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**Proceedings Paper:**
Selection of Robust Features for the Cover Source Mismatch Problem in 3D Steganalysis

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Abstract—This paper introduces a method extracting features from 3D objects characterising a robust steganalyzer such that would mitigate the cover source mismatch (CSM) paradigm. A steganalyzer is considered as a classifier aiming to identify separately cover and stego objects, representing 3D objects before and after embedding information through steganography. A steganalyzer behaves as a classifier considering a set of features extracted from stego-cover pairs of 3D objects as inputs during the training stage. However, during the testing stage, the steganalyzer would have to identify whether information was hidden in a set of 3D objects which is different from that used in the training. Addressing the CSM paradigm corresponds to testing the generalization ability of the steganalyzer when introducing distortions in the cover objects before hiding information through steganography. The proposed steganalysis robustness approach is tested when considering mesh simplification and additive noise to the 3D objects, bringing significant distortions to their shapes, in the context when using a high capacity steganography method.

I. INTRODUCTION

Steganography and information hiding in 3D graphics has known a rapid expansion during the last years. Steganalysis can be seen as a classification problem in which we aim to identify whether information was hidden or not into a specific medium through steganography or digital watermarking. Steganalysis in audio or image data was studied in [9], [13], [21]. 3D steganalysis algorithms extract certain features from a large number of cover-stego pairs, representing 3D objects before and after hiding information [17], [26]. The parameters characterizing the statistics of these features are then used as inputs for machine learning algorithms aiming to discriminate the stego-objects from cover-objects. In this study we assess the robustness of 3D steganalyzers in the context of the cover source mismatch (CSM) problem, which assumes that in the testing stage we have a much larger variability in the shapes of the objects than those used during the training.

The CSM problem is represented by the realistic scenario that the objects used for a steganalyzer may be originated in a cover source that is different from the one that the steganographer used for hiding information during the training stage [13]. A known example of CSM in the context of image steganalysis, was addressed during the “Break Our Steganographic System” (BOSS) contest [1]. The mismatch of the training set and testing set caused many difficulties to the participants in this contest [1], [8], [10]. The CSM problem was addressed in the image domain by considering the following aspects: the training sets, the feature set and the machine learning methods used for steganalysis.

In the case of digital images, the cover source mismatch problem is analyzed by testing the steganalyzers on images that are taken by cameras with different characteristics than those used during the training. Differences considered in those studies include different ISO levels of noise, characterizing various cameras, as well as different JPEG quality factors [16], [23]. Gul and Kurugollu [10] proposed a feature selection algorithm, in the BOSS context, which calculates the correlation between a feature and the embedding rate as the criterion for its selection. Pasquet et al. [19] proposed to use the Ensemble Classifier with Feature Selection [4] for the CSM problem. The feature selection is considered by evaluating the importance of each feature in the learning process [4]. A feature condensing method, called Calibrated Least Squares (CLS) is proposed in [20] in order to make the high dimensional feature sets compatible with the anomaly detector is employed for steganalysis. A method to mitigate the CSM due to changes in the cover feature is presented in [14]. This approach shifts all the centers of the cover features from different steganographers towards the origin by subtracting the centroid of each steganographer’s cover feature distribution. Other research studies addressing the CSM problem in images aim to find a classifier that would be robust to the variation between training and testing data. In [18] it was shown that simple classifiers, such as the Fisher Linear Discriminant (FLD) ensemble and the Ensemble Average Perceptron have better performances than other, more complex classifiers, when faced with the cover source mismatch problem. In order to mitigate the mismatch due to various changes in stego features, Ker and Pevný [14] used an ensemble of classifiers which gives more weight to those classifiers that are robust to changes in the stego features. A similar weighting strategy for improving the FLD ensemble’s performance in CSM context is presented in [23].

In this paper we propose the Robustness and Relevance Based Feature Selection (RRFS) algorithm for addressing the CSM problem in 3D steganalysis. While we consider that the training of the 3D steganalyzer is performed on a given set of objects, for the testing we apply certain transformations on the cover objects before embedding information into the resulting distorted objects though steganography. We propose to use the Pearson correlation coefficient (PCC) in order to evaluate the relevance of each feature. PCC is then used for estimating the consistency of using 3D features in distinguishing the cover and stego-objects, before and after applying certain transfor-
mations, such as mesh simplification or additive noise. We hide information into these distorted 3D shapes which and then used for testing the steganalyzer. The proposed methodology is tested on the Princeton Mesh Segmentation project database [5], when considering the 3D steganography algorithm proposed in [3]. 3D steganalysis is briefly described in Section II, while the proposed method addressing the CSM problem in the context of 3D steganalysis is explained in Section III. The experimental results are provided in Section IV and the conclusions of this study in Section V.

II. 3D STEGANALYSIS

3D steganalysis consists of training and testing stages as in a supervised pattern recognition approach. While during the first stage, the steganalyzer learns a set of parameters characterizing the differences between sets of 3D stego and cover objects, during the second stage these parameters are used for distinguishing a different set of stego and cover objects. The set of features extracted from the 3D objects is modelled statistically in both the training and testing stages. The first four statistical moments of their features are considered as inputs to a machine learning algorithm. The 3D steganalysis approach proposed in [26] uses the feature set YANG208, which includes the norms in the Cartesian and Laplacian coordinate system [25], the dihedral angles of faces and the face normals, among other features. These features are then used as inputs for a quadratic classifier. Yang et al. [27] proposed a new steganalysis algorithm, specifically designed for the mean-based watermarking algorithm proposed in [6]. Li and Bors propose the feature set LFS52 in [17], which includes the local curvature and vertex normals as steganography features, while dropping some of the other features used in [26], which are not found as being that important in 3D steganalysis. The quadratic discriminant [25] and the FLD ensemble [17], use such features as inputs in order to discriminate the stego-objects from cover-objects.

The cover source mismatch (CSM) problem in 3D steganalysis addresses the robustness of steganalyzers to be trained using a set of cover and stego 3D objects characterized by certain properties and then being tested on a set of stego and cover objects with different surface properties. The ability of the steganalyzer to perform well in different data during the testing stage is consistent to the ability of computational intelligence algorithms to generalize. This corresponds to the application of steganalyzers in practice, because in a general case the 3D objects are characterized by various resolutions and have a wide variation of surface smoothness among other changing factors. In this study we consider mesh simplification and noise addition as transformation factors of the cover objects for addressing the CSM problem. Such transformations would change significantly the geometrical and statistical characteristics of cover sources. Under these conditions, in order to deal properly with the CSM problem, 3D features should be consistent with characterizing stego and cover objects when considering such transformations. Moreover, the machine learning algorithms should be robust to the changes caused by such transformations in the statistical distributions of 3D object features.

III. ROBUSTNESS AND RELEVANCE BASED FEATURE SELECTION ALGORITHM

In the following we consider that we have a set of 3D objects \( O \), used as the cover source for training a steganalyzer. A set of features is extracted from these objects and the parameters characterizing their statistics are then used as inputs in a machine learning classifier in order to distinguish between stego and cover objects. Several 3D features have been found as useful for 3D steganalysis by various studies. The relevance of 3D features used in this study is performed by using the Pearson correlation coefficient between each feature and their object’ corresponding class. Nevertheless, not all of these features contribute equally to the performance of the steganalyzer and not all of them are robust enough to variations in the cover source during the testing stage. In this section we describe a selection mechanism for deciding which features would be robust enough to be used when addressing the CSM problem. The proposed algorithm, called Robustness and Relevance based Feature Selection (RFFS), defines a criterion for choosing those features which will guarantee the steganalysis performance. The key idea of the proposed algorithm is to find those features that are more robust to the variation of the cover source, while preserving a relatively strong relevance to the class label as well. Two criteria are considered during the selection: the relevance of the features to the class label, and the robustness of the selected feature set to the variation of the cover source.

The feature selection algorithm proposed in this study belongs to the filter methods [2], shown to be efficient when used for selecting input features in various machine learning algorithms and its pseudocode is provided on the next page. The filter methods are suitable to be applied in the cover source mismatch situations, because they can avoid the overfitting of the training data whilst being characterised by a better generalization during the testing stage [11]. In the proposed algorithm, the relevance of the features to the class label is estimated by using the Pearson correlation coefficient, calculated between the distribution of each feature and the steganalyzer’s classes:

\[
\rho(X_i, Y) = \frac{\text{cov}(X_i, Y)}{\sigma_X \sigma_Y},
\]

where \( X_i \) is the \( i \)-th feature of a given feature set, \( X = \{X_i| i = 1, 2, \ldots, N\} \), where \( N \) is the dimensionality of the input feature, \( Y \) is the class label indicating whether the class corresponds to a cover or a stego object, \( \text{cov} \) represents the covariance and \( \sigma_X \) is the standard deviation of \( X_i \). The Pearson correlation coefficient can capture the linear dependencies between features and the label, and it is widely used in science as a measure of the degree of linear dependence between two variables, with \( |\rho(X_i, Y)| = 1 \) indicating a high degree of linearity while \( \rho(X_i, Y) = 0 \) indicates a scattered dependency. The former value indicates a stronger relevance to the class
label [12]. All features are ranked according to their relevance to the class label, calculated using equation (1), in descending order as:

$$|\rho(X_i, Y)| > |\rho(X_j, Y)| > \ldots > |\rho(X_{i_N}, Y)|,$$

(2)

where \(I = \{I_1, I_2, \ldots I_N\}\) is the feature index.

**Algorithm 1: RRFS algorithm**

**Input:**
Features extracted from the cover objects used for training \(X_0 = \{X_{0,i} | i = 1, 2, \ldots, N\}\) features extracted from other cover sources \(X_j = \{X_{j,i} | i = 1, 2, \ldots, N, j = 1, 2, \ldots, M\}\) class label \(Y\) dimension of the selected feature \(N'\)

**Output:** Index of the selected feature subset \(F'\)

1. Compute the relevance of the features to the class label, \(\rho(X_i, Y) = \frac{\text{cov}(X_i, Y)}{\sigma_{X_i} \sigma_Y}\);
2. Compute the features’ robustness to the variation of the cover source, \(\rho_i(X_i, X_{j,i}) = \frac{\text{cov}(X_i, X_{j,i})}{\sigma_{X_i} \sigma_{X_{j,i}}}\);
3. Normalize the \(|\rho_i(X_i, X_{j,i})|\) to \([0, 1]\);
4. Compute the robustness of the features to the variation of the cover source, \(r_i = \frac{1}{M} \sum_{j=1}^{M} |\rho_i(X_i, X_{j,i})|\);
5. Sort the features by relevance \(|\rho_i(X_i, Y)|\) in the descending order and get the index \(I = \{I_1, I_2, \ldots I_N\}\);
6. Initialize \(p \leftarrow 90\) and \(\theta_p \leftarrow \text{percentile}([r_i | i = 1, 2, \ldots N], p)\);
7. while \(|F'| < N'\) do
   8.     for \(k \leftarrow I_1\) to \(I_N\) do
   9.         if \((k \notin F') \land (r_k > \theta_p)\) then
   10.             Add \(k\) to \(F'\);
   11.         end
   12.     end
   13.     \(p \leftarrow p - 10\);
   14.     \(\theta_p \leftarrow \text{percentile}([r_i | i = 1, 2, \ldots N], p)\);
15. end
16. return \(F'\);

Features’ robustness to the variation of the cover source is related to solving the CSM problem. If objects’ features do not change much after applying transformations to the cover objects, they would be expected to provide similar steganalysis results to those achieved with the original cover and stego objects. Such features would have a strong robustness in the context of steganalyzers. In the following we consider two different feature sets for a given set of 3D objects: the first one is extracted from the original objects used as the cover sources for training the steganalyzers while the other is extracted after applying certain transformations to the same objects. Then the Pearson correlation coefficient of two feature sets is calculated as:

$$\rho_i(X_i, X_{j,i}) = \frac{\text{cov}(X_i, X_{j,i})}{\sigma_{X_i} \sigma_{X_{j,i}}},$$

(3)

where \(X_i\) and \(X_{j,i}\) represent the vector of the feature \(i\) extracted from the original set of cover objects \(C\), used for training the steganalyzer, and from the objects obtained by applying specific transformations to the same cover source, \(j = 1, 2, \ldots, M\), where \(M\) represents the number of transformations applied to the original set of cover objects \(C\). This formula indicates how well correlated are the initial 3D features with those that are extracted after certain transformations. We normalize \(|\rho_i(X_i, X_{j,i})|\) to the interval \([0, 1]\). Ideally, robust features should model the statistical characteristics that distinguish cover and stego objects even after certain distortions are considered on the cover objects. The robustness is indicated by the average of the absolute values of the Person correlation coefficients, calculated for a specific feature \(i\), for all \(M\) transformations:

$$r_i = \frac{1}{M} \sum_{j=1}^{M} |\rho_i(X_i, X_{j,i})|,$$

(4)

where \(i = 1, 2, \ldots, N\).

Fig. 1. Applying surface simplication on the cover object in order to test cover-source mismatch paradigm in 3D steganalyzers.

The Robustness and Relevance based Feature Selection (RRFS) algorithm starts with a preset number of \(N\) features as input. The algorithm aims to find the most \(N'\) relevant features which have relatively strong robustness to be used for a steganalyzer that addresses the CSM problem. The \(N'\) features are selected by multiple passes through the features ranked according to their relevance, calculated using equation (1). During each pass, a subset of features is selected successively such that:

$$r_i > \theta_p,$$

(5)

where \(\theta_p\) represents the threshold for the correlation corresponding to the \(p\)-th percentile of all \(r_i\)’s, characterising the robustness of the steganalyzer. Initially, \(p\) is set at 90. If the number of selected features \(n < N'\), then we reduce the threshold to the value corresponding to \(p - 10\), and consider a new threshold \(\theta_{p-10}\) instead of \(\theta_p\). In this way with each iteration we add additional features to the set of selected features such that whilst increasing the feature set we preserve
the classification capability of the algorithm. The threshold is reduced, considering lower percentiles \( p \), until the total number of selected features becomes equal to \( N' \). Eventually, we would have \( N' \) selected features that are robust enough to the variation of cover source whilst having a high relevance to the class label, according to (1), at the same time.

IV. EXPERIMENTAL RESULTS

In the following we firstly apply the RRFS algorithm to select a feature subset from a given larger feature set. Then we test the performance of the selected feature subset by using it in a cover source mismatch scenario. For the experimental framework we consider 354 3D objects represented as meshes which are part of the Princeton Mesh Segmentation project [5] database. In order to test the robustness of the steganalyzer we distort the original objects of the database by considering two different transformations: mesh simplification and corruption by noise. These transformations significantly degrade the properties of 3D objects. While the former changes the actual topology of the mesh, the latter alters its geometry. The simplification algorithm from [22] reduces the number of the faces while preserving the overall shape of the 3D object, according to a simplification factor \( \lambda = \{0.98, 0.95, 0.9, 0.8, 0.6\} \). When considering corruption by noise, its amplitude of the noise is modulated by the parameter \( \beta D \), with \( \beta \in \{10^{-5}, 10^{-4}, 10^{-3}\} \), and \( D \) is the maximum distance between the projections of any two vertices on the first principal axis, obtained by applying the Principal Component Analysis (PCA) on the original 3D object.

The stego objects are generated by applying the 3D steganography algorithm proposed in [3] to the given set of cover sources. The number of steganographic embedding layers is considered as 10 and the number of intervals is chosen as 10000 in the algorithm proposed in [3]. The relative payload ratio is nearly 1, except for three vertices used for extracting the code, which are not modified at all. Similarly to the approach from [17] we consider FLD ensembles [7], [15] as the machine learning based steganalyzer. The parameters for the FLD ensembles, such as the number of the base learner and the subspace dimensionality, are chosen as in [15]. The close-up detail of one of the original 3D objects used in the experiments is shown in Figure 1a, while its corresponding stego object obtained by embedding information after mesh simplification with the factor \( \lambda = 0.6 \), is shown in Figure 1b.

In the following we test the efficiency of using various feature sets for 3D steganalysis. In Figures 2 and 3 we show the Receiver Operating Curves (ROC) results when considering the LFS52, proposed in [17], and YANG208 feature sets proposed in [26], for training the Quadratic Learning classifier and the FLD ensemble classifier, respectively, in the context when detecting the changes produces by the steganographic algorithm from [3], considering ten layers of embedding. According to the ROC curves from both plots we can observe that the feature set LFS52 provides the best results in the case of both classifiers.

In the following we combine two feature sets used for 3D steganalysis, LFS52 [17] and YANG208 [26], respectively, eliminating the eight features that are common to both feature sets, and we obtain a total of \( N = 252 \) features, called LAY252. This feature set is initially extracted from the cover-objects from the original set of objects. The same objects are then transformed by mesh simplification or by adding noise and their corresponding stego-objects are obtained by embedding information into the transformed objects. Then we use the RRFS algorithm to select the appropriate feature subset from LAY252 in order to mitigate the CSM problem due to either simplification or noise addition, respectively. In the case of mesh simplification, we firstly calculate the relevance of all the features from LAY252, \( \{\rho(X, Y) \mid i = 1, 2, \ldots, 252\} \), based
on the 354 cover-stego pairs obtained from the original cover source. Meanwhile, we compute the robustness of the feature set \( \{ r_i | i = 1, 2, \ldots, 252 \} \) based on the experiments using the cover-stego pairs from the simplified cover sources, assuming \( M = 5 \) different simplification factors as specified above. The \( N' \)-dimensional feature subset is selected as explained in Section III. The selection of the feature subset for the CSM due to noise addition is similar to that when assuming mesh simplification in the CSM paradigm. During the experiments we select various features, assuming \( N' \leq N \). If \( N' = 252 \) it would mean that no feature selection process is conducted at all. In order to test the performance of the selected features in the cover source mismatch (CSM) scenario, we randomly select 260 cover objects from the original cover source and the corresponding stego-objects for training the steganalyzer. Then we test the steganalyzer on 94 pairs of cover and stego-objects originated from different cover sources from the database, after they had been simplified or distorted by additive noise. We repeat the steganalysis experiments, using FLD ensembles for 30 times and consider the final test results as the median of the resulting errors.

![Fig. 4. Test results, under the CSM paradigm, when selecting features for steganalysis where the distortion to the original cover objects is due to mesh simplification.](image)

Figures 4 and 5 show the test results when using features selected by the proposed RRFS method from the initial feature set LAY252 for steganalysis under the CSM assumption, by considering the distortions caused by mesh simplification and by additive noise, respectively. As it can be observed from these two plots, as the dimensionality of the selected features increases, the error rates first decline and then rises up. There are several local fluctuations in the plots, but generally these plots display clear minima, except for the case when the noise level of the testing set corresponds to \( \beta = 10^{-3} \), when the level of the error does not change much for \( N > 60 \). When testing the CSM problem for mesh simplification, the results from Figure 4 show that the steganalyzer achieves the best detection accuracy for \( N = 40 \), while when considering the CSM problem for additive noise, the results from Figure 5, indicate that the best results are obtained for \( N = 90 \). The bar plots from Figure 6 show clearly that the steganalyzers trained with a lower dimensional data set, when considering the features selected by the proposed RRFS method, achieve better performance when compared to the results produced by training the steganalysed with the entire dataset LAY252, under the CSM paradigm.

![Fig. 5. Test results, under the CSM paradigm, when selecting features for steganalysis where the distortion to the original cover objects is due to noise addition to the mesh surface.](image)

![Fig. 6. Test results when using the entire feature set compared to the results provided by a selected set of robust features for training the steganalyzers under the CSM paradigm.](image)

V. Conclusion

This research study proposes a solution for the cover source mismatch problem in the context of 3D steganalyzers. According to the CSM paradigm, we consider that the objects considered during the testing stage are significantly different from those used during the training. In this study we consider mesh simplification and additive noise for transforming the cover objects when testing the steganalyzer under the CSM paradigm. In the experimental results we consider a high capacity 3D steganography method for hiding information in...
the transformed objects. A robust feature selection algorithm, called the Robustness and Relevance based Feature Selection, is proposed in this paper. This algorithm employs the Pearson correlation coefficient to define the relevance and robustness for each feature leading to the selection of a relevant feature subset. The proposed methodology is shown to choose a better feature set, than those considered by other studies, when addressing the CSM problem. A limitation of this study is that for selecting the robust features we consider a limited set of transformations for addressing the CSM problem. A more general study should compare the set of cover objects with a set of transformed objects originated from completely different cover sources than those initially used in the training stage.

REFERENCES


