Numerical modelling of hydro-morphological processes dominated by fine suspended sediment in a stormwater pond

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Abstract

Fine sediment plays a crucial and multiple role in the hydrological, ecological and geomorphological functioning of river systems. This study employs a two-dimensional (2D) numerical model to track the hydro-morphological processes dominated by fine suspended sediment, including the prediction of sediment concentration in flow bodies, and erosion and deposition caused by sediment transport. The model is governed by 2D full shallow water equations with which an advection–diffusion equation for fine sediment is coupled. Bed erosion and sedimentation are updated by a bed deformation model based on local sediment entrainment and settling flux in flow bodies. The model is initially validated with the three laboratory-scale experimental events where suspended load plays a dominant role. Satisfactory simulation results confirm the model's capability in capturing hydro-morphodynamic processes dominated by fine suspended sediment at laboratory-scale. Applications to sedimentation in a stormwater pond are conducted to develop the process-based understanding of fine sediment dynamics over a variety of flow conditions. Urban flows with 5-year, 30-year and 100-year return period and the extreme flood event in 2012 are simulated. The modelled results deliver a step change in understanding fine sediment dynamics in stormwater ponds. The model is capable of quantitatively simulating and qualitatively assessing the performance of a stormwater pond in managing urban water quantity and quality.

1. Introduction

In river systems, fine-grained sediment is a natural and essential component and plays a crucial role in the hydrological, ecological and geomorphological functioning of the system. It has been recognised that fine-grained sediment management in urban rivers is environmentally significant (Birch et al., 2006). Sustainable sediment management requires a structure of supporting research on fine sediment dynamics and its interactions within hydrological catchments such as rivers, floodplains, reservoirs and Sustainable Urban Drainage Systems (SuDS) (Owens et al., 2005).

In general, fine-grained sediment has a controlling influence on the quality and quantity of receiving water. In an urban catchment, contaminants and pollutants including heavy metals and nutrients are generally absorbed by fine sediment which is then conveyed to the receiving waters (Saeedi et al., 2004; Jartun et al., 2008; Jones et al., 2008). These urban pollutants attached to sediments have implications on both habitats of downstream receiving waters and human health (Wood and Armitage, 1997; Owens et al., 2005; Crosa et al., 2010). To mitigate these risks, more sustainable features, such as stormwater ponds, are increasingly used in urban catchments as an option to manage fine suspended sediments (Ahilan et al., 2016; Allen et al., 2017) by storing stormwater runoff, trapping fine sediments and improving urban runoff quality. The movement of sediment will be minimised by the interrupted flows in a storm water pond. The low energy environment in the pond enables the considerable proportion of fine suspended load is trapped which provides water quality benefits to receiving water bodies. However, from a longer-term viewpoint, this will diminish the storage capacity of stormwater ponds, thereby influencing their hydraulic performance and maintenance. Similarly, fine-grained sedimentation occurs in dam reservoirs where the release of deposited sediments often leads to cascading effects in downstream reaches through sediment transport and re-deposition.
This has been considered to be a worldwide problem (Vörösmarty et al. (2003)). Additionally, excessive suspended sediment inputs to rivers due to catchment erosion and in-channel bank erosion can cause sedimentation in channels which may affect channel morphology, stream habitats and navigation (Eekhout et al., 2015). In view of the sediment effects, natural processes have been widely used for river and flood management in recent years (Dadson et al., 2017). In the aforementioned cases, fine suspended sediment has a controlling influence on the quality and quantity of receiving waters in hydrosystems through playing a variety of roles. Therefore, there is a need to develop an improved understanding of how fine-grained sediment is eroded, transported and deposited by a variety of flow environments.

In recent years, numerical models have been increasingly used to understand complex flows, sediment transport and the corresponding morphological changes in rivers, floodplains and SuDS. In view of the multiple roles of fine-grained sediment in receiving waters, a robust fine sediment model is crucial to develop coupled models enabling the simulations and understanding of hydrological, ecological and geomorphological conditions of catchments. Recently numerical models have been used to simulate dam-break induced in-channel evolution (Cao et al., 2004; Simpson and Castellotti, 2006; Bohorquez and Fernandez-Feria, 2008; Zech et al., 2008; Guan et al., 2015a; Benkhaldoun et al., 2012; Li and Duffy, 2012; Guan et al., 2014), sediment routing in dam reservoirs (Liu et al., 2004; Guertault et al., 2016), turbidity currents over damaged levees (Duffy, 2012; Guan et al., 2014), sediment routing in dam reservoirs (Eekhout et al., 2015). In view of the sediment effects, natural processes have been widely used for river and flood management in recent years (Dadson et al., 2017). In the aforementioned cases, fine suspended sediment inputs to rivers due to catchment erosion and in-channel bank erosion can cause sedimentation in channels which may affect channel morphology, stream habitats and navigation (Eekhout et al., 2015).

2. Numerical model

2.1. Hydrodynamic model

Shallow water based numerical models have been widely used for hydraulic modelling due to their robustness in capturing flow hydraulics (Guan et al., 2013; Vacondio et al., 2014; Costabile and Macchione, 2015; Hou et al., 2015; Guan et al., 2015b). The 2D shallow water equations can be expressed by:

\[ \frac{\partial h}{\partial t} + \frac{\partial hu}{\partial x} + \frac{\partial hv}{\partial y} = 0 \]  

\[ \frac{\partial hu}{\partial t} + \frac{\partial}{\partial x} \left( hu^2 + \frac{1}{2} gh^2 \right) + \frac{\partial hu v}{\partial y} = \frac{\partial T_{xx}}{\partial x} + \frac{\partial T_{xy}}{\partial y} - gh \frac{\partial z_b}{\partial x} - gh S_h + \frac{\Delta \rho}{\rho} \frac{\partial z_b}{\partial t} - \frac{\Delta \rho g h^2}{2 \rho} \frac{\partial C}{\partial x} \]  

\[ \frac{\partial hu}{\partial t} + \frac{\partial hu v}{\partial y} + \frac{\partial}{\partial y} \left( hv^2 + \frac{1}{2} gh^2 \right) = \frac{\partial T_{xy}}{\partial x} + \frac{\partial T_{yy}}{\partial y} - gh \frac{\partial z_b}{\partial y} - gh S_h + \frac{\Delta \rho}{\rho} \frac{\partial z_b}{\partial t} - \frac{\Delta \rho g h^2}{2 \rho} \frac{\partial C}{\partial y} \]  

where \( h \) = flow depth, \( z_b \) = bed elevation, \( \eta = h + z_b \) denotes the water surface elevation which includes both changes of the water depth and bed elevation varying with the time \( t \), \( u \) and \( v \) = the depth-averaged flow velocity components in the two Cartesian directions, \( g \) = acceleration due to gravity, \( p \) = sediment porosity, \( C \) = total volumetric sediment concentration, \( \rho_1 \) and \( \rho_2 \) denote the densities of sediment and water respectively, \( \Delta \rho = \rho_2 - \rho_1 \) = density of flow-sediment mixture, \( S_h \), \( S_r \) = frictional slope in \( x \) and \( y \) components which are calculated based on Manning's roughness coefficient \( n \) by \( S_h = \sqrt[3]{\frac{e_i}{e_x}} \), \( S_r = \sqrt[3]{\frac{e_i}{e_y}} \), \( T_{xx}, T_{xy}, T_{yy} \) and \( T_{yx} \) are the depth-averaged turbulent stresses which are determined by the Boussinesq approximations which has been widely used in the literature (e.g. Wu, 2004; Abad et al., 2008; Begnudelli et al., 2010). This gives the Reynolds stresses as:

\[ T_{xx} = -2 \left( \nu + v \right) \frac{\partial u}{\partial x} \]  

\[ T_{xy} = - \left( \nu + v \right) \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) \]  

\[ T_{yy} = -2 \left( \nu + v \right) \frac{\partial v}{\partial y} \]  

where \( \nu \) = the turbulence eddy viscosity and \( v \) = the molecular viscosity which can be ignored in environmental applications. Various approaches have been adopted to estimate the turbulence viscosity, e.g. assuming a constant eddy viscosity, an algebraic turbulence model (\( \nu = \beta h u^* \)), as well as the \( k-\epsilon \) turbulence model. In this study, the eddy viscosity is estimated by \( \nu = \beta h u^* \) with \( \beta = 0.5 \).

2.2. Fine suspended load model

The suspended load transport is governed by the advection–diffusion equation. For non-uniform graded sediment mixtures, it is necessary to divide the graded sediments into fractions due to the difference of grain-size related parameters (Guan et al., 2015b). For the suspended transport of each fraction, the governing equation is described by:

\[ \frac{\partial \bar{C}_i}{\partial t} + \frac{\partial \bar{u} \bar{C}_i}{\partial x} + \frac{\partial \bar{v} \bar{C}_i}{\partial y} = \frac{\partial}{\partial x} \left( e_i \bar{h} \frac{\partial \bar{C}_i}{\partial x} \right) + \frac{\partial}{\partial y} \left( e_i \bar{h} \frac{\partial \bar{C}_i}{\partial y} \right) + \left( S_{E,i} + S_{D,i} \right) \]  

where \( e_i \) = the diffusion coefficient of sediment particles; \( S_{E,i} \) = the entrainment flux of sediment for the ith fraction; \( S_{D,i} \) = the deposition flux of sediment of the ith fraction. The diffusion coefficient of sediment particles is related to the diffusion of fluid momentum, and it is determined by using the below formula presented in van Rijn (1984):

\[ e_i = 6 \beta \phi V_i \]  

where the factor \( \beta \) represents the difference in the diffusion of a sediment particle and a fluid particle and it is assumed to be constant over the flow depth (van Rijn 1994). \( \phi \) represents the damping
of the fluid turbulence by the sediment particles and it is assumed to be dependent on the local sediment concentration. Both factors are calculated by using the formula derived by van Rijn (1984), which are widely used (e.g. Duan and Nanda, 2006).

\[ \beta = 1 + 2 \left( \frac{\theta_f}{u_r} \right)^2 \] for \( 0.1 < \frac{\theta_f}{u_r} < 1 \)

\[ \phi = 1 + \left( \frac{C_a}{C_{aw}} \right)^{0.8} - 2 \left( \frac{C_a}{C_{aw}} \right)^{0.4} \]

where \( C_a \) is the near-bed concentration at the reference level \( a \) (average for non-uniform sediments); \( C_{aw} \) is the near bed equilibrium concentration (average for non-uniform sediments). Both are defined below. As there is no universal theoretical expression for the entrainment flux and deposition flux of sediments, both variables are calculated by the following widely-used function.

\[ S_{E,j} = F_t \theta_f \delta C_{aw} \quad S_{D,j} = F_t \theta_f C_{aw} \] (5)

where \( F_t \) percentage of the \( j \)th grain fraction; \( \theta_f \) is the effective settling velocity for the \( j \)th grain fraction which is calculated by the function derived by Soulsby (1997) as below;

\[ \theta_f(j) = \sqrt{10.36^2 + (1 - C_i)^4 1.049d_i^3 - 10.36} \] (6)

\[ C_{aw} = \delta C_a \] is the near-bed concentration for the \( j \)th grain fraction at the reference level \( a \); the definition of the coefficient \( \delta \) by Cao et al., (2004) is: \( \delta = \min \{2(0.1 - C_i)/C_i \} \); \( C_{aw} \) is the near bed equilibrium concentration for the \( i \)th grain fraction at the reference level that is calculated by using the van Rijn formula (van Rijn, 1984). For each grain fraction, the function can be expressed as

\[ C_{aw,i} = 0.015 \frac{d_{50}}{a} \frac{T^{1.5}}{d_{50}^2} \] (7)

\[ T = \frac{\left( u^2 - u_{cr}^2 \right)}{u_{cr}} \]

\[ a = \min \{ \max \{ k, 2d_50, 0.01h \}, 0.2h \} \]

where \( k \) is the equivalent roughness height; \( d_50 = d \rho_d/\rho_w - 1 \) is the dimensionless particle diameter; \( v \) is the viscosity of water; \( u_r = \sqrt{gh/C} \) is bed-shear velocity related to grain; \( C' \) is the Chézy-coefficient related to grain; \( u_{cr} = \sqrt{(s - 1)gd/\theta_c} \) is the critical bed-shear velocity, where \( \theta_c \) is the Shields shear stress.

2.3. Morphological change model

Morphological evolution is determined by the difference of sediment entrainment and deposition that is calculated per grid cell at each time step. The equation used to calculate morphological change is written by

\[ \frac{\partial z_g}{\partial t} = \sum_{i=1}^{N} \frac{\partial z_g}{\partial t} = \frac{1}{1 - p} \sum_{i=1}^{N} \left( S_{D,i} - S_{E,i} \right) \] (8)

where \( N \) is the number of grain size fractions.

2.4. Numerical method

Eqs. (1) and (3) and (8) constitute the model system which is a shallow water non-linear system. In compact form, the governing equations can be expressed by

\[ \frac{\partial \mathbf{U}}{\partial t} + \frac{\partial \mathbf{E}}{\partial x} + \frac{\partial \mathbf{F}}{\partial y} + \frac{\partial \mathbf{E}}{\partial x} + \frac{\partial \mathbf{F}}{\partial y} + \mathbf{S} \]

where

\[ \mathbf{U} = \begin{bmatrix} \eta \\ hu \\ hv \\ hC_i \end{bmatrix}, \quad \mathbf{E} = \begin{bmatrix} hu \\ hu^2 + \frac{1}{2}gh^2 \\ hv \\ hC_i \end{bmatrix}, \quad \mathbf{F} = \begin{bmatrix} hu \\ hv \\ h^2v^2 + \frac{1}{2}gh^2 \end{bmatrix}, \quad \mathbf{S} = \begin{bmatrix} \end{bmatrix} \]

where \( \mathbf{U} \) is the vector of conserved variables; \( \mathbf{E} \) and \( \mathbf{F} \) are the flux vectors of the flow in the \( x \) and \( y \) directions respectively; \( \mathbf{E} \) and \( \mathbf{F} \) contain the turbulent terms in the \( x \) and \( y \) directions, \( \mathbf{S} \) is the source term vector.

The model is solved numerically by a well-balanced Godunov-type finite volume method (FVM) based on Cartesian coordinates. To update the variables in each cell, the following equation is used to update hydrodynamics:

\[ U^{i+1} = U^i - \frac{\Delta t}{\Delta x} (E^i - E^{i+1}) - \frac{\Delta t}{\Delta y} (F^i - F^{i+1}) + \Delta S_{ij} \] (9)

where the vectors \( E^i \) and \( F^i \) are the difference of the fluxes at the left and right interfaces of the cell \((i, j)\) in the \( x \) and \( y \) direction; \( E^i \) and \( F^i \) represents the flux difference of turbulent and dispersion stresses at the left and right interfaces of the cell \((i, j)\) and \( \Delta t, \Delta x, \Delta y \) are the time step, cell size in the \( x \) and \( y \) direction, respectively. To calculate the first three flux terms (e.g. \( E_{r_{123}} \)), the Harten, Lax and van Leer (HLL) scheme has been used in this study. More details are described in Guan et al., (2014). Similar to updating the hydrodynamic variables, the sediment concentration is updated at the same cell and time step based on the sediment inter-cell flux \( C^* \) as follows,

\[ C^{i+1}_{ij} = \frac{C^*_{ij} - x \left( \Delta t / \Delta x \right) \left( C^{i+1}_{ij} - C^*_{ij} / \Delta t \right) + \Delta t \left( C^{*}_{ij} - C^*_{ij} / \Delta t \right) + \Delta S_{ij}}{\Delta t} \] (10)

where \( t \) represents the time; \( S_{ij} \) is the source term shown in the right hand side of Eq. (3). The sediment flux \( C^* \) is calculated using the following equation,

\[ C^* = C^{i+1}_{ij} + \frac{\left( E^i_{l_{ij}} + F^i_{r_{ij}} \right) C S^i_{ij}}{C_{ij}} \]

where \( C \) and \( C^* \) are the volumetric sediment concentration at the left and right cells; \( E^i_{l_{ij}}, F^i_{r_{ij}} \) represent the flow intercell mass flux. \( S_{ij} \) is the middle wave speed calculated by the equation of Toro (2001). A variable time step \( \Delta t \), adapted to local flow conditions, is calculated at each time step based on a fixed Courant number (CFL) for stability (0 < CFL < 1.0).
3. Results and discussion

3.1. Model validation

Three laboratory cases were used to verify the model capability in simulating morphological changes dominant by fine suspended load, which includes (1) sediment transport in a trench, (2) partial dam-breach flow over a mobile channel, and (3) localised erosion and deposition in a pond with erodible bed. In all three experimental cases, it has been observed that suspended load is the main transport mode, which ensures the applicability of the cases in the model verification. Here the model errors with the measured data were quantified using the Brier Skill Score (BSS) as:

$$\text{BSS} = 1 - \frac{1}{n} \sum_{i=1}^{n} \left( \frac{x_i^o - x_i^m}{x_i^o - x_i^{\min}} \right)^2$$  \hfill (13)

where superscripts $m$ and $o$ refer to modelled and observed point data, respectively, and $n$ is the total number of point data.

3.1.1. Sediment transport in a trench

To verify the capability of the proposed model in predicting bed evolution under the conditions of unsteady flows a simulation was carried out to compare with experiments originally conducted at the Delft Hydraulics Laboratory to investigate the movable bed evolution caused by steady open channel flow (van Rijn, 1980). The trench is located in the middle of the 30 m long channel. Three tests with different side slopes of the trench (1:3, 1:7 and 1:10) were performed in the experiments. Following van Rijn (1980), the key information of the three tests is listed in Table 1. The mean inflow velocity was 0.51 m/s at the inlet and the water depth were kept constant as 0.39 m. The erodible bed consists of fine sand with $d_{10} = 0.115$ mm, $d_{50} = 0.16$ mm and $d_{90} = 0.2$ mm. The sand density and porosity was 2650 kg/m$^3$ and 0.4 respectively. According to the experiment, the settling velocity of sediment particles was 0.013 m/s ± 25%. A hindering settling velocity $v_{hs} = 0.015$ m/s is used. Manning’s coefficient $n$ is set to be 0.016. In addition, to maintain the sediment equilibrium conditions in the upstream, i.e. no scour or deposition occurring, sand with the same composition was fed at a constant rate of 0.04 kg/s/m; thereby, the suspended load transport rate was estimated to be 0.03 ± 0.006 kg/s/m and the bed load transport rate of about 0.01 kg/s/m. The contribution of the suspended load transport to the total load transport was in the range of 60% to 90%.

For simulation, the whole domain is discretised by 150 cells with $\Delta x = 0.2$ m. To ensure steady flow, the model is run for 900 s. After 900 s, sand is fed and bed evolution occurs. Van Rijn (1984) suggested estimating the reference level by the following equation, $a = \min[\max(k_i, 2d_{90}, 0.01h), 0.2h]$. Based on this formulation, $a = 0.01$ m and $a = 0.02$ m was used in the model to demonstrate the influence of the reference level. Fig. 1 plots the simulated velocity and depth-averaged measurement at the five measured sections. It can be seen that the model produces the velocity reasonably well around the trench. Also, the water surface has been simulated to be close to the real constant value 0.39 m. Regarding the predictin of changes in bed profiles, Fig. 2 indicates that the simulated bed profiles with $a = 0.01$ m and $a = 0.02$ m show similar shape with only a slight difference. With both reference levels, the simulated bed has a high Brier Skill Score which is over 0.9. When $a = 0.01$ m, the model gives a better results. Therefore, the model is also verified in Test 2 and Test 1 with the reference level $a = 0.01$ m. As shown in Fig. 3, the general bed profiles at both 7.5 h and 15 h are produced with a good BSS. This implies the capability of the model in simulating bed changes due to sediment transport dominant by suspended load.

3.1.2. Partial dam-breach flow over a mobile channel

To verify and validate the performance of the suspended load model it was used to reproduce partial dam-breach flow experiments over a mobile bed, which were carried out at the Hydraulics Laboratory of Tsinghua University, China (Xia et al., 2010). A thin dam was located 2.0 m downstream of a 18.5 m × 1.6 m rectangular flume, and a 0.2 m wide dam-breach centred at $y = 0.8$ m; the region of 4.5 m after dam site was covered by fine non-uniform coal ash with a median diameter of 0.135 mm, and its natural and dry density were measured approximately as 2248 kg/m$^3$ and 720 kg/m$^3$ respectively; the water depth was initially set to be 0.4 m in the reservoir and 0.12 m downstream of the dam. In this experiment, the bed levels at two cross sections CS1 ($x = 2.5$ m) and CS2 ($x = 3.5$ m) after 20 s were measured. During the whole experiment, only suspended load transport occurs due to the particles being so fine. Table 2 lists the key parameters used in the simulation. For the simulation, the domain is discretised by 370 × 80 cells, and the time interval is $\Delta t = 0.005$ s. The Manning’s coefficient $n = 0.02$ s/[m$^{1/3}$]; the sediment porosity is set as 0.35. The suspended load model is run for 20 s. Fig. 4 shows a comparison between the observed and modelled cross-sectional profiles at 20 s. It is shown that the trend of the predicted bed profiles is similar to that of the measured profiles. Erosion occurs in the middle of the cross sections. The bed erosion quantity is less than the measurement at CS1 where the predicted bed is underestimated, particularly in terms of the erosion width. However, a similar maximum scour depth and location are predicted here. At CS2, the simulated and measured bed profiles are in good agreement with each other. The simulated and measured scour depths are very close and the erosion areas agree very well with each other, but the measured range of bed profile is about 20 cm wider than the simulated range. For this reason, it can be seen that the BSS for CS2 is relatively smaller. The bed deposition is underestimated by the model here. This is possibly due to either the

![Fig. 1. Depth-averaged measured velocity and simulated velocity at the equilibrium state for Test 3.](image-url)

<table>
<thead>
<tr>
<th>Table 1</th>
<th>Key parameters of the three tests.</th>
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<tbody>
<tr>
<td>side slopes</td>
<td>1:3 (Test 1), 1:7 (Test 2), 1:10 (Test 3)</td>
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<tr>
<td>channel length</td>
<td>30 m</td>
</tr>
<tr>
<td>inflow velocity at inlet</td>
<td>0.51 m/s</td>
</tr>
<tr>
<td>water depth at inlet</td>
<td>0.39 m</td>
</tr>
<tr>
<td>sand diameters</td>
<td>$d_{10} = 0.115$ mm, $d_{50} = 0.16$ mm, $d_{90} = 0.2$ mm</td>
</tr>
<tr>
<td>sand density</td>
<td>2650 kg/m$^3$</td>
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<tr>
<td>hindering settling velocity</td>
<td>0.015 m/s</td>
</tr>
<tr>
<td>Suspended load</td>
<td>0.03 ± 0.006 kg/s/m</td>
</tr>
<tr>
<td>bed load</td>
<td>0.01 kg/s/m</td>
</tr>
<tr>
<td>Manning’s coefficient</td>
<td>0.016 s/[m$^{1/3}$]</td>
</tr>
<tr>
<td>mesh size/number</td>
<td>0.02 m/150</td>
</tr>
</tbody>
</table>
experimental errors or the neglected turbulence term, which means the model may not be able to generate the rapid formation of horizontal circulating flow at the downstream of the dam. Fig. 5 illustrates the contour plot of the simulated bed topography after 20 s. Severe erosion occurs at the outlet of the dam, and the eroded suspended load is flushed to deposit downstream due to the decrease of bed shear stress.

3.1.3. Erosion and deposition in a pond with erodible bed

The experiment was conducted to investigate the erosion process in a rectangular basin due to clear water inflow from a narrow channel by Thuc (1991). In this test, the initial setup involves an inlet rectangular channel of 2.0 m long and 0.2 m wide, a rectangular movable basin with 5.0 m long and 4.0 m wide, and a 1.0 m long and 1.2 m wide channel in the downstream. Therein, the movable basin consists of fine sand with median diameter of 0.6 mm, with a movable bed layer was 0.16 m thick. For the initial hydraulic conditions, initial water depth was specified as 0.15 m; the inflow velocity at the inflow boundary was kept constant at 0.6 m/s, and the water depth at the outlet was a constant value of 0.15 m. Only basin area is erodible during the experiment period. Table 3 show the key parameters of the experimental case. This experiment is simulated in this study because the sediment particle diameter is small (0.6 mm), and the rouse number of the case is estimated to be in a range of 0–2.4 in the main movable area, which means suspended load is the dominant transport mode. This fits the capability of the present model.

The length of channel is discretised with a constant interval $D_x = 0.1$ m, but in width direction, the grid spacing around the

![Fig. 2. Simulation results for different reference levels at 7.5 h and 15 h.](image1)

![Fig. 3. Simulated and measured bed profiles for (a) Test 2 and (b) Test 1.](image2)

![Fig. 4. Comparison between measured and simulated bed profiles at CS1 and CS2.](image3)

<table>
<thead>
<tr>
<th>Table 2</th>
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<tr>
<td>Key parameters of the case.</td>
</tr>
<tr>
<td>water depth</td>
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<td>sand diameters</td>
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<td>sand density</td>
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<td>hindering settling velocity</td>
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centreline (±0.6 m) is set to be finer (Δy1 = 0.02 m) than that in other parts (Δy2 = 0.05 m). The computational mesh in the basin consists of 80 × 116 cells. The time step for flow and sediment calculation is set the same at 0.009 s. The Manning’s roughness coefficient n in the basin is given a value of 0.03 s/[m1/3]. The model was run for 2 h of experiment time. Eq. (4) is used to calculate the entrainment and deposition fluxes in this case. Fig. 6(a) shows the simulated bed change pattern around the inflow region at the centre part of the basin after 4 h, and Fig. 6(b) demonstrates the flow velocity field and bed shear stress. It can be seen that the inflow pipe has the biggest bed shear stress due to the high flow velocity, and the inflow pipe outfall area and the outlet area also have higher bed shear stress. Therefore, it can be seen that significant erosion occurs at the outfall area due to the inflow of clear water, then the eroded sediment moves downstream and deposits forming a hill. Since only basin area is erodible, no bed changes are found at the outlet area. Fig. 7 further shows the comparison of the measured and simulated bed changes along the longitudinal centreline at 1 h, 2 h and 4 h. All have a satisfying Brier Skill Score (BSS). Overall, the simulated morphological evolution tendency at 1 h and 2 h are in good agreement with the measured results. However, the maximum deposition heights are slightly underpredicted, with a 13.4% difference at 1 h and 30.6% at 2 h. Furthermore, it can be seen that the model overestimates the erosion depth at the inlet of the basin. There the simulated erosion is much more severe than the measured erosion. This is most likely because secondary flow plays an important role here; however, these non-hydrostatic flows are neglected in the current model.

| Table 3 |
| Key parameters of the case. |
| water depth at outlet | 0.15 m |
| inflow velocity at inlet | 0.6 mm |
| sand diameters | d50 = 0.6 mm |
| sand density | 2650 kg/m³ |
| settling velocity | 0.013 m/s |
| Manning’s coefficient | 0.03 s/[m1/3] |
| sediment porosity | 0.35 |
| mesh size | Δx = 0.1 m, Δy1 = 0.02 m, Δy2 = 0.05 m |
| mesh number | 80 × 116 cells |

Fig. 5. Bed topography contour at 20 s.

Fig. 6. (a) Bed topography contour, and (b) bed shear stress and velocity field at 2 h.

Fig. 7. Comparison between measured and simulated bed profiles at the centerline.
3.2. Application in a stormwater pond

Stormwater ponds are characterised by urban runoff detention, runoff quality improvement and sediment trapping. The decrease in flow velocity and the low energy environment causes deposition of fine sediments delivered by urban flows as it enters the pond. Stormwater pond sedimentation leads to a decrease in pond storage capacity and triggers environmental and economic issues. The validated model is applied to a case study of a stormwater pond in Newcastle Great Park and based on the results, improved understanding of fine sediment dynamics is developed.

3.2.1. Study site

The study area is located in Ouseburn catchment (the black boundary in Fig. 8a) in Newcastle upon Tyne in the UK. The stormwater pond connects the upstream newly built urban development and the Ouseburn River. Fig. 8c shows the simulated domain which is an area of 230 m by 140 m. It was observed that the pond is covered with dense vegetation which protects the local bed. For simulations, the flow discharge is input to the model via a pipe section as an upstream boundary. The other boundary is set to be free open which means that the floodwater can freely flow out based on the local flow conditions.

3.2.2. Model scenarios

Three scenarios were considered: non-flood (5 year), sewer design (30 year) and flood (100 year) (Fig. 9a). Also, rainfall events in the extreme flow year 2012 with 15 min interval rainfall measurements at the Jesmond Dene gauging station (EA #19356) were used to conduct an annual sediment simulation, and the flow at the inlet for the identified rainfall events is quantified by using the physically-based conceptual rainfall-runoff model – the Revitalised Flood Hydrograph (ReFH) model (Fig. 9b).

Allen et al. (2015) measured the continuous flow records from January to May 2015 at the pond’s outfall. The ReFH rainfall runoff model is calibrated with the observed flow data sets by varying the drainage length parameter (DPLBAR) in the model. Based on the field survey, the fine sediment composes of three classes: $d_{10} = 5 \text{ mm}$ (fine silt), $d_{50} = 12 \text{ mm}$ (fine silt) and $d_{90} = 50 \text{ mm}$ (silt) that were obtained from the manual sampling and equally distributed as an input in the upstream boundary. The fine sediment concentration is estimated based on the regression relationships between flow, turbidity and suspended sediment concentration from the analogue catchment (Ahilan et al., 2016). In order to assess the relative impact of the pond on the hydrologic and morphologic responses during high flow events, two Digital Elevation Model (DEM) data sets were incorporated in the model setup. The current DEM represents existing topography (‘with’) pond condition and the DEM corresponding to the year 2000 represents the predevelopment stage (‘without’) pond scenario in the hydro-morphodynamic model. Table 4 lists the key information about this case study.

3.3. Model validation with sampling data

Allen et al. (2015) surveyed the cumulative sediment deposition at monthly intervals at six locations in the pond during the monitoring period, which is used to validate the morphodynamic model in simulating sediment deposition in the pond. Flow events between 23/04/2015 and 26/05/2015 (as shown in Fig. 10) were modelled because there are a number of high flow events over the period apart from low base flows. Fig. 10 shows the simulated sediment deposition in the pond and the location of the six monitoring points. It indicates that the main deposition area is located at the outfall area. This is because the flow velocity sharply decreases after the water flows to the pond from upstream pipe, this leads to bed shear stress be so small that sediment particles settle down to the bed. Resuspension during high flows causes slight sedimentation in the far area from the outfall. Table 5 shows the measured and simulated depths at the six monitoring points. It is indicated that the model predicts the sedimentation in the stormwater pond generally well despite the fact that there are
clear discrepancies at some points. These differences are expected because of the uncertainty factors in reality. The main uncertainty factors include: (1) the stormwater pond is covered by a variety of soft vegetation which causes clear implication on flow dynamics and sediment transport, however, this is difficult to quantify and predict; (2) the inflow discharge and sediment concentration are quantified based on a conceptual rainfall-runoff model and regression relationship between flow and turbidity, thus this brings about uncertainties in model inputs; (3) sediment particles are very fine, and the sedimentation depth is small, the field monitoring quantifies sediment weights rather depths which might cause some errors to quantify its real depth. Despite of the discrepancies, it can be seen that both simulated and measured shows a higher deposition near the outfall location and a smaller sedimentation at the far-point from the outfall. Therefore, considering the main objective of this study in developing better understanding of fine suspended load transport, the model results are deemed to be adequate.

3.4. Fine-grained sediment tracking during single events

The validated model is used in the hydro-morphological simulations during single events (5-year flow, 30-year flow, and 100-year flow). Fig. 11 shows the water depths, suspended load concentration, and bed shear stress and velocity field during the flow peak for each scenario, as well as the resultant sediment deposition in the stormwater pond after each event. In the viewpoint of hydrodynamic effects, it is clear that the pond has the capability to store the 5-year flow, and the sediment particles in the flow bodies are mostly trapped in the stormwater pond (Fig. 11b) and gradually settle down in the stormwater pond because of the slow flow velocity and the low bed shear stress. However, during the 30-year and 100-year flow events (Fig. 11f and j), a considerable amount of water flows from the pond into the river, which transports fine sediments downstream. As shown in Fig. 11f and j, although the waters in the pond still have relative higher suspended load, sediment particles are flushed out to the river with the increasing inflow. This leads to deposition not only inside the pond, but also in the river downstream (Fig. 11g and l). Table 6 quantifies the input sediments and the deposited sediments for the three scenarios. It shows that the increasing of inflow magnitude results in a decrease in sediment trapping efficiency of the pond as expected.

Before building the stormwater pond, the urban flows were directly drained into the river. The simulated results in Fig. 12 clearly shows that the direct drainage to the watercourse leads to much wider inundation and sedimentation during flooding in comparison with that with the ‘pond’ in Fig. 12. Consequently, sediment particles are deposited in the inundated areas after flood recession, as demonstrated in Fig. 12f and j. Even for the more frequent 5-year flow event, the direct drainage causes considerable amount of sedimentation in the river channel. If there is any, the contaminants attached with sediment particles will potentially influence the water quality in the receiving water. Therefore, the simulations imply that the stormwater pond has the benefits of retaining urban flows and trapping sediment particles generated from upstream urban catchment. The model is capable of quantitatively simulating and qualitatively assessing the performance of a stormwater pond in managing urban floods.

3.5. Fine sediment dynamics varying with flows

As indicated in Table 4, an extreme event in year, 2012, was simulated by the validated model in order to numerically investigate the fine sediment response to an extreme flood event.

Table 4
The data and key parameters used in the study.

<table>
<thead>
<tr>
<th>Data</th>
<th>Description</th>
<th>Purpose</th>
</tr>
</thead>
<tbody>
<tr>
<td>DEMs</td>
<td>developed bed with pond: 1 m × 1 m</td>
<td>Model input</td>
</tr>
<tr>
<td>Sediment concentration</td>
<td>it is estimated based on the regression relationships between flow, turbidity and suspended load concentration from the analogue catchment (Ahilan et al., 2016)</td>
<td>Model validation</td>
</tr>
<tr>
<td>Recorded inflow</td>
<td>23/04/2015–26/05/2015</td>
<td>Analysis of dynamics of flow and fine suspended sediment</td>
</tr>
<tr>
<td>Scenario-based hydrograph</td>
<td>5-year flow (non-flooding)30-year flow (designed flow)100-year flow (flooding)</td>
<td></td>
</tr>
<tr>
<td>2012 extreme inflow</td>
<td>modelled hydrograph based on the measured rainfall with 15 min interval at the Jesmond</td>
<td></td>
</tr>
<tr>
<td>Sediment composition</td>
<td>d10 = 5 μm (fine silt) d50 = 12 μm (silt) d90 = 50 μm (silt)</td>
<td></td>
</tr>
<tr>
<td>Sediment density</td>
<td>1800 kg/m³</td>
<td></td>
</tr>
<tr>
<td>Manning’s roughness coefficient</td>
<td>n = 0.038 s/[m1/3]</td>
<td></td>
</tr>
<tr>
<td>Mesh size/number</td>
<td>1 m × 1 m/230 × 140 cells</td>
<td></td>
</tr>
</tbody>
</table>

Table 5
Measured and simulated deposition depth at the 6 monitoring points.

<table>
<thead>
<tr>
<th></th>
<th>Measured (mm)</th>
<th>Simulated (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>10</td>
<td>17.8</td>
</tr>
<tr>
<td>2</td>
<td>8.3</td>
<td>19.9</td>
</tr>
<tr>
<td>3</td>
<td>8.7</td>
<td>7.6</td>
</tr>
<tr>
<td>4</td>
<td>3.7</td>
<td>7.4</td>
</tr>
<tr>
<td>5</td>
<td>3.8</td>
<td>8.4</td>
</tr>
<tr>
<td>6</td>
<td>0.1</td>
<td>1.6</td>
</tr>
</tbody>
</table>
Fig. 13 plots the inflow at the pond inlet and the cumulative sediment deposition over the whole period in the study domain. Clearly, we can see a non-linear relationship between inflow discharge and cumulative deposition which demonstrates two distinctively different response modes: (1) steadily rising (e.g. zone 1 in Fig. 13a), and (2) sharply dropping (zone 2 in Fig. 13a). To look at the trend of change in deposition volume and the inflow discharge in Fig. 13b, we found that a high inflow leads to a sharp increase in deposition, and consistent low flows increase the sedimentation, but with a lower rate. However, the extreme flows in Fig. 13b reduce the deposition volume sharply, and the higher the inflow, the more significant the reduction is.

Fig. 14 further demonstrates the changes of pond sedimentation due to the three selected representative events in the year 2012 (Event 1, 2, and 3 in Fig. 13). It is found that a considerable amount of sediment is trapped during Event 1, whilst the extreme Events 2 and 3 re-suspend the deposited sediment and transport them to the downstream, particularly in the area facing the pipe outlet. The behaviour is similar to the laboratory event reported in Section 3.1.3. At the pipe outlet bed shear stress is sufficiently high to cause re-suspension of sediments. The two different response

<table>
<thead>
<tr>
<th>Event</th>
<th>5-year</th>
<th>30-year</th>
<th>100-year</th>
</tr>
</thead>
<tbody>
<tr>
<td>input (m³)</td>
<td>7.35</td>
<td>16.71</td>
<td>28.41</td>
</tr>
<tr>
<td>deposition (m³)</td>
<td>4.58</td>
<td>7.29</td>
<td>7.50</td>
</tr>
<tr>
<td>percentage (%)</td>
<td>62.0</td>
<td>43.6</td>
<td>26.4</td>
</tr>
</tbody>
</table>

Table 6
Sediment mass balance for different flood event.
modes observed during varying flow conditions raise a hypothesis, that is: sediment deposition in the pond increases with the inflow discharge, but after a critical value where there is a balance between erosion and deposition, the bed will be eroded due to the high bed shear stress, and the erosion rate is proportional to the inflow magnitude.

Fig. 12. Simulated water depths (a, d, g), bed shear stress and velocity field during peak flow (b, e, h), and sedimentation (c, f, i) for the 5-year, 30-year and 100-year flow events for the ‘without’ pond scenarios.
To verify the hypothesis raised above, we picked out 24 different flow events with a flow peak varying from 0.2 m$^3$/s to 10 m$^3$/s from the extreme year 2012, and quantified the deposition volume before and after each event. Fig. 15 plots the scatter points between the change in deposition volume and flow peak for each event, and the trendlines among the points. It can be seen that two trendlines are derived as postulated, and both have a good determination coefficient, $R^2$, that is larger than 0.8. The deposition volume has a linear relation with a high determination coefficient (0.8775) with the flow discharge. The linear relationship of erosion volume and flow discharge is also significant, but there is a clear large difference during extreme high flows (see Fig. 15). These two events with significant difference are event 2 and event 3 in Fig. 14. With a similar high flow, event 2 has more severe erosion than event 3. This is because there is significant deposition in the pond before event 2 occurs, which allows more sediment to be re-suspended during the extreme flow of event 2. However, event 3 occurs about 110 h after event 2, the deposited sediment available for re-suspension is clearly much less than the pre-event 2 volume. Therefore, this leads to a significant bias for the two events with similar high flow discharge. We found that there is a critical value defined as ‘balance point’ of the flow peak, and the value is approximately in a range of 1.79–1.96 m$^3$/s for the studied stormwater pond. In other words, sediment deposition in the stormwater pond increases with the inflow, and the rate is proportional to the flow peak when the flow peak is below the balance point; however, for the flow with a peak above the balance point, fine sediment particles will be re-suspended and transported downstream, and the re-suspension rate is proportional to the flow peak. Clearly, this balance point is a transition value causing bed deposition or erosion in the pond. This point provides a valuable indicator for stormwater ponds design and maintenance. Removing sediment from stormwater ponds is needed periodically to maintain proper function and restore capacity to prevent localised flooding. Traditionally, machinery dredging is one option during dry conditions (United States Environmental Protection Agency, 2009). However, the understanding of ponds’ balance point can suggest a natural hydraulic regulation method, so saving maintenance cost, and sediments transporting to downstream can also improve the river habitat. Similar hydraulic regulation method has been used for sustainable sediment management in reservoirs (Kondolf, et al., 2014). It should be mentioned that the actual changes in sedimentation volume are also related to inflow volume in addition to flow peak, because a larger flow volume means more fine sediments discharging into the pond. Nonetheless, the flow peak is the deterministic factor causing fine sediments either to be deposited in the pond or to be flushed out of the pond.

4. Conclusions

The study has developed a numerical model to track the hydro-morphological processes dominated by fine-grained suspended sediment, including the prediction of sediment concentration in flow bodies, and erosion and deposition caused by sediment transport. The model has been validated with three laboratory-scale test cases where suspended load plays a dominant role. The results show that the model is capable of reproducing the flow dynamics and the resultant morphological changes reasonably well. Applications in real-world events are performed to further develop the process-based understanding of fine sediment activities in a stormwater pond during varying flow conditions. Findings drawn from this study include: (1) a stormwater pond can be used to attenuate flow peak and trap fine sediment particles, and the effect is more significant for flow events with a smaller flow peak; (2) a
balance point for the inflow peaks determines whether fine sediments settled down or are re-suspended, and the value is determined in a range of 1.79–1.96 m³/s for the studied pond; (3) the consistent low flows lead to gradual accumulation of sediment particles in the pond, and each rainfall-induced flow event results in a sharp rising in the deposition volume below the balance point, but
above the value, the high flow event will flush away the sedimentation in the pond; and (4) the model is capable of quantitatively simulating and qualitatively assessing the performance of a stormwater pond in managing urban water quantity and quality.

Acknowledgements

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