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**Proceedings Paper:**
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Fault-tolerant Learning in Spiking Astrocyte-Neural Networks on FPGAs

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Abstract—The paper presents a neuromorphic system implemented on a Field Programmable Gate Array (FPGA) device establishing fault tolerance using a learning method, which is a combination of the Spike-Timing-Dependent Plasticity (STDP) and Bienenstock, Cooper, and Munro (BCM) learning rules. The rule modulates the synaptic plasticity level by shifting the plasticity window, associated with STDP, up/down the vertical axis as a function of postsynaptic neural activity. Specifically when neurons are inactive, either early on in the normal learning phase or when a fault occurs, the window is shifted up the vertical axis (open), leading to an increase in firing rate of the postsynaptic neuron. As learning progresses, the plasticity window moves down the vertical axis until the desired postsynaptic neuron firing rate is established. Experimental results are presented to show the effectiveness of proposed approach in establishing fault tolerance. The system can maintain the network performance with at least one nonfaulty synapse. Finally, we discuss a robotic application utilizing the proposed architecture.

Keywords—Neuromorphic Computing, Fault Tolerance, Self-Repair, Spiking Neural Network, Astrocyte, Field Programmable Gate Array, Bio-inspired Engineering.

I. INTRODUCTION

Neuromorphic computation is an emerging research domain, which derives inspiration from the architecture of nervous systems of living beings to solve complex tasks. Spiking neurons are core components of many computational models of the brain that aim to improve understanding of brain function. Although neuromorphic systems based on Very Large Scale Integration (VLSI) architecture were introduced in the late 1980s [1], use of FPGAs in the design of spiking neuromorphic architectures started to be used over the last ten years [2]. In Spiking Neural Networks (SNNs), communication and computation happen by an exchange of spatiotemporal patterns encoded as spikes as in biological neurons. Astrocytes have been shown to coexist with neurons [3] where these cells communicate with synapses and neurons, thereby regulating synaptic activity [4]. The astrocyte cells together with spiking neurons form a Spiking Astrocyte-Neural Network (SANN) with a distributed and fine-grained self-repair capability.

Neural activity levels in the nervous system rely on various plasticity mechanisms, environmental variations and developmental changes. Synaptic plasticity is a mechanism used by neurons to counteract excessive excitation or inhibition by adjusting synaptic strengths [5], [6]. In this work, we propose such a synaptic plasticity mechanism in hardware where the activity of a post synaptic neuron is used to modify synaptic weights to overcome faults in the system through learning mechanisms.

Hebbian learning is a synaptic plasticity rule where a synapse between two neurons is strengthened when its pre and post synaptic neurons have highly correlated outputs. Spike Timing Dependent Plasticity (STDP) is an asymmetric form of Hebbian learning induced by tight temporal correlations between the presynaptic and postsynaptic neuron spikes [7], [8]. The Bienenstock, Cooper, and Munro (BCM) synaptic modification rule modulates the postsynaptic activity if it deviates from the required response [9], [10]. In this paper, we use a self-repairing learning rule [11] that uses evidence [12] to explain how the STDP and BCM learning rules co-exist to give a learning function that is under the control of postsynaptic neuron activity.

When faults occur in the pathways between neurons the postsynaptic neurons can fall silent. Silent/near silent neuron presents a weak node in the system. This issue might be due to hardware failures in the system. The proposed work is a solution for faults leading to failures in the interconnections between the neurons. These may be sensor failures, SEUs, stuck-at fault, interconnect fracture, noise, etc. We define repair as the ability of the system to restore firing rates through synaptic weight modulations regulated by learning rules.

To summarize, this paper consists of the following contributions: Firstly, we propose a novel learning rule utilizing STDP and BCM rules, implemented on an FPGA. Secondly, an efficient fault tolerance is demonstrated on the proposed architecture, showing repair capability if at least one healthy synapse exists in the system. Finally, we use the strengths of biological SANN systems with their parallel processing and learning capabilities to solve a real world task.

The rest of the paper is organized as follows. Section II describes the biological background of the self-repairing learning rule. Section III presents a hardware implementation of the proposed self-repair learning methodology. In section IV, we analyze the repair capability of the proposed system implemented on an FPGA. Section V presents experimental results establishing the effectiveness of the proposed scheme. Section VI demonstrates an application of the proposed learning mechanism. Finally, conclusions and future work are discussed in Section VII.
II. SELF-REPAIRING LEARNING RULE

The network uses the Leaky Integrate and Fire (LIF) [13] neuron model \((N_1, N_2, N_3\) and \(N_4\) in Figure 1), which is a simplified model of a biological neuron widely used in neuromorphic computing. It represents a good trade-off between computational complexity and biological realism. The representation of a LIF neuron is shown in Equation (1).

\[
\tau_{\text{mem}} \frac{dv}{dt} = -v(t) + R_{\text{mem}} \sum_{i=1}^{m} I_{\text{syn}}^i(t)
\]

where \(\tau_{\text{mem}}, R_{\text{mem}}, v\) and \(I_{\text{syn}}\) are the time constant, membrane resistance, membrane potential and current injected by a synapse respectively. \(m\) represents the total number of synapses connected to the neuron. On reaching the threshold voltage, the membrane potential is brought back and held at 0V following a nominal refractory period (2 clock cycles). The expression is evaluated using the Euler method.

A tripartite synapse is a junction between a presynaptic terminal, a postsynaptic terminal and an astrocyte cell. Let us consider a signaling pathway between these three terminals and a GABA interneuron terminal. We assume that the presynaptic spiking frequency \(f_{\text{pre}}\) is same as that of the GABA neuron. Interneuron-astrocyte signaling dynamically affects excitatory neurotransmission. Astrocytes, by the action of retrograde signaling [12], regulates transmission of spikes between two layers of the network (\(A^*\) in Figure 1). For example, under low \(f_{\text{pre}}\), the interneuron-astrocyte interaction leads to an inhibitory effect representing a low transmission probability (\(PR\)) with the associated neuron. However, at high \(f_{\text{pre}}\), the effect gets reversed leading to a high transmission probability. These outcomes are due to release of inositol 1, 4, 5-trisphosphate (\(IP_3\)), Calcium and Glutamate released within the astrocyte [14]. The above phenomenon controls the spikes arriving at the postsynaptic terminal by regulating the \(PR\) and can be mathematically modeled by Equation (2).

\[
PR = \exp\left(\frac{(f_{\text{pre}} - f_0)^2}{2\sigma^2}\right)
\]

In biological systems, dendrites of a presynaptic neuron make multiple connections with a postsynaptic neuron [15]. The propagation delays between these paths may differ. Hence, in the proposed SANN, each pre-post neural coupling has multiple synaptic pathways (8 in our experiments) where each pathway is assumed to be morphologically modeled by a different delay. This design of multiple pathways permits the postsynaptic potential to build up in a realistic way. Also, more pathways gives greater fault tolerance, but the cost is in implementation overhead.

To implement a self-repairing mechanism for the SANN, a learning algorithm needs to be designed. In this approach, the STDP [7], [8], together with BCM learning rule [9], [10] are combined to develop the BCM-STDP rule. STDP uses the time difference between presynaptic and postsynaptic spikes to adjust the synaptic weights, where the equations in (3) cause long-term potentiation (LTP) for \(\Delta t \leq 0\) and long-term depression (LTD) for \(\Delta t > 0\). In this approach, potiation/depression is described by, Equation (3)

\[
\delta w(\Delta t) = \begin{cases} 
+ A_0 \exp \left(\frac{\Delta t}{\tau_+}\right), & \Delta t \leq 0 \\
- A_0 \exp \left(-\frac{\Delta t}{\tau_-}\right), & \Delta t > 0
\end{cases}
\]

where \(\delta w(\Delta t)\) is the weight update, \(A_0\) is the time varying height of STDP learning window controlling the maximum levels of weight potentiation and depression, \(\tau_+\) and \(\tau_-\) control the decay rate of weight updating. \(\Delta t = (t_{\text{pre}} - t_{\text{post}})\) is the time difference between presynaptic spike time \(t_{\text{pre}}\) and postsynaptic spike time \(t_{\text{post}}\). Symmetrical plasticity window is assumed and \(\tau_+ = \tau_- = 5\) clock cycles. In addition, the BCM learning rule modulates the height of the STDP plasticity window as a function of the firing rate. This is modelled by Equation (4).

\[
A_0 = \frac{A}{1 + \exp\left(a(f - f_0)\right)} - A_{\text{~}}
\]

where \(f\) and \(f_0\) are the actual and target firing rate of the postsynaptic neuron \((N_4\) in Figure 1), respectively. \(A\) is the maximum height of plasticity window and \(A_\text{~}\) is the maximum height of plasticity window for depression. The parameter \(a\) is constant which controls the opening/closing speed of plasticity window and is found experimentally to be 0.1. The BCM rule modulates the synaptic plasticity level by \(A_0\) associated with STDP, as a function of postsynaptic neural activity. Specifically when neurons are inactive, either early on in the normal learning phase or when a fault occurs, the window is shifted up the vertical axis \((A_0\) increases) and as the postsynaptic neuron activity increases, as learning progresses, the plasticity window is moved down the vertical axis \((A_0\) decreases) until learning ceases.

III. HARDWARE IMPLEMENTATION OF SELF-LEARNING RULES

The basic sub-block implemented on the FPGA for detecting a three bit pattern associated with firing rates is shown
in Figure 1. We use a window of size $2^{10}$ clock cycles to determine the spike rate of the post synaptic neuron. Moving average is used to determine the spike frequency. Input spike trains of frequency 54 spikes/window and 64 spikes/window are used to represent the input pattern. Neurons in layer 1 facilitate transmission of spike trains. There are 8 parallel variable delay paths between the presynaptic and postsynaptic neuron. Astrocyte $A^*$ regulates the spikes received by the neuron in layer 2. For example, let us consider a case in which the sub-block presented in Figure 1 is used for detecting a pattern $(54,54,64)$. If pattern $(54,54,64)$ is selected, the neurons in layer 1 produces spikes of frequencies 54, 54 and 64 respectively. Astrocyte monitors the spikes and generates transmission $PR$ depending on the pattern to permit the selected pattern in the neuron $N_4$. Considering a compact hardware implementation, the $PR$ represented in equation 2 consumes more resources and should be approximated. We try to implement equation 2 using a set of piecewise linear equations (8 in our implementation). Due to the astrocyte PR regulation, if the pattern $(54,54,64)$ is received by the input neurons, the spike trains are delivered to the neuron $N_4$. Astrocyte restricts any other patterns of firing rates to be transited to $N_4$ by lowering $PR$ as per equation (2).

The neurons in the system are LIF and have the following parameters. $R_{mem}=1M\Omega$, $V_{th}$ (threshold voltage) = $15mV$, $\tau_{mem}=10ms$ and resting membrane potential $V_r=0$. Euler method of integration evaluates the LIF expression with a fixed time step of $\Delta t=2^{-10}s$ (an approximation for $1ms$). The synapses used in this model are probabilistic in nature. We use a uniformly distributed pseudorandom number generator to produce a random number which is denoted by $rand$. We use a Linear Feedback Shift Register (LFSR) to generate $rand$. If $rand$ is less than or equal to the release $PR$, synapse injects a current to the neuron.

$$I_{syn} = \begin{cases} I_{inj}, & rand \leq PR \\ 0, & rand > PR \end{cases}$$ (5)

Based on the input pattern, neuron $N_4$ learns to achieve the required spike rate (54 spikes/window). Learning is achieved using STDP and BCM rules. As per equation 3 and equation 4, if output frequency deviates from the required output frequency (54 spikes/window for neuron $N_4$), the weights of synapses are updated by a certain amount. Equation 3 is approximated using the following relation.

$$\delta w^*(\Delta t) = \begin{cases} +A_0 2^{\frac{\Delta t}{\tau^*}} , & \Delta t \leq 0 \\ -A_0 2^{\frac{-\Delta t}{\tau^*}} , & \Delta t > 0 \end{cases}$$ (6)

Equation 6 is efficient for hardware implementation as this requires $A_0$ to be shifted by a certain amount controlled by $\Delta t$. Considering a compact hardware implementation, the BCM rule represented in equation 4 consumes more resources and should be approximated. We implement equation 4 using a set of 8 piecewise linear equations (Greater the number of piecewise linear equations higher is the accuracy of approximation). Based on the synaptic weights, a current is generated.

$$I_{inj} = (w + \delta w)^* \cdot \varepsilon$$ (7)

where $w$ is the weight of the synapse at the current time step and $\varepsilon$ is a scaling factor determined empirically. In our implementation $\varepsilon = 2^{-6}$.

![Fig. 2: (A) Firing rate of $N_4$ under fault free condition: All synapses between neurons in layer 1 and layer 2 are fault free enabling 8 parallel delayed paths between each connected neuron. A stable firing rate of 54 spikes/window is established around 0.25ms. (B) Synaptic weights under fault free condition: During the training phase, the synaptic weights (24 plots: 8 synapses $\times$3) increases and achieves a stable value around 0.25ms.](#)

One aspect of our model is that it operates at an accelerated biological time scale similar to that in [16], proving to be an efficient realization of real-world tasks compared to [11].

IV. FAULT ANALYSIS

A. No Faults

Three input spike trains of frequency 54 spikes/window, 54 spikes/window, and 64 spikes/window are used for testing the basic functionality of architecture depicted in Figure 1. These input spike trains are compatible with the center frequency of the associated synapses and hence the astrocyte delivers a high $PR$ for this pattern. The target frequency of neuron $N_4$ is set to be 54 spikes/window. A normal learning phase will occur and the spike rate gradually increases during the training phase and eventually stabilizes at the target frequency of 54 spikes/window in 0.25ms as shown in Figure 2-A. Figure 2-B shows the synaptic weights which, as expected, show a slow rise over the learning period and stabilize at 0.25ms.

Additionally, the system is tested with presynaptic spike train frequencies outside the filter window (patterns other than $(54,54,64)$ spikes/window) (results not shown) showed that no learning occurred, which verified that the proposed network is selective to the input spike train patterns.

B. Partial Faults

To evaluate the self-repairing capability of the proposed SANN, the spike train frequency of both $N_1$, $N_2$, and $N_3$ was set to the center frequency of the Gaussian $PR$ curve $(54,54,64)$ spikes/window respectively and the SANN was trained with a target frequency for $N_4$ of 54 spikes/window. Next, the system is subjected to faults gradually after every 100ms (Figure 3). For example, at 100ms, one of the path between $N_1$ and $N_4$ is broken, we can see an activity drop here in Figure 3-A, which subsequently causes the learning window to re-open and the training process restarts. Likewise, we gradually increase the
Fig. 3: (A) **Firing rate of \( N_4 \) under different faulty conditions**: Synapses between neurons in layer 1 and layer 2 are induced faults gradually (1-7 under neuron \( N_1 \) specifies the point in which each synapses between \( N_1 \) and \( N_4 \) is broken). A stable firing rate of \( 54 \text{spikes/window} \) is established in all faulty cases. (B) **Synaptic weights between \( N_1 \) and \( N_4 \) under faults of different percentage**: We induce gradual faults on the system after every 100\( \text{ms} \). Only one synapse of \( N_1 \) is left unbroken after 700\( \text{ms} \). (C) **Synaptic weights between \( N_2 \) and \( N_4 \) under faults of different percentage**: We induce gradual faults on the system after 700\( \text{ms} \). The only synapse of \( N_2 \) is left unbroken after 1400\( \text{ms} \). (D) **Synaptic weights between \( N_3 \) and \( N_4 \) under faults of different percentage**: We induce gradual faults on the system after 1400\( \text{ms} \). Only synapse of \( N_2 \) is left unbroken after 2100\( \text{ms} \). We can see that for each fault percentages, the systems learn and modulates the synaptic weights for establishing a constant firing rate similar to the fault-free results. The broken synapses do not increase the weight it just retains the weight.

Faults in synapses between \( N_1 \) and \( N_4 \) leaving at least one (No repair happens if all paths between \( N_1 \) and \( N_4 \) break). At 700\( \text{ms} \), 7 synapses between \( N_1 \) and \( N_4 \) are broken. Then we induced faults in synapses between \( N_2 \) and \( N_4 \). At 1400\( \text{ms} \), 7 synapses between \( N_2 \) and \( N_4 \) are broken and at 2100\( \text{ms} \), 7 synapses between \( N_3 \) and \( N_4 \) are broken. Hence weights of nonfaulty synapses increase to compensate for synaptic input to \( N_4 \). This process of re-training the network to recover the firing rate of \( N_4 \) defines the self-repairing process. The modulated weights of synapses associated with \( N_1, N_2, N_3 \) are shown in Figure 3-B, C and D respectively. It is evident from Figure 3-A that the fault repair happens at a rate of \( \text{ms} \), proving...
to be a very efficient scheme for real world applications. This is a very important capability for the fault-tolerant hardware systems due to the distributed, fine-grained repair capability which will yield a significantly enhanced performance over conventional approaches [17], [18]. This enhancement is also due to ability of the system to run at an accelerated time scale.

V. Hardware Results

The proposed architecture is implemented on a Xilinx Virtex-7 FPGA board. The firing rates of the output layer neurons are monitored using the Xilinx ChipScope Pro analyzer. Power estimation of the circuits was carried out using Xilinx XPower Analyzer and timing analysis using Xilinx Timing Analyzer. Table I reports the hardware resource footprint of the proposed models. Total on-chip power dissipation of the system is 0.535W. As evident from these reports, the proposed architecture of neural self-learning can be implemented on the FPGA with minimal hardware overhead and power consumption. But, on considering large network architectures and applications, the proposed implementation should be improved in terms of hardware especially in the amount of DSP consumption. In our implementation, we have 8 equations for realizing PR/synapse and 8 equations for realizing $A_o$. Each equation consumes 2 DSPs, proving to be a constrain for larger SANNs. We are considering alternative approximation techniques to overcome this issue. The results presented in Figure 2 and Figure 3 corresponds to the system operating at a frequency of 10MHz. The maximum operating frequency observed for the complete system is 60MHz. Hence fault recovery can happen 6 times faster than the reported figures.

VI. Application

The main aim of the proposed work is to implement fault tolerant SANN in FPGA. Once this is established successfully, we apply the concept to a real-world task. There are some works which demonstrate the application of FPGA-based neural networks in solving real world tasks [19]–[21]. Compared to these works, the proposed system has enhanced fault-tolerance and learning capabilities. The emphasis of the selected application is on the fault recovery while establishing the task of robot navigation towards the direction of a colored target (say red). The task implemented by the proposed architecture can be explained in association with Table II. The image of the red target is sensed in forward, right and left direction. Based on the direction of the red target either in forward, right or left direction, the FPGA input pins reflect a value of logic 1 in $F_c$, $R_c$ or $L_c$ respectively. The system receives information on the presence of an obstacle and is presented a logic 1 in $F_o$, $R_o$ or $L_o$ on pins of the FPGA in the forward, right or left directions respectively. $D$ represents the final direction of robot movement. In our experiment forward direction has the highest priority and the reverse direction has the lowest priority (Forward > Right > Left > Reverse). To analyze this let us consider the first case reported in Table II. Here $F_c$ and $F_o$ have a logic 0, since there is no obstacle in the forward direction spikes are delivered in the forward neuron establishing movement in the forward direction. In the second case $F_c$, $F_o=(1, 0)$ detects the presence of the colored target in the forward direction, hence robot navigates to forward direction. In the third case, we have $F_c$, $F_o=(1)$, detecting the red target and the obstacle. We assume that the red target is treated as the obstacle and hence the robot navigates towards the red target by having spikes in forward direction. Case $F_c$, $F_o=(0, 1)$ depicts an obstacle in the forward direction which is not the red target, hence priority goes to the right direction. Similar interpretation holds for the right, left, and reverse directions.

Figure 4 represents the complete system required for navigation considering the specification in Table II. The SANN consists of three layers. The input layer, the hidden layer, and an output layer. The system consists of 6 neurons in the input layer, each detecting either the presence of a red target or an obstacle. These neurons are connected to the hidden layer neuron using 8 variable delay synapses. An astrocyte provides required $PR$ tuning for each pattern and enables the encoded pattern to be passed to the hidden layer neuron. For example, there are 10 patterns to be distinguished by the hidden layer and hence there are 10 astrocytes (not shown in the figure) and 10 hidden layer neurons for detecting these patterns. If there is a spike in the forward direction, this disables spike generation in right, left and reverse direction. The output layer neuron combines the hidden layer neurons responsible for each direction. Since we consider 4 directions, we have 4 motor neurons in the output layer.

VII. Conclusion

In this paper, we discussed three contributions. Firstly, we built a fault tolerant neuromorphic architecture for SANNs. Based on this self-repairing mechanism, when faults occur and the synaptic connection is broken, the network still retains the capability to reorganize itself by re-training and consequently recover to the pre-fault mapping. Secondly, we discussed an approximate model of the system for FPGA-based implementations. The work presented represents an initial step towards a new form of fault tolerant designs, with low overhead and

<p>| TABLE I: Hardware Overhead for the basic unit (Figure 1) implemented on the FPGA |
|---------------------------------|----------------|----------------|----------------|----------------|</p>
<table>
<thead>
<tr>
<th>Methodology/Components</th>
<th>Slice</th>
<th>Slice Reg</th>
<th>LUT</th>
<th>BRAM</th>
</tr>
</thead>
<tbody>
<tr>
<td>8 delayed paths per input</td>
<td>3153</td>
<td>3407</td>
<td>9108</td>
<td>128</td>
</tr>
<tr>
<td>$A_o$ Generator</td>
<td>140</td>
<td>32</td>
<td>470</td>
<td>0</td>
</tr>
<tr>
<td>Moving Average</td>
<td>16</td>
<td>32</td>
<td>42</td>
<td>2</td>
</tr>
<tr>
<td>LIF Neuron</td>
<td>7</td>
<td>36</td>
<td>15</td>
<td>0</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>TABLE II: Mapping of input sensor reading to output spikes</th>
</tr>
</thead>
<tbody>
<tr>
<td>$F_c$, $F_o$, $R_c$, $R_o$, $L_c$, $L_o$, $D$</td>
</tr>
<tr>
<td>---------------------------------------------</td>
</tr>
<tr>
<td>0, 0, 0, x, x, x</td>
</tr>
<tr>
<td>1, 0, x, x, x, x</td>
</tr>
<tr>
<td>1, 1, x, x, x, x</td>
</tr>
<tr>
<td>0, 0, 1, 0, x</td>
</tr>
<tr>
<td>1, 0, 1, 0, x</td>
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<tr>
<td>1, 0, 0, 1, 0, 0, 0</td>
</tr>
<tr>
<td>0, 1, 0, 1, 1, 1</td>
</tr>
<tr>
<td>0, 0, 1, 0, 1</td>
</tr>
</tbody>
</table>
| $F_c$, $F_o=(1, 0)$ represents presence of the selected coloured target in the robot’s forward direction. $F_c$, $F_o=(0, 1)$ detects the presence of the colored target in the forward direction, hence robot navigates to forward direction. $F_c$, $F_o=(1)$, detecting the red target and the obstacle. $F_c$, $F_o=(0, 1)$ depicts an obstacle in the forward direction which is not the red target, hence priority goes to the right direction.
high performance. We are working further towards a more compact architecture based on the proposed methodology for large scale implementations of SANNs. Finally, the proposed idea is applied to a robotic application. The proposed architecture is appropriate for FPGA-based applications running in environments that induce faults in systems, where reliability is crucial.

VIII. ACKNOWLEDGEMENTS

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REFERENCES