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# An extensible framework for multicore response time analysis

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**Abstract** In this paper, we introduce a *multicore response time analysis (MRTA) framework*, which decouples response time analysis from a reliance on context-independent WCET values. Instead, the analysis formulates response times directly

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This paper extends initial research on “A *Generic and Compositional Framework for Multicore Response Time Analysis*” presented at RTNS 2015 (Altmeyer et al. 2015).

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The additional material includes: Section 4: analysis for warmed-up caches and dynamic scratchpads (Sects. 4.3 and 4.2). Section 7: extensions to the task model, including RTOS and interrupts, shared software resources, and open systems and incremental verification. Section 8: presentation of a cycle-accurate multicore simulator. Section 9: evaluation of different local memory types (Sect. 9.2), a comparison between predictable and reference architectures (Sect. 9.3), and a verification of the precision of the analysis using results from the simulator (Sect. 9.4).

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from the demands placed on different hardware resources. The MRTA framework is extensible to different multicore architectures, with a variety of arbitration policies for the common interconnects, and different types and arrangements of local memory. We instantiate the framework for single level local data and instruction memories (cache or scratchpads), for a variety of memory bus arbitration policies, including: Round-Robin, FIFO, Fixed-Priority, Processor-Priority, and TDMA, and account for DRAM refreshes. The MRTA framework provides a general approach to timing verification for multicore systems that is parametric in the hardware configuration and so can be used at the architectural design stage to compare the guaranteed levels of real-time performance that can be obtained with different hardware configurations. We use the framework in this way to evaluate the performance of multicore systems with a variety of different architectural components and policies. These results are then used to compose a predictable architecture, which is compared against a reference architecture designed for good average-case behaviour. This comparison shows that the predictable architecture has substantially better guaranteed real-time performance, with the precision of the analysis verified using cycle-accurate simulation.

**Keywords** Multicore scheduling · Timing analysis · Verification

## 1 Introduction

Effective analysis of the worst-case timing behaviour of systems built on multicore architectures is essential if these high-performance platforms are to be deployed in critical real-time embedded systems used in the automotive and aerospace industries. We identify four different approaches to solving the problem of determining timing correctness.

With single-core systems, a *traditional two-step* approach is typically used. This consists of timing analysis which determines the *context-independent* worst-case execution time (WCET) of each task, followed by schedulability analysis, which uses task WCETs and information about the processor scheduling policy to determine if each task can be guaranteed to meet its deadline. When local memory (e.g. cache) is present, then this approach can be augmented by analysis of Cache Related Pre-emption Delays (CRPD) (Altmeyer et al. 2012), or by partitioning the cache to avoid CRPD altogether. Both approaches are effective and result in tight upper bounds on task response times (Altmeyer et al. 2014, 2016).

With a multicore system, the situation is more complex since WCETs are strongly dependent on the amount of *cross-core interference* on shared hardware resources such as main memory, L2 caches, and common interconnects, due to tasks running on other cores. The uncertainty and variability in this cross-core interference renders the traditional two-step process ineffective for many multicore processors. For exam-

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ple, on the Freescale P4080, the latency of a read operation varies from 40 to 600 cycles depending on the total number of cores running and the number of competing tasks (Nowotsch et al. 2014). Similarly, a 14 times slowdown has been reported (Radojković et al. 2012) due to interference on the L2 cache for tasks running on Intel Core 2 Quad processors. Further, recent work by Valsan et al. (2016) has shown that in some multicore systems with out-of-order execution, cache partitioning is insufficient to provide effective isolation, with shared Miss Status Handling Registers (MSHR) causing up to 20 times slowdown to code allocated its own separate cache partition.

At the other extreme is a *fully integrated* approach. This involves considering the precise interleaving of instructions originating from different cores (Gustavsson et al. 2010); however, such an approach suffers from potentially insurmountable problems of combinatorial complexity, due to the proliferation of different path combinations, as well as different release times and schedules.

An alternative approach is based on *temporal isolation* (Bui et al. 2011). The idea here is to statically partition the use of shared resources, e.g. space partitioning of cache and DRAM banks, time partitioning of bus access etc., so that context-independent WCET values can be used and the traditional two-step process applied. This approach raises a further challenge, how to partition the resources to obtain schedulability (Reineke and Doerfert 2014). Techniques which seek to limit the worst-case cross-core interference, for example by using TDMA arbitration on the memory bus or by limiting the amount of contention by suspending execution on certain cores (Nowotsch et al. 2014), can have a significant detrimental effect on performance, effectively negating the performance benefits of using a multicore system altogether. We note that TDMA is rarely if ever used as a bus-arbitration policy in real multicore processors, since it is not work-conserving and so wastes significant bandwidth. This impacts both worst-case and average-case performance, which are essential for application areas such as telecommunications that have a major influence on processor design.

The final approach is the one presented in this paper, based on *explicit interference modelling*. We argue that the strong interdependencies between timing analysis and schedulability analysis on multicore systems lead to undue pessimism. Thus a more nuanced and expressive interface is needed to integrate the demands placed on different resources by each task into schedulability analysis. In our approach, we omit the notion of WCET per se and instead directly target the calculation of task response times based on the demands that tasks place on the different hardware resources.

In this work, as a proof of concept, we use execution traces to model the behaviour of tasks and their resource demands. Traces provide a simple yet expressive way to model task behaviour, that captures information about the sequence of instructions and their memory accesses and corresponding types (read/write). Note that relying on execution traces does not pose a fundamental limitation to our approach as all required parameters can also be derived using static analysis (Li and Malik 1995; Ferdinand et al. 1999; Altmeyer 2013); however, traces enable a simple analysis of resource demands and so allow us to focus on an integrated response time analysis for multicore systems.

The main parameters used are the processor demand and the memory demand of each task. The latter quantity is used in analysis of the arbitration policy for the common interconnect, enabling us to upper bound the total memory access delays which may occur during the response time of a task. By computing the overall processor demand and memory demand over a relatively long interval of time (i.e. the task response time), as opposed to summing the worst case over many short intervals (e.g. individual memory accesses), we are able to obtain much tighter response time bounds.

The *Multicore Response Time Analysis framework (MRTA)* that we present is extensible to different types and arrangements of local memory, and different arbitration policies for the common interconnect. We instantiate the MRTA framework assuming the local memories used for instructions and data are single-level and either cache, scratchpad, or not present. In the case of caches we consider both cold caches, i.e. execution from an empty cache, and warm caches, taking advantage of information that resides in the cache from previous execution. With scratchpads, we consider both static and dynamic behaviour. Further, we assume that the memory bus arbitration policy may be TDMA, FIFO, Round-Robin, Fixed-Priority (based on task priorities), or Processor-Priority. We also account for the effects of DRAM refresh (Atanassov and Puschner 2001; Bhat and Mueller 2011). The general approach embodied in the MRTA framework is extensible to more complex, multi-level memory hierarchies, and to other sources of interference. We outline how the framework and analysis can be adapted to cover interference due to operation of the real-time operating system (RTOS) and Interrupt Handlers, we also discuss how to take into account the effects of policies used to control access to shared software resources, and how the framework can be used with open systems and for incremental verification.

The MRTA framework provides a general timing verification framework that is parametric in the hardware configuration (common interconnect, local memories, number of cores, etc.) and so can be used at the architectural design stage to compare the guaranteed levels of real-time performance that can be obtained with different hardware configurations, and also during the development and integration stages to verify the timing behaviour of a specific system. We use the framework in this way to evaluate guaranteed performance for multicore systems with a variety of different architectural components and policies. These results are then used to compose a predictable architecture, which is compared against a reference architecture designed for good average-case behaviour. This comparison shows that the predictable architecture has substantially better guaranteed real-time performance, with the precision of the analysis verified using cycle-accurate simulation.

While the specific hardware models and their mathematical representations used in this paper cannot capture all of the interference and complexity of actual hardware, they serve as a valid starting point. They include the dominant sources of interference and represent current architectures reasonably well.

## 1.1 Organisation

The rest of the paper is organised as follows. Section 2 discusses the related work. Section 3 describes the system model and notation used. Sections 4 and 5 show

how the effects of a local memory and the common interconnect can be modelled. Section 6 presents the nucleus of our framework, interference-aware MRTA. This analysis integrates processor and memory demands accounting for cross-core interference. Extensions to the presented analysis are discussed in Sect. 7. Section 8 describes a cycle-accurate simulator used to verify the precision of the analysis. Section 9 provides the results of an experimental evaluation using the MRTA framework, and Sect. 10 concludes with a summary and perspectives on future work.

## 2 Related work

The problem of estimating the response time of software real-time tasks executed on a multicore architecture is not new. The research community has been active in this area for the past ten years and an array of solutions have been proposed. Most of these solutions are, however either single-point solutions applicable to specific software and hardware models, or they focus exclusively on one particular sub-problem and abstract the rest by making simplistic assumptions. Only a few research works aim at designing a holistic analysis technique, typically because the solutions specific to the various sub-problems are very difficult to combine.

We note that it is challenging to organize the related work, since it is rare to find papers that share the same assumptions about the application and the hardware model. We therefore make a simple classification based on the primary focus of the analysis, whether it is on interference at the shared cache, memory bus, or main memory level, or on parameterizing WCETs. Further works are also covered that assume distinct application models and hardware models.

### 2.1 Related work with a focus on the memory bus

Although listed in this category, some of the works cited below also consider interference at the cache(s) or main memory level as well. However, they typically make either pessimistic or simplistic assumptions (like having private caches only) at those levels in order to simplify the model and thus focus on the contention for the shared memory bus.

Rosen et al. (2007) proposed an analysis technique for systems in which the shared memory bus uses TDMA arbitration and the time slots are statically assigned to the cores. This technique relies on (i) the availability of a user-programmable table-driven bus arbiter, which is typically not available in real hardware, and (ii) on the knowledge at design time of the characteristics of the entire workload that executes on each core.

In the same vein, also relying on TDMA arbitration of the memory bus, Chattopadhyay et al. (2010) and Kelter et al. (2011) proposed a response time analysis technique that considers a shared bus and an instruction cache, assuming separate buses and memories for both code and data. Their methods have limited applicability though, as they do not address data accesses to memory.

Paolieri et al. (2009) proposed a *multicore architecture* with hardware that enforces a constant upper bound on the latency of each access to a shared L2 memory through a shared bus. This approach enables the analysis of tasks in isolation since the interference on other tasks can be conservatively accounted for using this bound on the latency of each access. Similarly, the PTARM (Liu et al. 2012) enforces constant latencies for all instructions, including loads and stores; however, both cases represent customized hardware.

Lv et al. (2010) used *timed automata* to model the memory bus and the memory request patterns. Their method handles instruction accesses only and may suffer from state-space explosion when applied to data accesses. Another method employing timed automata was proposed by Gustavsson et al. (2010) in which the WCET is obtained by proving special predicates through model checking. This approach enables detailed system modelling, but is also prone to the problem of state-space explosion.

Schliecker et al. (2010) proposed a method that employs a *general event-based model* to estimate the maximum load on a shared resource. This approach makes few assumptions about the task model and is thus quite generally applicable; however, it only supports a single unspecified work-conserving bus arbiter.

Yun et al. (2012) proposed a *software-based memory throttling mechanism* to explicitly limit the memory request rate of each core and thereby control the memory interference. They also developed analytical solutions to compute proper throttling parameters that ensure the schedulability of critical tasks while minimising the performance impact of throttling.

Kelter et al. (2014) analysed the maximum bus arbitration delays for multicore systems sharing a TDMA bus and using both (private) L1 and (shared) L2 instruction and data caches.

Dasari et al. (2016) proposed a general framework to compute the maximum interference caused by the shared memory bus and its impact on the execution time of the tasks running on the cores. This method is more complex than the one proposed in this paper, and may be more accurate when it estimates the delay due to the shared bus; however, it assumes partitioned caches and therefore does not take cache-related effects into account, which makes it less general than the framework proposed here.

Jacobs et al. (2016) proposed a formal framework for the derivation of sound WCET analyses for multi-core processors. They show how to apply their analysis to account for interference on shared buses, accounting for cumulative information about the interference from tasks on other cores.

Huang et al. (2016) presented a response-time analysis that applies to multicores with one shared resource under fixed-priority arbitration. They give a simple task-to-core allocation algorithm and show that in conjunction with their response-time analysis it has a speedup factor of 7. Unlike the work in this paper, their model neither accounts for cache-related pre-emption delays nor for DRAM refreshes. Huang et al. (2016) also provide an improved response-time analysis for the case where tasks suspend from their processing core when accessing a shared resource. This is a reasonable assumption for DMA transfers, but not for individual memory accesses.

## 2.2 Related work with a focus on main memory

Most of the related work on memory controllers proposes scheduling algorithms that improve the controller performance, i.e., the average time to serve a sequence of requests, by (re)ordering the incoming requests at the controller level. Typically, these techniques are aimed at reducing the number of transitions between read and write modes. They seek to get the best performance from an open page policy by exploiting data locality.

Targeting real-time systems and thus time-predictability rather than performance, Kim et al. (2014a, 2016) presented a model to upper bound the memory interference delay caused by concurrent accesses to shared DRAM. Their work differs from this paper in that they primarily focus on the contention at the DRAM controller, assuming either fully-partitioned private caches or shared caches. For shared caches, they simply assume that either task preemption does not incur cache-related preemption delays (assuming in this case that cache coloring mechanisms are employed), or that the extra number of memory requests resulting from cache line evictions at runtime is given. Any further delays from shared resources, such as the memory bus, are simply assumed to be accounted for in the tasks' WCETs.

## 2.3 Related work with a focus on shared caches and scratchpads

Regarding the problem of estimating the WCET of tasks running in systems with shared caches, Yan and Zhang (2008) proposed a solution assuming direct-mapped, shared L2 instruction caches on multicores. The applicability of the approach is unfortunately limited as it makes very restrictive assumptions such as (i) data caches are perfect, i.e. all accesses are hits, and (ii) data references from different threads will not interfere with each other in the shared L2 cache.

Li et al. (2009a) proposed a method to estimate the worst-case response time of concurrent programs running on multicores with shared L2 caches, assuming set-associative instruction caches using the LRU replacement policy. Their work was later extended by Chattopadhyay et al. (2010) by adding a TDMA bus analysis technique to bound the memory access delay.

Regarding flash memory, Li and Mayer (2016) proposed a post-processing analysis methodology to acquire precise information about task flash memory contentions based on non-intrusive traces. For scratchpad memory, most of the works aim at reducing the WCET by proposing optimized stack management techniques (Lu et al. 2013) or dynamic code management techniques (Kim et al. 2014b), for loading program code from the main memory to the scratchpad.

Considering shared caches, there are a plethora of works that aim at reducing the impact of task pre-emptions and hence also the cache related pre-emption delays. Solutions to that problem are various: some address the problem at the task scheduling level Davis et al. (2013, 2015) by adding restrictions on the time at which tasks may be pre-empted, or at the cache management policy level (Ward et al. 2013; Mancuso et al. 2013; Slijepcevic et al. 2014). It is outside the scope of this paper to discuss all these research works.



## 2.4 Related work with a focus on parameterized WCETs

Rather than computing a unique upper-bound on the tasks' context independent WCET, some works propose solutions to characterize the WCET as a function of the platform characteristics and environment.

Paolieri et al. (2011) introduced an interference-aware task allocation algorithm that considers a set of WCET estimations per task, where each WCET estimation corresponds to a different execution environment (e.g. number of contending cores in a multicore system). The sensitivity of the WCET estimates to changes in the execution environment is used to guide the task to core allocation.

Reineke and Doerfert (2014) introduced *architecture-parametric* WCET analysis, which determines a function that bounds a task's WCET in terms of the amount and speed of resources allocated to that task. If a temporal-isolation approach is taken then such an analysis is required to partition shared resources in an informed manner. This analysis can also be adapted to determine WCET bounds in terms of the amount of interference on shared resources.

## 2.5 Related work assuming different application models

Most of the related work assumes independent tasks and only a few approaches have been proposed so far that consider task dependencies to some extent. Among them, the approach proposed by Li et al. (2009b) analyzes the worst-case cache access scenario of parallelized applications modeled by Message Sequence Graphs. The approach suffers from a very high time-complexity and assumes that the cache access behaviors are known and finite. Choi et al. (2016) used a more general model, comprising an event stream model for resource access and a task graph model for dependent tasks, in order to support a wider range of resource access patterns and parallelized execution of an application.

Schranzhofer et al. (2010) developed a framework based on a TDMA-arbitrated bus. This was followed by work on resource adaptive arbiters (Schranzhofer et al. 2011). Their work assumes a task model where each task consists of sequences of super-blocks, themselves divided into phases that represent implicit communication (fetching or writing of data to/from memory), computation (processing the data), or both. In contrast to the techniques presented in this paper, their approach requires major program intervention and compiler assistance to prefetch data. Adopting a similar model, Pellizzoni et al. (2010) compute an upper bound on the contention delay incurred by periodic tasks, for systems comprising any number of cores and peripheral buses sharing a single main memory. Their method does not cater for sporadic tasks and does not apply to systems with shared caches. In addition it relies on accurate profiling of cache utilization, suitable assignment of the TDMA time-slots to the tasks' super-blocks, and imposes a restriction on where the tasks can be pre-empted.

Pellizzoni et al. (2011) introduced the PRedictable Execution Model (PREM) framework. This framework considers tasks as consisting of memory phases where they pre-fetch instructions and data, and execution phases where they execute with-

out the need to access memory or I/O devices. The aim is to enable more efficient operation whereby the memory phase of one task overlaps with the execution phase of another. Yao et al. (2012) presented a TDMA scheduling algorithm for PREM tasks on a multicore, and Wasly and Pellizzoni (2014) provided schedulability analysis for non-preemptable PREM tasks on a partitioned multicore. Lampka et al. (2014) proposed a formal approach for bounding the worst-case response time of concurrently executing real-time tasks under resource contention and almost arbitrarily complex resource arbitration policies, with a focus on main memory as a shared resource. Global scheduling of PREM tasks has also been considered by Alhammad and Pellizzoni (2014) and Alhammad et al. (2015).

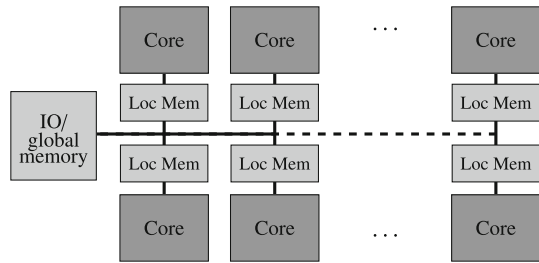
## 2.6 Related work assuming COTS hardware components

COTS multicore processors are typically designed to optimize average-case performance and most of their internal mechanisms are usually not documented. For such multicore platforms, Yun et al. (2015) proposed a worst-case memory interference delay analysis under the assumptions that (i) multiple memory requests can be simultaneously outstanding and (ii) the COTS DRAM controller has a separate read and write request buffer, prioritizes reads over writes, and supports out-of-order request processing. In contrast with this work, they assume non-blocking caches (common in COTS processors) that can handle multiple simultaneous cache-misses and focus solely on non-shared LLC (last level of cache) and DRAM bank partitioned systems. Non blocking caches have been the focus a multiple studies recently; however, we do not cover those techniques here. The main problem with non-blocking caches is that the miss status holding registers (MSHRs), special hardware registers which track the status of outstanding cache-misses, can be a significant source of contention (Valsan et al. 2016).

Trilla et al. (2016) proposed a timing model to predict the performance of applications at an early design stage. Their approach is based on generating an execution profile for each application that allows contention analysis on the shared processor resources. The main difference with our approach resides in their assumption that most of the hardware arbitration mechanisms are undocumented and therefore the applications' execution profiles are obtained based on an empirical analysis.

Most work on response time analysis for multicores, including this paper, assumes *timing compositionality* (Hahn et al. 2013). Intuitively, for a timing-compositional multicore, it is safe to separately account for delays from different sources, such as computation on a given core, additional cache misses due to preemptions, and interference on a shared bus. Unfortunately, recent results by (Hahn et al. 2015) indicate that even simple commercial multicores are non-compositional, rendering most existing analyses unsound for these architectures. Hahn et al. (2016), however, introduced an extended WCET analysis that enables compositional response time analysis for arbitrary, non-compositional multicores.

**Fig. 1** Multicore platform. A set of  $\ell$  cores with local memories connected via a common bus to a global memory



### 3 System model

In this paper, we provide a theoretical framework that can be instantiated for a range of different multicore architectures with different types of memory hierarchy and different arbitration policies for the common interconnect. Our aim is to create a flexible, adaptable, and generic analysis framework wherein a large number of common multicore architecture designs can be modeled and analysed. Inevitably, in this paper we can only cover a limited number of types of local memory, bus, and global memory behaviour. We select common approaches to model the different hardware components and integrate them into an extensible framework.

#### 3.1 Multicore architectural model

We model a generic multicore platform with  $\ell$  timing-compositional cores  $P_1, \dots, P_\ell$  as depicted in Fig. 1. By timing-compositional cores we mean cores where it is safe to separately account for delays from different sources, such as computation on a given core and interference on a shared bus (Hahn et al. 2013).

The set of cores is defined as  $\mathbb{P}$ . Each core has a local memory which is connected via a shared bus to a global memory and IO interface. We assume constant delays  $d_{\text{main}}$  to retrieve data from global memory under the assumption of an immediate bus access, i.e., no wait-cycles or contention on the bus. We assume atomic bus transactions, i.e., no split transactions, which furthermore are not re-ordered, and non-preemptable busy waiting on the core for requests to be serviced. Further, we assume that bus access may be given to cores for one access at a time. The types of the memories and the bus policy are parameters that can be instantiated to model different multicore systems.

In this paper we assume write-through caches only and omit consideration of delays due to cache coherence and synchronization. We also consider write-through and write-back scratchpads.

#### 3.2 Task model

We assume a set of  $n$  sporadic tasks  $\{\tau_1, \dots, \tau_n\}$ ; each task  $\tau_i$  has a minimum period or inter-arrival time  $T_i$  and a deadline  $D_i$ . Deadlines are assumed to be constrained, hence  $D_i \leq T_i$ .

We assume that the tasks are statically partitioned to the set of  $\ell$  identical cores  $\{P_1, \dots, P_\ell\}$ , and scheduled on each core using fixed-priority pre-emptive scheduling. The set of tasks assigned to core  $P_x$  is denoted by  $\Gamma_x$ .

The index of each task is unique and thus provides a global priority order, with  $\tau_1$  having the highest priority and  $\tau_n$  the lowest. The global priority of each task translates to a local priority order on each core which is used for scheduling purposes. We use  $hp(i)$  ( $lp(i)$ ) to denote the set of tasks with higher (lower) priority than that of task  $\tau_i$ , and we use  $hep(i)$  ( $lep(i)$ ) to denote the set of tasks with higher or equal (lower or equal) priority to task  $\tau_i$ .

We initially assume that the tasks are independent, in so far as they do not share mutually exclusive software resources (discussed in Sect. 7); nevertheless, the tasks compete for hardware resources such as the processor core, local memory, and the memory bus.

The execution of task  $\tau_i$  is modelled using a set of traces  $O_i$ , where each trace  $o = [\iota_1, \dots, \iota_k]$  is an ordered list of instructions. For ease of notation, we treat the ordered list of instructions as a multi-set, whenever we can abstract away from the specific order. We distinguish three types of instruction  $it$ :

$$it = \begin{cases} r[m^{da}] & \text{read data from memory block } m^{da} \\ w[m^{da}] & \text{write data to memory block } m^{da} \\ e & \text{execute} \end{cases} \quad (1)$$

An instruction  $\iota$  is a triple consisting of the instruction's memory address  $m^{in}$ , its execution time  $\Delta$  without memory delays, i.e., assuming a perfect local memory, and the instruction type  $it$ :

$$\iota = (m^{in}, \Delta, it) \quad (2)$$

We use  $m$  to denote a memory block, and the set of memory blocks is defined as  $\mathbb{M}$ .  $\mathbb{M}^{in}$  denotes the instruction memory blocks and  $\mathbb{M}^{da}$  the data memory blocks.  $m^{in}$  and  $m^{da}$  are defined accordingly. We assume that data memory and instruction memory are disjoint, i.e,  $\mathbb{M}^{in} \cap \mathbb{M}^{da} = \emptyset$ .

### 3.2.1 Using traces to model the tasks' behaviour

The use of traces to model a task's behaviour is unusual as the number of traces is exponential in the number of control-flow branches. Despite this obvious drawback, we decided to use traces for a number of reasons:

- Traces provide a simple yet expressive way to model task behaviour. They enable a near-trivial static cache analysis and a simple multicore simulation to evaluate the accuracy of the timing verification framework.
- Traces show that the worst-case execution behaviour of a task  $\tau_i$  on a multicore system is *not* uniquely defined. For example, the highest impact on a task scheduled on the same core due to task  $\tau_i$  may occur when it uses that core for the longest possible time interval, whereas the highest impact on tasks scheduled on other cores may occur when task  $\tau_i$  produces the largest number of bus accesses. These two cases may well correspond to different execution traces.

As a remedy for the exponential number of traces, complexity can be reduced by (i) computing a synthetic worst-case trace or by (ii) deriving the set of Pareto optimal traces that maximize the task's impact on a given performance metric or combination of different performance metrics, see (Li and Malik 1995). (The derivation of the Pareto front of traces is part of our future work.)

We note that using traces does not reduce the applicability of our approach. We use traces as a simple model which allows us to describe the computation of resource demand for various types of architectural component, and to focus on the multicore response time analysis. We can also completely resort to static analysis to derive independent upper bounds on the resource demands. For example, a static cache analysis (Ferdinand et al. 1999) can be used to bound the number of bus and also DRAM accesses. Static pre-emption cost analyses (Altmeyer 2013) are also available to bound the impact of pre-emptions, and we can use implicit path enumeration (Li and Malik 1995) to derive an upper bound on the purely computational demand of a task. These independently derived upper bounds can then be represented by a single, synthetic trace that maximizes each type of resource demand. Using static analyses in this way strongly reduces the computational complexity, but may lead to pessimism. These static analyses are, however, outside the scope of this paper, and an evaluation of the trade-off in terms of pessimism is left for future work.

### 3.3 Pre-emption cost model

We now extend the task model introduced above to include pre-emption costs. These costs occur when the pre-empting task evicts cache blocks of the pre-empted task that have to be reloaded after the pre-empted task resumes. To analyse the effect of pre-emption on a pre-empted task, Lee et al. (1998) introduced the concept of a useful cache block. Applying this concept to traces, a memory block  $m$  is referred to as a useful cache block (*UCB*) at a program point corresponding to instruction  $\iota$  on trace  $o$ , if (i)  $m$  is cached at that program point and (ii)  $m$  is reused by a later instruction in the trace without prior eviction. In the case of pre-emption at the program point corresponding to instruction  $\iota$  on trace  $o$ , only the memory blocks that (i) are cached and (ii) will be reused, may cause additional reloads. Hence, the number of UCBs at a program point gives an upper bound on the number of additional reloads due to a pre-emption at that point in the trace. A tighter definition is presented by Altmeyer and Burguière (2009); however, in this paper we need only the basic concept.

The worst-case impact of a pre-empting task is given by the number of cache blocks that the task may evict during its execution. A memory block accessed during the execution of a trace  $o$  is referred to as an evicting cache block (*ECB*). Accessing an ECB may evict a cache block of a pre-empted task. The intersection of UCBs of the pre-empted tasks with ECBs of the pre-empting task provides a tight upper bound on the cache-related pre-emption costs.

In this paper, we represent the sets of ECBs and UCBs as sets of integers with the following meaning:

$s \in \text{UCB}_{\iota,o} \Leftrightarrow$  the program point  $\iota$  in trace  $o$  has a useful cache block in cache-set  $s$   
 $s \in \text{ECB}_o \Leftrightarrow$  trace  $o$  may evict a cache block in cache-set  $s$

We note that a separate computation of the pre-emption cost is restricted to architectures without timing anomalies (Lundqvist and Stenström 1999) but is independent of the type of cache used, i.e. data, instruction or unified cache. For examples of the use of UCBs and ECBs to compute pre-emption costs, see the work of Altmeyer et al. (2012).

### 3.4 Table of notation

Table 1 provides a quick reference for the notation used in this paper. Much of this notation is introduced and defined in later sections. Note we do not include in this table notation that is only used locally for the purpose of simplifying expressions.

## 4 Memory modelling

In this section we show how the effects of a local memory can be modelled via a MEM function which describes the number of accesses due to a task which are passed to the next level of the memory hierarchy, in this case main memory. The MEM function is instantiated for both cache and scratchpads. We model the effect of a (local) memory using a function of the form:

$$\text{MEM}: \mathbb{O} \rightarrow \mathbb{N} \times 2^{2^{\mathbb{N}}} \times 2^{\mathbb{N}} \tag{3}$$

where  $\mathbb{O}$  is the domain of traces and  $\text{MEM}(o) = (\text{MD}_o, \overline{\text{UCB}}_o, \text{ECB}_o)$  computes, for a trace  $o$ , three quantities: (i) the number of bus accesses i.e., the number of memory accesses which cannot be served by the local memory alone, referred to as the memory demand  $\text{MD}_o$ ; (ii) a multiset  $\overline{\text{UCB}}_o$  containing, for each program point  $\iota$  in trace  $o$ , the set of Useful Cache Blocks (UCBs), which may need to be reloaded when trace  $o$  is pre-empted at that program point, i.e.  $\overline{\text{UCB}}_o = \bigcup_{\iota \in o} \{\text{UCB}_{\iota,o}\}$ ; (iii) the set  $\text{ECB}_o$  of Evicting Cache Blocks (ECBs) corresponding to the set of all cache blocks accessed by trace  $o$  which may evict memory blocks of other tasks from the cache. MD does not just cover cache misses, but also has to account for write accesses. In the case of write-through caches, each write access will cause a bus access, irrespective of whether or not the memory block is present in cache. (We leave integration of analysis for write-back caches (Davis et al. 2016) as future work).

MD assumes non-preemptive execution. With preemptive execution and caches, more than MD memory accesses can contribute to the bus contention. In this paper, we make use of the CRPD analysis for fixed-priority preemptive scheduling introduced by Altmeyer et al. (2012) to upper bound the additional memory accesses needed to reload cache blocks evicted due to pre-emption.

We now derive instantiations of the function  $\text{MEM}(o)$  for a trace  $o = [\iota_1, \dots, \iota_k]$  for instruction memories and data memories for systems (i) without cache, (ii) with

**Table 1** Notation

|  |  |
|--|--|
| Set of cores   | $\mathbb{P} = \{P_1, \dots, P_\ell\}$  |
| Number of cores  | $\ell$   |
| Core index   | $x, y$   |
| Task set   | $\Gamma = \{\tau_1, \dots, \tau_n\}$   |
| Number of tasks  | $n$  |
| Task index   | $i, j$   |
| Tasks on core $P_x$  | $\Gamma_x$   |
| Task worst-case execution time with no interference                | $C_i$  |
| Task period  | $T_i$  |
| Task deadline  | $D_i$  |
| Task response time   | $R_i$  |
| Task memory demand   | $MD_i$   |
| Task processor demand  | $PD_i$   |
| Tasks with higher priority than $\tau_i$                           | $hp(i)$  |
| Tasks with higher or equal priority to $\tau_i$                    | $hep(i)$   |
| Tasks with lower priority than $\tau_i$                            | $lp(i)$  |
| Tasks with lower or equal priority to $\tau_i$                     | $lep(i)$   |
| Tasks $\tau_j$ may pre-empt within the response time of $\tau_i$   | $aff(i, j)$  |
| Bus accesses from tasks in $hep(i)$ on core $P_x$ in time $t$      |  |
| Where $\tau_i$ is the task under analysis                          | $S_i^x(t)$   |
| Bus accesses from tasks in $hep(j)$ on core $P_y$ in time $t$      | $A_j^y(t)$   |
| Bus accesses from tasks in $lp(j)$ on core $P_y$ in time $t$       | $L_j^y(t)$   |
| Memory block   | $m$  |
| Set of memory blocks   | $\mathbb{M}$   |
| Instruction type   | $it = \begin{cases} r[m] \\ w[m] \\ e \end{cases}$   |
| Instruction  | $\iota = (m, \Delta, it)$  |
| Execution trace  | $o = [t_1, \dots, t_k]$  |
| Set of traces of task $\tau_i$                                     | $O_i$  |
| Memory demand of trace $o$   | $MD_o$   |
| ECBs of trace $o$  | $ECB_o$  |
| ECBs of task $\tau_i$  | $ECB_i$  |
| UCBs at instruction $\iota$ of trace $o$                           | $UCB_{\iota,o}$  |
| Multi-set of UCBs of trace $o$                                     | $\overline{UCB}_o$   |
| Memory blocks cached after executing trace $o$                     | $Cached(o)$  |
| Cache lines that may be evicted by tasks other than $\tau_i$       | POT-EVICTED <sub><math>i</math></sub>  |
| Definitely cached memory blocks at the start of $\tau_i$           | DEF-CACHED <sub><math>i</math></sub>   |
| Cost of a pre-emption by $\tau_j$ during response time of $\tau_i$ | $\gamma_{i,j,x}$   |
| Bus function   | $BUS: \mathbb{N} \times \mathbb{P} \times \mathbb{N} \rightarrow \mathbb{N}$                           |
| Memory function  | $MEM: \mathbb{O} \rightarrow \mathbb{N} \times \mathbb{N} \times 2^{\mathbb{N}} \times 2^{\mathbb{N}}$ |

**Table 1** continued

|   |   |
|---|---|
| Scratchpad function   | SPM: $\mathbb{M} \rightarrow \{true, false\}$                   |
| Cache hit function  | Hit: $\mathbb{I} \times \mathbb{M} \rightarrow \{true, false\}$ |
| Number of bus access slots assign to each core                    | $v$   |
| Global memory delay   | $d_{main}$  |
| DRAM refresh delay  | $d_{refresh}$   |
| DRAM refresh period   | $T_{refresh}$   |
| Processor interference on task $\tau_i$ on core $P_x$ in time $t$ | $I^{PROC}(i, x, t)$   |
| Bus interference on task $\tau_i$ on core $P_x$ in time $t$       | $I^{BUS}(i, x, t)$  |
| DRAM interference on task $\tau_i$ on core $P_x$ in time $t$      | $I^{DRAM}(i, x, t)$   |

scratchpads, and (iii) with direct-mapped or LRU caches. In the following, the superscripts indicate data (da) or instruction memory (in), and the subscripts the type of memory, i.e., uncached (nc), scratchpad (sp), or caches (ca).

### 4.1 Uncached

Assuming a system with no cache, considering instruction memory, the number of bus accesses  $MD_o$  for a trace  $o$  is given by the number of instructions  $k$  in the trace. The sets of UCBs and ECBs are empty, as pre-emption has no effect on the performance of the local memory, since there is none.

$$MEM_{nc}^{in}(o) = (k, \emptyset, \emptyset) \tag{4}$$

Considering data memory, we have to account for the number of data accesses, irrespective of whether they are read or write accesses. The number of accesses  $MD_o$  is thus equal to the number of data access instructions.

$$MEM_{nc}^{da}(o) = \left( \left| \left\{ \iota_i \mid \iota_i \in o \wedge \iota_i = (\_, \_, r/w[m^{da}]) \right\} \right|, \emptyset, \emptyset \right) \tag{5}$$

### 4.2 Scratchpads

Scratchpads are explicitly managed local memories that exhibit higher predictability and less dynamic behavior than caches. Hence, scratchpads are commonly advocated for embedded multicore systems.

Scratchpads can implement a write-back or, less commonly, a write-through policy for write accesses. Furthermore scratchpad management may be either static or dynamic. With a static scratchpad management, the scratchpad contents remain constant throughout operation, whereas with dynamic scratchpad management, scratchpad blocks can be reloaded as needed, for example on pre-emptions, which makes better use of the available scratchpad memory (Whitham et al. 2012, 2014).



### 4.2.1 Static scratchpads

A static scratchpad memory is defined using a function  $\text{SPM}: \mathbb{M} \rightarrow \{\text{true}, \text{false}\}$ , which returns *true* for memory blocks that are stored in the scratchpad.

For an instruction scratchpad, each access to a memory block which is not stored in the scratchpad causes an additional bus access. Thus for each trace  $o$ , we have:

$$\text{MEM}_{\text{sp}}^{\text{in}}(o) = \left( \left| \left\{ l_i | l_i \in o \wedge l_i = (m^{\text{in}}, \_, \_) \wedge \neg \text{SPM}(m^{\text{in}}) \right\} \right|, \emptyset, \emptyset \right) \quad (6)$$

For a data scratchpad, we have to distinguish between a write-through (*wt*) policy, where each write-access results in a bus access:

$$\begin{aligned} \text{MEM}_{\text{sp-wt}}^{\text{da}}(o) = & \left( \left| \left\{ l_i | l_i \in o \wedge l_i = (\_, \_, r[m^{\text{da}}]) \wedge \neg \text{SPM}(m^{\text{da}}) \right\} \right| \right. \\ & \left. + \left| \left\{ l_i | l_i \in o \wedge l_i = (\_, \_, w[m^{\text{da}}]) \right\} \right|, \emptyset, \emptyset \right) \quad (7) \end{aligned}$$

and a write-back (*wb*) policy, where each accessed memory block only results in one bus access at job completion, irrespective of the number of reads and writes to it:

$$\begin{aligned} \text{MEM}_{\text{sp-wb}}^{\text{da}}(o) = & \left( \left| \left\{ l_i | l_i \in o \wedge l_i = (\_, \_, r[m^{\text{da}}]) \wedge \neg \text{SPM}(m^{\text{da}}) \right\} \right| \right. \\ & \left. + \left| \left\{ l_i | m^{\text{da}} \in o \wedge l_i = (\_, \_, w[m^{\text{da}}]) \right\} \right|, \emptyset, \emptyset \right). \quad (8) \end{aligned}$$

As with other forms of local memory, the aim of a scratchpad is to reduce the number of bus accesses. An effective scratchpad configuration is obtained by storing the  $N$  most frequently used memory blocks, where  $N$  is the maximum number of memory blocks that the scratchpad can hold. With execution traces, identifying the most frequently used memory blocks is nearly trivial; however, in general more sophisticated optimization techniques have to be used (Falk and Kleinsorge 2009).

### 4.2.2 Dynamic scratchpads

A scratchpad can be dynamic in two respects: (i) tasks can share the scratchpad space with other tasks, and (ii) a task can reload and change the scratchpad contents during its own execution. In the first case, the scratchpad configuration has to be loaded at the beginning of a task's execution and restored after each pre-emption. In the second case, different scratchpad contents are used for different sub-traces of the task. In the following, we only present the implementation of MEM for the first case, i.e., where the scratchpad is shared among different tasks. Extension to the second case is trivial.

In a slight abuse of notation, we model the pre-emption overhead in the case of shared scratchpads using sets of UCBs and ECBs. These are used to represent the memory blocks of a task that are stored in the scratchpad. A tighter integration, which

requires dedicated hardware support is described by Whitham et al. (2012, 2014); however, analysis for it is beyond the scope of this paper. As in the static case, a scratchpad memory is defined using a function  $SPM: \mathbb{M} \rightarrow \{true, false\}$ , which returns *true* for memory blocks that are stored in the scratchpad.

For an instruction scratchpad, for each trace  $o$  we define the set of memory blocks that are accessed by the trace and are stored in the scratchpad as follows:

$$ECB_o^{in} = \begin{cases} \{m^{in} | (m^{in}, \_, \_) \in o \wedge SPM(m^{in})\} & \text{shared scratchpad} \\ \emptyset & \text{dedicated scratchpad} \end{cases} \quad (9)$$

Similarly for a data scratchpad:

$$ECB_o^{da} = \begin{cases} \{m^{da} | (\_, \_, r/w[m^{da}]) \in o \wedge SPM(m^{da})\} & \text{shared scratchpad} \\ \emptyset & \text{dedicated scratchpad} \end{cases} \quad (10)$$

The set of UCBs is then defined using the set of ECBs, i.e.  $\overline{UCB}_o^{in/da} = \{ECB_o^{in/da}\}$

In the case of an instruction scratchpad, each memory access to a memory block which is not stored in the scratchpad causes an additional bus access:

$$MEM_{sp}^{in}(o) = \left( |ECB_o^{in}| + \left| \{l_i | l_i \in o \wedge l_i = (m^{in}, \_, \_) \wedge \neg SPM(m^{in})\} \right|, \overline{UCB}_o^{in}, ECB_o^{in} \right) \quad (11)$$

The term  $|ECB_o^{in}|$  in (11) accounts for the initialization of the scratchpad at the start of the task in the case of a shared scratchpad. (The set  $ECB_o^{in}$  is empty in case of a dedicated scratchpad memory).

In the case of a data scratchpad, we again have to distinguish between a write-through (*wt*) policy and a write-back (*wb*) policy. Assuming a write-through policy, each write-access results in a bus access:

$$MEM_{sp-wt}^{da}(o) = \left( |ECB_o^{da}| + \left| \{l_i | l_i \in o \wedge l_i = (\_, \_, r[m^{da}]) \wedge \neg SPM(m^{da})\} \right| + \left| \{l_i | l_i \in o \wedge l_i = (\_, \_, w[m^{da}])\} \right|, \overline{UCB}_o^{da}, ECB_o^{da} \right) \quad (12)$$

Whereas assuming a write-back policy, each memory block that is written to causes only one bus access at job completion:

$$MEM_{sp-wb}^{da}(o) = \left( |ECB_o^{da}| + \left| \{l_i | l_i \in o \wedge l_i = (\_, \_, r[m^{da}]) \wedge \neg SPM(m^{da})\} \right| + \left| \{m^{da} | (\_, \_, w[m^{da}]) \in o\} \right|, \overline{UCB}_o^{da}, ECB_o^{da} \right). \quad (13)$$

### 4.3 Caches

Caches are commonly used in multicore systems to bridge the performance gap between processor and main memory speeds. Unlike scratchpads they require no explicit management, rather the eviction of cache blocks is determined by the cache replacement policy. In this section, we consider both *cold* caches, representing the pessimistic case where the cache is empty or contains no useful blocks when a job of task starts to execute, and *warm* caches, where some useful blocks may persist from the execution of previous jobs of the same task.

#### 4.3.1 Cold caches

We assume a function  $\text{Hit}: \mathbb{I} \times \mathbb{M} \rightarrow \{\text{true}, \text{false}\}$ , which classifies each memory access at each instruction as a cache hit or a cache miss. This function can be derived using cache simulation of the access trace starting with an empty cache or by using traditional cache analysis (Ferdinand et al. 1999), where each unclassified memory access is considered a cache miss. This allows us to upper bound the number of cache misses. For each possible program point  $\iota$  on trace  $o$  (i.e. for each possible pre-emption point), the set of UCBs is derived using the corresponding analysis described in the thesis of Altmeyer (2013, Chap. 5, Sect. 4): a forward cache analysis derives for each program point the set of cached memory blocks, and a backward cache analysis provides the set of memory blocks that will be reused before they may be evicted. The set of UCBs per program point  $\iota$  is then given by the intersection of the result of the forward and the backward cache analyses at  $\iota$ . For the purpose of our analysis, it is sufficient to store only the cache sets that useful memory blocks map to. The multiset  $\overline{\text{UCB}}_o$  contains, for each program point  $\iota$  in trace  $o$ , the set of UCBs for that program point, i.e.  $\overline{\text{UCB}}_o = \bigcup_{\iota \in o} \{\text{UCB}_{\iota,o}\}$ . The set of ECBs is the set of cache sets that memory blocks accessed in trace  $o$  map to. Finally, the memory demand of trace  $o$  is given by the number of instructions in the trace that are not cache hits.

In the case of an instruction cache, we have:

$$\text{MEM}_{\text{ca}}^{\text{in}}(o) = \left( \left| \left\{ \iota_i | \iota_i \in o \wedge \iota_i = (m^{\text{in}}, \_, \_) \wedge \neg \text{Hit}(m^{\text{in}}, \iota_i) \right\} \right|, \overline{\text{UCB}}_o^{\text{in}}, \text{ECB}_o^{\text{in}} \right) \quad (14)$$

For a data cache, since we assume a write-through policy, each write access contributes a bus access, thus:

$$\begin{aligned} \text{MEM}_{\text{ca}}^{\text{da}}(o) = & \left( \left| \left\{ \iota_i | \iota_i \in o \wedge \iota_i = (\_, \_, r[m^{\text{da}}]) \wedge \neg \text{Hit}(m^{\text{da}}, \iota_i) \right\} \right| \right. \\ & \left. + \left| \left\{ \iota_i | \iota_i \in o \wedge \iota_i = (\_, \_, w[m^{\text{da}}]) \right\} \right|, \overline{\text{UCB}}_o^{\text{da}}, \text{ECB}_o^{\text{da}} \right) \quad (15) \end{aligned}$$

### 4.3.2 Warmed-up caches

Previously, we pessimistically assumed that each job of each task starts its execution with an empty cache. In reality, starting from the second job of a task, some of its instructions and data may still be cached when the job starts, reducing its execution time and memory demand. In order to capture this phenomenon, we propose an analysis that can be used to bound the response time of jobs after each task has run at least once, for example during a separate *start-up* phase.

We now consider which memory blocks can safely be assumed to be cached at the start of a job of task  $\tau_i$ , when another job of that task has run before. This set of memory blocks is determined by what *must* be cached at the end of the job’s execution when it runs in isolation, minus those memory blocks that *may* be evicted by a job of any task  $\tau_j$  that can run *between* the two jobs of task  $\tau_i$ . Since task  $\tau_i$  is not active during this time, evicting jobs can belong to any task  $\tau_j$  with higher or lower priority than  $\tau_i$ .

Let,  $Cached(o)$  be the set of memory blocks that are cached after executing trace  $o$  of task  $\tau_i$  starting from an empty cache. For a given trace  $o$ , this set can be determined by simulation. The set of blocks that are definitely cached at the end of one run of the task in isolation is given by  $\bigcap_{o \in O_i} Cached(o)$ , where  $O_i$  is the set of traces representing the task. The set of memory blocks that are guaranteed to be cached after executing one job of a task could similarly be approximated by must-cache analysis (Ferdinand and Wilhelm 1999).

Let  $P_x$  be the core that task  $\tau_i$  executes on. The set of cache lines that may be evicted by tasks other than  $\tau_i$  is determined as follows:

$$POT-EVICTED_i = \bigcup_{\tau_j \in \Gamma_x \setminus \{\tau_i\}} \bigcup_{o \in O_j} ECB_o^{in} \cup ECB_o^{da}. \tag{16}$$

Given the sets defined above, we can compute the set of definitely cached memory blocks DEF-CACHED<sub>*i*</sub> of task  $\tau_i$  as follows:

$$DEF-CACHED_i = \left\{ b \in \bigcap_{o \in O_i} Cached(o) \mid line(b) \notin POT-EVICTED_i \right\}, \tag{17}$$

where  $line(b)$  determines the cache line that memory block  $b$  maps to.

To take information about definitely cached memory blocks into account, we assume the function Hit from Sect. 4.3.1 is extended to take into account which blocks are guaranteed to be cached initially. The MEM functions for warmed-up instruction and data caches are hence:

$$MEM_{ca,w}^{in}(o) = \left( \left| \{l_i \mid l_i \in o \wedge l_i = (m^{in}, \_, \_) \wedge \neg Hit(m^{in}, l_i, DEF-CACHED_i)\} \right|, \overline{UCB}_o^{in}, ECB_o^{in} \right) \tag{18}$$

$$\begin{aligned} \text{MEM}_{ca,w}^{da}(o) = & \left( \left| \{l_i | l_i \in o \wedge l_i = (\_, \_, r[m^{da}]) \wedge \neg \text{Hit}(m^{da}, l_i, \text{DEF-CACHED}_i)\} \right| \right. \\ & \left. + \left| \{l_i | l_i \in o \wedge l_i = (\_, \_, w[m^{da}])\} \right|, \overline{\text{UCB}}_o^{da}, \text{ECB}_o^{da} \right) \end{aligned} \quad (19)$$

Note, in order to avoid any interference effects from the start-up or warm-up phase into regular operation, we assume the following protocol:

1. In the warm-up phase, a single job of each task is run non-preemptively on its allocated core. The order of task execution is arbitrary.
2. When the final job of the warm-up phase has finished, regular operation commences, and tasks are scheduled by fixed-priority preemptive scheduling.

Apart from the above protocol no further changes to the scheduling policy or analysis are needed to account for warmed-up caches.

#### 4.4 Memory combinations

To allow different combinations of local memories, for example scratchpad memory for instructions and an LRU cache for data, we define the combination of instruction memory  $\text{MEM}^{in}$  and data memory  $\text{MEM}^{da}$  as follows

$$\text{MEM}(o) = \left( \text{MD}_o^{in} + \text{MD}_o^{da}, \overline{\text{UCB}}_o^{in} \cup \overline{\text{UCB}}_o^{da}, \text{ECB}_o^{in} \cup \text{ECB}_o^{da} \right) \quad (20)$$

with  $\text{MEM}^{in}(o) = \left( \text{MD}_o^{in}, \overline{\text{UCB}}_o^{in}, \text{ECB}_o^{in} \right)$  being the result for the instruction memory and  $\text{MEM}^{da}(o) = \left( \text{MD}_o^{da}, \overline{\text{UCB}}_o^{da}, \text{ECB}_o^{da} \right)$  the result for the data memory.

### 5 Bus modelling

In this section we show how the memory bus delays experienced by a task can be modelled via a BUS function of the form:

$$\text{BUS}: \mathbb{N} \times \mathbb{P} \times \mathbb{N} \rightarrow \mathbb{N} \quad (21)$$

where  $\text{BUS}(i, x, t)$  denotes an upper bound on the number of bus accesses that can delay completion of task  $\tau_i$  on core  $P_x$  during a time interval of length  $t$ . This abstraction covers a variety of bus arbitration policies, including Round-Robin, FIFO, Fixed-Priority, and Processor-Priority, all of which are *work-conserving*, and also TDMA which is not work-conserving.

We now introduce the mathematical representations of the delays incurred under these arbitration policies. We note that the framework is extensible to a wide variety of different policies. The only constraints we place on instantiations of the  $\text{BUS}(i, x, t)$  function is that they are monotonically non-decreasing in  $t$ .

Let  $\tau_i$  be the task of interest, and  $x$  the index of the core  $P_x$  on which it executes. Other task indices are represented by  $j, k$  etc. while  $y, z$  are used for core indices.

Let  $S_i^x(t)$  denote an upper bound on the total number of bus accesses due to  $\tau_i$  and all higher priority tasks that run on the same core  $P_x$  during an interval of length  $t$ , while one job of task  $\tau_i$  is active, i.e. within its response time. Let  $A_j^y(t)$  be an upper bound on the total number of bus accesses due to all tasks of priority  $j$  or higher executing on a different core  $P_y \neq P_x$  during an interval of length  $t$ . (Note,  $j$  may not necessarily be the priority of a task allocated to core  $P_y$ ). In Sect. 6.3 we show how the values of  $S_i^x(t)$ ,  $A_j^y(t)$  and  $L_j^y(t)$ , defined below, are computed and explain why  $S_i^x(t)$  and  $A_j^y(t)$  are subtly different and hence require distinct notation.

As memory bus requests are typically non-preemptive, one lower priority<sup>1</sup> memory request may block a higher priority one, since the global shared memory may have just received a lower priority request before the higher priority one arrives. To account for these blocking accesses, we use  $L_j^y(t)$  which denotes an upper bound on the total number of bus accesses due to all tasks of priority lower than  $j$  executing on some other core  $P_y \neq P_x$  during an interval of length  $t$ .

In the following equations for the  $BUS(i, x, t)$  function, we account for blocking due to one non-preemptive access from lower priority tasks running on the same core  $P_x$  as task  $\tau_i$  (this is the +1 in the equations). This holds because such blocking can only occur at the start of the priority level- $i$  (processor) busy period.

For a fixed-priority bus with memory accesses inheriting the priority of the task that generates them, we have:

$$BUS(i, x, t) = S_i^x(t) + \sum_{\forall y \neq x} A_i^y(t) + \min \left( S_i^x(t), \sum_{\forall y \neq x} L_i^y(t) \right) + 1 \quad (22)$$

Here, the term  $S_i^x(t)$  covers the accesses from task  $\tau_i$  and higher priority tasks running on core  $P_x$ . The term  $\sum_{\forall y \neq x} A_i^y(t)$  is the interference due to accesses from higher priority tasks running on other cores. The term  $\min \left( S_i^x(t), \sum_{\forall y \neq x} L_i^y(t) \right)$  upper bounds the blocking due to tasks of lower priority than  $\tau_i$  running on other cores. (The number of blocking accesses is limited to one per access made by task  $\tau_i$  and higher priority tasks running on core  $P_x$  during time  $t$  i.e.  $S_i^x(t)$ , and also restricted to the maximum number of accesses made by tasks of lower priority than  $\tau_i$  running on other cores i.e.  $\sum_{y \neq x} L_i^y(t)$ ). Finally, the +1 accounts for a single blocking access from a task of priority lower than that of  $\tau_i$  on core  $P_x$ .

For a Processor-Priority bus with memory accesses inheriting the priority of the core rather than the task, we have:

$$BUS(i, x, t) = S_i^x(t) + \sum_{y \in HP(x)} A_n^y(t) + \min \left( S_i^x(t), \sum_{y \in LP(x)} A_n^y(t) \right) + 1 \quad (23)$$

<sup>1</sup> Here we mean priorities on the bus, which are not necessarily the same as task priorities.

where  $HP(x)$  ( $LP(x)$ ) is the set of cores with higher (lower) priority than that of  $P_x$ , and  $n$  is the index of the task with the lowest priority. The summation term  $\sum_{y \in HP(x)} A_n^y(t)$  captures the interference from all tasks (independent of their task priority) running on cores which have a higher processor priority than  $P_x$ . The term  $\min\left(S_i^x(t), \sum_{y \in LP(x)} A_n^y(t)\right)$  upper bounds the blocking due to tasks running on cores which have a processor priority lower than that of  $P_x$ .

A Round-Robin bus and a TDMA bus both make use of a pre-determined cycle of slots, where a slot is a time interval during which a single access can be serviced. Slots in the cycle are assigned to cores. With TDMA, the bus arbiter iterates over the cycle, taking the same time for each slot regardless of whether there is an access pending from the associated core, or not (i.e. the slot is empty). In contrast, a Round-Robin bus skips any empty slots, immediately moving to the next one with a pending access.

For a Round-Robin bus with  $v$  adjacent slots per core in a cycle of length  $\ell \cdot v$ , we have:

$$BUS(i, x, t) = S_i^x(t) + \sum_{\forall y \neq x} \min\left(A_n^y(t), v \cdot S_i^x(t)\right) + 1 \tag{24}$$

The worst-case situation for each access in  $S_i^x(t)$  from core  $P_x$  occurs when it just misses its last slot in the cycle and is therefore delayed by  $v$  accesses by each core  $P_y \neq P_x$ . This leads to interference of at most  $v \cdot S_i^x(t)$  from each core  $P_y \neq P_x$ ; however, the overall interference from each core  $P_y$  is also bounded by the number of accesses  $A_n^y(t)$ , hence the  $\min\left(A_n^y(t), v \cdot S_i^x(t)\right)$  term. Again, as we already account for all possible accesses from all other cores, there is no separate contribution to blocking.

For a TDMA bus with  $v$  adjacent slots per core in a cycle of length  $\ell \cdot v$ , we have:

$$BUS(i, x, t) = S_i^x(t) + ((\ell - 1) \cdot v) \cdot S_i^x(t) + 1 \tag{25}$$

Since TDMA is not work-conserving, the worst case corresponds to each access in  $S_i^x(t)$  just missing the last slot in the cycle for core  $P_x$  and hence having to wait  $((\ell - 1) \cdot v + 1)$  slots to be serviced. Effectively, there is additional interference from the  $(\ell - 1) \cdot v$  slots reserved for other cores on each access, irrespective of whether these slots are used or not (in contrast to Round-Robin). Note that when  $v = 1$ , Eq. (25) simplifies to  $BUS(i, x, t) = \ell \cdot S_i^x(t) + 1$ .

It is interesting to note that while TDMA provides more predictable behaviour, this is at a cost of significantly worse guaranteed performance over long time intervals (e.g. the response time of a task) due to the fact that it is not work-conserving. Effectively, this means that the memory accesses of a task may suffer additional interference due to empty slots on the bus. Nevertheless, Round-Robin behaves like TDMA when all other cores create a large number of competing memory accesses.

We note that the equal number of slots per core for Round-Robin and TDMA, and the grouping of slots per core are simplifying assumptions to exemplify how TDMA and Round-Robin buses can be analysed. An analysis for more complex configurations (patterns of slots) is reserved for future work.

For a FIFO bus, we assume that all accesses generated on the other cores may be serviced ahead of the last access of  $\tau_i$ , hence we have:

$$\text{BUS}(i, x, t) = S_i^x(t) + \sum_{\forall y \neq x} A_n^y(t) + 1 \quad (26)$$

Note that accesses from other cores do not contribute to blocking since we already pessimistically account for all these accesses in the summation term.

We note that the above analysis for a FIFO bus is potentially very pessimistic. If we assume that tasks busy wait on accesses and therefore only one access request per core can be in the FIFO queue at any given time then the worst-case situation for each access in  $S_i^x(t)$  from core  $P_x$  occurs when it finds the FIFO queue already contains one access request from each of the other cores. This case can be analysed using (24) for a Round-Robin bus assuming that  $v = 1$  i.e. one slot per core in the cycle. We note that some architectures may permit multiple requests to be queued by a single core (e.g. 8 in the case of the Kalray MPPA). Again, the bound on the number of requests in the queue means that the worst-case analysis equates to that for a Round-Robin bus assuming that  $v = 8$  i.e. 8 slots per core in the cycle. We include pure FIFO behaviour here to illustrate the degraded performance in this case.

## 6 Response time analysis

In this section, we present the nucleus of our timing verification framework: interference-aware MRTA. This analysis integrates the processor and memory demands of the task of interest and higher priority tasks running on the same core, including CRPD. It also accounts for the cross-core interference on the memory bus due to tasks running on the other cores.

A task set is deemed schedulable, if for each task  $\tau_i$ , its response time  $R_i$  is less than or equal to its deadline  $D_i$ :

$$\forall_i : R_i \leq D_i \Rightarrow \text{schedulable}$$

The traditional response time calculation (Audsley et al. 1993; Joseph and Pandya 1986) for fixed-priority pre-emptive scheduling on a uniprocessor is based on an upper bound on the WCET of each task  $\tau_i$ , denoted by  $C_i$ . By contrast, our MRTA framework dissects the individual components (processor and memory demands) that contribute to the WCET bound and re-assembles them at the level of the worst-case response time. It thus avoids the over-approximation inherent in using context-independent WCET bounds.

In the following, we assume that  $\tau_i$  is the task of interest whose schedulability we are checking, and  $P_x$  is the core on which it runs. Recall that there is a unique global ordering of task priorities even though the scheduling is partitioned with a fixed-priority pre-emptive scheduler on each core.



## 6.1 Interference on the core

We compute the maximal processor demand  $PD_i$  for each task  $\tau_i$  as follows:

$$PD_i = \max_{o \in O_i} \sum_{(\_, \Delta, \_) \in o} \Delta \quad (27)$$

where  $\Delta$  is the execution time of an instruction without memory delays. Task  $\tau_i$  suffers interference  $I^{\text{PROC}}(i, x, t)$  on its core  $P_x$  due to tasks of higher priority running on the same core within a time interval of length  $t$  starting from the critical instant:

$$I^{\text{PROC}}(i, x, t) = \sum_{j \in \Gamma_x \wedge j \in \text{hp}(i)} \left\lceil \frac{t}{T_j} \right\rceil PD_j \quad (28)$$

## 6.2 Interference on the local memory

Local memory improves a task's execution time by reducing the number of accesses to main memory. The memory demand of a trace gives the number of accesses that go to main memory and hence the bus, despite the presence of the local memory. The maximal memory demand  $MD_i$  of a task  $\tau_i$  is defined by the maximum number of bus accesses of any of its traces:

$$MD_i = \max_{o \in O_i} \left\{ MD \mid \text{MEM}(o) = (MD, \_, \_) \right\} \quad (29)$$

Note that the maximal memory demand refers to the demand of the combined instruction and data memory as defined in Eq. (20).

The memory demand  $MD_i$  is derived assuming non-preemptive execution, i.e. that the task runs to completion without interference on the local memory. The sets of UCBs and ECBs are used to compute the additional overhead due to pre-emption. In the computation of this overhead, we use the sets of UCBs per trace  $o$  to preserve precision,

$$\overline{UCB}_o = \overline{UCB} \text{ with } \text{MEM}(o) = (\_, \overline{UCB}, \_) \quad (30)$$

and derive the maximal set of ECBs per task  $\tau_i$  as the union of the ECBs on all traces.

$$ECB_i = \bigcup_{o \in O_i} \left\{ ECB \mid \text{MEM}(o) = (\_, \_, ECB) \right\} \quad (31)$$

We use  $\gamma_{i,j,x}$  (with  $j \in \text{hp}(i)$ ) to denote the overhead (additional accesses) due to a pre-emption of task  $\tau_i$  by task  $\tau_j$  on core  $P_x$ .

We use the ECB-Union (Altmeyer et al. 2011, 2012) approach as an exemplar of CRPD analysis, as it provides a reasonably precise bound on the pre-emption overhead with low complexity. (Other CRPD analysis techniques (Altmeyer et al. 2012; Lee et al. 2001) could also be integrated into this framework). The ECB-Union

approach first computes the union of all ECBs that may affect a pre-empted task. The intuition here is that direct pre-emption by task  $\tau_j$  is represented by the pessimistic assumption that task  $\tau_j$  has itself already been pre-empted by all of the tasks of higher priority and hence may result in evictions due to the set  $\bigcup_{h \in \text{hep}(j) \wedge h \in \Gamma_x} \text{ECB}_h$ . Note that a CRPD analysis has to correctly account for all pre-emption scenarios including nested pre-emption, as it otherwise may compute optimistic bounds on the CRPD (Altmeyer et al. 2011). The ECB-Union approach considers the maximum impact of these evicting cache blocks on any job of a task  $\tau_k$  that could be running during the response time of task  $\tau_i$ , where  $\tau_i$  is the task of interest in the response time analysis. Such a task  $\tau_k$  must have a priority equal to or higher than that of task  $\tau_i$  (otherwise it could not run in the busy period), but lower than that of the pre-empting task  $\tau_j$  (otherwise it could not be pre-empted). These are referred to as the set of *affected* tasks  $\text{aff}(i, j) = \text{hep}(i) \cap \text{lp}(j)$ . Further, task  $\tau_k$  must also be on core  $P_x$ . Thus the set of potentially pre-empted tasks is therefore indicated by  $k \in \text{aff}(i, j) \wedge k \in \Gamma_x$ . Further, pre-emption may take place at any program point in any trace of task  $\tau_k$ . Putting all this together, the follow expression upper bounds the pre-emption cost by determining the maximum intersection between the evicting cache blocks of task  $\tau_j$  and higher priority tasks and the useful cache blocks at any program point in any trace of any task that can be pre-empted by task  $\tau_j$  during the response time of task  $\tau_i$ .

$$\gamma_{i,j,x} = \max_{k \in \text{aff}(i,j) \wedge k \in \Gamma_x} \left( \max_{o \in O_k} \left( \max_{\text{UCB}_t \in \overline{\text{UCB}}_o} \left| \left\{ \text{UCB}_t \cap \left( \bigcup_{h \in \text{hep}(j) \wedge h \in \Gamma_x} \text{ECB}_h \right) \right\} \right| \right) \right) \tag{32}$$

For dynamic shared scratchpads, our slight abuse of notation in defining ECBs and UCBs enables the above analysis of pre-emption costs to be used. Recall that for dynamic shared scratchpads, (9) and (10) define the ECBs for a trace as all of the memory blocks that the trace stores in the scratchpad. The UCBs are then defined as equal to the ECBs. With these definitions, the pre-emption cost analysis effectively assumes that at any program point in any trace in any pre-empted task, all of the UCBs (i.e. memory blocks stored in the scratchpad) for that trace are useful and will need reloading if they are evicted by the ECBs (i.e. memory blocks transferred to the scratchpad) by a pre-empting task.

### 6.3 Interference on the bus

In this section, we instantiate the functions  $S_i^x(t)$ ,  $A_j^y(t)$ , and  $L_j^y(t)$  that count the number of accesses from the cores and are used as input to the BUS function (see Sect. 5), which we use to derive the maximum bus delay that task  $\tau_i$  on core  $P_x$  can experience during a time interval of length  $t$ :

$$I^{\text{BUS}}(i, x, t) = \text{BUS}(i, x, t) \cdot d_{\text{main}} \tag{33}$$

where  $d_{\text{main}}$  is the bus access latency to the global memory.

We first compute  $S_i^x(t)$ , an upper bound on the total number of bus accesses that can occur due to tasks of priority  $i$  or higher running on core  $P_x$  during an interval of length  $t$ , while one job of task  $\tau_i$  is active, i.e. within its response time. Since lower priority tasks cannot execute on  $P_x$  during the response time of task  $\tau_i$  (a priority level- $i$  processor busy period), the only contribution from those tasks is a single blocking access as discussed in Sect. 5. The maximum number of accesses is computed assuming task  $\tau_i$  is released simultaneously with all higher priority tasks that run on  $P_x$ , and subsequent releases of those tasks occur as soon as possible, while also assuming that the maximum possible number of pre-emptions occur.

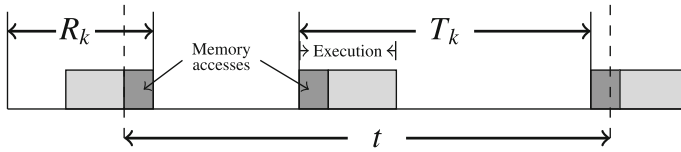
$$S_i^x(t) = \sum_{k \in \Gamma_x \wedge k \in \text{hep}(i)} \left\lceil \frac{t}{T_k} \right\rceil (MD_k + \gamma_{i,k,x}) \quad (34)$$

$MD_k$  denotes the memory demand of task  $\tau_k$  and  $\gamma_{i,k,x}$  accounts for the pre-emption costs on core  $P_x$  due to jobs of task  $\tau_k$ .

In the appendix, we show that in the context of the response time analysis given in this paper, it is correct to compute  $S_i^x(t)$  assuming synchronous release with higher priority tasks on the same core.

Recall that we use  $A_j^y(t)$  to denote an upper bound on the total number of bus accesses due to all tasks of priority  $j$  or higher executing on core  $P_y \neq P_x$  during an interval of length  $t$ . A special case is  $A_n^y(t)$ : since  $\tau_n$  is the lowest priority task, this term includes accesses due to *all* tasks running on core  $P_y$ . In contrast to the derivation of  $S_i^x(t)$ , for  $A_j^y(t)$  we can make no assumptions about the synchronisation or otherwise of tasks on core  $P_y$  with respect to the release of task  $\tau_i$  on core  $P_x$ . The value of  $A_j^y(t)$  is therefore obtained by upper bounding, for each task  $\tau_k$  running on some other core  $P_y$ , the number of memory accesses that it could produce in an interval of length  $t$ , considering only the time constraints on when jobs of that task can execute. The worst-case scenario is illustrated in Fig. 2. The first job of task  $\tau_k$  executes as late as possible, i.e. just prior to its worst-case response time, while the next and subsequent jobs execute as early as possible. Further, we assume that the first job of task  $\tau_k$  has all of its memory accesses in a region as late as possible during its execution, while for subsequent jobs we assume the opposite is true, with execution and a region of memory accesses occurring as early as possible after release of the job. This scenario maximizes the number of memory accesses from task  $\tau_k$  in an interval of length  $t$ , as shown in Fig. 2. This is similar to the concept of carry-in interference used in the analysis of global multiprocessor fixed-priority scheduling (Bertogna and Cirinei 2007; Davis and Burns 2010). Effectively due to local interference from higher priority tasks on its core, the memory accesses of the first job are *carried-in* to the interval of interest leading to increased interference on the bus during the interval.

In the following, the number of memory accesses in each region, shown in dark grey in Fig. 2, is given by  $MD_k + \gamma_{j,k,y}$  and thus the length of each region is  $(MD_k + \gamma_{j,k,y}) \cdot d_{\text{main}}$ . We now upper bound the largest number of memory accesses in an interval of length  $t$  due to task  $\tau_k$  executing on core  $P_k$  along with its cache related pre-emption effects. The next job release of task  $\tau_k$  after the *carried-in* memory accesses (first dark grey region) occurs at a time  $(MD_k + \gamma_{j,k,y}) \cdot d_{\text{main}} + T_k - R_k$  after the start of the



**Fig. 2** Illustration of the carry-in interference analysis

interval of length  $t$ . Subsequent jobs of  $\tau_k$  are then released periodically every  $T_k$ . The number of complete periods (by this we mean from the start of one memory access region to the start of the next one) that contribute memory accesses in the interval of length  $t$  is given by:

$$\begin{aligned}
 N_{j,k}^y(t) &= \left\lfloor \frac{t - ((MD_k + \gamma_{j,k,y}) \cdot d_{\text{main}} + T_k - R_k)}{T_k} \right\rfloor + 1 \\
 &= \left\lfloor \frac{t + R_k - (MD_k + \gamma_{j,k,y}) \cdot d_{\text{main}}}{T_k} \right\rfloor
 \end{aligned}
 \tag{35}$$

The remaining incomplete period in which further memory accesses can occur is therefore of length  $t + R_k - (MD_k + \gamma_{j,k,y}) \cdot d_{\text{main}} - N_{j,k}^y(t) \cdot T_k$ . In this time at most one memory access can occur every  $d_{\text{main}}$ , up to  $MD_k + \gamma_{j,k,y}$  accesses in total. Putting all this together, the total number of accesses possible in an interval of length  $t$  due to task  $\tau_k$  (on core  $P_y$ ) and its cache related pre-emption effects is given by:

$$\begin{aligned}
 W_{j,k}^y(t) &= N_{j,k}^y(t) \cdot (MD_k + \gamma_{j,k,y}) \\
 &+ \min \left( MD_k + \gamma_{j,k,y}, \left\lceil \frac{t + R_k - (MD_k + \gamma_{j,k,y}) \cdot d_{\text{main}} - N_{j,k}^y(t) \cdot T_k}{d_{\text{main}}} \right\rceil \right)
 \end{aligned}
 \tag{36}$$

We note that  $W_{j,k}^y(t)$  is *sustainable* (Baruah and Burns 2006) with respect to a reduction in the number of memory accesses per job, and also to the spreading out of memory accesses within a job. Neither can cause the value of  $W_{j,k}^y(t)$  to increase. This can be seen graphically by considering, in Fig. 2, what happens if the number of memory accesses is reduced i.e. the size of the grey regions is reduced, or if the memory accesses are spread out within the jobs.  $W_{j,k}^y(t)$  is also monotonically non-decreasing with respect to  $t$ .

Using  $W_{j,k}^y(t)$ , we obtain an expression for  $A_j^y(t)$ , an upper bound on the total number of bus accesses due to all tasks of priority  $j$  or higher executing on core  $P_y \neq P_x$  during an interval of length  $t$ , as follows:

$$A_j^y(t) = \sum_{k \in \Gamma_y, \wedge k \in \text{hep}(j)} W_{j,k}^y(t)
 \tag{37}$$

The value of  $L_j^y(t)$  is obtained in a similar way to  $A_j^y$ , but considering accesses with lower priority than  $j$ :

$$L_j^y(t) = \sum_{k \in \Gamma_y \wedge k \in \text{lp}(j)} W_{n,k}^y(t) \quad (38)$$

We note that the carry-in interference was not accounted for in the analysis given by Kim et al. (2014a) (Eqs. (5) and (6) in that paper), resulting in potentially optimistic bounds on the number of competing memory requests.

#### 6.4 Global memory—DRAM

Global memory is usually realized based on dynamic random-access memory (DRAM), which needs to be refreshed periodically. During a refresh, memory accesses cannot be serviced by the DRAM, and hence DRAM refreshes cause interference on tasks. Now, we show how to take into account delays imposed by refreshes. We assume a DRAM controller with a First Come First Served (FCFS) scheduling policy so that memory accesses cannot be reordered within the controller. Further, we assume a closed-page policy to minimize the effect of the memory access history on access latencies. We consider two refresh strategies (Micron Technologies, Inc. 1999): *distributed refresh* where the controller refreshes each row at a different time, at regular intervals, and *burst refresh* where all rows are refreshed immediately one after another.

Under distributed refresh, an upper bound on the maximum number of refreshes within an interval of length  $t$  in which  $m$  memory accesses occur is given by:

$$\text{DRAM}_{\text{dist}}(t, m) = \min \left( m, \left\lceil \frac{t \cdot \# \text{rows}}{T_{\text{refresh}}} \right\rceil \right) \quad (39)$$

where  $\# \text{rows}$  is the number of rows in the DRAM module, and  $T_{\text{refresh}}$  is the interval at which each row needs to be refreshed.  $T_{\text{refresh}}$  is usually 64 ms for DDR2 and DDR3 modules. This formula holds, since at most one memory access can be delayed by each of the refreshes, whereas under burst refresh, a single memory access can be delayed by  $\# \text{rows}$  many refreshes. Under burst refresh, the upper bound is given by:

$$\text{DRAM}_{\text{burst}}(t, m) = \left\lceil \frac{t}{T_{\text{refresh}}} \right\rceil \cdot \# \text{rows} \quad (40)$$

Note that the parameter  $m$  is redundant in (40); however, we keep it to retain the same signature for the function.

As the number of memory accesses within  $t$  is equal to the number of BUS accesses, we can bound the interference due to DRAM refreshes on task  $\tau_i$  on core  $P_x$  as follows:

$$I^{\text{DRAM}}(i, x, t) = \text{DRAM}(t, \text{BUS}(i, x, t)) \cdot d_{\text{refresh}} \quad (41)$$

where  $d_{\text{refresh}}$  is the refresh latency.

### 6.5 Multicore response time analysis

The response time  $R_i$  of task  $\tau_i$  is given by the smallest solution to the following recurrence relation:

$$R_i = PD_i + I^{\text{PROC}}(i, x, R_i) + I^{\text{BUS}}(i, x, R_i) + I^{\text{DRAM}}(i, x, R_i) \quad (42)$$

where  $PD_i$  is the processor demand for task  $\tau_i$  given by (27),  $I^{\text{PROC}}(i, x, R_i)$  is the interference due to processor demand from higher priority tasks running on the same core assuming no misses on the local memory, given by (28),  $I^{\text{BUS}}(i, x, R_i)$  is the delay due to bus accesses from tasks running on all cores and includes  $MD_i$ , given by (33), and  $I^{\text{DRAM}}(i, x, R_i)$  is the delay due to DRAM refreshes, given by (41).

Since the response time of each task can depend on the response times of other tasks via the functions (37) and (38) describing memory accesses  $A_j^y(t)$  and  $L_j^y(t)$ , we use an outer loop around a set of fixed-point iterations to compute the response times of all the tasks, and so deal with the apparent circular dependency. Iteration starts with  $\forall_i: R_i = PD_i + MD_i \cdot d_{\text{main}}$  and ends when all the response times have converged (i.e. no response time changes w.r.t. the previous iteration), or the response time of a task exceeds its deadline in which case that task is unschedulable. See Algorithm 1 for the pseudo-code of the response time calculation. Since the response time  $R_i$  of a task  $\tau_i$  is monotonically increasing w.r.t. increases in the response time of any other task, convergence or exceeding a deadline is guaranteed in a bounded number of iterations.

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#### Algorithm 1 Response Time Calculation

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```

1: function MULTICORERTA
2:    $\forall_i: R_i^0 = 0$ 
3:    $\forall_i: R_i^1 = PD_i + MD_i \cdot d_{\text{main}}$ 
4:    $l = 1$ 
5:   while  $\exists_i: R_i^l \neq R_i^{l-1} \wedge \forall_i: R_i^l \leq D_i$  do
6:     for all  $i$  do
7:        $R_i^{l,0} = R_i^{l-1}$ 
8:        $R_i^{l,1} = R_i^l$ 
9:        $k = 1$ 
10:      while  $R_i^{l,k} \neq R_i^{l,k-1} \wedge R_i^{l,k} \leq D_i$  do
11:         $R_i^{l,k+1} = PD_i + I^{\text{PROC}}(i, x, R_i^{l,k}) + I^{\text{BUS}}(i, x, R_i^{l,k}) + I^{\text{DRAM}}(i, x, R_i^{l,k})$ 
12:         $k = k + 1$ 
13:      end while
14:    end for
15:     $\forall_i: R_i^{l+1} = R_i^{l,k}$ 
16:     $l = l + 1$ 
17:  end while
18:  if  $\forall_i: R_i^l \leq D_i$  then
19:    return schedulable
20:  else
21:    return not schedulable
22:  end if
23: end function

```

---

We note that the analysis is sustainable (Baruah and Burns 2006) with respect to the processor  $PD_j$  and memory demands  $MD_j$  of each task, since values that are smaller than the upper bounds used in the analysis cannot result in a larger response time. This sustainability extends to traces; if any trace of task execution results in practice in a lower processor or memory demand than that considered by the analysis, then this also cannot result in an increase in the response time. Similarly, a decrease in the set of UCBs or ECBs such that they are a subset of those considered by the analysis cannot increase the worst-case response time.

Note that the definitions of  $MD_i$ ,  $PD_i$  and  $ECB_i$  completely decouple the traces from the response time analysis. This comes at the cost of possible pessimism, but strongly reduces the complexity of the analysis. Different traces may maximize different parameters, meaning that the combination of the parameters in this way may represent a synthetic worst-case that cannot occur in practice. An alternative solution is to define a multicore response time analysis that is parametric in the execution traces. In the extreme, completely expanding the analysis to explore every combination of traces from different tasks would be intractable. However, as a first step in this direction, response times could be computed for each individual trace of the task of interest  $\tau_i$ , using combined traces for all other tasks. The maximum such response time would then provide an improved upper bound.

We note that the presented analysis framework is not fine-tuned to specific hardware features or execution scenarios such as burst accesses, since this counteracts its extensibility and generality.

## 7 Extensions to the task model

In the previous section we instantiated the multicore response time analysis (MRTA) framework for a relatively simple task model. In the section, we briefly discuss extensions including: RTOS and interrupts, sharing software resources, and open systems and incremental verification.

### 7.1 RTOS and interrupts

The analysis presented so far only considers tasks and their execution, as represented by traces. We now outline how the MRTA framework can be extended to cover RTOS and interrupt handler behaviour.

We assume that task release is triggered via interrupts from a timer/counter or other interrupt sources. When an interrupt is raised, the appropriate handler is dispatched and may pre-empt the currently executing task.<sup>2</sup> When the interrupt handler returns, then if a higher priority task has been released, the scheduler will run and dispatch that task, otherwise control returns to the previously running task. When a task completes, then the scheduler again runs and chooses the next highest priority task to execute.

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<sup>2</sup> Or interrupt handler if multiple interrupt priority levels are supported.

The behaviour of each interrupt handler is represented by a set of execution traces similar to those for tasks. Thus interrupt handlers can be included in the MRTA framework in a similar way to tasks, but at higher priorities. (We note that there may be some differences if all interrupts share the same interrupt priority level; however due to the wide variety of possible arrangements of interrupt priorities, we do not go into details here). In some cases, interrupt handlers may be prohibited from using the cache, have their own cache partition, or have their code permanently locked into a scratchpad. All of these possibilities can be covered using variants of the analysis described in Sect. 6.

The RTOS is different from interrupt handlers and tasks in that it is not a schedulable entity in itself, rather RTOS code is run as part of each task, typically before and after the actual task code, and interleaved with it in the form of system calls. Similarly with interrupt handlers that release tasks, RTOS code is typically called as the handler returns. With our representation of tasks and interrupt handlers as sets of traces, execution of the RTOS can be fully accounted for by a concatenation of the appropriate sub-traces for the RTOS onto the start and end of the traces for tasks and interrupt handlers.

## 7.2 Sharing software resources

The analysis presented in Sect. 6 assumes that tasks are independent in the sense that they do not share software resources that must be accessed in mutual exclusion, rather the only contention is over hardware resources. We now consider how that restriction can be lifted.

We assume that tasks executing on the same core may share software resources that are accessed in mutual exclusion according to the stack resource protocol (SRP) (Baker 1991). Under SRP, a task  $\tau_i$  may be blocked from executing by at most a single critical section where a task of priority lower than  $i$  locks a resource shared with task  $\tau_i$  or a task of higher priority. Further, under SRP, blocking only occurs before a task starts to execute, thus SRP introduces no extra context switches. We assume a set of traces  $O_i^B$  for all of the critical sections that may block task  $\tau_i$ .

In the MRTA framework, the impact of blocking needs to be considered in terms of both processor and memory demand. This can be achieved by considering the traces  $O_i^B$  as belonging to a single virtual task with higher priority than  $\tau_i$ . Thus we obtain a contribution  $PD_i^B$  to the processor demand which is added into  $I_i(i, x, t)$  and a contribution  $MD_i^B$  to the memory demand which contributes to  $S_i^x(t)$ .

Accounting for the CRPD effects due to blocking are more complex, here we make use of the approach given by Altmeyer et al. (2012) to extend the ECB-Union approach to accounting for pre-emption costs to take account of blocking.

Specifically, we extend the formula for the pre-emption cost (32) to include the UCBs of tasks in the set  $b(i, j)$ , where  $b(i, j)$  is defined as the set of tasks with priorities lower than that of task  $\tau_i$  that lock a resource with a ceiling priority higher than or equal to the priority of task  $\tau_i$  but lower than that of task  $\tau_j$ . These tasks can block task  $\tau_i$ , but can also be pre-empted by task  $\tau_j$ . Hence they need to be included in the set of tasks  $\text{aff}(i, j)$  whose UCBs are considered when determining the pre-emption cost  $\gamma_{i,j,x}$  due to task  $\tau_j$ :



$$\text{aff}(i, j) = (\text{hep}(i) \cap \text{lp}(j)) \cup b(i, j) \quad (43)$$

Tasks in  $b(i, j)$  have lower priorities than task  $\tau_i$  and so cannot pre-empt during the response time of task  $\tau_i$ , hence their ECBs do not need to be considered when computing  $\gamma_{i,j,x}$ . Using (43) extends the ECB-Union approach (32) to correctly account for pre-emption costs when tasks share resources according to the SRP. We note that the simplest form of resource locking, sometimes called *critical sections* has the resource accesses at the highest priority. In that case, there is no additional pre-emption cost, since no tasks can pre-empt the critical sections, and so  $b(i, j)$  is empty.

Blocking due to software resources accessed by tasks on other cores does not affect the term  $A_n^y(t)$  since SRP introduces no additional context switches, and at the lowest priority level  $n$ , there are no extra tasks to include in the CRPD computation ( $b(n, j)$  is empty, since there are no tasks of priority lower than  $n$ ). The value of  $A_j^y(t)$  used in the analysis of a Fixed-Priority bus is also unchanged due to resource accesses, since we assume that the bus access priority reflects only a task's base priority, rather than any raised priority as a result of SRP.

We note that accounting for resources that are shared between tasks on different cores using for example the MSRP (Gai et al. 2001) or MrsP (Burns and Wellings 2013) protocols is beyond the scope of this paper.

### 7.3 Open systems and incremental verification

The basic analysis for the MRTA framework given in the paper assumes that we have information (i.e. traces etc.) for all of the tasks in the system. There are a number of reasons why this may not be the case: (i) the system may be open, with tasks on one or more cores loadable post deployment, (ii) the system may be under development and the tasks on another core not yet known, (iii) incremental verification may be required, so no assumption can be made about the tasks executing on another core, (iv) the system may be mixed criticality and tasks on another core may not be developed to the same criticality level, and hence cannot be assumed to be well behaved. Instead we must assume they may exhibit the worst possible behaviour.

For a core  $P_y$  where we have no information, or need to assume the worst, we may replace  $A_j^y(t)$  and  $A_n^y(t)$  with a function that represents continual generation of memory accesses at the maximum possible rate. In practice, this may be equivalent to simply setting  $A_j^y(t) = A_n^y(t) = \infty$ . We note that analysis for TDMA and Round-Robin bus arbitration still results in bounded response times in this case, while the analysis for FIFO and Fixed-Priority arbitration will result in unbounded response times. With arbitration based on processor priority, then bounded response times can only be obtained if  $P_y$  is a lower priority processor than  $P_x$ . We note that the use of memory throttling mechanisms may result in a bounded number of memory accesses from a core  $P_y$  in any given time interval, independent of the tasks running on that core. Such a bound can be used to define an appropriate interference function  $A_j^y(t)$ .

## 8 Multicore simulator

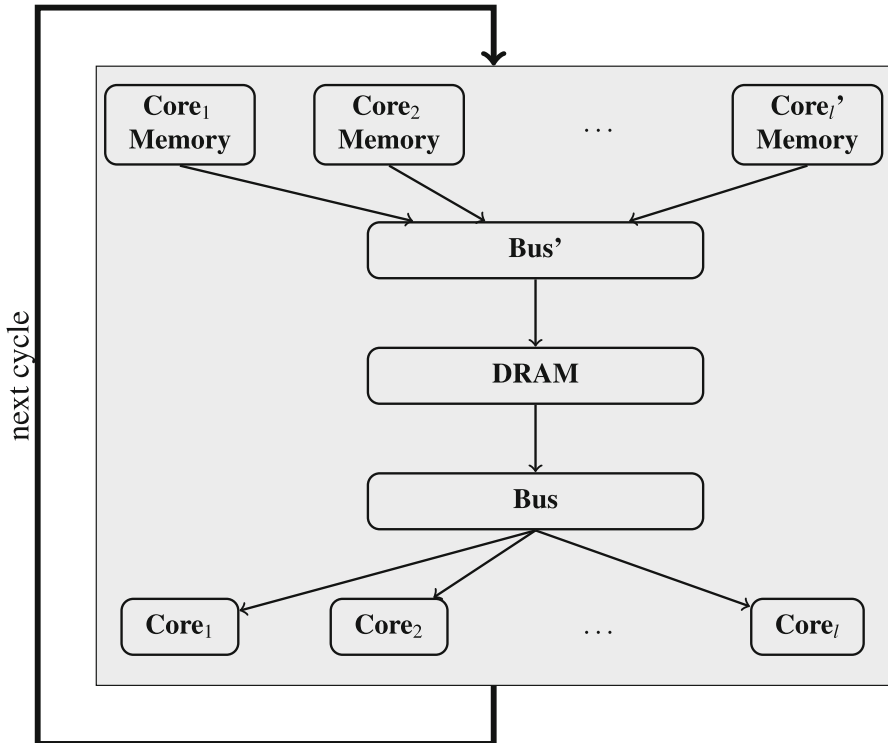
In this section, we present a Discrete Event (DE) multicore simulator that implements the system model presented in Sect. 3. The simulator serves two purposes. Firstly, it validates the soundness of the response time analysis from Sect. 6: all task sets deemed schedulable by the analysis must not incur a deadline miss under simulation. Secondly, it enables us to investigate the precision of the analysis. The precision of timing analyses in general, and in particular timing analyses for multicore systems, is often unknown. Due to the inherent complexity and the large state-space, determining the ground-truth, i.e., a task's worst-case execution time or the exact determination of the schedulability of a task set, is computationally infeasible. Simulation cannot provide precise schedulability results; however, it can be used as a *necessary* test or over-approximation of task set schedulability. It can also provide an under-approximation of the amount, and thus the impact, of the interference on shared resources.

In this paper, we are only concerned with the timing behaviour of the multicore system, so a fully-functional simulation is not needed, hence we do not need to simulate the contents of registers or the precise arithmetic and logic operators of the cores. Therefore, we opted for a so-called transaction-level modelling (TLM) approach, as proposed by (Cai and Gajski 2003). With this approach, the interactions between different components are modelled separately from the computation that is performed by them, and each component can be modelled at a different level of detail and timing accuracy if required. For our simulator, we modelled the complete multicore system in a cycle-accurate way, implementing the exact task and system model assumed by the analysis.

The simulation needs to be capable of detecting any possible deadline miss in a given simulation run, therefore the model includes the detailed timing behaviour of bus arbitration, cache policies, core scheduling and memory accesses, but it abstracts away the individual functional behaviour of the cores (i.e. the computation they do), the bus (i.e. the data it carries) and the memory (i.e. the data it stores). According to Cai and Gajski's TLM taxonomy, this is known as a TLM implementation model.

Hardware, and in particular a multicore system is inherently parallel, whereas a DE simulator executes sequentially. To model the parallelism of the hardware, we follow the simultaneous event handling approach used in most DE simulation languages (Muliadi 1999), assuming that all actions within one cycle happen instantaneously, but ordered by infinitesimally small delays; and that signals also propagate within the same cycle to all receiving components, but ordered from upstream to downstream components. Once all signals have been propagated and processed, the simulator proceeds with the next cycle. To eliminate cyclic dependencies between the hardware components, the behaviour of the cores and the bus are each modeled within two functions, a pre-computation function and a post-computation function. The DRAM function is implemented using a single process. The dependencies of the processes and the process order of the simulator are depicted in Fig. 3.

In the following, we sketch the simulation procedure for a single execution cycle. Each core stores the set of currently active jobs that are ready to execute, and for each of these jobs a trace index. The trace index indicates how much of the trace has already been executed. The execution of a trace, and thus of a job, finishes once the



**Fig. 3** Illustration of hardware dependencies and process order of the multicore simulator

final instruction of the trace is reached. The job is then set to completed. Further, each core has a boolean flag indicating whether or not the core is currently stalled waiting for a memory access to be serviced.

1. The local scheduler on each core is simulated and scheduler events such as job releases or a deadline miss are handled. If the core is not stalled, the execution of the next instruction of the currently active job with the highest priority is simulated. If the execution of this instruction incurs any memory accesses to memory blocks that are not stored in the local memory then a bus request to that memory block is issued and added to a global bus request queue, and the boolean flag is set to stalled. This step is repeated for each core.
2. The simulation proceeds with the bus controller. The bus also features a boolean flag indicating if the bus is busy or idle. If the bus is busy, the simulation immediately proceeds to the next step. If the bus is idle, the next bus access from the access queue is taken and the internal bus counter is set to the global memory latency  $d_{\text{main}}$ . The access which is taken from the queue depends on the bus arbitration policy.
3. The DRAM process counts the number of cycles and served bus accesses until a DRAM refresh is required. When a refresh is needed, the DRAM is stalled for  $d_{\text{refresh}}$  cycles.

4. Next, the simulator executes the bus post-processing, which decrements the bus counter. If the bus counter is equal to zero, a memory request is served and the post-processing for the corresponding core is invoked.
5. The post-processing for the core associated with a served memory request sets the boolean flag of the core from stalled to ready.
6. Goto step 1.

The simulation stops either after a pre-defined number of cycles, or when a deadline miss is detected. In the first case, the task set executed on the multicore system is deemed schedulable, in the second case, it is deemed unschedulable, thus providing a *necessary* test of schedulability.

Note that we assume sporadic task releases. Consequently, no initial release offsets can be assumed and all possible task interleavings are permissible. Due to the large number of release patterns full coverage of all possibilities cannot be achieved. Furthermore, the precision decreases with increasingly dynamic behaviour of the multicore, similarly, increasing the number of cores, tasks, or the size of the cache, increases the size of the state space and hence reduces the proportion of it which can be covered by simulation.

We note that one drawback of our simulator is that it does not account for any overlapping between the execution of processor instructions and memory accesses. Effectively each core always stalls waiting for its memory accesses to be serviced. Overlapping of execution and memory accesses is an area which we aim to explore in future work, both in terms of analysis and simulation.

## 9 Experimental evaluation

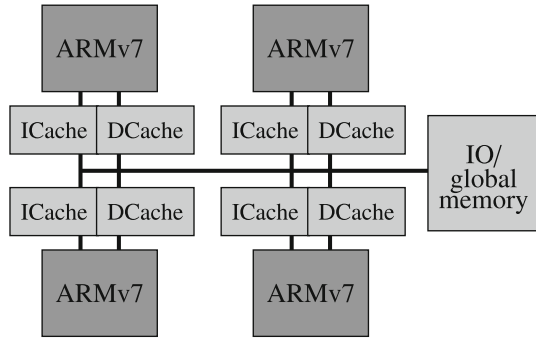
In this section we describe the results of an experimental evaluation using the MRTA framework.<sup>3</sup> We define a reference architecture, which serves as the baseline for the experimental evaluation. In the first set of experiments, we vary the bus architecture, and in the second set of experiments, we vary the type of local memory used. In the third experiment, we compare three distinct multicore architectures: a predictable architecture tailored towards optimizing the guaranteed real-time performance, an architecture that implements full temporal and spatial isolation, and the reference architecture. Finally, we evaluate the precision of the MRTA framework using the multicore simulator presented in Sect. 8.

*Reference Architecture* We model a multicore system based on an ARM Cortex A5 multicore<sup>4</sup> and use this as a reference architecture. As this work is intended to provide an overview of the MRTA framework, we do not model all the details of the specific multicore architecture; however, the ARM Cortex A5 provides the cache configuration, and memory and bus latencies. The reference architecture depicted in Fig. 4 is configured as follows: It has 4 ARMv7 cores connected to the global memory and I/O over a shared bus assuming a Round-Robin arbitration policy and a core

<sup>3</sup> The software is available on demand by contacting the first author.

<sup>4</sup> <http://www.arm.com/products/processors/cortex-a/cortex-a5.php>.

**Fig. 4** Multicore architecture case study:  $m = 4$  cores with local caches connected via a common bus to a global memory



frequency of 200 MHz. Each core has separate instruction and data caches, both direct-mapped with 512 cache sets each and a block size of 32 Bytes. The global memory latency  $d_{\text{main}}$  and the DRAM refresh latency  $d_{\text{refresh}}$  are both 5 cycles. The DRAM refresh period  $T_{\text{refresh}}$  is 64 ms. We assume the DRAM implements the distributed refresh strategy (see Sect. 6.4).

*Trace Generation* For the evaluation, we use the Mälardalen benchmark suite (Gustafsson et al. 2010) to provide traces. The traces for the benchmarks were generated using the gem5 instruction set simulator (Binkert et al. 2011) and contain statically linked library calls. As the benchmark code corresponds to independent tasks, no data is shared between the tasks. Table 2 shows information for all 39 benchmark programs used to provide traces including the total number of instructions (which is equal to the processor demand), the number of read/write operations, the memory demand, and the maximum number of UCBs and ECBs on the reference multicore architecture. Each benchmark is assigned only one trace, which is sufficient due to the simple structure of the benchmark suite: The benchmarks are either single-path by design or the input is provided as part of the benchmark suite. Despite the rather simple structure of the benchmarks, the tasks show a strong variation in processor and memory demand. As all benchmarks exhibit only one trace, the worst-case processor and memory demand coincide. Evaluation for multi-path benchmarks is left for future work, and will require a more realistic set of benchmarks than those currently available. (The Mälardalen benchmark suite contains mostly single-path benchmarks, or benchmarks with little variation between the execution paths).

*Task Set Generation* We evaluated the guaranteed performance of various architectural configurations as computed using the MRTA framework on a large number of randomly generated task sets. The task set parameters were as follows:

- The default task set size was 32, with 8 tasks per core.
- Each task was randomly assigned a trace from Table 2.

**Table 2** Benchmark traces

| Name          | # Instr. (PD) | Read/Write  | MD       | UCB | ECB |
|---------------|---------------|-------------|----------|-----|-----|
| adpcm_dec     | 627, 553      | 123, 641    | 38, 575  | 144 | 332 |
| adpcm_enc     | 628, 795      | 124, 168    | 38, 729  | 155 | 346 |
| binarysearch  | 678           | 293         | 229      | 20  | 118 |
| bsort100      | 272, 715      | 1, 305, 613 | 25, 464  | 31  | 135 |
| bs            | 658           | 201         | 226      | 19  | 117 |
| cnt           | 7765          | 1573        | 573      | 33  | 150 |
| compressdata  | 3166          | 1040        | 494      | 22  | 134 |
| compress      | 8793          | 3358        | 993      | 74  | 174 |
| countnegative | 34, 860       | 7861        | 2240     | 74  | 181 |
| cover         | 3661          | 1495        | 696      | 19  | 231 |
| crc           | 67, 359       | 20, 452     | 6656     | 44  | 162 |
| duff          | 3121          | 1484        | 553      | 24  | 130 |
| edn           | 164, 596      | 73, 857     | 15, 383  | 104 | 306 |
| expint        | 8058          | 2221        | 716      | 27  | 118 |
| fac           | 1096          | 411         | 274      | 17  | 108 |
| fdct          | 5923          | 3098        | 1088     | 67  | 193 |
| fft1          | 92, 289       | 11, 229     | 4766     | 133 | 231 |
| fibcall       | 1194          | 571         | 319      | 19  | 106 |
| fir           | 6938          | 3585        | 1207     | 39  | 140 |
| insertsort    | 2218          | 1317        | 415      | 18  | 121 |
| janne_complex | 1038          | 390         | 254      | 18  | 113 |
| jfdctint      | 7771          | 2987        | 1086     | 63  | 198 |
| lcdnum        | 794           | 326         | 240      | 22  | 116 |
| lms           | 3, 023, 813   | 373, 874    | 120, 821 | 150 | 276 |
| loop3         | 10, 539       | 4412        | 1820     | 16  | 351 |
| ludcmp        | 8278          | 3004        | 768      | 59  | 189 |
| matmult       | 384, 140      | 78, 058     | 11, 923  | 123 | 272 |
| minver        | 16, 256       | 3627        | 1437     | 121 | 284 |
| ndes          | 107, 957      | 50, 632     | 13, 186  | 96  | 252 |
| nsichneu      | 8648          | 4841        | 1582     | 397 | 589 |
| ns            | 25, 494       | 7238        | 1219     | 23  | 186 |
| petrinet      | 2272          | 1206        | 438      | 160 | 250 |
| qsort-exam    | 535           | 219         | 202      | 18  | 109 |
| qurt          | 8663          | 1351        | 735      | 75  | 182 |
| recursion     | 5564          | 1949        | 907      | 19  | 113 |
| select        | 7211          | 2183        | 986      | 58  | 173 |
| sqrt          | 26, 167       | 3185        | 1438     | 62  | 151 |
| statemate     | 62, 188       | 51, 792     | 13, 360  | 117 | 235 |
| st            | 1, 498, 482   | 125, 946    | 31, 969  | 341 | 429 |

- The base WCET per task  $\tau_i$  (needed solely to set the task periods and deadline), was defined as

$$C_i = PD_i + MD_i \cdot d_{\text{main}} + \text{DRAM}(PD_i + MD_i \cdot d_{\text{main}}, MD_i) \cdot d_{\text{refresh}}$$

$C_i$  denotes the execution time of the task without any interference from any other task.

- The task utilizations were generated using UUnifast (Bini and Buttazzo 2005) with an equal utilization assumed for each core.
- Task periods were set based on task utilization and base WCET, i.e.,  $T_i = C_i/U_i$ .
- Task deadlines were implicit.
- Priorities were assigned in deadline monotonic order.
- Tasks were assumed to be independent, i.e. no shared software resources.
- The tasks were assumed to be located in memory sequentially in priority order. (We note that improvements in layout can reduce CRPD (Lunniss et al. 2012); however, such optimisations were not considered here).

The utilization per core was varied from 0.025 to 0.975 in steps of 0.025. For each utilization value, 1000 task sets were generated and the schedulability was determined for each architectural configuration.

We note that the processor utilization is often not the limiting factor on a multicore system, but rather the memory utilization, defined as follows is:

$$U^{\text{BUS}} = \sum_i \frac{MD_i \cdot d_{\text{main}}}{T_i} \quad (44)$$

Note the task set utilization is determined for the reference architecture and we use the same task sets throughout all experiments. Since we adapt the reference architecture and assume varying types of local memories, task set utilizations that are notionally larger than 1 can be deemed schedulable.

## 9.1 Bus arbitration policies

In our first set of experiments, we examine derivatives of the reference architecture assuming the different bus arbitration policies presented in Sect. 5 and also a hypothetical **perfect bus** which eliminates all bus interference if the bus utilization is  $\leq 1$ .

Figure 5 shows the number of schedulable task sets plotted against the core utilization (computed using the base WCETs on the reference architecture) and Fig. 6 against the bus utilization  $U^{\text{BUS}}$ .

Most traces from Table 2 have a high memory demand, which results in a large number of bus accesses even at low core utilizations. Consequently, many task sets are not schedulable even with a perfect bus. The Fixed-Priority bus (green line) where the memory accesses inherit the task priority shows the best performance, followed by Round-Robin (black line) and then TDMA (purple line). Note for TDMA and Round-Robin, we assume a cycle with 2 slots per core.

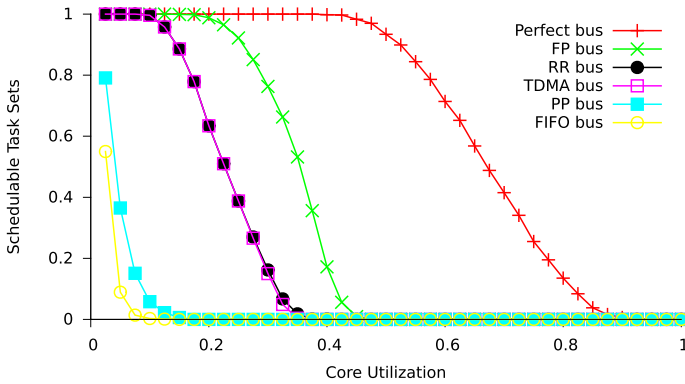


Fig. 5 Number of schedulable task sets versus core utilization: varying bus arbitration policy

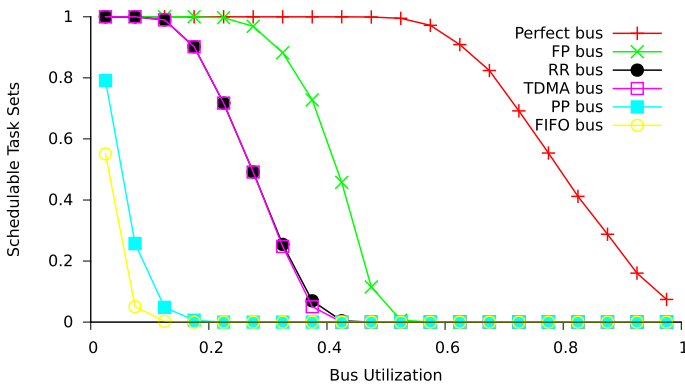
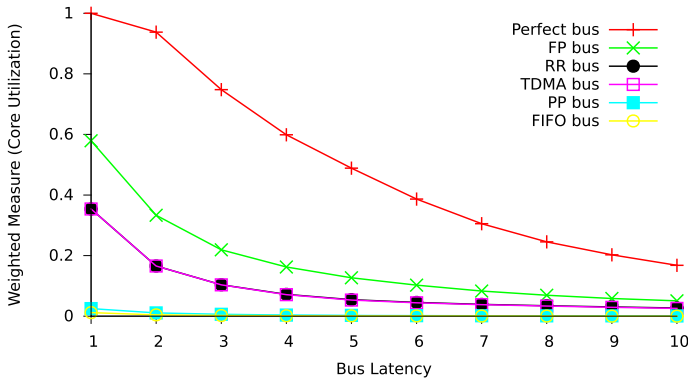


Fig. 6 Number of schedulable task sets versus bus utilization: varying bus arbitration policy

The FIFO bus shows the lowest performance, closely followed by the Processor-Priority bus (PP). The worst-case arrival pattern for a FIFO bus (yellow line) assumes that each potentially co-running task has issued bus requests just before the release of the task of interest, which results in a very pessimistic bus contention and response times. The analysis for the Processor-Priority bus (light blue line) assumes that only accesses due co-running tasks assigned to a core of higher priority cause interference, which explains the improved performance compared to the FIFO bus. We note that the task set generation does not optimize the task assignment with respect to the Processor-Priority bus. Such an optimization could greatly improve the relative performance of this policy by assigning tasks with shorter deadlines to a core with higher priority.

The difference between the Fixed-Priority and Round-Robin/TDMA policies shows the MRTA framework is able to guarantee good real-time performance even if the bus policy does not provide a tightly bounded bus latency for single accesses, as is the case with TDMA and Round-Robin.





**Fig. 7** Weighted schedulability: varying bus latency

### 9.1.1 Weighted schedulability measure

Figures 5 and 6 provide results for different bus policies, showing how guaranteed performance varies with the core and bus utilization. In our second set of experiments, we examine how other parameters including: the main memory latency, the number of cores, and the DRAM refresh latency impact schedulability. We use the weighted schedulability measure (Bastoni et al. 2010)  $W_\phi(p)$  for schedulability test  $\phi$  to show how schedulability varies across a range of values for each of these parameters  $p$ . For each value of  $p$ , this measure combines results for the task sets  $\tau$  generated for all of a set of equally spaced utilization levels (0.025–0.975 in steps of 0.025).

Let  $\Psi_\phi(\tau, p)$  be the binary result (1 or 0) of schedulability test  $\phi$  for a task set  $\tau$  with parameter value  $p$ :

$$W_\phi(p) = \frac{\sum_{\forall \tau} (u(\tau) \cdot \Psi_\phi(\tau, p))}{\sum_{\forall \tau} u(\tau)} \quad (45)$$

where  $u(\tau)$  is the utilization of task set  $\tau$ .

As the memory demand of the benchmark traces is high, the bus latency  $d_{\text{main}}$  has a tremendous impact on overall schedulability (see Fig. 7). The bus latency affects all bus arbitration policies similarly. By increasing the number of cores, the number of tasks also increases, assuming a fixed number of tasks per core, and so does the bus utilization. The performance of all configurations therefore decreases with more cores, as shown in Fig. 8, since fewer task sets are deemed schedulable irrespective of the bus policy used. As might be expected, longer DRAM refresh latencies also have a significant detrimental effect on schedulability for all policies, as shown in Fig. 9.

## 9.2 Local memory types

In our third set of experiments, we examine derivatives of the reference architecture assuming the different types of local memory as presented in Sect. 4, a hypothetical

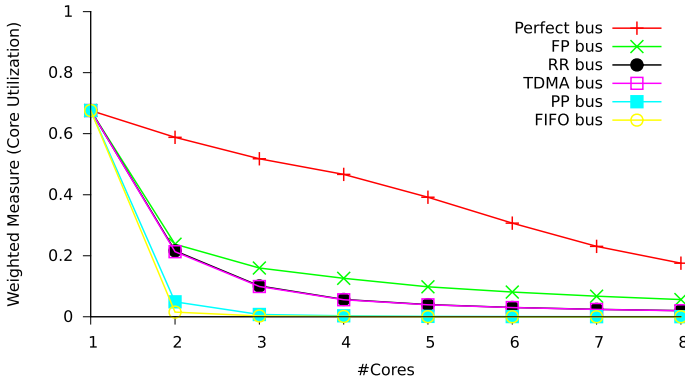


Fig. 8 Weighted schedulability: varying number of cores

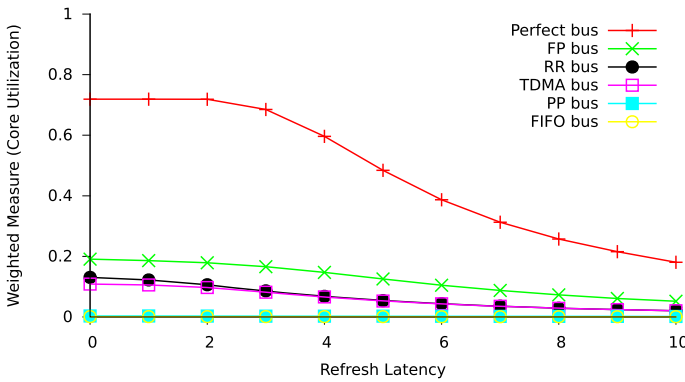
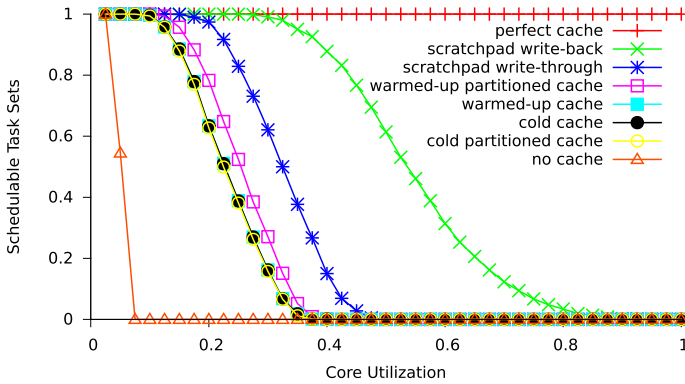


Fig. 9 Weighted schedulability: varying DRAM refresh latency

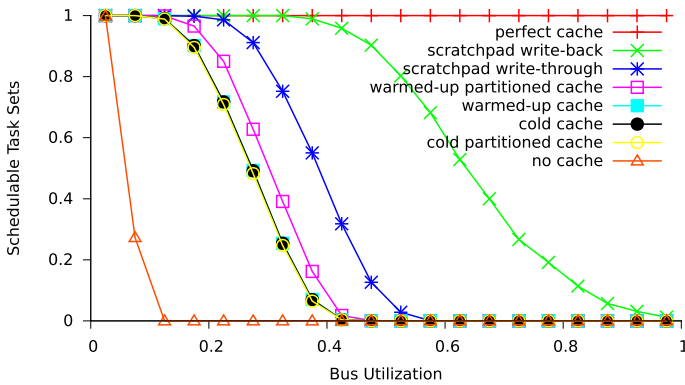
**perfect cache** which eliminates all memory accesses, and a configuration without any caches. Local caches are either partitioned per task, with a uniform partition size, or unconstrained, meaning that all tasks on the same core share the same local cache and can potentially use all of it. The scratchpads are partitioned per task and are configured statically to store the most frequently used memory blocks. We present results for the partitioned and unconstrained cases assuming either a cold cache, or a warmed-up cache where memory blocks have been loaded into the cache by running all tasks once during a warm-up phase (see Sect. 4). Irrespective of the type of local memory, its size remains constant at 16kB.

Figure 10 shows the number of schedulable task sets plotted against the core utilization (computed using the base WCETs on the reference architecture), and Fig. 11 the number of schedulable task sets plotted against the bus utilization  $U^{BUS}$ .

Except for uncached architectures, traditional cache architectures, i.e. both partitioned (yellow line) and unconstrained (black line), exhibit the lowest performance: at a core utilization of 0.275 and a bus utilization of 0.3 less than half of the task sets are schedulable. Accounting for a warm-up phase has an insignificant impact for unconstrained caches (light blue line), and a visible, but still somewhat limited impact on



**Fig. 10** Number of schedulable task sets versus core utilization: varying types of local memory



**Fig. 11** Number of schedulable task sets versus bus utilization: varying types of local memory

partitioned caches (purple line). With 8 tasks per core, the combined set of ECBs often exceeds the cache size, thus the simple analysis accounting for warmed-up caches is not able to guarantee the presence of cache blocks from a previous job of the same task. Like partitioned caches, static scratchpads reduce the size of the available local memory per task. The evaluation shows, however, that the simple policy of storing the  $N$  most frequently used memory blocks in the scratchpad reduces the overall number of bus accesses significantly compared to partitioned caches. The scratchpad architecture with write-back caches (green line) offers the best performance: more than half of all task sets at a core utilization of 0.55 and at a bus utilization of 0.65 are still schedulable. The difference in performance between using a scratchpad with a write-through policy (dark blue line) compared to a write-back policy (green line) shows the substantial impact of write-accesses on the overall system performance.

### 9.2.1 Weighted schedulability measure

Figures 10 and 11 show the results for different types of local memory against the core and bus utilization. Using the weighted schedulability measure defined in (45), we also

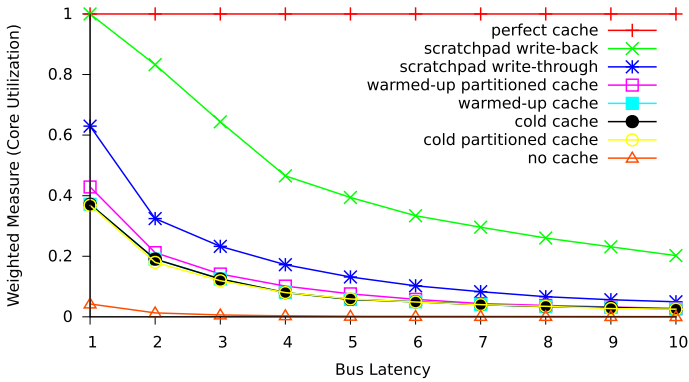


Fig. 12 Weighted schedulability: varying bus latency

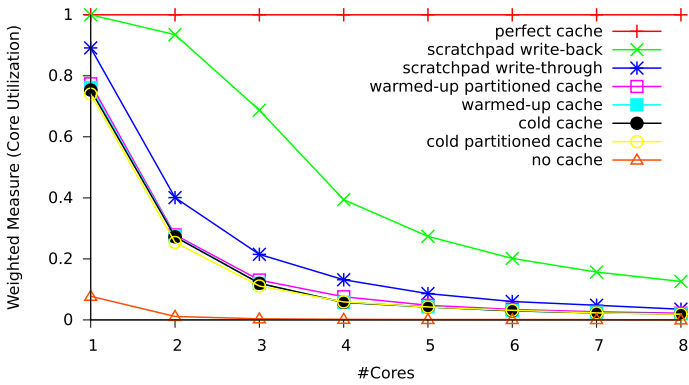


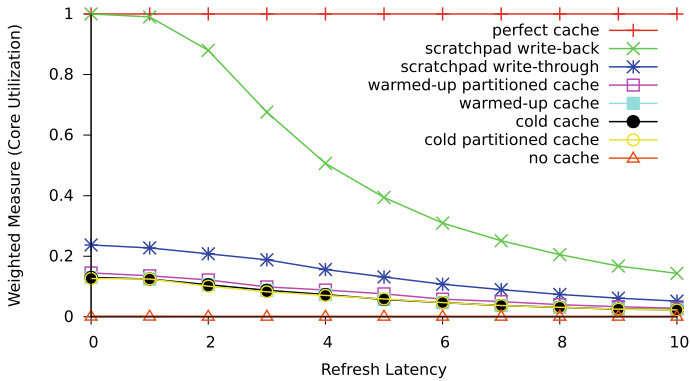
Fig. 13 Weighted schedulability: varying number of cores

examined how the main memory latency (Fig. 12), the number of cores (Fig. 13), and the DRAM refresh latency (Fig. 14) impact schedulability.

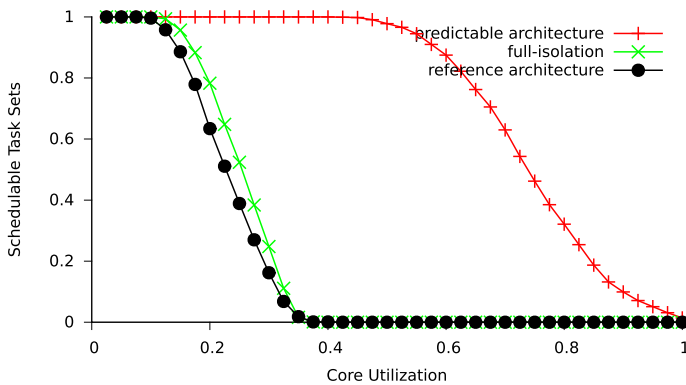
In all these cases, the performance benefit of using scratchpad memory with a write-back policy is clear, retaining its relative advantages as overall schedulability decreases.

### 9.3 Predictable multicore architecture

In our third set of experiments, we compare the reference architecture with two alternatives. The first, referred to as the **full-isolation architecture** is a derivative of the reference architecture that implements complete spatial and temporal isolation. The local caches are partitioned with an equal partition size for each task and the bus uses a TDMA arbitration policy. All other parameters remain the same as for the reference architecture. Performance on the isolation architecture corresponds to the traditional two-step approach to timing verification with context-independent WCETs. In addition, we note that the isolation architecture can be considered as a software



**Fig. 14** Weighted schedulability: varying DRAM refresh latency



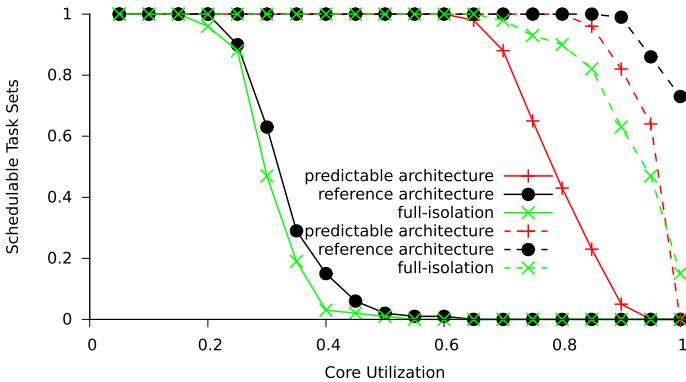
**Fig. 15** Number of schedulable task sets versus core utilization

configuration of the reference architecture. The second alternative, referred to as the **predictable architecture**, has been designed to maximize the guaranteed real-time performance. From the previous evaluation, we found that using scratchpad memory with a write-back policy and a Fixed-Priority bus outperforms all other configurations in terms of guaranteed real-time performance. These components and policies were therefore chosen for the predictable architecture.

Figure 15 shows the number of schedulable task sets plotted against the core utilization (computed using the base WCETs on the reference architecture).

For the reference architecture and the full-isolation architecture, we assumed warmed-up caches as detailed in Sect. 4.

We observe that the predictable architecture, tailored towards guaranteed real-time performance, accumulates the performance benefits of both scratchpads and a Fixed-Priority bus; its performance far exceeds that of the full-isolation architecture, which uses partitioned caches and a TDMA bus, and that of the reference architecture, which uses shared caches and a Round-Robin bus.



**Fig. 16** Number of schedulable task sets versus core utilization: MRTA framework (*solid lines*) and multicore simulator (*dashed lines*)

## 9.4 Precision

Based on our experiments, we were able to identify three main sources of over-approximation (pessimism) in the MRTA framework: The number of memory accesses on the same core cannot be precisely estimated due to imprecision in the pre-emption cost analysis. The interference due to bus accesses may be pessimistic as not all tasks running on another core can simultaneously access the bus. The DRAM refreshes are assumed to occur too frequently if the number of main memory accesses are over-approximated. In this section, we examine the precision of the analysis for the different architectures using the simulator described in Sect 8.

In the previous experiments, we investigated architectures and configurations assuming a total of 32 tasks distributed over 4 cores. Since all tasks are assumed to be sporadic with no relationship between their release times, we cannot reduce the state space of possible scenarios that could be simulated. Consequently, the multicore simulator is only able to cover a negligibly small fraction of the total state space. In order to achieve a meaningful level of coverage, we reduced the number of tasks in the system to 8. The simulation runs for  $10^9$  cycles or until it detects a deadline miss. Further, we use the WCET in isolation on the predictable architecture, instead of on the reference architecture for the task-set generation.<sup>5</sup>

The results are shown in Fig. 16. The dashed lines indicate results from the simulator and solid lines results from the MRTA analysis.

The predictable architecture not only provides the highest level of guaranteed real-time performance, but also the tightest results. Both lines, the solid line for the results of the analysis and the dashed line for results from the simulator are close, which indicates a high precision in the analysis. For the other two architectures, i.e., the reference architecture and the full-isolation architecture, we cannot draw the same conclusion.

<sup>5</sup> We did this since using WCETs based on the reference architecture would mean that the predictable architecture could schedule some task sets with utilization  $>1$  which makes the differences more difficult to comprehend.

In these cases, there are large differences between the lower and upper bounds on the number of schedulable task sets. We note that this could be due to imprecision in the necessary test formed by the simulation, imprecision in the sufficient test given by the MRTA framework, or both.

The reference architecture is optimized towards achieving good average case performance, whereas the predictable architecture is optimized towards guaranteed real-time performance. From the results of the simulation, we observe that the optimization targets may have been achieved. The upper bound on the number of schedulable task sets for the reference architecture is well above the upper bound for the predictable architecture. On the other hand, the predictable architecture provides significantly better guaranteed performance. The results provide an indication that multicore architectures should be tailored towards their intended use.

## 10 Conclusions

In this paper, we introduced the *Multicore Response Time Analysis framework (MRTA)*. This framework is extensible to different multicore architectures, with various types and arrangements of local memory, and different arbitration policies for the common interconnects. In this paper, we instantiated the MRTA framework assuming single level local data and instruction memories (cache or scratchpads), and for a variety of memory bus arbitration policies, including: Round-Robin, FIFO, Fixed-Priority, Processor-Priority, and TDMA.

The MRTA framework decouples response time analysis from a reliance on context-independent WCET values. Instead, the analysis formulates response times directly from the demands on different hardware resources. Such a separation of concerns trades different sources of pessimism. The simplifications used to make the analysis tractable are unable to take advantage of overlaps between processing and memory demands; however, this compromise is set against substantial gains acquired by considering the worst-case behaviour of resources, such as the memory bus, over long durations equating to task response times, rather than summing the worst case over short durations such as a single accesses, as is the case with the traditional two-step approach using context-independent WCETs.

While the initial instantiation of the MRTA framework given in this paper cannot capture every source of interference or delay exhibited in actual multicore processors, it captures the most significant effects. Importantly, the framework can be: (i) extended to incorporate effects due to other hardware resources, and different scheduling/resource access policies, (ii) refined to provide tighter analysis for those elements instantiated in this paper, (iii) tailored to better model the implementation of actual multicore processors.

The MRTA framework provides a general timing verification framework that is parametric in the hardware configuration (common interconnect, local memories, number of cores, etc.) and so can be used at the architectural design stage to compare the guaranteed levels of real-time performance that can be obtained with different hardware configurations, and also during the development and integration stages to verify the timing behaviour of a specific system.

We used the framework to first model, analyse and evaluate the effectiveness of different local memory components (cache and scratchpads) and bus arbitration policies with respect to a reference architecture based on a 4-core ARM Cortex A5. The evaluation utilised software from the Mälardalen benchmark suite as code for the tasks in this case study. These results were then used to compose a predictable architecture using scratchpads with a write-back policy and a Fixed-Priority bus arbitration policy, which was compared against a reference architecture designed for good average-case behaviour, and also a full isolation architecture. This comparison showed that the predictable architecture has substantially better guaranteed real-time performance than either the reference or the full isolation architecture, with the precision of the analysis verified using cycle-accurate simulation.

Our results show that while a full-isolation architecture may be preferable with the traditional two-step approach to timing verification, the MRTA framework can leverage the substantial performance improvements that can be obtained by using dynamic bus arbitration policies and components such as scratchpads designed with worst-case performance in mind.

In future, we aim to extend our work by instantiating the analysis for more complex behaviours and architectures. Examples include: (i) covering processor clusters and multi-level bus/network-on-chip (NoC) arbitration policies. Initial work in this area is reported in (Rihani et al. 2016). (ii) covering processor scheduling policies where analysis of cache-related pre-emption delays already exists, such as fixed-priority scheduling with pre-emption thresholds (Bril et al. 2014, 2017), and EDF (Lunniss et al. 2013). (iii) covering write-back caches, following recent work in this area (Davis et al. 2016; Blass et al. 2017). Further, we aim to evaluate the impact of multi-path benchmarks on the precision of the framework, and explore the optimal selection of a Pareto front of traces. We also aim to integrate the approach with the M/C task model (Melani et al. 2015, 2016) to leverage the improvements in performance that can be obtained by accounting for the overlapping of memory accesses and execution. We would also like to analyse a more complex case study with an application made up of multiple tasks running on different cores, with locally shared software resources and a simple RTOS. Our analysis framework could also be used as a means of optimising the allocation of tasks to cores.

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## Appendix: priority level- $i$ busy periods and the validity of $S_i^x(t)$

In this paper,  $S_i^x(t)$  is used to denote an upper bound on the total number of bus accesses that can occur due to tasks running on core  $P_x$  during the worst-case response time of the task of interest  $\tau_i$ . In this appendix, we show that it is sound to compute  $S_i^x(t)$  assuming that the job of  $\tau_i$  that exhibits the largest upper bound response time (according to our analysis) is released simultaneously with all higher priority tasks on core  $P_x$ , and that these tasks are re-released as soon as possible. This is referred to as a *synchronous arrival sequence*.

In the following, we use the concept of a *busy period* defined with respect to the method used to compute an upper bound response time for task  $\tau_i$ . A priority level- $i$  busy period is defined as an interval of time during which the notional system is busy with activities (processor demand, memory accesses, DRAM refreshes etc.) which are required by the analysis to be finished before a job of task  $\tau_i$  can complete its execution. (In other words, all interference is assumed to be serialised). Let  $\Phi_i(t)$  be the total load in a time interval of length  $t$  that can delay the completion of  $\tau_i$ , including any execution (processor demand) and memory accesses of  $\tau_i$  itself. The system is considered busy with respect to  $\tau_i$  (i.e. a priority level- $i$  busy period) starting at some arbitrary time (for simplicity redefined as time zero) until time  $e$  iff  $\forall t < e \Phi_i(t) > t$ . It follows from this definition that release and completion of any specific job of task  $\tau_i$  must occur within a single priority level- $i$  busy period. Further, since all tasks have constrained deadlines, only at most one job of  $\tau_i$  can execute in a single priority level- $i$  busy period, which ends with the completion of that job. (Note, the next priority level- $i$  busy period may start at the next discrete time instant that follows the completion of the job of  $\tau_i$ ).

We consider contributions to  $\Phi_i(t)$  from two sources (i) external to core  $P_x$  on which  $\tau_i$  executes, (ii) internal to core  $P_x$ .

In case (i), we assume the maximum possible load due to memory accesses that can be generated in an arbitrary interval of length  $t$ . This leads to the definition of  $A_i^y(t)$  given in (37). We do this because for tasks on another core  $P_y$  only their memory accesses can directly impact  $\tau_i$ . Their processor demand does not directly interfere with  $\tau_i$ , but may do so indirectly by delaying memory accesses emanating from tasks on core  $P_y$ .

In case (ii) we assume the maximum possible load due to memory accesses in a specific priority level- $i$  busy period in which a single job of  $\tau_i$  exhibits the worst-case response time for the task. We now show that this worst-case response time occurs assuming a synchronous arrival sequence for tasks executing on the same core. This leads to the definition of  $S_i^x(t)$  given in (34).

1. As  $\tau_i$  is preemptable in terms of its processor demand (execution), some of which can be considered as occurring after all memory accesses and other activities which delay its completion, then since all interference on  $\tau_i$  is considered serialised, there can be no interference emanating from or caused by a previous job of  $\tau_i$  which impacts the job of interest. This is because, due to constrained deadlines, no two jobs of  $\tau_i$  can occur within the same priority level- $i$  busy period.

2. By definition of a priority level- $i$  busy period, there must exist some such busy period and pattern of task releases that results in the job of task  $\tau_i$  in that busy period assuming the worst-case response time for the task. Consider moving the release of the job of  $\tau_i$  back to the start of this busy period. This has no effect on the length of the busy period, or on the completion time of the job, hence its computed response time cannot decrease.
3. For any task  $\tau_k \in hp(i)$  executing on core  $P_x$ , then the computed response time of  $\tau_i$  for the above busy period cannot be decreased by moving the release of each job of  $\tau_k$  as early as possible within the busy period. Further, it cannot be impacted by any release of a job of  $\tau_k$  that takes place prior to the start of the busy period. (This is the case because both the processor demand and memory accesses of  $\tau_k$  interfere with  $\tau_i$  and therefore form part of any priority level- $i$  busy period).

From the three points above, it follows that in the context of our analysis, for fixed-priority preemptive (partitioned) scheduling of tasks with constrained deadlines, the computed worst-case interference (due to both processor demand and memory accesses) from tasks on the same core occurs assuming a synchronous arrival sequence, hence the definition of  $S_i^x(t)$  given in (34).

The difference between  $S_i^x(t)$  and  $A_i^y(t)$  comes from the fact that the total interference, both processor demand and memory accesses, from tasks on the same core is maximised by synchronous arrival; whereas for tasks on a different core (which do not cause direct interference due to their processor demand) it is not.

We note that the contribution of CRPD in  $S_i^x(t)$  is over-approximated similar to existing analysis (2012) by counting each release in the synchronous arrival sequence as a potential pre-emption.

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