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**Discrete Choice Experiments:  
A Guide to Model Specification, Estimation and Software**

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**Abstract**

We provide a user guide on the analysis of data (including best-worst and best-best data) generated from discrete choice experiments (DCEs), comprising a theoretical review of the main choice models followed by practical advice on estimation and post estimation. We also provide a review of standard software. In providing this guide we endeavor not only to provide guidance on choice modeling, but to do so in a way that provides a 'way in' for researchers to the practicalities of data analysis. We argue that choice of modeling approach depends on: the research questions; study design and constraints in terms of quality/quantity of data and that decisions made in relation to analysis of choice data are often interdependent rather than sequential. Given the core theory and estimation of choice models is common across settings, we expect the theoretical and practical content of this paper to be useful not only to researchers within but also beyond health economics.

**Compliance with Ethical Standards**

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## **Key Points for Decision Makers**

- We provide a user guide on the analysis of data, including best-worst and best-best data, generated from DCEs, addressing the questions of 'what can be done in the analysis of DCE data' and 'how to do it'.
- We provide a theoretical overview of the main choice models and review three standard statistical software packages: Stata; Nlogit; and Biogeme.
- Choice of modeling approach depends on the research questions; study design and constraints in terms of quality/quantity of data and decisions made in relation to analysis of choice data are often interdependent rather than sequential.
- A health based DCE example for which we provide the data and estimation code is used throughout to demonstrate the data set up, variable coding, various model estimation and post estimation approaches.

## 1. Introduction

Despite researchers having access to ever-expanding sources and amounts of data, gaps remain in what existing data can provide to answer important questions in health economics. Discrete choice experiments (DCEs) [1] are currently in demand because they provide opportunities to answer a range of research questions, some of which cannot otherwise be satisfactorily answered. In particular, they can provide: insight into preferences (e.g., to inform clinical and policy decisions and improve adherence with clinical/public health programs or to understand the behaviour of key agents in the health sector such as the health workforce, patients, policy makers etc.); quantification of the tradeoffs individuals are prepared to make between different aspects of health care (e.g., benefit-risk tradeoffs); monetary and non-monetary valuation (e.g., valuing healthcare and/or health outcomes for use in both cost-benefit and cost-utility analysis and priority setting more generally); and demand forecasts (e.g., forecasting uptake of new treatments to assist in planning appropriate levels of provision).

DCEs are a stated preference method which involve the generation and analysis of choice data. Usually implemented in surveys, respondents are presented with several choice sets, each containing a number of alternatives between which respondents are asked to choose. Each alternative is described by its attributes and each attribute takes one of several levels which describe ranges over which the attributes vary.

Existing reviews [2, 3] document the popularity and growth of such methods in health economics while others [4-6] provide guidance on how to use such methods in general. Given the detailed research investment needed to generate stated preference data via DCEs, not surprisingly, more detailed user guides on specific components of undertaking a DCE have also been developed, including the use of qualitative methods in DCEs [7], experimental design [8] and external validity [9]. A natural next large component of undertaking and interpreting DCEs to be addressed is guidance on the analysis of DCE data. This topic has recently received some attention; Hauber et al (2016) [10] provide a useful review of a number of statistical models for use with DCE data. We go beyond that work in both scope and depth in this paper, covering not only model specification which is the focus of the Hauber et al paper, (and within model specification we cover more ground), but also estimation, post estimation and software.

We provide an overview of the key considerations that are common to data collected in DCEs and the implications these have in determining the appropriate modeling approach before presenting an overview of the various models applicable to data generated from standard first-best DCEs as well as for models applicable to data generated via best-worst and best-best DCEs. We discuss the fact that the parameter estimates from choice models are typically not of intrinsic interest (and why that is) and instead encourage researchers to undertake post estimation analysis derived from the estimation results to both improve interpretation and to produce measures that are relevant to policy and practice. Such additional analysis includes predicted uptake or demand, marginal rates of substitution, elasticities and welfare analysis. Coupled with this theoretical overview we discuss how such models can be estimated and provide an overview of statistical software packages that can be used in such estimation. In doing so we cover important practical considerations such

as how to set up the data for analysis, coding and other estimation issues. We also provide information on cutting edge approaches and references for further detail.

Of course, there are many steps involved in generating discrete choice data prior to their analysis including reviews of the relevant literature and qualitative work to generate the appropriate choice context and attributes and levels, survey design and, importantly, experimental design used to generate the alternatives between which respondents are asked to make choices and of course piloting and data collection. As noted, many of these 'front end' steps have received attention in the literature and we do not discuss those topics here. Instead, we take as the starting point the question of how best to analyse the data generated from DCEs. Having said that, it is important to note that model specification and experimental design are intimately linked, not least because the types of models that can be estimated are determined by the experimental design. That means the analysis of DCE data is undertaken within the constraints of the identification and statistical properties embedded in the experimental design used to generate the choice data. For that reason, consideration of the types of models one is interested in estimating (and the content of this current paper) is important prior to creating the experimental design for a given DCE.

In providing this guide we endeavor not only to provide guidance on choice modeling, but to do so in a way that provides a 'way in' for researchers to the practicalities of data analysis. To this end we refer throughout to and demonstrate the data set up, variable coding, various model estimation and post estimation approaches using a health based DCE example by Ghijben et al., (2014) [11] for which we provide the data and Stata estimation code in supplementary appendices. This resource adds an additional dimension which complements the guidance provided in this paper by providing a practical example to help elucidate the points made in the paper and can also be used as a general template for researchers when they come to estimate models from their own DCEs.

As such, the two main components of the paper are 'what can be done in the analysis of DCE data' and 'how to do it'. Given many (but not all) considerations in the analysis of DCE data are common across contexts in which choice data may be collected, we envisage the content of this paper being relevant to DCE researchers within and outside of health economics.

## **2. Choice models**

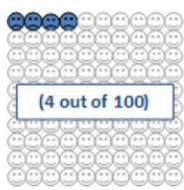
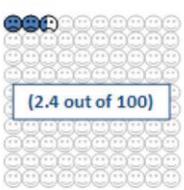
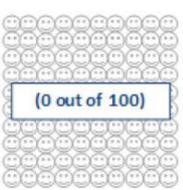
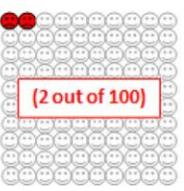
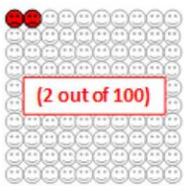
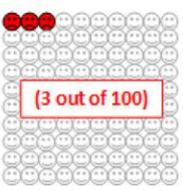
### **2.1 Introduction**

Continual reference to the case study provided by Ghijben et al. (2014)[11] allows us to provide insights behind some of the modelling decisions made in that paper as well being able to make the associated data available as supplementary material to enable replication of all results produced in the current paper; some but not all of which appear in Ghijben et al. (2014). This carefully chosen example is broadly representative of the type of studies found in health economics and enables us to illustrate a relatively wide range of features of DCEs. Naturally one example cannot provide an exhaustive coverage of issues likely to be faced by practitioners and when appropriate, reference will be made to other applied work

that supply templates for aspects that fall outside the scope of our case study.

Ghijben et al. (2014) [10] were motivated by the growing public health problem associated with atrial fibrillation and concerns of under treatment. The study aimed to examine patient preferences for warfarin and new anticoagulants and motivated a decision problem where individuals faced with atrial fibrillation and an elevated risk of stroke needed to decide upon alternative treatments. These considerations motivated the development of the final choice task, an example of which is presented in Figure 1. Sequences of such tasks were presented to respondents and forms an integral part of the data collection. Again we emphasize that getting to the stage of having a data set amenable to analysis is a significant part of conducting a DCE and should not be underestimated. But this is not our focus and interested readers should consult [8, 12, 13] for details on the important topics of experimental and survey design.

Your doctor tells you that your current risk of stroke is 4% and risk of bleed is 2%. Suppose you have the following options:

	No treatment	Drug A	Drug B
Risk of stroke	 (4 out of 100)	 (2.4 out of 100)	 (0 out of 100)
Risk of bleed	 (2 out of 100)	 (2 out of 100)	 (3 out of 100)
Antidote available	N/A	<u>No</u> antidote	<u>Yes</u> antidote
Monthly blood test	N/A	<u>No</u> monthly blood tests	<u>Yes</u> monthly blood tests
Dose frequency	N/A	<u>Once</u> a day dosing	<u>Twice</u> a day dosing
Interactions likely	N/A	<u>No</u> interactions likely	<u>Yes</u> interactions likely
Cost per month	\$0 per month	<u>\$0</u> per month	<u>\$10</u> per month

Which would you choose?  No treatment  Drug A  Drug B

From the remaining two options, which would you choose?  No treatment  Drug A  Drug B

Figure 1: Example of a discrete choice experiment choice set (Ghijben et al. (2014))

It is useful to first introduce some terminology and to discuss a number of key features that are common to data collected in DCEs. In broad terms the features are:

- A. *Discrete choices*: On each choice occasion, respondents face a choice set containing two or more discrete and mutually exclusive alternatives. Respondents are then required to answer one or more questions reflecting their evaluation of these alternatives. In Figure 1, respondents are required to first choose their most preferred alternative amongst the choice set of three options. They are then asked a follow-up question requiring them to choose the better of the two options remaining after their initial choice which delivers a complete ranking of the three alternatives. Including just the first question is possibly the most common way to generate choice outcomes and our discussion will focus on this case. However, the second type of question is an example that falls under the rubric of best-worst scaling that is becoming increasingly popular because of the extra preference information provided at low marginal cost; [14, 15].
- B. *Choice sets*: Choice sets contain two or more alternatives<sup>1</sup>. The choice set in our case study contains three alternatives, two referring to hypothetical drugs and one being a no-treatment option. Variants of such a structure include a status quo option so the investigator is determining which hypothetical alternatives would be attractive enough to make respondents switch from what they currently use; see [16, 17] for examples<sup>2</sup>.

Where no-choice is a realistic alternative but it is not provided as part of the choice set, the situation is referred to as a forced choice problem. Including no-choice or status quo options usually adds realism to the choice task and is especially relevant in forecasting exercises and welfare analysis.

The two hypothetical alternatives in Figure 1 are fully described by their attributes and the drugs are denoted by generic titles, Drug A and Drug B. They are said to be unlabelled alternatives. Sometimes it is more appropriate to provide a descriptive name for the hypothetical alternatives. For example, the choice set could include warfarin and a new oral anticoagulant such as dabigatran and the alternatives are now said to be labelled.

- C. *Alternatives defined by attributes*: Alternatives are defined by a set of attributes that are individually assessed by consumers in coming to an evaluation of the product as a whole [17]. The levels of the attributes are varied over choice occasions as part of the experimental design. Thus the structure of these variables that figure prominently in subsequent analysis are under the control of the analyst. A good experimental design is one that ensures that they deliver the best possible estimates and so problems prominent with revealed preference data, such as limited variation in key variables and multicollinearity, can be avoided in DCEs. It is true though that this comes with added responsibility on the part of analysts. For example, if there are interaction effects between attributes that are theoretically relevant then it is necessary for the design to ensure that such effects are in fact

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<sup>1</sup> This can include presenting a single profile and asking respondents to accept or reject it.

<sup>2</sup> In our case study the status quo is no treatment but more generally status quo and no treatment need not coincide.

identified.

- D. *Repeated measures*: The data have a panel structure with the same respondent providing multiple outcomes for a sequence of different choice occasions or scenarios. While asking respondents to answer more than one choice task is an economical way of gathering more information it is clear that extra observations from the same respondent do not represent independent information. As in our case study there are also examples where multiple outcomes are available for each scenario.
- E. *Respondent characteristics*: In a section of the survey instrument separate from the choice scenarios, personal characteristics of respondents are routinely collected. Different respondents may value different alternatives and attributes in different ways and so trying to capture these sources of preference heterogeneity with observable characteristics will typically form part of the analysis plan. In our case study the medical history of respondents including any history of atrial fibrillation is potentially very relevant. While personal characteristics and relevant health history are natural inclusions, there is scope to collect and use less standard characteristics such as attitudinal variables [18-20].
- F. *Context*: Choices depend on the environment or context in which they are made [21]. In designing a DCE, the choice context plays a major role in making the hypothetical choice realistic. Context can also be manipulated as part of the experimental design by defining different contexts in which the choice is to be made and then allocating respondents to these context treatments and by including context variables as attributes. For example, our case study could be extended by allocating respondents to treatments that differed in the form or amount of information they were provided on atrial fibrillation or by including attributes of the cardiologist that respondents visited.

Apart from providing an overview of typical DCE data and introducing some terminology, this initial discussion is important because several features of these data will eventually impact model specification.

## 2.2 Standard discrete choice models

It is natural to start with the classical multinomial logit (MNL) and its link to the random utility model established by McFadden (1974, 2001) [22, 23]. This provides an opportunity to introduce most of the key specification and estimation issues and represents the baseline for most extensions to more sophisticated models and for research on the theoretical underpinnings of decision-making in choice problems.

Assume the utility that respondent  $i$  derives from choosing alternative  $j$  in choice scenario  $s$  is given by

$$(1) U_{isj} = V_{isj} + \varepsilon_{isj}; i = 1, \dots, N; s = 1, \dots, S; j = 1, \dots, J;$$

where there are  $N$  decision-makers choosing amongst  $J$  alternatives across  $S$  scenarios.

$V_{isj}$  represents the systematic or predictable component of the overall utility of choosing alternative  $j$  and  $\varepsilon_{isj}$  is the stochastic disturbance term representing characteristics unobservable by the analyst. We have data on the discrete choice  $y_{is} = j$  which is then linked to the associated utilities by assuming the individual decision-maker chooses alternative  $j$  if it delivers the highest utility in comparison with the utility associated with all other alternatives in the choice set. Thus we model the probability of choosing alternative  $j$  as:

$$(2) P_{isj} = Prob(y_{is} = j) = Prob(U_{isj} - U_{isl} > 0) \forall l \neq j.$$

(1) and (2) imply that the overall scale of utility is irrelevant in that multiplying both  $V_{isj}$  and  $\varepsilon_{isj}$  by a positive constant yields a different utility level but does not change the resultant choice. Consequently the scale of utility needs to be normalized which is equivalent to normalizing the variance of  $\varepsilon_{isj}$ .

Econometric analysis proceeds within this framework by making a number of assumptions and specification decisions. First consider the distribution of the stochastic disturbance terms. Under the assumption that these are independently and identically distributed Type-I extreme value, the probability of choosing  $j$  takes the familiar MNL form:

$$(3) P_{isj} = \frac{\exp(\lambda V_{isj})}{\sum_{l=1}^J \exp(\lambda V_{isl})}$$

where  $\lambda$  is the scale parameter (inverse of the standard deviation of the disturbance). We will return to a further discussion of scale but in a standard MNL model  $\lambda$  cannot be separately identified and by convention is set to unity. Such normalizations should be familiar to anyone with knowledge of basic binary choice models such as logit and probit.

For modelling purposes there is no compelling reason to prefer this specification for the disturbance distribution in preference to say normality that leads to a multinomial probit model. Historically the preference for MNL arose because of the availability of a closed form solution for the probabilities as in (3) which leads to considerable computational advantages over multinomial probit where such representations of probabilities are not available. While computational considerations are today less of an issue, as we will see later, more complicated estimation problems can still benefit from having a MNL model as its base.

Turning to the specification of  $V_{isj}$  as an initial starting point one might consider a linear specification:

$$(4) V_{isj} = \alpha_j + A'_{isj}\delta + Z'_i\gamma_j$$

where  $A_{isj}$  is a vector of attributes describing alternative  $j$ ,  $Z_i$  is a vector of characteristics of the individual decision-maker and  $\alpha_j, \delta, \gamma_j$  are parameters to be estimated. Note the different sources of variation in the covariates. The attributes by design will typically vary over individuals, scenarios and alternatives while personal characteristics will only vary over individuals and will be constant over scenarios and alternatives. According to (2) only

differences in utilities matter and so another generic specification issue is that characteristics of the individual have an impact on choice only to the extent that their associated parameters vary over alternatives, specified here as  $\gamma_j$ . Similarly, the alternative specific constants,  $\alpha_j$ , are specified to vary over alternatives. As there are  $J - 1$  differences in utilities it is also necessary to apply at least one normalization to the alternative specific constants and the parameters for the individual characteristics. This can be accommodated in a number of ways but typically one alternative is set as the base and the associated parameters are normalized to zero. Because attributes do vary over alternatives, it is possible to estimate associated effects or preference weights that are not alternative specific. One could allow  $\delta$  to vary over alternatives but it is not necessary for the purposes of estimation.

Some discussions make a distinction between models of multinomial outcomes based on the structure of the regressors calling a model with alternative-specific regressors a conditional logit model, one with case-specific regressors a MNL model and where there is a mixture of alternative-specific and case-specific regressors as we have specified in (4) some authors call this a mixed model. They are essentially the same model and so such distinctions can lead to confusion. Thus we simply call the model given by (1)-(4) a MNL specification[24].

One way to interpret (4) is that the alternative specific constants vary by respondent characteristics. Faced with a choice between the same alternatives, different individuals make different choices that can be predicted by differences in their observable characteristics. A natural extension to (4) also allows attribute weights to vary with respondent characteristics. Such heterogeneity can be captured by including interactions between attributes and individual characteristics. Decisions about these specification choices will depend on the subject matter of the particular problem and the research questions being considered.

As various models are introduced, we will supply associated estimation results produced using Stata and collect these in Table 1. Section 3 provides a comparison of estimates using alternative packages and more detail on estimation issues. The first column of results are for MNL, where we have used the first-best data and Model B of Table 5 in [10] as the particular specification.

There are three alternatives,  $j = N, A, B$ , corresponding to no treatment and Drugs A and B. The no treatment choice parameters are normalized to zero;  $\alpha_N = 0$ ,  $\gamma_N = 0$ . These constraints are necessary for identification. Ghijben et al. (2014) [10] impose two further constraints, neither of which is necessary for the purposes of identification but both are sensible in this case. The first constraint,  $\alpha_A = \alpha_B$ , implies a single “treatment” alternative specific constant. Because the hypothetical alternatives are unlabelled, we would expect any preference for one drug over the other to be attributed solely to differences in attributes. In other words, if A and B were described by the same attribute levels, respondents would be expected to be indifferent between them. Conversely, in the case of labelled alternatives it would not be prudent to impose such constraints. In such applications, alternative specific constants would be capturing effects attributable to the label or brand over and above those captured by the attributes and hence these would be

expected to differ across alternatives. Ghijben et al. (2014) [10] also imposed the constraint  $\gamma_A = \gamma_B$ . Once  $\gamma_N = 0$  has been imposed, this second constraint is not necessary. It would be possible to specify alternative specific attribute effects, for example, preferences over risk could differ depending on the treatment option, but specifying generic attribute effects is appropriate with these data.

In Table 1, the block effect, which is a dummy variable to control for which version of the survey the respondent answered, is written as an interaction with the treatment alternative specific constant as are the personal characteristics in Model C of Table 5 [10] (an exception is age which is interacted with the risk attribute). This is operationally equivalent to allowing the associated parameters to vary between treatment and no treatment and depending on the options available in the software this may be how the data needs to be constructed for estimation to be undertaken. (These and other estimation issues are addressed in Section 3.)

**Table 1: Estimates of standard discrete choice models using data from Ghijben et al. (2014)\***

	MNL	MXL	SH	G-MNL	ROL	MROL
	Estimate (std.err.)	Estimate (std.err.)	Estimate (std.err.)	Estimate (std.err.)	Estimate (std.err.)	Estimate (std.err.)
Stroke risk	0.698 (0.080)	0.774 (0.088)	0.886 (0.165)	0.867 (0.117)	0.503 (0.058)	0.705 (0.076)
Bleed risk	0.684 (0.080)	0.742 (0.094)	0.790 (0.135)	0.816 (0.120)	0.572 (0.066)	0.767 (0.088)
Antidote	0.066 (0.116)	0.137 (0.133)	0.108 (0.192)	0.137 (0.147)	0.149 (0.121)	0.228 (0.146)
Blood test	-0.079 (0.075)	-0.088 (0.081)	-0.107 (0.099)	-0.120 (0.092)	-0.052 (0.059)	-0.038 (0.079)
Dose frequency	-0.064 (0.061)	-0.079 (0.065)	-0.132 (0.096)	-0.107 (0.078)	-0.014 (0.051)	-0.019 (0.067)
Drug/food interactions	-0.267 (0.083)	-0.314 (0.091)	-0.319 (0.097)	-0.338 (0.090)	-0.280 (0.078)	-0.385 (0.099)
Cost	-0.010 (0.001)	-0.011 (0.002)	-0.009 (0.002)	-0.011 (0.002)	-0.011 (0.001)	-0.014 (0.002)
Bleed risk* antidote	-0.337 (0.081)	-0.321 (0.094)	-0.320 (0.105)	-0.327 (0.100)	-0.213 (0.060)	-0.273 (0.077)
ASC *block	-0.589 (0.518)	-0.655 (1.533)	-0.810 (0.825)	-1.513 (0.575)	-0.216 (0.335)	-0.327 (0.656)
ASC (mean)	0.926 (0.404)	2.767 (0.966)	1.824 (0.738)	3.201 (0.538)	1.043 (0.233)	1.514 (0.431)
ASC (SD)		3.052 (0.948)		3.178 (0.332)		2.438 (0.246)
$\tau$			0.961 (0.240)	-0.388 (0.109)		
Log-likelihood	-944.3	-786.1	-884.7	-781.8	-1713.2	-1377.9

\* ROL/MROL estimates use the complete ranking data coming from the best-best choices of respondents while all other columns of estimates only use the first best choices. All standard errors are cluster-robust, which allows for arbitrary correlation between the disturbance terms at the individual level. Estimation

was undertaken in Stata 14.2. MNL (multinomial logit); MXL (mixed logit); SH (scale heterogeneity model); GMNL (generalised multinomial logit); ROL (rank ordered logit); MROL (mixed rank ordered logit). ASC (alternative specific logit). SD (standard deviation).

While the specification has been shaped somewhat by the generic features of DCE data, there are a number of features that have been overlooked in this basic MNL model. Simplicity of estimation and interpretation are among the main advantages of MNL but these come at the cost of some restrictive assumptions that are clearly unrealistic in the context of DCEs.

The assumption of iid disturbances is especially problematic. We have already noted that the panel structure of the data is likely to induce correlation across choice occasions. A respondent in the case study with a preference for no treatment that is not captured by observable characteristics will carry that preference across choice occasions inducing persistence in their choices. Such effects cannot be explicitly captured by any aspect of the current specification, but it is possible to adjust the standard errors to allow for clustering at the respondent level and this we have done in Table 1.

It has long been recognized that the independence of irrelevant alternatives (IIA) is a problematic aspect of the MNL. Proportional substitution across alternatives is a consequence of this model, irrespective of the actual data. Empirically it may be a reasonable approximation in some settings such as when all alternatives are generic. But in many DCE settings, especially those involving labelled alternatives this is unlikely to be the situation. In the case study, it is highly likely that the impact of changing the cost of Drug B is going to have a very different impact on the demand for Drug A relative the impact on the choice of the no treatment option. But for MNL we know beforehand that the predicted relative market shares would not change in response to a change in the cost of one drug. Thus in situations where differential substitution patterns are likely it is advisable to move to a more flexible specification.

It has already been suggested that attribute weights may vary with respondent characteristics. However, in modelling individual behavior, unobserved heterogeneity is pervasive implying a need to allow some or all of the parameters in (3) and (4) to vary over individuals even after controlling for variation explained by observable characteristics.

Rather than building up the model with extensions targeting separate issues we will move to a very general model specification provided by the Generalized MNL (G-MNL) developed in Fiebig et al. (2010)[25]. This is not the only model that could be chosen and it is not without its critics [26] although these criticisms are more about interpretation rather than the model itself. It is a convenient choice in our discussion because it has the potential to capture all of the issues just raised. Moreover, it is a very flexible specification nesting several models often used in empirical applications and therefore provides a convenient framework for choosing between competing models. G-MNL is based on a utility specification that explicitly includes both individual-specific scale and preference heterogeneity. In other words we allow  $\lambda$ , the scale parameter in equation (3), to vary by respondent: a form of heteroscedasticity. This allows for differential choice variability in that the errors are more important relative to the observed attributes for some respondents compared to others. Differences in scale are often interpreted as differences in choice consistency. In addition, the utility weights in (4) are assumed to be

random coefficients that vary over respondent. G-MNL is written as:

$$(5) U_{isj} = X'_{isj}\beta_i + \varepsilon_{isj}$$

$$(6) \beta_i = \lambda_i\beta + \gamma\eta_i + (1 - \gamma)\lambda_i\eta_i$$

For notational convenience all variables and parameters have been collapsed into single vectors  $X$  and  $\beta$ .

If  $\lambda_i = \lambda$  implying no scale heterogeneity, G-MNL reduces to the mixed logit (MXL) specification which has long been the most popular model used in DCE work; see for example [27-30]. After normalizing scale to unity (6) becomes  $\beta_i = \beta + \eta_i$  so that MXL is a random coefficient specification designed to capture preference heterogeneity where  $\eta_i$  represents random variation around the parameter means. There are error component versions of MXL [25] where the motivation comes from the need to induce correlation and heteroscedasticity across alternatives rather than from preference heterogeneity. Suppose only the alternative specific constants are specified to be random. Assuming they are correlated provides a convenient way to avoid IIA and allow more flexible substitution between choices. It also provides a means to capture dependence due to the panel structure because  $\eta_i$  varies over individuals but it is assumed to be fixed over choice occasions. This then induces a positive correlation across choice occasions and represents a typical baseline specification common in panel analyses. Importantly, it will provide estimated standard errors that better reflect the nature of the data. Such a specification has been estimated and the results are denoted by MXL in Table 1.

If  $\eta_i = 0$  so that there is no preference heterogeneity, G-MNL reduces to a model where  $\beta_i = \lambda_i\beta$ . Allowing only for scale heterogeneity (SH), indicates how this specification is observationally equivalent to a particular type of preference heterogeneity in the utility weights, an observation that has led Louviere et al. (2008)[31] to be critical of the standard MXL model. The estimation results for this model are denoted by SH in Table 1. While conceptually there is a difference between scale and preference heterogeneity, they are intrinsically linked and hence in practice it is difficult to disentangle the two empirically [26]. In particular, rather than making this distinction one could simply motivate the G-MNL as a flexible parametric specification for the distribution of heterogeneity.

Restricting  $\gamma$  to zero implies  $\beta_i = \lambda_i(\beta + \eta_i)$  while  $\gamma$  equal to one implies  $\beta_i = \lambda_i\beta + \eta_i$ . In these two variants of G-MNL, it is either the random coefficients or just their means that are scaled. Both of these are sensible alternatives although the choice between them may not be a priori obvious. Freely estimating  $\gamma$  allows more flexibility in how the variance of residual taste heterogeneity varies with scale. The estimation results denoted by G-MNL in Table 1 are for a specification that simply combines the features of the current MXL and SH specifications with  $\gamma = 0$ . The full G-MNL model provides flexibility in how scale and taste heterogeneity are combined but can involve a large number of parameters especially when there is a large number of alternatives and their random coefficients are assumed to be correlated. Given the relatively small sample size in the case study this parsimonious specification is a sensible choice here.

The specification is completed by choosing distributions that capture the individual

heterogeneity. Preference heterogeneity is often specified to follow a multivariate normal distribution. This is what has been assumed in the results used to generate MXL and G-MNL in Table 1. In principle, the choice of distribution is flexible, but in practice normality is by far the most common choice. Lognormality is another popular option used when restricting coefficient signs. Scale heterogeneity in the SH and G-MNL models is assumed to be:

$$(7) \lambda_i = \exp(\bar{\lambda} + \tau v_i)$$

where  $v_i \sim N(0,1)$  and  $\bar{\lambda}$  is a normalizing constant required to ensure identification of  $\lambda_i$ . Note, the GMNL results in Table 1 include scaling the ASC; in other situations it may be problematic to do so; see Fiebig et al. (2010) for further discussion. The additional parameter  $\tau$  provides a measure of scale heterogeneity. If  $\tau=0$ , the G-MNL model reduces to a standard MXL specification. The work of Fiebig et al. (2010) highlights the empirical importance of accommodating this extra dimension of heterogeneity. One attraction of this specification of scale heterogeneity, is a considerable amount of flexibility with the addition of only one parameter. In principle, researchers have considerable flexibility in choosing these distributions but in practice most are confined to what options are offered in available software. (Again these are issues to be addressed below in Section 3.)

We stress that there are different approaches to model specification. An alternative to specifying random coefficient models that is quite popular in applications is to assume that there are a finite number of types where parameters vary within but not across types. So modelling heterogeneity is again the motivation but finite mixture or latent class models result; see [30] for an example. Keane and Wasi (2013)[32] provide a comparison of the two approaches in terms of fit and while they do not proclaim a clear winner they do suggest that G-MNL performs well in comparison with finite mixture models in part because the former tends to be more parsimonious.

### 2.3 Best-worst and best-best discrete choice models

The term best-worst scaling (BWS) has been used somewhat loosely in the literature. It is in fact a generic term that covers three specific cases: (1) best-worst object scaling, (2) best-worst attribute scaling and (3) best-worst discrete choice experiments (BWDCE). All three involve asking respondents to choose the best and worst (most and least preferred) from a set of three or more items. In reverse order, respondents choose best and worst between alternatives in (3); between attribute levels within a single alternative or profile in (2) and between whole objects (or sometimes statements, principles etc.) which are not decomposed into attributes in (1). See [14] [15] for further description and comparison of the three cases. Here we focus on BWDCEs for two reasons. First, they are the form of BWS closest to traditional DCEs, or can be thought of as a specific type of DCE. Second, the models we discuss here for BWDCE data can readily be applied to the other two types of BWS.

Like standard DCEs, respondents make repeated choices between alternatives offered in choice sets, each described by a number of attributes. However, BWDCEs are designed to elicit extra preference information per choice set by asking respondents not only to choose the best option but also to sequentially choose the worst option, potentially followed by

choice of best of the remaining options and so on until an implied preference ordering is obtained over all alternatives in a set. For a choice set containing  $J$  alternatives, respondents can be asked to make (and the analyst build models based on) up to  $J-1$  sequential best and worst choices. At a minimum, a BWDCE doubles the number of observations for analysis (or more if more alternatives are included per set and additional best and worst questions are answered), which in turn can be used to increase the statistical efficiency of the choice models or reduce sample sizes for a given target number of observations [14]. By providing a higher number of degrees of freedom for analysis, the extra preference data obtained via BWDCEs also opens up new research avenues such as the estimation of individual level models [5], something generally not possible with the amount of data collected per person in a standard DCE.

More recently, Ghijben et al. (2014) introduced a variation of BWDCE, namely a best-best DCE in which best is chosen from the full choice set followed by repeated choice of best (instead of worst) from the remaining alternatives until a preference order is obtained over all alternatives and used this elicitation process in their study. Like a BWDCE, this increases the number of observations collected per choice set but does so without asking respondents to swap to a new mental task of choice of worst.

We discuss three ways to analyse best-worst data that account for varying amounts and composition of preference information. The first is to simply harness the first (best) choice in each choice set, ignoring the additional choice data using models outlined above in Section 2.2 (as done by [33, 34]). Alternatively, the additional preference information obtained from a BWDCE can be used to estimate discrete choice models by noting that the best and worst choice questions produce an implied rank order over alternatives which can be modelled with rank ordered logit (ROL) (e.g. [35, 36]). ROL ([37-39]) models the probability of a particular ranking of alternatives as the product of MNL models for choice of best. For example, the ranking of three alternatives  $A>B>C$  is modelled as the product of the (MNL) probability of choosing A as best from the set (A B C) times the probability of choosing B as best from the remaining alternatives (B C)

$$(8) \Pr(\text{ranking } A, B, C) = \Pr(A \text{ is 1st best}) * \Pr(B \text{ is 2nd best}) \\ = \frac{\exp(V_A)}{\sum_{j=A,B,C} \exp(V_j)} * \frac{\exp(V_B)}{\sum_{j=B,C} \exp(V_j)}$$

Subscripts are omitted for notational brevity. In using ROL to estimate the implied preference order from a BWDCE the best-worst structure used to generate that order is ignored since ROL assumes best (not worst) is chosen from successively smaller choice sets. In contrast, the ROL matches exactly the data generation process of a best-best DCE in which best is chosen from successively smaller choice sets. The data are modelled using ROL in Table 1.

The sequential best-worst MNL (SBWMNL) model [14, 35] directly models the series of sequential best and worst choices made in each choice set as the product of MNL models. Using the above example of a choice set containing three alternatives (A B C), the probability of observing the preference order  $A>B>C$  is modelled as the (MNL) probability of choosing A as best from the set (A B C) times probability of choosing C as worst from the

remaining alternatives (B C) which can be expressed as

$$(9) \quad \Pr(\text{best worst ordering } A, B, C) = \Pr(A \text{ is best}) * \Pr(C \text{ is worst}) \\ = \frac{\exp(V_A)}{\sum_{j=A,B,C} \exp(V_j)} \times \frac{\exp(-V_C)}{\sum_{j=B,C} \exp(-V_j)}$$

Here the best-worst ordering of the three alternatives is represented as the two choices made by respondents per choice set in the BWDCE and the deterministic part of utility of choosing an alternative as worst is modelled as the negative of the deterministic utility of choosing that alternative as best. SBWMNL models the choice data in the way they were generated so that the worst choice is modelled in the second MNL model in equation (8) and the composition of the denominator reflects the actual choice sets considered by respondents associated with each choice set in the sequence.

Equations (7) and (8) can both be generalized to account for the types of heterogeneity discussed in Section 2.2. For example, Lancsar et al. (2013)[14] demonstrated how mixed logit, heteroscedastic logit and G-MNL versions of ROL and SBWMNL could be estimated. The mechanics of doing so is made very straight forward due to the fact that (as we will discuss in Section 3) both ROL and the SBWMNL models can be estimated by “exploding” the data into the implied choice sets and then estimating MNL on the exploded data. As such, it is straightforward to estimate any of the models discussed earlier on rank or best-worst data. In the final column of Table 1 we present the estimates for the mixed ROL (MROL) that reproduces the specification B results from Table 3 in Ghijben et al. (2014). Thus these results are directly comparable to the MXL estimates in Table 1 that just uses the first best choice.

## 2.4 Post estimation

Good econometric practice suggests one should conduct various robustness checks to ensure the internal validity of the estimated model. When dealing with revealed preference data a constant threat is omitted variable biases meaning that effects of interest may be very sensitive to the variables not included in the model. This is much less of a concern with stated preference data where the effects of interest are typically associated with the attributes that are created as part of the experimental design, meaning that there is typically no correlation between attributes and no reason to believe they will be correlated with respondent characteristics. For omitted variable biases to arise in stated preferences, attributes would need to be omitted from the design that lead respondents to change their evaluation of included attributes because of expectations about the relationship between omitted and included attributes. This would lead to biased estimates of coefficients of included attributes and these biases could depend on respondent characteristics. But such problems can readily be minimized at the design stage and is an argument for avoiding simple designs with minimal numbers of attributes.

What is a potential threat are features of the design such as when respondents are assigned to different versions of the survey. In the case study the authors included a dummy variable to control for block effects. From Table 1 we see that these effects are never statistically significant at any conventional level and so at least in this dimension one should be confident about the results.

Often issues of model choice can be resolved by testing restrictions associated with nested versions of more general models. Because maximum likelihood is the basis for estimation likelihood ratio tests can easily be conducted for this purpose. For example, in Table 1 MNL, MXL and SH are nested within G-MNL. It is wise to remember that except for MNL, the log-likelihood function is simulated rather than known exactly and so subject to simulation noise. In the case of non-nested models such as a comparison between MXL and SH or between MROL and MXL information criteria such as AIC and BIC may be used to discriminate between alternative models.

While model fit may provide some guidance in choice of models, often what is more important is the specific research question being considered and the specific features of the data being used and how they map into the model being considered. For example, if data are being pooled across very different subsamples of respondents, scale heterogeneity would be an obvious concern; see for example [29]. If one is simulating the impact of the introduction of a new product or treatment as in [34] then it would be prudent to avoid MNL and allow for flexible substitution patterns.

Section 3.4 discusses other post-estimation issues, such as how the estimated model can be used to generate measures of marginal willingness to pay (mWTP) and carry out predictive analyses.

### **3. Software and estimation**

#### **3.1 Discrete choice**

This section provides an overview of software for estimating the models described in the previous section. The focus will be on general statistics/econometrics packages with built-in commands for estimating discrete choice models<sup>3</sup>, rather than programming languages which require user-written code.<sup>4</sup>

##### **Nlogit**

Nlogit ([www.limdep.com/products/nlogit](http://www.limdep.com/products/nlogit)) is an extension of the Limdep statistical package. It has a very comprehensive set of built-in commands for estimating discrete choice models, and can be used to estimate all of the models covered in Section 2. It has various post-estimation routines for generating predicted probabilities, performing simulations and calculating elasticities. Nlogit is relatively easy to use and comes with a comprehensive PDF-manual.

##### **Stata**

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<sup>3</sup> Our overview is not exhaustive as other software packages capable of estimating some of the discrete choice models in our review are available. The three packages that we have reviewed are among the most commonly used for estimating these models, however.

<sup>4</sup> This implies that we will not cover software such as Gauss, Matlab and R, despite there being excellent routines written in these packages for estimating e.g. mixed logit models. A prominent example is Kenneth Train's codes for mixed logit estimation (available at <http://eml.berkeley.edu/~train/software.html>), which served as inspiration for many of the routines later introduced in other statistical packages.

Stata ([www.stata.com](http://www.stata.com)) is a general statistics package which offers a broad range of tools for data analysis and data management. While it has fewer built-in commands for estimating discrete choice models than Nlogit, there is a range of user-written commands freely available that can be used to implement the methods covered in Section 2 [40-43]. It has routines for generating predicted probabilities, and simulations can be performed and elasticities calculated by using the generated probabilities. Like Nlogit, Stata is relatively easy to use and comes with a comprehensive PDF-manual. User-written commands are often documented in articles published in the Stata Journal ([www.stata-journal.com](http://www.stata-journal.com)).

### Biogeme<sup>5</sup>

Unlike Stata and Nlogit, which are general statistical packages, Biogeme ([biogeme.epfl.ch](http://biogeme.epfl.ch)) is specifically created for estimating discrete choice models. It also stands out for being the only package of the three which is free; both Stata and Nlogit require the user to pay a licence fee. Biogeme is capable of estimating MNL models with both linear and non-linear utility functions and with random coefficients, which means that all of the models covered in Section 2 can be implemented. It also has a routine for performing simulations (biosim). While Biogeme is somewhat less easy to use for beginners than Stata and Nlogit in our experience, the documentation is comprehensive and has helpful examples. Since Biogeme requires a somewhat higher initial time investment, it is recommended in particular for more advanced users that wish to go beyond standard model specifications. As Biogeme has fewer built-in commands for data management than Stata and Nlogit, it will often be necessary to use an alternative software package to set up the data in the form required by Biogeme.

**Table 2: A summary of the modelling capabilities of the main software packages covered in the review**

Software Package	MNL	MXL	Latent class	MXL Bayesian	G-MNL
Nlogit	✓	✓	✓		✓
Stata	✓	UW	UW	UW	UW
Biogeme	✓	✓	✓		✓

Notes: This is not an exhaustive list; all of the packages have options for estimating other discrete choice models not covered in this review. The packages differ in terms of which distributions are supported for the random coefficients in the mixed logit routines, with Nlogit having the widest selection of distributions. GMNL can be fit in Biogeme by exploiting the option for specifying non-linear utility functions, however it is less straightforward to do than in the other two packages. Scaled ASCs are the default GMNL option in Stata and Nlogit and can be done in Biogeme. However, this can be potentially problematic depending on the context and model and we suggest testing with and without scaling the ASC (in our case it made little difference). UW = user-written. MNL (multinomial logit); MXL (mixed logit); GMNL (generalised multinomial logit)

To sum up, Nlogit, Stata and Biogeme are all good options for estimating discrete choice models. We would argue that there is no “one size fits all”: no package strictly dominates the others, and it will therefore be up to the individual user to choose the package that best suits their needs. As mentioned, Biogeme has the advantage that it’s free and very powerful, but requires a somewhat greater time investment on the part of the user to learn how to use it effectively. Nlogit has a very comprehensive set of built-in commands which

<sup>5</sup> Two versions of Biogeme are available: BisonBiogeme and PythonBiogeme. We focus on BisonBiogeme, which is designed to estimate a range of commonly used discrete choice models.

cover most, if not all, of the models that the majority of DCE analysts would want to estimate. Stata has a less comprehensive set of built-in commands, but has user-written routines which cover the most commonly used models. Both Nlogit and Stata have the advantage that all data processing and cleaning can be done in the same package which is used to run the analysis. All three packages have active on-line user group discussion forums where queries are typically answered quickly. The forum archives are searchable, and contain a wealth of useful information in the form of past questions and answers, so it's typically worth spending some time searching the archives before posting a new question.

## 3.2 Estimation of discrete choice models

### 3.2.1 Data setup

Before proceeding to the estimation stage the analyst needs to organise the data in the way required by the estimation software. In general there are two ways the data can be organized: 'long form' (see Appendix 1) and 'wide form' (see Appendix 2):

- Long form, which is the data structure required by Stata and Nlogit<sup>6</sup>, implies that the dataset has one row per alternative for each choice scenario that the decision-makers face. Thus, with  $N$  decision-makers choosing amongst  $J$  alternatives across  $S$  scenarios the dataset will have  $N \times J \times S$  rows. The dependent variable is coded 1 for the chosen alternative in each scenario and 0 for the non-chosen alternatives.
- Wide form, which is the data structure required by Biogeme, implies that the dataset has one row for each choice scenario that the decision-makers face. The dataset will therefore have  $N \times S$  rows. In this case the dependent variable is coded  $1, \dots, J$ , indicating the chosen alternative. Each design attribute will have  $J$  associated variables, containing the level of the attribute for the respective alternative. This contrasts with the long form structure, where there is only one variable per design attribute.

Both Stata and Nlogit have built-in commands for transforming the dataset from long to wide form, and vice versa. For convenience the example dataset is available as supplementary material in both long and wide form.

When the data is in long form, ASCs can be defined as a dummy variable which is equal to one in the row corresponding to the relevant alternative and zero otherwise. Alternative-specific coefficients can then be estimated by interacting the ASCs with the desired attribute(s) and including the interactions in the model. In Biogeme such effects are specified by explicitly defining the utility function of the different alternatives, an option which is also available in Nlogit. More generally, categorical attributes and covariates can be coded as dummy variables or effects coded, either being appropriate as long as interpreted appropriately [44, 45]. Indeed even for continuous variables (e.g. price), it can often prove useful to initially treat the levels as categorical in exploratory testing in order to

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<sup>6</sup> Nlogit also optionally allows the data to be organized in wide form, although the manual suggests that long form is typically more convenient.

plot the coefficients to help inform choice of functional form for the continuous variable.

### 3.2.2 Other estimation issues

Implementing the models presented in Section 2 in practice requires the analyst to make a number of choices at the estimation stage.<sup>7</sup> As we will show these choices can impact on the results, and it is therefore recommended to carry out a sensitivity analysis to examine the robustness of the findings.

#### Starting values

Estimating the parameters in the model involves maximising a non-linear log-likelihood function, and the maximisation process requires the user to provide an initial guess of the parameter values.<sup>8</sup> The software package then searches for improvements in the log-likelihood iteratively, by changing the values of the parameters using an optimisation algorithm. In the case of the MNL model the choice of starting values typically does not matter in practice, as the MNL log-likelihood function has a single maximum. The algorithm will therefore find the maximum even if the starting values are far from the values that maximize the log-likelihood. In the case of models such as MXL and G-MNL, however, matters are less simple. For those models the log-likelihood may have several optima, of which only one is the overall (global) optimum which we seek to identify. Starting from a set of parameter values far away from the global optimum may lead the algorithm to identify one of the inferior local optima, at which point the algorithm will declare convergence as it cannot distinguish between local and global optima. Only the parameter values associated with the global optimum have the desirable properties of maximum likelihood estimates, and it is therefore recommended to investigate the sensitivity of the results to a different choice of starting values. Hole and Yoo (2014)[46] discuss these issues in the context of the G-MNL model. Czajkowski and Budziński (2015) [47] find that increasing the number of simulation draws (see below) improves the chance of the algorithm converging to the global optimum.

#### Simulation draws

Another issue that the analyst needs to be aware of when estimating MXL and G-MNL models is that the log-likelihood function must be approximated using simulation methods, as it cannot be calculated analytically. Simulation methods involve taking a large number of random draws, which represent the distribution of the coefficients at the current parameter values. As the draws are generated by a computer they are not truly random, but created using an algorithm designed for the purpose of generating draws which have similar properties to random draws. The analyst needs to decide how many draws to use to approximate the log-likelihood function and which method to use to generate the draws. Regarding the number of draws there is a tradeoff between accuracy and estimation time; a large number of draws gives a better approximation of the true log-likelihood function, but slows down the estimation process. It is therefore common to start with a relatively small number of draws at the exploratory stage, for example using the default setting in the

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<sup>7</sup> Interested readers are referred to chapters 8-10 in Train (2009) for more information about the issues covered in this section.

<sup>8</sup> Both Nlogit and Stata will use a default set of starting values unless explicitly specified by the user, while Biogeme requires the user to specify the starting values.

software used.<sup>9</sup> It is then strongly advisable to check for the stability of the final solution to be reported in a paper, report etc. by increasing the draws. The number of draws required to stabilize the results will depend on the model specification; typically a larger number of draws is needed if there are more random coefficients in the model. The number of draws required is also related to the method chosen to generate the draws. For example, in the context of mixed logit estimation, 100 Halton draws have been found to be more accurate than 1000 pseudo-random draws [48, 49]. For this reason Halton draws are often used when estimating MXL and G-MNL models.<sup>10</sup>

Table 3 below shows the results from estimating a simplified version of the MXL model described in Section 2 (Model A from Ghijben et al., 2014) in Nlogit, Stata and Biogeme. The starting values are set at the default values in Nlogit and Stata, and the Biogeme starting values are set to be identical to the Stata default values.<sup>11</sup> While it can be seen that there are no qualitative differences between the results – the coefficients have the same sign and significance and the point estimates are similar - they are not exactly identical. This is in spite of using the same number of simulation draws (500) and the same method for generating the simulation draws (Halton).<sup>12</sup> As long as the results do not differ to the extent that it has an impact on the substantive implications of the findings, however, this should not give much cause for concern.

**Table 3: Results from estimating a MXL model in the different software packages\***

	Nlogit		Stata		Biogeme	
	Coef.	SE	Coef.	SE	Coef.	SE
Stroke risk	0.706	0.060	0.706	0.060	0.706	0.060
Bleed risk	0.578	0.049	0.578	0.049	0.578	0.049
Antidote	0.600	0.081	0.600	0.081	0.600	0.081
Blood test	-0.082	0.077	-0.082	0.077	-0.082	0.077
Dose frequency	-0.089	0.077	-0.089	0.077	-0.089	0.077
Drug/food interactions	-0.340	0.079	-0.340	0.079	-0.340	0.079
Cost	-0.012	0.001	-0.012	0.001	-0.012	0.001
ASC x block	-1.051	0.862	-1.003	0.856	-1.000	0.854
ASC (mean)	3.108	0.759	3.086	0.750	3.090	0.742
ASC (SD)	3.102	0.492	3.069	0.477	3.050	0.478
Log-likelihood	-791.03		-790.91		-790.85	

<sup>9</sup> The default number of draws is 100 in Nlogit, 50 in Stata and 150 in Biogeme.

<sup>10</sup> In models with several random coefficients alternative approaches such as shuffled or scrambled Halton draws 50. Hess S, Train KE, Polak JW. On the use of a Modified Latin Hypercube Sampling (MLHS) method in the estimation of a Mixed Logit Model for vehicle choice. *Transportation Research Part B: Methodological*. 2006;40(2):147-63. or Sobol draws 51. Garrido RA. Estimation performance of low discrepancy sequences in stated preferences. 10th International Conference on Travel Behaviour Research. Lucerne 2003, 52. Munger D, L'Ecuyer P, Bastin F, Cirillo C, Tuffin B. Estimation of the mixed logit likelihood function by randomized quasi-Monte Carlo. *Transportation Research Part B: Methodological*. 2012;46(2):305-20. are sometimes used to minimise the correlation between the draws, which can be substantial for standard Halton draws in higher dimensions. See Train (2009, chapter 9) for a discussion.

<sup>11</sup> Nlogit and Stata's default starting values are the MNL parameters for the means of the random coefficients and 0 (Nlogit)/ 0.1 (Stata) for the standard deviations.

<sup>12</sup> Differences can still arise, for example because the optimisation algorithms differ in the three packages, subtle differences in terms of how the Halton draws are generated and different starting values (in this case Stata/Biogeme vs Nlogit).

\*The following versions were used for estimation: Stata 14.2, NLOGIT 5 and Biogeme 2.0. Coeff (coefficient); SE (standard error).

### 3.3 Estimation of best-worst and best-best models

Estimation of choice models harnessing just the first best choice from best-worst or best-best data proceeds as outlined in Section 3.1. Estimation of ROL in Stata involves the `rol` command. In Nlogit ROL models can be estimated using the rank as the dependent variable and adding “ranks” to the usual model syntax. In Biogeme the data need to be exploded manually (See Appendix 3). Indeed, an attractive property of both ROL and SBWMNL is that they can be estimated using standard MNL (or extensions such as MIXL, G-MNL etc.) after the data have been set up appropriately. In fact, ROL is also known as “exploded logit” because, drawing on the IIA property of MNL models, it can be estimated by exploding the data from each choice set into statistically independent choice subsets. For a choice set with  $J$  alternatives, the data can be expanded into  $J-1$  sub choice sets. For example, for a ranking over  $J=3$  alternatives, the data can be exploded into two sub choice sets. The first contains three rows of data representing the three alternatives contained in the original choice set with the dependent variable equal to 1 for the alternative ranked first (chosen as best) and 0 for the remaining alternatives which is identical to data set up for standard first best choice model. The second sub choice set identifies best from the remaining 2 alternatives and contains two rows of data pertaining to the two alternatives not ranked first with the dependent variable equal to 1 for the alternative ranked second (chosen as best from the two on offer) and 0 for the remaining alternative. So for each original choice set containing 3 alternatives, there are five rows of data<sup>13</sup>. Once the rankings are exploded in the dataset to the implied choices made in each of the subsets, the ROL parameters can be estimated using a traditional MNL model (or extensions of the MNL model) from the expanded choice data. Indeed, prior to ROL routines being programmed in software packages, this was the standard way to estimate a ROL. A good check that the data have been exploded correctly before moving on to more sophisticated models accounting for unobserved heterogeneity etc. is to run an MNL (e.g. via the `clogit` or `asclogit` command in Stata) on the exploded data and then run a ROL on the un-exploded data (e.g. using `rol` in Stata). The results should be identical in all decimal places.

In all three software packages (Stata, Nlogit and Biogeme), the data need to be exploded to estimate SBWMNL models. Like the ROL model, estimation of the SBWMNL model draws on the IIA property and exploits the additional preference information obtained in each choice set in a BWDCE, expanding the data in a similar but slightly different way. Again, for a choice set with  $J$  alternatives, the data can be exploded into  $J-1$  sub choice sets. So data from a choice set containing 3 alternatives from which best and worst are chosen are expanded into two sub choice sets. The first contains three rows of data corresponding to the three alternatives presented in the original choice set with the dependent variable equal to 1 for the alternative chosen as best, and 0 for the remaining alternatives. The second sub choice set contains two rows of data representing the two alternatives not chosen as best in the full choice set with the dependent variable equal to 1 for the alternative chosen as worst and 0 for the remaining alternative. Thus, again for each original choice set containing 3 alternatives, there are 5 rows of data. In addition, for the sub choice set in

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<sup>13</sup> Applying this procedure modifies the data from the standard set up in Appendix 1 to the exploded set up in Appendix 3.

which worst is chosen the utility of worst is scaled to be the negative of the utility of best which in practice means multiplying the data for the alternatives in the second sub choice set by -1. Parameters can then be estimated using MNL (or its extensions) on the exploded choice data. Code for all estimation contained in this paper is provided in Appendix 4.

### 3.4 Post estimation

As discussed in Section 2.4 issues of model choice can be resolved by testing restrictions associated with nested versions of more general models. Such tests can easily be carried out using the tools available in Nlogit and Stata for performing Wald tests. In all packages an alternative approach is to carry out a likelihood ratio test using the reported simulated log likelihood values for the restricted and unrestricted models.

Information criteria such as AIC and BIC may be used to discriminate between alternative models which are not nested. Apart from the examples mentioned in Section 2.4 this can be useful when assessing the goodness of fit of MXL models with different distributions for the random coefficients, for example. The information criteria can be readily calculated in all packages using the reported simulated log likelihood values, along with the relevant information regarding the number of parameters in the competing models and (in the case of BIC) the sample size.

It is worth re-iterating that while model fit may provide some guidance in choice of models often what is more important is the specific research question being considered and the specific features of the data being used. Rather than choosing one preferred specification it is typically better to report the output of interest (such as mWTP measures, predictive analyses) for a range of model specifications and compare and contrast the results, as demonstrated below.

#### Marginal willingness to pay measures

Calculating marginal willingness to pay measures is a convenient and useful way to compare attribute estimates. mWTP can be derived as the marginal rate of substitution between attribute  $X^k$  and cost (C):

$$(10) mWTP_{X^k} = - \frac{MU_{X^k}}{MU_C}$$

where  $MU_{X^k}$  and  $MU_C$  are the marginal utilities of attribute  $X^k$  and cost, respectively. When the utility function is specified to be linear in parameters the marginal utility of an attribute is equal to its coefficient, which means that mWTP is given by the negative of the ratio of the coefficients for attribute  $X^k$  and cost. In Table 4, we use the MNL, MXL and MROL results from Table 1 to produce mWTP estimates for the most important attributes, stroke risk and bleed risk. The latter replicate the results in Table 4 in Ghijben et al. (2014).

**Table 4: Selected estimates of marginal willingness to pay for a subset of attributes using data from Ghijben et al. (2014)\***

	MNL	MXL	MROL
	Estimate	Estimate	Estimate

	(95% CI)	(95% CI)	(95% CI)
Stroke risk	68.37 (44.24-92.51)	70.53 (44.31-96.75)	50.48 (33.68-67.28)
Bleed risk (without antidote)	67.02 (42.29-91.75)	67.66 (41.09-94.23)	54.87 (35.70-74.05)
Bleed risk (with antidote)	34.02 (18.55-49.50)	38.36 (21.93-54.79)	35.70 (21.70-48.99)

\* mWTP/month in AUD\$ for a 1 percentage point reduction in absolute risk MNL (multinomial logit); MXL (mixed logit); MROL (mixed rank ordered logit). CI (confidence interval).

The MNL results indicate that, for example, the willingness to pay for a one-percentage-point reduction in the stroke risk is about 69 AUD per month. The remaining estimates can be interpreted in an analogous way. The estimates are reasonably stable across models, with the MNL and MXL estimates being especially close while the MROL stroke risk mWTP is somewhat of an exception. If we refer back to the actual parameter estimates used in these calculations, those for MNL are systematically smaller in magnitude, a scaling effect, but those for MXL and MROL are very similar as we would expect.

While mWTP measures are straightforward to calculate when the utility function is linear in parameters, routines for obtaining confidence intervals using either the delta method or parametric (Krinsky-Robb) or non-parametric bootstrapping [53] are useful since a measure of the precision of the estimates should always be reported. Such routines are available in both Nlogit and Stata. In some cases the assumption of linearity is not appropriate, as a researcher may want to allow the marginal utility of a change in an attribute to depend on the level of the attributes (e.g. due to interactions or non-linear functional form; see e.g.[33]). In such cases the calculation of mWTP is slightly more involved, but we can still use general routines for calculating non-linear combinations of parameters in Stata and Nlogit to obtain point estimates and measures of precision.

Calculating mWTP measures following the estimation of a model with random coefficients, such as MXL or G-MNL, can be more complicated depending on the model specification. If both the attribute coefficient and the cost coefficient are fixed, as in our examples, the calculation is the same as for the MNL model. If the attribute coefficient is normally distributed and the cost coefficient is fixed, which is a common specification, the mean mWTP is simply given by the ratio of the mean attribute coefficient to the negative of the estimated cost coefficient. Relaxing the assumption that the cost coefficient is fixed can lead to complications: a normally distributed cost coefficient, for example, leads to a distribution for mWTP that has no defined mean since the cost coefficient can now be equal to zero. Researchers therefore often choose a distribution for the cost coefficient which is constrained to be negative to avoid this problem, such as the negative of a log-normal distribution.<sup>14</sup> While this solves the problem of the mWTP distribution not having a defined mean it can lead to a non-standard distribution whose mean may not be straightforward to

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<sup>14</sup> Log-normal parameter distributions are supported by all of the packages. The negative of the log-normal can easily be implemented by multiplying the price attribute by -1 before entering the model. This is equivalent to specifying the negative of the price coefficient to be log-normally distributed. The sign of the coefficient can easily be reversed post-estimation.

calculate.<sup>15</sup> One solution is to approximate the mean using simulation by taking many draws from the distribution of the attribute coefficient and the price coefficient, calculate the ratio for each draw and taking the average of the calculated ratios. If we take a large number of draws the resulting average should be close to the true mean of the mWTP distribution.

An alternative to estimating the model in the usual way and calculating mWTP as the ratio of parameters is to reformulate the model so that mWTP is estimated directly. This approach, called estimation in willingness-to-pay space [54], is appealing as it avoids the complications described above. The recent paper by Ben-Akiva et. al. (2015)[55] covers this estimation approach in detail with illustrative examples. Estimation in WTP-space is supported in both Nlogit and Stata, and is possible to implement in Biogeme by exploiting the option for specifying non-linear utility functions.

The marginal willingness to pay measures can be conditioned on observed choices to obtain individual-level estimates of mWTP; see for example [30, 56]. The individual-level mWTP measures can be useful for policy analysis, for example to identify respondents who are likely to benefit particularly highly from a policy improvement.

### Predictive analysis

A predictive analysis is an extremely flexible post estimation tool. It is a convenient way to characterize how predicted probabilities change in response to changes in attributes as well as providing a means to simulate interesting scenarios. We illustrate the former here and refer interested readers to [57] for an application involving policy changes and for applications where the impact of the introduction of a new product is investigated see [34] and [11] who operationalize procedures outlined in Train (2009)[49].

Again using the MNL, MXL and MROL results from Table 1 consider a base case where all attributes have been set to zero. This produces predicted probabilities for each of the estimation methods given in the rows labeled “Baseline” of Table 5. Then subsequent rows show how these predicted probabilities would change in response to two particular changes in the attributes of Drug B. The first is a AUD\$50 increase making Drug B less attractive and the second that makes Drug B more attractive is a 1percentage point eduction in stroke risk. Each of these changes in Drug B is simulated separately and so the appropriate comparison in each case is with reference to the baseline probabilities.

Nlogit, Stata and Biogeme all have built-in routines for conducting predictive analyses. Confidence intervals for the predictions can be generated by taking many draws from the attribute coefficients, generating the predicted probabilities of interest for each draw and calculating the desired percentiles of the generated distributions.

**Table 5: Comparison of predictions for each alternative in response to changes in selected attributes using data from Ghijben et al. (2014)\***

	No treatment	Drug A	Drug B
	Probability (95% CI)	Probability (95% CI)	Probability (95% CI)
<i>MNL</i>			

<sup>15</sup> One exception is when both the attribute coefficient and the negative of the price coefficient are log-normally distributed, in which case the distribution of mWTP is also log-normal.

Baseline	0.165 (0.079-0.317)	0.417 (0.341-0.461)	0.417 (0.341-0.461)
Increase cost of \$50 for Drug B	0.198 (0.098-0.363)	0.501 (0.394-0.567)	0.301 (0.238-0.348)
Reduction of 1% in stroke risk for Drug B	0.116 (0.054-0.234)	0.294 (0.244-0.331)	0.590 (0.515-0.640)
<i>MXL</i>			
Baseline	0.177 (0.020-0.389)	0.412 (0.306-0.490)	0.412 (0.306-0.490)
Increase cost of \$50 for Drug B	0.193 (0.025-0.408)	0.511 (0.377-0.620)	0.295 (0.215-0.366)
Reduction of 1% in stroke risk for Drug B	0.148 (0.013-0.348)	0.269 (0.199-0.327)	0.583 (0.445-0.682)
<i>MROL</i>			
Baseline	0.243 (0.174-0.336)	0.379 (0.332-0.413)	0.379 (0.332-0.413)
Increase cost of \$50 for Drug B	0.273 (0.200-0.372)	0.486 (0.415-0.542)	0.242 (0.203-0.279)
Reduction of 1% in stroke risk for Drug B	0.204 (0.142-0.289)	0.263 (0.226-0.298)	0.533 (0.474-0.581)

\* Notes: (i) These are the probabilities that each alternative is chosen as best.

(ii) Baseline refers to the case when all of the attributes for Drug A and Drug B are set to zero.

(iii) Each variation in attribute level is simulated one at a time and only selected variations have been reported. MNL (multinomial logit) MXL (mixed logit); MROL (mixed rank ordered logit)

The implications of IIA are clear from the changes in MNL predicted probabilities in comparison with those for MXL and MROL. For example, the response to the cost change implies a dramatic predicted shift away from Drug B but in the case of MNL the change in predicted probabilities is such that relativities between say Drug A and No treatment are maintained at the baseline level;  $(0.501/0.198)=(0.417/0.165)=2.55$ . In contrast, the increase in the predicted share of Drug A is proportionally larger in the case of MXL and MROL implying a more realistic substitution pattern. We note that the above analysis differs to the predicted probability analysis presented in Ghijben et al. (2014) where more complex policy scenarios are explored, including the introduction of new medications, as well as recalibration to market data.

Marginal effects are essentially a simple form of predictive analysis, in which the probabilities in a baseline scenario are compared to the probabilities in an alternative scenario following a marginal increase in a single attribute of one of the alternatives in the model. When viewed this way marginal effects can be calculated using the same tools as those used to carry out predictive analyses. Elasticities can be calculated in an analogous way, only that in this case we are looking at the percentage change in the probabilities resulting from a 1% increase in an alternative attribute.

It is worth bearing in mind that a potential issue with using DCE data for predictive analysis is that the data do not embody the market equilibrium. Calibrating the ASCs using market data is therefore strongly advisable where such data are available.

## Welfare analysis

A key behavioural outcome of interest to economists is individual and aggregate willingness to pay and willingness to accept monetary amounts in response to policy changes such as a change in single attributes, multiple attributes or the introduction or removal of entire options from the choice set. Indeed, such values are essential in cost benefit analysis. Such values can be calculated in post estimation welfare analysis using the compensating variation. In the case of the MNL model the compensating variation can be expressed as:

$$(11) \quad CV = \frac{1}{\mu} \left[ \ln \sum_{j=1}^J e^{V_j^0} - \ln \sum_{j=1}^J e^{V_j^1} \right]$$

where  $V_j^0$  and  $V_j^1$  are the values of the utility function,  $V$ , estimated in the choice model for each choice option  $j$  before and after the quality change, respectively, and  $J$  is the number of options in the choice set. The log sum terms in equation (10) weight the utility associated with each alternative by the probability of selecting that alternative and as such can be interpreted as the expected utility. The CV therefore calculates the change in expected utility before and after the policy change and scales this utility difference by the marginal utility of income,  $\mu$ , to provide a monetary and therefore cardinal measure of the change in welfare. Often information on income is unavailable, in which case the coefficient on the price attribute (which represents the marginal disutility of price) can be used as the negative of the marginal utility of income. In fact any quantitative numeraire would work – see for example Lancsar et al (2011) who use the marginal utility of a QALY as the numeraire. Calculation of the CV involves harnessing the coefficients estimated in the choice model along with the values of the attributes of interest and can easily be undertaken by hand or in standard software packages (e.g. using nlcom in Stata which also produces confidence intervals). The interested reader is referred to [58] for further discussion of the theory and methods for such calculations.

## 4. Discussion

Choice modelling is a critical component of undertaking a DCE but to date has received less attention in terms of guidance than other components. As we highlight in Section 2, researchers face a number of decisions when analysing DCE data and arriving at a final model. Some decisions are resolved by the choice problem and design (e.g. binary versus multinomial choice, which variables are independently identified in the experimental design, whether the choice is labeled therefore allowing for the possibility of alternative specific utility functions, or generic, etc.) while others are specification decisions that need to be made on a case by case basis (e.g. functional form of specific variables which could be linear, quadratic, logarithmic etc., forms of heterogeneity to be explored etc.). Such decisions are not necessarily linear and sequential and instead many are simultaneous and interdependent.

There is no single model that we would recommend in all cases with each having a number of advantages, and possible disadvantages depending on the research question being addressed. In selecting a modeling approach, we would recommend finding a model that addresses the researcher's questions of interest and provides a reasonable device with

which to represent the choice at hand. Ultimately, it is still a model and all models involve assumptions. The question to address is which assumptions are most appropriate (or have minimum detriment) to the research questions being explored. It is important to note that the choice of model to be estimated is not only dependent on the research objectives, study design etc. but is also constrained by what can be estimated given the data a researcher has (including such issues as quantity and quality) and so is based on considerations from both Sections 2 and 3.

MNL was for decades the workhorse of choice modeling and we recommend it as a natural first model to estimate. Where to go next after MNL is not always clear and depends on the research objectives but a basic first step would be the estimation of a mixed logit model to account for the panel structure of the data, providing more reliable standard errors and move away from proportional substitution (by relaxing IIA). It also allows for unobserved preference heterogeneity by allowing coefficients to vary randomly across individuals. Whether one takes a Frequentist or Bayesian approach to the estimation of mixed logit in part comes down to preferences of the researcher but with the use of simulation methods the distinction between the two approaches is becoming less pronounced and recent evidence suggests little difference in estimates [59]. Focus on mixed logit in the health economics literature has often been motivated by interest in unobserved heterogeneity. To our minds, the other two reasons for exploring mixed logit are at least as important.

Having said that, exploration of heterogeneity can be important and has received much attention. If one views the distribution of preference heterogeneity to be discrete rather than continuous a latent class model would be appropriate. By allowing for different preference parameters between classes an advantage of latent class modeling is it allows heterogeneity to be interpreted in terms of class type and class membership. Another form of heterogeneity gaining attention is scale heterogeneity. A modification to the MNL leads to the heteroscedastic logit which allows for between person differences in scale to be modeled as a function of covariates. Alternatively, interest in unobserved scale heterogeneity could lead to the scale heterogeneity model. G-MNL offers a very flexible approach which nests several of the standard models discussed in Section 2 including mixed logit, heteroscedastic logit and scale heterogeneity models.

When exploring heterogeneity key decisions to make include which form(s) of heterogeneity are most of interest to the researcher – e.g. preferences or scale, unobserved or observed; noting that these need not be mutually exclusive. While both observed and unobserved heterogeneity can be important, and indeed can be explored within the same model, a distinction between the two is that the latter often improves model fit but is not always readily interpretable. In contrast observed heterogeneity is interpretable in relation to known covariates (e.g. age, gender, past experience etc.) thereby potentially generating useful implications for policy and practice. Ultimately, the source(s) of heterogeneity to be explored depends on the research questions, the assumptions researchers are prepared to make and what is revealed by the data. Whichever model is estimated, it is important to be cognizant of the implications of the model (and associated assumptions) chosen for the conclusions that can be drawn.

We also provided model and estimation procedures for best-worst and best-best DCEs

including rank ordered logit and sequential best worst MNL. The fact that both models can be estimated by expanding the data as described in Section 3 and then applying MNL has a particularly advantageous feature that it is straightforward to estimate more sophisticated versions of these base models, allowing for non IIA, correlated errors and various forms of heterogeneity. For example, all of the models discussed in Section 2 for estimation with first best-data (mixed logit, GMNL etc.) can be estimated simply by running such commands on the expanded best-worst or best-best data. Correct data set up is therefore crucial and we offer advice on a useful way to check this.

More generally, the advantages and limitations of best-worst data collection have been outlined elsewhere. As Lancsar et al. (2013)[14] note, a key advantage is the generation of more data relative to a standard DCE which can prove particularly useful when sample size constraints exist (due to budget considerations or when the population from which the sample is being drawn is itself small) or even when sample size is not a constraint, it can prove an efficient way to generate a given quantity of data or simply provide more data. The additional data can also prove particularly useful for the estimation of models for single individuals [31, 35].

We presented several standard software options in Section 3. An advantage of Stata and Nlogit beyond estimation is that they provide comprehensive data management. In contrast Biogeme requires external data management but is very flexible in estimation; it is also free. Which a researcher selects will in part depend on personal preferences, particularly if they have already invested time and resources in a particular software package. We also offered advice on data set up and best practice in terms of estimation, including issues such as choice of starting values, number of draws in estimation etc.

When it comes to interpretation of results, the parameter estimates from choice models are typically not of intrinsic interest and indeed parameters often cannot meaningfully be compared due to the different scales on which they are measured, some of which may be quantitative (e.g. time, cost, risk, etc.) while others may be qualitative (provider type, location etc.) [33]. It is therefore surprising that many researchers stop after generating attribute coefficients without undertaking post estimation, particularly given post estimation is not difficult to carry out and provides useful insights. We strongly encourage researchers to harness model parameters in post estimation analysis to both improve interpretation and to produce measures that are relevant to policy and practice. At a minimum we suggest the calculation of marginal rates of substitution, but depending on the goals of the research additional analysis could include predicted uptake or demand, elasticities and welfare analysis.

As with all methods, validity is crucial. Internal validity has received considerable attention in the health economics literature, including checking signs of estimated parameters accord with a priori expectations and the testing of axioms of consumer theory (e.g. [60, 61]) Lancsar and Louviere (2006) [62] caution against deleting data on the basis of such tests. Lancsar and Swait (2014) [9] provide a new and more comprehensive conceptualization of external validity which advocates that its investigation should be broader than the comparison of final outcomes and predictive performance and indeed encompasses process validity. They suggest innovative ways in which the broader definition can be pursued in

practice starting from the initial conception and design of a DCE through to model and post estimation. Most relevant to the modeling stage of DCE research is the possible extension of the basic random utility choice modeling framework in an attempt to more closely replicate reality, for example to account for decision rule selection and choice set formation (discussed further below).

We did not set out to be exhaustive in our coverage of either choice models or software, instead focusing on standard models that can be estimated in standard commonly used software. There are of course interesting extensions to these core models that warrant attention for particular research questions, often requiring bespoke coding and estimation. One interesting stream of choice modeling is to account for different underlying decision rules and processing strategies. Two examples of this are choice set formation, championed by Swait and colleagues in the general choice modeling literature (e.g. [20]) and starting to be used in health (e.g. [63]) and attribute non-attendance (e.g. [64-66]), where the latter can also arise from the broader issue of excessive cognitive burden [67]. Another useful stream of choice modeling is data fusion. We discussed the need to calibrate ASCs for market data where such data are available, particularly for welfare and forecasting analysis. A natural extension is more complete data fusion where stated preference data collected in a DCE can be combined with revealed preference data either from observed choices [68, 69] or indeed from linking or embedding experiments in other data collection (cross sectional, panel, experimental, RCT) more generally to harness the advantages of the various data sources [70]. There are of course other interesting choice modeling extensions and we refer the interested reader to the Handbook of Choice modeling [71] for a recent survey of cutting edge choice models and estimation issues on the research frontier.

## **5. Conclusion**

As the use of DCEs and DCE results by researchers, policy makers and practitioners in the health sector continues to increase, so too will the importance placed on the theory and methods underpinning the approach in general and the analysis and interpretation of the generated choice data in particular. As this guide has highlighted, choice of modeling approach depends on a number of factors (research questions, study design and constraints such as quality/quantity of data) and decisions regarding analysis of choice data are often simultaneous and interdependent. When faced with such decisions we hope the theoretical and practical content of this paper proves useful not only to researchers within but also beyond health economics.

## **Data Availability Statement**

The data and estimation code used in this paper are available in supplementary material. Appendix 1 contains the data in 'long form', Appendix 2 contains the data in 'wide form', Appendix 3 contains the data in 'exploded form' and Appendix 4 contains the Stata, Nlogit and Biogeme estimation code.

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