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Comparison Of Chemical Clustering Methods Using Graph-Based And Fingerprint-Based Similarity Measures

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Abstract This paper compares several published methods for clustering chemical structures, using both fingerprint-based and graph-based similarity measures. The clusterings from each method were compared to determine the degree of cluster overlap. Each method was also evaluated on how well it grouped structures into clusters possessing a non-trivial substructural commonality. The methods which employ adjustable parameters were tested to determine the stability of each parameter for datasets of varying size and composition. Our experiments suggest that both fingerprint-based and graph-based similarity measures can be used effectively for generating chemical clusterings; it is also suggested that the CAST method, suggested recently for the clustering of gene expression patterns, may also prove effective for the clustering of 2D chemical structures.

INTRODUCTION

Cluster analysis methods are used to identify groups, or clusters, of similar objects in multivariate datasets 1. In brief, a cluster analysis involves the following components: a set of objects, each of which is represented by one or more attributes; a measure of the similarity (or

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dissimilarity or distance) between pairs of objects, between an object and a cluster, or between a pair of clusters; and a clustering method that processes the similarity data to identify groups that are (hopefully) both homogeneous and distinct. The reader should note that there may be several different algorithms that can implement a particular clustering method; for example, Rohlf reviews a range of algorithms for the single linkage method ², which is an hierarchic agglomerative method that fuses pairs of clusters on the basis of the objects, one in one cluster and one in the other, that are most similar to each other. Many other methods, conversely, are defined solely in algorithmic terms, e.g., the Jarvis-Patrick method ³ that has been extensively used in previous studies of chemical clustering and that is one of the methods considered later in this paper.

Biological taxonomy⁴ provided the basis for the development of many of the clustering techniques that are available today, but these are now used in a wide range of application domains, with the current interest in data mining spurring the introduction of many new methods. Structural features provide an obvious source of attributes for chemical applications of clustering but early studies of the use of such features ⁵⁻⁸ were restricted to very small datasets. An extensive series of studies by Willett and co-workers in the early and mid-Eighties (as reviewed in ⁹) demonstrated the use of large-scale clustering for the selection of compounds for biological screening and for the processing of substructure search output, and highlighted the Jarvis-Patrick method as providing an appropriate combination of effectiveness and efficiency. Later work ¹⁰⁻¹² demonstrated the greater effectiveness of Ward's method ¹³ and the availability of improved algorithms for this method ¹⁴ have allowed it to join Jarvis-Patrick as the most widely used clustering method for chemical applications.

The structural features that are normally used in chemical clustering are the fragment substructures encoded in a fingerprint to enhance the efficiency of 2D substructure searching. The similarity between two molecules is then computed as a function of the number of bits (and thus fragment substructures) that are common to the fingerprints representing those molecules. The Tanimoto coefficient is generally used to calculate such similarities but there are many other coefficients that can be used for this purpose. Fingerprint-based similarities can be calculated

extremely rapidly and have been found to perform reasonably well in practice, but there are many other ways in which one might seek to quantify the structural relationships between pairs of molecules ¹⁵. One such approach uses a maximum common subgraph isomorphism algorithm to identify the largest substructure common to a pair of molecules, with the size of this maximum common substructure (MCS) being determined by some function of the numbers of constituent atoms and/or bonds. This provides a natural way of calculating the degree of similarity between a pair of molecules but the NP-complete nature of the maximum common subgraph isomorphism problem has ruled out the large-scale use of MCS-based similarities. We have recently described a new MCS algorithm, called RASCAL, that is sufficiently rapid in execution to permit graph-based similarity searching of large chemical databases ¹⁶, ¹⁷ and that seems to provide a viable complement, or even an alternative, to existing, fingerprint-based approaches to virtual screening ¹⁸.

Given the close relationship that exists between similarity searching (where a single target molecule is matched against each of the molecules in a database) and clustering (where each molecule is matched against every other molecule in a database) this paper seeks to assess the suitability of graph-based similarity measures for chemical clustering and to compare their effectiveness with that of fingerprint-based measures. The natural starting point for such an evaluation is to take the current clustering methods of choice (i.e., Ward's method and the Jarvis-Patrick method, for which there is already a large body of practical experience) and to use them to process graph-based similarities, with the results from conventional fingerprint-based similarities providing a benchmark of comparison. However, we have taken the opportunity to consider several additional clustering methods, one of which has been designed specifically for use with graph-based measures of chemical similarity.

GRAPH-BASED AND FINGERPRINT-BASED CLUSTERING

Terms And Definitions

All graphs referred to in the following text are assumed to be simple, undirected graphs. For an introduction to graph-related concepts and notation, the reader is referred to a standard text on

graph theory such as the recent book by Diestel ¹⁹. A graph *G* consists of a set of vertices V(G) and a set of edges E(G) representing lines connecting all or some of the vertices in V(G). A *subgraph* of *G* is a graph whose vertices and edges are subsets of *G* preserving the connectivity between the vertices and edges. A *maximum common edge subgraph* (MCES) is a subgraph common to two or more graphs consisting of the largest number of edges possible. Figure 1 illustrates the MCES G_{12} between two molecular graphs G_1 and G_2 .

In this paper, two different types of similarity measure are investigated, *feature-based* measures and *cost-based* measures, these corresponding to the use of fingerprints and of structure diagrams (i.e., 2D chemical graphs), respectively. In feature-based measures, a set of features or invariants is established from a structural description of a graph, and these features are then used in a vector representation to which various distance or similarity coefficients can be applied. Similarity coefficients obtained using the feature-based approach are functions of the relative number of bit positions that are set in each fingerprint (as reviewed by Willett *et al.* 15). For instance, the well-known Tanimoto coefficient is given as c/(a+b-c) where *a* and *b* are the number of features present in the two structures being compared and *c* is the number of features in common between the two structures. In our experiments, the feature-based measures are calculated using Daylight fingerprints, which have been shown previously to be effective in chemical database studies 20.

In cost-based measures, the similarity between two compounds reflects the number of edit operations that are required in order to transform one structural graph into the other. Recently, an efficient cost-based method based on the MCES, and called RASCAL, has been published ¹⁶, ¹⁷. RASCAL can be used with the same similarity coefficient formulae as are used with the feature-based methods ¹⁸, the difference being that the size of each graph is used to replace the number of features representing each structure. Therefore, the size of the MCES graph G_{12} replaces the number of features in common, and the sizes of the two molecular graphs being compared replace the number of bits set in each respective fingerprint. For example, the Tanimoto coefficient is given as $|G_{12}|/(|G_1|+|G_2|-|G_{12}|)$.

In its simplest form, the graph size is determined by treating atoms and bond pairs equally (i.e., $|G_{12}| = |V(G_{12})| + |E(G_{12})|$). However, it has been found ¹⁸ that the RASCAL approach better approximates a chemical notion of similarity using

$$|V(G_{12})| + \beta \cdot (1 - \alpha \cdot (n(p, G_{12}) - 1)) \cdot |E(G_{12})|$$

for $|G_{12}|$, and

$$|V(G_1)| + \beta \cdot |E(G_1)|$$
 and $|V(G_2)| + \beta \cdot |E(G_2)|$

for $|G_1|$ and $|G_2|$, respectively. The function $n(p,G_{12})$ represents the number of unconnected subgraph components in the MCES (G_{12}) containing p or more edges: if all subgraphs have fewer than p edges, then $n(p,G_{12})$ will be assumed to be the total number of subgraph components. The constant β reflects the additional weight assigned to matched bond pairs with respect to compatible atoms, and the constant α is a penalty score for each unconnected component present in G_{12} . It has been found that values of p=3, $\alpha=0.05$, and $\beta=2.0$ are effective in discerning chemical similarity, and are used in all of the experiments reported here. The current analysis also uses strict atom and bond typing so that only atoms and bonds of the same type can be matched, e.g., chlorine cannot match to fluorine. It may be possible to improve the results of a graph-based method by allowing some "fuzziness" in the compatibility between the various atom and bond types, but this prospect is not investigated here.

Clustering Methods

Five different clustering methods were evaluated in this study. Two of them (Ward's 13 and Jarvis-Patrick ³) are well-known within the chemical information community and have previously proven effective for the clustering of chemical structures. The other three have been selected from the clustering literature as being new to the clustering of chemical structure databases and hence appropriate for evaluation. Each method is described briefly below: the reader is referred to the original publications for details of the various procedures. In addition, the algorithm of Umesh 21 was also investigated, but in preliminary investigations it proved inferior to the others tested and was therefore omitted from further consideration.

Ben-Dor et al. (CAST) ²²: The CAST method is based on an approximate clique-finding algorithm that avoids much of the costly enumeration necessary in traditional algorithms, and that

uses a threshold parameter t to establish cliques of mutually similar objects. Adjustable parameter(s): t.

Jarvis-Patrick ³: This clustering method uses a table of k nearest neighbors for each object being clustered, and then sequentially merges clusters which have at least k_t nearest neighbors in common. Adjustable parameter(s): k and k_t .

Raymond-Willett ²³: This method is based on a greedy algorithm that establishes clusters using a technique involving line graphs. It is a fuzzy clustering procedure in that it allows for the possibility of overlapping clusters using three adjustable similarity thresholds. Adjustable parameter(s): S, S_a and S_b .

Ward ¹³: This is Ward's well-known hierarchical clustering method, which establishes a hierarchy of clusterings whereby each level in the hierarchy represents a unique clustering. A representative clustering is typically selected using a rapidly calculable cluster validation index. The use of cluster validation indices in conjunction with Ward's algorithm has been studied in detail, and it was found that Kelley's validation index ²⁴ was among the best of those tested ²⁰. In our studies, Ward's method will be used in conjunction with the Kelley index. Adjustable parameter(s): *none*.

Yin-Chen ²⁵: This approach is basically a two phase threshold method. It uses a built-in constant for thresholding as published, but we have found that converting this constant to an adjustable parameter y_t affords significantly greater flexibility (a value of y_t equal to 0.5 is equivalent to the originally published method). Adjustable parameter(s): y_t .

PARAMETER OPTIMISATION

Methods

To evaluate the relative quality of the clusterings resulting from the various methods, we compare each calculated clustering with a reference clustering of the same data. In our experiments, we have used the seven datasets used in a previous evaluation of cluster validation indices ²⁰ as well as two additional datasets created specifically for these trials. The characteristics of each dataset are summarized in Table 1. Each dataset was manually clustered in order to establish an 'ideal' clustering. This procedure is obviously subjective to a certain degree but, we believe, represents a reasonable partitioning of the structures. Four of the datasets were taken directly from the NCI

anti-HIV database. Three are taken from the Pfizer corporate compound collection, and the two final datasets are a subset of the ID Alert database. These datasets represent various possible scenarios that may arise in a practical application.

NCI-A and NCI-B contain multiple distinct, but similar, structures, and NCI-C and NCI-D contain a more random assortment of structures. PD-X is a diverse set of compounds determined to be active in a high-throughput screening assay, and PD-Y and PD-Z are combinatorially synthesized compounds derived from a single scaffold for a single project. The clusters contained in ID-1 and ID-2 are diverse in that some of the clusters contain closely related compounds while others contain more loosely related compounds. Some clusters are structurally related to other clusters, and other clusters are distinct from all other clusters. Each dataset was evaluated for selfsimilarity by calculating the average nearest neighbor (ANN), average farthest neighbor (AFN), and the overall average similarity for all neighbors (AAN). The results are listed in Table 2. As previously mentioned, the combinatorial sets display a marked degree of self-similarity.

In this paper, we use two separate methods to evaluate the clusterings resulting from each method by comparing them with a reference clustering. The first comparison measure is the well-known Jaccard coefficient ²⁶ given as:

$$J(C_1,C_2)=\frac{c}{a+b-c},$$

where c is the number of pairs of structures that share a common cluster in both respective clusterings (C_1 and C_2), a is the number of pairs of structures that share a common cluster in the first clustering C_1 , and b is the number of pairs of structures that share a common cluster in the second clustering C_2 . The Jaccard measure ranges from zero to one, where zero indicates a perfect mismatch and one indicates a perfect match. In our studies, C_1 will indicate the reference clustering for a particular dataset, and C_2 will represent the calculated clustering resulting from each method.

The second comparison measure is based on the distance between two clusterings using an assignment procedure, where the distance can be regarded as the number of misclassified structures when a calculated clustering is compared to the reference clustering. Gusfield ²⁷ has

proposed a method whereby the distance between two clusterings C_1 and C_2 is calculated using $D(C_1, C_2) = |N| - A(C_1, C_2)$, where N is the set of structures in the reference clustering C_1 and $A(C_1, C_2)$ is the value of the assignment of the clusters from clustering C_1 to clustering C_2 .

The value of $A(C_1,C_2)$ is calculated by first constructing an assignment matrix where each row *i* corresponds to a unique cluster in C_1 and each column *j* corresponds to a unique cluster in C_2 . The value of each element (i_3j) in the assignment matrix consists of the number of structures that cluster *i* and cluster *j* have in common. The value of $A(C_1,C_2)$ then corresponds to the value of the linear assignment of the assignment matrix. A linear assignment is a subset of elements (i_3j) in the assignment matrix whose sum is the maximum possible subject to the constraint that no two selected elements can be located in the same row or the same column in the matrix. Efficient algorithms exist for this procedure ²⁸, 29.

Results

With the exception of Ward's, all of the clustering methods considered in this study involve the use of adjustable parameters. This presents a problem for the general application of these methods since, in order for a particular clustering method to be useful to the general practitioner, the user must have some idea of what parameter values to use with each method for a given problem. This raises two questions. What is a good 'rule of thumb' value to use for each adjustable parameter for a given problem? Are these values consistent from one problem to another? To be an effective general purpose method, it must be possible to determine a representative value for each parameter for a given clustering method, and these representative values must be consistent across similar problems. The less variable a clustering method's parameters are, the easier it is for non-expert users of the method to apply it in practice.

To determine the most appropriate values for each methods adjustable parameters, we have run several optimization experiments. These used the ScatterSearch optimization procedure 30, 31, with the objective functions to be minimized being $-J(C_1,C_2)$ and $D(C_1,C_2)$, respectively, where C_1 is the manual reference clustering and C_2 is the calculated clustering.

Fingerprint-based clustering

The optimization procedure was performed for the CAST, Jarvis-Patrick, and Yin-Chen methods for all nine datasets using Daylight fingerprints and the Tanimoto coefficient. The Raymond-Willett algorithm has not been included in this analysis because it proved to be ineffective for use with fingerprint-based similarity coefficients. This is hardly surprising as it has been designed specifically for the processing of graph-based similarity measures. In addition, Ward's (using the Kelley level selection index) algorithm was included to serve as the benchmark method due to its success in previous analyses ²⁰. The results of the optimization study are presented in Table 3, which lists the optimal value for each adjustable parameter as well as the corresponding Jaccard and Gusfield score for the resulting calculated clustering.

Table 3 shows that the CAST, Jarvis-Patrick, and Yin-Chen methods all performed substantially better than the benchmark Ward's/Kelley method. The resultant objective function values for the Jaccard and Gusfield measures for the optimal clusters were also relatively consistent between methods. Further inspection of the data, however, reveals that the adjustable parameter values corresponding to the optimal clusterings for Jarvis-Patrick display considerable variability with respect to the various datasets, as well as between the Jaccard and Gusfield objective functions. This indicates that while the Jarvis-Patrick method is capable of producing high quality clusterings, it does not appear that there exists a predictable range for each adjustable parameter that would provide an optimal or near-optimal clustering with any degree of confidence. The reason for this is that the other methods tested operate on the values of the pair-wise similarity coefficients directly, whereas Jarvis-Patrick operates on the ordered list of nearest-neighbour rankings. If the relative sizes of the clusters present in the data vary widely, then a particular nearest-neighbor ranking cut-off that works well for a cluster of particular size may not work well for another cluster of a markedly different size. For this reason, Jarvis-Patrick will tend to perform best when the clusters are approximately the same size.

This contrasts with the CAST and Yin-Chen methods, where we consider the datasets containing diverse sets of compounds separately from the combinatorially generated compounds possessing a common scaffold. The CAST method demonstrates relatively narrow ranges of values for which its adjustable parameter (t) provides optimal or near-optimal clusterings. For instance, the value

of *t* ranges from 0.713 to 0.766 with an average of 0.740 for the combinatorial sets (PD-Y and PD-Z) and from 0.284 to 0.486 with an average of 0.384 for the diverse datasets. Like the CAST method, the Yin-Chen method also exhibits a substantial degree of consistency between the optimal clusterings resulting from the Jaccard and Gusfield objective functions. However, it does not display the high degree of consistency with respect to the various datasets exhibited by CAST. The higher values associated with the combinatorial sets are conspicuous, but the level of consistency noted between the diverse datasets with CAST algorithm isn't present with Yin-Chen, as the value of y_t ranges from 0.373 to 0.799 for these datasets.

While it is not possible to claim that one clustering method is the 'best', especially when evaluated on a limited number of datasets, it appears that the CAST method can be used by nonexperts with a reasonable degree of confidence that the resulting clusters will represent a reasonable facsimile of a chemist's notion of a chemical series. Based on the data presented in Table 3, it is suggested that a 'rule of thumb' value for CAST's adjustable parameter t when used in conjunction with Daylight fingerprints and the Tanimoto coefficient is approximately 0.38 for diverse sets of compounds and 0.74 for combinatorial sets possessing a common scaffold. The value of 0.38 for diverse sets of compounds is an interesting discovery considering that the threshold parameter t for the CAST algorithm is simply an average similarity threshold. CAST iteratively increases the size of a cluster by adding a compound to an existing cluster if the average similarity between the compound and all other compounds in the cluster is greater than t. The value of this cluster similarity threshold value is in marked contrast to those established for similarity searching ¹⁸. This is due primarily to the fact that clustering uses all pair-wise similarities between objects in a cluster, which tends to mitigate the presence of inappropriate pair-wise similarity values; whereas, similarity searching only considers the pair-wise similarity values between the query compound and the database of compounds, ignoring the potentially compensating information contained in the similarities between all of the compounds in the database.

Graph-based clusterings

The optimization procedure described above was then applied to the RASCAL-derived, graphbased similarities, as detailed in Table 4. The RASCAL similarity measure requires the use of a minimum similarity index threshold, MSI, for which a value of 0.6 (for the Wallis coefficient, which is the graph form of the Tanimoto coefficient¹⁸) was used for experiments involving the CAST, Jarvis-Patrick, and Yin-Chen methods. The value of 0.6 was found to be low enough so as not to affect the results of these methods. In contrast, the Raymond-Willett method is dependent upon the selected value of MSI, where it is used in lieu of the adjustable parameter S. It was found that an MSI value of 0.7 and 0.85 worked well for the diverse sets and combinatorial sets (PD-Y and PD-Z), respectively. As a note, since the use of the MSI threshold in RASCAL omits pair-wise similarities less than the threshold from further consideration, it was assumed for the purposes of the CAST method that any missing similarity values had a value of 0.5. The use of a threshold enables very substantial reductions in computation 16,17 but is a limitation when used in a clustering context especially when, as here, many different datasets need to be processed.

The results of the experiments with the RASCAL similarities show many of the same patterns observed with the fingerprint similarities. Although the Jarvis-Patrick method demonstrates more consistency with respect to the adjustable parameters when used in conjunction with RASCAL rather than fingerprints, it still exhibits more variability than is desirable for a general purpose procedure. The CAST, Raymond-Willett, and Yin-Chen methods demonstrate similar objective function results for each of the datasets; however, CAST shows the most consistency in its adjustable parameter t, ranging from 0.752 to 0.803 with an average of 0.769 for the combinatorial sets (PD-Y and PD-Z) and from 0.511 to 0.584 with an average of 0.540 for the diverse datasets (all others).

In comparison with the graph-based clusterings, the fingerprints scored consistently higher on the combinatorial sets possessing a common scaffold (PD-Y and PD-Z) as well as two of the NCI datasets (NCI-C and NCI-D). It is interesting to note that these sets possess the most subjective clusterings as the differences between the clusters in the combinatorial sets are subtle and the clusters in NCI-C and NCI-D tend to be more loosely related (not necessarily direct structural analogues). For the ID Alert datasets (ID-1 and ID-2), the graph-based clusterings outperformed the fingerprint-based clusterings: these clusters tended to constitute structural analogues with the

characteristics that some clusters are distinct from all other clusters, but there are also clusters that are structurally related to other clusters in the dataset.

MANUAL INSPECTION OF CLUSTERINGS

Methods

Although the quantitative comparisons described above give an objective assessment of behavior in somewhat contrived situations, we wanted to compare the methods in a situation more closely related to a practical task. One obvious application of such methods is to generate groupings that might be designated as "series" in a medicinal chemist's perception. This corresponds to a common task in the conduct of HTS protocols where typically an initial large and diverse set of primary hits must be organized for analysis. To simulate this situation, a customized collection of 1325 diverse drugs and drug candidates covering a broad spectrum of therapeutic classes and chemical types was used as a dataset. Each method was applied using the optimized parameter settings determined above to partition the dataset. Several known classes were then examined with the following questions in mind: how effectively were the compounds grouped; were there situations where one method was superior to another; and was there any evidence for complementarities between methods in difficult cases? Since the performance of the graphbased methods was of special interest in this work, groups were chosen for examination where an MCES-based approach might be expected to perform particularly well; in addition, cases were sought where differences might be expected from a fingerprint method.

It bears repeating at the outset of this part of the discussion that, although the group selections were driven by the commonality of their biological effects, the methods being used here for partitioning use only topological chemical information. Thus, it is the effectiveness of grouping by chemical class that is most central; if biological commonality is also observed then that is a fortuitous, but not critical, factor in the determination of effectiveness. The following classes were chosen for illustration: tetracycline antibiotics, angiotensin antagonist antihypertensives, calcium antagonist dihydropyridines, antifungal agents, β -lactam antibiotics, angiotensin converting enzyme (ACE) inhibitors and opiate analgesics. For each of the groups, the cluster

membership and frequency are given for Ward's/Kelley, Jarvis-Patrick/6:10, and CAST using Daylight fingerprints, and CAST using RASCAL similarities, in each case with the parameter settings derived from the first part of the study. What is of interest here for a determination of effectiveness is the number of clusters required to include all members of the series (and number of singleton members) and the degree to which each series is cleanly discriminated from other compounds in the dataset, i.e., the number of "non-series" compounds in class clusters. Further, could subsets be perceived or were "extraneous" compounds "interesting" in any sense? A summary of the observations on these series is given in Table 5 for the compounds listed in Table 6. For each class or major subclass examined, the number of members and the ANN similarity (Tanimoto using Daylight fingerprints) as an indication of the diversity of the collection are recorded. This is followed, for each method, by the number of clusters and singletons, the size of the largest single cluster and the purity of that cluster. An ideal result would be a single pure cluster with no singletons for each grouping of interest.

Results

The first three classes have large and common ring templates. They show a decreasing level of internal similarity as measured by their mean nearest neighbor similarities. The tetracyclines, with their unique and characteristic template are efficiently grouped and discriminated by all methods. The smaller and somewhat more diverse dihydropyridines are also effectively grouped by all methods except for one analog which is clearly a substantial structural variant from the rest and is a singleton in all methods. The RASCAL method also fails to include one additional analog which is grouped appropriately by all the other methods. This compound, nilvadipine, differs from all the others by having one of the ring methyl groups replaced by a cyanide group. The common substructure method might have been expected to be the most sensitive to this minor structural change. The angiotensin-2 antagonists show a very low internal similarity by fingerprint methods: clustering based on fingerprints might hence be expected to find these too far apart to group, in spite of the presence of the biphenyl tetrazole as a large common substructure. Indeed, the Ward's method fails to group these compounds at all, while the Jarvis-Patrick and CAST/Daylight methods do find a subset of three compounds to group. These compounds, however, are grouped with other non-class compounds as shown by the low purity of the clusters. The commonality that is keyed upon appears to be a smaller fragment related to

the benzyl imidazole moiety rather than the "pharmacophoric" biphenyl tetrazole. This is deduced by examining the non-class compounds retrieved. The RASCAL method does what is expected and groups all five appropriately.

The next two groups represent therapeutic groupings which each contain two clearly recognizable structural subclasses. In the case of the antifungals, the two classes have very little in common structurally. The conazoles, all of which are characterized by an elaborated phenethyl imidazole or triazole moiety are grouped cleanly by all methods. However, the Jarvis-Patrick method is the only one to get all of them into one cluster. Ward's method fails to include four which appear as singletons, while the two CAST methods break this group into two or three clusters, respectively, with RASCAL generating the most partitions. The four compounds of the nitroimidazole subclass are grouped into a single cluster by all methods except RASCAL which misses one as a singleton. In this group, there is one extraneous compound included by all methods. Upon examination, this turned out to be an antitumor candidate which also contained the nitroimidazole moiety and which was otherwise quite similar to the compounds in this subset. The Jarvis-Patrick and CAST/Daylight methods also put these same five compounds cleanly into their own cluster, while Ward's method failed to discriminate them from a large number of other small compounds. The extra compound included is correct from a chemical viewpoint, if not from a biological one.

The β -lactam antibiotics are slightly more complicated in that, in addition to the well recognized subclasses of the cephalosporins and penicillins, which themselves have a high degree of internal similarity, there are five additional β -lactams more distantly related structurally. The internal similarity, except for the miscellaneous class, is much higher than for the antifungal subclasses. Here, there is a clear difference between the CAST methods and the Ward's or Jarvis-Patrick methods: the former tend to group the two subclasses together, with CAST/Daylight being more efficient (one clean cluster as against three or two for RASCAL on cephalosporins or penicillins, respectively). Ward's gives a high number of singletons for both subclasses as well as multiple clusters; Jarvis-Patrick gives one clean cluster for all cephalosporins and three for the penicillin analogs. Neither of these latter methods mixes penicillins and cephalosporins at the default settings selected. The miscellaneous class compounds are either singletons or members of

larger, undifferentiated clusters in all methods. Surprisingly, RASCAL generated more subclusters than expected. This is basically "subsetting" of the sort more commonly observed in Ward's method (as seen here also). However, not all of these smaller clusters contain the same compounds across methods.

Peptide-like drugs represent a challenge for automated series organization methods. We examined the behavior of these methods with the set of 17 ACE inhibitors present in the collection. Interestingly, Jarvis-Patrick gave the best result. It grouped 12 of the 17 into one cluster with only two other non-class compounds. A subset of four, also segregated by all of the other methods, was grouped into a second class which, however, was not very pure (22%). Captopril was a singleton. The small class of four was cleanly found by Ward's, but not by CAST/Daylight (38%). RASCAL groups a different subset of 13 together, but at low purity (50%). The non-class compounds in each case are primarily non-peptide drugs, not compounds from other peptide classes. The operational commonality keyed on appears to be related to the region of the ACE inhibitors including the phenylalanine-derived moiety.

As a final example, the structurally complex class of opiate drugs was examined. This collection does not include any of the peptide opiates, and the one kappa compound was excluded from the comparison leaving 37 compounds. Not unexpectedly, all methods split this collection into several clusters. Both Ward's and Jarvis-Patrick isolated clusters of ten and eight compounds that cleanly contained natural product analogs related to morphine. In addition, a smaller clean cluster of four compounds with related polycyclic structures was found. The two CAST methods gave larger single clusters (23 for CAST/Daylight and 24 for RASCAL), which grouped the compounds in all three of these clusters together, but at the expense of including non-class compounds (purities of 72% for CAST/Daylight and 57% for RASCAL). Examination of the incorrect compounds surprisingly showed that several estrogenic compounds had been included. This led to the conclusion that the substructure keyed upon by the CAST methods isolated the phenol and alicyclic carbon ring systems but did not include the tertiary piperidine substructure characteristic of the opiate analgesics. The remaining compounds in this class are the simplified piperidine analogs of morphine. Small subsets of these are isolated by the fingerprint methods, but most fall into undifferentiated clusters in all methods.

Discussion

Several conclusions can be drawn from the observations above. When series are characterized by relatively large or unique ring templates, all methods tend to group their members effectively. There is a suggestion that the RASCAL method may do a better job if the internal fingerprint similarity of the collection to be grouped drops too low (angiotensin antagonists). The β -lactams and opiates illustrated an interesting difference between Ward's and Jarvis-Patrick on the one hand and the two CAST methods on the other. The former methods achieved a finer but cleaner grouping of related structures of high complexity at the cost of generating a larger number of clusters, whereas the two CAST methods found regions of commonality that could consolidate these subgroups, but at the expense of purity or diminished coverage. This suggests that further examination of the appropriate option settings for the latter methods may be necessary to tune these for particular types of structures. We already know that this is the case for the betterstudied Ward's and Jarvis-Patrick methods, especially when applied in a single pass to datasets with high structural diversity. In particular, the Ward's/Kelley method we have used typically chooses a level where there is one large cluster (30-50% of the dataset) in the first pass on datasets with the sort of diversity represented here. This accounts for the cases in Table 6 where there are very low purities for Ward's method and where recursive clustering of this large cluster is necessary to generate additional groupings for more structurally similar classes. Collections of small compounds with relatively simple structural commonality are still not easily differentiated by any of the methods. The Jarvis-Patrick method performed quite well across the board in this study, but the newly proposed CAST/Daylight method also did quite well.

The graph-based RASCAL methods generally did not perform as well as the fingerprint-based methods in partitioning this large and structurally diverse 1325-member dataset in the desired manner. Examination of the compound groupings suggests that the substructures keyed upon by this method are more akin to queries than to "series templates" in many cases, resulting in decreased purity in the groupings. A better strategy for partitioning such datasets might be to use a fingerprint method for the initial partitioning and then to apply RASCAL to the clusters to extract a more appropriate MCES for that grouping. Finally, it must be pointed out that none of

these methods can be expected in general to group compounds efficiently based on pharmacophoric patterns, even if the latter have a large topological content.

CONCLUSIONS

Most approaches to the clustering of 2D chemical databases structures have been based on similarity measures calculated using fingerprint representations of chemical structure. In this paper, we have discussed clusterings that are based on similarity measures calculated using graph-based representations. Specifically, we have applied our recent algorithm for the identification of maximum common edge subgraphs to the calculation of inter-molecular similarities based on the graph similarity coefficient of Wallis; these similarities have then been used for the implementation of several different clustering methods, with comparable experiments being carried out using a conventional, fingerprint- and Tanimoto-based similarity measure.

Two groups of experiments were carried out. The first involved an extensive series of simulations that were designed to identify the most appropriate parameter values for the various clustering methods that were studied (CAST, Jarvis-Patrick, Raymond-Willett, Yin-Chen and Ward's), and the extent to which these values were dataset-dependent. These simulations suggested that the CAST method of Ben-Dor *et al.* 22 is the most robust of those tested. The second involved consideration of the bioactivity of several sets of compounds, focusing principally on the ability of the various approaches to highlight meaningful chemical series in datasets comparable to those resulting from HTS analyses. No obvious advantage appeared to result from the use of the more sophisticated, graph-based similarity measures when compared to conventional, fingerprint-based measures.

We draw two principal conclusions from the study. First, while the results obtained from the use of graph-based similarities are different from fingerprint-based similarities, there is no evidence to suggest that one approach is consistently better than the other: each approach has its strengths and weaknesses, and it may be that an investigation should employ both approaches to obtain a fuller view of the structural relationships present within a dataset. Second, the CAST method warrants further investigation as a potential alternative to the Ward's and Jarvis-Patrick methods for the

clustering of chemical structure databases; not only has it proved effective in the evaluations carried out here, but it is also sufficiently fast to permit the processing of large chemical datasets.

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TABLES

Table 1. Characteristics of the datasets use din the parameter optimization experiments. |N|: number of compounds, $|C_1|$: number of clusters as determined by manual review, |S|: number of singletons, |MW|: average molecular weight, |R|: average number of rotatable bonds, %L: percent of compounds satisfying the Lipinski Rule of Five

Dataset	N	$ C_1 $	S	MW	R	%L	Source	Comments
NCI-A	55	7	4	306	2.5	98	NCI Anti-HIV database	distinct but similar clusters
NCI-B	79	5	2	424	10.1	78	NCI Anti-HIV database	distinct but similar clusters
NCI-C	564	45	198	439	6.9	77	NCI Anti-HIV database	more subjective clusters than for NCI-A and NCI-B
NCI-D	194	21	73	421	7.0	78	NCI Anti-HIV database	random subset of NCI-C
PD-X	305	29	43	361	5.3	92	Pfizer compound library	diverse set found active in HTS
PD-Y	345	13	7	389	6.0	96	Pfizer combinatorial compound	derived from a single scaffold
PD-Z	538	68	18	441	10.5	97	Pfizer combinatorial compound	derived from a single scaffold
ID-1	358	68	41	373	6.5	100	ID-Alert database	collection of closely related and loosely related clusters
ID-2	262	43	24	367	5.4	100	ID-Alert database	collection of closely related and loosely related clusters

Table 2. Dataset similarities calculated using the Tanimoto coefficient and Daylight fingerprints. ANN: average nearest neighbor, AFN: average farthest neighbor, AAN: average of all neighbors

Data	Sel	Self-Similarity									
Set	ANN	AFN	AAN								
NCI-A	0.818	0.077	0.242								
NCI-B	0.916	0.133	0.401								
NCI-C	0.693	0.027	0.171								
NCI-D	0.616	0.055	0.169								
PD-X	0.739	0.082	0.197								
PD-Y	0.940	0.425	0.623								
PD-Z	0.922	0.223	0.439								
ID-1	0.708	0.059	0.194								
ID-2	0.714	0.076	0.201								

Table 3. Optimal Daylight fingerprint clusterings. In this table, the objective function scores are highlighted in italics next to the corresponding adjustable parameter value. Jaccard coefficients have been multiplied by 100 so that they range from 0 to 100

			PD	-X	PD	-Y	PD	-Z	NCI	-A	NCI	[-B	NCI	-C	NCI	-D	ID	-1	ID	-2	
Word's	Jaccard	Kallay	Kallan 17.4		22.8		38.6		66.4		30.9		12.8		10.9		4.6		7.2		
walu s	Gusfield	Kelley	200		21	212		246		14		41		329		115		256		175	
CAST	Jaccard	+	0.344	53.0	0.715	48.5	0.765	54.7	0.355	96.0	0.379	100	0.407	81.6	0.353	77.1	0.486	28.7	0.410	43.9	
Gus	Gusfield	l	0.285	103	0.713	104	0.766	147	0.355	5	0.379	2	0.347	226	0.331	77	0.472	148	0.473	85	
VC	Jaccard	y_t	0.617	47.0	0.902	47.1	0.946	53.6	0.373	96.1	0.633	100	0.692	84.8	0.683	86.7	0.799	20.4	0.720	58.3	
1-0	Gusfield		0.609	121	0.945	140	0.937	188	0.375	5	0.639	2	0.633	222	0.659	79	0.774	186	0.720	78	
	Incourd	k	19 16.2	11 46.0	10	61.2	11	012	37	00 /	30	72.2	13	71.0	10	26.0	32	116			
J-P	Jaccalu	k_t	12	40.5	2	40.0	4	01.5	6	91.2	31	00.4	20	12.2	8	/1.9	5	20.9	22	41.0	
	Guafield	k	26	120	37	122	17	170	15	5	35	10	28	201	8	80	7 167	14	124		
	Gustiela	k_t	16	129	23	132	9	172	11	5	25		13		2	09	3	10/	9	124	

Table 4. Optimal RASCAL clusterings. In this table, the objective function scores are highlighted in italics next to the corresponding adjustable parameter value. Jaccard coefficients have been multiplied by 100 so that they range from 0 to 100.

			PD	-X	PD	-Y	PD	-Z	NCI	[-A	NC	I-B	NC	[-C	NCI	[-D	ID	-1	ID	-2
CAST Jaccard Gusfield	Jaccard	4	0.547	53.7	0.752	37.0	0.767	32.5	0.571	86.6	0.511	99.5	0.518	50.1	0.513	60.2	0.584	58.2	0.537	59.6
	Gusfield	l	0.548	112	0.752	156	0.803	246	0.571	9	0.511	4	0.516	282	0.514	95	0.578	85	0.540	67
V C	Jaccard		0.879	47.7	0.937	31.6	0.966	23.7	0.633	78.7	0.633	99.5	0.828	51.0	0.826	52.7	0.874	52.9	0.871	84.4
1-0	Gusfield	y_t	0.879	138	0.935	206	0.941	307	0.633	11	0.633	4	0.810	308	0.835	104	0.875	110	0.866	59
Terrent	Incourd	k	14	50.8	15	521	14	20.1	14	04.0	38	70.2	33	197	15	50.0	28	12 2	22	12 2
ТD	Jaccaru	k_t	k_t 5	50.8	6	55.1	7 59.	39.1	39.1 3	94.0	7	19.2	9	40.7	4	50.0	6	42.3	6	42.3
J-F	Guafiald	k	15	158	15	126	<u>16</u> 8 250	14	12	38	18	9	250	7	120	25	170	18	120	
	Gustielu	k_t	5		6	130		3	3 12	7	10	2	2 339	2	150	4	170	2	139	
	Incourd	S_a	0.909	52.5	0.925	20.1	0.906	24.0	0.902	86.6	0.870	011	0.910	15 7	0.965	571	0.881	62.6	0.859	66.6
R-W Gusfi	Jaccaru	S_b	0.555	52.5	0.620	39.1	0.598	24.9	0.533	80.0	0.540	01.1	0.528	0.528 45.7	0.491	57.1	0.610	05.0	0.479	00.0
	Guafiald	S_a	0.909	120	0.967	142	0.920	0.902	0	0.870	10	0.904	205	0.960	102	0.833	0.833	0.896	60	
	Gustiela	S_{b}	0.430	120	0.455	145	0.496	224	0.533	5	0.540	10	0.638	305	0.489	102	0.597	0.597 09	0.482	00

				#Clusters/	#Singletons	5	Largest cluster Purity of largest cluster(%)				·(%)	Comments			
Class	N	ANN	Ward/ Kelley	JarPat (6:10)	CAST/ Daylight	CAST/ RASCAL	Ward/ Kelley	JarPat (6:10)	CAST/ Daylight	CAST/ RASCAL	Ward/ Kelley	JarPat (6:10)	CAST/ Daylight	CAST/ RASCAL	
Tetracyclines	8	0.950	1/0	1/0	1/0	1/0	8	8	8	8	100	100	100	100	
Ang2-1 antags	5	0.553	0/5	1/2	2/0	1/0	1	3	3	5	-	43	75	100	
Dihydropyridines	13	0.777	1/1	1/1	1/1	1/2	12	12	12	11	100	100	100	100	One cmpd is singleton in all methods
Antifungasl	11	0.690	2/4	2/0	3/0	4/1		4	4	2		80	80	75	All methods include a nitroimidazole antitumor
Nidazoles	4	0.010	1/0	1/0	1/0	1/1	4	4	4	ა ი	100	6U 100	60 100	100	agent
β-lactams	50	0.842	5/12	6/3	3/3	4/4	16	22	45	38*	100	100	90	76	*One cmpd from misc class included (loracarbef)
Cephalosporin	22	0.874	3/4	1/0	1/0	3/0	12	22	45	17	100	100	49	45	Smaller clusters are also pure in all methods
Penicillin	23	0.895	2/3	3/0	1/0	2/1	16	17	45	20	100	100	49	53	Not grouped together or with
MISC.	5	0.453	0/5	2/3	2/3	2/3	1	1	2	1	-	13	50	33	other b-lactam clusters
ACE inhibitors	17	0.797	2/5	2/1	4/2	3/0	8	12	8	13	1	86	26	50	
Opiates	37(38)	0.856	4/5	9/5	5/2	4/2	11/10/8	10/8	23	24	2/100/100	100/100	72	57	Largest clusters contain morphine analogs; small clusters are<50%pure for CAST methods

Table 5. Results of manual inspection of the various clusterings of the 1325-member dataset.

Table 6.	List of com	pounds in eac	h of the seven	activity classes.
10010 01	Dist of \$0111			

Ang2 antagonists	<u>β-lactams</u>	cephapirin	Opiates	
candesartan	aztreonam	cephradine	acetylnormethadol	
irbesartan	clavulanic_acid	amdinocillin	alfentanil	
losartan	imipenem	amoxicillin	buprenorphine	
valsartan	loracarbef	ampicillin	butorphanol	
Proprietary compound	moxalactam	azidocillin	butylmorphine	
	cefaclor	carbenicillin	codeine	
Dihydropyridines	cefadroxil	carbenicillin_indanyl	dextromethorphan	
amlodipine	cefamandole	carbenicillin_phenyl	dezocine	
felodipine	cefatrizine	cloxacillin	dihydrocodeine	
isradipine	cefazolin	cyclacillin	ethylmorphine	
lacidipine	cefdinir	dicloxacillin	etorphine	
nicardipine	cefixime	flucloxacillin	fentanyl	
nifedipine	cefmetazole	hetacillin	heroin	
niguldipine	cefoperazone	methicillin	hydrocodone	
nilvadipine	cefotaxime	nafcillin	hydromorphone	
nimodipine	cefoxitin	oxacillin	ketobemidone	
nisoldipine	cefpodoxime	penicillin_G	levallorphan	
nitrendipine	cefprozil	penicillin_V	meperidine	
oxodipine	ceftriaxone	piperacillin	meptazinol	
Proprietary compound	cefuroxime	piridicillin	methadone	
	cefuroxime_axetil	pivampicillin	methadyl_acetate	
ACE inhibitors	cephacetrile	sulbenicillin	morphine	
benazepril	cephalexin	ticarcillin	nalbuphine	
candoxatril	cenhaloglycin	Proprietary	nalmefene	
CandoXadin	eepitatogryein	compound		
captopril	cephalothin		nalorphine	
cilazapril		<u>Antifungals</u>	naloxone	
enalapril	<u>Tetracyclines</u>	benznidazole	naltrexone	
enalaprilat	chlortetracycline	metronidazole	oxycodone	
fosinopril	demethylchlortetracycline	misonidazole	pentazocine	
indolapril	doxycycline	tinidazole	pholcodine	
lisinopril	methacycline	econazole	prodilidine	
moexipril	minocycline	fluconazole	profadol	
moexiprilat	oxytetracycline	itraconazole	propiram	
perindopril	rolitetracycline	ketoconazole	propoxyphene	
quinapril	tetracycline	miconazole	sufentanil	
quinaprilat		sertaconazole	tilidine	
ramipril		voriconazole	Proprietary compound	
trandolapril				
zofenoprilat				

FIGURES



Figure 1. Example MCES for two chemical graphs