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# Undrained Soil Behavior under Bidirectional Shear

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## ABSTRACT:

In practice, the soil is subject to more than one shear stress in many cases. For instance, the soil in an embankment is subject to a static shear stress along sloping direction, and the sloping direction is usually different from the direction of an earthquake loading. Therefore, there is a necessity to investigate undrained soil behaviors under shear stresses along multiple directions. This paper employs the first commercially available bidirectional direct simple shear apparatus (VDDCSS) to investigate the soil responses of Leighton Buzzard sand under two directional shear stresses. Sand samples are first subject to a static shear stress under drained conditions along different directions from 0° to 180°, followed by a monotonic or cyclic shear stress along 0° until failure occurs. In static tests, the soil strength is the lowest when the angle between these two shear stresses is near 90°, and the strength is the highest at 0°. In addition, a smaller angle leads to a more brittle response, and a greater angle leads to a more ductile response. In dynamic tests, liquefaction resistance is decreased from the angle of 0° to 90°, and then increased from 90° to 180°.

## INTRODUCTION

In geotechnical testing, traditional simple shear apparatus and torsional shear apparatus have been widely used to study the shear behavior of sand. In these tests, stress conditions are usually different from in-situ conditions, and shear stress can be only added in one direction. A bi-directional simple shear apparatus can better replicate complex in-situ conditions, for example, the soil in an embankment under an earthquake loading. In recent years, a few apparatuses have been developed to apply bi-directional shear loading to soil specimens (Boulanger et al, 1993; DeGroot et al, 1993; Rutherford, 2012). However, a limited number of bidirectional simple shear

apparatuses have been used to investigate the effect of consolidation shear stress ( $\tau_c$ , also called initial static driving shear stress) on undrained shear behavior (Boulanger et al, 1993; DeGroot et al, 1993; Biscontin, 2001; Kammerer, 2002; Rutherford, 2012). The consolidation shear stress duplicates the stress state of the soil under a slope or foundation, and its magnitude depends on the inclination of a slope or structure weight, respectively. Static undrained shear stress represents horizontal forces like ice loading on an offshore arctic gravity structure, and cyclic undrained shear stress represents seismic loading like transverse earthquake motions.

DeGroot et al (1996), Biscontin (2001) and Rutherford (2012) have studied the effect of consolidation shear stress on clay in monotonic simple shear tests. In these monotonic tests, testing specimens are first sheared under drained condition along different directions, and then sheared under drained condition along a fixed direction. Results in these studies show that a smaller angle between consolidation shear stress and undrained shear stress leads to a higher strength and more brittle response, and a greater angle results in a lower strength and more ductile response. The lowest strength occurs in tests with angles around  $90^\circ$ . However, in these static loading tests, the soil studied is mainly clay.

Boulanger and Seed (1995) and Kammerer (2002) have researched on the effect of consolidation shear stress on sand in cyclic simple shear tests. In the cyclic tests, consolidation shear stresses parallel or perpendicular to cyclic direction with different magnitudes are applied on sand specimens during consolidation, followed by cyclic shear stresses. Results in these studies show that when the two stresses are parallel, liquefaction resistance usually increases with increasing consolidation shear stress. In perpendicular tests, the liquefaction resistance is decreased with the increasing consolidation shear stress.

The aim of this study is to more comprehensively investigate sand behavior in multidirectional simple shear tests. Leighton Buzzard sand Fraction B is tested, with consolidation shear stresses in different directions. More directions of consolidation shear stress, vary from  $0^\circ$  to  $180^\circ$  with an interval of  $30^\circ$ , are tested in both static and cyclic simple shear test.

## **THE BI-DIRECTIONAL SIMPLE SHEAR TESTS**

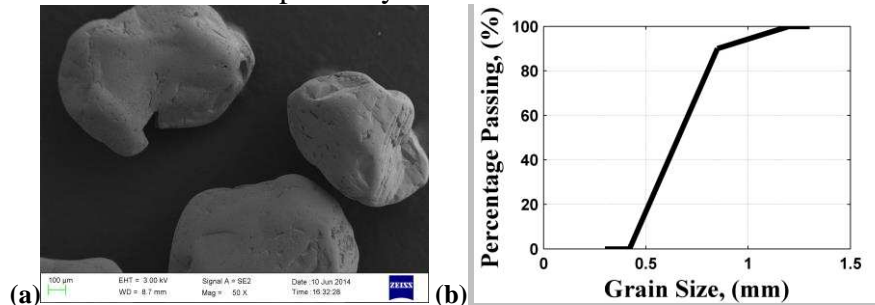
### **Testing Facility**

Variable Direction Dynamic Cyclic Simple Shear (VDDCSS) is used in this study. It is the first commercially available bidirectional direct simple shear apparatus, manufactured by GDS (Global Digital Systems) Instruments Ltd. UK. Two orthogonal shear stresses can be applied independently on a soil specimen. The secondary shear actuator that acts at  $90^\circ$  degrees to the primary shear actuator enables the VDDCSS to perform simple shear tests in any horizontal direction.

In this study, the cylindrical specimen has a diameter of 70 mm and height of 17 mm. A stack of low-friction Teflon coated rings with 1 mm high each is placed outside membrane of the specimen. Undrained loading tests are performed under constant volume condition. The change of vertical stress in a dry specimen is assumed equivalent to the excess pore water pressure generated when a saturated specimen is tested under true undrained condition (Finn, 1985; Dyvik et al, 1987).

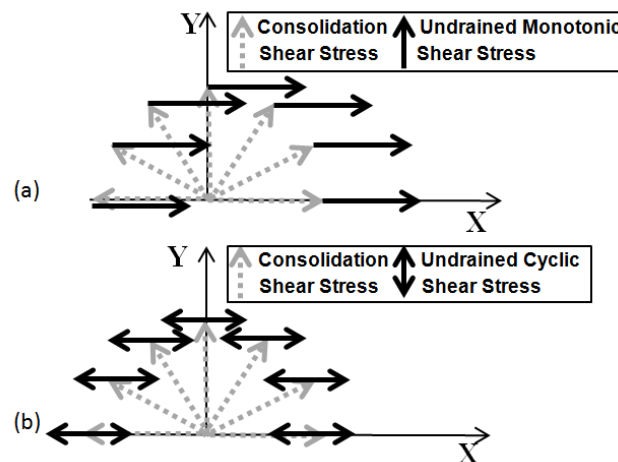
## Testing Material and Procedure

Leighton Buzzard sand (Fraction B) is tested in this study. It has sub-rounded particles and contains mainly quartz with some carbonate material. The Scanning electron micrograph of Leighton Buzzard sand (Fraction B) is shown in Figure 1 (a). The grading curve of the soil is shown in Figure 1 (b). Its maximum and minimum void ratios are 0.79 and 0.52 respectively.



**FIG. 1. (a) Scanning electron micrograph (b) Grading curve of Leighton Buzzard sand (Fraction B)**

Sand specimens are prepared by dry funnel method described by Ishihara (1993). Sand specimens are anisotropically consolidated under a vertical normal stress ( $\sigma'_{vc}$ ) of 200 kPa and a consolidation shear stress ( $\tau_{hc}$ ), and then sheared in undrained condition by adding a secondary shear stress acting along a different direction with the first consolidation shear stress. The relative density ( $D_r$ ) after consolidation is controlled approximately at 75%. The tested stress paths in monotonic and cyclic tests are described in Figure 2 (a) and (b), respectively. The direction of consolidation shear stresses varies from  $0^\circ$  to  $180^\circ$  with an interval of  $30^\circ$ . In undrained monotonic tests, sand specimens are sheared monotonically with the shearing speed of 0.01 mm/min. In undrained cyclic tests, a frequency of 0.1 Hz is used to allow for a better data acquisition. For the ease of comparing with monotonic tests, strain control is used in cyclic tests.



**FIG. 2. Stress paths of soil specimens with the consolidation shear stress (a) in**

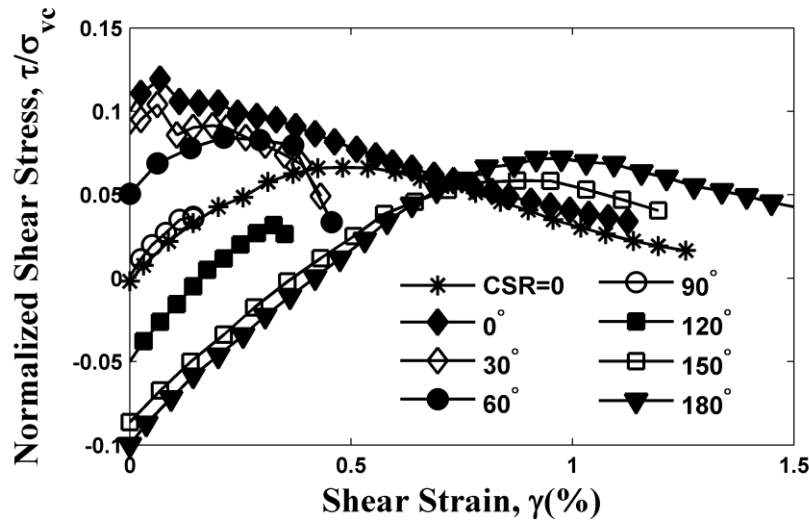
## undrained monotonic shear tests (b) in undrained cyclic shear tests

In test results, the shear stress and shear strain are presented along x direction. All the tests are terminated after the effective vertical stress drops below 10 percent of the initial vertical stress. This is because the existence of shear stress prevents the effective vertical stress from reaching zero (Ishihara and Yamazaki, 1980; Kammerer, 2002).

### TEST RESULTS

#### Monotonic Tests

Tests under the Consolidation Shear Ratio (CSR,  $\frac{\tau_{hc}}{\sigma_{vc}}$ ) of 0.05 and 0.1 are conducted with various angles of consolidation shear stresses, as shown in Figure 2 (a). A test without the consolidation shear stress is also included for comparison. Figure 3 shows the responses of shear stress for different angles of the consolidation shear stress at the CSR of 0.1. Tests with smaller angles reach the peak shear stress at an earlier stage of shearing, and show more brittle responses. Tests with angles around  $90^\circ$  fail at the initial stage of shearing, and these samples fail in the y direction with rapid shear strain development.



**FIG. 3. Responses of shear stress for different angles of the consolidation shear stress**

Figure 4 shows the shear strength of tests with different magnitudes and directions of consolidation shear stress. In the tests with the same CSR, the shear strength decreases from  $0^\circ$  to  $90^\circ$ , and then increases from  $90^\circ$  to  $180^\circ$ . Increasing CSR increases the effect of angles, and the trend is similar to previous results on clay (DeGroot et al, 1993; Biscontin, 2001; and Rutherford, 2012). In the tests with the CSR of 0.05, the shear strengths are increased in all directions compared with the test without the consolidation shear stress. This is due to the dominant effect of densification during adding the consolidation shear stress. On the other hand, in the

tests with the CSR of 0.1, the effect of angles dominates the shear responses over the effect of densification.

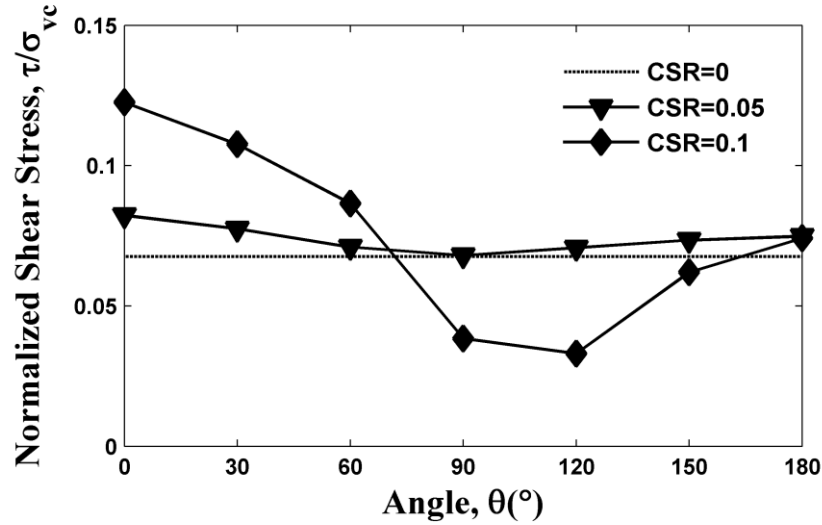


FIG. 4. The shear strength for tests with different magnitudes and directions of consolidation shear stress

### Cyclic Tests

In the cyclic tests, three series of tests are conducted using different amplitudes of cyclic shear displacement, which are 0.025mm 0.03mm and 0.04mm. Figure 5 shows a typical stress path of monotonic and cyclic tests under the CSR of 0.05 with the amplitude of 0.04mm. Tests with the amplitudes of 0.025mm and 0.03mm have a similar trend. It can be seen that the cyclic stress path is below that in monotonic test. Andersen (2009) reported a similar result and attributed it to the breakdown of soil structure in cyclic loading, which causes a tendency for volumetric reduction in the soil and drop of vertical stress.

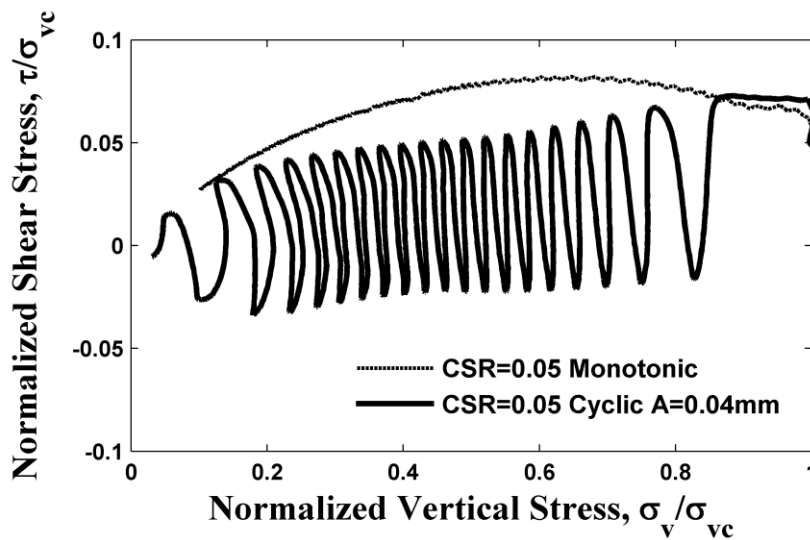


FIG. 5 Stress paths of monotonic and cyclic tests ( $0^\circ$ ) under the CSR of 0.05.

Figure 6 shows the pore water generation during shear at the amplitude of 0.04mm. Tests with the amplitudes of 0.025mm and 0.03mm have a similar trend. PWP increases the slowest in the test without the consolidation shear stress, followed by the 0° and 180° tests. In the 90° test, PWP increases the fastest, and fails in the least cyclic number. It should be noted that all the tests except the 0° test and 180° test fail in the direction perpendicular to the cyclic shear displacement.

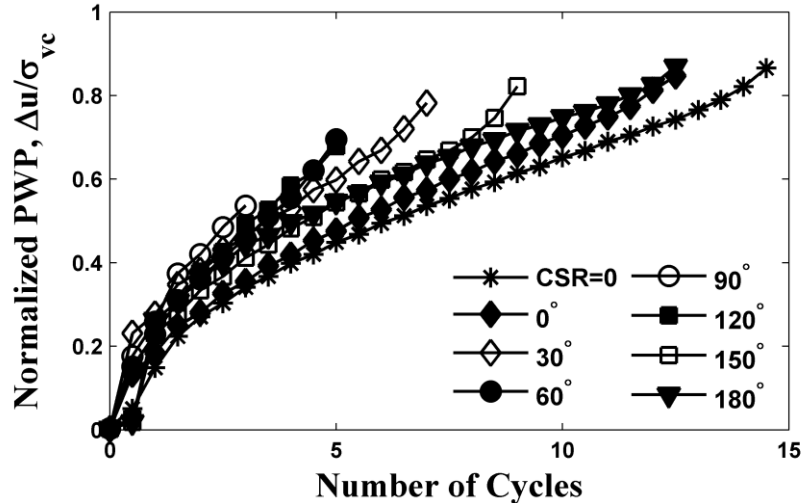


FIG. 6. Responses of pore water generation for different angles of the consolidation shear stress in cyclic tests with the amplitude of 0.04mm

Figure 7 shows the number of cycles at failure for all the shear amplitudes with and without the consolidation shear stress. It indicates that under the same shear amplitude, the number of cycles is greater without the consolidation shear stress than that with the consolidation shear stress, and correspondingly a larger liquefaction resistance. Under the consolidation shear stress, the number of the cycle is the greatest at 0°, and gradually decreases with increasing angle until 90°. The number of cycles increases again from 90° to 180°. In all the shear amplitudes, the liquefaction resistance is the smallest at 90°.

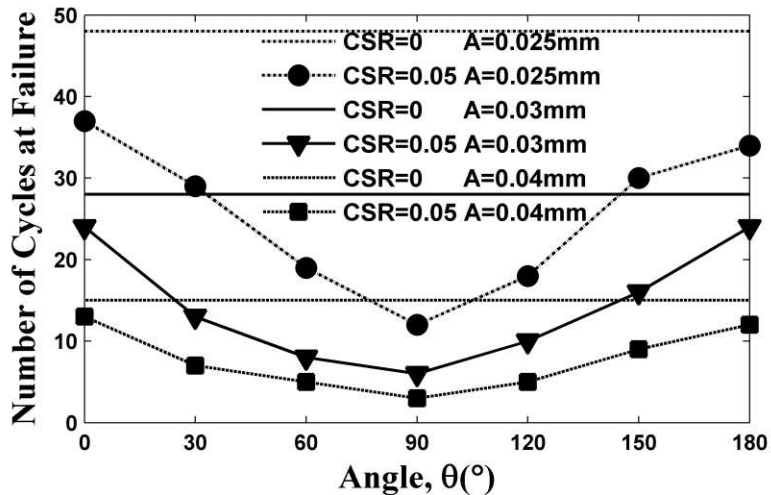


FIG. 7. Number of cycles at failure for tests with different amplitude of cyclic

## shears displacement

### CONCLUSIONS

This paper investigates the impact of the consolidation shear stress on the following undrained shear strengths of sand under monotonic and cyclic loading by using the VCCDSS. The study indicates that the deviation between the consolidation shear and undrained shear has a significant effect on the undrained responses. In the monotonic loading tests, the consolidation shear stress at  $0^{\circ}$  increases the following undrained shear strength compared with that without the consolidation shear stress. But the response is more brittle in the former than in the latter. The shear strength decreases from  $0^{\circ}$  to  $90^{\circ}$ , and then increases from  $90^{\circ}$  to  $180^{\circ}$ . The impact of angle is greater at a higher consolidation shear stress. In addition, a larger angle leads to more ductile response. In the cyclic loading tests, the number of cycles at failure is also significantly affected by the deviation between the consolidation shear stress and undrained shear stress. Similar to the trend in the monotonic loading tests, under the same cyclic shear stress, the number of cycles at failure decreases from the  $0^{\circ}$  test to the  $90^{\circ}$  test, and then increases from the  $90^{\circ}$  test to the  $180^{\circ}$  test. However, the consolidation shear stress decreases the number of cycles at failure compared with that in the tests without the consolidation shear stress.

### ACKNOWLEDGMENTS

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