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# The investigation of CO<sub>2</sub> effect on the characteristics of a methane diffusion flame

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## Abstract

Image processing is used to investigate the effect of mixing carbon dioxide with methane on flame properties by digitally analysing the flame chemiluminescence emission. The images are captured by a high speed colour camera, which is able to record and monitor the spatial and temporal changes in flame chemiluminescence when adding different amounts of carbon dioxide to methane from the moment of ignition to any specific time during combustion. Results confirmed that by increasing carbon dioxide, the flame temperature and soot level are reduced and the flame height is getting longer. On the other hand it has been qualitatively observed that the ignition time is increased. Also, the presence of soot that only emits infrared light is observed during the ignition period. The average value of B/G ratio is calculated through digital image processing. It is found that B/G ratio increases by adding more CO<sub>2</sub>.

*Keywords:* Soot, CO<sub>2</sub>, Biogas, Chemiluminescence, Digital image processing, High speed imaging

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## 1. INTRODUCTION

Many researchers showed their interest on the effects of CO<sub>2</sub> addition to hydrocarbon fuels on soot production. This is mainly because of different reasons. One is that CO<sub>2</sub> is one of the main greenhouse gases responsible for

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5 global warming which is generally produced due to fossil fuel combustion [1, 2].  
 One solution to reduce the amount of carbon dioxide is to find alternative environmental friendly fuels. Biogas and bio-syngas are two alternative fuels that recently are in centre of attention [2]. Biogas is produced by fermentation of biomass by anaerobic bacteria and is mainly composed of  $\text{CH}_4$  and  $\text{CO}_2$  [3],  
 10 whereas Bio syngas is a synthetic gas produced from the thermal gasification of biomass and composed from different proportions of  $\text{CH}_4$ ,  $\text{H}_2$ ,  $\text{CO}$  and  $\text{CO}_2$  [4]. As it can be seen, for both gases,  $\text{CH}_4$  and  $\text{CO}_2$  are two common components. Note as these gases are produced from different sources, the amount of  $\text{CO}_2$  varies from one source to the other source. This causes an impact on  
 15 the combustion, especially flame stability and soot formation. The soot fraction will also have an impact on the radiation heat transfer characteristics. To have a better design for non-fossil fuel combustion system, well understanding of the influence of mixing  $\text{CO}_2$  with  $\text{CH}_4$  is a good step forward. Many valuable contributions have been done in this area [5, 6, 7] and it is known that adding  $\text{CO}_2$   
 20 causes soot suppression in the combustion process [8]. Yet, it is not precisely known under which procedure the soot level reduces [9]. It is found that soot formation is affected by three classes of operation, diluent, thermal and chemical [10, 11]. The dilution effect is due to reduction of the species, and therefore reducing their collision frequencies. The thermal effect is due to the change in  
 25 flame temperature. The chemical effect is due to the participation of additives in reactions related to soot formation. Considering that these three effects are not acting independently, and they do have effect on the performance of each other. Different soot measurement techniques are proposed and improved by scientists, which can be categorised into two main approaches, invasive and non-  
 30 invasive techniques [12]. In invasive techniques direct sampling is taken from the combustion area. Molecular beam mass spectrometry (MBSM) is an example of invasive technique, where a probe is inserted in the flame area very fast to take the sample [13]. Although it takes direct information, but during sampling a strong perturbation occurs, which results in a change to the chemical reactions in combustion area [14]. Non-invasive methods take advantage of flame

optical properties. Despite the fact that some non-invasive techniques might be complicated or costly, the advantage is the combustion area is not touched, and also a spatial and temporal information can be collected. Various number of non-invasive approaches are established and developed by researchers for different applications. Popular examples are Laser-induced incandescence (LII) [15, 16], multiwavelength [17], chemiluminescence based [2] and digital imaging techniques [18, 19]. Colour is one of the inherent specifications of flame. The sensation of colour by human eye is generally due to receive the emitted or reflected light in a specific range of light spectrum, 400-720nm. Colour can be specified and created by colour spaces. Several colour spaces are proposed such as CIE, RGB, sRGB, HSV, HSI for different applications [20]. In this work, RGB and HSV colour spaces are employed. RGB is the common colour space which is often found in computer systems and camera devices. In RGB, colours are specified in terms of three primary colours red (R), green (G) and blue (B), which can be displayed as a cube. Although the RGB colour space provides a straightforward way to display colour images, but it is not always the best choice for processing and analysis. One of the disadvantages is the inability to separate the colour information from the intensity. HSV colour space represents colour in terms of Hue (colour depth), Saturation (colour purity) and Value (Colour brightness). Hue refers to colour type, such as red, blue or yellow. It takes values from  $0^\circ$  to  $360^\circ$ . Saturation refers to the purity of the colour. It takes values from 0-100%. The lower saturation of a colour, the more faded the colour is represented. Finally, Value component refers to the brightness of the colour. It takes the same range as saturations, 0-100%. The appearance of flame colour depends on several conditions during combustion process, such as burning condition, fuel composition and equivalence ratio ( $\phi$ ) [21]. Flame colour is mostly because of the chemiluminescence emission in visible light spectrum of radicals and soot particles produced during the chemical reactions of combustion process. Chemiluminescence is in fact the emitted light due to the de-excitation of excited radicals during the chemical process of combustion [22]. It is found in previous studies that  $\text{CH}^*$  intensity radiation peak at 431nm, and  $\text{C}_2^*$  intensity

radiation peak at 516nm, are responsible for the variable degree of blue-green flame colour (asterisk (\*) denotes the electronically excited state species) [21]. While the soot particles are responsible for yellow-orange colour in flame [21].

70 Considering that some species and radicals chemiluminescence emission are out of visible range and cannot be seen by eye, such as OH\* radical, intensity radiation peak at 309nm [2], or some soot particles appear at early stage of ignition, which are in infrared region [21]. These known spectral signatures can be used to extract and provide hidden flame information in combustion zone. Recently,

75 many combustion applications, such as monitoring, modelling and diagnosing the combustion system, have used flame chemiluminescence emission [23, 24]. Human eye is not only limited in sensing the radiation intensity in small scale of light spectrum, but also it is limited in detecting fast moving objects and can only sense moving objects equivalent to a camera standard speed up to 25fps.

80 The chemical reactions and turbulence in combustion are taking place very fast, and human eye is not able to detect the flame dynamics. Recent studies showed that it is feasible to capture combustion process by using high speed camera (3000fps) with acceptable resolution (1024×1024) [18]. Also, it is shown that some cameras can detect the emissions in some parts of infrared spectral regions

85 [21]. Hunag & Zhang [21, 18] proposed a non-invasive technique, Digital Flame Colour Discrimination (DFCD), to investigate flame characteristics by applying digital image processing to digital colour flame images which are captured by a high speed camera. Within DFCD it is possible to track the spatial and temporal presence of soot as well as the chemiluminescence emissions of CH\* and

90 C<sub>2</sub>\* in visible range. Also, invisible soot during ignition time, which is in infrared can be tracked. Details of DFCD technique on processing and analysing flame images are well explained and available in [21, 18, 19]. The main goal of this study is to employ DFCD technique to investigate the effects of mixing CO<sub>2</sub> with methane gas on soot production and the presence of CH\* and C<sub>2</sub>\*

95 in combustion area. The effects on flame height and temperature are also examined. Recent developed version of colour band two-colour method [25, 26], is employed here to measure flame temperature. In two-colour method, flame

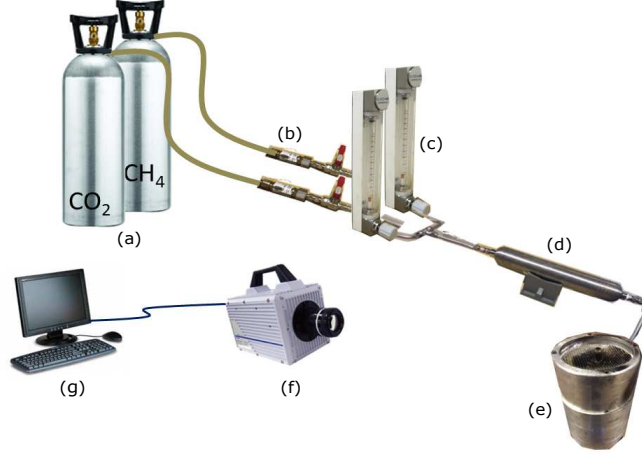


Figure 1: The schematic of experimental setup a) Gas cylinders, b) Connecting pipes, c) Rotameters, d) Mixing gas cylinder, e) Bunsen burner, f) High speed camera, g) Computer with Photron software.

images are captured in RGB colour format. Any two combinations of these three red (R), green (G) and Blue (B) colour channels can be used for flame  
 100 temperature determination. In order to avoid image saturation caused by the very intense soot light emission, the high speed camera is set to a high shutter speed ( $\frac{1}{10000}$ s).

## 2. EXPERIMENTAL SETUP & PROCEDURE

The experimental setup is consisted of the high speed colour camera, fuel  
 105 gas cylinder, rotameters for flow measurement, gas mixing cylinder and Bunsen burner. The schematic of the experimental setup is shown in Figure1.

Fuel gases, CH<sub>4</sub> and CO<sub>2</sub>, are supplied from gas cylinders. Each cylinder is connected by pipe, with 6mm diameter, to a separate mechanical rotameters. A gas mixing chamber with 500cm<sup>3</sup> capacity is used to mix the gases well  
 110 before reaching the burner. The input of the mixing cylinder is from a gas line coming from the flow meters, and the output is connected by pipe to the Bunsen burner, with outer nozzle diameter 8.94mm and honeycomb mesh. The

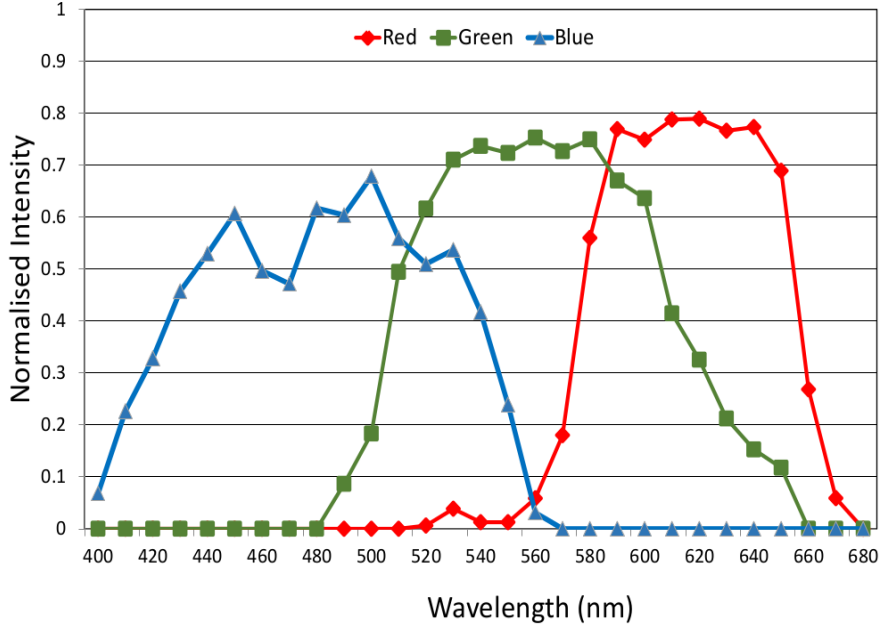


Figure 2: Photros Fastcam SA4 camera spectral response.

ignition is activated by an electrode device with approximately 30kV output voltage. Pair of steel electrodes is kept apart, 9mm, from each other. High speed CMOS camera 'Photron Fastcam SA4' is used to capture images with 1024×1024 pixel resolution. The spectral response of the camera is investigated in previous research [27] and is given in Figure 2. The high speed camera frame rate and shutter speed are set to 500fps and  $\frac{1}{800}$ s respectively for soot study. The camera is connected to a computer having *PHOTRON* software for setting the camera parameters, and also capturing and saving images in RGB (Red-Green-Blue) colour space. The post processing and analysing of flame images are done on Matlab routine, which is written in previous study [21], where captured flame images are converted to HSV (Hue-Saturation-Value) colour space. The presence of CH\* & C<sub>2</sub>\* and soot can be easily distinguished, as the colour of CH\* & C<sub>2</sub>\* appears in 180°-300° and soot appears in 1°-80° of Hue channel.

Eight sets of experiment are conducted with different mixing rate of methane

Table 1: Different amount of added CO<sub>2</sub> with methane, and corresponding velocity and Reynolds No.

Case	1	2	3	4	5	6	7	8
CO <sub>2</sub> (l/min)	0	0.123	0.37	0.618	1.236	1.854	2.47	3.09
CO <sub>2</sub> %	0	12	37	61	123	185	247	309
CH <sub>4</sub> (l/min)	1	1	1	1	1	1	1	1
Velocity (m/min)	0.159	0.179	0.218	0.258	0.356	0.455	0.553	0.652
Re No	0.0086	0.0108	0.0152	0.0196	0.0306	0.0416	0.0525	0.0636

and CO<sub>2</sub>. Methane flow rate is set to 1l/min for all cases and carbon dioxide flow rate is varied as shown in Table 1. Camera settings, the position of the camera and burner are fixed and kept unchanged throughout the whole experiment.

130 To measure the flame temperature, SiC fibre with 15 $\mu$ m thickness is placed in a frame, located at top of the Bunsen burner, in a way to cover different areas of flame. The fibres are 1.5cm apart. SiC fibres involving in the measurement plays a role of greybody radiation emitters, as the flame becomes soot deficient. The camera for temperature measurement is set to frame rate  
135 1000fps and shutter speed  $\frac{1}{10,000}$ s. The very high shutter speed is necessary to avoid image saturation. The analysis of flame temperature from digital images is based on two-colour method that has been widely used over last decade [28]. The detectable temperature range within this measurement method is between 1300K-2400K [29]. The accuracy of two-colour measurement is verified by mea-  
140 suring the temperature of the tungsten lamp within the error of 3 percent and comparing with infra-pyrometer on measuring fiber temperature [29]. Detail of the methodology is available in[26].



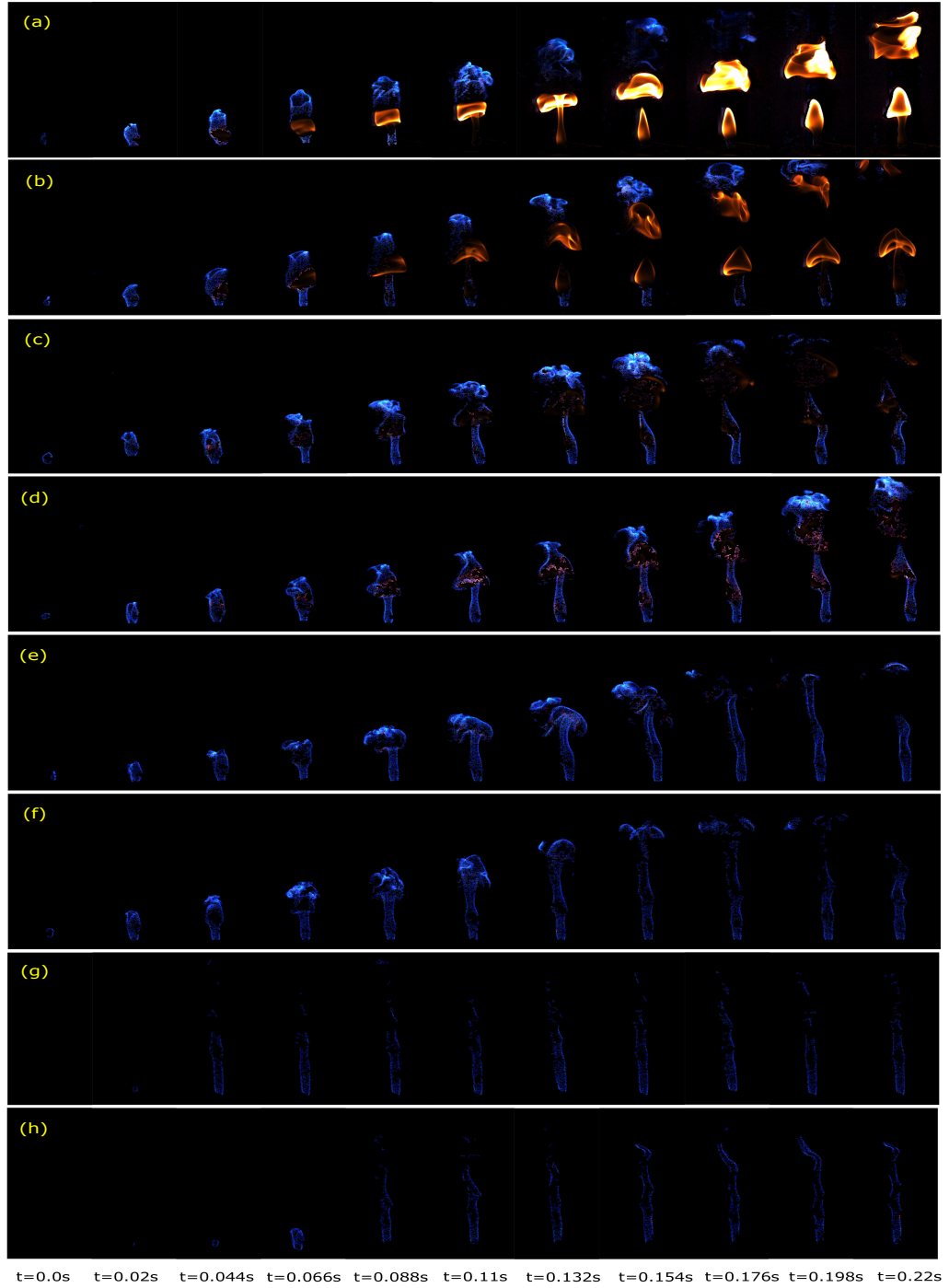


Figure 3: Sample flame images of mixing methane with different levels of  $CO_2$ , a) Case1, b) Case2, c) Case3, d) Case4, e) Case5, f) Case6, g) Case7, h) Case8.

### 3. RESULTS

The sample of captured flame images at  $t=0\text{sec} - 0.22\text{sec}$  for different cases  
145 are presented in Figure 3. The intensity of blue pixels in cases 2-8 are enhanced  
by magnifying 50 times (50 out of 255) in order to be presented. It can be  
seen that the flame colour has dramatically changed from bright yellow-orange  
to orange-blue colour as soon as  $\text{CO}_2$  is introduced. From Case3 afterwards,  
by increasing the level of  $\text{CO}_2$ , the yellow-orange colour is gradually faded and  
150 disappeared and flame only appears in blue colour. Note that for Case1,  $\text{CO}_2 = 0\%$ ,  
some pixels in flame images seems to be saturated. This is unavoidable.  
At first, diffusion methane, the flame colour is bright (yellow-orange) light. For  
other cases the dominant flame signal become blue, which is a weak signal and  
hard to be captured by the camera sensor. Therefore, the camera should be set  
155 in a way to be able to capture weak blue signals in later cases and as we want  
to have a fair comparison between different flame images. The camera position  
and setting are unchanged throughout the experiment.

It has been observed that as the level of  $\text{CO}_2$  increased the ignition time  
delayed more. Case8,  $\text{CO}_2 = 309\%$ , is the maximum limit of adding  $\text{CO}_2$  to  
160 methane because it was very difficult to ignite the flame, and also, after ignition  
the flame will easily blow out. This shows the limit for maximum amount of  
 $\text{CO}_2$  that can be added.

#### 3.1. Flame colour

##### 3.1.1. Soot flame (Orange) region

165 Orange region refers to hue channel space of  $0^\circ$ - $40^\circ$  from HSV colour image  
format, which represent the soot broadband emissions. Figure 4(a) shows the  
3D plot of temporal variation of the number of pixels in orange region. It can  
be seen that the number of orange pixels at Case1, has the highest level. By  
introducing  $\text{CO}_2$  at Case2 the orange pixels drop and at Case4, the number of  
170 orange pixels is close to zero, and hardly can be seen. After Case4 no orange  
pixel exists. This implies the soot level is very high for pure methane diffusion

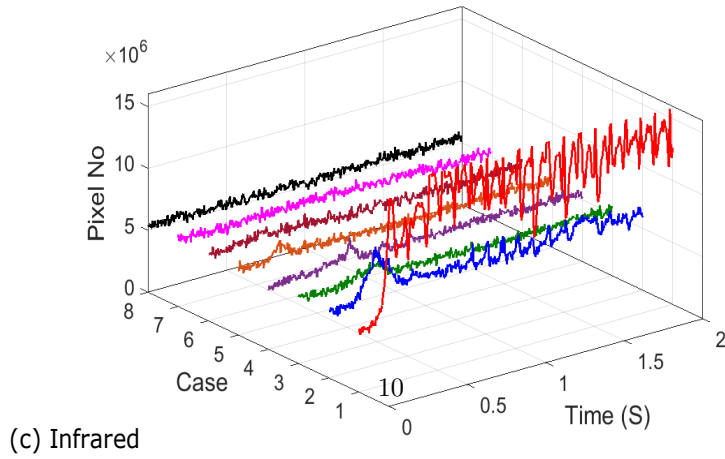
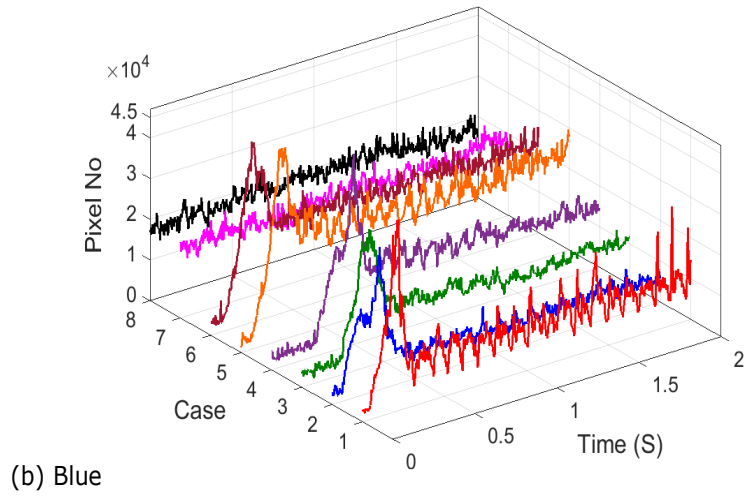
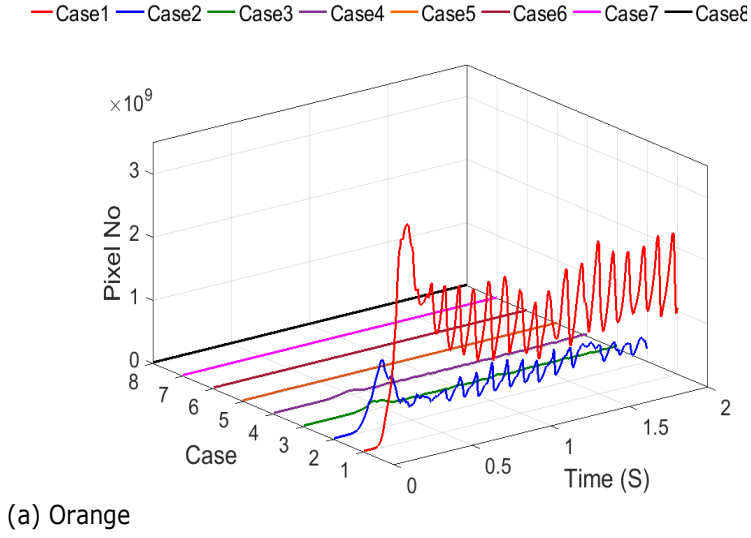


Figure 4: The plot of number of pixels in continuous flame images of 2s in duration a) Orange region, b) Blue region c) Infrared region for all the 8 cases.

flame (Case1) and mixing CO<sub>2</sub> with methane causes reduction in soot level. When the volume flow rate of CO<sub>2</sub> is half the methane, no soot is detectable.

### 3.1.2. Blue flame region

Blue flame region refers to hue channel space of 130°-252° from HSV colour image format, which represents CH\* and C<sub>2</sub>\*. Figure 4(b) shows the 3D plot of temporal variation of the number of pixels in blue region. It can be seen that the number of blue pixels at Case1, is at lowest level. Only at early ignition time, some blue pixels can be detected, and when flame gets stable, blue pixels are nearly zero. By the time CO<sub>2</sub> is added, from Case2 afterwards, the number of blue pixels gradually increased and they reached to maximum level at Case4. From Case4 to 8 the number of blue pixels remains nearly the same. This implies that the area of CH\* and C<sub>2</sub>\* radicals increased due to added CO<sub>2</sub>. A sharp peak can be seen at the beginning of the plots of the first cases. This is because of the excess of the fuel in the pipe at ignition time.

### 3.1.3. Infrared region

The recent research has shown that the colour camera is able to detect some infrared emission and it is found that the infrared colour corresponds to hue channel space of 252°-360° from HSV colour image format, which represents soot particles appear at early stage of the ignition process.

Figure 4(c) shows the 3D plot of temporal variation of the number of pixels in infrared region. It can be seen that the number of infrared pixels has the highest amount at t<0.4sec for Cases1-4. At Case5, the infrared pixels decrease dramatically even during the ignition period. From Case6 afterwards, no infrared pixels is detected even in early ignition period.

## 3.2. Flame temperature

It is shown in previous study that the Sic fibre temperature is proportional to the flame temperature[30]. Therefore, the trend of temperature variation by adding CO<sub>2</sub> is examined by measuring the temperature of the fibres in this experiment. Figure 5 shows a sample of flame image with fibres installed for

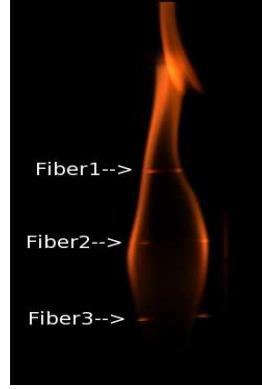


Figure 5: Sample of flame image at temperature experiment.

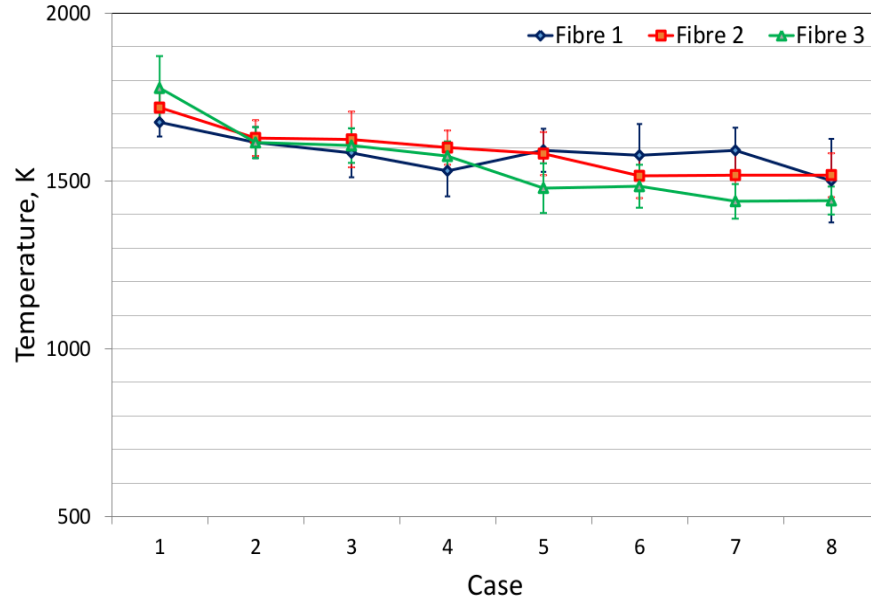


Figure 6: The plot of mean fibre temperature of 1000 continuous images with respect to different levels of added  $\text{CO}_2$  with relative value of standard deviation.

temperature measurement. The mean temperature and corresponding standard deviation of 1000 continuous images (1sec) at each fibre and for all the 8 cases are calculated and presented in Figure6. It can be seen, as soon as adding

CO<sub>2</sub> to diffusion methane, the flame temperature at 3 different fibre locations  
 205 has dropped. Comparing the plots of Figure6 indicates that the temperature  
 variation at fibre 2 and 3 show good agreement. However, fibre 1 which is more  
 away from the nozzle and close to the flame tip, shows some instability after  
 Case4. This may be mainly correlated with the buoyancy-driven oscillation  
 that is associated with the Kelvin-Helmholtz instability and the considerable  
 210 number of vortices appearing due to the buoyant interaction between the cold  
 ambient air and the hot burnt gases. Shepherd [31] used a joint experimental  
 and numerical approach to demonstrate the formation of the vortices near the  
 flame tip, and to explain how flame flicker occurs from heat release at the flame  
 front, which compels the burnt gas flow in a radial direction opposed to the  
 215 rotating vortex motion induced in the pressure field. This explains the increase  
 of the flame temperature instability from the flame base to the tip.

### 3.3. Flame height

Fifteen flame sample flame images are selected from t=1.5 secs of captured  
 images with time intervals of 0.1 seconds. The average of flame heights for  
 220 different levels of added CO<sub>2</sub> are found in pixel space in vertical dimension  
 (image length). Each pixel approximately corresponds to 0.2mm. Figure 7  
 presents the plot of flame height versus different amounts of added CO<sub>2</sub>. It can  
 be seen at the beginning, where soot presents in flame, mixing CO<sub>2</sub> decreases  
 the flame height. Then after, when the soot is faded after Case3, and the flame  
 225 colour turns to pure blue, flame height increases by adding more CO<sub>2</sub>. The  
 increment of flame height is because of the change in reaction rate. As the flow  
 rate is constant, by decreasing the reaction rate the flame area increases. As  
 it is seen in flame temperature chart, the temperature decreases which means  
 decreasing the flame reaction rate. The reason for the flame height decrement  
 230 at first two cases is not known and further investigation is required.

### 3.4. B/G Ratio

It is shown in previous study [18] that the value of each pixel in blue channel  
 (RGB colour space) with respect to the value in green channel, B/G ratio,

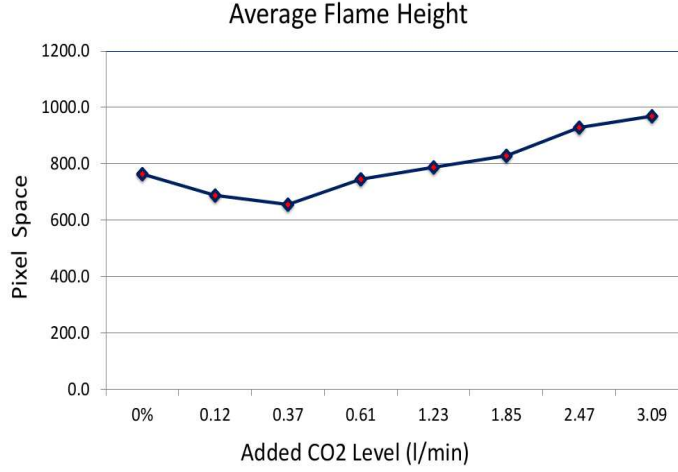


Figure 7: The plot of flame height (in pixels) versus different percentage of mixing CO<sub>2</sub>.

corresponds to the presence of CH<sup>\*</sup>/C<sub>2</sub><sup>\*</sup> in the flame spatial position. The  
 235 B/G ratio is calculated for each pixel position in flame images for all cases  
 of added CO<sub>2</sub>. The mean value of each image with value higher than zero  
 can be calculated to see the variations. Figure 8 presents the 3D plot of the  
 mean B/G ratio for 2s of flame image duration for all the 8 cases. It is shown  
 that the average B/G ratio increases by adding more CO<sub>2</sub>, which means the  
 240 average increasing rate of CH<sup>\*</sup> radicals are more than that of C<sub>2</sub><sup>\*</sup> radicals. The  
 underlying physics needs further investigation.

#### 4. CONCLUSION

Digital image processing is applied to investigate the effect of mixing CO<sub>2</sub>  
 to methane gas. The results have shown that by increasing CO<sub>2</sub>, the level of  
 245 soot emissions in visible spectrum reduces. No soot is detectable if the volume  
 flow rate of CO<sub>2</sub> reaches around half of the CH<sub>4</sub> volume flow rate. Also, the  
 amount of CH<sup>\*</sup> and C<sub>2</sub><sup>\*</sup> radicals increased by increasing CO<sub>2</sub>, and it reaches to  
 maximum when CO<sub>2</sub> flow rate reaches around half of the amount of CH<sub>4</sub> flow  
 rate. The B/G ratio, which corresponds to CH<sup>\*</sup>/C<sub>2</sub><sup>\*</sup>, increases by increasing  
 250 CO<sub>2</sub>. Moreover, the amount of pixels for infrared soot particles are detectable

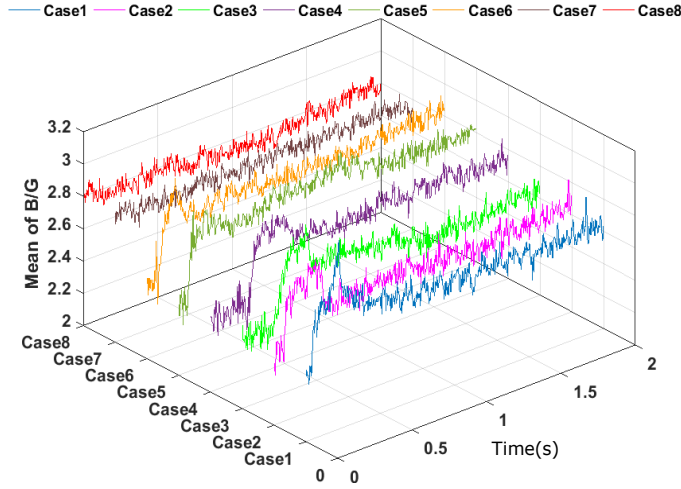


Figure 8: The plot of B/G ratio (mean value) in continuous flame images of 2s in duration for all the 8 cases.

and nearly have the same amount till Case5 and afterwards, hardly any infrared pixels can be detected. This might be related to the fact that considerable ignition delay has been observed during the experiment when the  $\text{CO}_2$  flow rate is greater than the  $\text{CH}_4$  flow rate (Case6 afterwards).

255 In this work, it is shown the capability of image processing in flame temperature measurement. In previous studies, it was found that flame temperature decreases by adding  $\text{CO}_2$ , and in this work the same result was shown by digital image processing technique.

It has been shown that the flame height increases by increasing  $\text{CO}_2$  after  
 260  $\text{CO}_2$  flow rate is higher than half of the  $\text{CH}_4$  flow rate. When  $\text{CO}_2$  flow rate is lower than  $\text{CH}_4$  flow rate (soot is detectable at this stage), flame height decreases. The reason is not exactly clear, and further investigation is required.

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- 355