorithms for the evaluation of MBT quantities [such as the dielectric function $\hat{\epsilon}(\omega)$, the self-energy operator $\hat{\Sigma}(\omega)$, and the one-particle Green function $\hat{G}(\omega)$] required in the study of excited-state properties of real materials [12,13]. The application of these techniques to the calculation of ground-state properties, such as the density or the total energy, opens the appealing possibility of treating all the electronic properties in the same fashion. Although more expensive than DFT, these MBT methods do not require the demanding computational effort of quantum Monte Carlo simulations [14]. Nonetheless, ground-state calculations based on MBT must be painstakingly assessed. First, approximations that have proved successful for spectral properties might not necessarily be good methods for structural properties. Second, the energies and lifetimes of quasiparticles are mainly determined by the pole structure of $\hat{G}(\omega)$, while ground-state properties emerge from a multidimensional integration of $\hat{G}(\omega)$. As a consequence, features that can be safely ignored in the determination of quasiparticle properties, like the high-frequency behavior or high-energy-transfer matrix elements, play an important role if we want to calculate, for instance, the ground-state energy. The development of general-purpose procedures requires a careful study of the optimal treatment of these points.

In this Letter we present nonselfconsistent (in the sense described below) GW calculations for the ground-state properties of two families of simple inhomogeneous systems: the quasi-two-dimensional (2D) electron gas and a pair of interacting jellium slabs. These provide a suitable test cases for an extensive assessment of the performance of GW-MBT ground-state calculations. First, despite the simplicity of these systems, LDA and GGA fail to describe them properly. For the quasi-2D gas, the high inhomogeneity of the density profile along the confining direction is clearly beyond the scope of local or semilocal approaches [15]. The situation is quite different if we consider interacting jellium slabs. In the limit of large separation, in which the densities of each subsystem do not overlap, dispersion or van der Waals (vdW) forces are evident. These forces are due to long-ranged Coulomb correlations and, hence, cannot be described at all by the LDA or GGA [4,16]. As shown below, even nonlocal DFT prescriptions for the XC energy, such as the weighted density approximation (WDA) [17], are unable to reproduce such forces. On the other hand, these systems exhibit translational invariance along the xy plane, thus reducing significantly the number of independent variables needed to describe the spatial dependence of all the operators, assisting the production of the highlyconverged test calculations required here.

In Hedin's GW framework, the self-energy $\hat{\Sigma}$ of a system of N electrons under an external potential v_{ext} (**r**) is approximated by

$$\Sigma(1,2) = iG(1,2^+) W(1,2), \qquad (1)$$

where the labels 1 and 2 symbolize space-time coordinates. \hat{W} is the screened Coulomb potential, which is exactly related to the bare Coulomb potential \hat{w} and the polarizability \hat{P} by $\hat{W}(\omega) = \hat{w} + \hat{w}\hat{P}(\omega)\hat{W}(\omega) =$ $\hat{\epsilon}^{-1}(\omega)\hat{w}$ (the usual matrix operations are implied). Under the *GW* approach, the polarizability is given by $P(1,2) = -2iG(1,2)G(2,1^+)$. Finally, $\hat{\Sigma}$ and \hat{G} are linked through the Dyson equation $\hat{G}^{-1}(\omega) = \omega - [\hat{t} +$ $\hat{v}_{\rm el} + \hat{\Sigma}(\omega)$], with \hat{t} the one-electron kinetic energy, and $v_{\rm el}(\mathbf{r})$ the classical electrostatic potential [the sum of $v_{\rm ext}(\mathbf{r})$ and the Hartree interaction potential]. This set of equations defines a selfconsistent problem, but routine GW calculations concerned with the quasiparticle properties do not attempt selfconsistency: when evaluating $\hat{\Sigma}$, the interacting Green function \hat{G} is generally substituted by that corresponding to the noninteracting Kohn-Sham (KS) system under the LDA (or GGA) approximation.

It is well known that full selfconsistency implies a worsening of the description of spectral properties [18]. However, for the 3D [5,10] and 2D [10] homogeneous electron gases, the total energy arising from \hat{G} by using the Galitskii-Migdal formula of MBT [19] fits the (essentially exact) QMC values extremely well if \hat{G} is obtained selfconsistently. Nonetheless, at the nonselfconsistent level (which we will call G_0W_0) the exact exchange energy is already built in and, at the same time, correlation effects beyond the random-phase approximation (RPA) are taken into account, as reflected in good total energies and very good total energy differences [5,10] for these homogeneous systems. Since the relevant quantity for structural properties is the total energy difference, $G_0 W_0$ (and even, in some cases, RPA [20]) is likely to fulfill a useful role. The known particle-number violation under the $G_0 W_0$ approximation [21], while non-zero, is so small that it can be ignored in practical applications [22].

All the calculations reported in this Letter are done as follows. First, we perform a standard LDA-KS calculation, in which, owing to the translational invariance along the xy plane, the KS orbitals are organized into subbands. That is, each KS state is given by $\phi_{n\mathbf{k}}(\mathbf{r}) =$ $\psi_n(z) e^{i\mathbf{k}\cdot\boldsymbol{\rho}}/\sqrt{2\pi}$, where $\mathbf{k} = (k_x, k_y)$ and $\boldsymbol{\rho} = (x, y)$ denote the two-dimensional momentum and position in the xy-plane. Then, the noninteracting polarizability $P_0(1, 2) = -2iG_0(1, 2)G_0(2, 1^+)$ is calculated at imaginary frequencies using the expression

$$P_0(z, z', k; i\omega) = \sum_{n=1}^{N_{occ}} \sum_{m=1}^{\infty} S_{nmk}(i\omega) \gamma_{nm}(z) \gamma_{nm}(z') \quad (2)$$

Here, N_{occ} is the number of occupied KS subbands, $\gamma_{nm}(z) = \psi_n(z) \psi_m(z)$, and the coefficients $S_{nmk}(i\omega)$ admit a fully analytical expression [9,23]. $P_0(i\omega)$ could be also calculated fully numerically [13] but due to the high symmetry of the system, the present method is more efficient. The infinite sum in Eq. 2 is truncated at a certain value N_{B} , which acts as a convergence parameter.

The next step is the inversion of the RPA dielectric function $\hat{\epsilon}_0(i\omega) = \hat{1} - \hat{w}\hat{P}_0(i\omega)$ and the evaluation of $\hat{W}_0(i\omega) = \hat{\epsilon}_0^{-1}(i\omega)\hat{w}$. This can be done in a double cosine basis representation [9,22], but the high inhomogeneity of the systems along the z direction suggests a different method based on Ref. [12]. Note that the polarizability spans a Hilbert space made up by the product states γ_{nm} . Obviously, the set { γ_{nm} } has a large number of linear dependences which can be eliminated using a standard Gramm-Schmidt procedure, so obtaining an optimized basis set $\mathcal{B}_{op} = \{\zeta_{\alpha}(z)\}$. In all the cases here studied, $N_{\rm op} = N_{\rm B} + N_{\rm occ} - 1 \zeta$ -functions ensure an almost perfect representation (with a relative error less than 10^{-4}) of all the product states γ_{nm} . Hence, $P_0(z, z', k; i\omega) = \sum_{\alpha, \beta} \zeta_{\alpha}(z) P_0(k, i\omega)_{\alpha\beta} \zeta_{\beta}(z')$, where the matrix elements $P_0(k, i\omega)_{\alpha\beta}$ can be immediately obtained from S_{nmk} and the scalar products $\langle \gamma_{nm}, \zeta_{\alpha} \rangle$. Then, we calculate the representation $w(k)_{\alpha\beta}$ of the bare Coulomb potential, and the matrix elements $W(k, i\omega)_{\alpha\beta}$ of the screened Coulomb potential are easily obtained by a matrix inversion for each value of k. Well converged results are typically obtained with $N_{\rm B} \simeq 80$ subbands, although for quasi-2D systems $N_{\rm B}$ is significantly less. RPA correlation energies, where required, can be straightforwardly obtained in this representation.

The real-space representation of W_0 is given by the expansion

$$W_{0}(z, z', ; i\tau) = i \sum_{\alpha, \beta, \mathbf{k}} \int \frac{d\omega}{2\pi} e^{i(\omega\tau + \mathbf{k} \cdot \boldsymbol{\rho})} \\ \times \zeta_{\alpha}(z) \zeta_{\beta}(z') W(k, i\omega)_{\alpha\beta} ,$$

where $\sum_{\mathbf{k}} = (2\pi)^{-2} \int d\mathbf{k}$, whereas the KS Green function $G_0(z, z', \rho; i\tau)$ is calculated directly from the KS eigenstates [13]. By using (1) we readily get the self-energy operator in real space and imaginary time and, eventually, its representation $\Sigma (k, i\tau)_{nm}$ in the KS basis set. We use typically 100 (or fewer) τ/ω points in a Gauss-Legendre grid with $\omega_{\max} \simeq 80\Delta_c$ (Δ_c is the width of the conduction band), and 100-150 ρ/k points with $k_{\max}^2/2 \simeq \omega_{\max}$. It is important to emphasize that the asymptotic time and frequency tails of all the operators must be treated analytically to ensure smooth and rapid convergence.

In the imaginary-time/frequency representation $\hat{\Sigma}(\mu + i\omega) = -i \int d\tau \hat{\Sigma}(i\tau) e^{-i\omega\tau}$, with μ the interacting chemical potential. Hence, the Green function at imaginary frequencies is the solution of the Dyson equation

$$\hat{G}^{-1}(\mu + i\omega) = \mu + i\omega - \left[\hat{h}_{KS} + \hat{\Sigma}(\mu + i\omega) - \hat{v}_{XC}\right]$$
(3)

with $h_{\rm KS} = \hat{t} + \hat{v}_{\rm S}$ the KS-LDA hamiltonian and $v_{\rm XC}(\mathbf{r})$ the LDA-XC potential. \hat{G} is calculated in the KS representation $G(k, i\omega)_{nm}$, with μ previously obtained by diagonalizing the quasiparticle hamiltonian at $i\omega = 0$, $\hat{h}_{\rm QP}(\mu) = \hat{h}_{\rm KS} + \hat{\Sigma}(\mu) - \hat{v}_{\rm XC}$, and by imposing that the volume enclosed by the interacting Fermi surface equals the KS value. A small term $\delta v(\mathbf{r})$, accounting for the change in the Hartree potential due to the differences between the $G_0 W_0$ and LDA densities, should be included into (3) and $\hat{h}_{\rm QP}$. However, this term induces an imperceptible change in the shape of \hat{G} , and it has a negligible influence on the ground-state properties.

The electron density and energy are given, respectively, by $n(\mathbf{r}) = \pi^{-1} \oint d\omega G(\mathbf{r}, \mathbf{r}; i\omega)$ and $E = E_{el} + E_{el}$

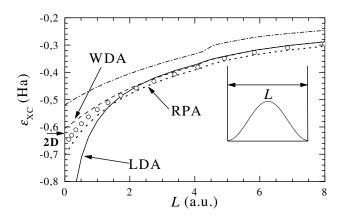


FIG. 1. XC energy per particle for thin confined jellium slabs of fixed 2D density $n^{2D} = 3/4\pi$ as a function of their thickness *L*. Lines: LDA, WDA, and RPA; circles: G_0W_0 . The exchange energy (dash-dotted line) has been included as a reference. Note the effect due to the filling of a second subband at $L \simeq 4.2a_0$, which is especially evident in ε_X . The arrow indicates the QMC value for the 2D limit.

 $\pi^{-1} \operatorname{tr} \oint d\omega [\hat{t} + \frac{1}{2}\hat{\Sigma}(i\omega)]\hat{G}(i\omega)$, where E_{el} is the classical electrostatic energy [which can be obtained from $n(\mathbf{r})$], and tr symbols the spatial trace. Owing to the symmetry of our model systems (the generalization to arbitrary geometries is straightforward), we can write $n(z) = n_0(z) + \delta n(z) = n_0(z) + \sum_{n,\mathbf{k}} |\psi_n(z)|^2 \delta f_{nk}$, $n_0(z)$ being the LDA density, and

$$\delta f_{nk} = \int \frac{d\omega}{\pi} \left[G\left(k, \mu + \mathrm{i}\omega\right)_{nn} - G_0\left(k, \mu_0 + \mathrm{i}\omega\right)_{nn} \right] , \quad (4)$$

 $(\mu_0 \text{ is the LDA chemical potential}).$ On the other hand, the exchange energy per surface unit is given directly by $E_{\rm X}/S = \frac{1}{2} \sum_{n,\mathbf{k}} f_{nk} \Sigma_{\rm X} (k)_{nn}$, where $\hat{\Sigma}_{\rm X}$ is the frequency-independent part of the self-energy $\Sigma_{\rm X} (\mathbf{r}_1, \mathbf{r}_2) = \operatorname{ilim}_{\tau \to 0^+} G_0 (\mathbf{r}_1, \mathbf{r}_2; i\tau) w (r_{12})$ (i.e., the Fock operator). Finally, the correlation energy $E_{\rm C}$ is written as the sum of its kinetic-energy and electrostatic parts:

$$\frac{T_{\rm C}}{S} = \sum_{n,\mathbf{k}} \varepsilon_{nk} \delta f_{nk} - \int dz v_{\rm S}(z) \,\delta n(z) \tag{5}$$

$$\frac{W_{\rm C}}{S} = \sum_{n,\mathbf{k}} \left[\frac{1}{2} \Sigma_{\rm X} \left(k \right)_{nn} \delta f_{nk} + \sum_{m} \int \frac{d\omega}{\pi} \Sigma_{\rm C} \left(k, \mu + i\omega \right)_{nm} G \left(k, \mu + i\omega \right)_{mn} \right]$$
(6)

where we have included the frequency-dependent part of the self-energy $\hat{\Sigma}_{\rm C}(i\omega) = \hat{\Sigma}(i\omega) - \hat{\Sigma}_{\rm X}$. As usual, we suppose that the total electrostatic energy is given correctly by the LDA, since we have checked carefully that the density variation $\delta n(z)$ causes only minor changes in the electronic energy. We also note that when evaluating $E_{\rm C}$ we do not need all the matrix elements of $\hat{\Sigma}$ and \hat{G} . In general, full convergence is achieved by performing the sum only over LDA states such that $\varepsilon_{n\mathbf{k}} \lesssim 6\Delta_c$, and this also applies to the resolution of Dyson's equation. Therefore, the most demanding part of the calculation is the evaluation of $\hat{\epsilon}^{-1}(i\omega)$ which, in any case, is required to obtain the RPA correlation energy.

To mimic a quasi-2D electron system, we have taken a thin jellium slab with a background density \overline{n} = $(\frac{4}{2}\pi r_s^3)^{-1}$ and width L. This slab is bounded by two infinite planar walls, and overall charge neutrality is assumed. We keep the number of particles per unit surface area $n_{2D} = \overline{n}L$ constant, in such a way that the limit $L \rightarrow 0$ corresponds to a 2D homogeneous electron gas (HEG) with density n_{2D} . In Fig. 1 we plot, for several values of L, the XC energy per particle $\varepsilon_{\rm XC}$ given by the LDA, the nonlocal WDA, the RPA, and the G_0W_0 method. As commented previously, the LDA diverges when approaching the 2D limit, whereas the WDA behaves reasonably well, slightly underestimating the absolute value of $\varepsilon_{\rm XC}$ in the strict 2D limit. The RPA does not show any pathological behaviour, but it overestimates $|\varepsilon_{\rm XC}|$ by more than 20 mHa/e⁻ for all configurations. Finally, $G_0 W_0$, whose superiority to the RPA has already been established in the 3D limit, [5,10] retains this in the transition to the 2D limit. Its performance is similar to that of the WDA for these systems (although the residual error for the 2D gas has the opposite sign). It is important to point out that the RPA and $G_0 W_0$ XC energies obtained by starting from a WDA-KS calculation are indistinguishable from those plotted in Fig. 1. Thus, the specific choice of the KS method seems to be of minor importance when calculating XC energies using MBT.

The study of the interacting energy between two unconfined jellium slabs is of more direct significance, as it has been considered as a benchmark for seamless correlation functionals attempting to describe vdW forces [4,24]. By varying the distance d between the slabs we cover configurations in which the density profiles of each subsystem overlap (i.e. there is a *covalent* bond), and situations (when $d \gg 0$) in which there is no such overlap and the only source of bonding is the appearance of vdW forces. In the upper panel of Fig. 2 we plot the XC energy per particle $\varepsilon_{\rm XC}(d)$ as a function of d using the LDA (the WDA gives very similar results), the RPA, and the $G_0 W_0$, for two slabs of width $L = 12a_0$ and a background density \overline{n} corresponding to $r_{\rm s} = 3.93$. We can see that the $G_0 W_0$ reduces the RPA error by 60%. In the lower panel we represent the correlation binding energy per particle [defined as $e_{\rm C}(d) = \varepsilon_{\rm C}(d) - \varepsilon_{\rm C}(\infty)$]. First, neither the LDA nor even the nonlocal WDA is able to reproduce the characteristic asymptotic d^{-2} vdW behavior. This behavior is described by the RPA and the $G_0 W_0$, and for both approximations $e_{\rm C} (d \gg 0)$ is very similar (which is not a surprise because such an asymptotic behavior is fully described at the RPA level [4]). For

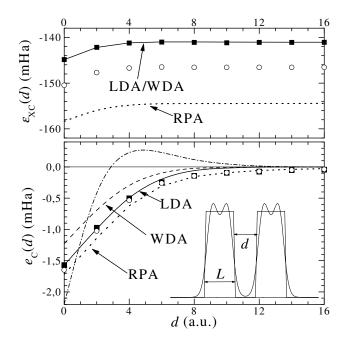


FIG. 2. Upper panel: XC energy per particle for two jellium slabs as a function of the distance d. Lines: LDA, WDA and RPA; circles: G_0W_0 ; squares: G_0W_0 plus LDA-like correction term. Lower panel: correlation binding energy per particle. The LDA and WDA contributions have been obtained by subtracting the exact exchange energy from the corresponding XC values. The exchange binding energy (dashed-dotted line) has been also included in this panel.

intermediate and small separations, there are slight differences between the RPA and the G_0W_0 but much less important than those appearing when comparing the total correlation energies.

A detail that is worth pointing out is the fact that the error in the *absolute* G_0W_0 correlation energy is amenable to a LDA-like correction. From the differences, given in Ref. [10], between QMC and G_0W_0 correlation energies for the HEG, we can build a functional $\Delta E_{\rm C} = \int d\mathbf{r}n(\mathbf{r}) \,\delta \varepsilon_{\rm C} [n(\mathbf{r})]$. The absolute G_0W_0 energy corrected in this way is in broad correspondence with the LDA energy, while the binding energy retains its correct $1/d^2$ behavior at large d and is little altered for small d(see Fig. 2).

In summary, we have performed GW-MBT calculations to evaluate the ground-state energy of inhomogeneous systems. With practically the same cost we have obtained correlation energies beyond the random phase approximation. The importance of a truly *ab initio* treatment of electron many-body effects is evident in the model systems we have chosen, for which traditional implementations of DFT are completely inaccurate.

The authors thank C.-O. Almbladh, J.E. Alvarellos, U. von Barth, E. Chacón, J. Dobson, B. Holm, P. Rinke, and A. Schindlmayr for many valuable discussions. This work was funded in part by the EU through the NANOPHASE Research Training Network (Contract No. HPRN-CT-2000-00167) and by the Spanish Education Ministry DGESIC grant PB97-1223-C02-02.

- [1] L. Hedin, Phys. Rev. **139**, A796 (1965).
- [2] See, for instance: F. Aryasetiawan and O. Gunnarsson, Rep. Prog. Phys. **61**, 237 (1998); W.G. Aulbur, L. Jönsson, and J.W. Wilkins, Solid State Physics **54**, 1 (2000).
- [3] M.M. Rieger and R.W. Godby, Phys. Rev. B 58, 1343 (1998).
- [4] J.F. Dobson and J. Wang, Phys. Rev. Lett. 82, 2123 (1999); Phys. Rev. B 62, 10038 (2000).
- [5] B. Holm, Phys. Rev. Lett. 83, 788 (1999).
- [6] C.-O. Almbladh, U. von Barth, and R. van Leeuwen, Int. J. Mod. Phys. B 13, 535 (1999).
- [7] B. Holm and F. Aryasetiawan, Phys. Rev. B 62, 4858 (2000).
- [8] P. Sánchez-Friera and R. W. Godby, Phys. Rev. Lett. 85, 5611 (2000).
- [9] J.M. Pitarke and A.G. Eguiluz, Phys. Rev. B 63, 045116 (2001).
- [10] P. García-González and R.W. Godby, Phys. Rev. B 63, 075112 (2001).
- [11] P. Hohenberg and W. Kohn, Phys. Rev. **136**, B864 (1964); W. Kohn and L.J. Sham, *ibid.* **140**, A1133 (1965).
- [12] F. Aryasetiawan and O. Gunnarsson, Phys. Rev. B 49, 16214 (1994).
- [13] H.N. Rojas, R.W. Godby, and R.J. Needs, Phys. Rev. Lett. **74**, 1827 (1995); M.M. Rieger *et al.*, Computer Physics Communications **117**, 211 (1999); L. Steinbeck *et al.*, *ibid.* **125**, 105 (2000).
- [14] W.M.C. Foulkes et al., Rev. Mod. Phys. 73, 17 (2000).
- [15] Y. Kim *et al.*, Phys. Rev. B **61**, 5202 (2000); L. Pollack and J.P. Pedew, J. Phys.: Condens. Matter **12**, 1239 (2000); P. García-González, Phys. Rev. B **62**, 2321 (2000).
- [16] W. Kohn, Y. Meir, and D.E. Makarov, Phys. Rev. Lett. 80, 4153 (1998).
- [17] O. Gunnarsson, M. Jonson, and B.I. Lundqvist, Phys. Rev. B **20**, 3136 (1979); E. Chacón and P. Tarazona, Phys. Rev. B **37**, 4013 (1988).
- B. Holm and U. von Barth, Phys. Rev. B 57, 2108 (1998);
 W.D. Schöne and A.G. Eguiluz, Phys. Rev. Lett. 81, 1662 (1998).
- [19] V.M. Galitskii and A.B. Migdal, Zh. Eksp. Teor. Fiz. 34, 139 (1958) [Sov. Phys. JETP 7, 96 (1958)].
- [20] S. Kurth and J.P. Perdew, Phys. Rev. B 59, 10461 (1999); Z. Yan et al., ibid. 61, 2595 (2000).
- [21] A. Schindlmayr, Phys. Rev. B 56, 3528 (1997).
- [22] A. Schindlmayr, P. García-González, and R.W. Godby, Phys. Rev. B (in press).
- [23] A. G. Eguiluz, Phys. Rev. B 31, 3303 (1985).
- [24] H. Rydberg et al., Phys. Rev. B 62, 6997 (2000).