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Change in structure between the $I = 1/2$ states in $^{181}$Tl and $^{177,179}$Au

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Abstract

The first accurate measurements of the $\alpha$-decay branching ratio and half-life of the $I^\pi = 1/2^+$ ground state in $^{181}$Tl have been made, along with the first determination of the magnetic moments and $I = 1/2$ spin assignments of the ground states in $^{177,179}$Au. The results are discussed within the complementary systematics of the reduced $\alpha$-decay widths and nuclear $g$ factors of low-lying, $I^\pi = 1/2^+$ states in the neutron-deficient lead region. The findings shed light on the unexpected hindrance of the $1/2^+ \rightarrow 1/2^+$, $^{181}$Tl$^9 \rightarrow ^{177}$Au$^9$ $\alpha$ decay, which is explained by a mixing of $\pi 3s_1/2$ and $\pi 2d_{3/2}$ configurations in $^{177}$Au$^9$, whilst $^{181}$Tl$^9$ remains a near-pure $\pi 3s_{1/2}$. This conclusion is inferred from the $g$ factor of $^{177}$Au$^9$ which has an intermediate value between those of $\pi 3s_{1/2}$ and $\pi 2d_{3/2}$ states. A similar mixed configuration is proposed for the $I^\pi = 1/2^+$ ground state of $^{179}$Au. This mixing may provide evidence for triaxial shapes in the ground states in these nuclei.

Keywords: nuclear physics, decay spectroscopy, laser spectroscopy, nuclear deformation, gold nuclei, thallium nuclei

1. INTRODUCTION

Low-energy shape coexistence, whereby states of differing shape compete at low-excitation energies within the same nucleus, is an intriguing and complex facet of nuclear structure [1]. This phenomenon results from an interplay between two opposing behaviours: the stabilising effect of shell closures which preserves sphericity, and residual interactions between protons and neutrons that drive deformation [2]. However, the description of such behaviour remains a challenge for contemporary nuclear theory.

To simplify the description of this complex phenomenon, theoretical models often invoke axial and reflection symmetries. However, as highlighted in e.g. Ref [3] for germanium isotopes, the use of such restrictions may lead to problems. In particular, coexisting energy minima at different quadrupole deformations could be connected by a valley of triaxiality, along which the true energy minimum lies. Therefore, special care should be taken when modelling nuclei that inhabit known or expected regions of triaxiality.

The neutron-deficient gold ($Z = 79$) isotopes have proved to be fertile ground for the study of shape coexistence and triaxiality [4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14]. The ground-state structures of odd-mass gold isotopes are seen to gradually evolve as the mass reduces down to $A = 187$ ($N = 108$). This is evidenced by their $g$ factors, spins and parities which change from those of near-pure $\pi 2d_{3/2}$ configurations with $I^\pi = 3/2^+$ for the odd-$A$ isotopes with $A \geq 191$, to mixed $\pi 2d_{3/2}/\pi 3s_{1/2}$ states with $I^\pi = 1/2^+$ in $^{187,189}$Au [15, 4]. However, these nuclei are seen to retain weakly oblate (near spherical) shapes. A more dramatic change in structure is seen below $A = 187$, with a large increase in the mean-squared charge radius indicating a sudden increase in the ground-state deformation [5, 6, 7]. This transition from weakly oblate to
strongly prolate shapes makes these nuclei of particular interest for investigating
coeexisting structures within the region. The large increase in deformation is
accompanied by a change in the ground-state configuration to the 5/2− member
of the band, based upon the strongly prolate 1/2[541] and/or 3/2[532] deformed
states of a π1h9/2 parentage, as was proposed for 181,183,185Au in Refs. [4, 16, 17].
The ground states of the neutron-deficient gold isotopes were predicted to stay
strongly deformed until \( A \approx 177 \), where a return to near-spherical shapes was
proposed to occur (see Fig. 31 in Ref. [18]). However, results from in-beam and
\( \alpha \)-decay studies suggest that this region of strong deformation ends earlier, at
\( A = 179 \), where it is proposed that the ground state returns to a π2d3/2/π3s1/2
configuration [19, 20, 21].

Evidence for triaxial shapes has been found in the neighbouring platinum
isotopes. In particular, the magnetic moments of the lowest 3/2− states in the
odd-\( A \) isotopes 187−193Pt were shown in Ref. [22] (see Fig. 6 therein) to have
a strong dependence on the triaxial deformation parameter, \( \gamma \). Gold isotopes,
which can be viewed as a proton coupled to a platinum core, may also display
such behaviour. Signatures of triaxiality have been seen in the excited states of
some gold isotopes (see Refs. [23, 11, 12, 13] and references within). Thus, it
may be possible to observe signs of triaxiality in ground-state magnetic moments
of gold nuclei, similar to those seen in the neighbouring platinum isotopes.

This article reports on a two-pronged experimental study of the ground
and isomeric states of thallium and gold isotopes. First, an \( \alpha \)-decay study
of the \( I = 1/2^+ \) ground state in 181Tl (\( T_{1/2} = 3.2(3) \) s [24]) was performed
to investigate the unexpected hindrance to the decay observed in a study by
Andreyev et al. [25], at the velocity filter SHIP (GSI). In this work, the authors
deduced an upper limit for the \( \alpha \)-decay branching ratio of \( b_\alpha(181Tl^g) < 10\% \),
which resulted in an upper limit for the reduced \( \alpha \)-decay width of \( \delta_\alpha^2 < 19 \) keV.
The latter is notably smaller than those of other unhindered 1/2^+→1/2^+ \( \alpha \)
decays in the region, which typically have values of \( \delta_\alpha^2 \) = 45–90 keV. This
raises the question as to the possible cause of hindrance in the 181Tl^g \( \alpha \) decay.
Recent mean-squared charge radii measurements by Barzakh et al. [26] show
181Tl^g to be nearly spherical, with a magnetic moment in good agreement with
values for the \( I = 1/2^+ \) states in other odd-\( A \) thallium isotopes, which have
near-pure \( \pi 3s_1/2 \) configurations. This proves that there is nothing unusual with
the underlying structure of 181Tl^g. Therefore, the main goals of the present
work were to extract a value for \( b_\alpha \) and the half-life (\( T_{1/2} \)) of 181Tl^g, in order
to confirm or disprove the hindrance observed in Ref. [25].

On the other hand, a difference in configurations between 181Tl^g and its
\( \alpha \)-decay daughter nucleus, 177Au^g, could explain this hindrance. Prior to this
work, 177Au^g was tentatively assigned a spin of \( I^g = (1/2^+, 3/2^+) \), based on the
in-beam study by Kondev et al. [21], with the most likely configuration being
either \( 1/2^+[411](d_3/2) \) at oblate deformation with some admixture from \( \pi 3s_1/2 \),
or a prolate \( 3/2^+[402](d_3/2) \) state.

Therefore, in-source laser spectroscopy measurements of 177Au^g were per-
dformed. The present work provides the first unambiguous measurements of the
spins and magnetic moments of 177,179Au^g. The new results for 181Tl^g and
Au will be discussed within the context of the systematics of reduced $\alpha$-decay widths for $1/2^+ \rightarrow 1/2^+$ $\alpha$ decays and nuclear $g$ factors of $I = 1/2$ states within the region.

2. EXPERIMENT

Two experimental campaigns were performed for the isotopes $^{181}$Tl$^g$ and $^{177,179}$Au$^g$. In both cases the experimental method was the same as that employed in the studies of the thallium isotopic chain presented in Refs. [26, 27]. Additional details pertinent to the present work are given below. The radioactive thallium and gold nuclei were produced at the ISOLDE facility [28, 29], in spallation reactions induced by a 1.4-GeV proton beam, impinging upon a 50 g/cm$^2$-thick UC$_x$ target. The proton beam was delivered by the CERN PS Booster with an average current of 2.1 $\mu$A, in a repeated sequence known as a supercycle that typically consisted of 35–40, 2.4-$\mu$s long pulses, with a minimum interval of 1.2 s between each pulse.

After proton impact the reaction products diffused through the target matrix and effused towards a hot cavity ion source, kept at a temperature of $\approx 2000$ °C. Inside the cavity, the thallium or gold atoms were selectively ionised by the ISOLDE Resonance Ionization Laser Ion Source (RILIS) [30, 31]. The ions were then extracted from the cavity using a 30 kV electrostatic potential and separated according to their mass-to-charge ratio by the ISOLDE GPS mass separator. The mass-separated beam was then delivered to either the ISOLTRAP Multi-Reflection Time-of-Flight Mass Spectrometer (MR-ToF MS) [32] or the Windmill decay station [33, 34], for photoion monitoring during RILIS laser-wavelength scans across the hyperfine structure (hfs) of an atomic transition used in the resonance ionization process (see Fig. 1). Details of the scanning procedures can be found in Ref. [35] for the MR-ToF MS, and Refs. [33, 36] for the Windmill system.

As well as hfs scanning, the Windmill decay station was used for the decay studies of $^{181}$Tl$^g$. The mass-separated beam entered the Windmill system through the central hole of an annular silicon detector (Si1) and was implanted into one of ten, 20 $\mu$g/cm$^2$-thick carbon foils mounted on a rotatable wheel. A second surface-barrier silicon detector (Si2) was positioned a few mm behind the foil at the implantation site. Together, Si1+Si2 were used to measure the short-lived $\alpha$ activity at the implantation site. After a fixed number of supercycles the wheel of the Windmill was rotated within a 0.8 s time window, moving the irradiated foil to a decay site, between a pair of closely spaced silicon detectors (Si3 and Si4), which were used to measure long-lived decays. The full-width at half maxima of the recorded $\alpha$-decay peaks were 22–35 keV, within the energy region of interest ($E_\alpha = 5000$–$7000$ keV).

The $\alpha$-decay study of $^{181}$Tl$^g$ was part of the experiment described in Ref. [26], in which the change in mean-squared charge radii and nuclear magnetic dipole moments of the thallium isotopic chain were discussed. During this experiment, a two-step resonant ionisation scheme was used to ionise the thallium isotopes. In the case of $^{181}$Tl, only beams of the ground state were produced, as the
Figure 1: The three-step resonant photoionization scheme used to produce gold ions [37], along with the hyperfine structures (not to scale) expected for a nucleus with spin $I = 1/2$, or $I = 3/2$. The green arrows indicate the allowed transitions between different electronic states: three lines for $I = 1/2$, and four for $I = 3/2$.

production rate and half-life of the $I^x = 9/2^-$ isomer were too low for its extraction from the target ($T_{1/2} = 1.40(3)$ ms [19]).

In the separate experiment on $^{177,179}$Au, the laser spectroscopy measurements were made using the three-step resonant ionisation scheme shown in Fig. 1 [37]. The IS and hfs measurements were made upon the 267.7-nm transition, by scanning a frequency-tripled titanium sapphire (Ti:Sa) laser in a narrowband mode (FWHM bandwidth of 600 MHz before tripling). Two broadband dye lasers (BBDL; FWHM bandwidth of $\approx 20$ GHz) were used for the second and third excitation steps.

3. Results

3.1. $^{181}$Tl $\alpha$-decay branching ratio and half-life

Figure 2 shows the singles $\alpha$-decay spectra recorded by the four silicon detectors of the Windmill system, during the $\alpha$-decay study of $^{181}$Tl. In the spectra, $\alpha$ decays originating from $^{181}$Tl$^9$ and its $\alpha$-$\beta$-decay daughter and granddaughter nuclei ($^{181}$Hg, $^{181}$Au, $^{177}$Au and $^{177}$Pt) can be seen, along with an unidentified, low-intensity decay at $E_\alpha \approx 5750$ keV in the Si1 and Si2 spectra. Due to the long half-life of $^{181}$Tl$^9$ ($T_{1/2} = 3.2(3)$ s [24]), its $\alpha$ decays are also seen in Si3 and Si4 after the movement of the Windmill. Energy calibrations for the silicon detectors were made using the evaluated $\alpha$-decay energies of $^{181}$Hg ($E_\alpha = 6006(5)$ keV) and $^{177}$Pt ($E_\alpha = 5517(4)$ keV) [38], both of which are part of the $^{181}$Tl decay chain and were produced in the same run.

It is important to note the proximity in energy of the $^{177}$Au$^9$ and $^{181}$Tl$^9$ $\alpha$ decays, which differ by just $\approx 20$ keV (see Fig. 2 and the following discussion). Because of this and their relatively long half-lives ($T_{1/2}(^{177}$Au$^9$) = 1.462(32) s [21]),
previous attempts to extract values of $b_\alpha$ and $T_{1/2}$ from the mixed $^{181}\text{Tl}^9+^{177}\text{Au}^9$ peak have had limited precision $^{39, 40, 24, 19}$. This issue is highlighted in Fig. 2, in which the energy peaks of the $^{181}\text{Tl}^9$ and $^{177}\text{Au}^9$ $\alpha$ decays are seen to overlap in all four spectra. This problem could be overcome by using the $\alpha-\alpha$ correlation method for $^{181}\text{Tl}^9\rightarrow^{177}\text{Au}^9$ decays at recoil separators, but so far such studies have resulted in low statistics, making determination of the branching ratio difficult $^{40, 24, 19}$, with only an upper limit of $b_\alpha < 10\%$ reported in Ref. $^{25}$.

Despite this issue, it was possible to extract an accurate value of $b_\alpha$($^{181}\text{Tl}^9$) in the present work. This was done by fitting the singles $\alpha$-decay spectra for each silicon detector separately, the results of which are shown by the red and blue curves in Fig. 2. The fitting was performed by the ROOT Minuit minimiser $^{41}$, using a binned-likelihood method and Crystal Ball functions $^{42, 43, 44}$ to describe the shape of the $\alpha$-decay peaks. The parameters of the fits were left free, but kept such that those defining the tail and the width were the same for all peaks belonging to the spectrum of each individual detector. The fits yielded energies of $E_\alpha(^{181}\text{Tl}^9) = 6183(7)$ keV and $E_\alpha(^{177}\text{Au}^9) = 6159(7)$ keV. These values are in good agreement with those of Ref. $^{19}$: $E_\alpha(^{181}\text{Tl}^9) = 6181(7)$ keV and $E_\alpha(^{177}\text{Au}^9) = 6160(7)$ keV, as well as Ref. $^{21}$ ($E_\alpha(^{177}\text{Au}^9) = 6160$ keV), where the isotope $^{177}\text{Au}^9$ was directly produced, and therefore the determination of
$E_\alpha$ had no interference from the presence of $^{181}$Tl$^g$.

The $\alpha$-decay branching ratio of $^{181}$Tl$^g$ was determined by comparing the number of detected $^{181}$Tl$^g$ and $^{181}$Hg $\alpha$ decays taken from the fits, corrected by the $\alpha$-decay branching ratio of $^{181}$Hg, such that

$$b_\alpha(^{181}\text{Tl}^g) = \frac{100\% \times N_\alpha(^{181}\text{Tl}^g)}{N_\alpha(^{181}\text{Tl}^g) + N_\beta(^{181}\text{Tl}^g)} = \frac{100\% \times N_\alpha(^{181}\text{Tl}^g)}{N_\alpha(^{181}\text{Tl}^g) + \frac{N_\alpha(^{181}\text{Hg})}{b_\alpha(^{181}\text{Hg})}}$$

(1)

where $N_\alpha(X)$ represents the sum of the counts from all four silicon detectors, for a particular isotope. Using the evaluated value $b_\alpha(^{181}\text{Hg}) = 27(2)\%$ [38], an $\alpha$-decay branching ratio of $b_\alpha(^{181}\text{Tl}^g) = 8.6(6)\%$ was deduced, which is in agreement with the upper limit of $b_\alpha(^{181}\text{Tl}^g) \leq 10\%$ determined by Andreyev et al. [25].

A value of $T_{1/2}(^{181}\text{Tl}^g)$ was extracted from the combined decay curve recorded in Si3+Si4 (see Fig. 3). By selecting events belonging to the high-energy side of the combined $^{177}\text{Au}^g + ^{181}\text{Tl}^g$ peak ($6180 \leq E_\alpha \leq 6225$ keV, see Fig. 3 inset), the contribution of $^{177}\text{Au}^g$ $\alpha$ decays was < 10\% of the total statistics. The extracted data were fitted with an exponential plus constant background, and a value of $T_{1/2}(^{181}\text{Tl}^g) = 2.9(1)\s$ was extracted. This new value is in agreement with the literature value of $T_{1/2}(^{181}\text{Tl}^g) = 3.2(3)\s$ [24] but is three times more precise.

The $E_\alpha$, $T_{1/2}$ and $b_\alpha$ values extracted from the present data are compared with those from previous studies in Table 1. Using results from the current work and assuming $\Delta L = 0$ (see Sec. 3.2.1 for spin assignment of $^{177}\text{Au}^g$), a value of $\delta_\alpha(^{181}\text{Tl}^g) = 17.9(18)$ keV was deduced using the Rasmussen approach [45].
Table 1: Comparison of the $E_\alpha$, $T_{1/2}$ and $b_\alpha$ values for the $\alpha$ decays of the ground states of $^{181}$Tl and $^{177}$Au extracted from the present work and previous studies.

<table>
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<th>Isotope</th>
<th>$E_\alpha$ [keV]</th>
<th>$T_{1/2}$ [s]</th>
<th>$b_\alpha$ [%]</th>
<th>$\delta_\alpha$ [keV]</th>
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<td>8.6(6)</td>
<td>17.9(18)</td>
<td>Present work</td>
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<td>&lt;10</td>
<td>&lt;19$^1$</td>
<td>[19]</td>
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<tr>
<td>$^{181}$Tl$^g$</td>
<td>6186(10)</td>
<td>3.2(3)</td>
<td>—</td>
<td>—</td>
<td>[24]</td>
</tr>
</tbody>
</table>

3.2. Ground-state spins and magnetic dipole moments of $^{177,179}$Au$^g$

3.2.1. Spins of $^{177,179}$Au$^g$

Although $^{177}$Au has two long-lived states ($T_{1/2} = 1462(32)$ ms and $E_\alpha = 6161(7)$ keV for the ground state, and $T_{1/2} = 1180(12)$ ms and $E_\alpha = 6124(7)$ keV for the isomeric state [21, 19]), their respective hfs of the 267.6-nm transition do not overlap. Thus, with the laser tuned to the correct frequency, it is possible to obtain a clean $^{177}$Au$^g$ singles $\alpha$-decay spectrum (see inset of Fig. 4(a), in which only the 6161-keV $\alpha$ decay of $^{177}$Au$^g$ is present). By gating on this peak, it was possible to extract a pure $^{177}$Au$^g$ hfs spectrum (Fig. 4(a)) from which a value of $\mu$ was deduced$^2$.

The hfs spectrum for $^{177}$Au$^g$, an example of which is shown in the main panel of Fig. 4(a), represents the measured $\alpha$-decay rate as a function of the scanned laser frequency. The positions of the hyperfine components as a function of the scanning laser frequency are determined by the formula:

$$\nu^{F,F'} = \nu_0 + a(6p) \cdot \frac{K'}{2} - a(6s) \cdot \frac{K}{2},$$

(2)

where $\nu_0$ is the centroid frequency of the hfs, the prime symbol denotes the upper level of the atomic transition (see Fig. 1), $K = F(F+1) - I(I+1) - J(J+1)$, $F$ is the quantum number for the total angular momentum of the atomic level, $I$ and $J$ are the quantum numbers for the nuclear spin and the angular momentum for the electronic state, respectively, and $a(nl)$ is the magnetic hyperfine coupling constant for the atomic level with the quantum numbers $n$ and $l$.

As the upper and lower levels of the scanned transition both have $J = 1/2$, it is possible to distinguish between the two possibilities of nuclear spin, $I = 1/2$ and $I = 3/2$, by the number of peaks present in the hfs spectra shown in Fig. 4. For $I = 1/2$, the $F = 0 \rightarrow F' = 0$ excitation is forbidden. Therefore only three transitions are possible (see Fig. 1), with a hfs peak intensity profile of 1:2:1. In the case of $I = 3/2$, four peaks with a 5:5:1:5 relative intensity ratio would be expected (the blue arrows in Fig. 4 approximate the expected

$^2$The results for the isomeric state will be published elsewhere [46]. They confirm that the hfs of $^{177}$Au$^g$ and $^{177}$Au$^m$ do not overlap.
Figure 4: The hfs spectra for (a) $^{177}$Au$^9$ (Windmill) and (b) $^{179}$Au$^9$ (MR-ToF MS). The insets in panels (a) and (b) show the singles $\alpha$-decay and the time-of-flight spectra recorded during the laser scans for $^{177}$Au$^9$ and $^{179}$Au$^9$, measured by the Windmill and MR-ToF MS, respectively. Along with the $^{179}$Au nuclei of interest, a number of mass contaminants can be seen in the $A = 179$ time-of-flight spectrum. In order to produce the hfs spectrum of $^{179}$Au$^9$ shown in panel (b), a ToF gate was placed upon its peak shown in the inset. The zero frequency corresponds to the hfs centroid of stable $^{197}$Au$^9$. Both hfs spectra contain only three peaks, which firmly establishes that $^{177,179}$Au$^9$ have $I = \frac{1}{2}$. The blue arrows indicate the approximate location a fourth peak would be expected, were $I^{(177,179\text{Au}^9)} = \frac{3}{2}$ (see text for details).
position of the lowest-intensity peak in the case of $I = 3/2$). Thus, the three
components of the hfs spectrum in Fig. 4(a) and the observed intensity ratios
(similar to the expected 1:2:1 profile) unambiguously prove $I(^{177}\text{Au}^\pi) = 1/2$
(which justifies the use of $\Delta L = 0$ in the Rasmussen calculations of Sec. 3.1, for
$I^\pi = 1/2^+ \text{Tl}^9$ [26]). The same situation is seen for $^{179}\text{Au}^\pi$, the hfs of which
also possesses three peaks and an intensity profile that prove it too has $I = 1/2$
(see Fig. 4(b)).

In passing we note that this new spin assignment for $^{179}\text{Au}^\pi$, combined with
the unhindered nature of its $E_\alpha = 5848(5)$ keV [38] $\alpha$ decay (see Fig. 5(a)),
establishes a spin and parity of $I^\pi = 1/2^+$ for the state in the daughter nucleus
$^{175}\text{Ir}$ that is fed by this $\alpha$ decay. Interestingly, previous in-beam studies did not
find such a state and suggested that the $^{175}\text{Ir}$ ground state is $I^\pi = 5/2^-$ [47, 48].
The structure of the low-lying states in $^{175}\text{Ir}$ will be further investigated in a
forthcoming, dedicated decay study [49].

3.2.2. Magnetic dipole moments of $^{177,179}\text{Au}^\pi$

The extracted hfs spectra were fitted using Voigt profiles [26], with $I = 1/2$,
resulting in values of $a(6s,^{177}\text{Au}^\pi) = 66940(260)$ MHz and $a(6s,^{179}\text{Au}^\pi) =
58460(230)$ MHz.

To determine the magnetic moments, the prescription of Ekström et al. was
used [4]:

$$\mu = \frac{a(6s)I}{29005} \pm 0.012, \quad \text{for } I = j \pm \frac{1}{2}, \quad (3)$$

This relationship takes into account the hyperfine anomaly [50], by applica-
tion of the Moskowitz-Lombardi empirical rule [51]. This rule holds for single-
particle shell model states with an orbital angular momentum, $l$, and a total
angular momentum, $j$. However, in a recent work by Frömmgen et al. [52], it
was shown that the Moskowitz-Lombardi rule could not be applied to $I^\pi = 1/2^+$
states in cadmium isotopes. Analysis of the hyperfine anomaly for thallium iso-
topes with an odd proton in a $\pi 3s_{1/2}$ orbital shows that the correction factor
of $\pm 0.012$ in Eq. 3 should be replaced by a value of 0.05 [53]. The long-lived
$I^\pi = 1/2^+$ states in gold isotopes can be an admixture of $\pi 3s_{1/2}(j = l + 1/2)$,
and $\pi 2d_{3/2}(j = l - 1/2)$ states (see below). Therefore, a simplified version of
Eq. (3) was used\(^3\), where the correction factor was removed and the uncertainty
on $\mu$ was increased by 0.05, accordingly. This yields $\mu(^{177}\text{Au}^\pi) = 1.15(5) \mu_N$
and $\mu(^{179}\text{Au}^\pi) = 1.01(5) \mu_N$.

4. DISCUSSION

Figure 5(a) shows the $\delta_\alpha^2$ values for $1/2^+ \rightarrow 1/2^+ \alpha$ decays, calculated using
the Rasmussen approach [45], for gold ($Z = 79$, pink downwards triangles) [54,
55, 56, 46], astatine ($Z = 85$, red circles) [57, 58, 59, 60, 61], bismuth ($Z = 83,$
\footnote{This is the same approach as used in Refs. [5, 6, 7, 8, 10]}

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blue squares) \[62, 57, 58, 38, 63\], thallium (\(Z = 81\), black triangles) \[54, 56\] and iridium isotopes (\(Z = 77\), teal crosses) \[64, 55, 56, 65\]. The reader is reminded that unhindered \(\alpha\) decays for odd-\(A\) nuclei within this region have typical values of \(\delta_\alpha^2 = 45 - 90\) keV (indicated by the green, shaded region in Fig. 5(a)). In general terms, the \(\delta_\alpha^2\) values decrease as \(N \rightarrow 126\), due to a lowering of the \(\alpha\)-particle preformation probability (see Refs. [66, 67] for details). One sees this effect in the astatine and bismuth isotopes (as well as in the even-Z polonium, radon, radium and thorium isotopes, not shown in the plot). However, \(^{181}\text{Tl}\) (\(N = 100\)) is far from the \(N = 126\) shell closure and so this effect is not pertinent to the following discussion.

The value of \(\delta_\alpha^2(\text{Tl}^{181}; 1/2 \rightarrow 1/2) = 17.9(18)\) keV deduced in the present work is smaller than typical \(\delta_\alpha^2(1/2 \rightarrow 1/2)\) values in the region, in particular, those belonging to \(^{177,179}\text{Tl}\) (\(\delta_\alpha^2 = 56(19)\) and 50(3) keV, respectively) which are in good agreement with the observed systematics. A comparison of the \(\delta_\alpha^2\) value of \(^{181}\text{Tl}\) and the unhindered \(\alpha\) decay of its even-even neighbour, \(^{180}\text{Hg}\)\(^4\), yields a hindrance factor of \(\text{HF}_\alpha = 4.1(5)\), indicating that the \(^{181}\text{Tl}\) \(\alpha\) decay is hindered. The mean-squared charge radii and magnetic moment results from Ref. [26] showed \(^{181}\text{Tl}\) to be spherical, with a near-pure \(\pi 3s_{1/2}\) configuration. These results are supported by potential energy surface (PES) calculations, made using the finite-range liquid drop model (FRDM) for the macroscopic part of the energy functional [71]. The results of these calculations for \(^{181}\text{Tl}\) have a lowest-energy minimum that corresponds to a spherical nucleus (see Fig. 6).

Thus, both the experimental results and the theoretical calculations show that there is nothing unusual with the structure of \(^{181}\text{Tl}\). Therefore, the observed hindrance in the \(^{181}\text{Tl}\) \(\alpha\) decay must be due to an unusual configuration in the daughter nucleus, \(^{177}\text{Au}\)\(^4\).

This configuration may be probed by investigating the \(g\) factor of \(^{177}\text{Au}\)\(^4\). In Fig. 5(b), the \(g\) factors for the \(I = 1/2\) ground/isomeric states are plotted for gold (pink, downwards triangles [72] and references therein), astatine (red circles) [35], bismuth (blue squares) [77] and thallium (black triangles) [73, 74, 75, 76, 26] isotopes, along with those of the \(I = 3/2\) ground states in gold nuclei (green diamonds) [72]. It is worth noting the remarkable constancy of the \(g\) factors as a function of neutron number for the thallium, bismuth and astatine isotopes. The data plotted in Fig. 5(b) show that the \(g\) factor for \(^{181}\text{Tl}\)\(^9\) is in good agreement with those of other \(I = 1/2\), odd-\(A\) thallium isotopes, as well as those of the astatine and bismuth chain. These nuclides, with \(g \approx 3.2\), are characteristic of nuclei with a valence proton occupying a predominantly \(\pi 3s_{1/2}\) orbital. In passing, we also note that the \(I = 1/2\) states in the astatine and bismuth nuclei belong to weakly-deformed intruder configurations [77, 35], whereas in thallium nuclei they are the normal, spherical states [26]. Thus, at least for small deformations, \(g(\pi 3s_{1/2})\) is not sensitive to variations in the quadrupole deformation parameter, \(\epsilon_2\) (see also Ref. [78]).

\[^4\text{A value of } \delta_\alpha^2(\text{Hg}^{180}) = 74(4)\text{ keV was deduced for the unhindered } \text{Hg}^{180}\text{ decay, using data taken from Refs. [68, 69, 70]}\]
Figure 5: (a) The reduced widths for $I = 1/2 \rightarrow 1/2 \alpha$ decays, the green shaded region represents $\alpha^2 = 45 - 90$ keV, typical of unhindered decays in odd-$A$ isotopes in the region; (b) nuclear $g$ factors, for $I = 1/2$ ground and isomeric states of isotopes surrounding the $Z = 82$ shell closure, along with the $I = 1/2$ (pink, downwards triangles) and $I = 3/2$ (green diamonds) states in gold isotopes, the blue and pink shaded regions represent the approximate $g$-factor values for near-pure $\pi_3s_{1/2}$ and $\pi_2d_{3/2}$ states, respectively. The hollow symbols for $\delta_2\alpha^{(181\text{TI})}$ and $g(\text{177\text{Au}})$ are the results of the present work.

In contrast to those of the near-pure $\pi_3s_{1/2}$ configurations in the thallium, bismuth and astatine isotopes, $g(\text{177\text{Au}})$ is noticeably smaller. This suggests that $\text{177\text{Au}}$ has a different structure.

To understand this fact, we first note that the $I = 3/2$ states in $^{191-199\text{Au}}$ with $g \approx 0.1$ are dominated by a $\pi_2d_{3/2}$ configuration. All five measured $g$ factors for the $I = 1/2$ states in $^{177,179,187,189,197\text{Au}}$ lie between the values of $g(\pi_3s_{1/2})$ and $g(\pi_2d_{3/2})$ (see Fig. 5(b)). This indicates that these states have mixed $\pi_3s_{1/2}/\pi_2d_{3/2}$ configurations. The values of $g(\text{187,189,197\text{Au}}; I = 1/2)$ are closer to those of the $I = 3/2$ states in heavier gold isotopes, which suggests their configurations are primarily $\pi_2d_{3/2}$. In contrast to this, the values of $g(\text{177,179\text{Au}})$ from the present work lie closer to those of $g(\pi_3s_{1/2})$, and appear to approach the latter with decreasing neutron number. This shift reveals a change in the dominant component of the wavefunction and a trend towards near-pure $\pi_3s_{1/2}$ configurations in the lightest gold isotopes. Furthermore, the hindrance in the $^{181\text{TI}}\rightarrow^{177\text{Au}}\alpha$ decay could be accounted for by a mixed $\pi_3s_{1/2}/\pi_2d_{3/2}$ configuration in $^{177\text{Au}}$ daughter nucleus, in comparison to the near-pure $\pi_3s_{1/2}$ configuration in $^{181\text{TI}}$.

In order to better understand the structures of $^{177,179\text{Au}}$ it is instructive to explore the nature of the $I = 1/2$ states in $^{187,189\text{Au}}$ in more detail. The first measurement of $g(\text{187\text{Au}}; I = 1/2) = 1.44(14)$ ($\mu = 0.72(7) \mu_N$) was made by Ekström et al. [4]. Particle-plus-Triaxial Rotor Model (PTRM) calculations showed that $g(\text{187\text{Au}}; I = 1/2)$ has a high sensitivity to the degree of axial
asymmetry, $\gamma$ (see Fig. 7 in Ref. [4]). Using these calculations, the authors proposed that $^{187}$Au$^9$ was triaxial.

However, subsequent measurements performed by Wallmeroth et al. [7] (confirmed by Savard [8]) found $g( ^{187}$Au$^9; I = 1/2) = 1.07(3)$ (shown in Fig. 5). Using the results from the PTRM calculations in Ref. [4], this new value was explained by a weak, oblate deformation, with no triaxiality (see discussion in Ref. [7]).

Further PTRM calculations were performed for $^{187,189}$Au, by Passler et al. [9], using combinations of quadrupole, hexadecapole and triaxial degrees of freedom, and modified oscillator or Woods-Saxon single-particle potentials. Again, the calculated $g$ factors of $I = 1/2$ states were seen to be highly sensitive to variations in $\gamma$. The results of the calculations showed that the $g$ factors of the $I = 1/2$ states in $^{187,189}$Au were best described by weakly-oblative, axially-symmetric deformations, with some hexadecapole contribution, and mixed $\pi 3s_{1/2}/\pi 2d_{3/2}$ configurations.

In contrast to the PTRM results, the lowest-energy minima in the PES calculations for $^{187,189}$Au are triaxial (see Fig. 6), albeit $\gamma$ soft [71]. However, in the PES of $^{187}$Au, there is another minimum at $\gamma \approx 55^\circ$, $\epsilon_2 \approx 0.15$. This may correspond to the weakly-deformed, axially-symmetric oblate states proposed by Wallmeroth and Passler [7, 9].

If one applies the same PTRM considerations used for $^{187,189}$Au$^9$ to $^{177,179}$Au$^9$, the results from the present work are best described by assuming $|\epsilon_2| \approx 0.18$ and $25^\circ < \gamma < 30^\circ$. Similar conclusions may be drawn from the PES plotted in Fig. 6, in which the lowest-energy minima for $^{177,179}$Au correspond to nuclei with $|\epsilon_2| \approx 0.15$, $\gamma \approx 30^\circ$.

To summarise, the degree of mixing between $\pi 3s_{1/2}$ and $\pi 2d_{3/2}$ shell-model orbitals is crucial when describing the $I = 1/2$ states in the odd-A gold nuclei, with $A \leq 179$. Two completely different phenomena, reduced $\alpha$-decay widths and magnetic dipole moments, point towards such mixed structures in $^{177,179}$Au$^9$. This may also be an indication of triaxiality in these nuclei, however, a more rigorous theoretical interpretation is required. The use of beyond mean-field techniques may clarify the role of mixing between configurations of different deformations in cases with $\gamma$-soft minima in the PES, such as those of the present work.

5. CONCLUSION

In this study, the $b_\alpha$ and $T_{1/2}$ values of $^{181}$Tl$^9$ have been determined, along with spins and magnetic dipole moments of $^{177,179}$Au$^9$. The results prove that the $\alpha$ decay of $^{181}$Tl$^9$ is hindered, which is surprising for a decay between states of equal spin. The reason for this hindrance is evident from the measured $g$ factor of $^{177}$Au$^9$, which lies between those of states dominated by a $\pi 3s_{1/2}$ or $\pi 2d_{1/2}$ orbital, indicating that $^{177}$Au$^9$ has a mixed $\pi 3s_{1/2}/\pi 2d_{3/2}$ configuration.

Based on the similarity in their $g$ factors, the $I = 1/2$ ground state of $^{179}$Au is proposed to have a similar, mixed configuration to that of $^{177}$Au$^9$. 

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Figure 6: Potential energy surface calculations for $^{181}$TI and $^{175,177,179,187,189}$Au [71]. The blue triangles indicate the lowest-energy minimum, and the red spots other minima in the potential energy surfaces.
The presence of mixed $\pi 3s_{1/2}/\pi 2d_{3/2}$ states could be a possible indication of triaxiality in the very neutron-deficient gold nuclei. However, further theoretical investigations are required to understand the relationship between these two phenomena. The highlighted interplay between mixing, triaxiality and shape coexistence is an important guide for constraining PES calculations that will accompany the next experimental step for $g$ factor measurements for $N < 98$. Extending the measurements of magnetic dipole moments for $I = 1/2$ states in the gold nuclei further towards the proton drip line will help to elucidate whether they have mixed $\pi 3s_{1/2}/\pi 2d_{3/2}$ configurations, as in $^{177,179}$Au, or if their structures evolve to near-pure $\pi 3s_{1/2}$ states. Indeed, results from $\alpha$- and proton-decay studies of $^{171,173}$Au suggest that they possess spherical, $I^{\pi} = 1/2^+$ ground states [54, 79, 80].

For example, the $\delta_2^2$ value of the $I^{\pi} = 1/2^+$ state in $^{179}$Tl matches well with those of other unhindered $\alpha$ decays (see Fig. 5), suggesting that $^{175}$Au has a near-pure $\pi 3s_{1/2}$ configuration. However, the PES plot of $^{175}$Au shown in Fig. 6 would suggest that the ground state of $^{175}$Au is triaxial, and may have a similar structure to $^{177,179}$Au. Thus, laser spectroscopy measurements of the $I = (1/2)$ state in $^{175}$Au ($T_{1/2} = 207(7)$ ms [56]) are essential in gaining a better understanding of the evolving structures within the region. Such measurements are expected to be within the capabilities of current radioactive ion beam facilities.

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[38] NNDC, Evaluated nuclear structure data file, Evaluated Nuclear Structure Data File.


