The uppermost mantle seismic velocity and viscosity structure of central West Antarctica

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Abstract

Accurately monitoring and predicting the evolution of the West Antarctic Ice Sheet via secular changes in the Earth’s gravity field requires knowledge of the underlying upper mantle viscosity structure. Published seismic models show the West Antarctic lithosphere to be ∼70-100 km thick and underlain by a low velocity zone extending to at least ∼200 km. Mantle viscosity is dependent on factors including temperature, grain size, the hydrogen content of olivine, the presence of partial melt and applied stress. As seismic wave propagation is particularly sensitive to thermal variations, seismic velocity provides a means of gauging mantle temperature. In 2012, a magnitude 5.6 intraplate earthquake in Marie Byrd Land was recorded on an array of POLENET-ANET seismometers deployed across West Antarctica. We modeled the waveforms recorded by six of the seismic stations in order to determine realistic estimates of temperature and lithology for the lithospheric mantle beneath Marie Byrd Land and the central West Antarctic Rift System. Published mantle xenolith and magnetotelluric data provided constraints on grain size and hydrogen content, respectively, for viscosity modeling. Considering tectonically-plausible stresses, we estimate that the viscosity of the lithospheric mantle beneath Marie Byrd Land and the central West Antarctic Rift System ranges from ∼10^{20} - 10^{22} Pa.s. To extend our analysis to the sublithospheric seismic low velocity zone, we used a published shear wave model. We calculated that the velocity reduction observed between the base of the lithosphere (∼4.4-4.7 km/s) and the centre of the low velocity zone (∼4.2-4.3 km/s) beneath West Antarctica could be caused by a 0.1-0.3% melt fraction or a one order of magnitude reduction in grain size. However, the grain size reduction is inconsistent with our viscosity modeling constraints, suggesting that partial melt more feasibly explains the origin of the low velocity zone. Considering plausible asthenospheric stresses, we estimate the viscosity of the seismic low velocity zone beneath West Antarctica to be ∼10^{18} - 10^{19} Pa.s. It has been shown elsewhere that the inclusion of a low viscosity layer of order 10^{19} Pa.s in Fennoscandian models of glacial isostatic adjustment reduces disparities between predicted surface uplift rates and
corresponding field observations. The incorporation of a low viscosity layer reflecting
the seismic low velocity zone in Antarctic glacial isostatic adjustment models might
similarly lessen the misfit with observed uplift rates.

**Key words:** West Antarctica, mantle viscosity, glacial isostatic adjustment, seismic
low-velocity zone, seismology
1 Introduction

Warming Circumpolar Deep Water is eroding ice shelves that buttress the West Antarctic Ice Sheet (WAIS) (e.g., Jacobs et al., 2011). The stability of the WAIS is of particular concern because several large outflow glaciers such as Thwaites and Pine Island are thought susceptible to irrevocable ice loss through marine-ice sheet instability (e.g., Joughin et al., 2014). Satellite gravimetry theoretically offers an efficient means of monitoring WAIS mass change and hence quantifying its predicted contribution to sea level rise. In practice, the superimposed gravitational signal of glacial isostatic adjustment (GIA), the slow flow of the Earth’s ductile mantle toward a new equilibrium following the advance or retreat of a significant surface ice load, must first be removed. The viscosity of the mantle means that the adjustment process can lag the instantaneous elastic response of the crust by hundreds or thousands of years. Thus, accurately modeling the GIA process necessitates knowledge of both the ice sheet history and the rheology of the Earth. Both tasks are challenging in a region with limited geological and geophysical data. These limitations are reflected in the disparities between surface uplift rates predicted by GIA models and corresponding field observations (e.g., Thomas et al., 2011).

Progression from the use of global average 1D radial viscosity profiles in GIA modeling to 3D viscosity models informed by global and continental scale seismic tomography models (e.g., van der Wal et al., 2015) has lessened the misfit. As seismic wave propagation is particularly sensitive to thermal variations, and viscosity to temperature, seismic velocity models can help constrain viscosity structure. Recently developed higher resolution seismic models showing crustal and upper mantle heterogeneity beneath West Antarctica can help in this regard. For example, Heeszel et al. (2016) model the West Antarctic lithosphere as being ∼70-100 km thick and underlain by a low velocity zone extending to at least ∼200 km. Such studies circumvent the relative seismic quiescence of the Antarctic continent by relying on teleseismic surface wave and ambient noise analyses to probe the underlying absolute velocity
structure. However, these techniques lend themselves to the determination of shear wave velocity ($V_S$) structure; compressional wave velocity ($V_P$) information is generally unforthcoming. This is unfortunate because the combination of $V_P$ and $V_S$ data can further inform rock type and the presence of partial melt, both of which influence viscosity. In 2012, a magnitude 5.6 intraplate earthquake in Marie Byrd Land (MBL) was recorded on an array of POLENET-ANET seismometers deployed across West Antarctica (Figure 1). Many of the seismograms recorded a Pnl wave. This is a long-period body wave observable at regional distance representing a superposition of upper mantle head wave (Pn) and partially trapped crustal (PL) energy (e.g., Helmberger & Engen, 1980). In conjunction with the recorded Rayleigh wave, this afforded us the opportunity to probe the $V_P$ and $V_S$ structure of the crust and uppermost mantle across MBL and the central West Antarctic Rift System (WARS).

In addition to temperature and melt, viscosity also depends on factors such as grain size and the hydrogen content of nominally anhydrous minerals (e.g., Hirth & Kohlstedt, 2003) which are not well constrained across West Antarctica and not so readily extractable from seismic velocity measurements. To this end we combined the seismic information obtained from modeling the MBL earthquake waveforms with magnetotelluric, petrological and mineral physics data to infer realistic values for temperature, grain size, hydrogen content and melt fraction in order to estimate realistic viscosity bounds for the West Antarctic lithospheric mantle. As GIA is thought especially sensitive to upper mantle viscosity structure (e.g., Whitehouse et al., 2012), and because our new seismic model does not extend below the lithosphere, we extended our analysis to the sublithospheric mantle using the shear wave model from Heeszel et al. (2016). We estimated an average viscosity for the central West Antarctic sub-lithospheric mantle based on the corresponding average velocity structure inferred by Heeszel et al. (2016). The sublithospheric low velocity layer imaged by Heeszel et al. (2016) beneath much of West Antarctica shares many of the attributes of the global seismic low velocity zone (LVZ) that exists beneath most continental areas (Thybo, 2006, and references therein). The global LVZ is generally attributed to either a small
amount of partial melt (e.g., Anderson & Spetzler, 1970) or solid-state mechanisms which affect the elastic properties of solid peridotite (e.g., Karato & Jung, 1998). We examined the feasibility of these hypotheses to account for the LVZ beneath West Antarctica and compared them in terms of their viscosity implications.
2 Data and Method

The third International Polar Year 2007-2008 motivated the first deployment of broadband seismometer arrays in the interior of the Antarctic continent. In particular, across West Antarctica an array of seismometers was deployed as part of the POLENET-ANET project (www.polenet.org) to probe the structure of the WARS. The instruments deployed were a mixture of cold-rated Guralp CMG-3T (120 s) and Nanometrics T240 (240 s) seismometers sampling at 1 and 40 samples per second (sps). 16 of these recorded the June 1st 2012 M5.6 MBL event, an intraplate extensional earthquake estimated to have occurred at a depth of $\sim 13$ km (Figure 1).

At the given epicentral distances of $\sim 175$ to 1500 km, the first energy to arrive at the POLENET-ANET seismometers was the Pn seismic phase. This is the portion of the seismic energy that transits the majority of the path between the earthquake hypocenter and seismometer as a compressional head wave in the lithospheric mantle. At these distances, the energy transiting entirely within comparatively lower velocity crustal rock arrived later. The precise arrival time of the Pn wave was readily identifiable on the seismograms and allowed us to infer associated travel times using the hypocenter and origin time reported in the Global Centroid-Moment-Tensor (CMT) catalogue. Analysis of the Pn travel times as a function of epicentral distance points to a consistent regional lithospheric mantle $V_P$ of $\sim 7.95$ km/s beneath the WARS and MBL (Figure 2). The Sn wave arrival, by comparison, was not reliably identifiable on the seismograms. To extract additional crustal and lithospheric mantle velocity structure information from the earthquake we compared the observed seismograms with synthetic seismograms calculated using the reflection-matrix reflectivity code \textit{mijkenett} (Randall, 1994) for 1D stratified Earth models excited by the reported CMT focal mechanism.

As a preliminary step in the analysis, instrument responses were deconvolved and the observed 1 sps radial- and vertical-component displacement seismograms were
then bandpass filtered between 80 and 5 s using a standard Butterworth filter. The 5 s cut-off eliminated shorter period content from the seismograms that couldn’t be adequately replicated by simple 1D Earth models. The processed seismograms thus encoded the signature of crustal (including the ice layer) and lithospheric mantle structure. In a final step the seismograms were windowed from several seconds before the Pn arrival to several tens of seconds beyond the end of the Rayleigh wave packet, and the amplitudes normalised to the maximum Rayleigh wave amplitude within the respective windows. Aside from the instrument deconvolution, these same steps were applied to the synthetic displacement seismograms to facilitate comparison.

We sought synthetic seismograms calculated using mijkennett that matched the Pn arrival times and Pnl wave train (if evident) and Rayleigh wave shapes using the statistical concordance coefficient (Lin, 1989) as a metric of wave shape fit. As expected, seismometers located approximately coincident with the earthquake nodal plane recorded little Pnl energy. Conversely, seismometers located off the nodal plane recorded well developed Pnl wave trains. In the former case, fitting the data amounted to matching the Pn phase arrival time and shape of the fundamental mode Rayleigh wave train. In the latter case, the Pnl wave train shape had to be fit in addition. Comparing relative rather than absolute amplitudes made the problem more tractable but precluded us from inferring attenuation values.

For each earthquake-seismometer path the 1D Earth structure was parameterised as an ice layer atop a three-layer crust over a lithospheric mantle half-space (see Table 1). The modeled ice layer thicknesses were allowed to vary in accordance with the BEDMAP2 ice thickness estimates (Fretwell et al., 2013) and the ice $V_P$ from 3.5 - 4.0 km/s with a fixed $V_P/V_S$ ratio of 1.98 (e.g., Kohnen, 1974). Preceding studies infer crust as thin as $\sim$20 km beneath parts of the central WARS and up to $\sim$35 km thick beneath MBL (e.g., Chaput et al., 2014; O’Donnell & Nyblade, 2014; Ramirez et al., 2016). As each earthquake-seismometer path samples both domains to differing degrees (Figure 1), we simply required the modeled total crustal thicknesses
to lie in the range 22-36 km. Single and two layer crustal parameterisations were initially assessed but found to not fit the observed seismograms to the same degree as three layer crusts. A three-layer parameterisation is additionally in accordance with standard models of continental crustal stratification into upper, mid and lower layers (e.g., Christensen & Mooney, 1995). Incorporation of a seismic LVZ underlying the lithospheric mantle did not improve the waveform fits. As expected, the depth sensitivity of the recorded Rayleigh waves did not extend beyond the lithospheric mantle.

The modeled lithospheric mantle $V_P$ was permitted to vary between 7.9 - 8.0 km/s in line with the value estimated from the PnP travel time analysis, while the lithospheric mantle $V_S$ range was guided by shear wave velocities of 4.4 - 4.7 km/s inferred in West Antarctica by Heeszel et al. (2016) using teleseismic Rayleigh wave tomography. For the mid and lower crustal layers, $V_P/V_S$ ratios were allowed vary within the range 1.73 - 1.87 ascribed to continental crust lithologies (e.g., Christensen, 1996). We imposed the additional constraint that the $V_P/V_S$ ratios increase from the mid to lower crust in accordance with the accepted transition to progressively more mafic rock (e.g., Christensen, 1996). By contrast, the upper crustal $V_P/V_S$ ratio was allowed to vary independently and within the broader range 1.55 - 1.90 to account for the possibilities of crystalline felsic upper crust lithologies and/or the presence of thick sediment (e.g., Christensen, 1996). An upper mantle $V_P/V_S$ ratio range of 1.75 - 1.80 was imposed considering published $V_P$, $V_S$ and $V_P/V_S$ values for common upper mantle rocks (e.g., Abers & Hacker, 2016, and references therein).

To account for potential depth-origin time trade-off in the GCMT solution we permitted the reported depth (13.1 km) to vary by ±4 km when generating synthetic seismograms. Otherwise we assumed the reported focal mechanism to be correct. Young et al. (2012) describe the pitfalls of inadvertently mapping erroneous focal information into velocity structure. The fact that we recover velocity structure consistent with seismic models developed independent of this earthquake (Section 3)
lends us confidence that any such inadvertent mapping here is negligible.

It is important to note that we determined vertically-polarised shear wave velocities, $V_{SV}$, by modeling the Rayleigh waves, and not isotropic velocities, $V_S$. Isotropic velocities must be calculated from both vertically- and horizontally-polarised wave velocities, either as a pure or weighted average depending on assumptions about the anisotropy. As vertically-polarised shear wave velocities are generally slower than horizontally-polarised counterparts, the $V_P/V_S$ ratios that we infer (more correctly, $V_P/V_{SV}$ ratios) are systematically larger than corresponding isotropic $V_P/V_S$ ratios, probably by about 2%. This systematic bias is not large enough to affect the conclusions drawn from the models. Layer densities, meanwhile, were calculated from the $V_P$ values using an empirical linear velocity-density relationship (Christensen & Mooney, 1995). However, density variations by themselves were found to have a negligible effect on the seismograms in comparison to velocity variations and are not discussed further.

Subject to these considerations, we used *mijkennett* in conjunction with genetic algorithm code *NSGA-II* (Deb et al., 2002) to search for the 1D stratified velocity models best explaining the seismograms for each earthquake-seismometer path. In each case, 60 1D stratified Earth models satisfying the imposed geologic boundary conditions were generated to serve as an initial population for the search algorithm. We found that evolution through 40 subsequent generations (using crossover and mutation probabilities of 0.9 and 0.05, respectively) was sufficient to arrive at the suite of best solutions according to the concordance coefficient metric of waveform similarity. Evolution beyond this yielded no discernible improvements in waveform fitting.
3 Results

3.1 Seismograms

We present 1D velocity models for six of the earthquake-stations paths that yielded concordance coefficients $>0.8$ for both radial and vertical component seismograms. The paths in question span both the WARS and MBL dome (Figure 1). Figure 3 compares the observed and best fitting synthetic seismograms for these six stations. Station FALL recorded the best-developed Pnl wave train owing to its location with respect to the earthquake epicenter and focal mechanism. Although the Pnl wave train and dominant Rayleigh wave packet are explained reasonably well, the long period energy arriving between 285 - 315 s is poorly fit. It is noteworthy that this portion of the seismogram can be fit if the Pnl constraint is ignored. However, a realistic velocity model should simultaneously explain both the Pnl and Rayleigh wave trains. Thus, we disregard those velocity models which fail to adequately match the Pnl wave train.

Stations WAIS and BYRD also recorded Pnl wave trains, albeit less well-developed than at FALL. In both cases the gross features of the radial and vertical component seismograms are reproduced aside from the higher-frequency oscillations preceding the main Rayleigh wave packet. In contrast, stations DNTW, BEAR and KOLR were located approximately coincident with the nodal plane (see Figure 1) and thus recorded little or no compressional Pnl energy. In these cases, waveform fitting reduces to matching the Rayleigh wave train. In each case the synthetic seismograms re-create the gross features of the recorded seismograms.
3.2 Seismic Velocity Models

Model for paths to stations FALL, WAIS, BYRD and KOLR show lithospheric mantle $V_{SV}$ velocities of $\sim$4.4-4.5 km/s, while those for DNTW and BEAR show $\sim$4.5-4.6 km/s (Figure 4). In each case the lithospheric mantle $V_P/V_{SV}$ values are consistent with published values (e.g., Abers & Hacker, 2016, and references therein). The seismic velocities and $V_P/V_{SV}$ values for the mid and lower crustal layers show some spread but generally similarly cluster about values consistent with continental crust averages (e.g., Christensen, 1996). In contrast, the upper crustal layers exhibit large spreads in $V_P/V_{SV}$ values ($\sim$1.55 - 1.90). This partly reflects the fact that the upper crustal layer velocities parameters were permitted to explore a larger model space than deeper counterparts (Table 1), but also that the shorter period Rayleigh waves (shallow structure) were not fit to the same extent as the longer period Rayleigh waves (deeper structure). This renders the upper crustal layer the least robust part of our velocity models. Consequently we can neither prove nor discount the existence of thick sedimentary layers on the basis of our analysis.

The inferred crustal thicknesses are consistent with the model of relatively thick crust underlying and extending southward from MBL abutting thinner crust characteristic of the WARS (e.g., Chaput et al., 2014). Models for paths predominantly sampling the MBL crustal block (WAIS, BYRD and KOLR) show crustal thicknesses in the range $\sim$29-33 km, while those for FALL ($\sim$26-28 km), DNTW ($\sim$23 km) and BEAR ($\sim$25-27 km) show comparatively thinner crust because significant portions of these paths also sample the WARS. While the path average models cannot be compared directly to seismic receiver function point estimates of crustal thickness, the patterns are nonetheless consistent with receiver function data (Ramirez et al., 2016), thickness maps developed from the joint interpretation of receiver functions and ambient noise (Chaput et al., 2014), and receiver functions and gravity data (O’Donnell & Nyblade, 2014). Given the consistency of our crustal models with other studies, we turn our attention to the uppermost mantle and its viscosity structure.
4 Discussion

4.1 Uppermost Mantle Viscosity

For plastic deformation, the effective viscosity, \( \mu_{\text{eff}} \), characterises the relationship between stress, \( \sigma \), and strain rate, \( \dot{\varepsilon} \), according to:

\[
\dot{\varepsilon} = \mu_{\text{eff}} \sigma
\]  

Subcontinental lithospheric mantle peridotites typically consist of more than 60% volume fraction of olivine, so olivine is commonly regarded as the governing control on upper mantle rheology. Major mechanisms of plastic deformation in olivine are diffusion creep, dislocation creep and dislocation-accommodated grain boundary sliding (DisGBS) (e.g., Hirth & Kohlstedt, 2003; Hansen et al., 2011; Ohuchi et al., 2015). We operate under the assumption that these mechanisms function simultaneously in the upper mantle and that deformation at a point is dominated by the mechanism with the lowest viscosity. For each mechanism, the relationship between stress and strain rate can be formulated as:

\[
\dot{\varepsilon} = A d^{-p} C_{\text{OH}}^{r} \exp\left(\frac{E}{RT}\right) \sigma^{n},
\]

where \( A \) is a pre-exponential factor, \( d \) is grain size, \( p \) is the grain size exponent, \( C_{\text{OH}} \) is water (hydrogen) content, \( r \) is the water exponent, \( E \) is activation enthalpy, \( R \) is the gas constant, \( T \) is absolute temperature and \( n \) is the stress exponent (e.g., Hirth & Kohlstedt, 2003). If the applied stress is known, a combination of laboratory rheological data and geophysical field observations can be used to constrain the values of the various parameters in Equation 2 and thus infer the effective viscosity of the upper mantle.

Lithospheric differential stress magnitudes are generally thought to range from \( \sim 10-100 \) MPa (Ghosh & Holt, 2012). Shear stresses acting at the base of slabless tectonic plates are thought not to exceed 1 MPa (e.g., Bird et al., 2008). In particular, by modeling and iteratively adjusting the stresses acting on each tectonic plate to match
observed plate velocities Bird et al. (2008) suggest that a mean shear stress of 0.1 MPa acts at the base of the Antarctic plate. Meanwhile, a representative stress range up to order 10 MPa associated with ice sheet growth and decay has been suggested by a geodynamic study examining the enhancement of volcanism and geothermal heat flux by ice-age cycling in Greenland (Stevens et al., 2016).

In what follows we combine seismic, magnetotelluric, petrological and mineral physics data to infer plausible temperature, grain size and water content ranges for both the lithospheric mantle and sublithospheric uppermost mantle beneath West Antarctica. The inferred temperature, grain size and water content ranges are then inserted in Equation 2 in order to estimate effective viscosity ranges for the lithospheric mantle and sublithospheric uppermost mantle beneath West Antarctica. Rheological parameters for diffusion creep, dislocation creep and DisGBS regimes in Equation 2 are taken from Hirth & Kohlstedt (2003), Hansen et al. (2011) and Ohuchi et al. (2015) \((p=3, r=0.8, n=1\) for diffusion creep; \(p=0, r=1.2, n=3.5\) for dislocation creep; \(p=1, r=1.25, n=3\) for DisGBS).
4.1.1 The Lithospheric Mantle

Hammond & Humphreys (2000) calculated that seismic $V_P$ and $V_S$ reductions per percent partial melt will be at least 3.6% and 7.9%, respectively, accompanied by a pronounced increase in the $V_P/V_S$ ratio. Recent seismic tomography studies of the broader WARS attributed seismic velocity anomalies to thermal variations within the upper mantle (e.g., Lloyd et al., 2015; Heeszel et al., 2016) without recourse to melt. Furthermore, the lithospheric mantle $V_P/V_{SV}$ ratios obtained in the present study are consistent with typical melt-free lithospheric mantle. We do not discount the fact that pockets of melt may be present in the lithospheric mantle of West Antarctica; numerous active and relict magmatic complexes have been identified (e.g., Lough et al., 2013) and high heat flow measurements have been reported at ice-core drill sites (e.g., 285±80 mW/m$^2$ at Subglacial Lake Whillans; Fisher et al., 2015). However, the seismic data suggest that if melting is occurring in the West Antarctic lithospheric mantle, it is localised rather than pervasive and therefore not a dominant influence on the regional viscosity structure.

Conductive anomalies can likewise be caused by melt or fluids, but the conductivity of melt-free lithospheric mantle is controlled by temperature and the hydrogen content of nominally anhydrous minerals (Selway, 2014). Magnetotelluric data indicate a relatively resistive lithospheric mantle beneath the Byrd Subglacial Basin of the central WARS, which Wannamaker et al. (1996) interpreted as reflecting a dormant state of rifting. According to laboratory experiments on the dependence of the conductivity of olivine on water content at upper mantle conditions (Gardés et al., 2014), the 3000 Ohm m resistivity inferred by Wannamaker et al. (1996) for the lithospheric mantle can be explained by dry olivine. Thus, the survey points not only to an absence of melt and fluid, but to a negligible hydrogen content locally in the uppermost mantle beneath the Byrd Subglacial Basin. However, we will also consider a typical “wet” rheology (100 wt ppm H$_2$O, e.g., Selway, 2014) in case the Byrd Subglacial Basin is not representative of the broader WARS.
Based on data from 60 mineral end-members, Abers & Hacker (2016) provide software for calculating seismic velocities of crustal and mantle rocks at temperature and pressure conditions relevant to the upper few hundreds of kilometers of the Earth. Alternatively, temperature can be inferred at a given pressure if rock composition and seismic velocity are known. A spinel peridotite xenolith suite from Marie Byrd Land described in Handler et al. (2003) serves as a compositional guide to the regional West Antarctic lithospheric mantle. We used Abers & Hacker (2016) to infer a plausible lithospheric mantle temperature range at \( \sim 50 \) km depth by matching predicted and observed \( V_P \) values for similar peridotitic rock compositions at a pressure of 1.5 GPa. The \( V_P \) range inferred in this study, \( \sim 7.9-8.0 \) km/s, translates to a temperature bracket of \( \sim 800-1000^\circ \) C at \( \sim 50 \) km depth. This is in agreement with lithospheric mantle temperatures inferred from xenoliths in other regions which have undergone Phanerozoic tectonism (Artemieva, 2006, and references therein). Handler et al. (2003) report the xenolith textures as ranging from fine to coarse. In the viscosity calculations we vary the grain size from 0.1-10 mm to encompass grain sizes typically observed in lithospheric mantle xenoliths worldwide. Taking these considerations into account, using Equation 2 we calculated the effective viscosity of the lithospheric mantle as a function of temperature, grain size and representative lithospheric stresses of 1, 10 and 100 MPa for both dry (0 wt ppm \( \text{H}_2\text{O} \)) and wet (100 wt ppm \( \text{H}_2\text{O} \)) conditions (Figure 5). For both dry and wet compositions, the effect of grain size reduction on viscosity is most pronounced at small stresses: a grain size reduction of one order of magnitude leads to an approximately two to three orders of magnitude viscosity reduction at 1 MPa, but less than an order of magnitude viscosity reduction at 100 MPa. At all stress levels, dry olivine is, as expected, more viscous than wet olivine. The \( 200^\circ \) C temperature uncertainty translates to a three to five orders of magnitude variation in viscosity. Considering only those solutions giving tectonically plausible strain rates (\( 10^{-16} - 10^{-14} / \) s, e.g. Turcotte & Schubert, 2002), the viscosity of dry lithospheric mantle is \( \sim 10^{21} - 10^{22} \) Pa/s and the viscosity of wet lithospheric mantle is \( \sim 10^{20} - 10^{22} \) Pa/s. This is in good agreement with experimental analysis based on the Oman Ophiolite (Homburg et al., 2010) and global geodynamic
models (e.g., Ghosh & Holt, 2012).
4.1.2 The Sublithospheric Mantle

Because the seismic models developed in this study do not constrain the velocity structure of the sublithospheric mantle, we use the seismic model of Heeszel et al. (2016) to estimate the viscosity of the upper mantle directly beneath the lithosphere. Heeszel et al. (2016) imaged seismically fast lithospheric mantle \( V_{SV} \) velocities with magnitudes consistent with the results of this study extending to 70-100 km depth beneath West Antarctica, underlain by slower \( V_{SV} \) velocities of \( \sim 4.2-4.3 \) km/s extending to depths of at least 180 km. This represents a \( V_S \) reduction in the range \( \sim 2-9\% \). Heeszel et al. (2016) interpret the slow shear wave velocities as representing thermally perturbed mantle from Mesozoic through Cenozoic extension in the WARS. Lloyd et al. (2015) similarly interpret relative reductions in \( V_P \) and \( V_S \) velocities beneath the Bentley Subglacial Trench of the central WARS as reflecting a thermal anomaly consistent with Neogene extension. Both studies attribute seismic velocity reductions beneath MBL to an upper mantle thermal anomaly conceivably related to a putative mantle plume.

The seismic velocity and thickness (70-100 km) of the lithosphere inferred by our work and Heeszel et al. (2016) indicate little broad-scale modification of the uppermost mantle from Cenozoic tectonism. In addition, the low velocity layer imaged by Heeszel et al. (2016) in the sublithospheric mantle beneath much of West Antarctica, on average, shares many of the attributes of the global seismic low velocity zone (Thybo, 2006, and references therein). In what follows we investigate the rheological implications of the average velocity structure of the central West Antarctic sublithospheric mantle. In doing so we neglect localised velocity variations rooted in Cenozoic tectonism (e.g., Lloyd et al., 2015) that will play an important role in 3D viscosity analyses.

Although still a matter of debate, the origin of the LVZ is generally attributed to either a small amount of partial melt (e.g., Anderson & Spetzler, 1970) or solid-state
mechanisms which affect the elastic properties of solid peridotite (e.g., Karato & Jung, 1998). Chantel et al. (2016) suggest that 0.1 to 0.3% melt fractions are consistent with seismic, electrical conductivity and petrological observations, and that partial melt is a viable physical origin for the LVZ. Models of solid-state mechanisms such as grain size evolution successfully replicate many of the observed seismic signatures of the upper mantle (e.g., Behn et al., 2009). However, in contrast to melt, solid-state explanations generally struggle to explain the sharp velocity drop at the top of the LVZ (e.g., Stixrude & Lithgow-Bertelloni, 2005). Elastically accommodated grain-boundary sliding (EAGBS; Raj & Ashby, 1971) causes a frequency, temperature, and grain-size dependent peak in seismic attenuation and may be a solid-state candidate capable of producing the observed sharp gradient in velocity (e.g., Karato, 2012). In what follows, we examine the implications of the partial melt and EAGBS hypotheses for the viscosity of the LVZ beneath West Antarctica.

We estimate the temperature difference between the lithosphere and the LVZ by assuming a mantle potential temperature of $\sim$1300-1450°C (e.g., O’Reilly & Griffin, 2010) and an upper mantle adiabat of 0.4-0.5°C/km (Katsura et al., 2010). Taking 85 km as a reasonable average lithospheric thickness for West Antarctica (Heeszel et al., 2016), these values translate to temperature estimates of $\sim$1340-1490°C at the lithosphere-asthenosphere boundary (LAB) and $\sim$1360-1515°C at a depth of 125 km in the center of the LVZ.
Partial melting of dry peridotite will only begin to occur at \( \sim 1570^\circ \text{C} \) at 125 km depth (\( \sim 4 \text{ GPa} \)) (Hirschmann et al., 2009). However, asthenospheric peridotite is likely to contain 100-500 ppm hydrogen, which would lower its solidus in the LVZ to a temperature below the geotherm (e.g., Hirschmann et al., 2009; Ardia et al., 2012, and references therein) and produce melt fractions of the order of 0.1-0.3% (Hirschmann et al., 2009). A melt fraction of this magnitude would cause the \( V_S \) velocity reduction (\( \sim 4.4-4.7 \text{ km/s} \) to \( \sim 4.2-4.3 \text{ km/s} \)) observed in the LVZ below West Antarctica (Chantel et al., 2016).

Figure 6 shows the hydrogen content necessary to generate melt at our calculated range of LVZ temperatures at 125 km depth (1360, 1435 and 1515\(^\circ \text{C} \)). At 1360\(^\circ \text{C} \), melting will not initiate unless the peridotite contains at least \( \sim 490 \text{ ppm} \) hydrogen and a melt fraction of 0.1-0.3% will not be generated unless the hydrogen content reaches \( \sim 580-800 \text{ ppm} \). These hydrogen contents approach and exceed the estimated peridotite hydrogen storage capacity at this depth (e.g., Ardia et al., 2012). At the higher estimated temperatures of 1435 and 1515\(^\circ \text{C} \), physically plausible hydrogen contents of \( \sim 285 \text{ ppm} \) and \( \sim 115 \text{ ppm} \) will initiate melting while melt fractions of 0.1-0.3% will be generated for hydrogen contents of \( \sim 340-470 \text{ ppm} \) and \( \sim 140-190 \text{ ppm} \), respectively.
Velocity reduction due to EAGBS

Since grain size affects both viscosity and seismic velocity, we considered whether grain size reduction could be a solid-state cause for the LVZ. We used the experimental results summarised in Jackson et al. (2014) to calculate the predicted change in shear wave velocity due to EAGBS between 85 km depth (at the base of the lithosphere; \( \sim1340-1490^\circ C \)) and 125 km depth (in the center of the LVZ; \( \sim1360-1515^\circ C \)) for grain sizes between 0.1 and 10 mm. Figure 7 shows that while EAGBS is unlikely to account for the seismic observations if grain size does not vary between these depths, a reduction in grain size of one order of magnitude can produce a velocity decrease that matches the seismic observations.
Viscosity implications of the partial melt and EAGBS LVZ hypotheses

For small melt fractions, $\phi$, several constitutive equations relating the viscosity of partially-molten rock, $\mu(\phi)$, to its melt-free counterpart, $\mu_0$, have been proposed. Experimentalists suggest that viscosity decreases exponentially with increasing melt fraction according to:

$$\mu(\phi) = e^{-\alpha\phi} \mu_0,$$

where $\alpha \approx 26$ for diffusion creep and $\alpha \approx 31$ for dislocation creep (e.g., Hirth & Kohlstedt, 2003). Meanwhile, Takei & Holtzman (2009) derived a theoretical formulation:

$$\mu(\phi) = 0.2(1 - A\phi^{1/2})^2 \mu_0,$$

where $A = 2.3$ is a semi-empirically determined constant, while Holtzman (2016) developed a parameterisation for very small ($<< 1\%$) melt fractions:

$$\mu(\phi) = e^{\phi - (\alpha\phi + \ln x_{\phi_c} \text{erf}(\phi/\phi_c))} \mu_0,$$

where $x_{\phi_c}$ is the viscosity reduction factor at the critical melt fraction, $\phi_c$, and $\alpha \approx 26$. According to the experimental formulation of Equation 3, melt fractions of 0.1-0.3% will reduce the viscosity of partially-molten rock relative to the melt-free counterpart by a factor of $\sim 1.02-1.09$. For the same melt fractions, the theoretical formulations of Equations 4 and 5 (taking $x_{\phi_c} = 120$ and $\phi_c = 10^{-5}$ as suggested for peridotite) result in viscosity reduction factors of $\sim 5.8-6.5$ and $\sim 123-130$, respectively.

Using Equation 2 we calculated the effective viscosity of the LVZ beneath West Antarctica for anhydrous and water-saturated peridotite as a function of temperature, grain size and stress (Figure 8). We then used Equations 3, 4 and 5 to calculate the viscosity for a melt fraction of 0.1% for the respective viscosity-melt formulations (Figure 9). The applied stress range of 0.1-10 MPa considered encompasses the superposition of an assumed mean basal shear stress of 0.1 MPa (Bird et al., 2008) and a representative stress range associated with ice sheet growth and decay (up to 10 MPa; Stevens et al., 2016). Several broad trends are apparent from Figures 8 and 9. The
effect of grain size reduction on viscosity is very large for small stresses but becomes
negligible at large stresses. This is due to the transition from the grain-size sensitive
diffusion creep regime at low stresses towards the grain-size insensitive dislocation
creep regime at higher stresses. Our 150°C temperature uncertainty has a larger ap-
parent effect on the viscosity of anhydrous peridotite compared to water-saturated
or partially molten peridotites. However, temperature has secondary impacts on
viscosity for wet conditions, particularly in that it controls the amount of hydrogen
required to saturate and melt peridotite. At all stress levels, the anhydrous peridotite
has the highest viscosity, while the calculated reduction in viscosity due to partial
melt depends on the constitutive equation used.

We constrain our set of solutions by considering only those giving plausible as-
thenospheric strain rates (10^{-16} – 10^{-14} /s, e.g. Turcotte & Schubert, 2002). For
stresses of 0.1 to 10 MPa, these strain rates translate to viscosities ranging from
\sim 10^{18} – 10^{20} MPa. Within our modelled range of compositions and stresses, these
viscosities are only realisable for a grain size of 10 mm and a stress of 0.1 MPa (Figures
8 and 9). The 0.1 MPa stress level suggests that asthenospheric stresses associated
with GIA are of the same order of magnitude as stresses acting on the base of the
Antarctic plate due to mantle convection (~0.1 MPa; Bird et al., 2008).

Figure 7 showed that a grain size reduction of one order of magnitude from the
base of the lithosphere would be necessary for EAGBS to explain the LVZ. Given
that we can only model plausible LVZ strain rates for grain sizes equal to (or larger
than) lithospheric mantle counterparts (Figure 5), our analysis does not support
grain size reduction as a means of explaining the LVZ. For West Antarctica, the 0.1
to 0.3% melt fractions that viably explain the LVZ seismically translate to a viscosity
of \sim 10^{18} – 10^{19} Pa s for a 10 mm grain size at 0.1 MPa according to the formulation
of Takei & Holtzman (2009) (Equation 4), a 0.1% melt fraction gives a viscosity of
\sim 10^{18} Pa s for a 10 mm grain size and stress of 0.1 MPa at 1360°C. However, we
have previously commented that the hydrogen content required to generate such a melt fraction at this temperature approaches the estimated peridotite hydrogen storage capacity for the estimated depth (e.g., Ardia et al., 2012). The formulation of Holtzman (2016) (Equation 5), meanwhile, results in implausibly low strain rates for all considered scenarios. Within the limitations of our analysis, this suggests that the partial melt hypothesis for the origin of the seismic LVZ is feasible only if the associated viscosity reduction is of the magnitude suggested by the formulations of Hirth & Kohlstedt (2003), and perhaps Takei & Holtzman (2009). Taking these considerations into account, the viscosity of $\sim 10^{18} - 10^{19}$ Pa s inferred for plausible strain rates is in broad agreement with van der Wal et al. (2015) who determined that West Antarctic uppermost mantle viscosities may in places be less than $10^{19}$ Pa s. In comparison, the volume-averaged viscosity of the upper mantle is thought to be of order $10^{20}$ Pa s (e.g., Kaufmann & Lambeck, 2002).

Much of what we know about GIA and mantle viscosity comes from studies of Fennoscandia and North America. In fact, the comparative paucity of Antarctic data means that Antarctic GIA models are typically calibrated against northern hemisphere data sets (e.g., van der Wal et al., 2015). Fennoscandia and much of North America are shield regions: the lithosphere is thick, cold, buoyant and stable. West Antarctica, by comparison, is an amalgamation of several terranes that have witnessed significant tectonic deformation and re-organisation since the breakup of Gondwana. The upper mantle velocity structure, and hence anticipated thermal and viscosity structure, of the respective regions is markedly different.

Fjeldskaar (1994) argued that Fennoscandian GIA models including a low viscosity asthenospheric layer of order $10^{19}$ Pa s better explain observed surface uplift rates than models lacking this layer. The incorporation of a low viscosity layer ($\sim 10^{18} - 10^{19}$ Pa s) reflecting the seismic LVZ in Antarctic GIA models might similarly improve the fit to surface observables used to validate the GIA models. However, care should be taken if Antarctic GIA models including a sublithospheric low viscosity layer models are
calibrated against northern hemisphere data sets: the LVZ beneath shield regions is considerably thinner than it is beneath actively deforming regions (Thybo, 2006).
Surface Heat Flow

Another crucial factor influencing ice sheet behaviour, the average heat flow at the ice sheet base, can similarly be estimated from seismic models. Based on a compilation of global data, Artemieva (2006) suggests that a correlation between depth to the upper mantle high-conductivity layer, $Z_{HCL}$, (interpreted as electrically conductive asthenosphere) and surface heat flow, $Q$, can be approximated as:

$$Z_{HCL} = 418 \times e^{-0.023 Q} \quad (6)$$

While acknowledging that seismic and electrical lithospheres need not coincide, a lithospheric thickness range of 70-100 km in Equation 6 translates to a surface heat flow of $\sim$62 - 78 mW/m$^2$. Such a range may better represent the average heat flow of West Antarctica than locally elevated measurements such as 285±80 mW/m$^2$ inferred at Subglacial Lake Whillans (Fisher et al., 2015). Heeszel et al. (2016) and Ramirez et al. (2016) draw similar conclusions from their seismic analyses.
5 Conclusion

Accurately estimating the upper mantle viscosity structure of West Antarctica is a critical aspect of the monitoring and prediction of West Antarctic Ice Sheet evolution by satellite gravimetry. As both seismic wave propagation and viscosity are particularly sensitive to thermal variations, seismic data can provide useful constraints on mantle viscosity. We utilised seismograms from the 2012, magnitude 5.6, intraplate earthquake in Marie Byrd Land to obtain $V_P$ and $V_S$ data for West Antarctica. While thermal variations can be estimated from $V_S$ (or $V_P$) alone, the additional $V_P/V_S$ information informs rock type and the presence of partial melt, both of which influence viscosity. We used a genetic algorithm to converge on a population of path-average crustal and uppermost mantle velocity models best explaining the observed seismograms at six POLENET-ANET stations. Inferred crustal thicknesses are consistent with the concept of relatively thick crust underlying and extending southward from MBL abutting thinner crust characteristic of the WARS. Models for paths predominantly sampling the MBL crustal block (WAIS, BYRD and KOLR) show crustal thicknesses in the range $\sim$29-33 km, while those for FALL ($\sim$26-28 km), DNTW ($\sim$23 km) and BEAR ($\sim$25-27 km) show comparatively thinner crust because significant portions of these paths also sample the WARS. $V_P/V_S$ values for the mid and lower crustal layers generally cluster about values consistent with continental crust averages. The inferred uppermost mantle seismic velocities are consistent with melt-free peridotite. We combined the seismic information with petrological and magnetotelluric data to examine the rheology of the West Antarctic lithospheric mantle. For realistic differential stresses of 1-100 MPa and tectonically plausible strain rates of $10^{-16} - 10^{-14}$/$s$, the lithospheric mantle viscosity ranges from $\sim 10^{20} - 10^{22}$ Pa.s. Furthermore, if the West Antarctic lithosphere is 70-100 km thick as suggested by Heeszel et al. (2016), a correlation between depth to the asthenosphere and surface heat flow postulated by Artemieva (2006) suggests that $\sim 62 - 78$ mW/m$^2$ may represent the average surface heat flow of West Antarctica.
To extend our analysis to the sublithospheric mantle, we used the shear wave model from Heeszel et al. (2016). We calculated that the velocity reduction observed between the base of the lithosphere and the centre of the LVZ beneath West Antarctica could be caused by a 0.1-0.3% melt fraction (Chantel et al., 2016) or a one order of magnitude reduction in grain size (Jackson et al., 2014). For plausible asthenospheric stresses of 0.1-10 MPa and strain rates of $10^{-16} - 10^{-14}/s$, the viscosity of the LVZ is $\sim 10^{18} - 10^{20}$ Pa s. Fjeldskaar (1994) showed that the incorporation of a low viscosity asthenospheric layer of order $10^{19}$ Pa s in Fennoscandian GIA models improved matches to surface observations. Notably our inferred viscosities are only realisable for a grain size of 10 mm and a stress of 0.1 MPa.

Our results have important implications for the stress level of the asthenosphere and the cause of the LVZ. Estimates for realistic asthenospheric strain rates can only be replicated for low stresses (<1 MPa). This implies that, if these estimates are valid for asthenosphere affected by GIA, asthenospheric stresses associated with GIA are of the same order of magnitude as stresses acting on the base of the Antarctic plate due to mantle convection. These asthenospheric strain rates can also only be replicated for coarse grain sizes (~10 mm). This implies that the seismic velocity decrease observed in the LVZ cannot be caused by a solid state mechanism (EAGBS) responding to a grain-size reduction in this zone, suggesting that partial melt is more likely responsible for the LVZ. That said, we argue that the partial melt hypothesis is only valid if the viscosity reduction associated with a 0.1-0.3% melt fraction is relatively modest, in line with the formulations of Hirth & Kohlstedt (2003) and, under certain conditions, Takei & Holtzman (2009). Formulations which infer larger viscosity reductions (e.g., Holtzman, 2016) give implausibly low strain rates for the conditions considered. Interestingly, the vast majority of our models for reasonable sublithospheric compositions, grain-sizes and stresses (Figure 7) produce viscosities significantly lower than those generally predicted from GIA studies (e.g., Kaufmann & Lambeck, 2002). Figure 8 demonstrates the large influence hydrogen exerts on sublithospheric mantle viscosity. If the initiation of partial melting leads to a decrease
in peridotite hydrogen content below its water-saturated level, it is conceivable that partial melting could result in an actual increase in viscosity. Since most of the modelled compositions have viscosities too low to match the observations, a LVZ with a small degree of partial melt and an associated decrease in peridotite hydrogen content will broaden the range of parameters that can reconcile the seismic, viscosity, grain size and stress constraints.
6 Acknowledgements

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References


Figures and Tables
Figure 1: Map showing the locations of POLENET-ANET stations (pink circles) that recorded the 2012 magnitude 5.6 intraplate Marie Byrd Land (MBL) earthquake. The hypocenter and origin time information is from the Global Centroid-Moment-Tensor catalogue. Full waveform modeling of seismograms from the labelled stations were used to infer crustal and upper mantle velocity information for MBL and the West Antarctic Rift System (WARS).
Figure 2: Travel time of the Pn seismic phase from the MBL earthquake to POLENET stations (black circles) as a function of epicentral distance. Linear regression yields an average Pn velocity of $\sim$7.95 km/s.
Figure 3: Observed and modeled radial and vertical component seismograms. Station labels are in the upper-right hand corner of each window. The Pn phase, long-period Pnl body-wave and Rayleigh wave (R1) are labelled for station FALL.
Figure 4: The best generation 1D stratified Earth velocity models ($V_P$, $V_S$, and $V_P/V_S$) for each of the earthquake-stations paths. Station labels are in the lower-left hand corner of each window.
Figure 5: The effective viscosity of the West Antarctic lithospheric mantle as a function of stress, temperature and grain size for both “dry” (0 wt ppm H$_2$O) and “wet” (100 wt ppm H$_2$O) conditions. We used Abers & Hacker (2016) to infer a plausible lithospheric mantle temperature range at $\sim$50 km depth by matching predicted and observed $V_P$ values for peridotitic rock compositions at a pressure of 1.5 GPa. The inferred $V_P$ range ($\sim$7.9-8.0 km/s) translates to a temperature range of $\sim$800-1000°C at $\sim$50 km depth. Grain size is varied from 0.1-10 mm to encompass grain sizes typically observed in lithospheric mantle xenoliths worldwide. The viscosities were calculated using Equation 2 for representative lithospheric stresses of 1, 10 and 100 MPa at a pressure of 1.5 GPa. Rheological parameters for diffusion creep, dislocation creep and DisGBS regimes taken from Hirth & Kohlstedt (2003), Hansen et al. (2011) and Ohuchi et al. (2015) ($p=3$, $r=0.8$, $n=1$ for diffusion creep; $p=0$, $r=1.2$, $n=3.5$ for dislocation creep; $p=1$, $r=1.25$, $n=3$ for DisGBS). Stars represent solutions giving tectonically plausible strain rates between $10^{-16}$ and $10^{-14}$/s.
Figure 6: Peridotite solidus and melt fraction as a function of hydrogen content for representative LVZ temperatures of 1360, 1435 and 1515°C at 125 km (~4 GPa). The shaded regions encompass melt fractions of 0.1-0.3%, a range thought consistent with geophysical observations that attribute the origin of the LVZ to the presence of partial melt.
Figure 7: Predicted reduction in shear wave velocity due to the solid-state EAGBS mechanism between 85 km depth (at the base of the lithosphere) and 125 km depth (at the centre of the LVZ) for representative temperature and grain size conditions. If grain size does not change from the lithosphere to the LVZ, EAGBS is unlikely to account for the sharp reduction in observed seismic velocities. However, a grain size reduction of one order of magnitude from the lithosphere to the LVZ can easily produce a velocity decrease replicating the observations.
Figure 8: The effective viscosity of the seismic LVZ of West Antarctica as a function of stress, temperature, grain size and hydrogen content for anhydrous and water-saturated peridotite. Taking 85 km as a reasonable average lithospheric thickness for West Antarctica (Heeszel et al., 2016), an assumed mantle potential temperature of $\sim$1300-1450°C (e.g., O’Reilly & Griffin, 2010) and upper mantle adiabat of 0.4-0.5°C/km (Katsura et al., 2010) translate to a temperature range of $\sim$1360-1515°C at a depth of 125 km in the center of the LVZ. $\sim$490, 285 and 115 ppm hydrogen are required to lower the peridotite solidus to representative temperatures of 1360, 1435 and 1515°C, respectively. Grain size is varied from 0.1-10 mm. The viscosities were calculated using Equation 2 for representative stresses of 0.1, 1 and 10 MPa at a pressure of 4.0 GPa. Rheological parameters for diffusion creep, dislocation creep and DisGBS regimes taken from Hirth & Kohlstedt (2003), Hansen et al. (2011) and Ohuchi et al. (2015) ($p=3$, $r=0.8$, $n=1$ for diffusion creep; $p=0$, $r=1.2$, $n=3.5$ for dislocation creep; $p=1$, $r=1.25$, $n=3$ for DisGBS). Stars represent solutions giving tectonically plausible strain rates between $10^{-16}$ and $10^{-14}$/s. Viscosities are calculated for a pressure of 4 GPa. The additional effect of partial melt on viscosity is shown in Figure 9.
Figure 9: The effective viscosity of the seismic LVZ of West Antarctica as a function of stress, temperature, grain size and hydrogen content for a melt fraction of 0.1%. Solutions are shown for three formulations that quantify the viscosity reduction due to partial melt: Hirth & Kohlstedt (2003), Takei & Holtzman (2009), and Holtzman (2016). Stars represent those solutions giving tectonically plausible strain rates between $10^{-16}$ and $10^{-14}$/s. Viscosities are calculated for a pressure of 4 GPa.
Table 1: Layer thickness (km), $V_P$ (km/s), $V_S$ (km/s) and $V_P/V_S$ ratio constraints that the velocity models had to meet in order to be considered geologically plausible. The constraints are in accordance with the published studies outlined in Section 2.

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