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**Article:**

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Effect of Lateral Displacement of a High-Altitude Platform on Cellular Interference and Handover

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Abstract—A method for predicting movements in cellular coverage caused by lateral drift of a high-altitude platform (a quasi-stationary platform in the stratosphere) is developed. Cells are produced by spot beams generated by horn-type antennas on the platform. It is shown how the carrier-to-interference ratio (CIR) across these cells varies when the antenna payload is steered to accommodate the lateral movement of the platform. The geometry of the antenna beam footprint on the ground is first developed and then applied to a system of many cochannel beams. Pointing strategies are examined, where the pointing angle is calculated to keep, for example, a center cell or an edge cell in the same nominal position before and after the platform drift, and the CIR distribution is calculated. It is shown that the optimum pointing angle depends on the desired level of CIR across the service area, typically lying between $3 \pm 0.75^\circ$ for a platform drift of 2 km and corresponding to a cell in the middle ring. It is shown that it is necessary for a significant proportion of users to perform a handover to maintain a given CIR after platform drift. The analysis reveals that there is an optimum pointing angle that minimizes the probability of handover for a particular value of drift and CIR.

Index Terms—Antennas, broadband communication, high-altitude platforms, interference.

I. INTRODUCTION

With an ever increasing demand for capacity for future generation multimedia applications, service providers are looking toward the millimetric wave bands. One possible means of their exploitation is the use of high-altitude platforms (HAPs) [1]–[14], which will operate in the stratosphere at an altitude of 17–22 km. HAPs have the potential to provide line-of-sight links to a large number of users situated over a large geographical area and use considerably less communications infrastructure than that required if delivered by a terrestrial network. Such systems will employ a cellular architecture in order to provide overall system capacity, with cells served by a number of antenna spot beams from the HAP.

The performance of terrestrial cellular architectures has been described by Lee [15]. To provide wide coverage, the cells are tessellated, with different channels assigned to neighboring cells in order to manage cochannel interference; assignments can take the form of frequencies, time slots, or codes. Conventionally, cells are clustered into groups of three, four, seven, or nine, dividing the overall frequency allocation between them. The larger the number of cells in the cluster, the greater the reuse distance and the higher the carrier-to-interference ratio (CIR), but the fewer the number of channels per cell; this trade-off is fundamental to most cellular systems. Fixed channel assignment has been shown to produce the highest capacities in nonshadowed environments, but when the traffic load per cell varies, dynamic channel assignment has been shown to provide higher capacity [16]. Dynamic channel assignment is also particularly useful when the environment and/or the traffic load are hard to predict [17]–[21].

A major difference between HAP and terrestrial cellular architectures is the station-keeping characteristics and stability of the platform, and this has been highlighted by a number of aeronautical programs based on airship- and aircraft-type platforms [1]. An emerging body of work [2]–[13] has been examining other communications challenges in increasing detail. However, the effects of HAP station-keeping on cellular communications system performance have yet to be examined in depth. This is partially because it has been difficult to determine accurate specifications for platform movement owing to the scarcity of data regarding their actual aeronautical performance. The International Telecommunications Union has specified that such platforms should be kept within a circle radius sphere of 400 m with height variations of $\pm 700$ m [9]; the HeliNet project has specified two position cylinders that depend on platform availability [7], and the HALO project has suggested that its platform will remain within a toroid of 4–6 km [10]. This work, however, sidesteps this issue and sets out to develop generic models for the effects of platform instability on cellular interference characteristics, with an aim to identifying strategies for accommodating a range of platform movement. Our emphasis is on broadband fixed wireless access-type services typically operating at 28 GHz and above. For this application, the required antenna efficiency and sidelobe suppression are most likely to be offered by aperture- or horn-type antennas. These imply nonadaptive beams that may require mechanical ground stabilization and/or steering. These effects will be explored in this paper. In Section II, the geometry of the HAP and cell footprint is introduced and the effect of platform roll angle is investigated. This analysis will be used in subsequent sections to determine CIR performance when the antennas are subject to different pointing angles in order to correct for platform displacement. Section III then quantifies the system level performance in terms of CIR values resulting from different antenna pointing strategies that are employed to compensate for platform displacement. Three strategies are examined: center cell correction, edge cell correction, and optimized correction.
Section IV then quantifies the performance from the user’s perspective, evaluating the probability that handover is desirable as a way of maintaining quality of service to the user.

II. GEOMETRY OF A CELL FOOTPRINT SUBJECT TO PLATFORM ROLL

Here we show how the footprint of a cell is changed when the HAP experiences a change of roll angle. A similar problem is addressed by [2] in the context of a code division multiple access cellular network. In [2], an approximation is made where a cell is assumed to follow a straight line when there is a change in platform roll angle.\(^1\) We introduce a more general description of the cell’s displacement that is illustrated in Fig. 1. Here the trajectory of the cell describes a curve that yields both \(x\) and \(y\) displacements, this being particularly important for more distant cells and large values of platform roll angle.

In Fig. 1, for a platform roll angle relative to the \(x-y\) plane (\(\Delta \phi\) in Fig. 2), a cell on the \(x\)-axis would undergo displacement along the \(x\)-axis only. However, for a cell on the \(y\)-axis such as footprint \(A\), a platform roll angle change yields displacement in both \(x\) and \(y\) on the ground. Here, the cell footprint \(A\) is assumed circular, having been formed from an antenna beam that is asymmetric, i.e., it has different beamwidths, in the elevation and azimuth planes, which are chosen to yield a circular cell.\(^2\) Cell footprints \(A’\) and \(A''\) are distorted and result, respectively, from positive and negative roll angles of the platform. Footprints \(B, B’\), and \(B''\) show an equivalent but more general case for a cell footprint that lies on neither \(x\)- nor \(y\)-axis.\(^3\)

The new antenna pointing angles may be derived by considering the circle through which the antenna boresight passes following a change in platform roll angle, as shown in Fig. 2, where the platform is on station at point \(s\) at height \(h\). Point \(a\) is the cell center, on the \(x-y\) plane of the ground, before the platform experiences a change in roll angle. When the platform roll angle changes by \(\Delta \phi\), the boresight passes through point \(p\) on a circle that is centered at \(x = 0, z = z_p, y = y_a\) and is parallel to the \(x-z\) plane. The new boresight \(a'\) intersects the \(x-y\) plane at the new cell center \(a'\). By deriving the coordinates of point \(p\), the new boresight pointing angles can be derived.

The “roll circle” has radius \(r_c\) given by

\[
r_c = \frac{h}{\cos \phi}\tag{1}
\]

where \(\phi\) is the angle of the original cell center \(a\) with respect to the axis of platform roll

\[
\phi = \arctan \frac{x_a}{h}\tag{2}
\]

and, after [2], the original point where the beam intersects the ground \(a\) (which we also define as cell center) has \(x\) and \(y\) coordinates given by

\[
x_a = h \tan \theta_0 \cos \phi_0\tag{3}
\]

and

\[
y_a = h \tan \theta_0 \sin \phi_0.\tag{4}
\]

The antenna boresight elevation and azimuth pointing angles are, respectively, \(\theta_0\), measured with respect to the platform local vertical, and \(\phi_0\), measured on the \(x-y\) plane with respect to the \(x\)-axis. The Cartesian coordinates of point \(p\) are

\[
x_p = r_c \sin(\phi + \Delta \phi)\tag{5}
\]

and

\[
y_p = y_a\tag{6}
\]

and

\[
z_p = h \left[1 - \frac{\cos(\phi + \Delta \phi)}{\cos \phi}\right].\tag{7}
\]

The new boresight azimuth and elevation angles, respectively, are

\[
\phi' = \arctan \frac{y_p}{x_p}\tag{8}
\]

and

\[
\theta' = \arctan \frac{\sqrt{x_p^2 + y_p^2}}{h - z_p}.\tag{9}
\]

Fig. 3 illustrates the effect of roll angle change on the power contours for a nominal group of six cells, where in case (a) the boresight pointing elevation angle for each cell is 52°, the HAP is at a height of 17 km, and the cells are spaced in azimuth at integer multiples of 30°. The power contours of the cells are initially circular, being formed from asymmetric beams. The power contours are at 3-dB intervals and the directivity of each antenna is 26 dBi.

Fig. 3 case (b) shows how the power contours of each cell are affected by platform roll and further illustrates the movement of

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\(^1\)El-Jabu and Steele [2] use the term “inclination” where we use “roll.” The terms are interchangeable here.

\(^2\)Such an antenna has been reported whereby an asymmetric lens is used to shape the beam [22].
Fig. 2. Change in antenna pointing angles following platform roll $\Delta \varphi$.

Fig. 3. Effect of platform roll angle on six nominally circular cells’ power footprints (power contours are relative to cell center power and spaced by 3 dB). (a) Zero platform roll. (b) $+8^\circ$ platform roll.

Cell centers first introduced in Fig. 1. The method may now be extended to derive changes in CIR for a cochannel cell group. In particular, we may study the consequence of mechanically steering a group of antennas toward the nominal center of the service area when the platform is laterally displaced from its intended position as discussed in Section I above.

III. RESULTS FOR ANTENNA POINTING ON A NETWORK OF 121 CELLS

The analysis developed in Section II now allows us to quantify the effects of different antenna pointing strategies on the CIR obtained from a 121-cell architecture when used to
compensate for lateral drift in the platform. Thus, (8) and (9) may be used to derive the antenna pointing angles for each cell and the method of [8] to derive CIR values. To briefly review [8], CIR is calculated in each cell as the ratio of the power received from the main antenna beam and the sum of the powers from all the other cochannel beams.

The CIR level is important because it determines the modulation and coding schemes that can be used: the higher the CIR, the higher the data rate that can be accommodated. For example, coded quaternary phase-shift keying (QPSK) requires a signal-to-noise ratio (SNR, assumed here to be equivalent to CIR) of at least 2.9 dB and will carry 1.38 b per symbol [7]. When the platform suffers lateral displacement, the cell footprints on the ground will undergo an equal lateral movement, unless compensated for by angular adjustment in the antenna payload. This displacement of the cellular pattern may lead to loss of service for users near the edge of the intended service region while for other users the cell movement may lead to a requirement for handover to another channel. These effects may be decreased if the platform antennas can be pointed towards the original cell center locations. We choose to steer the antenna group as one in order to reduce mechanical complexity. The geometry for the new pointing angles, power and CIR contours, is equivalent to that described in Section II for changes in platform roll angle.

A standard four-channel reuse scheme is used here, where the total service area has a diameter of 60 km and the HAP is at a height $h = 17$ km. The antenna main lobes are modeled after [8] and the sidelobes are assumed to be a flat floor at $-40$ dB below peak directivity for each antenna. (These simple models have been used so that the effects of beamwidths, cochannel cell spacing, and platform displacement can be studied with greater clarity because the system has many variable parameters [8], [14].) Fig. 4(a) shows the CIR contours for one of four channels, for zero platform displacement, and therefore without an applied antenna pointing correction.

Three pointing strategies are assessed in the next subsections: center cell correction, edge cell correction, and optimized coverage correction. Results are obtained using the equations above by calculating the CIR at each point $(x, y)$. The spacing of these points depends on the spatial resolution required, and we have found that an interval of 0.625 km is adequate. Contour plots are then used to determine the fraction of the coverage area affected with each strategy. In some cases, so as to illustrate areas of coverage, an arbitrary CIR level has been used—areas with CIR above this level are colored in grey, areas below are shown in white.

### A. Center Cell Correction

Here, a pointing angle is derived that always ensures that the center cell is positioned in the center of the service area. This requires a change in antenna pointing angle

$$\Delta \varphi = \arctan \frac{d}{h}$$

where $d$ is the platform drift. The effect of applying this pointing angle is shown in Fig. 4(b).
Fig. 5. Effect of platform drift on the fractional coverage of the fixed cell group where central cell position is used to choose antenna pointing angle.

Fig. 6. Effect of platform drift: fractional coverage on any of the four channels for the entire service area for different choices of antenna pointing correction.

Fig. 7(a). In Fig. 7, an arbitrary CIR level of 16 dB has been used to illustrate where such small gaps in coverage occur at this level—areas above 16 dB are shown in grey, areas below 16 dB appear as white gaps.

The gaps are a consequence of the spatial overlap of the antenna radiation patterns. The CIR level has been chosen here so that nearly all the service area experiences this level. Hence, it is useful to show that where the white area increases [Fig. 7(b)], the system performance is being degraded. Our rationale is to choose the antenna pointing strategy that minimizes the degradation of the quality of service. In the following sections, it will be shown that the residual CIR and coverage degradation of Fig. 7(b) can be eliminated by careful choice of antenna pointing angle.

B. Edge Cell Correction

It is apparent in Fig. 7 that there is a tendency for CIR coverage to extend beyond the nominal 60-km diameter service area. When the angle from (10) is applied as a pointing angle to correct for platform displacement, the coverage tends to be extended toward $-x$ while being truncated toward $+x$. This would suggest that the angle from (10) overcompensates for displacement for most cells across the coverage area as a whole and should be reduced. This can be achieved by instead correcting the position of a cell on the edge of the service area—an “edge cell.” This is equivalent to the difference in the subtended elevation before and after platform displacement, i.e.,

$$
\Delta \varphi = \arctan \frac{r_c}{h} - \arctan \frac{r_c - d}{h} \tag{11}
$$

where $r_c$ is the radius of the service area (30 km in this example). Using this revised strategy for antenna pointing, the coverage gaps for all channels are shown in Fig. 7(c), which we see is very similar to case (a) with zero drift. Having identified what appears to be an improved algorithm for pointing correction, we return to a consideration of coverage for a single channel of fixed cells. This is shown in Fig. 8 for a 2-km platform drift and the two different pointing algorithms discussed above. In Fig. 8, we see that the revised method (11) yields a less severe
Fig. 7. Coverage gaps for four channel schemes where handover to any channel is allowed at 16-dB CIR level (dark shading is above this). (a) Zero displacement. (b) 2-km drift, center cells corrected. (c) 2-km drift, revised correction.

Fig. 8. Effect of platform drift: comparison of coverage for the fixed cell group (one channel only, handover not allowed) for different pointing corrections.

CIR degradation in terms of the geographical area of a fixed cell group served on a single channel (handover not allowed). The implication here is that because the average CIR reduction is less severe, fewer users will need to handover to another channel in an attempt to re-establish the CIR they experienced before the platform was displaced. Thus, the above study has shown that a relationship exists between platform displacement, the associated choice of antenna pointing correction, cellular CIR coverage, and the likelihood of handover being required.

C. Optimized Coverage Correction

An optimum pointing angle for a specific channel and desired CIR level can be derived. This may be found numerically by examining the fractional coverage available at a specific minimum CIR for different pointing angles as shown in Fig. 8 and the fractional coverage as a function of pointing angle for various fixed CIR thresholds as shown in Fig. 9.

Fig. 9 affords considerable insight into many aspects of the system, which we will briefly discuss. For each CIR threshold shown, the intercept at the coverage axis shows the fractional area of a fixed cell group that is served at or above the threshold when zero pointing angle is applied to the antenna payload. Relative to this, the maximum of each curve shows an increase in coverage. Interestingly, this optimum angle is not constant for each curve but falls within a fairly narrow range (3 ± 0.75°)—the deviation occurs because the centers of the CIR contours, as illustrated in Fig. 4, are not exactly colocated due to the path length difference across the cell. This angular range corresponds to cells lying in the middle rings of the service area. When this 3° angle is applied, coverage on any of the four channels (i.e., when handover is used) approaches the curve for zero platform displacement shown in Fig. 8 almost exactly—hence, CIR at any point will be maintained at between 15.5 and 27.5 dB. To guarantee that CIR does not fall below the 15.5-dB minimum, 9% of the cell group area requires handover to another channel, which is apparent from the arrowed region in Fig. 9.

IV. Probability of Required Handover and Successful Handover

The previous results have examined the system performance over the service area. Here we now extend the analysis to look at the performance from a user’s perspective, where users are assumed to be located uniformly across the service area. We
present a method of predicting the probability that handover to another channel is required in order to maintain at least the same CIR following a platform lateral drift, and also quantify the associated influence of antenna pointing correction. These measures quantify the spatial effects due to the platform drift and changes to the cellular coverage rather than quantifying the temporal effects such as the frequency of handover arising from the platform movement dynamics. Temporal effects are beyond the scope of this paper and will be highly dependent on platform type. Recalling that from [8] the CIR at each ground location (or “element”) can be derived, we may use set theory notation to aid a comparison of CIR coverage before and after the platform drift and antenna pointing correction. \( T \) is the set of all elements within the coverage area, so the set of elements \( (E) \) within \( T \) that is above or equal to a CIR threshold \( x \) on a single channel when the HAP is located at point \( p \) (over the subplatform point) is

\[
E = \{ e \in T : e(n,p) \geq x \}
\]  

where \( n \) is the index to the single channel of interest and \( p \) is the index referring to the CIR values obtained when the HAP is at point \( p \). Similarly, after the platform has moved to a new location \( p' \), then

\[
E' = \{ e \in T : e(n,p') \geq x \}
\]  

where \( e \) is now in the set of elements within set \( T \) that have their CIR above (or equal to) the threshold \( x \) on the single channel. Several performance measures can be defined using the above. The probability that the CIR remains above \( x \) after drift \((P_{a,x})\) is

\[
P_{a,x} = \frac{|E \cap E'|}{|E|}
\]  

and the probability that the CIR decreases below \( x \) after drift \((P_{b,x})\) is

\[
P_{b,x} = 1 - \frac{|E \cap E'|}{|E|} \quad \text{or} \quad P_{b,x} = \frac{|E \setminus E'|}{|E|}.
\]  

This is also the probability that handover is desired. We now define the set \( H' \) as the elements in the original set \( T \) that are above the threshold CIR\(x\) on an alternative channel after the HAP has drifted to \( p' \):

\[
H' = \{ e \in T : e(n,p') \geq x, \quad n \in C \setminus C_1 \}
\]  

where \( n \) is the channel index, \( C \) is the set of all channels in the system, and \( C_1 \) is the set containing only the original channel of interest. That is, \( H' \) contains all the elements where a handover can be supported successfully. Hence, the probability that handover is successful \((P_{h,x})\) is

\[
P_{h,x} = \frac{|E \cap H'|}{|E|}
\]  

and probability that handover is required and successful \((P_{rh,x})\) is

\[
P_{rh,x} = \frac{|(E \setminus E') \cap H'|}{|E|}.
\]  

The probability that a user will continue to remain above the threshold \( x \) after drift, assuming handover to an alternative channel is allowed \((P_{ah,x})\), is

\[
P_{ah,x} = \frac{|E \cap (E' \cup H')|}{|E|}.
\]

Fig. 10 shows (15), (18), and (19) evaluated as a function of \( x \) for three cases of pointing angle. Fig. 10 presents some interesting results that should be interpreted in the context of the coverage plots shown in Fig. 6, which show that fewer users experience the higher CIR. Fig. 10 illustrates that these users are more likely to require handover to another channel to maintain their CIR and that handover is less likely to be successful, indicating that the links at higher CIR are less stable. The effect of pointing angle is also apparent in Fig. 10. Interestingly, an excessive angle increases the need for handover, exceeding that for zero pointing angle, although the total coverage after handover (Fig. 6) is rather worse for the zero angle case. When the optimum pointing angle is chosen (i.e., 3°), the probability of handover being required \((P_{b,x})\) at a given threshold \( x \) is minimized while the probability of CIR continuity \((P_{ah,x})\) is maximized. Also, while coverage at a CIR level can be maintained on average across the coverage area, handover is still required on a location-by-location basis as the peaks in CIR move around. In summary, the effects of lateral displacement can largely be mitigated using the developed antenna pointing strategy and handover. Nodes experiencing a high initial CIR are more likely to be affected than those with low initial CIR. However, effective use of adaptive modulation and coding will ensure that users will in general be able to maintain a minimum data rate.

V. CONCLUSION

A model for predicting the geographical coverage and handover requirements provided by a group of mechanically
steered, aperture-type antennas that serve a cellular network from an HAP has been presented. These have been expressed in terms of the CIR on the ground that is derived from the overlap of the power footprint of each antenna, whose radiation patterns are modeled using curve-fit approximations. A derivation of the footprints’ distortion as a function of platform roll angle has also been presented. These methods have been combined to model variations in CIR that would occur when the antennas are pointed, as a group, toward the center of the service area so as to accommodate lateral displacements of the platform (individual beam steering has not been considered).

An architecture of 121 cells using four channels has been investigated in detail for lateral platform displacements up to 2 km. When handover is not used, it has been shown that the geographical coverage of a cochannel cell group suffers a degradation whereby the average CIR is reduced across all cells. Different strategies for deriving a correction angle for antenna pointing have been considered, and it has been shown that the correction required is somewhat less than the change in elevation angle associated with the central cell. When handover is used, CIR levels are not on average degraded, although handover is required on a location-by-location basis because the peaks in CIR move around. When a pointing angle that maximizes coverage on a single channel is chosen, the probability of handover being required at a given CIR threshold is minimized. Thus, the combined effects of the pointing strategy and handover mean that the negative effects of HAP lateral displacement can be largely mitigated.

The full extent of the positional instability of future HAPs is not yet well defined, and the work is intended to present the development of a prediction tool that can be used to characterize the performance of future HAP systems once their positional specification becomes available.

REFERENCES

John Thornton is a graduate of physics from the University of York, Heslington, U.K., and received the M.Sc. degree in microwave physics from the University of Portsmouth, Hampshire, U.K., in 1995, and the Ph.D. degree from the Open University, Milton Keynes, U.K., in 2002. He has previously held research positions at the Rutherford Appleton Laboratory, Didcot, Oxfordshire, U.K., developing submillimetre wave solid state sources for space applications, and thereafter at the Department of Engineering Science, University of Oxford, U.K., working on a number of diverse communications projects that included passive radar transponders, adaptive antennas, and superconducting filters for broadcast and cellular applications. In 2000, he joined the Department of Electronics, University of York.

David Grace (S’95–A’99–M’00) received the M.Eng. degree in electronic systems engineering and the D.Phil. degree from the University of York, Heslington, U.K., in 1993 and 1999, respectively. He has worked on a variety of research contracts including several from the former Defence Evaluation and Research Agency. He is now Principal Scientific Officer for CAPANINA, a major European Framework 6 project that is developing broadband communications from high-altitude platforms. He has been an invited speaker at several conferences and industrial locations in the fields of HAP systems. He is also a nonpaid Researcher in the European NEWCOM Network of Excellence and a Director of SkyLARC Technologies Ltd., a York-based company specializing in broadband communications from aerial platforms. Current research interests include radio resource management for broadband communications particularly from high-altitude platform and terrestrial ad hoc networks. Since 1994, he has been a Member of the Communications Research Group at York, where he is now a Research Fellow.