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1 Investigation of particle radiation and its effect on NO
2 prediction in a pilot-scale facility for both air and
3 oxy-coal combustion

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9 **Abstract**

10 Radiation heat transfer plays an important role in pulverised coal combus-
11 tion, influencing the overall combustion efficiency, pollutant formation and
12 flame ignition and propagation. In this paper, the radiation properties of the
13 particles as well as gas property models on the overall influence of the predic-
14 tion of the formation of NO_x pollutants in a pulverised coal combustion have
15 been investigated. The non-grey weighted sum of grey gases (WSGG) model
16 has been employed to calculate the radiation of the gas phase coupled with
17 the radiation interaction from the particulate phase. The Mie theory, as well
18 as constant or linear models, have been employed to describe the particle
19 radiative properties. The prediction results, calculated from the data from
20 a 250 kW pilot scale combustion test facility (CTF), are compared against
21 experimental measurements under air-fired condition and a range of oxyfuel
22 conditions. The results show that the choice of radiation solution can have
23 a considerable impact on the radiative heat transfer results, in which the
24 Mie theory shows a significant improvement in the incident wall heat flux

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25 compared to the constant or linear models. Also, the more accurate solution
26 employed for radiation of gases and particles considerably improves the NO_x
27 prediction in the flame region.

28 *Keywords:* Radiative heat transfer, oxyfuel, combustion

29 **1. Introduction**

30 Although the global consumption of coal has undergone slower growth
31 in recent years, coal is still expected to remain 24% of primary energy con-
32 sumption in 2035 [1]. With increasing regulations focused on environmental
33 protection, coal combustion modelling has received special attention for its
34 potential role in reducing the environmental impact of utilising coal combus-
35 tion, such as retrofits of traditional power plants and new designs of coal fired
36 power plants for oxyfuel combustion, one of the main technologies for CO_2
37 capture. Radiation heat transfer is important in pulverised coal combustion
38 because of the high temperatures reached within combustion furnaces, as
39 well as the presence of participating species such as $\text{CO}_2/\text{H}_2\text{O}$, and solid-
40 phase coal, char and fly-ash particles [2, 3]. The characteristics of radiative
41 heat transfer under oxyfuel combustion are different from those of air-fired
42 combustion, due to the higher concentration of participating species and
43 potentially higher temperatures at elevated oxygen concentrations. Accu-
44 rate calculations, taking into account the impact of the variable combustion
45 medium, is considered to be a priority for retrofitting an existing unit to oxy-
46 fuel while maintaining similar temperatures and heat transfer characteristics
47 [4, 5]. The accuracy in radiative modelling of the combustion process has a
48 large effect on the overall prediction of the combustion efficiency, pollutant

49 formation and flame ignition and propagation. Accurate radiation modelling
50 needs to consider both gaseous phase and particulate participation in the
51 radiative mechanism. With the dominance of the radiative heat transfer of
52 the particles compared to that of the gases in pulverised coal combustion,
53 more attention needs to be focused on the radiative properties of particles
54 [5].

55 The global gas property model which has been a preferred selection for
56 complex combustion modelling, mostly due to its low computational expense,
57 is the weighted sum of grey gases (WSGG) model. The first WSGG model
58 applied for non grey media was proposed by Hotel and Sarofim [6] for use with
59 the zonal method, and it has been demonstrated by Modest [7] for application
60 as an arbitrary solution method. A widely used set of fitted coefficients for
61 the WSGG model for combustion gases, absorption coefficients and weighting
62 factors, was proposed by Smith [8]. However, these values were obtained at
63 specific mole fraction ratios of H_2O and CO_2 , which limits the use of these
64 coefficients under oxyfuel conditions. This limitation was improved by Yin
65 [9] for a wider range of discrete ratios and by Johansson [10] for a variable
66 and wide range of CO_2 and H_2O ratios that better presented the radiative
67 properties of the gas products for both air and oxyfuel combustion. One
68 of the most recent set of coefficients for the WSGG model was developed
69 by Kangwanpongpan [11], which was evaluated using the HITEMP 2010
70 spectroscopic database [12] for a wide range of CO_2 and H_2O ratios, and was
71 chosen in this paper to describe the properties of non-grey gases.

72 The presence of the particles in coal-fired combustion has a significant
73 effect on the radiative heat transfer mechanism [13, 14]. The radiative prop-

74 erties of the particles are complicated to define and depend on the particle
75 composition, size, and the wavelength of the incoming radiation, and vary
76 during the particle’s trajectory through the furnace. Therefore, the account-
77 ing of the properties of the particles, namely emissivity and scattering coeffi-
78 cients, are conventionally simplified to be constant values in most simulation
79 studies [15, 16]. It is necessary to employ global models for the radiative prop-
80 erties of gas-phase species in coupled computational fluid dynamics (CFD)
81 calculations, which discard spectral fidelity in order to solve the radiative in-
82 tensity field for integral values. With this disregard of the spectral locations,
83 it is necessary to couple the particulate radiative properties into the global
84 radiation property models using grey particle values.

85 The emission of nitrogen oxides from combustion systems is a significant
86 pollutant source that is threatening the global environment. Mechanisms
87 of NO_x formation and destruction processes in combustion systems are very
88 complicated [17]. As NO_x species are trace species within the domain, the
89 formation of the pollutants does not significantly affect the fluid dynamics or
90 heat transfer of the combustion process, and so can be calculated as a post-
91 processing step. This means that the accuracy in the predictions of flame
92 temperature, volatile release, char burnout and aerodynamics are prerequi-
93 sites to the prediction of NO_x formation [18]. This study will determine the
94 sensitivity of the NO_x prediction to the choice of the radiation models.

95 The grey radiative properties for the gas and particles has been widely
96 used in CFD modelling of pulverised coal combustion under oxyfuel condi-
97 tions. Applying non-grey WSGG models can be found in some studies for
98 pilot-scale [19, 20] and for large-scale furnaces [21, 22]. However, in these

99 studies, radiative properties of particle are assumed as constants. The pur-
100 pose of this paper is to investigate the radiative heat transfer in pulverised
101 coal combustion, focusing on the particle radiation and how this affects NO_x
102 predictions. The non-grey WSGG model [11] was employed to describe the
103 radiation of the gas and the Mie theory was used to describe the particle
104 radiative properties. The modelling results were compared against the ex-
105 perimental data from [23] and experimental measurements for in-flame NO
106 concentrations, which were obtained under air-fired and oxy-fired conditions.

107 2. Numerical model

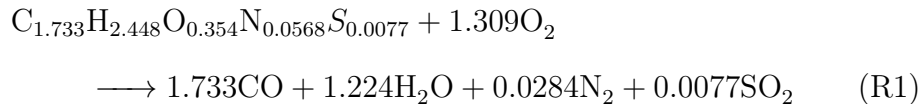
108 The commercial computational fluid dynamics (CFD) software ANSYS
109 FLUENT v17.0 has been employed to simulate the PACT 250 kW air/oxy-
110 fired CTF, which is part of the UKCCSRC PACT Core Facilities. The cylin-
111 drical furnace has an internal diameter of 0.9 m and is 4 m high. The furnace
112 is lined with a 0.1 m thick refractory and the first 3 m are water cooled. The
113 burner is a scaled version of a commercially available low- NO_x burner, which
114 has been scaled to 250 kW_{th} and provided by Doosan Babcock. The primary
115 stream and coal are supplied through a primary annulus and the secondary,
116 tertiary annuli supply the majority of the swirled oxidiser. More details
117 about the facility can be found in [24]. The properties of the coal investi-
118 gated are shown in Table 1 and the operating conditions for both the air- and
119 oxy-fired environments are listed in Table 2. The O_2 concentration in each
120 case is also shown in Table 2, where the balance of gas composition is taken
121 to be N_2 in the air case and CO_2 in the oxyfuel cases. Both cases were set
122 up with a thermal load of 200 kW. User defined functions (UDFs) were used

123 to customise the radiative property models of the gas and particle phases.
124 Three conditions have been considered, a baseline air-fired combustion case
125 and two oxyfuel regimes, Oxy-27 (overall 27 vol.% O₂ and 73 vol.% CO₂
126 in the oxidiser) and Oxy-30 (overall 30 vol.% O₂ and 70 vol.% CO₂ in the
127 oxidiser).

128 All of the cases presented in this study were calculated using a RANS
129 approach, using the Reynolds stress model of Launder et al. [25] to model
130 the unclosed terms. The Reynolds stress model has been found to produce
131 better prediction results for the temperature and oxygen concentration in
132 the recirculation zone [26] and better predictions of NO_x [27] than that when
133 using the k- ϵ model. The particle size distribution is modelled using a Rosin
134 Rammler distribution, where the mean particle diameter is 120 μm , and a
135 spread parameter of 1.1. A total of forty particle diameters were used to
136 describe the particle size distribution, resulting in 19,380 particle tracks for
137 every 100 fluid iterations. Using more diameters did not change the solution.

138 The CTF was modelled using one quarter of the full geometry, exploit-
139 ing the rotational symmetry of the furnace, resulting in a structured mesh
140 containing about 1.4 million hexahedral cells. The heat flux through the fur-
141 nace wall was modelled as a thin wall boundary condition, with the furnace
142 wall thickness of 0.1 m having outer temperature of 350 K, and an internal
143 emissivity of 0.8 [24]. The inlet and outlet surfaces were assumed to have
144 an emissivity of 1. The single kinetic rate [28] was used to describe the de-
145 volatilisation of the coal particles, with the pre-exponential factor of 14,841
146 s⁻¹ and an activation energy of 35.3 kJ/mol. A two-step global reaction
147 mechanism was employed for the homogeneous combustion of an empirically

148 defined volatile species, reactions (R1) and (R2), and the eddy dissipation
 149 model was used for the turbulence-chemistry interaction:



150

151 The surface char combustion reaction is described by the Smith intrinsic
 152 model [29], with kinetic parameters from [30]: a pre-exponential factor of
 153 $4 \times 10^{-4} \text{ kg}/(\text{m}^2 \cdot \text{s} \cdot \text{Pa})$ and an activation energy of 66 kJ/mol.

154 2.1. Radiative heat transfer

155 The radiative properties of the gas are described by the non-grey WSGG
 156 model, in which the total emissivity, ε , is the total weighted sum of grey gas
 157 emissivities, as

$$\varepsilon = \sum_{i=0}^{N_g} a_{g,i} (1 - e^{-\kappa_{g,i}s}) \quad (1)$$

158 where N_g is the number of grey gases, $a_{g,i}$ and $\kappa_{g,i}$ are the emissivity
 159 weighting factor and absorption coefficient for the i^{th} grey gas, respectively,
 160 s is the path length. The radiation transfer equation (RTE) for the i^{th}
 161 grey gas through a medium of a mixture of the non-grey gases and the grey
 162 particles is expressed as follows:

$$\begin{aligned} \frac{dI_i(\vec{r}, \vec{s})}{ds} = & -(\kappa_{g,i}(\vec{r}) + \kappa_p(\vec{r}) + \sigma_p(\vec{r})) I_i(\vec{r}, \vec{s}) + a_{g,i}(\vec{r}) \kappa_{g,i}(\vec{r}) I_{b,g}(\vec{r}) \quad (2) \\ & + E_{p,i}(\vec{r}) + \frac{\sigma_p(\vec{r})}{4\pi} \int_{4\pi} I_i(\vec{r}, \vec{s}') \Phi(\vec{s} \cdot \vec{s}') d\Omega' \end{aligned}$$

163 where $E_{p,i}(\vec{r})$ is the emission of the particles corresponding to the i^{th} grey
164 gas at position \vec{r} , $I_i(\vec{r}, \vec{s})$ is the radiative intensity at location \vec{r} travelling in
165 direction \vec{s} , $I_{b,g}(\vec{r})$ is the black body intensity calculated at the temperature
166 at position \vec{r} , $\sigma_p(\vec{r})$ is the scattering coefficient of particles, $\Phi(\vec{s} \cdot \vec{s}')$ is the
167 scattering phase function and Ω' denotes solid angle. The non-grey WSGG
168 model [11] is applied with 4 grey gases and 1 transparent gas ($\kappa_{g,0} = 0$).
169 Therefore, 5 RTEs, as shown in Eq.(2), have been solved, with the weighting
170 factors and the absorption coefficients for the gas as follows:

$$a_{g,i}(\vec{r}) = \sum_{j=1}^{N_c} c_{ij} \left(\frac{T_g(\vec{r})}{T_{ref}} \right)^{j-1}, i = 1, 2, \dots, N_g, \quad a_{g,0} = 1 - \sum_{i=1}^{N_g} a_{g,i}(\vec{r}) \quad (3)$$

$$\kappa_{g,i} = K_{g,i} P (Y_{\text{H}_2\text{O}} + Y_{\text{CO}_2}) \quad (4)$$

171 where c_{ij} , K_{gi} are the temperature dependent polynomial coefficients, N_c , N_g
172 are the number of polynomial coefficients and the number of grey gases,
173 respectively, P is the total pressure of the gas, and $Y_{\text{H}_2\text{O}}$, Y_{CO_2} are the molar
174 fractions of H_2O and CO_2 , respectively.

175 The grey WSGG model is often used in combustion modelling. In this
176 case, the properties of the gas is represented by the effective absorption co-
177 efficient and the number of RTE solutions required is reduced to one. The

178 effective absorption coefficient of the grey gas is calculated from the total
 179 emissivity, ε , and path length, s , as [31]

$$\kappa_g = -\frac{1}{s} \ln(1 - \varepsilon) \quad (5)$$

180 where ε is determined by Eq. (1) with the path length, s , being considered
 181 as a mean beam length of the domain. The mean beam length is often
 182 determined from the volume of the domain, V , and the internal surface of
 183 the domain, A , as [32]

$$s = 3.6 \frac{V}{A} \quad (6)$$

184 Using the mean beam length obtained from Eq. (6) for the grey WSGG
 185 model has been found to give considerably different heat flux results com-
 186 pared to those of the non-grey WSGG model in some cases [31, 33]. The RTE
 187 for the non-grey WSGG model, Eq. (2), is rewritten for the grey gas WSGG
 188 model, with the weighting factors for the gas and particles being unity, as

$$\begin{aligned} \frac{dI(\vec{r}, \vec{s})}{ds} = & -(\kappa_g(\vec{r}) + \kappa_p(\vec{r}) + \sigma_p(\vec{r})) I(\vec{r}, \vec{s}) + \kappa_g(\vec{r}) I_{b,g}(\vec{r}) + E_p(\vec{r}) \\ & + \frac{\sigma_p(\vec{r})}{4\pi} \int_{4\pi} I(\vec{r}, \vec{s}') \Phi(\vec{s}, \vec{s}') d\Omega' \end{aligned} \quad (7)$$

189 The particle effects are accounted for in Eqs.(2) and (7) with equivalent
 190 absorption coefficient κ_p , scattering coefficient σ_p and the equivalent emission
 191 $E_{p,i}$ being defined as follows:

$$\kappa_p = \lim_{V \rightarrow 0} \sum_{n=1}^N Q_{abs,n} \frac{A_{p,n}}{V} \quad (8)$$

$$\sigma_p = \lim_{V \rightarrow 0} \sum_{n=1}^N Q_{sca,n} \frac{A_{p,n}}{V} \quad (9)$$

$$E_{p,i} = \lim_{V \rightarrow 0} \sum_{n=1}^N a_{pi,n} I_{bp,n} Q_{abs,n} \frac{A_{p,n}}{V} \quad (10)$$

192 where N is the number of particles within the volume V , $a_{pi,n}$ is the
 193 weighting factor for the i^{th} grey gas, being determined from Eq. (3) with
 194 replacing T_g by the temperature of the n^{th} particle $T_{p,n}$, $I_{bp,n}$ is the black body
 195 intensity at the temperature of particle n , and $A_{p,n}$ is the projected area of the
 196 n^{th} particle. The summation over N particles is calculated during the particle
 197 tracks, where the number of particles is accounted for by the residence time of
 198 a trajectory through a control volume multiplied by the number of particles
 199 per second that trajectory represents. The particle radiative properties alter
 200 the heat exchange between the particles and the boundaries and gas phase,
 201 by modifying the radiation intensity field and affecting the heat available
 202 for convective transfer between the phases, which inherently modifies the
 203 gas temperature, combustion kinetics and fluid dynamics, which means that
 204 a fully coupled approach such as CFD is required to fully incorporate the
 205 impact of these properties on pollutant formation. The absorption efficiency
 206 $Q_{abs,n}$ and the scattering efficiency $Q_{sca,n}$ are calculated from the Mie theory
 207 [34] using the Planck mean values as follows:

$$Q_{abs,n}(T) = \frac{\int_0^\infty Q_{abs\lambda} e_{b\lambda}(T) d\lambda}{\int_0^\infty e_{b\lambda}(T) d\lambda} \quad (11)$$

$$Q_{sca,n}(T) = \frac{\int_0^\infty Q_{sca\lambda} e_{b\lambda}(T) d\lambda}{\int_0^\infty e_{b\lambda}(T) d\lambda} \quad (12)$$

209 where $e_{b\lambda}(T)$ is the spectral black body emissive power at the temperature
 210 T . $Q_{abs\lambda}$ and $Q_{sca\lambda}$ are spectral absorption and scattering efficiencies of a
 211 particle at wavelength λ , respectively.

212 In this study, the high degree of forward scattering of the particles was
 213 treated by using a so-called zero-order delta Eddington function, which ap-
 214 plies a modified scattering efficiency scaled by the asymmetry factor, g as in
 215 [32, 35], $Q_{sca,n}^* = (1 - g)Q_{sca,n}$. The optical constants used for the calcula-
 216 tion of the refractive index of the coal particles were taken from experimental
 217 measurements for the Kentucky No. 9 coal, with the real part $n=1.8$ and
 218 the wavelength-dependent k determined within the spectral range 2-20 μm
 219 [36]. For the fly-ash particles, the wavelength-dependent optical constants
 220 measured by Goodwin [37], as parametrised by Liu and Swithenbank [38],
 221 were used. The Planck mean coefficients were pre-calculated for a range of
 222 diameters and temperatures of the particles. For each calculation of the coal
 223 and fly ash particles, the $Q_{abs,n}$ and $Q_{sca,n}$ values were obtained by employ-
 224 ing linear interpolation. The radiative properties of the burning particles are
 225 also linearly interpolated between the coal and fly ash values based on the
 226 current mass of the char in the burning particles.

227 Two other approaches for the particle radiative properties were also inves-
 228 tigated and compared to the Planck mean coefficients, namely the constant
 229 and the linear-function values. In terms of constant values, a particle ab-
 230 sorption efficiency value of 0.9 [16, 23, 39, 40] and a particle scattering factor
 231 0.6 [23, 39] for both air-fired and oxy-fired conditions are employed. The

232 particle scattering efficiency is calculated from the scattering factor, f_p , as
 233 $Q_{sca} = (1 - f_p)(1 - Q_{abs})$, resulting in a constant scattering efficiency of 0.04.
 234 For the linear-function value, the radiative properties of particles vary as lin-
 235 ear functions of the mass fraction of char and volatiles in the particles. The
 236 linear emissivity function [41], as shown in Eq. (13), and the linear function
 237 scattering factor [42], as shown in Eq. (9), are used as follows:

$$\epsilon_p = X_c + 0.6(1 - X_c) \quad (13)$$

$$f_p = 0.9X_{v,c} + 0.6(1 - X_{v,c}) \quad (14)$$

238 where X_c is the fraction of unburnt char mass, and $X_{v,c}$ is the fraction of
 239 unburnt combustibles.

240 2.2. NOx formation

241 In pulverised coal combustion, the NO_x emissions consists mostly of NO,
 242 with much lower amounts of N₂O and NO₂ [43, 44]. Therefore, only NO
 243 formation and destruction are mentioned in this study. Existing sub-models
 244 for predicting NO emissions, which have been developed for conventional air
 245 combustion, are employed in modelling for both the air- and oxy-fired con-
 246 ditions. Previous studies have shown that the NO formation and reduction
 247 mechanisms in oxyfuel combustion are fundamentally similar to those in air
 248 condition [45–47]. Significant contributions to NO formation can result from
 249 four mechanisms: fuel-NO, thermal-NO, prompt-NO and N₂O mechanisms.
 250 The fuel-NO mechanism is the dominant source of NO formation in coal-fired
 251 systems, being responsible for approximately more than 80% of the total NO

252 formation [44, 48, 49], while the formation from the prompt-NO and N_2O
253 mechanisms can often be neglected [50]. The NO destruction includes a re-
254 burning mechanism and the heterogeneous reaction of NO with the carbon
255 atoms on the char surface. Fig. 1 illustrates a simple NO formation and
256 destruction pathway that is employed in this paper.

257 The fuel-NO mechanism occurs from the oxidation of fuel-bound nitro-
258 gen which is released from the fuel devolatilisation, called volatile-N, and
259 the nitrogen remains in the char, called char-N. The volatile-N converts to
260 intermediate nitrogen compounds, primarily HCN and NH_3 , which are then
261 oxidised to form NO. The char-N converts directly to NO from oxidised
262 char-N atoms or partly converts to intermediate nitrogen compounds which
263 is then converted partially to NO. As a results, the formation from char-N
264 is proportional to the carbon burnout. The volatile-N is dominant of NO
265 formation due to 70-90% of coal nitrogen converts to volatile under the de-
266 volatilisation precess [17, 51] and 60-80% of NO formation from the volatile-N
267 in regular pulverised coal combustion [51, 52].

268 Thermal-NO is formed from the oxidation of atmospheric nitrogen in rel-
269 atively high-temperature environment and this mechanism is strongly tem-
270 perature dependent. The formation of NO under this mechanism is described
271 by the extended Zeldovich mechanism. Themal-NO occurs in air-coal com-
272 bustion and can result in about 25% of the total NO emission [53], and this
273 mechanism is almost eliminated under oxy-fired condition where nitrogen is
274 replaced by CO_2 . The reactions governing the formation of the thermal-NO
275 mechanism are expressed as follows:



276 The net rate of thermal-NO formation is expressed as

$$\begin{aligned} \frac{d[\text{NO}]}{dt} = & k_{f1}[\text{O}][\text{N}_2] + k_{f2}[\text{N}][\text{O}_2] + k_{f3}[\text{N}][\text{OH}] \quad (15) \\ & - k_{r1}[\text{NO}][\text{N}] - k_{r2}[\text{NO}][\text{O}] - k_{r3}[\text{NO}][\text{H}] \end{aligned}$$

277 where k_{f1}, k_{f2}, k_{f3} are the rate constants for the forward reactions (R3)-
 278 (R5), respectively. The rate constants for the reverse reactions are k_{r1}, k_{r2}, k_{r3} .
 279 The forward and reverse rates from this study were employed from [54] as
 280 shown in Table 3.

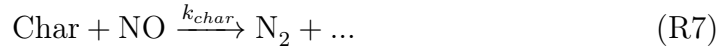
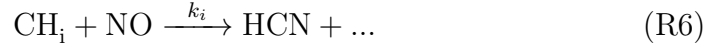
281 When assuming that the rate of consumption of free N atoms becomes
 282 equal to the rate of its formation, the overall rate for the three reversible
 283 reactions (R3)-(R5) can be expressed as [55]

$$\frac{d[\text{NO}]}{dt} = 2[\text{O}] \left(\frac{k_{f1}[\text{N}_2] - \frac{k_{r1}k_{r2}[\text{NO}]^2}{k_{f2}[\text{O}_2]}}{1 + \frac{k_{r1}[\text{NO}]}{k_{f2}[\text{O}_2] + k_{f3}[\text{OH}]}} \right) \quad (16)$$

284 The concentration of O and OH atoms can be estimated using equilibrium
 285 or partial equilibrium assumptions.

286 The NO destruction mechanisms occur when NO reactions with CH_i rad-
 287 icals, named reburning, and the heterogeneous reaction of NO with the car-
 288 bon atoms on the char surface. The destruction mechanisms are expressed

289 by a general reaction (R6) and heterogeneous reaction (R7), respectively, as
290 follows:



291 where CH_i are the hydrocarbon species, $i=1, 2, \text{ or } 3$, depending on the
292 hydrocarbons used in the flame, and k_i and k_{char} are the rate constants for
293 reactions (R6) and (R7), respectively.

294 In this paper, 80% of the coal nitrogen is assumed to be released with the
295 volatiles-N and 20% of the nitrogen is bound with char. The volatile-N con-
296 verts to HCN and NH_3 as intermediate species at 55% and 10%, respectively,
297 with the rest of the volatile-N forms directly to NO. A similar partition of
298 the intermediate species has been examined on a pulverised coal combustion
299 and showed a good agreement with the experiment data [56]. The char-N
300 is directly converted to NO [57]. The partial equilibrium approach [58] was
301 selected for the reburning solution with CH_4 selected as the best equivalent
302 fuel after examining different equivalent fuels CH_i ($i=1-4$).

303 *2.3. Measurement techniques and methods*

304 The PACT 250 kW air/oxy-fired CTF was designed with detailed mea-
305 surement and characterisation capabilities, and a range of techniques were
306 used to obtain a detailed assessment of the oxyfuel combustion process. The
307 experimental data obtained from measurement for air-fired condition and
308 different cases of oxy-fired conditions, such as Oxy-27, Oxy-30, were used to
309 evaluate the CFD study results.

310 The concentration of NO was measured at different regions within the fur-
311 nace and at the exit section of the furnace using a Signal 4000VMA chemi-
312 luminescence analyser which is based on the chemiluminescent gas phase
313 reaction between ozone and nitric oxide to give nitrogen dioxide and oxygen.
314 Approximately 10% of the NO₂ produced emission of a photon, varying in
315 wavelength between 0.6 and 0.3 micrometres. The intensity of this emission
316 is proportional to the mass flow rate of NO and is measured by a photomul-
317 tiplier tube.

318 **3. Results and discussion**

319 *3.1. Effect of radiative properties of the mixture*

320 Fig. 2 shows the radial distribution of the temperature at different posi-
321 tions along the furnace for both air- and oxy-fired conditions. Different cases
322 are implemented by employing the grey or non-grey gas radiative models cou-
323 pled with the constant, linear or Planck averaged coefficients for the radiative
324 properties of the particles. In terms of having the same radiative model for
325 the gases (grey WSGG or non-grey WSGG), there is only a small difference
326 in the temperature distribution between the cases that have constant and
327 linear radiative properties for the particles. In contrast, being described by
328 the same radiative model for the particles (constant or linear cases), the non-
329 grey gas models show higher temperature results than that of the grey gas
330 models, mainly in regions containing a higher particle concentration (such as
331 the inner recirculation zone located close to the exit of the burner) as shown
332 in Fig. 3. Temperature results for the case of the non-grey gas and the
333 Planck mean values for the particles (NGWSGG-Mie) is higher than cases

334 having constant or linear radiative coefficients for the particles (NGWSGG-
335 Const, NGWSGG-Linear). This is due to the radiative properties of the
336 particles being described by the Mie theory being the dominant scattering
337 coefficients and having significantly lower absorption coefficients, as shown in
338 Fig. 4, and consequently reducing the radiative heat loss from the particle,
339 and increasing convective heat transfer from the particles to the surrounding
340 gas. Applying the same value for the absorption efficiency of 0.9 for both
341 the coal/char and ash in the constant model results in a significantly higher
342 absorption coefficient compared to that of the Mie theory, which calculates
343 absorption efficiencies of coal and fly ash separately. The Mie theory val-
344 ues provide significantly lower absorption efficiency for the fly ash particles,
345 which, according to the limited published data on optical constant values for
346 coal and fly ash, is more physically reasonable.

347 In the near-burner region, the higher concentration of the particles in the
348 internal recirculation zone also causes a significantly higher in-flame temper-
349 ature of the non-grey WSGG cases than for the other cases described by
350 the grey gas model, while this is not found to be the situation in the outer
351 recirculation zone, where there is a lower concentration of particles. Further
352 downstream, at an axial distance of 575 mm from the exit of the burner,
353 where there is a substantial amount of fly ash with steady concentrations
354 in the radial direction, there is no fluctuation in the difference of the radial
355 temperature profiles. A similar variation trend can be seen at 3500 mm from
356 the exit of the burner in the burnout region. However, there is a similar tem-
357 perature distribution for all cases investigated in this region. The contours of
358 the temperature distribution for both the air-fired and oxy-fired conditions

359 are shown in Fig. 5. From these figures, the high-temperature flame of the
360 oxy-fired conditions are more close to the centre line of the furnace compared
361 to that of the air-fired condition. This can be a consequence of the lower vol-
362 ume flow rate of oxidant flows under the oxy-fired conditions compared to
363 that of the air-fired condition.

364 The results of this CFD study for the radiative incident wall heat fluxes
365 are shown in Fig. 6 for both air and oxy-fired conditions compared to ex-
366 perimental data from [23]. The experimental data show that the incident
367 wall heat fluxes increase quickly in the first section of the furnace, reaching
368 their peak values at about 0.5 m and 0.75 m from the burner exit for air and
369 oxy-fired conditions, respectively. The difference in the peak value's position
370 of the incident wall heat flux under the oxy-fired condition compared to that
371 of the air-fired condition can be explained by the different flame behaviour
372 under conditions investigated in this study, with the lower volume flow rates
373 of the inlet flows under oxyfuel conditions. The behaviour of the heat fluxes
374 are quite similar for both conditions in the downstream region of the furnace
375 from the axial distance of 1 m to the furnace exit. Results from CFD show
376 the same behaviours of incident wall heat fluxes compared to experimental
377 data for both conditions. The different flame behaviour, shown in Fig. 5, can
378 explain the differences in the peak positions of the heat fluxes for two condi-
379 tions. In terms of the effects of the gas and particle models to incident wall
380 heat fluxes under the CFD study for both air and oxy-fired conditions, the
381 non-grey gas model shows an improvement for the results in the flame zone
382 compared to that of the grey gas model. The GWSGG-const case and the
383 NGWSGG-Const case show over-predicted results in comparison with the

384 cases having linear coefficients for the particle radiation, namely GWSGG-
385 Linear and the NGWSGG-Linear. This is due to the reducing equivalent
386 absorption coefficients of the particles under the linear properties of the par-
387 ticles. The properties of the particles described by the Mie theory results in
388 a significantly lower incident wall heat flux but a much closer agreement with
389 the experimental data. The lower incident wall radiation is due to the Mie
390 theory cases showing a significantly lower equivalent absorption coefficient
391 and higher scattering efficient of the particles compared to the constant and
392 linear cases, as shown in Fig. 4.

393 *3.2. Effect of radiative properties on the NO_x emission*

394 The radial and central profiles of the NO concentration from the mea-
395 surement and CFD modelling for both the air- and oxy-fired conditions are
396 shown in Figs. 7 and 8, respectively. Experimental data for the cases investi-
397 gated in this study show that the NO concentration in the region close to the
398 burner in the air case is significantly higher than that in the oxy-fired con-
399 ditions. Under the oxy-fired conditions, the NO concentration at the burner
400 exit, Fig. 9, decreases by about 25% for the Oxy-27 and 30% for Oxy-30
401 cases compared to that of the air case. Because of the combustion in this
402 study using once-through O₂/CO₂ mixtures, without recycled flue gas, the
403 lower NO under the oxyfuel conditions can be explained by the missing nitro-
404 gen and potentially enhanced heterogeneous reburning because of the higher
405 CO concentration [59], as the CO concentrations are higher under Oxy-27,
406 and higher still under Oxy-30 conditions [23]. In terms of CFD modelling,
407 the influence of the NGWSGG and Mie theory values on NO prediction are
408 investigated in comparison with the standard approach for coal combustion

409 modelling (GWSGG-Const). The influence of the choice of particle models
410 on the prediction of NO emissions are also investigated. Because of the sim-
411 ilar effect of the constant and the linear models of particles on the radiative
412 heat transfer, as shown in Section 3.1, the constant model is selected to com-
413 pare to the Mie model. Figs. 7 and 8 show a comparison of the predicted
414 NO concentrations under two cases, the GWSGG-Const and NGWSGG-Mie
415 cases. Both sets of results show a similar trend and a reasonable agreement
416 with the experimental measurements, except in the inner recirculation zone
417 close to the burner. Although the NO formation/destruction mechanisms
418 employed for the oxyfuel cases in this study were originally developed for
419 air conditions, the NO prediction results for the oxy-fired cases show much
420 closer agreement with the measurements than for the air-fired case. In the
421 inner recirculation zone close to the burner, the NO distribution under the
422 NGWSGG-Mie case shows a better trend compared to that of the GWSGG-
423 Const case, with a significantly higher NO concentration. This can be due to
424 the higher temperature in the NGWSGG-Mie case subsequent to the other
425 changes in the combustion behaviour in this region, for example the lower
426 volatile concentration as shown in Fig. 10. The higher difference of NO con-
427 centration of the two cases for both the air and oxyfuel conditions at 200 mm
428 compared to that at 75 mm and 575 mm can be explained by the higher dif-
429 ference in the temperature of the two cases at this section. And this can be
430 seen more clearly in the oxyfuel case compared to the air case. Results from
431 the experiment and simulation, Fig. 9, show the same trend that the NO
432 concentration at the exit section of the air-fuel condition is higher than that
433 of the oxy-conditions. Under the air conditions, Fig. 9(a), the NGWSGG-

434 Mie case results in a significant increase in the exit NO concentration, with
435 a 21% increase compared with the experimental measurement, while the dis-
436 agreement is only 9.7% for the GWSGG-Const case. These differences are
437 much lower under the oxyfuel conditions as shown in Fig. 9(b). The higher
438 difference in the NO concentration between the NGWSGG-Mie case com-
439 pared to the GWSGG-Const under the air-fired condition compared to those
440 under the oxy-fired conditions can be explained by the NO formation from
441 the thermal mechanism, and this is almost eliminated under the oxy-fired
442 conditions.

443 **4. Summary and Conclusions**

444 This study has focused on the radiative properties of the particles for both
445 air-fired and oxy-fired coal combustion conditions, and the impact of mod-
446 elling these properties on the calculated predictions of the NO pollutants.
447 The grey and non-grey gas property models coupled with different solutions
448 for the particle properties are employed to describe the radiation heat trans-
449 fer and these results are compared against experimental data. The radiative
450 properties of the particles described by the Mie theory show a significant im-
451 provement in the incident wall heat flux. However, the temperature is much
452 higher compared to the case of having constant properties for the particles
453 in the inner recirculation region having higher coal/char particle concentra-
454 tion. Further studies need to focus on the influence of the radiation models
455 on combustion behaviours in the burner region, such as flame ignition and
456 particle combustion. This study is performed only on a pilot-scale facility
457 so the influence of the radiation models on large-scale furnace needs to be

458 investigated.

459 The non-grey WSGG coupled with the Mie theory results in a consider-
460 able improvement in the NO prediction in the burner region where containing
461 a high particle concentration of the coal/char particles, compared to those
462 from the simplified models for the gases and the particles. However, these
463 models show an over prediction of the NO concentrations at the exit section
464 of the furnace, especially for the air-fuel case. NO_x predictions can vary by
465 as much as 10% depending on choice of radiation model, due to the sensi-
466 tivity of the thermal NO_x mechanism, although this is somewhat reduced
467 when considering oxy-fired conditions. Accurate radiation modelling needs
468 to consider simultaneously the effects of other accurate sub-models in the
469 prediction of the NO formation, such as turbulence and chemical reaction
470 models. The importance of the heterogeneous reburning due to CO also
471 needs to be investigated as a potential addition to the current mechanism for
472 application to oxyfuel conditions.

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481 Nomenclature		
482	$a_{g,i}$ emissivity weighting factor for the gas	-
483	$a_{p,i,n}$ emissivity weighting factor for the n^{th} particle	-
484	A_p projected surface area of the particle	(m ²)
485	A_r pre-exponential factor	(1/s)
486	$c_{i,j}$ temperature dependent polynomial coefficients	-
487	$e_{b\lambda}(T)$ spectral black body emissive power	(W/(m ² .μm))
488	E_a activation energy	(J/kmol)
489	$E_{p,i}$ emission of the particles corresponding to the i^{th} grey gas	(W/m ³)
490	f_p scattering factor of particle	-
491	g asymmetry factor	-
492	$I_i(\vec{r}, \vec{s})$ radiative intensity of grey gas i^{th} at position \vec{r} in direction \vec{s}	(W/(m ² .sr))
493	$I_{b,g}(\vec{r})$ black body intensity of grey gas at position \vec{r}	(W/(m ² .sr))
494	$I_{bp,n}$ black body intensity of grey particle	(W/(m ² .sr))
495	$k_{g,i}$ absorption coefficient of the i^{th} grey gas	(m ⁻¹)
496	κ_p equivalent absorption coefficient of particles	(m ⁻¹)
497	$K_{g,i}$ temperature dependent polynomial coefficients	-
498	N number of particles go through volume V	-
499	N_c number of polynomial coefficients	-
500	N_g number of grey gases	-
501	P total pressure of gas	(bar)
502	Q_{abs} absorption efficiency of particles	-
503	Q_{sca} scattering efficiency of particles	-
504	Q_{sca}^* effective scattering efficiency of particles	-
505	$Q_{abs\lambda}$ spectral absorption efficiency of particles at wavelength λ	-

506	$Q_{sca\lambda}$ spectral scattering efficiency of particles at wavelength λ	-
507	R universal gas constant	(J/kmol.K)
508	T_g temperature of gas	(K)
509	T_p temperature of particle	(K)
510	T_{ref} reference temperature	(K)
511	V volume	(m ³)
512	Y_{H_2O} mole fraction of H ₂ O	-
513	Y_{CO_2} mole fraction of CO ₂	-
514		
515	Greek symbols	
516	β temperature exponential	-
517	ε emissivity of gas mixture	-
518	ε_p emissivity of particle	-
519	λ wavelength	μm
520	σ_p equivalent scattering coefficient of particles	(1/m)
521	Φ scattering phase function	-
522	Ω' solid angle	(sr)

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Table 1

Properties of El-Cerrejon coal.*

Proximate analysis (AR, wt.%)				Ultimate analysis (DAF, wt.%)					GCV(AR) (MJ/kg)
Fixed carbon	Volatiles	Ash	Moisture	C	H	N	S	O**	
53.98	35.50	2.9	7.63	80.92	5.12	1.65	0.52	11.79	29.61

* AR, as received; DAF, dry ash-free.

** Calculated by difference.

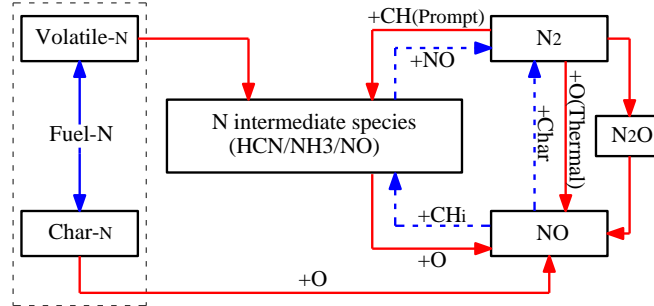
**Fig. 1:** Pathway of NO_x formation/destruction employed in the CFD prediction of NO pollutant.

Table 2

Inlet flow rates, temperature and gas concentrations that were employed for CFD calculation of the three cases (Air, Oxy-27 and Oxy-30). The balance of gas compositions for the primary, secondary and tertiary gas streams in the oxyfuel cases was CO₂.

	Air	Oxy-27	Oxy-30
<i>Mass flow rate (kg/h)</i>			
Coal	25.71	25.71	25.71
Primary	63.6	60.90	54.85
Secondary	92.2	87.77	78.00
Tertiary	158.4	150.73	133.96
<i>Inlet gas temperature (K)</i>			
Primary	297.15	294.95	294.95
Secondary	524.65	525.15	525.15
Tertiary	524.65	525.15	525.15
<i>Oxygen concentration (mass%)</i>			
Primary	23.15	16.20	16.20
Secondary	23.15	22.50	25.71
Tertiary	23.15	22.50	25.71

Table 3 Reaction rate coefficients in the form $k = A_r T^\beta \exp(-E_a/RT)$ [54].

Reaction constant	A_r (m ³ /kmol-s)	β	E_a (J/kmol)
k_{f1}	1.80×10^{11}	0	3.19×10^8
k_{f2}	1.80×10^7	1	3.89×10^7
k_{f3}	7.10×10^{10}	0	3.74×10^6
k_{r1}	3.80×10^{10}	0	3.53×10^6
k_{r2}	3.80×10^6	1	1.73×10^8
k_{r3}	1.70×10^{11}	0	2.04×10^8

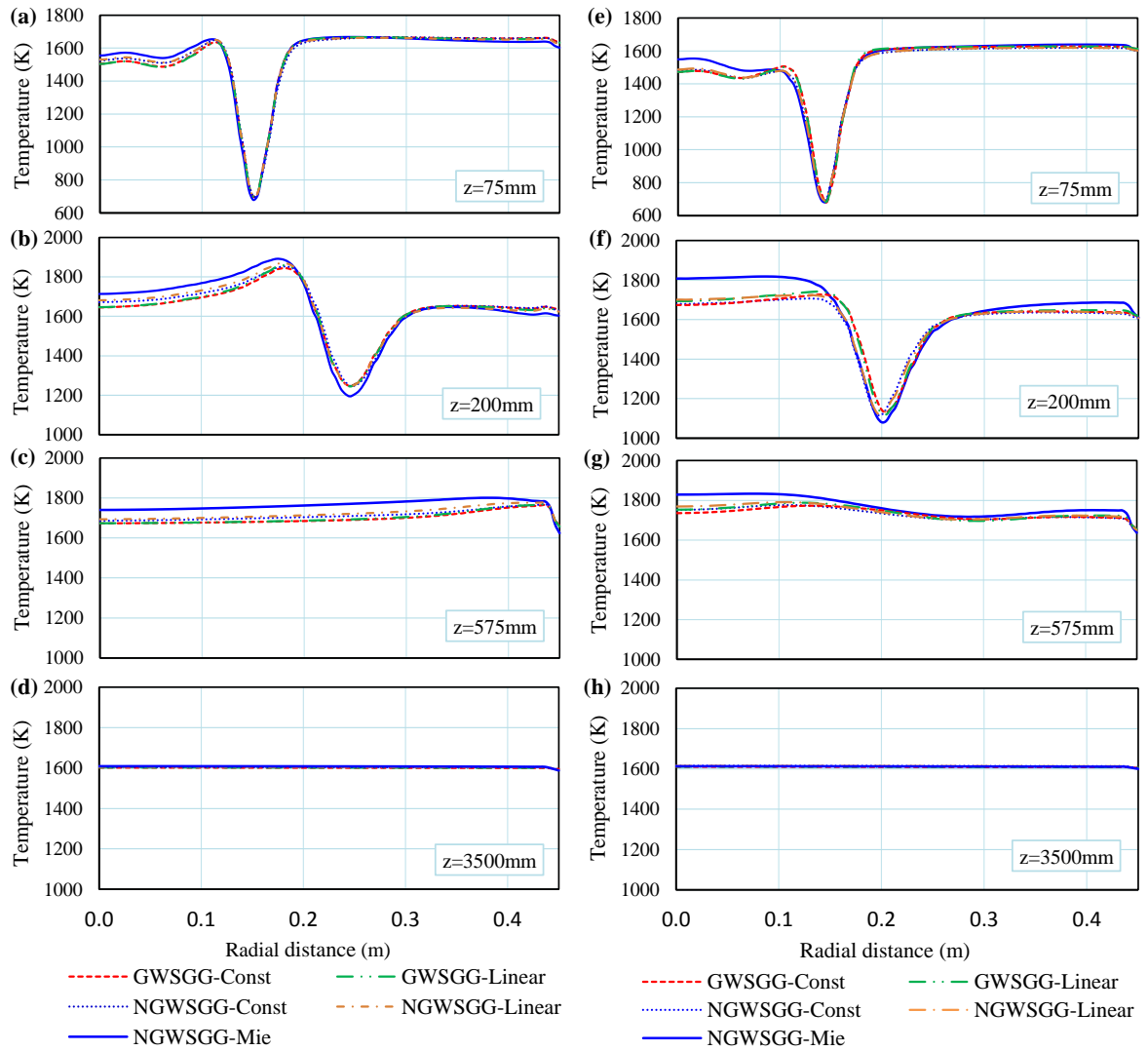


Fig. 2: Radial temperature distribution at several distances from the burner exit for the air-fired condition (a-d) and oxy-27 condition (e-h).

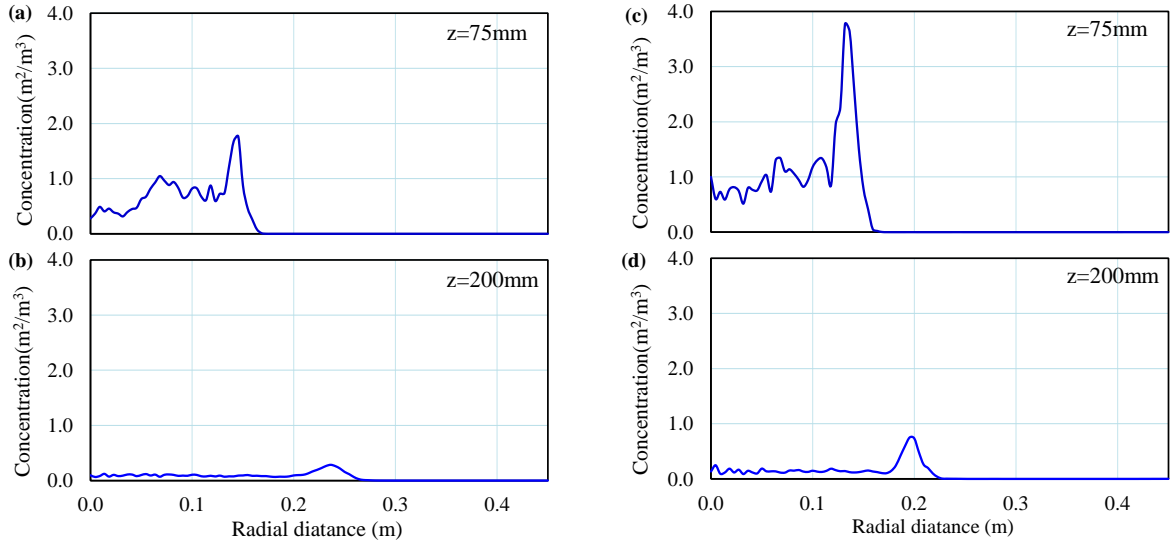


Fig. 3: Projected surface area distributions of coal/char particles calculated from NGWSGG-Mie cases at distances 75mm and 200mm from the burner exit for (a, b) air-fired condition and (c, d) Oxy-27 condition.

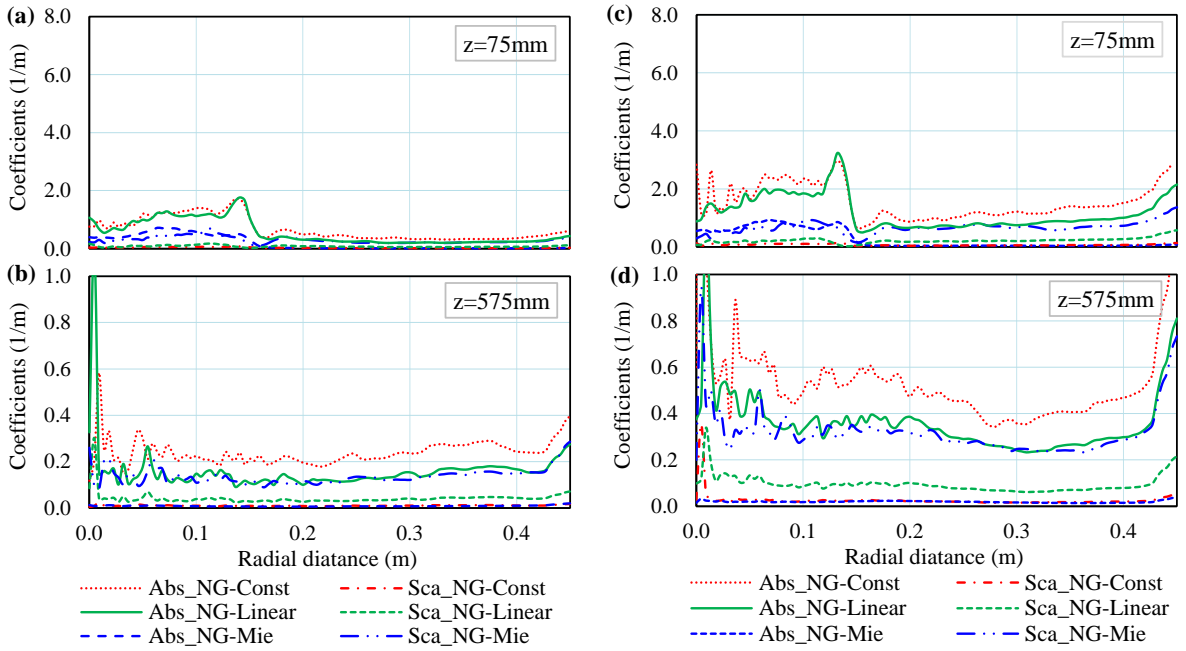


Fig. 4: Particles radiative properties at distances 75 mm and 575 mm from the burner exit for (a, b) air-fired condition, and (c, d) oxy-27 condition.

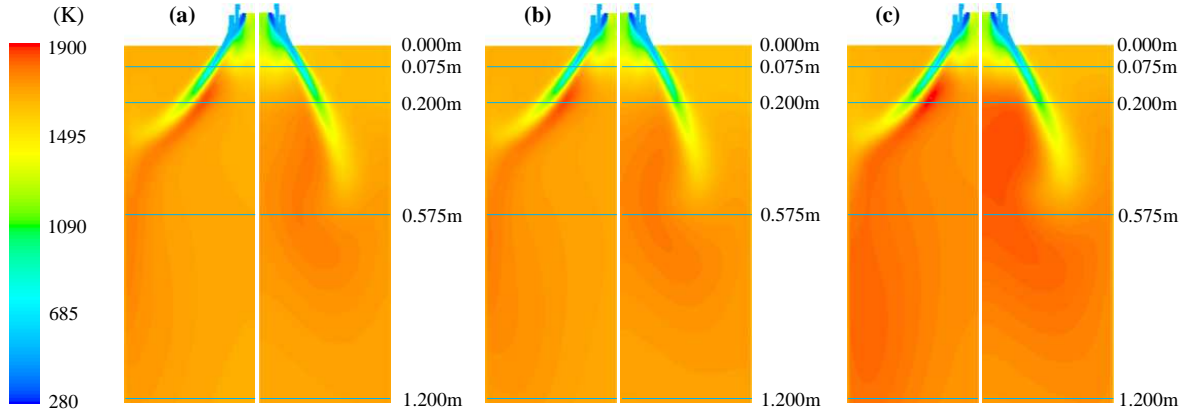


Fig. 5: Temperature distributions of the air-fired condition (left) and Oxy-27 condition (right) for different radiative properties of the gas and particles. (a) WSGG-Const, (b) NGWSGG-Const, and (c) NGWSGG-Mie.

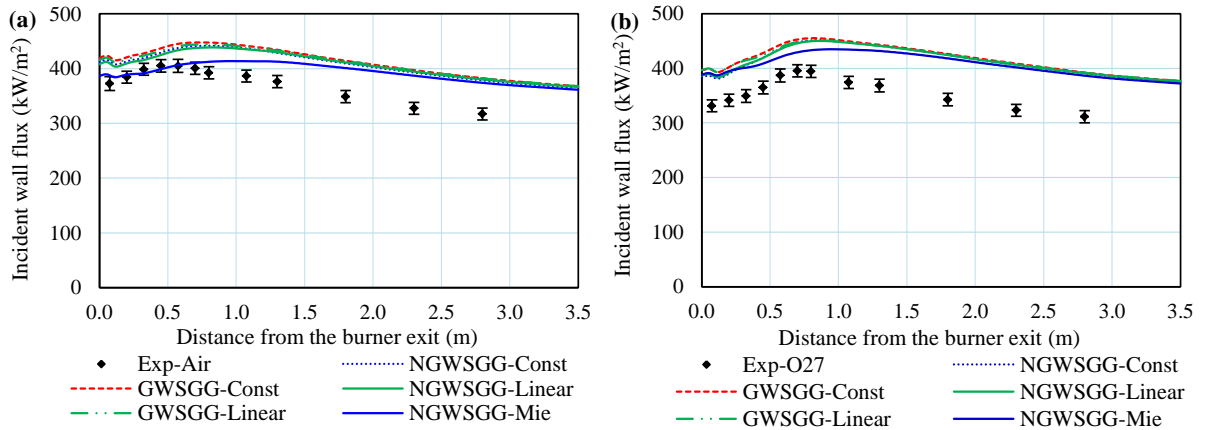


Fig. 6: CFD results for surface incident radiative heat fluxes for (a) air-fired condition, and (b) oxy-27 condition compared to experimental data from [23].

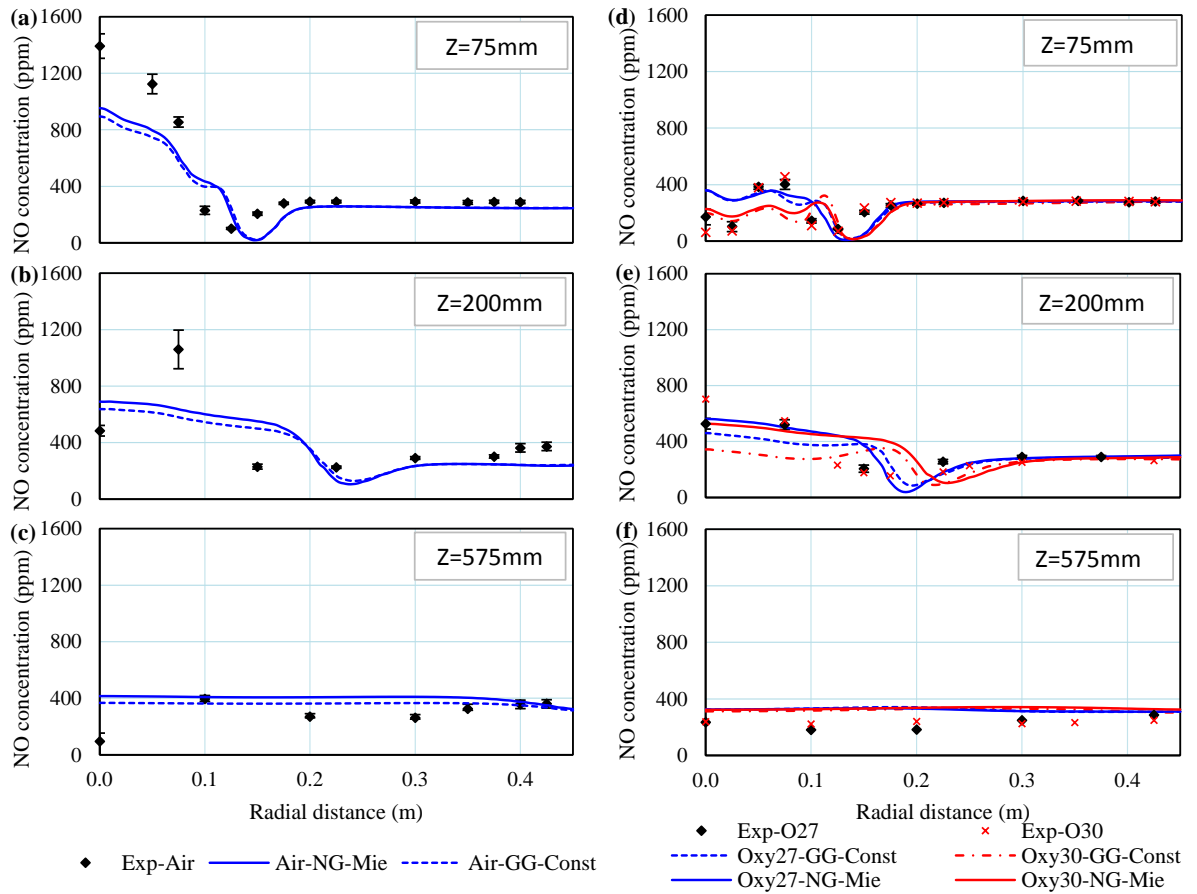


Fig. 7: Radial NO distribution at 75 mm, 200 mm and 575 mm from the burner exit for (a-c) air-fired condition and (d-f) oxy-fired conditions.

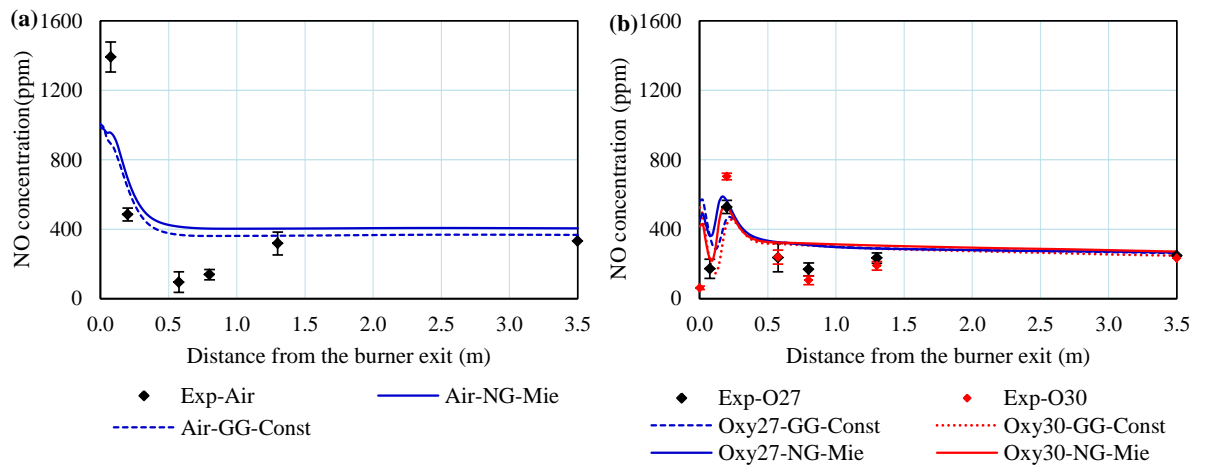


Fig. 8: Axial NO distributions were measured at the centreline of the furnace for (a) air-fired condition, and (b) oxy-fired conditions.

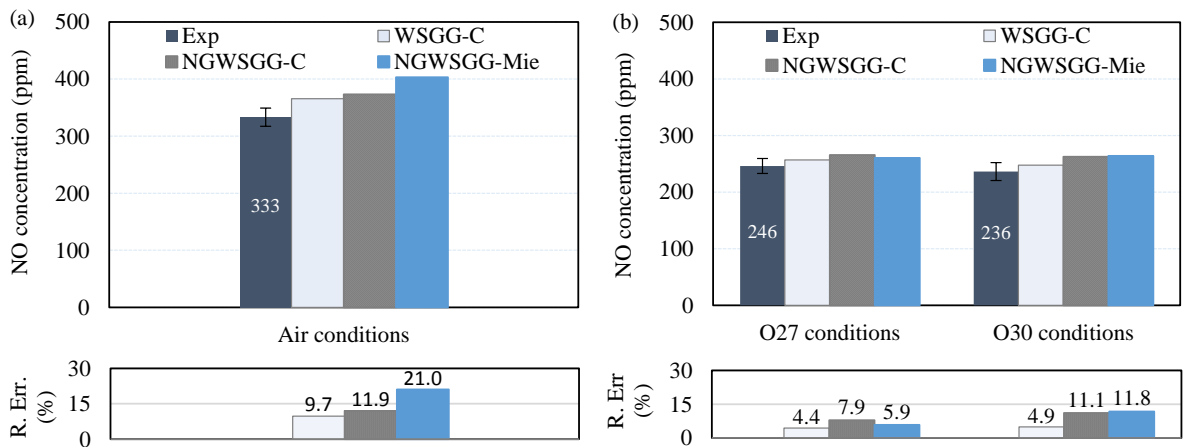


Fig. 9: The average NO concentration at the exit section of the furnace from experimental measurement and CFD calculation for (a) air-fired condition, and (b) oxy-fired conditions.

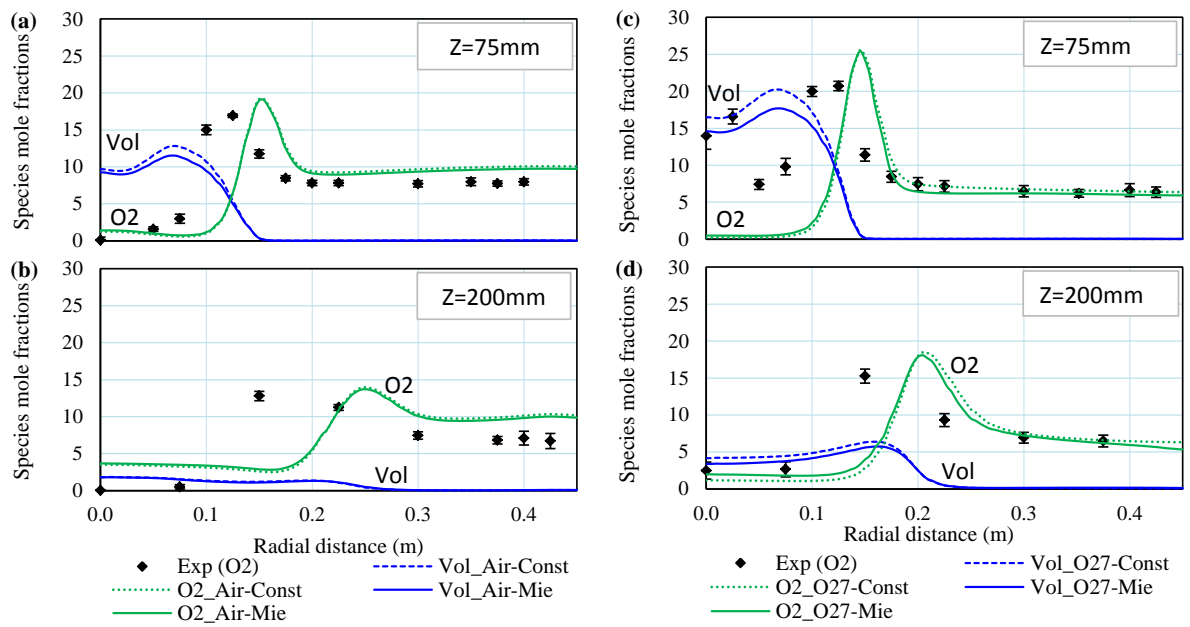


Fig. 10: Results for radial oxy and volatile distribution at 75 mm and 200 mm from the burner exit for (a, b) air-fired condition and (c, d) oxy-27 condition compared to experimental data from [23].