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## Refuting the nature of the sixth $0^+$ Hoyle-analogue state candidate in $^{16}\text{O}$

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A prominent candidate for a Hoyle-analogue state in  $^{16}\text{O}$  is the  $0_6^+$  state, previously observed at  $E_x = 15.097(5)$  MeV. This state is identified by several theoretical cluster calculations to be a good candidate for the  $4\text{-}\alpha$  cluster state, analogous to the Hoyle state in  $^{12}\text{C}$ . Whilst much theoretical work has been performed to reconcile a calculated  $\alpha$ -cluster state with this resonance, the experimental information on this state remained very scarce. To investigate this state, the  $^{16}\text{O}(\alpha, \alpha')$  reaction was studied at  $\theta_{lab} = 0^\circ$  at an incident energy of  $E_{lab} = 200$  MeV using the K600 magnetic spectrometer at iThemba LABS. For the first time, the decay channels of the  $E_x = 15.097(5)$  MeV state were isolated using a large acceptance silicon-strip detector array at backward angles. The lineshapes of the states were analysed within a phenomenological R-matrix framework. Results indicate the presence of a resonance at  $E_x \approx 15$  MeV which does not exhibit a  $J^\pi = 0^+$  nature.

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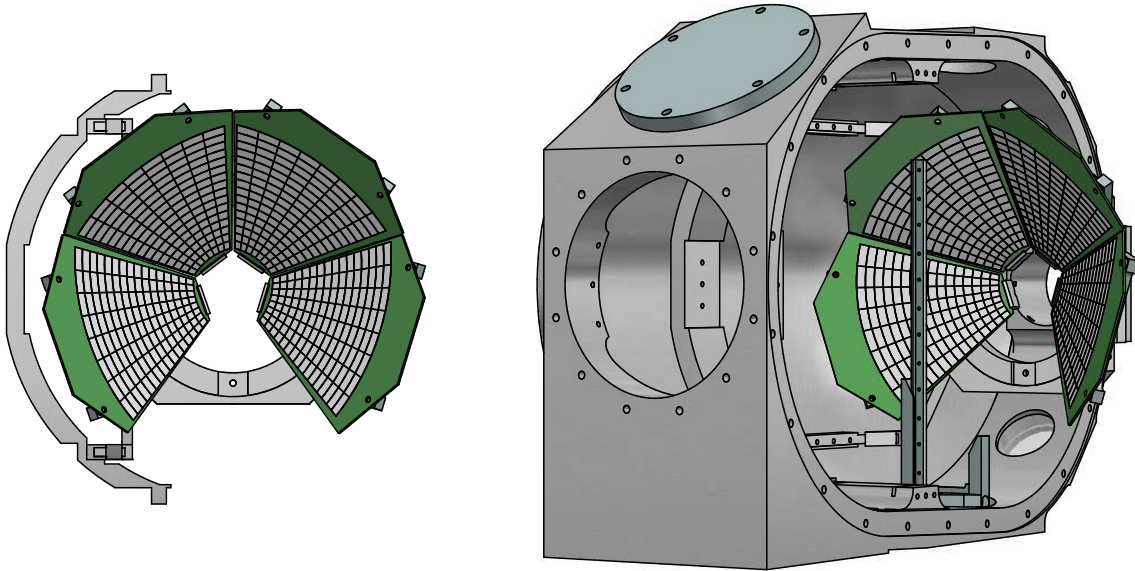
\*Speaker.

## 1. Introduction

The search for Hoyle-like states in nuclei has recently garnered much interest in both experimental and theoretical realms. A prominent candidate for a Hoyle-analogue state in  $^{16}\text{O}$  is the  $0_6^+$  state, previously observed at  $E_x = 15.097(5)$  MeV with a width of  $\Gamma = 166(30)$  keV [1]. This state is identified by several theoretical cluster calculations to be a good candidate for the  $4\text{-}\alpha$  cluster state [2, 3, 4], analogous to the Hoyle state in  $^{12}\text{C}$ . This candidate, theoretically calculated to be 2 MeV above the four  $\alpha$ -particle breakup threshold of  $S_{4\alpha} = 14.437$  MeV, satisfies the Ikeda prescription for cluster formation [5]. The relatively narrow width of this resonance, with respect to its high excitation energy above the four  $\alpha$ -particle breakup threshold, is indicative of a relatively long lifetime: a presumed characteristic of Hoyle-like states [4]. Whilst much theoretical work has been performed to reconcile a calculated  $\alpha$ -cluster state with this resonance, the experimental information on this state remained very scarce. The primary goal of this work was therefore to provide a more definitive characterisation of the nature of this state and extract the branching ratios of decay channels. Recent attempts to thoroughly investigate this resonance have been unsuccessful [6, 7], necessitating further investigation.

## 2. Experimental Method

To study the branching ratios of the  $0_6^+$  state in  $^{16}\text{O}$ , the low spin natural parity states of  $^{16}\text{O}$  were populated with a very selective nuclear reaction. The chosen  $^{16}\text{O}(\alpha, \alpha')$  reaction, with an incident beam energy of  $E_{lab} = 200$  MeV, was measured at  $\theta = 0^\circ$  (defined by a circular collimator with an opening angle of  $\Delta\theta_{lab} = \pm 2^\circ$ ). An advantage of this particular measurement is the dom-



**Figure 1:** The CAKE silicon detector array, comprised of 4 (out of a possible 5) MMM-type detectors. The array was mounted at backward angles, spanning a polar-angle range of:  $117^\circ < \theta_{lab} < 166^\circ$ . The minimum distance between the target and the active area of the CAKE was approximately 100(2) mm and the total solid angle subtended by the array in this configuration was approximately 20.4(5)% of  $4\pi$ .

inance of a single-step direct reaction mechanism which suppresses the population of unnatural parity states. The excited states in  $^{16}\text{O}$  were identified using the focal plane detector system of the K600 magnetic spectrometer [8] and the coincident charged-particle decay was detected using a double-sided silicon strip detector (DSSSD) array known as the Coincidence Array for K600 Experiments (CAKE) [9] (see Figure 1). A  $510\text{-}\mu\text{g}/\text{cm}^2$ -thick  $^{\text{nat}}\text{Li}_2\text{CO}_3$  target was used [10]. The target was prepared on a  $50\text{-}\mu\text{g}/\text{cm}^2$ -thick  $^{12}\text{C}$  backing and the total Li content was approximately  $50\text{-}\mu\text{g}/\text{cm}^2$ . To gauge the contamination from the carbon backing, an additional  $^{12}\text{C}$  target was also studied. The focal plane energy resolution was  $85(1)$  keV FWHM, as determined from the  $12.049(9)$  MeV  $J^\pi = 0^+$  resonance in  $^{16}\text{O}$ . The error on the calculated excitation energy was  $\delta E_x < 9$  keV. A comprehensive description of the experimental and analysis techniques is reported elsewhere [11].

### 3. Results

The detection of coincident charged-particle decay enabled the discrimination of decay modes through the coincident matrix of silicon energy versus excitation energy of the recoil nucleus, as displayed in Figure 2 (a). The  $\alpha_0$ ,  $\alpha_1$  and  $p_{0-3}$  decay lines from  $^{16}\text{O}$  are clearly observed. By projecting the  $\alpha_0$ ,  $p_0$  and  $\alpha_1$  decay loci onto excitation energy, the lineshapes of each decay mode can be analysed separately, as displayed on spectra (b), (c) and (d) respectively. The  $\alpha$ -particle and proton decay at  $E_x \approx 15$  MeV are focused upon in Figures 3 and 4 respectively. The lithium breakup is kinematically well-separated from the decays of interest from  $^{16}\text{O}$ . The  $^6\text{Li}$  and  $^7\text{Li}$  contributions to the observed excitation energy range form a continuum due to their relatively low  $\alpha$ -separation energies of  $E_{sep} = 1.47$  and  $2.47$  MeV respectively. These focal plane spectra were analysed within a phenomenological single-channel R-matrix framework which prescribes a resonance with an intrinsic Lorentzian lineshape with an energy-dependant width  $\Gamma(E)$ :

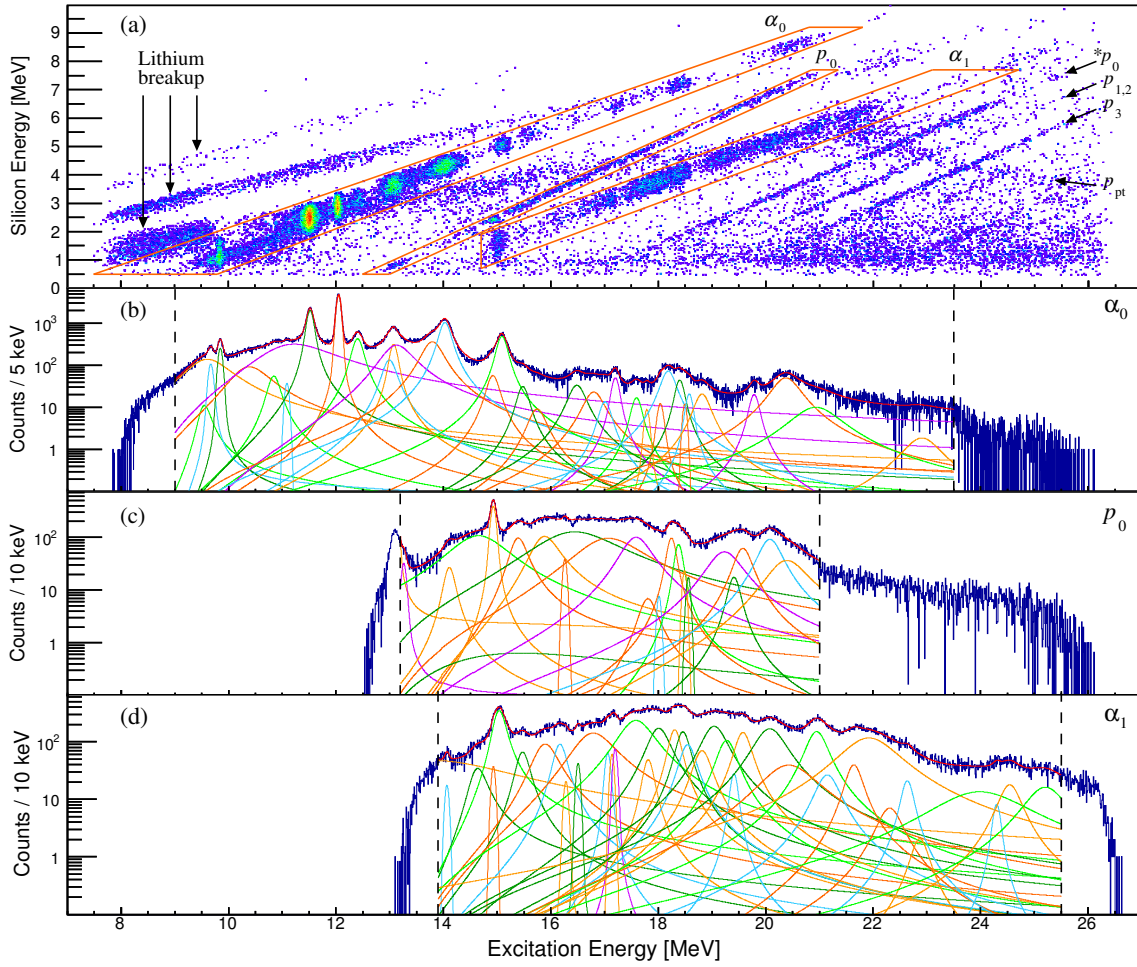
$$N(E) \propto \frac{\Gamma(E)}{[E - E_R]^2 + [\Gamma(E)/2]^2}, \quad (3.1)$$

where  $E_R$  and  $E$  represent the resonance energy and the excitation energy of the nucleus respectively. The partial width for the  $i^{\text{th}}$  decay channel,  $\Gamma_i(E)$ , is given by

$$\Gamma_i(E) = 2\gamma_i^2 P_i(E), \quad (3.2)$$

where the  $\gamma_i$  and  $P_i(E)$  represent the reduced width and penetrability of the decay channel. To account for the inherent energy resolution of the focal plane spectra, the observed lineshape of a resonance takes the form of a Voigt lineshape [12]: a convolution of the Gaussian lineshape with the aforementioned R-matrix Lorentzian lineshape.

The electronic segmentation of the CAKE array enables the gating of events detected at particular rings. The corresponding ring-gated focal plane spectra are also fitted with the same R-matrix formalism to extract the angular correlations of decay in the laboratory reference frame, as shown in Figure 5. To ensure that the extracted resonance parameters are consistent within each decay mode, the full data set for each decay mode is initially fitted. The extracted parameters are then



**Figure 2:** (a): The coincident matrix of silicon energy versus the excitation energy of the recoil nucleus for decay particles detected within the angular range:  $156^\circ < \theta_{lab} < 163^\circ$  (two strips within the array). The  $\alpha_0$ ,  $\alpha_1$  and  $p_{0-3}$  decay lines from  $^{16}\text{O}$  are indicated. The proton punchthrough structure from the  $p_0$  decay is labelled  $p_{p.t.}$ . The lithium breakup and the  $*p_0$  decay line from  $^{12}\text{C}$  are indicated. A display color threshold of  $>1$  is imposed. The projections of the  $\alpha_0$ ,  $p_0$  and  $\alpha_1$  decay loci onto excitation energy are displayed in spectra (b), (c) and (d) respectively. The ranges of each single-channel R-matrix fit are indicated with dashed lines.

fixed for the fitting of the ring-gated data: only the amplitudes of the resonances are free parameters. This not only enforces self-consistency of the results, but also suppresses the volatile nature of yield extraction from unresolved resonances which are intrinsically broad and overlapping.

To calculate the theoretical angular correlations of decay a distorted-wave Born approximation was used to describe the  $^{16}\text{O}(\alpha, \alpha')$  reaction, using the CHUCK3 code [13]. ANGCOR [14] was then employed to calculate the  $m$ -state population ratios which are used to determine the angular correlations of decay [15].

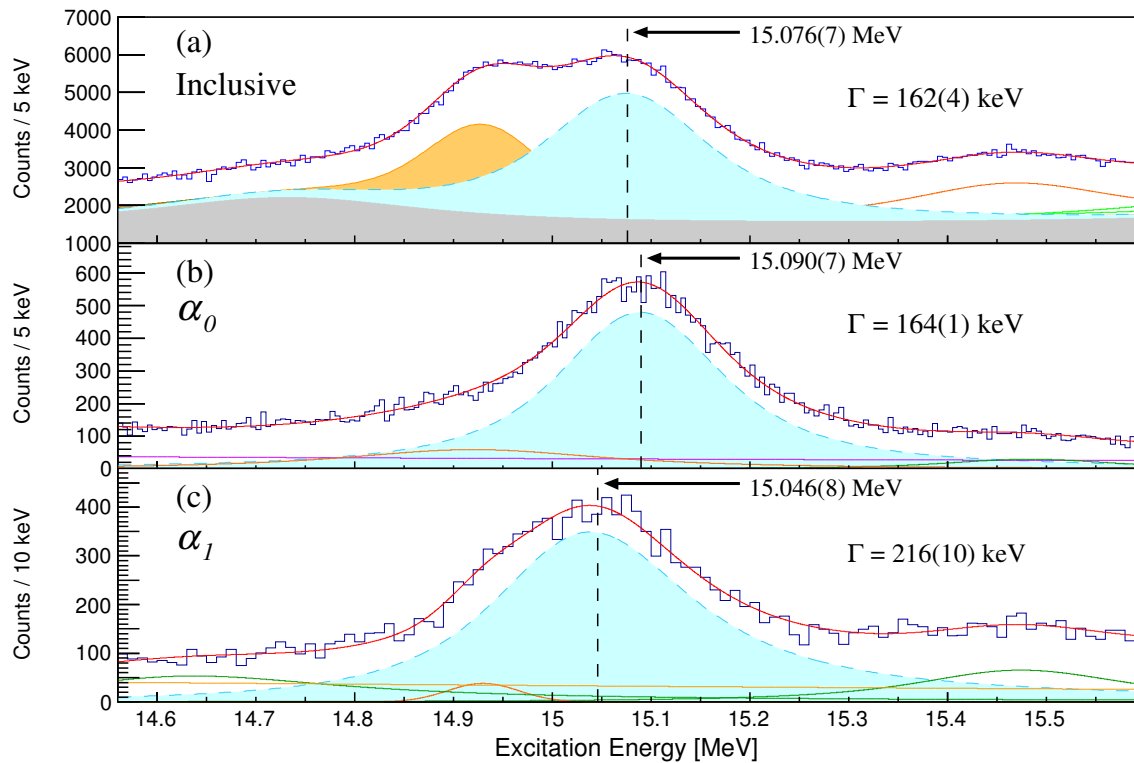
## 4. Discussion

### 4.1 The $0_6^+$ state in $^{16}\text{O}$

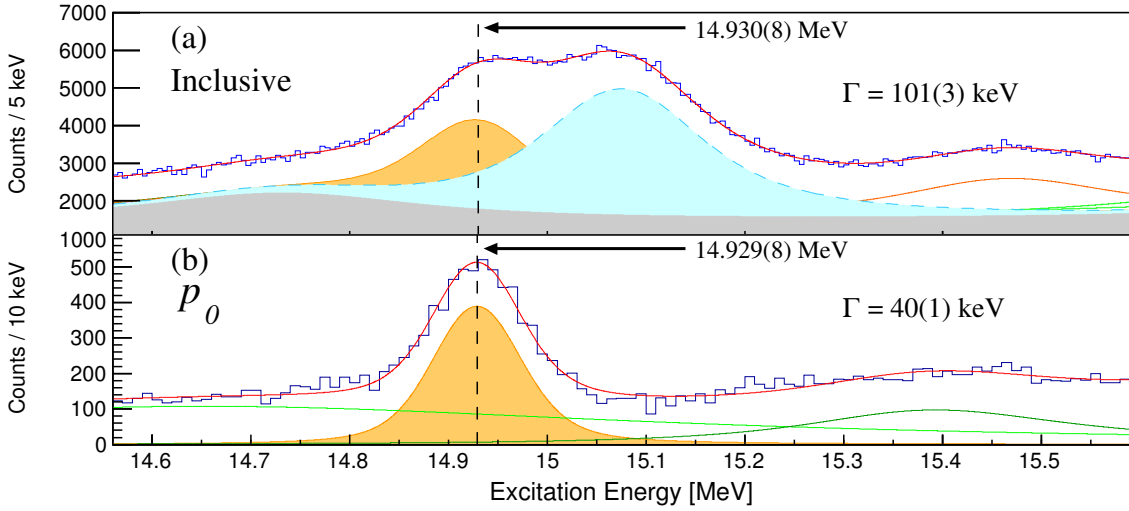
In the inclusive focal plane spectrum, a prominent resonance at  $E_x = 15.076(7)$  MeV is observed with a width of  $\Gamma = 162(4)$  keV, displayed on Figure 3 (a). This is in relatively good agreement with the corresponding literature values of  $E_x = 15.097(5)$  MeV and  $\Gamma = 166(30)$  keV. Whilst the widths extracted from the inclusive and  $\alpha_0$ -gated spectra are in good agreement ( $\Gamma = 162(4)$  and  $164(1)$  keV respectively), the corresponding  $\Gamma = 216(10)$  keV width extracted from the  $\alpha_1$ -decay spectrum on Figure 3 (c) is inconsistent.

The  $0_6^+$  resonance was not fully resolved from the neighbouring  $14.930(8)$  MeV  $J^\pi = 2^+$  resonance in  $^{16}\text{O}$ , shown on Figure 4 (a). There is a similar inconsistency between the widths extracted from the inclusive and  $p_0$ -gated spectra of  $101(3)$  and  $40(1)$  keV respectively: the  $p_0$ -extracted width agrees better with the literature value of  $54(5)$  keV. These two inconsistencies regarding inclusive and particle-gated widths are indicative of a previously unidentified resonance at  $E_x \approx 15$  MeV.

All decay channels from a  $J^\pi = 0^+$  resonance are isotropic in the reference frame of the parent nucleus. On Figure 5 (e), one observes that the  $\alpha_1$  decay agrees well to the calculated angular cor-



**Figure 3:** (a) The inclusive focal plane spectrum at  $E_x \approx 15$  MeV, highlighting the  $15.076(7)$  MeV  $0_6^+$  resonance in  $^{16}\text{O}$  (displayed with a dashed blue line and blue shading). The neighbouring  $14.930(8)$  MeV  $J^\pi = 2^+$  resonance in  $^{16}\text{O}$  is displayed with a solid orange line and orange shading. The total lithium background is shaded in grey. The projections of the  $\alpha_0$  and  $\alpha_1$  decay loci onto excitation energy are displayed in spectra (b) and (c) respectively. The resonance energy and width of each resonance of interest is indicated.



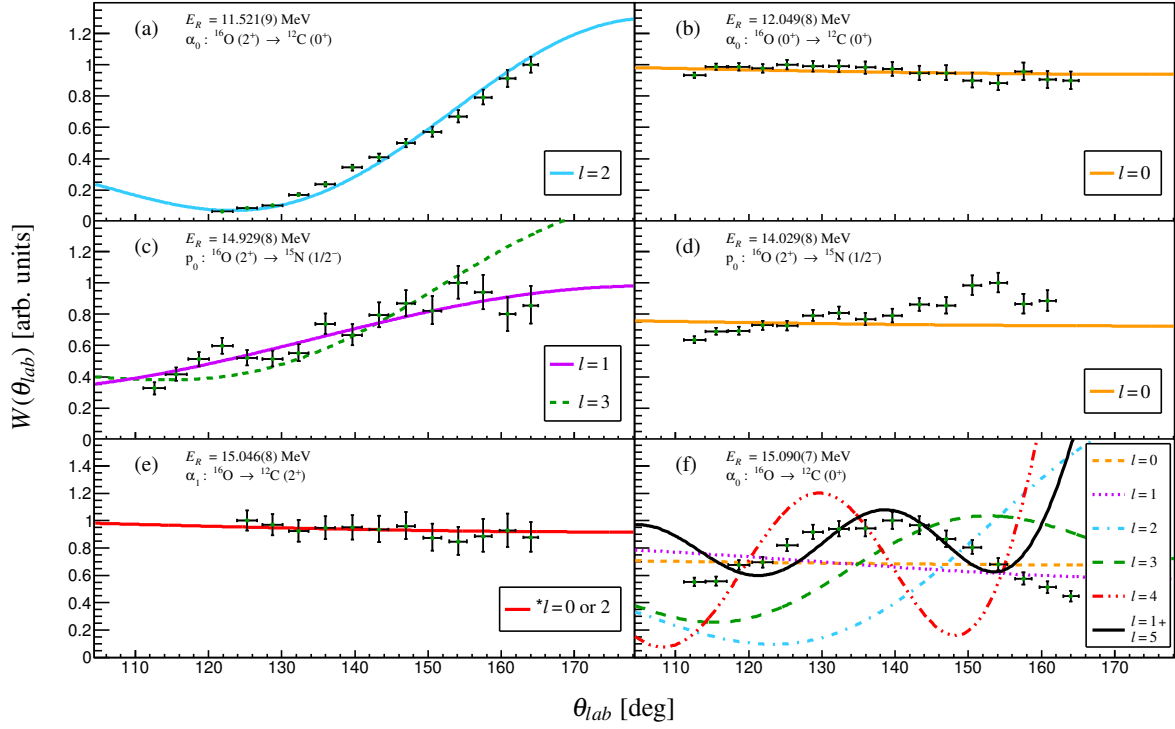
**Figure 4:** (a) The inclusive focal plane spectrum at  $E_x \approx 15$  MeV, highlighting the 14.930(8) MeV  $J^\pi = 2^+$  resonance in  $^{16}\text{O}$  (displayed with a solid orange line and orange shading). The neighbouring 15.076(7) MeV  $0_6^+$  resonance in  $^{16}\text{O}$  is displayed with a dashed blue line and blue shading. The total lithium background is shaded in grey. The projection of the  $p_0$  decay locus onto excitation energy is displayed in spectrum (b). The resonance energy and width of each resonance of interest is indicated.

relation from a  $J^\pi = 0^+$  resonance, however the  $\alpha_0$  decay on Figure 5 (f) exhibits clear anisotropy. This can only occur from a resonance with non-zero spin. The angular correlation of the  $p_0$  decay from the neighbouring 14.929(8) MeV  $J^\pi = 2^+$  state is well understood and fits well to the calculation on Figure 5 (c). To check that the  $\alpha_0$  decay of the  $0_6^+$  state is not contaminated by the neighbouring  $J^\pi = 2^+$  state, the  $\alpha_0$  decay from the well-resolved and strongly populated 11.521(9) MeV  $J^\pi = 2^+$  state was also analyzed, as shown in Figure 5 (a). This  $J^\pi = 2^+$   $\alpha_0$  angular correlation agrees relatively well to the associated calculation ( $\chi_{\text{red}}^2 = 1.42$ ) and is qualitatively different to the correlation in Figure 5 (f). Moreover, none of the calculated  $\alpha_0$  angular correlations from  $J^\pi = 0^+, 1^-, 2^+, 3^-, 4^+, 5^-$  resonances fit the data well. Assuming that the  $\alpha_0$  decay from an unidentified resonance of non-zero spin is contaminating the angular correlation, all possible pairs of the calculated correlations were incoherently summed and fitted to the data (with the relative contributions being free parameters). The best fitting combination is poor with  $\chi_{\text{red}}^2 = 7.67$ , corresponding to a combination of  $J^\pi = 0^+$  and  $1^-$  resonances. This may result from the coherent interference of particle decay from two distinct and intrinsically overlapping resonances.

#### 4.2 Known $0^+$ states observed in $^{16}\text{O}$ below the four $\alpha$ -particle breakup threshold

The strongly populated 12.049(8) MeV  $J^\pi = 0^+$  resonance is the most highly resolved on the focal plane spectra and is consequently an appropriate example for comparison to the  $0_6^+$  state. The angular correlation of  $\alpha_0$  decay from this resonance agrees well with calculation with  $\chi_{\text{red}}^2 = 1.01$ , as displayed on Figure 5 (d).

The angular correlation of the 14.029(8) MeV  $J^\pi = 0^+$  yields a poorer fit to calculation with  $\chi_{\text{red}}^2 = 2.90$ , however it is still qualitatively isotropic. This disagreement is probably due to the fact that this resonance is not well resolved from the surrounding excitation energy region (13 MeV



**Figure 5:** Angular correlations of charged particle decays from the resonances of interest in  $^{16}\text{O}$ , displayed in the laboratory frame relative to the beam axis: (a)  $\alpha_0$  decay from the 11.521(9) MeV  $J^\pi = 2^+$  resonance, (b)  $\alpha_0$  decay from the 12.049(8) MeV  $J^\pi = 0^+$  resonance, (c)  $p_0$  decay from the 14.929(8) MeV  $J^\pi = 2^+$  resonance, (d)  $\alpha_0$  decay observed at 14.029(8) MeV, (e)  $\alpha_1$  decay observed at 15.046(8) MeV, (f)  $\alpha_0$  decay observed at 15.090(7) MeV. \*The  $\alpha_0$  decays from  $J^\pi = 0^+$  and  $2^+$  resonances, corresponding to  $l = 0\hbar$  and  $2\hbar$  respectively, exhibit the same angular correlations. Data points affected by the electronic thresholds of the CAKE array are omitted.

$< E_x < 14$  MeV) which is dense with wide and overlapping resonances.

## 5. Conclusion

The measurement of the  $^{16}\text{O}(\alpha, \alpha')$  reaction at  $\theta_{lab} = 0^\circ$  was successful in populating the  $0_6^+$  state in  $^{16}\text{O}$ , observed at  $E_x = 15.076(7)$  MeV with a width of  $\Gamma = 162(4)$  keV from the inclusive focal plane data. This is in good agreement with the literature values of  $E_x = 15.097(5)$  MeV and  $\Gamma = 166(30)$  keV, however upon further inspection, some of the parameters extracted from the inclusive and particle-gated spectra at  $E_x \approx 15$  MeV are inconsistent. Together with the clear anisotropy of the  $\alpha_0$  decay observed at  $E_x = 15.090(7)$  MeV, this data suggests the existence of a previously unidentified resonance of non-zero spin at  $E_x \approx 15$  MeV. The analysis of the other observed resonances confirm that this anisotropy is not a consequence of the analysis method. Such a resonance is likely to have contaminated previous measurements of this Hoyle-analogue state candidate by augmenting the measurement of the resonance width. This is significant as a narrow width, with respect to a high excitation energy above the  $\alpha$ -disintegration threshold ( $S_{4\alpha} =$



14.437 MeV for  $^{16}\text{O}$ ), is a presumed characteristic of Hoyle-like states. This data may explain the disparity between the theoretical and experimentally observed widths of 34 keV and 166(30) keV respectively. Investigation into the  $0_6^+$  Hoyle-analogue state candidate in  $^{16}\text{O}$  is ongoing.

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